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THE PARALLELIZATION OF MONTE-CARLO PLANNING *Parallelization of MC-Planning*

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Abstract: Since their impressive successes in various areas of large-scale parallelization, recent techniques like UCT and other Monte-Carlo planning variants (Kocsis and Szepesvari, 2006a) have been extensively studied (Coquelin and Munos, 2007; Wang and Gelly, 2007). We here propose and compare various forms of parallelization of bandit-based tree-search, in particular for our computer-go algorithm XYZ.

1 INTRODUCTION

Dynamic programming (Bellman, 1957; Bertsekas, 1995) provides a robust and stable tool for dynamic optimization. However, its application to large scale problems is far from simple and involves approximations, as in approximate value functions in approximate dynamic programming (Powell, 2007). Some alternate approaches, like using simulations for focusing on more important areas of the state space as in RTDP (Barto et al., 1993), have provided some important yet unstable tools for large scale approximate dynamic programming. Monte-Carlo planning, applied to Go since (Bruegmann, 1993), and in particular Bandit-based Monte-Carlo planning (Kocsis and Szepesvari, 2006a), provides an alternate solution, increasing the importance of simulations. Bandit-based Monte-Carlo planning features the construction of a tree approximating incrementally the distribution of possible futures. Tools from the bandit literature (see (Lai and Robbins, 1985; Auer et al., 2001); adversarial case in (Kocsis and Szepesvari, 2005); huge sets of arms in (Banks and Sundaram, 1992; Agrawal, 1995; Dani and Hayes, 2006; Berry et al., 1997)) are used in order to bias the random development of the tree in the direction of the most important directions; the important paper (Kocsis and Szepesvari, 2006a) applies recursively bandits for the biased random development of a tree. The efficiency of recursive bandits is also shown by some challenges won by such methods (Hussain et al., 2006). Its application to computer-go has provided particularly impressive results (Coulom, 2006; Wang and Gelly, 2007). The decision taking, at each step, is far more expensive, but the overall cost is much lower than the computational cost of one dynamic programming loop when the branching factor (or the state space) is large. The analysis of Monte-Carlo planning if far from being closed, as it is not clear that upper-confidence bounds are the best tool for that, in particular when heuristics like AMAF(Bruegmann, 1993) (also termed RAVE) are included. However, we here consider a fixed empirically tuned algorithm, and we focus on its parallelization, for various forms of parallelization (multi-core machines, standard clusters). The application to computer-go is one of the most illustrative applications of bandit-based Monte-Carlo planning methods. In particular, Go is still far from being solved, as moderate human players are still much better than the best computer-go programs. Monte-Carlo planning is a revolution in computergo, in some cases combined with tactical knowledge (Cazenave and Helmstetter, 2005; Coulom, 2007) but also in some cases almost from scratch without any specific knowledge (Wang and Gelly, 2007), except some likelihood of random playouts. The parallelization of Monte-Carlo planning is classical in the multicore case; we here provide an analysis of the speedup of this multi-core approach (shared memory). We then move to the message-passing architecture, for a cluster-parallelization. We briefly introduce bandits and bandit-based Monte-Carlo planning below, for the sake of clarity of notations. We then present the multi-core parallelization in section 2, and two different approaches for the cluster parallelization in section 3, 3. A bandit problem is typically defined as follows: (1) A finite set $A = \{1, ..., N\}$ of arms is given. (2) Each arm $a \in A$ is equipped with an unknown probability of reward *pa*. (3) At each time step $t \in \{1, 2, \ldots\}$, the algorithm chooses $a_t \in A$ depending on $(a_1, ..., a_{t-1})$ and $(r_1, ..., r_{t-1})$. (4) The bandit gives a reward r_t , with $r_t = 1$ with probability p_{a_t} (independently), and $r_t = 0$ otherwise. A bandit algorithm is an algorithm designed for minimizing the so-called regret:

$$
Regret = T \inf_{a \in A} p_a - \sum_{i=1}^T r_t.
$$

Important results, depending on assumptions on the set of actions and their distribution of rewards, include (Lai and Robbins, 1985; Auer et al., 2001; Banks and Sundaram, 1992; Agrawal, 1995; Dani and Hayes, 2006; Berry et al., 1997; Hussain et al., 2006; Kocsis and Szepesvari, 2005; Coquelin and Munos, 2007). A bandit is said to have side information if some information other than the reward is available to the algorithm. We present various bandit algorithms in section 1: these bandit algorithms usually work as follows for each time step:

- compute a score, for each possible arm, which consists in (i) an exploitation term, larger for arms for which the average rewards in the past is good; (ii) an exploration term, larger for arms which have not been tried often.
- choose the arm with maximum score.

Typical improvements are: (i) give heuristically a score to arms which have not been visited yet (see e.g. (Wang and Gelly, 2007; Coulom, 2007)); (ii) guess some side information (see the AMAF heuristic e.g. (Gelly and Silver, 2007)); (iii) restrict the sampling to the $k(t)$ first nodes for $k(t)$ some non-decreasing mapping (see progressive widening in (Coulom, 2007)). In the case of Go and more generally bandit-based Monte-Carlo planning, we use one bandit at each node of the tree, as explained in section 1. The difficult elements are the anytime nature of the problem, its non stationarity (Hussain et al., 2006; Kocsis and Szepesvari, 2006b), its large number of arms (Banks and Sundaram, 1992). The side information (usually termed AMAF) is detailed below.

This section provides an overview of bandit-based Monte-Carlo planning algorithms. It is presented in the case of a game; the experiments are performed in

the case of Go. We point out that UCT can be applied to trees far from minimax problems: max/max problems, or max/Expectation, etc. Algorithm 1 provides an overview (see also flowchart in Fig. 1), and Algorithm 3 provides a more detailed presentation. The

Figure 1: Flow chart of UCT. The bandit algorithm is applied in the simulation part in the tree.

Algorithm 1 Monte-Carlo planning algorithm. The final line chooses the decision with the conservative rule that the most simulated decision should be chosen. Other solutions, such as taking the decision with the higher ratio "number of winning simulations divided by the number of simulations", are too much dangerous because a decision might be very poor due to a small number of simulations. Some other robust and elegant techniques include the use of lower confidence bounds. Here, rewards are binary (win or loss), but arbitrary distributions of rewards can be used.

Initialize T to the root, representing the current state. T is a tree of positions, with each node equipped with statistics.

- **while** Time left > 0 **do**
	- Simulate one game until a leaf (a position) *L* of *T* (thanks to bandit algorithms). Then, choose one son (a successor) L' of \overline{L} .
	- Simulate one game from position L' until the game is over.
	- Add *L* ′ as a son of *L* in *T*.
	- Update statistics in all the tree. In UCT, each node knows how many winning simulations (from this node) have been performed and how many simulations (from this node) have been performed. In other forms of tree-search, other informations are necessary (heuristic information in AMAF, total number of nodes in the tree in BAST(Coquelin and Munos, 2007)).
- **end while**

Pick up the decision which has been simulated most often from the root.

main point in Algorithm 1 is that the tree is unbalanced, with a strong bias in favor of important parts of the tree. The function used for taking decisions out of the tree (i.e. the so-called Monte-Carlo part) is defined in (Wang and Gelly, 2007) The function used for simulating in the tree is presented in Algorithm 2. This function is a main part of the code: it decides in which direction the tree should be extended. There are various formulas, all of them being based on the idea of a compromise between exploitation (further simulating the seemingly good moves) and exploration (further simulating the moves which have not been explored a lot). The empirically best tool in

Algorithm 2 Taking a decision in the tree. The total number of simulations at situation *s* is *Simulations* (s) = \sum_{d} *Simulations*(*s*,*d*). We present here various formulas for computing the score (see (Lai and Robbins, 1985; Auer et al., 2001; Gelly and Silver, 2007) for UCB1, UCB-Tuned and AMAF respectively); other very important variants (for infinite domains, larger number of arms, of specific assumptions) can be found in (Banks and Sundaram, 1992; Agrawal, 1995; Dani and Hayes, 2006; Coquelin and Munos, 2007).

Algorithm 2 is the AMAF-guided exploration. In that case, in the classical formalism of bandits, each time one arm is played, we get: (i) a positive or null reward for the chosen arm $(0 \text{ or } 1)$; (ii) a list of arms, consisting in half of the arms roughly, positively correlated with the list of arms for which the rewards would have been positive if these arms have been played. The bandit algorithm for this bandit problem has been empirically derived in (Gelly and Silver, 2007). To the best of our knowledge, there's no mathematically grounded bandit algorithm in that case. An important improvement (termed progressive widening(Coulom, 2007)) of Algorithm 2 consists in considering only the $K(n)$ "best" moves (the best according to some

heuristic), at the n^{th} simulation in a given node, with $K(n)$ is an non-decreasing mapping from $\mathbb N$ to $\mathbb N$.

Algorithm 3 More detailed Monte-Carlo planning algorithm.

- Initialize T to the root, representing the current state. T is a tree of positions.
- **while** Time left > 0 **do**

Simulate one game until a leaf (a position) *L* of *T* (thanks to bandit algorithms applied until a leaf is met, see Algorithm 2).

Choose one son (a successor) L' of L , possibly with some offline learning (Gelly and Silver, 2007).

Simulate one game from position L' until the game is over.

Add *L* ′ as a son of *L* in *T*.

Update statistics in all the tree. In UCT, each node knows how many winning simulations (from this node) have been performed and how many simulations (from this node) have been performed. In other forms of tree-search, other informations are necessary (heuristic information in AMAF, total number of nodes in the tree in BAST(Coquelin and Munos, 2007)).

end while

Pick up the decision which has been simulated most often from the root.

2 MULTI-CORE PARALLELIZATION

The multi-core parallelization is intuitively the most natural one: the memory is shared. We just have to distribute the loop on various threads (each thread performs simulations independently of other threads, with just mutexes protecting the updates in memory), leading to algorithm 4. Consider *N* the number of

threads. The number of simulations per second is

Nb threads \times comp. time	10 sec.procs	20 secs.procs	40 secs.procs
1 thread	$51.1 + 1.8$	$62.0 + 2.2$	$74.4 + 2.4$
2 threads		$62.9 + 1.8$	
4 threads			$66.4 + 2.1$

Table 1: Success rate against mogoRelease3, for various computation times. Under the two-assumptions (1) almost *N* times more simulations per second with *N* cores (2) no impact of the "delay" point pointed out in the text, the speed-up would be linear and all the raws would be equal. We see a decay of performance for 4 threads.

typically almost multiplied by *N*. However, this algorithm is not equivalent to the sequential one: possibly, $N-1$ simulations are running when one more simulation is launched, and the updates of *T* corresponding to these $N-1$ simulations are not taken into account. There is a $N-1$ delay, and the analysis of the delay is not straightforward - we will quantify this effect experimentally. We get the following empirical results: Table 1 confirms the roughly 63% success rate known when doubling the computational power. As a conclusion, in 9x9 Go, the speed-up of the multi-core algorithm 4 is linear for two nodes, slightly below the linear speed-up for 4 nodes (by interpolation, we can estimate the speed-up as 3 for 4-cores).

3 CLUSTER PARALLELIZATION

First, let's consider the generalization of the multicore approach to a cluster, i.e. a version with massive communication in order to keep roughly the same state of the memory on all nodes. As the memory is not shared here, we have to broadcast on the network many update-informations; each simulation on one node leads to one broadcast. Possibly, we can group communications in order to reduce latencies. This leads to the algorithm 5. $T = 0$ is perhaps possible, for high performance clusters or processors inside the same machine. Let's consider the idealized case of a cluster with negligible communication cost and infinite number of nodes. Let's assume that a proportion α of time is spent in the updates. Also, let's assume that the delay of updates does not reduce the overall efficiency of the algorithm. What is the speed-up in that case ? Consider *M* the number of simulations per second on one node in the (mono-node) case. With *N* nodes, at each time steps, we get *NM* simulations. The number of updates is therefore *NM* per second of simulation. If the time of one update is *T*, for each group of *M* simulations, (i) each node performs *M* simulations (costs $1 - \alpha$ second); (ii) each node sends *M* update**Algorithm 5** Cluster algorithm for Monte-Carlo planning. As there are many paths leading to the same node, we must use a hash table, so that with some key (describing a goban) we can find if a node is in the tree and what are its statistics in constant time.

for Each node **do**

Initialize T to the root, representing the current state of the root. *T* is a tree of positions, with statistics attached to each node.

end for

for For each computer simultaneously: **do**

for For each thread simultaneously: **do while** Time left > 0 **do** Simulate one game until a node (=position) *L* of *T* (thanks to bandit algorithms); put this simulation *S* in memory. Choose a successor *L* ′ of *L*. Simulate one game from position L' until the game is over; put this simulation S' in memory. S, S' is a complete game starting at the root. Add L' as a son of L in T , and update all the statistics in *T* with *S*, *S'*. Add (L, L', S, S') to a stack of to-be-sent simulations. **if** *time*−*t*0 ≥ *T* and thread=first thread **then** Set $t0 = time$. Send all the (L, L', S, S') in the stack to all other nodes. Reset the stack. Receive many (L, L', S, S') from all other nodes. **for** Each (*L*,*L* ′ ,*S*,*S* ′) received **do** Add *L* ′ as a son of *L* in *T* (if not present). Update all the statistics in T with S, S' . **end for end if end while end for end for** Pick up the decision which has been simulated most of-

ten.

information (costs 0 second); (iii) each node receives $(N-1)M$ update-informations (costs 0 second); (iv) each node updates its tree with these $(N-1)M$ update informations (costs $\alpha(N-1)$ second). If we divide by the number *N* of nodes and let $N \rightarrow \infty$, we get (i) a cost $(1 - \alpha)/N \rightarrow 0$; (ii) a cost 0 for sending update-informations; (iii) a cost 0 for receiving update-informations; (iv) a cost $\alpha(N-1)/N \rightarrow \alpha$ for updates. This implies that the main cost is the updatecost, and that asymptotically, the speed-up is $1/\alpha$. In the case of MoGo, this leads to $\alpha \simeq 0.05$ and therefore roughly 20 as maximal speed-up for the case of a tree simultaneously updated on all nodes. As communications are far from negligible, as preliminary experiments were disappointing and as we expect better than the 20 speed-up, we will not keep this algorithm in the sequel.

AN ALTERNATE SOLUTION WITH LESS COMMUNICATIONS

Section 3 showed that whenever communications are perfect, the speed-up¹ is limited to some constant $1/\alpha$, roughly 20 in MoGo. We propose the following algorithm (Algorithm 6), with the following advantages: (1) much less communications (can run on usual ethernet); (2) tolerant to inhomogeneous nodes (as other algorithms above also); (3) our implementation is not yet fault-tolerant, but it could be done; (4) self-assessment possible (strong variance \rightarrow more time). The algorithm is detailed in Algorithm 6.

An important advantage of this technique is that averaging vectors of statistics is possible quickly on a large number of nodes: the computational cost of this averaging over *N* nodes is $O(log(N))$. The case $T_0 = \infty$ in Algorithm 6 (no communication before the final step of the decision making) is just a form of averaging. For computer-go, we get 59 $% \pm 3%$ of success rate with an averaging over 43 machines versus a single machine, whereas a speed-up 2 leads to 63%. This means that averaging provides a speed-up less than 2 with 43 machines; this is not a good parallelization. We then experiment T_0 finite and $K = 0$ (i.e. only the root of the tree is shared between nodes):

We have no estimate for the 9-machines speedup, because comparing computational budget B with 9 machines and 9B with 1 machine implies the use of games with average time per move 5.B, which requires a lot of computational power. However, the 83.8% is in the extrapolation of linear speed-up. The results were not significantly different with higher numbers of levels. We guess that for larger numbers of nodes the results will be different but we have not yet any empirical evidence of this.

4 CONCLUSION

Computer-Go is both a main target for computergames, as the main unsolved game, and a challenging planification problem as the most promising approaches have a moderate expert knowledge and are therefore quite general. In particular, successful applications of the UCT approach have been reported very far from computer-Go (Kocsis and Szepesvari, 2006a). A main advantage of the approach is that it is fully scalable. Whereas many expert-based tools have roughly the same efficiency when doubling the computational power, bandit-based Monte-Carlo planning with time 2B has success rate roughly 63% against a bandit-based Monte-Carlo planning algorithm with time B. This leads to the hope of designing a parallel platform, for an algorithm that would be efficient in various tasks of planifications. The main results in this paper are the followings:

- The straightforward parallelization on a cluster (imitating the multi-core case by updating continuously the trees in each node so that the memory is roughly the same in all nodes) does not work in practice and has strong theoretical limitations, even if all computational costs are neglected.

- A simple algorithm, based on averages which are easily computable with classical message passing libraries, a few times per second, can lead to a great successes; in 19x19, we have reached, with 9 nodes, 84 % success rate against one equivalent node. This

¹This is not a "real" speed-up, as the parallel algorithm, even in the multi-core case, is not equivalent to the sequential one - the difference is the "delay" detailed in section 2. We here consider that the speed-up is *k* if the parallel algorithm is as efficient as the sequential one with *k* times more time.

⁻ Doubling the computational power (doubling the time per move) leads to a 63% success rate against the non-doubled version.

success rate is far above simple voting schemas, suggesting that communications between independent randomized agents are important and that communicating only at the very end is not enough.

- Our two parallelizations (multi-core and cluster) are orthogonal, in the sense that: (i) the multi-core parallelization is based on a faster breadth-first exploration (the different cores are analyzing the same tree and go through almost the same path in the tree; in spite of many trials, we have no improvement by introducing deterministic or random diversification in the different threads. (ii) the cluster parallelization is based on sharing statistics guiding the first levels only of the tree, leading to a natural form of load balancing. The deep exploration of nodes is completely orthogonal. Moreover, the results are cumulative; we see the same speed-up for the cluster parallelization with multi-threaded versions of the code or mono-thread versions.

- In 9x9 Go, we have roughly linear speed-up until 4 cores or 9 nodes. The speed-up is not negligible beyond this limit, but not linear. In 19x19 Go, the speed-up remains linear until at least 4 cores and 9 machines.

Extending these results to higher numbers of machines is the natural further work. Increasing the number of cores is difficult, as getting an access to a 16-cores machine is not easy. Monte-Carlo planning is a strongly innovative tool with more and more applications, in particular in cases in which variants of backwards dynamic programming do not work. Extrapolating the results to the human scale of performance is difficult. People usually consider that doubling the computational power is roughly equivalent to adding almost one stone to the level. This is confirmed by our experiments. Then, from the 2nd or 3rd Kyu of the sequential MoGo in 19x19, we need 10 or 12 stones for the best human level. Then, we need a speed-up of a few thousands. This is far from impossible, if the speed-up remains close to linear with more nodes.

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