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## Data Centric Workflows for Crowdsourcing

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Abstract. Crowdsourcing consists in hiring workers on internet to perform large amounts of simple, independent and replicated work units, before assembling the returned results. A challenge to solve intricate problems is to define orchestrations of tasks, and allow higher-order answers where workers can suggest *a process to obtain data* rather than a *plain answer*. Another challenge is to guarantee that an orchestration with correct input data terminates, and produces correct output data. This work proposes *complex workflows*, a data-centric model for crowdsourcing based on orchestration of concurrent tasks and higher order schemes. We consider termination (whether some/all runs of a complex workflow terminate) and correctness (whether some/all runs of a workflow terminate with data satisfying FO requirements). We show that existential termination/correctness are undecidable in general excepted for specifications with bounded recursion. However, universal termination/correctness are decidable when constraints on inputs are specified in a decidable fragment of FO, and are at least in co-2EXPTIME.

### 1 Introduction

Crowdsourcing leverages intelligence of crowd to realize tasks where human skills 19 still outperform machines [25]. It was successful in contributive science initiatives, 20 such as CRUK's Trailblazer [3], Galaxy Zoo [5], etc. Most often, a crowdsourcing 21 project consists in deploying a huge number of tasks that can be handled by humans 22 in a reasonable amount of time. Generally, work units are simple micro-tasks, that 23 are independent, cheap, repetitive, and take a few minutes to an hour to complete. 24 They can be labeling of images, writing scientific blogs, etc. The requester publishes 25 the tasks on a platform with a small incentive (a few cents, reputation gain, good-26 ies...), and waits for the participation from the crowd. However, many projects, 27 and in particular scientific workflows, can be seen as a coordination of high-level 28 composite tasks. As noted by [38], composite tasks are not or poorly supported 29 by crowdsourcing platforms. Crowdsourcing markets such as Amazon Mechani-30 cal Turk [1], Foule Factory [4], CrowdFlower[2], etc. already propose interfaces and 31 APIs to access crowds, but the specification of crowd based complex processes is still 32 in its infancy. Some works propose solutions for data acquisition and management 33 or deployment of workflows, mainly at the level of micro-tasks [17, 29]. Crowd-34 forge uses Map-Reduce techniques to solve complex tasks [23]. Turkit [30] builds 35 on an imperative language embedding calls to services of a crowdsourcing plat-36 form, which requires programming skills to design complex orchestrations. Turko-37 matic [26] and [41] implement a Price, Divide and Solve (PDS) approach: crowd 38 workers divide tasks into orchestrations of subtasks, up to the level of micro-tasks. 39 However, current PDS approaches ask clients to monitor workflows executions. In 40 this setting, clients cannot use PDS crowdsourcing solutions as high-level services. 41

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The next stage of crowdsourcing is hence to design more involved processes still relying on the crowd. A first challenge is to fill the gap between a high-level process that a requester wants to realize, and its implementation in terms of microtasks composition. Moving from one description level to the other is not easy, and we advocate the use of expertise of the crowd for such refinement. This can be achieved with higher-order answers, allowing a knowledgeable worker to return an orchestration of simpler tasks instead of a crisp answer to a question. A second challenge in this setting is to give guarantees on the termination (whether some/all runs terminate) and correctness of the overall process (whether the output data returned by a crowdsourced process meet some requirements w.r.t input data).

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This paper proposes a data-centric model called *complex workflows*, that define 11 orchestrations of tasks with higher-order schemes, and correctness requirements 12 on input and output data of the overall processes. Complex workflows are mainly 13 orchestrations of data transformation tasks, that start from initial input datasets 14 that are explicitly given as crisp data or represented symbolically with a logical 15 formula. Workers can contribute to micro-tasks (input data, add tags...) or refine 16 tasks at runtime. Some easy tasks (simple SQL queries or record updates) are au-17 tomated. Input/Output (I/O) requirements are specified with a fragment of FO. 18 We address the question of termination (whether all/some runs terminate) and cor-19 rectness (whether all/some runs terminate and meet the I/O requirements). Due 20 to higher-order, complex workflows are Turing complete, and hence existence of 21 a terminating run is undecidable. However, one can decide whether **all** runs of a 22 complex workflow terminate as soon as initial data is fixed or specified in an FO 23 fragment where satisfiability is decidable. Existential termination becomes decid-24 able with the same constraints on initial data as soon as recursion in higher-order 25 rewritings is bounded. We then show that existential correctness is undecidable, and 26 universal correctness is decidable if constraints on data are expressed in a decidable 27 fragment of FO. The complexity of termination and correctness depends mainly on 28 the length of runs, and on the complexity of satisfiability for the FO fragment used 29 to specify initial data and I/O requirements. It is at least in (co-)2EXPTIME for 30 the simplest fragments of FO, but can increase to an n-fold complexity for FO 31 fragments that use both existential and universal quantification. 32

Several formal models have been proposed for orchestration of tasks and ver-33 ification in data-centric systems or business processes. Workflow nets [40, 39], a 34 variant of Petri nets, address the control part of business processes, but data is 35 not central. Orchestration models such as ORC [22] or BPEL [36] can define busi-36 ness processes, but cannot handle dynamic orchestrations and are not made to 37 reason on data. [10] proposes a verification scheme for a workflow model depicting 38 business processes with external calls, but addresses operational semantics issues 39 (whether some "call pattern" can occur) rather than correctness of the computed 40 data. Several variants of Petri nets with data have been proposed. Obviously, col-41 ored Petri nets [20] have a sufficient expressive power to model complex workflows. 42 But they are defined at a low detail level, and encoding higher-order necessarily 43 have to be done through complex color manipulations. Complex workflows sepa-44 rate data, orchestration, and data transformations. Several variants of PNs where 45 transitions manipulate global variables exist (see for instance [14]), but they cannot model evolution of unbounded datasets. Other variants of PNs with tokens that carry data have also been proposed in [27]. Termination and boundedness are decidable for this model, but with non-elementary complexity, even when equality is the only predicate used. The closest Petri net variant to complex workflows are Structured Data nets [9], in which tokens carry structured data. Higher order was introduced in *nested* Petri nets [31] a model where places contain sub-nets. Interestingly, termination of nested nets is decidable, showing that higher-order does not imply Turing completeness. Data-centric models and their correctness have also been considered. Guarded Active XML [7] (GAXML) is a model where 10 guarded services are embedded in structured data. Though GAXML does not ad-11 dress explicitly crowdsourcing nor higher-order, the rewritings performed during 12 service calls can be seen as a form of task refinement. Restrictions on recursion in 13 GAXML allows for verification of Tree LTL (a variant of LTL where propositions 14 are statements on data). More recently, [8] has proposed a model for collaborative 15 workflows where peers have a local view of a global instance, and collaborate via 16 local updates. With some restrictions, PLTL-FO (LTL-FO with past operators) is 17 decidable. Business artifacts were originally developed by IBM [35], and verification 18 mechanisms for LTL-FO (LTL formula embedding FO statements over universally 19 quantified variables) were proposed in [13,24]. LTL-FO is decidable for subclasses 20 of artifacts with data dependencies and arithmetic. [15] considers systems com-21 posed of peers that communicate asynchronously. LTL-FO is decidable for systems 22 with bounded queues. Business artifacts allow for data inputs during the lifetime 23 of an artifact, but are static orchestrations of guarded tasks, described as legal 24 relations on datasets before and after execution of a task. Further, LTL-FO verifi-25 cation focuses mainly on dynamics of systems (termination, reachability) but does 26 not address correctness. [18] considers data-centric dynamic systems (DCDS), i.e. 27 relational databases equipped with guarded actions that can modify their contents, 28 and call external services. Fragments of FO  $\mu$ -calculus are decidable for DCDS with 29 bounded recursion. 30

#### $\mathbf{2}$ Motivation

Our objectives are to provide tools to develop applications in which human actors 32 execute tasks or propose solutions to realize a complex task, and check the cor-33 rectness of the designed services. The envisioned scenario is the following: a client 34 provides a coarse grain workflow depicting important phases of a complex task to 35 process data, and a description of the expected output. The tasks can be completed 36 in several ways, but cannot be fully automated. It is up to a pool of crowdwork-37 ers to complete them, possibly after refining difficult tasks up to the level of an 38 orchestration of easy or automated micro-tasks.

The crowdsourcing model presented in section 4 is currently used to design a 40 real example, the SPIPOLL initiative [6]. The objective of SPIPOLL is to study 41 populations of pollinating insects. The standard processes used by SPIPOLL call 42 for experience of large pools of workers to collect, sort and tag large databases 43 containing insects pictures. The features provided by our model fit particularly 44

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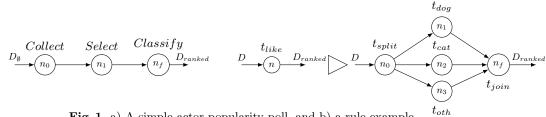


Fig. 1. a) A simple actor popularity poll, and b) a rule example.

with the needs of SPIPOLL, as tagging pictures of rare insects is not a simple annotation task, and usually calls for complex validation processes.

Let us illustrate the needs and main features of complex workflows, refinement, and human interactions on a simpler example. A client (for instance a newspaper) wants to rank the most popular actors of the moment, in the categories *comedy*, drama and action movies. The task is sent to a crowdsourcing platform as a highlevel process decomposed into three sequential phases: first a collection of the most popular actors, then a selection of the 50 most cited names, followed by a classification of these actors in comedy/drama/action category. The ranking ends with a vote for each category, that asks contributors to associate a score to each name. The client does not input data to the system, but has some requirements on the output: 11 it is a dataset  $D_{ranked}$  with relational schema  $r_{out}(name, cites, category, score)$ , 12 where *name* is a key, *cites* is an integer that gives the number of cites of an actor, 13 category ranges over {drama, comedy, action} and score is a rational number be-14 tween 0 and 10. Further, every actor appearing in the final database should have 15 a score and a number of cites greater than 0. Obviously, there are several ways to 16 collect actors names, several ways to associate a category tag, to vote, etc. How-17 ever, the clients needs are defined in terms of an orchestration of high-level tasks, 18 without information on how the crowd will complete them, and without any ter-19 mination guarantee. The orchestration is depicted in Figure 1-a. It starts from an 20 empty input dataset  $D_{\emptyset}$ , and returns an actor popularity dataset  $D_{ranked}$ . 21

In the rest of the paper, we formalize complex workflows and their semantics (Sec. 4). We then address termination (Sec. 5) and correctness (Sec. 6). More precisely, given a complex workflow CW, we consider the following problems: **Universal termination:** Does every run of *CW* terminate ?

**Existential termination:** Is there an input for which at least one run of CW terminates ?

**Universal correctness:** For a given I/O requirement  $\psi^{in,out}$  relating input and output data, does every run of CW terminate and satisfy  $\psi^{in,out}$ ?

**Existential correctness:** For a given I/O requirement  $\psi^{in,out}$ , is there a particular input and at least one run of CW that terminates and satisfies  $\psi^{in,out}$ ?

#### 3 **Preliminaries**

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We use a standard relational model [12], i.e., data is organized in *datasets*, that 33 follow relational schemas. We assume finite set of domains  $\mathbf{dom} = dom_1, \ldots, dom_s$ , 34 a finite set of attribute names **att** and a finite set of relation names **relnames**. Each 35 attribute  $a_i \in \mathbf{att}$  is associated with a domain  $dom(a_i) \in \mathbf{dom}$ . A relational schema 36 (or table) is a pair rs = (rn, A), where rn is a relation name and  $A \subseteq \mathbf{att}$  denotes a finite set of attributes. Intuitively, attributes in A are column names in a table, and rn the table name. The *arity* of rs is the size of its attributes set. A *record* of a relational schema rs = (rn, A) is tuple  $rn(v_1, \ldots v_{|A|})$  where  $v_i \in dom(a_i)$  (it is a row of the table), and a *dataset* with relational schema rs is a multiset of records of rs. A *database schema* DB is a non-empty finite set of tables, and an instance over a database DB maps each table in DB to a dataset.

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We address properties of datasets with *First Order logic* (FO) and predicates on records. For simplicity and efficiency, we will consider predicates defined as sets of linear inequalities over reals and integer variables. We use FO to define relations between the inputs and outputs of a task, and requirements on possible values of inputs and outputs of a complex workflow.

**Definition 1 (First Order).** A First Order formula (in prenex normal form) over a set of variables  $\overrightarrow{X} = x_1, \ldots, x_n$  is a formula of the form  $\varphi ::= \alpha(\overrightarrow{X}).\psi(\overrightarrow{X})$ where  $\alpha(\overrightarrow{X})$  is an alternation of quantifiers and variables of  $\overrightarrow{X}$ , i.e. sentences of the form  $\forall x_1 \exists x_2, \ldots$  called the prefix of  $\varphi$  and  $\psi(\overrightarrow{X})$  is a quantifier free formula called the matrix of  $\varphi$ .  $\psi(\overrightarrow{X})$  is a boolean combinations of atoms of the form  $rn_i(x_1, \ldots, x_k) \in D_i, P_j(x_1, \ldots, x_n)$ , where  $rn_i(x_1, \ldots, x_k)$ 's are relational statements, and  $P_j(x_1, \ldots, x_n)$ 's are boolean function on  $x_1, \ldots, x_n$  called predicates.

In the rest of the paper, we consider variables that either have finite domains 20 or real valued domains, and predicates specified by simple linear inequalities of 21 dimension 2, and in particular equality of variables, i.e. statements of the form 22  $x_i = x_i$ . One can decide in NP if a set of linear inequalities has a valid assignment, 23 and in polynomial time [21] if variables values are reals. Let  $\overrightarrow{X_1} = \{x_1, \ldots, x_k\} \subseteq$ 24  $\overrightarrow{X}$ . We write  $\forall \overrightarrow{X_1}$  instead of  $\forall x_1 . \forall x_2 ... \forall x_k$ , and  $\exists \overrightarrow{X_1}$  instead of  $\exists x_1 . \exists x_2 ... \exists x_k$ . 25 We use w.l.o.g. formulas of the form  $\forall \overrightarrow{X_1} \exists \overrightarrow{X_2} \dots \psi(X)$  or  $\exists \overrightarrow{X_1} \forall \overrightarrow{X_2} \dots \psi(X)$ , where  $\psi(X)$  is a quantifier free matrix, and for every  $i \neq j$ ,  $\overrightarrow{X_i} \cap \overrightarrow{X_j} = \emptyset$ . Every set of 27 variables  $X_i$  is called a *block*. By allowing blocks of arbitrary size, and in particular 28 empty blocks, this notation captures all FO formulas in prenex normal form. We 29 denote by  $\varphi_{[t_1/t_2]}$  the formula obtained by replacing every instance of term  $t_1$  in  $\varphi$ 30 by term  $t_2$ . Each variable  $x_i$  in  $\overline{X}$  has a domain  $Dom(x_i)$ . A variable assignment 31 is a function  $\mu$  that associates a value  $d_x$  from Dom(x) to each variable  $x \in X$ . 32

**Definition 2 (Satisfiability).** A variable free formula is satisfiable iff it evaluates to true. A formula of the form  $\exists x, \phi$  is satisfiable iff there exists a value  $d_x \in Dom(x)$  such that  $\phi_{[x/d_x]}$  is satisfiable. A formula of the form  $\forall x, \phi$  is satisfiable iff, for every value  $d_x \in Dom(x), \phi_{[x/d_x]}$  is satisfiable.

It is well known that satisfiability of an FO formula is undecidable in general, but it is decidable for several fragments. The *universal fragment* (resp. existential fragment) of FO is the set of formulas of the form  $\forall \vec{X} . \varphi$  (resp.  $\exists \vec{Y} . \varphi$ ) where  $\varphi$  is 39 quantifier free. We denote by  $\forall$ FO the universal fragment of FO and by  $\exists$ FO the existential fragment. Checking satisfiability of the existential/universal fragment of FO can be done non-deterministically in polynomial time. In our setting, where atoms in FO formula are relational statements and linear inequalities, satisfiability of formulas with only universal or existential quantifiers is decidable and (co)-NP-complete. We refer interested readers to Appendix B for a proof.

One needs not restrict to existential or universal fragments of FO to get decidability of satisfiability. A well known decidable fragment is  $(FO^2)$ , that uses only two variables [34]. However, this fragment forbids atoms of arity greater than 2, which is a severe limitation when addressing properties of datasets. The BS fragment of FO is the set of formulas of the form  $\exists \vec{Y}_1. \forall \vec{X}_2. \psi$ , where  $\psi$  is quantifier free, may contain predicates, but no equality. The Bernays-Schonfinkel-Ramsey fragment of FO [11] (BSR-FO for short) extends the BS fragment by allowing equalities in the matrix  $\psi$ . Satisfiability of a formula in the BS or BSR fragment of FO is NEXPTIME-complete (w.r.t. the size of the formula) [28].

Recent results [37] exhibited a new fragment, called the *separated fragment* of 16 FO, defined as follows: Let Vars(A) be the set of variables appearing in an atom 17 A. We say that two sets of variables  $Y, Z \subseteq X$  are separated in a quantifier free 18 formula  $\phi(X)$  iff for every atom At of  $\phi(X)$ ,  $Vars(At) \cap Y = \emptyset$  or  $Vars(At) \cap Z = \emptyset$ . 19 A formula in the Separated Fragment of FO (SF-FO for short) is a formula of the 20 form  $\forall \vec{X}_1 . \exists \vec{Y}_2 ... \forall \vec{X}_n . \exists \vec{Y}_n \phi$ , where  $\vec{X}_1 ... \cup \vec{X}_n$  and  $\vec{Y}_1 ... \cup \vec{Y}_n$  are separated. 21 The SF fragment is powerful and subsumes the Monadic Fragment [32] (where 22 predicates can only be unary) and the BSR fragment. Every separated formula can 23 be rewritten into an equivalent BSR formula (which yields decidability of satisfia-24 bility for SF formulas), but at the cost of an *n*-fold exponential blowup in the size of 25 the original formula. Satisfiability of a separated formula  $\varphi$  is hence decidable [37], 26 but with a complexity in  $O(2^{\downarrow n |\varphi|})$ . 27

A recent extension of  $FO^2$  called  $FO^2BD$  allows atoms of arbitrary arity, but only formulas over sets of variables where at most two variables have unbounded domain. Interestingly,  $FO^2BD$  formulas are closed under computation of weakest preconditions for a set of simple SQL operations [19]. We show in Section 4 that conditions needed for a non-terminating execution of a complex workflow are in  $\forall FO$ , and that  $\forall FO$ ,  $\exists FO$ , BSR-FO, SF-FO are closed under precondition calculus. 33

### 4 Complex Workflows

This section formalizes the notion of *complex workflow*, and gives their semantics 35 through operational rules. This model is inspired by artifacts systems [13], but 36 uses higher-order constructs (task decomposition), and relies on human actors (the 37 crowdworkers) to complete tasks. We assume a *client* willing to use the power of 38 crowdsourcing to realize a *complex task* that needs human contribution to collect, 39 annotate, or organize data. This complex task is specified as a workflow that or-40 chestrates elementary tasks or other complex tasks. The client can input data to 41 the system (i.e. enter a dataset  $D_{in}$ ), and may have a priori knowledge on the 42 relation between the contents of his input and the plausible outputs returned after 43 completion of the complex workflow. This scenario fits several types of applications 44

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such as opinion polls, citizen participation, etc. High-level answers of workers are seen as workflow refinements, and elementary tasks realizations are simple operations that transform data. During an execution of a complex workflow, we consider that each worker is engaged in the execution of at most one task.

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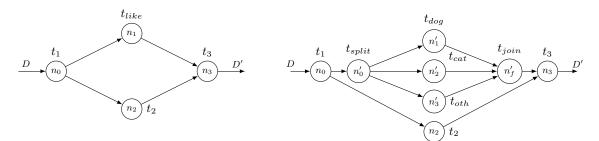
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**Tasks:** A task t is a work unit designed to transform input data into output data. It can be a high-level description submitted by a client, a very basic atomic task that can be easily realized by a single worker (e.g. tagging images), a task that can be fully automated, or a complex task that requires an orchestration of sub-tasks to reach its objective. We define a set of tasks  $\mathcal{T} = \mathcal{T}_{ac} \uplus \mathcal{T}_{cx} \uplus \mathcal{T}_{aut}$  where  $\mathcal{T}_{ac}$ is a set of *atomic tasks* that can be completed in one step by a worker,  $\mathcal{T}_{cx}$  is a set of *complex tasks* which need to be refined as an orchestration of smaller sub-11 tasks to produce an output, and  $\mathcal{T}_{aut}$  is a set of automated tasks performed by a machine (e.g. simple SQL queries: selection, union, projection...). Tasks in  $\mathcal{T}_{ac}$  and 13  $\mathcal{T}_{aut}$  cannot be refined, and tasks in  $\mathcal{T}_{aut}$  do not require contribution of a worker.

**Definition 3 (Workflow).** A workflow is a labeled acyclic graph  $W = (N, \rightarrow, \lambda)$ 15 where N is a finite set of nodes, modeling occurrences of tasks,  $\rightarrow \subseteq N \times N$  is a 16 precedence relation, and  $\lambda: N \to \mathcal{T}$  associates a task name to each node. A node 17  $n \in N$  is a source iff it has no predecessor, and a sink iff it has no successor. 18

In the rest of the paper, we fix a finite set of tasks  $\mathcal{T}$ , and denote by  $\mathcal{W}$  the set 19 of all possible workflows over  $\mathcal{T}$ . Intuitively, if  $(n_1, n_2) \in \longrightarrow$ , then an occurrence 20 of task named  $\lambda(n_1)$  represented by  $n_1$  must be completed before an occurrence 21 of task named  $\lambda(n_2)$  represented by  $n_2$ , and the data computed by  $n_1$  is used as 22 an input for  $n_2$ . We denote by min(W) the set of sources of W, by  $succ(n_i)$  the 23 set of successors of a node  $n_i$ , and by  $pred(n_i)$  its predecessors. The size of W 24 is the number of nodes in N and is denoted |W|. We assume that when a task 25 in a workflow has several predecessors, its role is to aggregate data provided by 26 preceding tasks, and when a task has several successors, its role is to distribute 27 excerpts from its input datasets to its successors. With this convention, one can 28 model situations where a large database is split into smaller datasets of reasonable 29 sizes that are then processed independently. We denote by  $W \setminus \{n_i\}$  the restriction 30 of W to  $N \setminus \{n_i\}$ , i.e. a workflow from which node  $n_i$  is removed along with all edges 31 which origins or goals are node  $n_i$ . We assume some well-formedness properties of 32 workflows: Every workflow has a single sink node  $n_f$ . Informally, we can think 33 of  $n_f$  as the task that returns the dataset computed during the execution of the 34 workflow. There exists a path from every node  $n_i$  of W to the sink  $n_f$ . The property 35 prevents from launching tasks which results are never used to build an answer to a 36 client. We define a *higher-order* answer as a *refinement* of a node n in a workflow 37 by another workflow. Intuitively, n is simply replaced by W' in W. 38

**Definition 4 (Refinement).** Let  $W = (N, \rightarrow, \lambda)$  be a workflow,  $W' = (N', \rightarrow')$ 39  $(\lambda')$  be a workflow with a unique source node  $n'_{src} = min(W')$ , a unique sink node  $n'_f$  such that  $N \cap N' = \emptyset$ . The refinement of  $n \in N$  by W' in W is the 40 41 workflow  $W_{[n/W']} = (N_{[n/W']}, \longrightarrow_{[n/W']}, \lambda_{[n/W']}), \text{ where } N_{[n/W']} = (N \setminus \{n\}) \cup N',$ 42  $\lambda_{[n/W']}(n) = \lambda(n)$  if  $n \in N, \lambda'(n)$  otherwise, and 43



**Fig. 2.** A refinement of node  $n_1$  using rule  $(t_{like}, W_{like})$  of Figure 1-b.

 $\rightarrow_{[n/W']} = \rightarrow' \cup \{(n_1, n_2) \in \rightarrow \mid n_1 \neq n \land n_2 \neq n\} \cup \{(n_1, n'_{src}) \mid (n_1, n) \in \rightarrow\} \cup \{(n'_f, n_2) \mid n_1 \neq n \land n_2 \neq n\} \cup \{(n'_f, n_2) \mid n_1 \neq n \land n_2 \neq n\} \cup \{(n'_f, n_2) \mid n_1 \neq n \land n_2 \neq n\} \cup \{(n'_f, n_2) \mid n_1 \neq n \land n_2 \neq n\} \cup \{(n'_f, n_2) \mid n_1 \neq n \land n_2 \neq n\} \cup \{(n'_f, n_2) \mid n_1 \neq n \land n_2 \neq n\} \cup \{(n'_f, n_2) \mid n_1 \neq n \land n_2 \neq n\} \cup \{(n'_f, n_2) \mid n_1 \neq n \land n_2 \neq n\} \cup \{(n'_f, n_2) \mid n_1 \neq n \land n_2 \neq n\} \cup \{(n'_f, n_2) \mid n_1 \neq n \land n_2 \neq n\} \cup \{(n'_f, n_2) \mid n_1 \neq n \land n_2 \neq n\} \cup \{(n'_f, n_2) \mid n_1 \neq n \land n_2 \neq n\} \cup \{(n'_f, n_2) \mid n_1 \neq n \land n_2 \neq n\} \cup \{(n'_f, n_2) \mid n_2 \neq n\} \cup \{(n'_f, n_2) \mid n_2 \neq n\} \cup \{(n'_f, n_2) \mid n_1 \neq n \land n_2 \neq n\} \cup \{(n'_f, n_2) \mid n_2$ 1  $(n, n_2) \in \rightarrow$ 2

**Definition 5.** A Complex Workflow is a tuple  $CW = (W_0, \mathcal{T}, \mathcal{U}, sk, \mathcal{R})$  where  $\mathcal{T}$ is a set of tasks,  $\mathcal{U}$  a finite set of workers,  $\mathcal{R} \subseteq \mathcal{T} \times 2^{\mathcal{W}}$  is a set of rewriting rules, and  $sk \subseteq (\mathcal{U} \times \mathcal{R}) \cup (\mathcal{U} \times \mathcal{T}_{ac})$  defines workers competences.  $W_0$  is an initial workflow, that contains a single source node  $n_{init}$  and a single sink node  $n_f$ .

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We assume that in every rule  $(t, W) \in \mathcal{R}$ , the labeling  $\lambda$  of W is injective. This results in no loss of generality, as one can create copies of a task for each node in W, but simplifies proofs and notations afterwards. Further, W has a unique source node src(W). The relation sk specifies which workers have the right to perform or refine a particular task. This encodes a very simple competence model. We refer 11 to [33] for further studies on competences and more elaborated competence models. 12

Let us consider the example of Figure 2-left: a workflow contains a complex task 13  $t_{like}$  which objective is to rank large collections of images of different animals with 14 a score between 0 and 10. The relational schema for the dataset D used as input for 15  $t_{like}$  is a collection of records of the form Picdata(nb, name, kind) where nb is a key, 16 name is an identifier for a picture, kind denotes the species obtained from former 17 annotation of data by crowdworkers. Let us assume that a worker u knows how 18 to handle task  $t_{like}$  (i.e.  $(u, t_{like}) \in sk$ ), and wants to divide dataset D into three 19 disjoint datasets containing pictures of cats, dogs, and other animals, rank them 20 separately, and aggregate the results. This is captured by the rule  $R = (t_{like}, W_{like})$ 21 of Figure 1-b, where node  $n_0$  is an occurrence of an automated tasks that splits 22 an input dataset into datasets containing pictures of dogs, cats, and other animals, 23  $n_1, n_2, n_3$  represent tagging tasks for the respective animal kinds, and node  $n_f$  is an 24 automated task that aggregates the results obtained after realization of preceding 25 tasks. A higher-order answer of worker u is to apply rule R to refine node  $n_1$  in 26 the original workflow with  $W_{like}$ . The result is shown in Figure 2-right. 27

It remains to show how automated and simple tasks are realized and process 28 their input data to produce output data. At every node n representing a task 29  $t = \lambda(n)$ , the relational schemas of all input (resp. output) datasets are known and 30 denoted  $rs_1^{in}, \ldots rs_k^{in}$  (resp.  $rs_1^{out}, \ldots rs_k^{out}$ ). We denote by  $\mathcal{D}^{in} = D_1^{in}, \ldots D_k^{in}$  the set of datasets provided by predecessors of t, and by  $\mathcal{D}^{out} = D_1^{out} \ldots D_q^{out}$  the set of 31 32 output datasets computed by task t. During a run of a complex workflow, we allow 33 tasks executions only for nodes which inputs are not empty. The contents of every  $D_i^{out}$  is the result of one of the operations below: 2 SQL-LIKE OPERATIONS : We allow standard SQL operations: - Selection: For a given input dataset  $D_i^{in}$  with schema  $rn(x_1, \ldots, x_n)$  and a predicate  $P(x_1, \ldots, x_n)$ , compute  $D_j^{out} = \{rn(x_1, \ldots, x_n) \mid rn(x_1, \ldots, x_n) \in$  $D_i^{in} \wedge P(x_1, \ldots x_n)\}.$ - **Projection:** For a given input dataset  $D_i^{in}$  with schema  $rn(x_1, \ldots x_n)$  and an index  $k \in 1..n$  compute  $D_j^{out} = \{rn(x_1, \dots, x_{k-1}, x_{k+1}, \dots, x_n) \mid rn(x_1, \dots, x_n) \in$  $D_i^{in}$ . - Insertion/deletion : For a given input dataset  $D_i^{in}$  and a fixed tuple  $rn(a_1, \ldots, a_n)_{\sharp 0}$ compute  $D_j^{out} = D_i^{in} \cup \{rn(a_1, \dots a_n)\}$  (resp.  $D_j^{out} = D_i^{in} \setminus \{rn(a_1, \dots a_n)\}$ ) 11 - Union: For two input dataset  $D_i^{in}, D_k^{in}$  with schema  $rn(x_1, \ldots x_n)$ , compute 12  $D_i^{out} = D_i^{in} \cup D_k^{in}$ 13 - Join: For two input dataset  $D_i^{in}, D_k^{in}$  with schema  $rn_i(x_1, \ldots, x_n)$  and  $rn_k(y_1, \ldots, y_q)_{i \neq j}$ for a chosen pair of indices  $ind_i$ ,  $ind_k$  compute  $D_i^{out} = \{rn'(x_1, \ldots, x_n, y_1, \ldots, y_{ind_k-1})\}$  $y_{ind_k+1}, \ldots y_q) \mid x_{ind_i} = y_{ind_k} \wedge rn_i(x_1, \ldots x_n) \in D_i^{in} \wedge rn_k(y_1, \ldots y_q) \in D_k^{in} \}$ **Difference:** For two input dataset  $D_i^{in}, D_k^{in}$  with the same schema  $rn(x_1, \ldots x_n)$ , 16 17 compute  $D_i^{out} = D_i^{in} \setminus D_k^{in}$ 18 WORKERS OPERATIONS: These are elementary tasks performed by workers to mod-19 ify the datasets computed so far. These operations may perform non-deterministic 20 choices among possible outputs. 21 - Field addition: Given an input dataset  $D_i^{in}$  with schema  $rn(x_1, \ldots x_n)$ , a 22 predicate P(.), compute a dataset  $D_j^{out}$  with schema  $rn'(x_1, \ldots, x_n, x_{n+1})$  such 23 that every tuple  $rn(a_1,\ldots,a_n) \in D_i^{in}$  is extended to a tuple  $rn(a_1,\ldots,a_n,a_{n+1}) \in 24$  $D_i^{out}$  such that  $P(a_1, \ldots a_{n+1})$  holds. Note that the value of field  $x_{n+1}$  can be 25 chosen non-deterministically for each record. 26 **Record input:** Given an input dataset  $D_i^{in}$  with schema  $rn(x_1, \ldots x_n)$ , and a 27 predicate P, compute a dataset  $D_i^{out}$  on the same schema  $rn(x_1, \ldots x_n)$  with 28 an additional record  $rn(a_1,\ldots,a_n)$  such that  $P(a_1,\ldots,a_n)$  holds. Note that 29 the value of fields  $x_1, \ldots x_{n+1}$  can be non-deterministically chosen. Intuitively, 30 P defines the set of possible entries in a dataset. 31 - Field update: For each record  $rn(a_1 \dots a_n)$  of  $D_i^{in}$ , compute a record  $rn(b_1, \dots b_n)_{32}$ in  $D_j^{out}$  such that some linear arithmetic predicate  $P(a_1, a_n, b_1, \dots, b_n)$  holds. 33 Again, any value for  $b_1, \ldots b_n$  that satisfies P can be chosen. 34 Record to record arithmetic operations : For each record  $rn_i(a_1 \dots a_n)$  of 35  $D_i^{in}$ , compute a record in  $D_j^{out}$  of the form  $rn_j(b_1, \dots b_q)$  such that each  $b_k, k \in 1..q$ 36 is a linear combination of  $a_1 \ldots a_n$ . 37 These operations can easily define tasks that split a database  $D_1^{in}$  in two

These operations can easily define tasks that split a database  $D_1^{in}$  in two datasets  $D_1^{out}$ ,  $D_2^{out}$ , one containing records that satisfy some predicate P and the other one records that do not satisfy P. Similarly, one can describe input of record from a worker, operations that assemble datasets originating from different threads... To summarize, when a node n with associated task t with I predecessors is executed, we can slightly abuse our notations and write  $D_k^{out} = f_{k,t}(D_1^{in}, \dots D_I^{in})$  when the task performs a deterministic calculus (SQL-based operations or record to record calculus), and  $D_k^{out} \in F_{k,t}(D_1^{in}, \dots, D_I^{in})$  when the tasks involves nondeterministic choice of a worker. We now give the operational semantics of complex workflows.

An execution starts from the initial workflow  $W_0$  (the initial high-level description provided by a requester). Executing a complex workflow consists in realizing all its tasks following the order given by the dependency relation  $\longrightarrow$  in the orchestration, possibly after some refinement steps. At each step of an execution, the remaining part of the workflow to execute, the assignments of tasks to workers and the data input to tasks are memorized in a *configuration*. Execution steps consist in updating configurations according to operational rules. They assign a task to a competent worker, execute an atomic or automated task (i.e. produce output data from input data), or refine a complex task. Executions end when the remaining workflow to execute contains only the final node  $n_f$ .

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A worker assignment for a workflow  $W = (N, \rightarrow, \lambda)$  is a partial map wa:  $N \rightarrow$  $\mathcal{U}$  that assigns a worker to a subset of nodes in the workflow. Let  $\mathbf{wa}(n) = w_i$ . If  $\lambda(n)$ 16 is a complex task, then there exists a rule  $r = (\lambda(n), W) \in \mathcal{R}$  such that  $(w_i, r) \in sk$ (worker  $w_i$  knows how to refine task  $\lambda(n)$ ). Similarly, if  $\lambda(n)$  is an atomic task, then  $(w_i, \lambda(n)) \in sk$  (worker  $w_i$  has the competences needed to realize  $\lambda(n)$ ). We furthermore require map wa to be injective, i.e. a worker is involved in at most one 20 task. We say that  $w_i \in \mathcal{U}$  is free if  $w_i \notin \mathbf{wa}(N)$ . If  $\mathbf{wa}(n)$  is not defined, and  $w_i$  is a free worker,  $\mathbf{wa} \cup \{(n, w_i)\}$  is the map that assigns node n to worker  $w_i$ , and is 22 unchanged for other nodes. Similarly, wa\ $\{n\}$  is the restriction of wa to  $N \setminus \{n\}$ . 23

A data assignment for a workflow W is a function **Dass** :  $N \to (DB \uplus \{\emptyset\})^*$ , 24 that maps nodes in W to sequence of input datasets. For a node with k predecessors 25  $n_1, \ldots n_k$ , we have  $\mathbf{Dass}(n) = D_1 \ldots D_k$ . A dataset  $D_i$  can be empty if  $n_i$  has not 26 been executed yet, and hence has produced no data.  $\mathbf{Dass}(n)_{[i/X]}$  is the sequence 27 obtained by replacement of  $D_i$  by X in **Dass**(n). 28

**Definition 6** (Configuration). A configuration of a complex workflow is a triple 29 C = (W, wa, Dass) where W is a workflow depicting remaining tasks that have to 30 be completed, wa is a worker assignment, and Dass is a data assignment. 31

A complex workflow execution starts from the *initial configuration* 32  $C_0 = (W_0, \mathbf{wa}_0, \mathbf{Dass}_0)$ , where  $\mathbf{wa}_0$  is the empty map,  $\mathbf{Dass}_0$  associates dataset 33  $D_{in}$  provided by client to  $n_{init}$  and sequences of empty datasets to all other nodes 34 of  $W_0$ . A final configuration is a configuration  $C_f = (W_f, \mathbf{wa}_f, \mathbf{Dass}_f)$  such that 35  $W_f$  contains only node  $n_f$ , wa<sub>f</sub> is the empty map, and Dass<sub>f</sub> $(n_f)$  represents 36 the dataset that was assembled during the execution of all nodes preceding  $n_f$ 37 and has to be returned to the client. The intuitive understanding of this type of 38 configuration is that  $n_f$  needs not be executed, and simply terminates the workflow 39 by returning final output data. Note that due to data assignment, there can be more 40 than one final configuration, and we denote by  $\mathcal{C}_f$  the set of all final configurations. 41

We define the operational semantics of a complex workflow with 4 rules that 42 transform a configuration C = (W, wa, Dass) in a successor configuration C' =43 (W', wa', Dass'). Rule 1 defines task assignments to free workers, Rule 2 defines 44 the execution of an atomic task by a worker, Rule 3 defines the execution of an automated task, and Rule 4 formalizes refinement. We only give an intuitive description of semantic rules and refer reader to appendix A for a formal definition. **Rule 1** (WORKER ASSIGNMENT): A worker  $u \in \mathcal{U}$  is assigned to a node n. The rule applies if u is free, has the skills required by  $t = \lambda(n)$ , if t is not an automated task  $(t \notin \mathcal{T}_{aut})$  and if node n is not already assigned to a worker. Note that a worker can be assigned to a node even if it does not have input data yet, and is not yet executable. This rule only changes the worker assignment part in a configuration. **Rule 2** (ATOMIC TASK COMPLETION): An atomic task  $t = \lambda(n)$  can be executed if node n is minimal in current workflow W, it is assigned to a worker  $u = \mathbf{wa}(n)$ 10 and its input data  $\mathbf{Dass}(n)$  does not contain an empty dataset. Upon completion 11 of task t, worker u publishes the produced data  $\mathcal{D}^{out}$  to the succeeding nodes of 12 n in the workflow and becomes available. This rule modifies the workflow part 13 (node n is removed), the worker assignment, and the data assignment (new data 14 is produced and made available to successors of n). 15

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**Rule 3** (AUTOMATED TASK COMPLETION): An automated task  $t = \lambda(n)$  can be 16 executed if node n is minimal in the workflow and its input data does not contain 17 an empty dataset. The difference with atomic tasks completion is that n is not 18 assigned a worker, and the produced outputs are a deterministic function of task 19 inputs. This rule modifies the workflow part (node n is removed), and the data 20 assignment. 21

**Rule 4** (COMPLEX TASK REFINEMENT): The refinement of a node n with t =22  $\lambda(n) \in \mathcal{T}_{cx}$  by worker  $u = \mathbf{wa}(n)$  uses a refinement rule  $R_t$  such that  $(u, t) \in sk$ , 23 and  $R_t = (t, W_t)$ . Rule 4 refines node n with workflow  $W_t = (N_s, \longrightarrow_s, \lambda_s)$  (see 24 Def. 4). Data originally used as input by n become inputs of the source node of 25  $W_t$ . All other newly inserted nodes have empty input datasets. This rule changes 26 the workflow part of configurations and data assignment accordingly. 27

We say that there exists a *move* from a configuration C to a configuration C', or 28 equivalently that C' is a successor of configuration C and write  $C \rightsquigarrow C'$  whenever 29 there exists a rule that transforms C into C'.

**Definition 7 (Run).** A run  $\rho = C_0.C_1...C_k$  of a complex workflow is a finite 31 sequence of configurations such that  $C_0$  is an initial configuration, and for every 32  $i \in 1 \dots k, C_{i-1} \rightsquigarrow C_i$ . A run is maximal if  $C_k$  has no successor. A maximal run is terminated iff  $C_k$  is a final configuration, and it is deadlocked otherwise. 34

In the rest of the paper, we denote by  $\mathcal{R}uns(CW, D_{in})$  the set of maximal 35 runs originating from *initial configuration*  $C_0 = (W_0, \mathbf{wa}_0, \mathbf{Dass}_0)$  (where  $\mathbf{Dass}_0$ ) 36 associates dataset  $D_{in}$  to node  $n_{init}$ ). We denote by  $\mathcal{R}each(CW, D_{in})$  the set of 37 configurations that can be reached from  $C_0$ . Along a run, the size of datasets in use 38 can grow, and the size of the workflow can also increase, due to refinement of tasks. 39 Hence,  $\mathcal{R}each(CW, D_{in})$  and  $\mathcal{R}uns(CW, D_{in})$  need not be finite. Indeed, complex 40 tasks and their refinement can encode unbounded recursive schemes in which work-41 flow parts or datasets grow up to arbitrary sizes. Even when  $\mathcal{R}each(CW, D_{in})$  is 42 finite, a complex workflow may exhibit infinite cyclic behaviors. Hence, without 43 restriction, complex workflows define transitions systems of arbitrary size, with 44 growing data or workflow components, and with cycles. 45

In section 5, we give an algorithm to check termination of a complex workflow with bounded recursion. Roughly speaking, this algorithms searches a reachable configuration  $C_{bad}$  in which emptiness of a dataset D could stop an execution. Once such a configuration is met, it remains to show that the statement  $D = \emptyset$ is compatible with the operations performed by the run (insertion, projections, unions of datasets...) before reaching  $C_{bad}$ . This is done by computing backward the weakest preconditions ensuring  $D = \emptyset$  along the followed run, and checking that they are satisfiable. Weakest precondition were introduced in [16] as a way to prove correctness of programs. They were used recently to verify web applications with embedded SQL [19]. 10

**Definition 8.** Let  $C \rightsquigarrow C'$  be a move of a complex workflow. Let m be the nature of this move (an automated task realization, a worker assignment, a refinement...). We denote by  $wp[m]\psi$  the weakest precondition required for C such that  $\psi$  holds in C' after move m.

Moves create dependencies among input and output datasets of a task, that are captured as FO Properties. Further, the weakest precondition  $wp[m]\psi$  of an FO property  $\psi$  is also an FO property.

**Proposition 1.** Let CW be a complex workflow, r be the maximal arity of relational schemas in CW and  $\psi$  be an FO formula. Then for any move m of CW,  $wp[m]\psi$  is an effectively computable FO formula, and is of size in  $O(r,|\psi|)$ .

We refer readers to Appendix B.1 for a proof of Proposition 1. If automated 21 tasks use SQL difference, universal quantifiers can be introduced in the weakest 22 precondition. Interestingly, if automated tasks do not use SQL difference, a weakest 23 precondition is mainly obtained by syntactic replacement of relational statements 24 and by changes of variables. It can increase the number of variables, but it does not 25 change the number of quantifier blocks nor their ordering, and does not introduce 26 new quantifiers when replacing an atom. We hence easily obtain: 27

**Corollary 1.** The existential, universal, BSR and SF fragments of FO are closed 28 under calculus of a weakest precondition if tasks do not use SQL difference. 29

#### $\mathbf{5}$ **Termination of Complex Workflows**

Complex workflows use the knowledge and skills of crowd workers to complete a 31 task starting from input data provided by a client. However, a workflow may never 32 reach a final configuration. This can be due to particular data input by workers 33 that cannot be processed properly by the workflow, or to infinite recursive schemes 34 appearing during the execution. 35

**Definition 9 (Deadlock, Termination).** Let CW be a complex workflow,  $D_{in}$ 36 be an initial dataset,  $\mathcal{D}_{in}$  be a set of datasets. CW terminates existentially on input 37  $D_{in}$  iff there exists a run in  $\mathcal{R}uns(CW, D_{in})$  that is terminated. CW terminates 38 universally on input  $D_{in}$  iff all runs in  $\mathcal{R}uns(CW, D_{in})$  are terminated. Similarly, 39 CW terminates universally on input set  $\mathcal{D}_{in}$  iff CW terminates universally on 40 every input  $D_{in} \in \mathcal{D}_{in}$ , and CW terminates existentially on  $\mathcal{D}_{in}$  iff some run of 41 CW terminates for an input  $D_{in} \in \mathcal{D}_{in}$ . 42

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When addressing termination for a set of inputs  $\mathcal{D}_{in}$ , we describe  $\mathcal{D}_{in}$  symbolically with a decidable fragment of FO ( $\forall$ FO,  $\exists$ FO, BSR, or SF-FO). Complex workflows are Turing powerful (we show in Appendix C.1 how to encode a counter machine). So we get :

#### **Theorem 1.** Existential termination of complex workflows is undecidable.

An interesting point is that undecidability does not rely on arguments based on the precise contents of datasets (that are ignored by semantic rules). Indeed, execution of tasks only requires non-empty input datasets. Undecidability holds as soon as higher order operations (semantic rule 4) are used.

Universal termination is somehow an easier problem than existential termination. We show in this section that it is indeed decidable for many cases and in 11 particular when the datasets used as inputs of a complex workflow are explicitly 12 given or are specified in a decidable fragment of FO. We proceed in several steps. 13 We first define symbolic configurations, i.e. descriptions of the workflow part of 14 configurations decorated with relational schemas depicting data available as input 15 of tasks. We define a successor relation for symbolic configurations. We then iden-16 tify the class of non-recursive complex workflows, in which the length of executions 17 is bounded by some value  $K_{\mathcal{T}_{cr}}$ . We show that for a given finite symbolic executions 18  $\rho^{S}$ , and a description of inputs, one can check whether there exists an execution  $\rho$ 19 that coincides with  $\rho_S$ . This proof builds on the effectiveness of calculus of weakest 20 preconditions along a particular run (see Prop. 1). Then, showing that a complex 21 workflow does not terminate amounts to proving that it is not recursion-free, or 22 that it has a finite symbolic run which preconditions allow a deadlock. 23

**Definition 10 (Symbolic configuration).** Let  $CW = (W_0, \mathcal{T}, \mathcal{U}, sk, \mathcal{R})$  be a 24 complex workflow with database schema DB. A symbolic configuration of CW is 25 a triple  $C^S = (W, Ass, Dass^S)$  where  $W = (N, \rightarrow, \lambda)$  is a workflow,  $Ass: N \rightarrow \mathcal{U}$ 26 assigns workers to nodes, and  $Dass^{S}: N \to (DB)^{*}$  associates a list of relational schemas to nodes of the workflow. 28

Symbolic configuration describe the status of workflow execution as in stan-29 dard configurations (see def. 6) but leaves the data part underspecified. For every 30 node n that is minimal in W, the meaning of  $\mathbf{Dass}^{S}(n) = rs_1, \dots rs_k$  is that task 31 attached to node n takes as inputs datasets  $D_1 \dots D_k$  where each  $D_i$  conforms 32 to relational schema  $rs_i$ . For a given symbolic configuration, we can find all rules 33 that apply (there is only a finite number of worker assignments or task executions 34 ), and compute successor symbolic configurations. This construction is detailed in 35 Appendix C.2. 36

Definition 11 (Deadlocks, Potential deadlocks). A symbolic configuration 37  $C^{S} = (W, Ass, Dass^{S})$  is final if W consists of a single node  $n_{f}$ . It is a dead-38 lock if it has no successor. It is a potential deadlock iff a task execution can occur 39 from this node, i.e. there exists  $n \in \min(W)$  such that  $\lambda(n)$  is an automated or 40 atomic task. 41

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A deadlocked symbolic configuration represents a situation where progress is blocked due to shortage of competent workers to execute tasks. A potential deadlock is a symbolic configuration  $C^S$  where empty datasets may stop an execution. This deadlock is *potential* because  $Dass^{S}$  does not indicate whether a particular dataset  $D_i$  is empty. We show in this section that one can decide whether a potential deadlock situation in  $C^{S}$  represents a real and reachable deadlock, by considering how the contents of dataset  $D_i$  is forged along the execution leading to  $C^S$ .

**Definition 12 (Symbolic run).** A symbolic run is a sequence  $\rho^S = C_0^S \xrightarrow{m_1} C_1^S \xrightarrow{m_2} \dots \xrightarrow{m_k} C_k^S$  where each  $C_i^S$  is a symbolic configuration,  $C_{i+1}$  is a successor of  $C_i$ , and  $C_0^S = (W_0, Ass_0, \mathbf{Dass}^S)$  where  $W_0, Ass_0$  have the same meaning as for configurations, and  $Dass_0^S$  associates to the minimal node  $n_0$  in  $W_0$  the relational schema of  $Dass_0(n_0)$ .

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One can associate to every execution of a complex workflow  $\rho = C_0 \xrightarrow{m_1} C_1 \dots C_k$  a symbolic execution  $\rho^S = C_0^S \xrightarrow{m_1} C_1^S \xrightarrow{m_2} \dots \xrightarrow{m_k} C_k^S$  called its *sig*-13 14 *nature* by replacing data assignment in each  $C_i = (W_i, Ass_i, \mathbf{Dass}_i)$  by a function from each node n to the relational schemas of the datasets in  $\mathbf{Dass}_i(n)$ . It is not true, however, that every symbolic execution is the signature of an execution of CW, as some moves might not be allowed when a dataset is empty (this can occur for instance when datasets are split, or after a selection). A natural question when considering a symbolic execution  $\rho^S$  is whether it is the signature of an actual run 20 of CW. The proposition below shows that the decidability of this question depends 21 on assumptions on input datasets. 22

**Proposition 2.** Let CW be a complex workflow,  $D_{in}$  be a dataset,  $\mathcal{D}_{in}$  be an FO formula with  $n_{in}$  variables, and  $\rho^S = C_0^S \dots C_i^S$  be a symbolic run. If tasks do not 23 24 use SQL difference, then deciding if there exists a run  $\rho$  with input dataset  $D_{in}$  and 25 signature  $\rho^S$  is in 2EXPTIME. Checking if there exists a run  $\rho$  of CW and an 26 input dataset  $D_{in}$  that satisfies  $\mathcal{D}_{in}$  with signature  $\rho^{S}$  is undecidable in general. If 27 tasks do not use SQL difference, then it is in 28

- 2EXPTIME if  $\mathcal{D}_{in}$  is in  $\exists$ FO and 3EXPTIME if  $\mathcal{D}_{in}$  is in  $\forall$ FO or BSR-FO. 29  $-n_{in}-foldEXPTIME$  where  $n_{in}$  is the size of the formula describing  $\mathcal{D}_{in}$  if 30  $\mathcal{D}_{in}$  is in SF-FO 31

This proposition is proved in Appendix C.3. It does not yet give an algorithm 32 to check termination, as a complex workflows may have an infinite set of runs and 33 runs of unbounded length. However, semantic rules 1,2,3 can be used a bounded 34 number of times from a configuration (they decrease the number of available users 35 or remaining tasks in W). Unboundedness then comes from the refinement rule 4, 36 that implements recursive rewriting schemes. 37

**Definition 13.** Let t be a complex task. We denote by Rep(t) the task names that 38 can appear when refining task t, i.e.  $Rep(t) = \{t' \mid \exists u, W, (u, t) \in sk \land (t, W) \in \mathcal{R} \land$ 39  $t' \in \lambda(N_W)$ . The rewriting graph of a complex workflow  $CW = (W_0, \mathcal{T}, \mathcal{U}, sk, \mathcal{R})$ 40 is the graph  $RG(CW) = (\mathcal{T}_{cx}, \longrightarrow_R)$  where  $(t_1, t_2) \in \longrightarrow_R$  iff  $t_2 \in Rep(t_1)$ . Then 41 CW is recursion-free if there is no cycle of RG(CW) that is accessible from a task 42 appearing in  $W_0$ . 43

When a complex workflow is not recursion free, then some executions may exhibit infinite behaviors in which some task  $t_i$  is refined infinitely often. Such an infinite rewriting loop can contain a deadlock. In this case, the complex workflow does not terminate. If this infinite rewriting loop does not contain deadlocks, the complex workflow execution will never reach a final configuration in which all tasks have been executed. Hence, complex workflows that are not recursion-free do not terminate universally (see the proof of Prop. 3 for further explanations). We show in Appendix C.4, Prop. 5 that recursion-freeness is decidable and in  $O(|\mathcal{T}_{cx}^2| + |\mathcal{R}|)$ . Further, letting d denote the maximal number of complex tasks appearing in a rule, there exists a bound  $K_{\mathcal{T}_{cx}} \leq d^{|\mathcal{T}_{cx}|}$  on the size of W in a configuration, and the length of a (symbolic) execution of CW is in  $O(3.K_{\mathcal{T}_{cx}})$  (see Prop. 6 in Appendix C.4). We now characterize complex workflows that terminate universally. 12

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**Proposition 3.** A complex workflow terminates universally if and only if: i) it is recursion free, ii) it has no (symbolic) deadlocked execution,

iii) there exists no run with signature  $C_0^S \dots C_i^S$  where  $C_i^S$  is a potential deadlock, with  $D_k = \emptyset$  for some  $D_k \in \mathbf{Dass}(n_j)$  and for some minimal node  $n_j$  of  $W_i$ .

Condition i) can be easily verified, as shown in Prop. 5, Appendix C.4. If i) 17 holds, then there is a bound  $3.K_{\mathcal{T}_{cx}}$  on the length of all symbolic executions, and 18 checking condition ii) is an exploration of reachable symbolic configurations to 19 find deadlocks. It requires  $\log(3.K_{\mathcal{T}_{cx}}).K_{\mathcal{T}_{cx}}$  space, i.e. can be done in EXPTIME 20 (w.r.t.  $K_{\mathcal{T}_{cx}}$ ). Checking condition *iii*) is more involved. First, it requires finding a 21 potential deadlock, i.e. a reachable symbolic execution  $C_i^S$  with a minimal node  $n_i$ 22 representing a task to execute. Then one has to check if there exists an actual run 23  $\rho = C_0 \dots C_i$  with signature  $C_0^S \dots C_i^S$  such that one of the input datasets  $D_k$  in 24 sequence  $\mathbf{Dass}_i(n_j)$  is empty. Let  $rs_j = (rn_k, A_k)$  be the relational schema of  $D_k$ , 25 with  $A_j = \{a_1, \ldots, a_{|A_j|}\}$ . Then, emptiness of  $D_k$  can be encoded as a universal FO 26 formula of the form  $\psi_i ::= \forall x_1, \dots, x_{|A_i|}, rn_k(x_1, \dots, x_{|A_i|}) \notin D_k$ . Then all weakest 27 preconditions needed to reach  $C_i$  with  $D_k = \emptyset$  can be computed iteratively, and 28 remain in the universal fragment of FO (see Prop. 1). If a precondition  $\psi_i$  computed 29 this way (at step j < i) is unsatisfiable, then there is no actual run with signature 30  $\rho^{S}$  such that  $D_{k}$  is an empty dataset. If one ends weakest precondition calculus 31 on configuration  $C_0^S$  with a condition  $\psi_0$  that is satisfiable, and  $D_{in} \models \psi_0$ , then 32 such a run exists and *iii*) does not hold. Similarly with inputs described by  $\mathcal{D}_{in}$ , if 33  $\mathcal{D}_{in} \wedge \psi_0$  is satisfiable, then condition *iii*) does not hold. Note that this supposes 34 that  $\mathcal{D}_{in}$  is written in a decidable FO fragment. 35

Theorem 2. Let CW be a complex workflow, in which tasks do not use SQL dif-36 ference. Let  $D_{in}$  be an input dataset, and  $\mathcal{D}_{in}$  be an FO formula. Universal ter-37 mination of CW on input  $D_{in}$  is in co - 2EXPTIME. Universal termination on 38 inputs that satisfy  $\mathcal{D}_{in}$  is undecidable in general. It is in 39

- co-2EXPTIME (in K, the length of runs) if  $\mathcal{D}_{in}$  is in  $\forall FO$ , co-3EXPTIME40 if  $\mathcal{D}_{in}$  is  $\exists FO \text{ or } BSR\text{-}FO$ 41
- $co n_{in}$ -fold-EXPTIME, where  $n_{in} = |\mathcal{D}_{in}| + 2^K$  if  $\mathcal{D}_{in}$  is in SF-FO.

One can notice that the algorithm to check universal termination of CWs guesses a path, and is hence non-deterministic. In the worst case, one may have to explore all symbolic executions of size at most  $3 \cdot K_{\mathcal{T}_{cr}}$ .

Undecidability of existential termination has several consequences: As complex workflows are Turing complete, automatic verification of properties such as reachability, coverability, boundedness of datasets, or more involved properties written in logics such as LTL FO [13] are also undecidable. However, the counter machine encoding in the proof of Theorem 1 uses recursive rewriting schemes. A natural question is then whether existential termination is decidable when all runs have a length bounded by some integer  $K_{\text{max}}$ . Indeed, when such a bound exists it is sufficient to find a terminating witness, i.e. find a signature  $\rho^S$  of size  $K_{\rm max}$  end-11 ing on a final configuration non-deterministically, compute weakest preconditions 12  $\psi_{lo^{S_1}},\ldots,\psi_0$  and check their satisfiability. The length of  $\psi_0$  is in  $O(r^{K_{\max}})$ , and as 13 one has to verify non-emptiness of datasets used as inputs of tasks to allow execu-14 tion of a run with signature  $\rho^S$ , the preconditions are in the existential fragment 15 of FO, yielding a satisfiability of preconditions in  $O(2^{r^{K_{\text{max}}}})$ . 16

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**Theorem 3.** Let CW be complex workflow in which tasks do not use SQL dif-17 ference, and which runs are of length  $\leq K_{\max}$ . Let  $D_{in}$  be a dataset, and  $\mathcal{D}_{in}$  a 18 FO formula. One can decide in 2 - EXPTIME (in  $K_{max}$ ) whether CW termi-19 nates existentially on input  $D_{in}$ . If  $\mathcal{D}_{in}$  is in  $\exists FO$ , termination of CW is also in 20 2 - EXPTIME. It is in 3 - EXPTIME when  $\mathcal{D}_{in}$  is in  $\forall FO$  or BSR-FO 21

Recursion-free CWs have runs of length bounded by  $3.K_{\mathcal{T}_{cr}}$ , so existential ter-22 mination is decidable as soon as automated tasks do not use SQL difference (which 23 makes alternations of quantifiers appear in weakest preconditions). The bound  $K_{Ter}$ 24 can be exponential (see proof of Prop. 2), but in practice, refinements are supposed 25 to transform a complex task into an orchestration of simpler subtasks, and one can 26 expect  $K_{\mathcal{T}_{cx}}$  to be a simple polynomial in the number of complex tasks. Another 27 way to bound recursion in a CW is to limit the number of refinements that can 28 occur during an execution. For instance, if each complex task can be decomposed 29 at most k times, the bound on length of runs becomes  $K_{\text{max}} = 3 \cdot k \cdot n^2 + 3 \cdot |W_0|$ . 30

#### **Correctness of Complex Workflows** 6

Complex workflows provide a service to a client, that inputs some data (a dataset 32  $D_{in}$ ) to a complex task, and expects some answer, returned as a dataset  $D_{out}$ . A 33 positive answer to a termination question means that the process specified by a 34 complex workflow does not deadlock in some/all executions. Yet, the returned data 35 can still be incorrect. We assume the client sees the crowdsourcing platform as a 36 black box, and simply asks for the realization of a complex task that needs specific 37 competences. However, the client may have requirements on the type of output 38 returned for a particular input. We express this constraint with a FO formula  $\psi^{in,out}$ 39 relating inputs and outputs, and extend the notions of existential and universal 40 termination to capture the fact that a complex workflow implements client's needs 41 if some/all runs terminate, and in addition fulfill requirements  $\psi^{in,out}$ . This is called 42 correctness. 43 **Definition 14.** A constraint on inputs and outputs is an FO formula  $\psi^{in,out} ::= \psi_E^{in,out} \wedge \psi_A^{in,out} \wedge \psi_{AE}^{in,out} \wedge \psi_{EA}^{in,out}$ , where

- $-\psi_E^{in,out}$  is a conjunction of  $\exists FO$  formulas addressing the contents of the input/output dataset, of the from  $\exists x, y, z, rn(x, y, z) \in D_{in} \land P(x, y, z)$ , where P(.) is a predicate,
- $-\psi_A^{in,out}$  is a conjunction of  $\forall FO$  formulas constraining all tuples of the input/output dataset, of the form  $\forall x, y, z, rn(x, y, z) \in D_{in} \Rightarrow P(x, y, z)$
- $-\psi_{AE}^{in,out}$  is a conjunction of formulas relating the contents of inputs and outputs, of the form  $\forall x, y, z, rn(x, y, z) \in D_{in} \Rightarrow \exists (u, v, t), \varphi(x, y, z, u, v, t)$ , where  $\varphi$  is a predicate.
- $-\psi_{EA}^{in,out}$  is a conjunction of formulas relating the contents of inputs and outputs, of the form  $\exists x, y, z, rn(x, y, z) \in D_{in}, \forall (u, v, t), \varphi(x, y, z, u, v, t)$

The  $\psi_{AE}$  part of the I/O constraint can be used to require that every record in an input dataset is tagged in the output. The  $\psi_{EA}$  part can be used to specify that the output is a particular record selected from the input dataset (to require correctness of a workflow that implements a vote).

**Definition 15 (Correctness).** Let CW be a complex workflow,  $\mathcal{D}_{in}$  be a set of input datasets, and  $\psi^{in,out}$  be a constraint given by a client. A run in  $\mathcal{R}uns(CW, D_{in})$  <sup>17</sup> is correct if it ends in a final configuration and returns a dataset  $D_{out}$  such that <sup>19</sup>  $D_{in}, D_{out} \models \psi^{in,out}$ . CW is existentially correct with inputs  $\mathcal{D}_{in}$  iff there exists a <sup>20</sup> correct run  $\mathcal{R}uns(CW, D_{in})$  for some  $D_{in} \in \mathcal{D}_{in}$ . CW is universally correct with <sup>21</sup> inputs  $\mathcal{D}_{in}$  iff all runs in  $\mathcal{R}uns(CW, D_{in})$  are correct for every  $D_{in} \in \mathcal{D}_{in}$ . <sup>22</sup>

In general, termination does not guarantee correctness. A terminated run start-23 ing from an input dataset  $D_{in}$  may return a dataset  $D_{out}$  such that pair  $D_{in}$ ,  $D_{out}$ 24 does not comply with constraint  $\psi^{in,out}$  imposed by the client. For instance, a run 25 may terminate with an empty dataset while the client required at least one an-26 swer. Similarly, a client may ask all records in the input dataset to appear with 27 an additional tag in the output. If any input record is missing, the output will be 28 considered as incorrect. As for termination, correctness can be handled through 29 symbolic manipulation of datasets, but has to consider constraints that go beyond 30 emptiness of datasets. Weakest preconditions can be effectively computed (Prop. 1): 31 one derives successive formulas  $\psi_i^{in,out}, \ldots, \psi_0^{in,out}$  between  $D_{in}, D_{out}$  and datasets in use at step  $i, \ldots 0$  of a run. However, the  $\psi_{AE}^{in,out}$  part of formulas is already in an 32 33 undecidable fragment of FO, so even universal termination is undecidable in gen-34 eral, and even when a bound on the length of runs is known. It becomes decidable 35 only with some restrictions on the fragment of FO used to write  $\psi^{in,out}$ . 36

**Theorem 4.** Existential and universal correctness of CW are undecidable, even when runs are of bounded length K. If tasks do not use SQL difference, and  $\psi^{in,out}$ is in a decidable fragment of FO, then

- existential correctness is decidable for CWs with runs of bounded length, and is respectively in 2EXPTIME, 3EXPTIME and  $2^{K}$ -fold-EXPTIME for the  $\exists FO, \forall FO, BSR, and SF$  fragments.
- universal correctness is decidable and is respectively in co 2EXPTIME, co - 3EXPTIME and  $co \cdot 2^{K}$ -fold-EXPTIME for the  $\forall FO$ ,  $\exists FO$ , BSR, and SF fragments.

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*Proof (Sketch).* First, a CW that does not terminate (existentially or universally) cannot be correct, and setting  $\psi^{in,out} ::= true$  we get a termination question. So existential correctness is undecidable for any class of input/output constraint. Then, if  $\psi^{in,out}$  is in a decidable fragment of FO, and operations do not use SQL difference, then weakest preconditions preserve this fragment, and we can apply the algorithm used for Thm. 2 and 3, starting from precondition  $\psi_{|\rho^{S}|} = \psi^{in,out}.\square$ 

Restricting constraints to ∃FO, ∀FO, BSR, or SF-FO can be seen as a limitation. However,  $\exists FO$  can already express non-emptiness properties:  $\exists x_1, \ldots, \exists x_k$ ,  $rn(x_1,\ldots,x_k) \in D_{out}$  says that the output should contain at least one record. Now, to impose that every input is processed correctly, one needs a formula of the form 10  $\psi_{in,out}^{valid} ::= \forall x_1, \dots, x_k, rn(x_1, \dots, x_k) \in D_{in} \Longrightarrow \exists y_1, \dots, y_q, rn(x_1, \dots, x_k, y_1, \dots, y_q) \in D_{in} \Longrightarrow \exists y_1, \dots, y_q, rn(x_1, \dots, x_k, y_1, \dots, y_q) \in D_{in} \Longrightarrow \exists y_1, \dots, y_q, rn(x_1, \dots, x_k, y_1, \dots, y_q) \in D_{in} \Longrightarrow \exists y_1, \dots, y_q, rn(x_1, \dots, x_k, y_1, \dots, y_q) \in D_{in} \boxtimes D_{i$ 11  $D_{out} \wedge P(x_1, \dots, x_k, y_1, \dots, y_q)$ , that asks that every input in  $D_{in}$  appears in the out-12 put, and P() describes correct outputs. Clearly,  $\psi_{in,out}^{valid}$  is not in the separated frag-13 ment of FO. We can decide correctness for formulas  $\psi_{AE}^{in,out}$  of the form  $\forall \overrightarrow{X_1} \exists \overrightarrow{Y_2}, \varphi$  as soon as every atom in  $\varphi$  that is not separated contains only existential variables 14 15 that take values from a finite domain. Then  $\psi_{AE}^{in,out}$  can be transformed into an 16 ∀FO formula which matrix is a boolean combination of separated atoms. 17

### 7 Conclusion

We have proposed *complex workflows*, a model for crowdsourcing applications which 19 enables intricate data centric processes built on higher order schemes. We studied 20 termination and correctness of complex workflows w.r.t. requirement on inputs and 21 output of the overall process. Unsurprisingly, termination of a complex workflow 22 is undecidable, already due to the control part of the model. Now the question 23 of whether all runs terminate can be answered when the initial data is specified 24 in a fragment of FO for which satisfiability is decidable. Similar remarks apply to 25 correctness. Table 1 below summarizes the complexities of termination and correct-26 ness for static complex workflows (without higher order answer) or with bounded 27 recursion, and for generic workflows with higher order. We consider complexity 28 of termination and correctness for different decidable FO fragments. The (co)-29 2EXPTIME bound for the fragments with the lowest complexity mainly comes 30 from the exponential size of the formula depicting preconditions that must hold at 31 initial configuration (the EXPTIME complexity is in the maximal length of runs). 32 This can be see as an untractable complexity, but one can however expect depth 33 of recursion to be quite low, or even enforce such a depth. 34

Several questions remain open: So far, we do not know whether the complexity bounds are sharp. Beyond complexity issues, crowdsourcing relies heavily on incentives to make sure that a task progresses. Placing appropriate incentives to optimize the overall cost of a complex workflow and ensure progress in an important topic. Similarly, a crux in crowdsourcing is monitoring, in particular to propose tasks to the most competent workers. Cost optimization and monitoring can be addressed as a kind of quantitative game. Other research directions deal with the representation and management of imprecision. So far, there is no measure of trust nor plausibility on values input by workers during a complex workflow

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execution. Equipping domains with such measures is a way to provide control techniques targeting improvement of trust in answers returned by a complex workflow, and trade-offs between performance and accuracy of answers.

| Workflow  | FO  | Problems & Complexity (no SQL diff.) |                             |                                   |   |  |
|-----------|---|--------------------------------------|-----------------------------|-----------------------------------|---|--|
| Type      | Fragment  | Existential                          | Universal                   | Existential                       | Universal                                   |  |
|           | (for $\mathcal{D}_{in}$ or $\psi^{in,out}$ )    | Termination                          | Termination                 | Correctness                       | Correctness                                 |  |
| Static,   | FO  | Undecidable                          | Undecidable                 | Undecidable                       | Undecidable                                 |  |
| Recursive | $\exists^*(\forall^* \text{ if univ. PB})$      | 2EXPT                                | co - 2EXPT                  | 2EXPT                             | co - 2EXP                                   |  |
| Bounded   | $BSR, \forall^*(\exists^* \text{ if univ. PB})$ | 3EXPT                                | co - 3EXPT                  | 3EXPT                             | co - 3EXPT                                  |  |
|           | SF  | $n_{in} - foldEXPT$                  | $co - n_{in}$ -fold- $EXPT$ | $2^{K_{\tau_{cx}}}$ -fold- $EXPT$ | $co-2^{K_{\mathcal{T}_{cx}}}$ -fold- $EXPT$ |  |
|           | FO  | Undecidable                          | Undecidable                 | Undecidable                       | Undecidable                                 |  |
| Recursive | $\exists^*(\forall^* \text{ if univ. PB})$      | Undecidable                          | co - 2EXPT                  | Undecidable                       | co - 2EXPT                                  |  |
| Unbounded | $BSR, \forall^*(\exists^* \text{ if univ. PB})$ | Undecidable                          | co - 3EXPT(K)               | Undecidable                       | co - 3EXPT                                  |  |
|           | SF  | Undecidable                          | $co - n_{in} - foldEXPT$    | Undecidable                       | $co-2^{K\tau_{cx}}$ -fold- $EXPT$           |  |

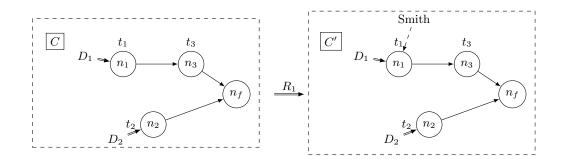
 Table 1. Complexity of Termination and Correctness (EXPT stands for EXPTIME).

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**Fig. 3.** Application of semantic rule  $R_1$ 

### A Appendix : Operational semantics of Complex Workflows

This appendix provides details on the operational semantics of complex workflows, the definition of the successor relation among symbolic configurations and the proofs of all theorems and propositions in the paper. All illustrations of semantics rules borrow examples from the SPIPOLL initiative [6].

#### A.1 Operational semantics

**Rule 1** (WORKER ASSIGNMENT): A worker  $u \in \mathcal{U}$  is assigned a task  $t = \lambda(n)$  such that  $t \notin \mathcal{T}_{aut}$ . The rule applies if u is free and has the skills required by t, and if node n is not already assigned to a worker. Note that a task can be assigned to a worker even if it does not have input data yet, and is not yet executable.

$$\frac{n \notin Dom(\mathbf{wa}) \land u \notin coDom(\mathbf{wa}) \land \lambda(n) \notin \mathcal{T}_{aut}}{\land ((u,\lambda(n)) \in sk \lor (u,r = (\lambda(n),W_r)) \in sk)}$$

$$(1)$$

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Consider for instance the application of rule  $R_1$  described in Figure 3. Config-11 urations are represented by the contents of dashed rectangles. Workflow nodes are 12 represented by circles, tagged with a task name representing map  $\lambda$ . The depen-13 dencies are represented by plain arrows between nodes. Worker assignments are 14 represented by dashed arrows from a worker name  $u_i$  to its assigned task. Data 15 assignment are represented by double arrows from a dataset to a node. The left 16 part of Figure 3 represents a configuration C with four nodes  $n_1, n_2, n_3$  and  $n_f$ . 17 The predecessors of  $n_1$  and  $n_2$  have been executed. Node  $n_1$  represents occurrence 18 of a task of type  $t_1$  and is attached dataset  $D_1$ . Let us assume that  $D_1$  is a database 19 containing bee pictures, and that task  $t_1$  cannot be automated  $(t_1 \notin \mathcal{T}_{aut})$  and con-20 sists in tagging these pictures with bee names, which requires competences on bee 21 species. Let us assume that worker *Smith* is currently not assigned any task and 22 has competences on bees. Then  $(Smith, t_1) \in sk$  and rule  $R_1$  applies. The resulting 23 configuration is configuration C' at the right of Figure 3, where the occurrence of 24  $t_1$  represented by node  $n_1$  is assigned to worker Smith. 25

**Rule 2** (ATOMIC TASK COMPLETION): An atomic task  $t = \lambda(n) \in \mathcal{T}_{ac}$  can be executed if node *n* is *minimal* in the workflow, it is assigned to a worker  $u = \mathbf{wa}(n)$ and its input data  $\mathbf{Dass}(n)$  does not contain an empty dataset. Upon completion of task *t*, worker *u* publishes the produced data  $\mathcal{D}^{out}$  to the succeeding nodes of *n* in the workflow and becomes available.

$$n \in min(W) \land \lambda(n) \in \mathcal{T}_{ac} \land \mathbf{wa}(n) = u$$

$$\land \mathbf{Dass}(n) \notin DB^*. \emptyset. DB^*$$

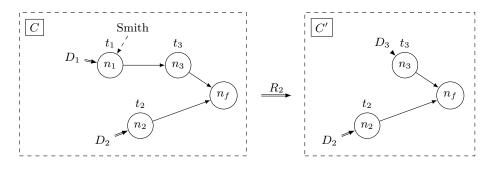
$$\land \exists \mathcal{D}^{out} = D_1^{out} \dots D_k^{out} \in F_{\lambda(n),u}(\mathbf{Dass}(n)),$$

$$\mathbf{Dass}' = \mathbf{Dass} \setminus \{(n, \mathbf{Dass}(n))\} \cup$$

$$\{(n_k, \mathbf{Dass}(n_k)_{[j/D_k^{out}]}) \mid n_k \in succ(n)$$

$$\land n \text{ is the } j^{th} \text{ predecessor of } n_k\}$$

$$(2)$$



**Fig. 4.** Application of semantic rule  $R_2$ 

Consider the example of Figure 4. We start from a configuration in which worker Smith has to tag bee images stored in a dataset  $D_1$ . We assume that the relational schema for  $D_1$  is a tuple R(id, pic) where id is a key and pic a picture. We also 8 assume that tags are species names from a finite set of taxons, e.g. 9  $Tax = \{Honeybee, Bumblebee, Masonbee, ..., Unknown\}$ . Worker Smith performs 10 the tagging task, which results in a dataset  $D_3$  with relational schema R'(id, pic, tag). 11 One can notice that no information is given of the way worker Smith tags the pic-12 tures in  $D_1$ , the only insurance is that for every tuple R(id, pic), there exists a 13 tuple R'(id, pic, tx) in  $D_3$  where  $tx \in Tax$ . Notice that application of this rule 14 may results in several successor configurations, as a human worker can choose non-15 deterministically any tag for each picture (including wrong answers). 16

**Rule 3** (AUTOMATED TASK COMPLETION): An automated task  $t = \lambda(n) \in \mathcal{T}_{aut}$  can be executed if node n is minimal in the workflow and its input data does not contain an empty dataset. The difference with atomic tasks completion is that  $t \in \mathcal{T}_{aut}$ , n is not assigned a worker, and that the produced outputs are deterministic functions of task inputs.

$$n \in min(W) \land \lambda(n) \in \mathcal{T}_{aut} \land \mathbf{Dass}(n) \notin DB^*. \emptyset.DB^*$$
  

$$\land \mathcal{D}^{out} = f_{\lambda(n),u}(\mathbf{Dass}(n)) = D_1^{out} \dots D_k^{out},$$
  

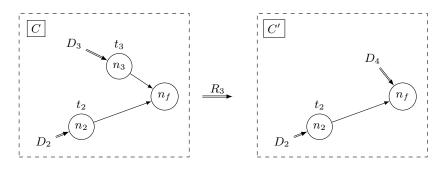
$$\mathbf{Dass}' = \mathbf{Dass} \setminus \{(n, \mathbf{Dass}(n))\} \cup$$
  

$$\{(n_k, \mathbf{Dass}(n_k)_{[j/D_k^{out}]}) \mid n_k \in succ(n)$$
  

$$\land n \text{ is the } j^{th} \text{ predecessor of } n_k\}$$
  

$$(3)$$

$$(W, \mathbf{wa}, \mathbf{Dass}) \xrightarrow{\lambda(n)} (W \setminus n, \mathbf{wa}, \mathbf{Dass}')$$



**Fig. 5.** Application of semantic rule  $R_3$ 

Consider the example of Figure 5. We resume from the situation in Figure 4, i.e. with two nodes  $n_2, n_3$  remaining to be executed before  $n_f$ , and with a dataset composed of tagged images attached to node  $n_3$ . Let us assume that task  $t_3$  is an automated task that consists in pruning out images with tag "unknown". This task can be realized as a projection of  $D_3$  of tuples R'(id, pic, tx) such that  $tx \neq 10$ "Unknown". As a result, we obtain a dataset  $D_4$ , used as input by node  $n_f$  such that  $\forall R'(id, pic, tx) \in D_4, tx \neq$  "unknown", This task can be realized by simple SQL query.

**Rule 4** (COMPLEX TASK REFINEMENT): The refinement of a node n with t = 14 $\lambda(n) \in \mathcal{T}_{cx}$  by worker  $u = \mathbf{wa}(n)$  replaces node n by a workflow  $W_s = (N_s, \longrightarrow_s, \lambda_s)$  if a rule  $R = (t, W_s)$  exists and is listed in the competences of u. Data originally accepted as input by n are now accepted as input by the source node of  $W_s$ . All newly inserted nodes have empty input datasets.

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$$t = \lambda(n) \in \mathcal{T}_{cx} \land \exists u, u = \mathbf{wa}(n) \land (u, R) \in sk \land R = (t, W_S)$$
  

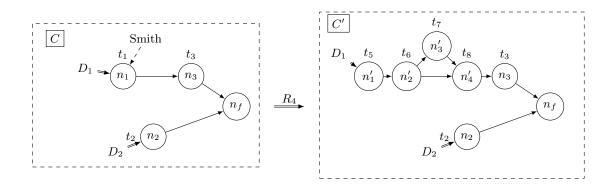
$$\land \mathbf{Dass'}(min(W_s)) = \mathbf{Dass}(n)$$
  

$$\land \forall x \in N_s \setminus min(W_s), \mathbf{Dass'}(x) = \emptyset^{|Pred(x)|}$$
  

$$\land \mathbf{wa'} = \mathbf{wa} \setminus \{(n, \mathbf{wa}(n))\}$$
  

$$ref(n)$$
(4)

 $(W, \mathbf{wa}, \mathbf{Dass}) \xrightarrow{ref(n)} (W_{[n/W_s]}, \mathbf{wa}', \mathbf{Dass}')$ 



**Fig. 6.** Application of semantic rule  $R_4$ 

Consider the example of Figure 6. Let us assume that worker "Smith" is assigned task  $t_1$  and that this task is a complex tagging task (for instance workers are asked to find names of rare species). In such situation, Smith can decide to replace the task by a simple single-worker tagging mechanism, or by a more complex workflow, that asks a competent worker to tag pictures, then separates the obtained datasets into pictures with/without tag "Unknown", and sends the unknown species to an expert (for instance an entomologist) before aggregating the union of all responses. This refinement lead to a configuration C', shown in the right part of Figure 6, where  $n'_1$ is a tagging task,  $n'_2$  is an automated task to split a dataset,  $n'_3$  is a tagging tasks which requires highly competent workers and  $n'_4$  is an aggregation task. Note that 10 conditions for worker assignment guarantee that refinement is always performed by 11 a competent worker, owning an appropriate refinement rule to handle a task. 12

Note that the definition of a *complex* task is very subjective and varies from one worker to another. Classifying tasks as complex or not a priori should not be seen as a limitation, as refinement is not mandatory: a worker can replace a node n labeled by task  $t \in \mathcal{T}_{cx}$  by a another node labeled by an equivalent task  $t' \in \mathcal{T}_{ac} \cup \mathcal{T}_{aut}$  if this possibility is allowed by the rules she can apply. This allows to model situations where a worker has the choice to realize a task or refine it when she thinks it is too complex to be handled by a single person.

Runs of a complex workflow are successive rewritings of configurations via rules. Figure 7 gives an example of run. The top-left part of the figure is an initial con-

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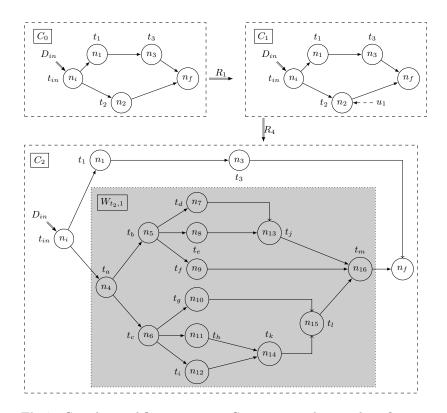
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figuration  $C_0 = (W_0, \mathbf{wa}_0, \mathbf{Dass}_0)$  composed of an initial workflow  $W_0$ , an empty map  $\mathbf{wa}_0$  and a map  $\mathbf{Dass}_0$  that associates dataset  $D_{in}$  to node  $n_i$ . The top-right part of the figure represents the configuration  $C_1 = (W_1, \mathbf{wa}_1, \mathbf{Dass}_1)$  obtained by assigning worker  $u_1$  for execution of task  $t_2$  attached to node  $n_2$  (Rule 1). The bottom part of the Figure represents the configuration  $C_2$  obtained from  $C_1$  when worker  $u_1$  decides to refine task  $t_2$  according refinement rule  $(t_2, W_{t_2,1})$  (Rule 4). Workflow  $W_{t_2,1}$  is the part of the Figure contained in the Grey square.



**Fig. 7.** Complex workflow execution.  $C_0$  represents the initial configuration with data  $D_{in}$  allocated to node  $n_i$ .  $C_1$  is the successor of  $C_0$ : worker  $u_1$  is allocated to node  $n_2$ , and  $t_2 = \lambda(n_2)$  is a complex task.  $C_3$  depicts the configuration after refinement of node  $n_2$  by a new workflow  $W_{t2}$  (shown in the Grey rectangle).

### A.2 A non-terminating Complex Workflow

Let us show on an example why complex workflow may not terminate. Consider a simple linear workflow composed of three nodes :  $n_i, n_f, n_1$  where  $n_1$  is attached task  $\lambda(n_1) = t_1$  such that  $\longrightarrow = \{(n_i, n_1), (n_1, n_f)\}$ . Let us assume that our system has a single worker  $u_1$ , and that this worker has the right to use rule  $rewrite_1 = (t_1, W_{t_1})$  where  $W_{t_1}$  is a workflow with three nodes  $w_1, w_2, w_f$ , such that  $\lambda(w_1) = t_2$  and  $\lambda(w_2) = t_1$  and where  $\longrightarrow = \{(w_1, w_2), (w_1, w_f)\}$ . Then, after application of semantic rule R1 (assigning worker  $u_1$  to the node that carries task  $t_1$ ) and semantic rule R4 (replacing via rewriting rule rewrite<sub>1</sub> task  $t_1$  by  $W_{t_1}$ ), one obtains a larger workflow that still contains an occurrence of task  $t_1$ . One can repeat these steps an arbitrary number of times, leading to configurations which workflow parts are growing sequences of nodes labeled by sequences of task occurrences of the form  $\lambda(n_i) t_2^k t_1 \lambda(w_f)^k \lambda(n_f)$ . In this recursive scheme, the workflow part of configurations obviously grows. Moreover, but one can easily modify this example to exhibit complex workflows with unbounded recursive schemes where 10 the data part of configurations grows unboundedly (for instance if  $t_2$  is a task that 11 adds records to some dataset). 12

#### В Proofs for FO

**Proposition 4.** Let X be a set of variables of the form  $X = X_b \uplus X_r$  where vari-14 ables from  $X_b$  take values from finite domains and variables from  $X_r$  take values in 15  $\mathbb{R}. \ Then, \ satisfiability \ of \ formulas \ of \ the \ form \ \phi ::= \exists \overrightarrow{X}. \bigwedge_{i \in 1..I} R_i(X) \land \bigwedge_{j \in 1..J} P_j(X)$ 16 is NP-complete. 17

*Proof.* Let us first show that the problem belongs to NP. Let us consider an ex-18 istential formula  $\phi ::= \exists X, \psi$  where  $\psi$  contains positive relational statements of 19 the form  $\phi_{R+} ::= R_1(X), \ldots R_k(X)$ , and negative relational statements of the form 20  $\phi_{R-} ::= \neg R_1(X), \ldots \neg R_{k'}(X)$ , and predicates of the form  $P_1(X), \ldots P_J(X)$ . For 21 each  $R_i(x_1,\ldots,x_q)$  in  $\phi_{R+}$ , with relational schema  $rn_i$  and legal domain  $Dom_i$ , 22 we define  $Ldom_i$  as the constraint  $(x_1, \ldots x_q) \in Dom_i$ . One can choose nondeter-23 ministically in polynomial time a value  $d_x$  for each bounded variable x in  $X_b$ , and 24 obtain a formula where only real variables appear by substitution of these variables 25 by their value. 26

Then one can choose non-deterministically which relational statements and 27 predicate hold, by guessing a truth value  $v_i \in \{true, false\}$  for each relation 28  $R_i \in 1..I$  (Resp. predicate  $P_j, j \in 1..J$ ). Now, for each pair of choices where 29  $rn(x_1, \ldots x_q)$  holds and  $rn(x'_1, \ldots x'_q)$  does not, we verify that the designed tuples are disjoint, i.e. that  $\neg(x_1 = x'_1 \land \cdots \land x_q = x'_q)$ . We call  $\phi_{RxR}$  the formula  $r(x_1 = x'_1 \land \cdots \land x_q = x'_q)$ . 30 31 mula that is the conjunction of such negations. The size of  $\phi_{RxR}$  is in  $O(r.|\phi^2|)$ 32 where r is the maximal arity in a relational schema of the complex workflow. 33 We can then verify that the guess of truth value for atoms yields satisfaction 34 of  $\phi$ , i.e. check that  $\phi'_{[R_i, P_j/true, false, v_j]}$  evaluates to true. In case of positive answer, it suffices to check that with the truth value choosen for atoms, the formula 35 36  $\phi_{RxR} \wedge \bigwedge_{i \in 1..k} Ldom_i \wedge \bigwedge_{v_i = true} P_i \wedge \bigwedge_{v_i = false} \neg P_i \text{ is satisfiable, i.e. that one can find an } P_i \wedge \bigwedge_{v_i = false} \neg P_i \text{ is satisfiable, i.e. that one can find an } P_i \wedge \bigwedge_{v_i = true} P_i \wedge \bigwedge_{v_i = false} \neg P_i \text{ is satisfiable, i.e. that one can find an } P_i \wedge \bigwedge_{v_i = true} P_i \wedge \bigwedge_$ 37 assignment for the real variables that are not yet valuated, which can be done in 38 polynomial time. Now, for the hardness proof, one can easily encode a SAT problem 39 with an FO formula over boolean variables. Checking satisfiability of a universally 40

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quantified formula can be done in co - NP in the same way, as  $\forall X\phi$  is satisfiable iff  $\exists X, \neg \phi$  is not.  $\Box$ 

### **B.1** Proof of Proposition 1:

**Proposition 1:** Let CW be a complex workflow, r be the maximal arity of relational schemas in CW and  $\psi$  be an FO formula. Then for any move m of CW,  $wp[m]\psi$ is an effectively computable FO formula, and is of size in  $O(r, |\psi|)$ .

*Proof (Sketch).* The effect of moves on the contents of datasets can be described as sequential composition of basic operations that are projections of datasets, selections, insertions of records or fields, differences, unions or joins of dataset. We first show that these basic dataset transformations allow for computation of a weakest precondition, and then show on a particular move (selection of records, 11 Lemma 1) application of these basic properties. We do not detail all technical lem-12 mas in this appendix, but they are rather straightforward, and will appear in an 13 extended version of this work. Let  $D_1, \ldots D_k$  be the datasets that appear in  $\psi$ . If 14 some  $D_i$  is obtained as a selection of records from a dataset  $D'_i$ , then  $D_i$  contains 15 only records of  $D'_i$  satisfying some predicate P. The precondition will hence be 16 obtained by a simple replacement in  $\psi$  of any statement of the form  $rn(\overrightarrow{X}) \in D_i$ 17 by  $rn(X) \in D_i \wedge P(X)$ . 18

If  $D_i$  is obtained after insertion of a fresh record in some dataset  $D'_i$  then every 19 statement  $rn(\overline{X}) \in D_i$  can be replaced by a subformula  $(rn(\overline{X}) \in D'_i \lor Dom_i(\overline{X}))$ 20 where  $Dom_i(\vec{X})$  represents constraints on legal values of inputs in a dataset with 21 the same relational schema as  $D_i$ . Note that  $Dom_i(X)$  is a quantifier free boolean 22 combination of predicates. 23

Similarly, if some dataset  $D_i$  is obtained as the union of two datasets  $D_1, D_2$ , 24 the precondition for  $\psi$  should consider that tuples that satisfy  $rn(\overrightarrow{X}) \in D_i$  belong 25 to  $D_1$  or  $D_2$ . We simply replace atoms of the form  $rs(\overrightarrow{X}) \in D_i$  by the disjunction 26  $rn(\overrightarrow{X}) \in D_1 \lor rn(\overrightarrow{X}) \in D_2$ . We also replace negative statements  $rn(\overrightarrow{X}) \notin D_i$  by 27 conjunction  $rn(\overrightarrow{X}) \notin D_1 \wedge rn(\overrightarrow{X}) \notin D_2$ . The size of the obtained formula is hence 28 in  $O(2.|\psi|)$ . 29

If some  $D_i$  is obtained by creation of a new field for each record in dataset  $D'_i$ , 30 then relational statement  $rn(\overrightarrow{X}) \in D_i$  is replaced by another statement  $rn(\overrightarrow{Y}) \in D_i$ 31  $D'_i \wedge P'(\overrightarrow{Y})$  where  $\overrightarrow{Y}$  is a subset of  $\overrightarrow{X}$ , and  $P'(\overrightarrow{Y})$  is a quantifier free predicate 32 indicating constraint on  $\overline{Y}$  obtained after variable elimination when  $\overline{X}$  takes 33 legal values imposed by relational schema of  $D_i$  (i.e. it satisfies  $Ldom_i$  –see proof 34 of Proposition 4–) and satisfies the constraints of relational schema of  $D'_i$ . As we 35 assume that arithmetic predicates are simple (two-dimensional) inequalities, the 36 size of P' is not larger than that of  $Ldom_i$ . The weakest precondition can hence 37 double the number of atoms, but keeps the same bound on the number of variables 38 used. 39

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For (binary) joins, relation of the form  $rs(\overrightarrow{X}_i)$  are transformed in statements of the form  $rs(\overrightarrow{Y_i}) \wedge rs(\overrightarrow{Z_i}) \wedge y_1 = z_1$ , where  $y_1 \in \overrightarrow{Y_i}$  and  $z_1 \in \overrightarrow{Z_i}$ . As every relational statement can be replaced and hence create new variables, this calculus of a weakest precondition may give a formula of size in  $O(2, |\psi|)$ .

Last, if some  $D_i$  is a projection of some dataset  $D'_i$  on a subset of its field, then the weakest precondition for  $\psi$  may multiply the number of variables in use by r, whence giving a formula of size in  $O(r, |\psi|)$ .

We rely on technical lemmas that detail the construction of a weakest precondition for each particular type of move.

#### **B.2** A technical lemma for weakest precondition

The computation of weakest precondition can be effectively performed for every 11 type of task (automated execution of SQL requests, insertion/creation/deletion 12 of answers by workers, refinement,...). We give below an example of weakest precondition calculus for a task that performs a selection of records that satisfy some 14 predicate in a dataset. For all other types of actions, computing a weakest precondition follows the same lines. For conciseness, we do not detail all of them. The 16 whole set of lemma for each type of action is considered in an extended version of 17 this work. 18

Lemma 1 (Weakest precondition for Selection of records). Let  $\varphi$  be a FO 19 formula, and mv be a move that selects records that satisfy a predicate P from 20 datasets. Then one can effectively compute an FO formula  $\psi = wp[mv]\varphi$ . Moreover, 21 if  $\varphi$  is in  $\forall FO$  (resp.  $\exists FO$ , BSR, SF) and P is an arithmetic/boolean predicate then 22  $\psi$  is also in  $\forall FO$  (resp.  $\exists FO$ , BSR, SF). 23

*Proof.* Let  $D'_1, \ldots, D'_j, \ldots, D'_k \models \varphi$ , and let  $D'_j$  be a dataset with relational schema 24 rs = (rn, A) obtained by selection of records from an input dataset  $D_i$  with rela-25 tional schema rs(rn, A). One can notice that selection keeps the same relational 26 schema, and in particular the same set of attributes  $A = (a_1, \ldots a_k)$ . We will as-27 sume that selected records are records that satisfy some predicate  $P(v_1, \ldots v_k)$ 28 that constrain the values of a record (but do not address properties of two or 29 more records of  $D_i$ ). That is, the records selected from  $D_i$  by P are records 30 that satisfy  $\psi_{sel} = \exists v_1, \ldots v_k, rn(v_1, \ldots v_p) \land P(v_1, \ldots, v_k)$ . We want to compute 31  $\psi = wp[Selection(\psi_{sel})] \varphi.$ 32

Formula  $\varphi$  is a formula of the form  $\alpha(\overrightarrow{X}).\phi$ , where  $\alpha(\overrightarrow{X})$  is a prefix. It contains  $K_{rn}$  subformulas of the form  $rn(w_i, \ldots, w_{i+k})$  or  $\neg rn(w_i, \ldots, w_{i+k})$  and we assume without loss of generality that these subformulas are over disjoint sets of variables (one can add new variables and equalities if this is not the case). Let  $\phi_{rn,1}, \ldots \phi_{rn,K_{rn}}$  be the subformulas of  $\phi$  addressing tuples with relational schema rs. For  $i \in 1..K_{rn}$ , we let  $\phi_{rn,i}^P$  denote the formula  $rn(w_i, \ldots, w_{i+k}) \wedge P(w_i, \ldots, w_{i+k})$ if  $\phi_{rn,i}$  is in positive form and  $\neg (rn(w_i, \ldots, w_{i+k}) \wedge P(w_i, \ldots, w_{i+k}))$  otherwise. Let us denote by  $\phi_{[\{\varphi_{rn,i}\}|\{\varphi_{rn,i}^{P}\}]}$  the formula  $\phi$  where every  $\phi_{rn,i}$  is replaced by  $\phi_{rn,i}^{P}$ .

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The weakest precondition on  $D'_1, \ldots, D'_k$  for a selection operation with predicate P is defined as

$$\psi = wp[Selection(\psi_{sel})]\varphi = \alpha(\overrightarrow{X}).\phi_{[\{phi_{rn,i}\}|\{phi_{rn,i}^{P}\}]}$$

Last, one can notice that transforming  $\alpha(\overrightarrow{X}).\phi$  into  $\alpha(\overrightarrow{X}).\phi_{[\{phi_{rn,i}\}|\{phi_{rn,i}^{P}\}]}$ does not introduce new variables, and preserve the prefix of the formula. As  $\varphi$  and  $\psi$  start with the same prefix  $\alpha(\overrightarrow{X})$ , we can claim that  $\varphi$  and  $\psi$  are in the same fragment of FO.  $\Box$ 

One can notice that this weakest precondition is a rather syntactic transformation, that replaces atoms of the form  $rn(x_1, \ldots x_k)$  by  $rn(x_1, \ldots x_k) \wedge P(x_1, \ldots x_k)$ . If  $x_1, \ldots, x_k$  are all existentially quantified variables (resp. all universally quantified) in  $\psi$ . Hence, if  $\varphi$  is in  $\exists$ FO, $\forall$ FO,BSR, SF-FO then so is  $wp[Selection(\psi_{sel})]\varphi$ . The same remark applies to all other types of moves (we do not give proofs for each move here, but they follow the same line as for selection, and will be available in an extended version of this work).

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## C Appendix : proofs for termination

### C.1 Proof of Theorem 1

**Theorem 1** Existential termination of complex workflows is an undecidable problem.

*Proof.* The proof is done by reduction from the halting problem of two counter machines to termination of complex workflows. A 2-counter machine (2CM) is a tuple  $\langle Q, c_1, c_2, I, q_0, q_f \rangle$  where:

- -Q is a finite set of states. -  $q_0 ∈ Q$  is the initial state,  $q_f ∈ Q$  is a particular state called the final state.
- $-c_1, c_2$  are two counters holding non-negative integers.
- $-I = I_1 \cup I_2$  is a set of instructions. Instructions in  $I_1$  are of the form  $inst_q =$ 23  $inc(q, c_l, q')$ , depicting the fact that the machine is in state q, increases the 24 value of counter  $c_l$  by 1, and moves to a new state q'. Instructions in  $I_2$  are 25 of the form  $inst_q = dec(q, c_l, q', q'')$ , depicting the fact that the machine is in 26 state q, if  $c_l == 0$ , the machine moves to new state q' without making any 27 change in the value of counter  $c_l$ , and otherwise, decrements the counter  $c_l$  and 28 moves to state q''. We consider deterministic machines, i.e. there is at most 29 one instruction  $inst_q$  per state in  $I_1 \cup I_2$ . At any instant, the machine is in a 30 configuration  $C = (q, v_1, v_2)$  where q is the current state,  $v_1$  the value of counter 31  $c_1$  and  $v_2$  the value of counter  $c_2$ . The machine executes instructions from its 32 current configuration, and stops as soon as it reaches state  $q_f$ . 33

From a given configuration  $C = (q, v_1, v_2)$ , a machine can only execute instruction  $inst_q$ , and hence the next configuration  $\Delta(C)$  of the machine is also unique. A run of a two counters machine is a sequence of configurations  $\rho = C_0.C_1...C_k$ such that  $C_i = \Delta(C_{i-1})$ . The halting problem is defined as follows: given a 2-CM, an initial configuration  $C_0 = (q_0, 0, 0)$ , decide whether a run of the machine reaches some configuration  $(q_f, n_1, n_2)$ , where  $q_f$  is the final state and  $n_1, n_2$  are arbitrary values of the counter. It is well known that this halting problem is undecidable.

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Let us now show how to encode a counter machine with complex workflows.

- We consider a dataset D with relational schema  $rs = (R, \{k, cname\})$  where k is a unique identifier, and  $cname \in Cnt_1, Cnt_2, \bot$ . Clearly, we can encode the value of counter  $c_x$  with the cardinal of  $\{(k, n) \in D \mid n = Cnt_x\}$ . We start from a configuration where the dataset contains a single record  $R(0, \bot)$
- For every instruction of the form  $inc(q, c_x, q')$  we create a task  $t_q$ , and a workflow  $W_q^{inc}$ , and a worker  $u_q$ , who is the only worker allowed to execute these tasks. The only operation that  $u_q$  can do is refine  $t_q$  with workflow  $W_q^{inc}$ .  $W_q^{inc}$ has two nodes  $n_q^{inc}$  and  $n_{q'}$  such that  $(n_q^{inc}, n_{q'}) \in \longrightarrow$ ,  $\lambda(n_q^{inc}) = t_q^{inc}$  and  $\lambda(n_{q'}) = t_{q'}$ . Task  $t_q^{inc}$  is an atomic task that adds one record of the form  $(k', Cnt_x)$  to the dataset. Hence, after executing tasks  $t_q$  and  $t_q^{inc}$ , the number of occurrences of  $Cnt_x$  has increased by one.
- For every instruction of the form  $dec(q, c_x, q', q'')$ , we create a complex task  $t_q$ and a worker  $u_q$  who can choose to refine  $t_q$  according to rule  $(t_q, W_{q,Z})$  or rule  $(t_q, W_{q,NZ})$ . The choice of one workflow or another will simulate the decision to perform a zero test or a non-zero test. Note that as the choice of a particular rule to replace a task workflow is non-deterministic, worker  $u_q$  can choose one or the other.
- Let us now detail the contents of  $W_{q,NZ}$ , represented in Figure 8. This workflow is composed of nodes  $n_q^{div}, n_q^{C_x}, n_q^{C_x \cup \perp}, n_q^{\otimes}, n_q^{dec}$  and  $n_{q''}$ , respectively labeled by 26 27 tasks  $t_q^{div}, t_q^{C_x}, t_q^{C_x \cup \perp}, t_q^{\otimes}, t_q^{dec}$  and  $t_{q''}$ . The dependence relation in  $W_{q,NZ}$  contains pairs  $(n_q^{div}, n_q^{C_x}), (n_q^{div}, n_q^{C_x \cup \perp}), (n_q^{C_x}, n_q^{\otimes}), (n_q^{C_x \cup \perp}, n_q^{\otimes}), (n_q^{\otimes}, n_q^{dec})$  and 28 29  $(n_q^{dec}, n_{q'})$ . The role of  $t_q^{div}$  is to split  $\mathbf{Dass}(n_q^{div})$  into disjoint parts: the first 30 one contains records of the form  $R(k, C_x)$  and the second part consists of all other remaining records. Tasks  $t_q^{C_x}$  and  $t_q^{C_x \cup \perp}$  simply forward their inputs, and 31 32 task  $t_q^{\otimes}$  computes the union of its inputs. Note however that if one of the inputs 33 is empty, the task cannot be executed. Then, task  $t_q^{dec}$  deletes one record of 34 the form  $R(k, C_x)$ . Hence, if  $D_q = \mathbf{Dass}(n_q)$  is a dataset that contains at least 35 one record of the from  $R(k, C_x)$ , the execution of all tasks in  $W_{q,NZ}$  leaves the 36 system in a configuration with a minimal node  $n_{q''}$  labeled by task  $t_{q''}$ , and 37 with  $\mathbf{Dass}(n_{q'}) = D_q \setminus R(k, C_x)$ 38
- Let us now detail the contents of  $W_{q,Z}$ . This workflow is composed of nodes  $n_q^{div}, n_q^{C_x \cup \perp}, n_q^{id}, n_q^{btest}, n_q^{done}, n_{q'}$  respectively labeled by tasks  $t_q^{div}, t_q^{C_x \cup \perp}, t_q^{id}, t_q^{div}, t_q^{C_x \cup \perp}, t_q^{id}, t_q^{dive}, t$

the input dataset and forwards it to node  $n_q^{id}$ . The role of task  $t_q^{C_x \cup \perp}$  is to perform a boolean query that returns  $\{true\}$  if the dataset contains a record  $R(k, C_x)$  and  $\{false\}$  otherwise, and forwards the result to node  $n_q^{btest}$ . Task  $t_a^{btest}$  selects records with value  $\{false\}$  (it hence returns an empty dataset as the result of the boolean test was  $\{true\}$ ). Task  $t_q^{id}$  forwards its input to node  $n_q^{done}$ . Task  $t_q^{done}$  received input datasets from  $n_q^{btest}$  and  $n_q^{id}$  and forwards the input from  $n_q^{id}$  to node  $n_{q''}$ . One can immediately see that if the dataset input to  $n_q^{div}$  contains an occurrence of  $C_x$  then one of the inputs to  $n_q^{done}$ is empty and hence the workflow deadlocks. Conversely, if this input contains no occurrence of  $C_x$ , then this workflows reached a configuration with a single 10 node  $n_{q''}$  labeled by task  $t_{q''}$ , and with the same input dataset as  $n_q$ . 11

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One can see that for every run  $\rho = C_0 \dots C_k$  of the two counter machine, where 12  $C_k = (q, v_1, v_2)$  there exists a single non-deadlocked run of the complex workflow, 13 that terminates of configuration (W, wa, Dass) where W consists of a single node 14  $n_q$  labeled by task  $t_q$ , and such that  $\mathbf{Dass}(n_q)$  contains  $v_1$  occurrences of records 15 of the form  $R(k, C_1)$  and  $v_2$  occurrences of records of the form  $R(k, C_2)$ . Hence, 16 a two counter machine terminates in a configuration  $(q_f, v_1, v_2)$  iff the only non-17 deadlocked run of the complex workflow that encodes the two counter machine 18 reaches a final configuration. 19

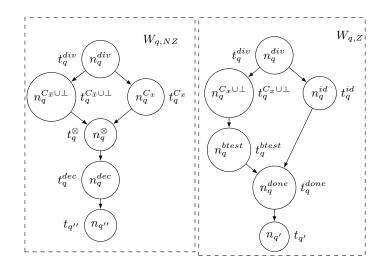


Fig. 8. Encoding of Non-zero test followed by decrement (left), and Zero Test followed by state change (right).

#### C.2Successor relation among symbolic configurations

From a symbolic configuration, that does not describe the exact contents of datasets in use, we can compute the effects of application of a particular rule, i.e. compute symbolic descriptions of configurations that appear after a move. A symbolic configuration  $C_j^S = (W_j, \mathbf{wa}_j, Dass_j^S)$  is the successor of a symbolic configuration  $C_i^S = (W_i, \mathbf{wa}_i, Dass_i^S)$  iff one of the following situation holds:

- there exists a worker  $u \in \mathcal{U}$  and a node  $n \in W_i$  such that  $\mathbf{wa}_i^{-1}(u) = \emptyset$ ,  $\mathbf{wa}_i(n) = \emptyset, \ \exists (u, \lambda(n)) \in sk \text{ or } (u, r) = (\lambda(n), W_t)) \in sk, \text{ and } W_i = W_i,$  $\mathbf{Dass}^{S} = \mathbf{Dass}^{S}$  and  $\mathbf{wa}_{i} = \mathbf{wa}_{i} \uplus \{(n, u)\}.$
- there exists  $n \in min(W_i)$  such that  $t = \lambda(n)$  is an automated task manipulating datasets  $D_1, \ldots, D_q, n$  has k successors  $n_1, \ldots, n_k, W_j = W_i \setminus \{n\}, \mathbf{Dass}^S$  assigns to each successor  $n_i, j \in 1..k$  the relational schema  $rs_i^{out}$ , and  $\mathbf{wa}_i = \mathbf{wa}_i$ .
- there exists  $n \in min(W_i)$  such that  $t = \lambda(n)$  is an atomic task manipulating datasets  $D_1, \ldots D_q$ , with and n has k successors  $n_1, \ldots n_k, W_j = W_i \setminus \{n\},\$ 14 **Dass**<sup>S</sup> assigns to each successor  $n_j, j \in 1..k$  the relational schema  $rs_j^{out}$ , and  $\mathbf{wa}_i = \mathbf{wa}_i \setminus \{(n, \mathbf{wa}_i(n))\}.$
- there exists  $n \in W_i$ ,  $\lambda(n)$  is a complex task, and  $\mathbf{wa}(n) = u$ ,  $W_j$  is the 17 workflow obtained by replacement of n in  $W_i$  by a workflow  $W^{new}$  such that 18  $r = (\lambda(n), W^{new}) \in \mathcal{R}$ , and  $(u, r) \in sk$ . **Dass**<sup>S</sup> assigns to the copy of minimal 19 node  $n_i$  of  $W^{new}$  the relational schemas in  $Dass_i^S(n)$ , and  $\mathbf{wa}_i = \mathbf{wa}_i \setminus \{(n, u)\}$ . 20

#### C.3 Proof of Proposition 2

**Proposition 2:** Let CW be a complex workflow,  $D_{in}$  be a dataset,  $\mathcal{D}_{in}$  be an FO formula with  $n_{in}$  variables, and  $\rho^S = C_0^S \dots C_i^S$  be a symbolic run. If tasks do not 22 23 use SQL difference, then deciding if there exists a run  $\rho$  with input dataset  $D_{in}$  and 24 signature  $\rho^{S}$  is in 2EXPTIME. Checking if there exists a run  $\rho$  of CW and an 25 input dataset  $D_{in}$  that satisfies  $\mathcal{D}_{in}$  with signature  $\rho^S$  is undecidable in general. If 26 tasks do not use SQL difference, then it is in 27

- 2EXPTIME if  $\mathcal{D}_{in}$  is in  $\exists$ FO and 3EXPTIME if  $\mathcal{D}_{in}$  is in  $\forall$ FO or BSR-FO. 28 29
- $-n_{in}-foldEXPTIME$  where  $n_{in}$  is the size of the formula describing  $\mathcal{D}_{in}$  if  $\mathcal{D}_{in}$  is in SF-FO

*Proof.* We have to check feasibility of  $\rho^S$ , that is starting from  $C_i^S$ , check that all 31 conditions met along a run with signature  $\rho^S$  to reach a configuration  $C_i$  com-32 patible with  $C_i^S$  are met at each step, and allow for existence of configurations 33  $C_0, C_1, \ldots C_{i-1}$ . First notice that the actual run with signature  $\rho^S$  performs the 34 same sequence of moves as in  $\rho^S$ , and that the question of existence of a run  $\rho$  with 35 signature  $\rho^S$  only needs to verify satisfiability of constraints on data computed at 36 each step of this run, not the sequence of moves along  $\rho$ . Second, one can notice 37 that if  $\rho^S$  contains a deadlock, it is necessarily the last symbolic configuration of 38 the run, as for every symbolic configuration from  $C_0^S$  up to  $C_{i-1}^S$  we are able to 39 find a successor configuration. So one needs not check existence of a deadlock sep-40 arately when checking feasibility of  $\rho^{S}$ , and we mainly have to check for emptiness 41

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of datasets for configurations that are potential deadlocks. A third remark is that semantic rules that affect workers to tasks or perform a refinement do not consider data contents. Hence, if the move from  $C_{i-1}$  to  $C_i$  is a worker assignment or a refinement, then it is necessarily feasible as long as  $C_{i-1}$  is reachable. The only cases where data can affect execution of a step along a run is when an automated task or an atomic task has to process empty data. For each of these steps, one has to check that the inputs of an executed task t are not empty, i.e. suppose that  $D_1 \neq \emptyset \land \dots \land D_k \neq \emptyset$  for some datasets  $D_1 \dots D_k$  used by t. Non-emptiness of a dataset  $D_k$  is simply encoded by the  $\exists FO$  formula  $\exists X, rn(X) \in D_k$ .

Non-emptiness of a dataset  $D_k$  at some configuration  $C_j$  is a property that 10 depends on properties of previous steps in the execution. For instance, if the move 11 from  $C_{j-1}$  to  $C_j$  realizes the projection of a dataset, i.e. filters records in a dataset 12  $D'_k$  to keep only those that satisfy some predicate P, then the precondition that 13 must hold at  $C_{j-1}$  is  $\psi_{j-1} ::= \exists \overrightarrow{X}, rn(\overrightarrow{X}) \land P(\overrightarrow{X})$ . We have seen in Proposition 1 that , if the move  $C_{j-1} \xrightarrow{m_{i-1}} C_{i-1}$  is a transformation of records, a transformation 14 15 of some dataset that adds new fields, a join of two datasets, the formula  $\psi_{i-1}$  is effectively computable. Further, from Corollary 1, if tasks do not use SQL differ-17 ence, the weakest precondition of an existential FO formula is an existential FO 18 formula. 19

This generalizes to the whole signature. Let  $\psi_k$  be an  $\exists$ FO formula that has to 20 be satisfied by configuration  $C_k$  in a run compatible with signature  $\rho^S.$  There exists 21 a sequence of moves  $C_0 \xrightarrow{m_1} C_1 \dots \xrightarrow{m_k} C_k$  iff the sequence  $C_0 \xrightarrow{m_1} C_1 \dots \xrightarrow{m_{k-1}} C_{k-1}$ 22 ends in a configuration  $C_{k-1}$  such that  $C_{k-1} \models wp[m_k]\psi_k$  (by definition of weakest 23 precondition). One can decide whether  $wp[m_k]\phi_k$  is satisfiable, as  $\psi_k$  is in  $\exists FO$ , 24 and by Prop. 1,  $wp[m_k]\psi_k$  is effectively computable and in the  $\exists FO$  fragment. 25 If  $wp[m_k]\psi_k$  is not satisfiable, then the move from  $C_{k-1}$  to  $C_k$  always ends with 26 datasets that do not fulfill  $\psi_k$ . If  $wp[m_k]\psi_k$  is satisfiable, then the runs that reach 27  $C_{k-1}$  are realizable only if we assume that several datasets (used as input of some 28 task realized at step k) are non-empty at stage k-1. We then have to add statements 29 of the form  $D_i \neq \emptyset$  to obtain a formula that should hold at step k-1, and get a 30 formula of the form  $\psi_{k-1} ::= wp[m_k]\psi_k \wedge D_1 \neq \emptyset \wedge \cdots \wedge D_m \neq \emptyset$ . This adds only 31 an existential conjunction, so  $\psi_{k-1}$  is also in  $\exists FO$ . 32

Now, one can starts from  $\psi_i ::= true$  and build inductively all weakest pre-33 conditions  $\psi_{i-1}, \psi_{i-2}, \ldots, \psi_0$  that have to be satisfied respectively by configura-34 tions  $C_{i-1}, \ldots, C_0$  so that an actual run of the complex workflow with signature 35  $C_0^S \dots C_i^S$  exists. If any of these preconditions is unsatisfiable, then there exists no 36 run with signature  $C_0^S \dots C_k^S$  leading to a configuration  $C_i$  compatible with  $C_i^S$ , and 37 hence  $\rho^S$  is not the signature of an actual run of CW. The size of  $\psi_0$  is in  $O(i.r^i)$ . 38 Indeed, we add obligations to prove non-emptiness at each step k, but proving 39 satisfiability of  $\exists \vec{X}, \phi(\vec{X}) \land \exists \vec{X}, \phi(\vec{X})$  amounts to checking separately satisfia-40 bility of  $\exists \overrightarrow{X}, \phi(\overrightarrow{X})$  and  $\exists \overrightarrow{Y}, \phi(\overrightarrow{Y})$ . According to Prop. 1, the size of  $wp[m_k]\psi$ 41 is in  $O(r, |\psi|)$ , where r is the maximal arity of relational schemas of the complex 42 workflow. So one can check separately satisfiability of  $\exists \vec{X}, \phi(\vec{X})$  and  $D_x \neq \emptyset$ , and 43

maintain a series of O(i) formulas of total size in  $O(i.r^i)$ . Hence, as  $\psi_0$  is still in the existential fragment of FO, and as checking satisfiability of an existential FO formula is in EXPTIME in the size of the formula (by proposition 4), checking all preconditions for a run of size k compatible with  $\rho^S$  can have a complexity that is in  $O(2^{r^i})$ .

Assume that  $\psi_{k-1}, \psi_{k-2}, \ldots, \psi_0$  are satisfiable. It remains to show that the input(s) of the complex workflow satisfy the weakest precondition for the execution of  $\rho^S$ , i.e. satisfy  $\psi_0$ . Then, when the input is a single dataset  $D_{in}$ , it remains to check that  $D_{in} \models \psi_0$  to guarantee existence of a run with signature  $C_0^S \ldots C_i^S$  that starts with input data  $D_{in}$  and leads to a configuration  $C_k$ . This is a standard model checking question, which can be solved in  $O(|D_{in}|^{|\psi_0|})$ , that is in  $O(|D_{in}|^{r^k})$ . As the complexity of checking satisfiability of weakest preconditions  $\psi_k \ldots \psi_0$  is already in 2EXPTIME, the overall complexity is in 2EXPTIME.

Similarly, if  $\mathcal{D}_{in}$  is given as an FO formula, the complexity depends on the 14 considered fragment used to specify  $\mathcal{D}_{in}$ . In general, if  $\mathcal{D}_{in}$  is given as an FO 15 formula, it is undecidable if  $\mathcal{D}_{in} \wedge \psi_0$  is satisfiable. If  $\mathcal{D}_{in}$  is an existential formula, 16 then the complexity is exponential in the size of  $\mathcal{D}_{in}$  and also exponential in the 17 size of  $\psi_0$ . Assuming that  $|\mathcal{D}_{in}| \leq 2^k$  we have a 2EXPTIME complexity. If  $\mathcal{D}_{in}$  is 18 in the BSR fragment, then checking satisfiability of  $\mathcal{D}_{in}$  is in NEXPTIME [28], 19 and so the overall complexity needed to check existence of a run with signature 20  $\rho^S$  from a dataset in  $\mathcal{D}_{in}$  is in 2EXPTIME w.r.t the size of  $\mathcal{D}_{in} \wedge \psi_0$ , and hence 21 3EXPTIME. If  $\mathcal{D}_{in}$  is a universal formula then we can use standard mini-scoping 22 rules to transform  $\mathcal{D}_{in} \wedge \psi_0$  is a formula in the BSR fragment, yielding again 23 a 3EXPTIME complexity. Last if  $\mathcal{D}_{in}$  is in the separated fragment of FO, then 24 checking its satisfiability is  $n_{in}$ -fold exponential in the size of the formula depicting 25  $\mathcal{D}_{in}$ , so the overall process of checking realizability of  $\rho^S$  has an  $n_{in}$ -fold exponential 26 complexity.  $\Box$ 27

#### C.4 Recursion freeness: decidability an bounds on runs

**Proposition 5.** Let  $CW = (W_0, \mathcal{T}, \mathcal{U}, sk, \mathcal{R})$  be a complex workflow. One can decide if CW is recursion free in  $O(|\mathcal{T}_{cx}^2| + |\mathcal{R}|)$ .

Proof. Building RG(CW) can be done in  $O(|\mathcal{R}|)$ . Checking existence of a cycle in RG(CW) that is accessible from some task in  $W_0$  can be done in polynomial time in the size of RG(CW), for instance using a DFS algorithm, than runs in time in  $O(|\mathcal{T}_{cx}|^2)$ .  $\Box$  34

In executions of recursion free CWs, a particular task t can be replaced by a workflow that contains several tasks  $t_1, \ldots t_k$  that differ from t. Then, each  $t_i$  can be replaced by workflows combining other tasks that are not t nor  $t_i$ , and so on... For simplicity, we assume that  $W_0$  and all workflows in rules have nodes labeled by distinct task names. We can then easily prove the following property:  $y_{ij}$ 

**Proposition 6.** Let  $C = (W, \mathbf{wa}, \mathbf{Dass})$  be a configuration of a recursion free complex workflow CW. Then there exists a bound  $K_{\mathcal{T}_{cx}}$  on the size of W, and the length of a (symbolic) execution of CW is in  $O(3.K_{\mathcal{T}_{cx}})$ 

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*Proof (Sketch).* We assume, without loss of generality, that all workflows in all rules have nodes labeled by distinct task names, and that the initial workflow 2 has a single node. Let d be the maximal number of new occurrences of complex tasks that can be rewritten in one refinement (i.e., the maximal number of complex tasks that appear in a rule). Each rewriting adds at most d-1 complex tasks to the current configuration. The number or rewritings is bounded, as CW is recursion free. For a given node n appearing in a configuration  $C_k$  along a run, one can trace the sequence of rewritings Past(n) performed to produce n. According to recursion freeness, when a node n is replaced by a workflow  $W_t$ , then none of the q tasks labeling nodes of  $W_t$  appears in Past(n). Hence, the number of nodes in a 10 configuration is at most  $K_{\mathcal{T}_{cx}} = d^{\mathcal{T}_{cx}}$ . Now, for a given configuration, the number 11 of applications of semantic rules R1, R2, and R3 is bounded, and decreases the 12 number of nodes in the workflow part of the configuration.  $\Box$ 13

#### **C.5 Proof of Proposition 3**

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#### **Proposition 3** A complex workflow terminates universally if and only if:

- *i*) *it is recursion free*
- ii) it has no (symbolic) deadlocked execution
- iii) there exists no run with signature  $C_0^S \dots C_i^S$  where  $C_i^S$  is a potential deadlock, with  $D_k = \emptyset$  for some  $D_k \in \mathbf{Dass}(n_j)$  and for some minimal node  $n_j$  of  $W_i$ . 19

*Proof.* Let us first prove that if i) fails, a complex workflow does not terminate 20 universally. If CW has recursive task rewriting, then there is a cycle in the rewriting 21 graph RG(CW) that is accessible from a task  $t_0 = \lambda(n_0)$  appearing in  $W_0$ . Hence, 22 there is an infinite run  $\rho^{\infty} = C_0 \xrightarrow{a_1} C_1 \xrightarrow{r_1} C_2 \dots$  of CW which moves are only 23 worker assignments (moves of the form  $a_i$  in  $\rho^{\infty}$ ) to a node of the current workflow 24 at configuration  $C_i$  followed by a rewriting (moves of the form  $r_i$  in  $\rho^{\infty}$ ) that creates 25 new instances of tasks, such that the sequence of rewritten task follows the same 26 order as in the cycle of RG(CW). Similarly, if CW terminates universally, then all 27 runs are finite, and infinite runs of the form  $\rho^{\infty}$  cannot exist, and CW must be 28 recursion free. 29

We can now address point ii) If CW can reach a deadlocked configuration, then by definition, it does not terminate. If all runs of CW terminate, then from any configuration, there is a way to reach a final configuration, and hence no deadlock is reachable.

The need for the last point *iii*) is proved in lemma 2 below.  $\Box$ 

**Lemma 2.** Let  $C_i^S$  be a potential deadlock with successors  $C_{i,1}^S, \ldots, C_{i,k}^S$  corresponding respectively to execution of tasks attached to minimal nodes  $n_1, \ldots, n_k$  in the 35 36 workflow part of node  $C_i^S$ . Then a run  $\rho$  with signature  $\rho^S = C_0^S \dots C_i^S$  such that 37  $D_k = \emptyset$  for some  $D_k \in \mathbf{Dass}(n_j)$  does not terminate. 38

*Proof.* If a node  $n_j$  in a configuration  $C_i$  with signature  $C_i^S$  is labeled by a task 39 and is attached an empty dataset, then any sequence of worker assignment, refine-40 ment, or task execution occurring from  $C_i$  will result in a configuration  $C'_i$  where 41 either  $n_j$  is still attached an empty dataset, or  $n_j$  was replaced, but the refinement produced fresh nodes with an empty dataset attached to it. Then either  $n_j$  or one of its refinements will never be executed, and the workflow cannot reach a final configuration.

This lemma has useful consequences: it is sufficient to detect a run with signature  $C_0^S \ldots C_i^S$  as prefix, where  $C_i^S = (W_i, \mathbf{wa}_i, \mathbf{Dass}_i^S)$ , and to prove that a node  $n_j$  in  $W_i$  can have an empty input dataset  $D_{n_j}$  to claim that there exists an execution that deadlocks in CW.

#### C.6 Proof of Theorem 2

**Theorem 2**: Let CW be a complex workflow, in which tasks do not use SQL difference. Let  $D_{in}$  be an input dataset, and  $\mathcal{D}_{in}$  be an FO formula. Universal termination of CW on input  $D_{in}$  is in co - 2EXPTIME. Universal termination on inputs that satisfy  $\mathcal{D}_{in}$  is undecidable in general. It is in

- $co-2EXPTIME \text{ (in } K \text{, the length of runs) if } \mathcal{D}_{in} \text{ is in } \forall \text{FO}, co-3EXPTIME$ if  $\mathcal{D}_{in}$  is  $\exists \text{FO or BSR-FO}$ 14
- $-co n_{in}$ -fold-EXPTIME, where  $n_{in} = |\mathcal{D}_{in}| + 2^{K}$  if  $\mathcal{D}_{in}$  is in SF-FO.

*Proof.* Complex workflows terminate iff they have bounded recursive schemes, and if they do not deadlock. Condition i) can be verified in  $O(|\mathcal{T}_{cx}^2| + |\mathcal{R}|)$  (see proposition 5).

If CW is recursion free, then condition ii) can be verified non-deterministically by guessing a symbolic execution  $C_0^S ldots C_k^S$  of length at most  $3.K_{\mathcal{T}_{cx}}$ . If this execution deadlocks, then there is an execution of CW that does not terminate, and we can safely conclude that CW does not terminate universally (for any input). Absence of deadlocks can hence be checked in EXPTIME.

If this execution contains a potential deadlock at symbolic configuration  $C_i^S$ , 25 then  $C_i$  is a configuration from which a particular dataset D must be used as input 26 by a task, and must be empty to cause a deadlock. Before concluding that  $C_i^S$  can 27 be a real deadlock, one has to check whether there exists an actual real execution 28  $C_0 \dots C_i$  such that property  $D = \emptyset$  holds at  $C_i$ . Emptyness of D can be encoded 29 as by a universal FO formula of the form  $\psi_i ::= \forall X, rn(X) \notin D$ . We can show 30 that the precondition  $\psi_{i-1}$  that needs to hold at  $C_{i-1}$  in order to obtain an empty 31 dataset D at step  $C_i$  are still of the form  $D' = \emptyset$  (hence expressible via an universal 32 formula) for some D' (this is the case if the move from  $C_{i-1}$  to  $C_i$  just adds a field 33 to D' to obtain D) or an FO formula in the universal fragment computed as the 34 weakest precondition  $wp[m_i]\psi_i$ . Then one can repeat the following steps at each 35 step  $k \in i - 1, i - 2, ...$  up to  $C_0^S$ : 36

- compute  $\psi_k = wp[m_k]\psi_{k+1}$ . We know that this weakest precondition can be computed, and that  $\psi_k$  is still an universal formula of size in  $O(r.|\psi_{k+1}|)$  (see proposition 1).

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- Check satisfiability of  $\psi_k$ . If the answer is false, then Fail: one cannot satisfy the conditions required to have  $D = \emptyset$  at step *i*, and hence there is no execution with signature  $C_0^S \dots C_i^S$  that deadlocks at  $C_i$ , the randomly chosen execution is not a witness for deadlock. If the answer is true, continue.

If the algorithm does not stop before step k = 0, then the iteration computes a satisfiable formula  $\psi_0$  of size in  $O(r^i)$ . It remain to show that inputs of the complex workflow meet the conditions in  $\psi_0$ .

Let us assume that the universal termination question is considered for a single input dataset  $D_{in}$ , one has to check that  $D_{in} \models \psi_0$ . As  $\psi_0$  is a universal formula i.e. is of the from  $\forall X, \varphi_0$ , this can be done in  $O(|D_{in}|^{|\psi_0|})$ . If the answer is true 10 then we have found preconditions that are satisfied by  $D_{in}$  and that are sufficient 11 to obtain an empty dataset in at configuration  $C_i$  in a run  $C_0 \ldots C_i$  that has 12 signature  $C_0^S \dots \overline{C_i^S}$ , i.e.  $C_0^S \dots \overline{C_i^S}$  witnesses the existence of a deadlock. Overall, 13 one has to solve up to  $i < 3.K_{\mathcal{T}_{cx}}$  satisfiability problems for universal FO formulas 14  $\psi_{i-1}, \psi_{i-2} \dots \psi_1$  of size smaller than  $r^i$ , and a model checking problem for input 15  $D_{in}$  with a cost in  $O(|D_{in}|^{r^{i}})$ . The satisfiability problems are NEXPTIME in 16 the size of the formula [28] whence checking satisfiability of  $\psi_{i-1}, \ldots, \psi_0$  has a 17 complexity that is doubly exponential in  $K_{\mathcal{T}_{cx}}$ . Considering that data fields are 18 encoded with c bits of information,  $D_{in}$  is a dataset of size in  $O(2^{r.c})$ . Hence, the overall complexity to check that  $C_0^S \dots C_i^S$  is a witness path that deadlocks is in 19 20 2 - EXPTIME.21

Conversely, if the universal termination question is considered for a several input 22 datasets described with an FO formula  $\mathcal{D}_{in}$ , one has to check that no contradiction 23 arises when requiring existence of an input  $D_{in}$  that satisfies both  $\mathcal{D}_{in}$  and  $\psi_0$ . This 24 can be done by checking the conjunction  $\mathcal{D}_{in} \wedge \psi_0$ . Now, this formula is of size in 25  $|\mathcal{D}_{in}| + |\psi_0|$ , and one can consider variables in  $\mathcal{D}_{in}$  and  $\psi_0$  to be disjoint. Standard 26 equivalence rules (miniscoping rules, see [37]) allow to rewrite this conjunction into 27 an equivalent formula in prenex normal form. If  $\mathcal{D}_{in}$  is in  $\forall FO$ , then  $\mathcal{D}_{in} \wedge \psi_0$  is in 28 ∀FO and we have a co-2EXPTIME procedure to verify its satisfiability. For frag-29 ments ( $\exists$ FO, BSR-FO),  $\mathcal{D}_{in} \wedge \psi_0$  fall is the class of BSR-FO or SF-FO formulas, but 30 with three alternations, with an NEXPTIME complexity of satisfiability, yielding a 31 triple exponential complexity. For  $\mathcal{D}_{in}$  in SF-FO, the complexity of the last step is 32  $n_{in}$ -fold exponential in the size of  $\mathcal{D}_{in}$ + the size of  $\psi_0$ . As for the unique input case, 33 if  $\mathcal{D}_{in} \wedge \psi_0$  is satisfiable, then  $C_0^S \dots C_i^S$  witnesses existence of a non-terminating 34 execution. 35

Hence, one can witness existence of a non-terminating run in  $O(K_{\tau_{cx}}.2^{r^{K_{\tau_{cx}}}} + C_{in})$  where  $C_{in}$  is the cost required to check satisfiability of  $\mathcal{D}_{in} \wedge \psi_0$ .

Last if  $\mathcal{D}_{in}$  is specified in an undecidable fragment of FO, then one cannot conclude whether there exists a legal input that satisfies  $\mathcal{D}_{in}$  and  $\psi_0$ .

### D Proofs for Section 6

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**Theorem 4 :** Existential and universal correctness of CW are undecidable, even when runs are of bounded length K. If tasks do not use SQL difference, and  $\psi^{in,out}$ is in a decidable fragment of FO, then 41 42

- existential correctness is decidable for CWs with runs of bounded length, and is respectively in 2EXPTIME, 3EXPTIME and  $2^{K}$ -fold-EXPTIME for the  $\exists FO, \forall FO, BSR, and SF fragments of FO.$
- universal correctness is decidable and is respectively in co 2EXPTIME, co - 3EXPTIME and  $co \cdot 2^{K}$ -fold-EXPTIME for the  $\forall FO, \exists FO, BSR, and$ SF fragments of FO.

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*Proof.* Let us first prove the undecidability part: It is well known that satisfiability of FO is undecidable in general, and in particular for the AE fragment with formulas of the form  $\forall \vec{X} \exists \vec{Y}, \phi(X, Y)$ . Hence  $\psi_{AE}^{in,out}$  can be a formula which satisfiability is not decidable. One can take an example of formula  $\psi_{unsat}$  which satisfiability is not decidable. One can also build a formula  $\psi_{id}$  that says that the input and output of a workflow are the same. One can design a workflow  $CW_{id}$  with a single final node which role is to return the input data, and set as client constraint  $\psi^{in,out} = \psi_{unsat} \wedge \psi_{id}$ . This workflow has a single run. Then,  $CW_{id}$  terminates properly iff there exists a dataset  $D_{in}$  such that  $D_{in} \models \psi_{unsat}$ , i.e. if  $\psi_{unsat}$  is satisfiable. Universal and existential proper termination are hence undecidable problems.

For the decidable cases, one can apply the technique of Theorem 2. One can 17 find non-determinisitically a symbolic run  $\rho^S$  that does not terminate and check that it is the signature of an actual run, or a symbolic run  $\rho^S$  that terminates and 19 check whether it satisfies  $\psi^{in,out}$ . 20

Let us first consider universal termination. Assume that CW terminates univer-21 sally, and select a symbolic run  $\rho^S=C_0^S\ldots C_n^S.$  We can then compute a chain of 22 weakest preconditions  $\psi_n, \psi_{n-1}, \dots, \psi_0$  that have to be enforced to execute success-23 fully CW and terminate in node n. In particular,  $\psi_n ::= true$ . Similarly, one can compute at each step, a weakest precondition  $\psi_i^{in,out}$  needed at step i so that  $\psi^{in,out}$ 24 25 holds. Intuitively,  $\psi_i^{in,out}$  describes the constraints between the initial dataset and 26 the output dataset "consumed" at stage i+1 in  $\rho^S$ . If at one stage,  $\psi_i \wedge \psi_i^{in,out}$ 27 is not satisfiable, then  $\rho^S$  is not the signature of an actual run of CW that termi-28 nates properly, and we have found a witness of non-proper termination. We have 29 assumed that  $\psi^{in,out}$  was specified in a decidable fragment of FO. As computing 30 the weakest precondition of a property in the existential, universal, BSR, SF frag-31 ment of FO gives a property in the same fragment, all  $\psi_i$ 's and  $\psi_i^{in,out}$ 's are in 32 a decidable fragment of FO. Then, the complexity will depend on the considered 33 fragment, and on the fragment of FO used to specify inputs. As for universal termi-34 nation, if inputs and  $\psi^{in,out}$  are specified with the universal fragment of FO, then 35 universal proper termination is in co - 2EXPTIME, and in co - 3EXPTIME36 for the existential fragment (as one may alternate  $\exists$  statements on outputs with  $\forall$ 37 statements inherited from obligation to prove non-emptiness of a dataset. Similar 38 remark and complexity holds for the BSR fragment (separation of variables main-39 tains an NEXPTIME complexity [37]). If  $\psi^{in,out}$  is in SF, then checking proper 40 universal termination is co - K - fold-exponential time, where  $K = r^{K\tau_{cx}}$ . 41

The proof and complexities for existential termination follow the same lines, 42 vielding 2EXPTIME complexity when  $\psi^{in,out}$  is written with the existential, 43 fragment of FO, 3 - EXPTIME complexity for when  $\psi^{in,out}$  is written in the 44 universal or BSR fragments (as checking satisfiability for a BSR formula is in NEXPTIME [28]) and K - fold-exponential for SF formulas [37].  $\Box$  2