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Visual Trajectories from Uncalibrated Stereo

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Abstract

This paper proposes a methodological framework for trajectory generation in projective space. The framework en-ables trajectories that respect rigidity constraints of structure and motion, that are furthermore uniform and optimal in terms of Euclidean configuration, eventhough no camera calibration is assumed.

In a projective reconstruction of the scene, obtained e.g. from an uncalibrated stereo-rig, the homography between corresponding feature points on a rigid object in different positions is employed to represent its spatial configuration. From its algebraic structure -it is similar to a rigid motion -decoupling of rotation and translation, and uniform interpolation of trajectories are derived.

Speaking in robotic terms, the merely point-to-point definitions of goals, as present in current approaches to visual servoing, are extended to a guarded motion along via points on complete-path trajectories which result from interpolation of a demanded type of motion. Translationonly, rotation-first, rotation-last task-functions are further explicited.

Introduction and motivation

Computer vision in robotics started as off-line system for part-or landmark-recognition, trajectory planning or mobile robot navigation, and computer-aided quality control. From the continuing increase in the capabilities of these systems and especially from the decrease of run-time towards real-time, the integration of computer vision into the on-line loop has become feasible. In consequence, the do-main of vision systems has extended to object detection, object tracking and pose estimation for the purposes of obstacle avoidance, target tracking, execution monitoring, and finally for position-based control. The respective control laws run an open loop which consists of successive but well separated stages, one for determining the position of the manipulator and one for correcting this position by actuator motions towards the control objective. These approaches are classified as "look-and-move" [6].

1.1 Closed-loop image-based approach

Further reduction of cycle time nowadays allows a full integration of dynamic visual sensor input into closed-loop feedback control [3]. In contrast to open-loop control, a closed-loop is less sensitive to inaccuracies in calibration, is robust to disturbances during execution, requires however careful design of its dynamics in order to ensure convergence and stability [12]. Indeed, such dynamic visual servoing systems have recently been developed. They are called "image-based", since the target is given merely in terms of images, e.g. by a set of image points, since the error-function is a distance between the current and the desired configuration of these image points, and since the control-law reduces this error by servoing a robot in closedloop mode without explicitely determining pose or spatial structure [5]. For these control-laws, local convergence and stability in presence of calibration errors has been demonstrated [2]. The principal deficiencies are that these approaches enable only point-to-point goals, that trajectories are not further confined, particularly that they are not optimal, that vanishing features due to occlusion or loss of focus often result in divergence, and that even in case of complete visibility convergence is guaranteed only locally. All these are consequences of the fact that rigidity of structure and motion is no longer ensured when

calculations are solely image-based. More figuratively, the straight-forward descend on the gradient of image error in P-controllers does not "look-ahead". So, either local minima might trap the controller before reaching the final goal or sudden changes in error due to occlusion or loss of focus cause divergence. Furthermore, trajectories induced by image-based gradient descend are neither physically valid nor optimal, i.e. they tend to deform structure by violating rigidity of motion and additionally fail to constrain motion to the shortest path towards the goal and direction of approach.

1.2 Generic task-functions

In this paper, we propose a method for complete-path goal definition and subsequent generation of optimal trajectories for image-based visual servoing. Although just weakly calibrated stereo-rigs are assumed, trajectories respect rigidity and guarantee shortest path-to-goal. At first, trajectories are calculated in projective space from a spatial reconstruction of the scene. They are later reprojected to the images

to serve as set-points for image-based control.

The investigated classes of complete-path trajectories

include translation-only, parallel-translation, rotation-first, rotation-last trajectories. A Cartesian-move mode in projective space should also be feasible. These occur quite often in pratice. For instance, the list of orders given by an operator in video-based telemanipulation constitutes generic robotic tasks that correspond to certain trajectory classes:

W



optical

Figure 1: Pin-hole camera model.

2.2 Intrinsic geometry

A canonical affine frame D is attached to the video-camera (CCD), such that the *u*-*v*-origin is the pixel origin, the *u*-axis is parallel to pixel columns, the *v*-axis is again parallel to image scan-lines, and the *w*-axis is parallel to the optical axis with unit length f in negative *z*-direction. Units on the *u*-and *v*-axis are in pixel of width $1/k_u$ and of height $1/k_v$. The transition from camera-frame C to video-frame D is by the affine transform A (Fig. 1).

$\gamma N = ATRT X$,

(1)

The deviation of the *u*-axis from orthogonality to *v* introduces a affine skew in the focal plane by k_{uv} .

2.3 Image projection

In *D*, normalization with γ yields affine space coordinates $[U, V, W]^{T}$ of *N*. Normalizing with γW results in image coordinates $[u, v]^{T}$ in pixel.



 $^{\mathbf{J}\mathbf{\otimes}}=\gamma ^{\mathbf{J}\mathbf{\otimes}}=\gamma W$

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•	grasp	object,	e.g.	fix,	load	part

 lift object. 	e.g.	car disassembly
----------------------------------	------	-----------------

- put-down object on table, e.g. surface mount
- insert peg into hole, e.g. plug in socket
- turn object, e.g. turn valve
- drag object, e.g. move heavy load
- parallel alignment of tool to target, e.g. driver to screw
- perpendicular alignment of tool and planar target, e.g. drill normal to surface
- angular alignment of tool and target, e.g. spray-can normal to surface

1.3 Outline

straight-line translation, observed by weakly calibrated cameras. Section 6 concludes with a discussion of the presented framework. The relevance of the preceeding results for visual servoing is demonstrated in section 5, which develops the continuous, uniform, complete path task-function for a including some consequences on the generation of point-to-point translations and R-T decomposition, both in a projective frame with known affine properties. representation of pure translations in a projective frame is investigated. An algebraic algorithm for translation-based affine auto-calibration follows in section 4, The paper is divided into six sections. After the introduction in section 1, some algebraic and geometric fundamentals are laid down in section 2. In section 3 the

Fundamentals

We will revisit this purely scalar relation between image coordinates and affine space coordinates in D in section

5. The usual formulation of perspective projection evokes now as a special case of the representation in the affine frame D, mainly because the u-v-plane is parallel to the

$$X = P \in X$$

× 2.1 Extrinsic geometry

οL・ TRT Euclidean camera-frame C is canonically attached to each camera, such that the origin of C coincides with the optical center, the z-axis co-The geometry of the scene is given in a world-frame of reference W and points X in W are in homogeneous coordinates W X = [X, Y, Z, 1]. A

0[**U**0 **V**0 - (Fig. 1). The displacement between world-and camera-frame is written as homogeneous transform TRT, which maps W-coordinates onto C- \circ incides with the optical axis, the x-y plane becomes the focal plane, parallel to the image plane, and the y-axis is parallel to image scan-lines coordinates: C X = TRT W X.

1vl

\ _u[**P**uv = 0 Øv 0 0 2.4 Projective reconstruction applying the infinity constraint to rectified coordiintrinsic parameters of the camera. nates $N = S \in M$ with $\mathbf{O} = -\mathbf{h}$, $\mathbf{O} = -\mathbf{h}$, $\mathbf{O} = -\mathbf{h}$, \mathbf{O} is the pixel where plane equation $\mathbf{O} = \mathbf{N} = 0$, so $\mathbf{O} = [0, 0, 0, 1]$ in the optical axis hits the image plane, and It is well know, that from at least two uncalibrated images and eight common points, a reconstruction of the scence in which reveals the forth ϕ w describes the affine coordinates. Projective coordinates of ϕ of follow affine skew between columns and rows of the CCD: the five from $[0,0,0,1] \quad S_E M = 0 \text{ iff } S_{E(4,\cdot)} \quad M = 0, \ (7)$

row $S_{\text{E}(4,\gamma)}^{T}$ of SE to hold the co-a freely chosen frame R of projective [4], [11]. They are however a projectivity SE placements, i.e. it is a	three-space $P(3)$ can ordinates of $\bigotimes \otimes$ in R . $\bigotimes \otimes$ rests fix under projective dis-be calculated eigenvector of any H^{T}
away from a Euclidean reconstruction in $W_V N = ASESE^{-1} X$,	
	$_{RT}$. Hence, its coordinates depend mainly on the projective frame in which the scene was reconstructed.
$\gamma N = HA M$, 2.7 Canonic representation	
where M is the representation of X in R and S_{ε} is a The so far arbit in a cano	rarily fixed Euclidean world-frame can be "Euclideanizing" homography $X = S_{\varepsilon}M$ constrained mical way, as it is done by the "Jordan canonical form" (JCF) of similar matrices. In case of a
2.5 Projective displacement, the similarity clas	writes as Consider now a set of k points X' on a rigid body and
let this body undergo a rigid displacement T_{RT} , such that	$\cos \phi = \sin \phi 00$
$X_{i}^{*} = TRT X_{i}$. Changing to projective coordinates	H_{RT} -1 $\sin \phi \cos \phi 00$
	$= V S_{RT} \Big 0 011 \stackrel{\clubsuit}{=} S_{RT}.$
$SE X = SE TRT SE SE Xi0 00$ $M' = \gamma HRT Mi(5)$	
$HRT = \gamma SRT \ JRT SRT$ shows that the Euclidean representation T_{RT} and the pro-where the chiral sector is of unit length in displace rate.	anonical frame is such that rotation is by an anjective representation H_{er} of one and the same z ment are related by a scaled algebraic similarity with Scalingtion. The x and travis are
	Т
as similarity transform (see also [13], [1]) nal in a plane perpendi	cular to the z-axis. This corresponds to representing H^{RT} in the frame of normalized screw- R^{T} = $P^{S} - T - S$. (6) $E - R^{T} - E$ motion, i.e. the origin is shifted to lie on the screw-axis,
whith the subgroup of projective whith the subgroup of projective whith the subgroup of projective whith the subgroup of the s	th then coincides with the z -axis, and scales are such
transforms, which are similar to a rigid displacement (Fig.	tt the screw-pitch is of unit-length (Fig. 3). The algebraic



A point is said to be "at infinity" iff its affine coordinates , The Jordan form is canonical up to permutations of the Jordan blocks.

Ч

fulfill $N = [U, V, W_i, 0]$. The set of all points at infin-Without loss of generality, we concentrate on the permutation as given ity form a "plane at infinity" $\mathbf{O}\mathbf{O}$, which is defined by the above.





Figure 4: Projective translation H_T , mapping points M_i ((onto $M_i(1)$. The eigenspace of the point-translation H_T spar the plane at infinity Π_{∞} , e.g., with the vanishing points of oc ordinate axis Δ_x , Δ_y , Δ_z as basis. The eigenspace of th

Π



dashed lines. Figure 3: Screw-geometry of a rigid displacement of a gripper (solid lines). The displacement in the original frame is drawn in dotted lines, the respective screw displacement in

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where γ is an arbitrary scale factor. S^T rectifies projective coordinates, such that translation is of unit length in z-direction.

pointwise the plane at infinity $\mathbf{\Phi} \mathbf{\Phi} = [0, 0, 0, 1]$, which is at the same time the eigenspace's orthogonal complement Algebraically J^{T} is characterized by $det(J^{T}) = 1$, $trace(J^{T}) = 4$, the quadruple eigenvalue $\mathbf{O} = 1$, and the dim = 3 eigenspace $E^{1} = [x, y, z, 0]^{T}$, which spans

\$♦

 $E_1 = 0$. From duality, the plane transformation corresponding to H^{T} follows as

$$=1/\gamma S^{\tau^{-\tau}\int_{0}^{0}1} \left[S^{\tau}, (10) \right]_{H^{\tau}}$$

Now, the dual eigenspace $\vec{E} = [x, y, 0, t]$ is the sub

space of planes parallel to the translation, including the plane at infinity, and the orthogonal complement $N \Leftrightarrow = [0, \frac{1}{2}, 1, 0]$ is the direction of translation

The translation direction is in the point eigenspace E_1 as well as the plane at infinity is in the plane eigenspace E

allows their calculation from a given HT. We will propose an efficient algorithm for doing so in section 4. Although they cannot be distinguished from any other vector of the eigenspace, their property of being orthogonal complement of the respective dual eigenspace

The similarity of H^{T} to J^{T} by S^{T} implies directly $det(H^{T}) = \gamma$, $trace(H^{T}) = 4\gamma$, a quadruple eigen-value $\diamondsuit = \gamma$, and a transformed eigenspace $E_{\gamma} = 0$

-1 S⊤

translation. Based on this, the geo-[x, y, z, 0]. Analogous arguments apply to the dual transform. In the following, we introduce a reduced parameterization for a projective

coordinate axis $\mathbf{\Phi} \mathbf{x}, \mathbf{\Phi} \mathbf{y}, \mathbf{\Phi} \mathbf{z}$ as basis. The eigenspace of the plane-translation H is spanned by the plane at infinity and Figure 4: Projective translation HT, mapping points Mi(0) onto Mi(1). The eigenspace of the point-translation HT spans the plane at infinity \mathbf{P}^1 , e.g. with the vanishing points of

Two planes parallel to the translation, e.g. $\diamond 1$, $\diamond xT$, $\diamond yT$ and the vanishing point of the translation $\diamond T$ is the intersection of these three planes

shown. to calculate the projective translation between a given point pair and the decomposition of a general projective displacement into rotation and translation is metric interpretations of the parameter vectors follow easily and a factorization-based algorithm for affine autocalibration of a stereo-rig is derived. Then, a way

of the complete object along a continuous-path, which yields a globally admissible task-function in the image domain. The uniform, shape-preserving interpolation of image trajectories and the incorporation of a-priori velocity profiles are finally developed. After that, the task-function of translational motion is explicited. The often found point-to-point definition of a positioning task is extended to a rigid translation

3.1 Reduced parameterization

plus an arbitrary scale factor. In the new form, the number of parameters of H^T reduces to eight, four of them are fix for all translations, the remaining four characterize the present translation,

After writing the columns/of S^{T} as *ci*, the rows of S^{T} as n', and separating the identity matrix *l*, equation (10) becomes:

$$H\tau = \gamma \Leftrightarrow S\tau^{-\tau} / I + \left[\left| \int S\tau \right| (11) \right] 0000$$

$$\int_{a} \int_{a} \int_{a$$

 r^{4} shows that r^{4} is a left

10

It obviously lies in the plane at infinity $Pi e^{r} N e = 0$. Its image PN e is called "focus of expansion" of the given translation.

direction, independant of their amplitude. More formally, σ is an eigenvector of H^{T} , which is evident by multiplying (12) from the right. shows that the column C3 appearing in (12) holds the projective coordinates Me of the vanishing point, which characterizes projective translations along this In the affine frame of (10), translation is along the z-axis and the vanishing point becomes $N = [0, 0, 1, 0]^T$. Going back to the projective frame R by ST

point-translation H^{T} , the plane at infinity μ is eigenvector of the plane-translation H. The eigenspace infinity, and the constraint places c^3 at infinity, i.e. it is the limit of all points translating in this direction. The vanishing point c^3 is eigenvector of the and a column of its inverse, respectively. They obey a single constraint $r^4 = c^3 = 0$. In geometric terms, c^3 is the direction of translation, r^4 is the plane at To sum up, a projective translation HT depends merely on a scalar factor V and two vectors 14 and C3, which appear as a row of the rectifying homography

and consists of all planes parallel to the translation, including the plane at infinity. T of HT is the plane at infinity and HT leaves all vanishing points unchanged. Dually, the eigenspace of H^{-r} is plane-wise fix

4 Affine calibration

4.1 The algorithm

weakly calibrated stereo system. In theory, affine calibration corresponds to determining the plane at infinity, which appears in H0 calculated like The relationship in equation (11) gives raise to a subspace method for affine auto-calibration of perspective cameras from one or more translation observed with a

$$H_0 = H_T / \gamma - I,$$
 (16)

by the components of *1*⁴. where $\gamma = trace(H^{T})/4$. In each row the plane at infinity r^{4} appears scaled by the components of c^{3} , and likewise the direction c^{3} appears in each column scaled

componentwise products (18\\is potentially unstable. In practice, an estimation H0 will be disturbed from fuzzy data and round-off errors. Straight-forward accumulation by componentwise sums (17) and

$$H_{0(i, 1)1}^{"} + H_{0(i, 1)1}^{4}$$

$$H_{0(i, 2)}^{I_{4}} = \Phi(17)$$

$$H_{0(i, 3)}^{I_{4}} + H_{0(i, 4)}^{I_{4}}$$

$$H_{G_{1}} \left[\int_{a}^{a} H_{G_{1}} \right]_{a}^{a} H_{G_{1}} \left[\int_{a}^{a} H_{G_{1}} \right]_{a}^{b} H_{G_{1}} \left[\int_{a}^{b} H_{G_{1}} \left[\int_{a}^{b} H_{G_{1}} \right]_{a}^{b} H_{G_{1}} \left[\int_{a}^{b} H_{G_{1}} \right]_{a}^{b} H_{G_{1}} \left[\int_{a}^{b} H_{G_{1}} \right]_{a}^{$$

in the same projective base. In practice, the calibration procedure is as follows: s different H^{T} estimates from various translational motions expressed

1. 1. Take *n* image pairs during arbitrary translations of the camera system and the scene.

2. 2. Calculate a projective reconstruction of the translating points in one and the same projective base for consecutive image pairs.





a concent of affine geometry hence the plane at infinity

M00000



$$H^{T} = I + - (26)$$

$$r^{4} M^{7} r^{4} r^{4} M^{7} r$$

the scene tion $H\tau$ is determined following section 4.2. The resid-Now, considering the calculated projective translation as a M1 = HRT M0. The corresponding projective translarobotic task, the whole object is moved rigidly in

7

obtain and contact, collision, or occlusion could be checked (Fig. ual displacement H = HRT HT is clearly the pro5). jective representation of a pure rotation HR. To

a rotation-first task, decomposition is $H^{\bullet} = H\tau HR\tau$ and $H^{\bullet} = HR\tau H\tau^{-t}$ for a rotation-last task. The condi-We will show how to decompose a projective displace-tion $Mt = H^{\bullet} Mt$ obviously holds, so the axis of rotation ment with respect to a central point, which moreover con-passes through Mt. strains the rotation axis to pass through it. One could think of generating rotation-first, rotation-last trajectories and a

transla at infinity permits calculating a projective transform which Cartesian-move mode. Isla as a sequence of one projective rotation *H_{R* and one pro-tional displacement. It furthermore enables to decompose as a sequence of one projective rotation *H_R* and one pro-tional displacement. It furthermore enables to decompose jective translation *H*^T (Fig. 6);} and rotation HR, whose axis is constrained to pass through the distin- $H_{RT} = H_R H_T(27)$ guished point. This is of particular importance in robotics, jective translation $H^{T}(Fig. 6)$:

be an ideal point robots' kinematics, e.g. the robot-wrist's center point, al-or an observed point - the destination M is calculated by lows to decouple the control-law as constraining the rotation to be around a point of the For a given center-point M^{0} – this might

5 The task of translation

defines a translational task. while orientation is defined by the order of Q(0) and Q(1). In addition, the reference point is not required to lie on the object itself, i.e. any pair of points only, taking an arbitrary via-point as Q(1) suffices and extrapolation yields the motion beyond this point. Noteworthy, \blacklozenge is an unoriented direction only. direction becomes $M \Rightarrow c^3$, according to (24). Distance and orientation are implied by the target point Q(1). If translation is to be defined by its direction its initial position Q(0), and in its target position Q(1), the corresponding projective translation H^{T} is determined by (26) and fully defines the task. The We are now considering a robotic task that consists of a uniform translational displacement of an object. Given the reconstruction of a point of reference Qin

5.1 Singleton set-point definition

Consider kpoints M on the object and their initial positions M(0) in the reconstruction. Compose the configuration matrix $S(\cdot)$

 $S(0) = M^{1}(0) M^{2}(0) \cdots M^{k}(0)$ (28)

which represents pose and shape of the object. Apply H^{T} to obtain the set-point configuration $S(1) = H^{T} S(0)$. Since H^{T} preserves rigidity, S(1) is, up to occlusion, an admissible configuration, i.e. corresponds to the image of the rigid object in the respective pose. The image configuration sand the image

set-points s^{\bullet} follow by simple backprojection
$s(0) = PS(0), s^{\bullet}(1) = PS^{\bullet}(1), (29)$
where <i>P</i> ls the projection matrix (3), that is available for each observing camera from the reconstruction step. So far, this corresponds to the usual task definition by "point-point-incidence", present in known approaches to visual servoing [3]. Neither trajectory, nor direction of approaching are defined. Unlike existing approaches, the definition of the task by the projective translation <i>H</i> ^T allows for the generation of multi-point set-points for an arbitrary rigid object. At the same time, the translation task <i>H</i> ^T can be calculated from any observed translation vector.
5.2 Complete-path task-function
The definition of the task given by the projective translation H^{T} now is extended to a continuous-path, uniform, straight-line translation. This completely constrains the trajectory and additionally the direction of approach. Having (10) in mind, the definition [10] of our continuous taskfunction $H^{T}(t)$ becomes
$H_{T}(t) = \gamma S_{T} \stackrel{-1}{\longrightarrow} S_{T}, t \not \gg [0, 1]. (30)$
loo 1 <i>t</i>
7 Please note that uniformity is with respect to spacial Euclidean distance, i.e. $H^{T}(t)$ corresponds to a <i>t</i> -fractile of the task's total distance. The formulation in (30) equally applies for moving backwards <i>t</i> <0, towards the set-point 0 < <i>t</i> <1, and beyond the set-point <i>t</i> >1. In contrast to simple interpolation of image set-points, rigidity is guaranteed at any <i>t</i> .
5.3 Uniform set-point interpolation
Thanks to the parameterization in (13), the calculation of $H^{T}(t)$ becomes a weighted linear interpolation between initial and final configuration $H^{T}(0)$ and $H^{T}(1)$ with the scale ratio γ
$H^{T}(t) = \gamma(l + tH^{0}) = \gamma(l + tH^{T}/\gamma - tl), = \gamma(1 - t) l + tH^{T}.$ (31)
Unless γ is respected, $H^{T}(t)$ is neither uniform, nor "rigid". The same holds for the interpolation of S^{\bullet} and s^{\bullet}

$$S'(t) = \gamma(1 - t)S'(0) + tS'(1), (32) s'(t) = \gamma(1 - t)s'(0) + ts'(1), (33)$$

reflect spatial distance. Moreover, the parameter t corresponds to relative Euclidean distance along the path. Purely image-based interpolation, in contrast, deforms the object and fails to rigid translation. This implies that at any the current set-point s (t) corresponds to an admissible pose of the object, which lies on the shortest path to the target. The singleton set-points S° and s° become a set-point function $S^{\circ}(t)$ and $s^{\circ}(t)$, the latter in homogeneous image coordinates. The trace of $s^{\circ}(t)$ coincides with the image lines connecting initial and target image points. The trajectory of $s^{\circ}(t)$, a dynamically varying set of kimage points, is however the projection of a uniform,

5.4 Velocity profiles

instance, depicts an initial acceleration until saturation, followed by a phase of constant velocity, and a final deceleration until complete set-point overlap S (1). parallel to the z-axis. Composing S (t) with the integral function of a desired "velocity profile" v(u) generates a set-point function of variable gain. Figure 7, for The dynamic formulation now allows to impose any velocity profile on the trajectory. Direct application of S(t): to [0,1] yields constant velocity translation More formally, let v(u): $u \not > [0,1]$ be the desired velocity profile. The resulting time-dilating function x is defined as

$$x(t) = 1/2$$
 $y(u) du$, with $s.t. x(1) = 1. (34)$

onto the direction of translation. Infact, this procedure corresponds to enrolling the velocity profile by integration, resulting in a one-dimensional trajectory over time, which is finally projected



Figure 7: Three-phase velocity profile v(u) and the time-dilation x(t).

6 Discussion and Conclusions

and from their transfer to the sensor-space. is assumed. Therefore, planning and generation of trajectories are moreless equivalent. In particular, no additional difficulty arises from trajectory generation the scence, without knowledge of the calibration parameters. In classic approaches to task planning, completely known Euclidean structure of the work-space In this framework we propose generating task-functions that correspond to complete-path trajectories solely and immediately from the visual information of

relationship is not accessible in an uncalibrated environment. figuratively, that a link between sensor-space and work-space is kept, that reflects as far as possible the implicit relations between both, as their explicit taken that the constraints resulting from observing a Euclidean world by a perspective visual sensor are respected by the generated task-functions, or more Unlike these approaches, the presented framework does without Euclidean scene structure, and does without a calibrated sensor. Hence, care has to be

6.1 A generated task

visual configuration of features and the geometric and kinematic configuration of tool and actuator have to be identified to the largest extend possible in an in terms of rigid motions of the object, articulated motions of the actuator, or Euclidean geometry of the scene. Thus, at any time the relationship between the the current visual configuration of the scene as input parameters (see Fig. 8). The specification of the above mentioned generic tasks is however thought to be visual taskfunction corresponds rather to transforming image information, such that the obtained task-function is a visual instantiation of a generic task, with uncalibrated setup. We distinguish generating a task-function from planning a task in the sense that no combinatoric search takes place, that no decisions are made. Generating a

some consequences and examples of determining the affine properties of the scene. However, the explicit step of affine reconstruction is avoided. phase" in the framework of visual trajectory generation. They sometimes require further knowledge about the scene structure. In this 8 report, we have given Apart from explicit task planning, the decomposition of observed displacements and composition from observed displacements is included as "construction



trajectory to reach the initial position of approach is generated. translation of twice the claw's edge is instantiated, which avoids an object collision during approaching. Finally, the present position of the gripper is taken and a rotation-first Figure 8: The instantiation of a generic grasping task. Starting from the object to be grasped, the gripper position can be transfered as shown in [5]. Subsequently, a pure

6.2 A plane at infinity

system-setup, rotation around a given center-point. An efficient algebraic method of motion-based affine auto-calibration was given, which nicely fits in the considered generate the projective translation between an ordered pair of points, and consequently to decompose a general projective displacement into a translation and a representation of rigid spatial motion. The identification of the plane at infinity introduces the concepts of parallelism and oriented directions. They allow to The affine properties of the scene have been proven to be of particular use in the construction and decomposition of projective displacements, the "uncalibrated"

i.e. controlled robot motions observed by a weakly calibrated stereo-rig.

trajectories in the sense of Euclidean configuration is achieved A further affine property are length ratios. They allow not just for the rigid interpolation of projective motion. Above that, uniformity of the corresponding

6.3 A complete path

image error are bridged. An additional contribution to globally convergent control of rigidly moving points. The interpolation of the path is of particular interest since potential local minima in usually point-to-point-wise defined functions of the It was demonstrated how to inter-and extrapolate projective motion to generate the complete-path of a rigid motion. Here, the path² consists primarily of the traces

globally convergent control. is that the path corresponds to motions with monotonically decreasing error in configuration. In conclusion, we consider a complete-path as a step towards "The ISO defines "path" as "... spatial locus drawn by the movement of any point on the robot or the workpiece, along which orientation of the end-effector may or may not be variable."

6.4 A uniform trajectory

trajectories are physically valid. varying set-points correspond at any time to an admissible configuration of the object, i.e. to a rigidly moving object in varying poses. Thus rigidity is preserved, whereas the path describes the swept trace of motion, only. Thus, the proposed interpolation of projective motion ensures that the reprojected, now dynamically The difference between a trajectory and a path is that the trajectory describes the progression of motion over time and the object's configuration at a time instant,

implicit calibration of and only of the currently instantiated visual task with respect to (relativ) error in configuration. functions. In other words, the visual set-points at t correspond to the tractile of distance in Euclidean configuration. One can also view this relationship as an Over and above that, the interpolation parameter t establishes an implicit relation between visual and Euclidean configuration, and the corresponding error

allows for optimizing with respect to dynamic properties, e.g. maximal acceleration, speed limits of the actuator [9]. actuator calibration [7], [8]. Furthermore, there is now an apparent connection between the gain in visual configuration and the gain in object configuration, which We consider the established relationship between visual and Euclidean configuration as a step towards weaker requirements on hand-eye and kinematic

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