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# BENCHMARKING FLEXIBLE ADAPTIVE TIME-FREQUENCY TRANSFORMS FOR UNDERDETERMINED AUDIO SOURCE SEPARATION

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#### **ABSTRACT**

We have implemented several fast and flexible adaptive lapped orthogonal transform (LOT) schemes for underdetermined audio source separation. This is generally addressed by time-frequency masking, requiring the sources to be disjoint in the time-frequency domain

We have already shown that disjointness can be increased via adaptive dyadic LOTs. By taking inspiration from the windowing schemes used in many audio coding frameworks, we improve on earlier results in two ways. Firstly, we consider non-dyadic LOTs which match the time-varying signal structures better. Secondly, we allow for a greater range of overlapping window profiles to decrease window boundary artifacts. This new scheme is benchmarked through oracle evaluations, and is shown to decrease computation time by over an order of magnitude compared to using very general schemes, whilst maintaining high separation performance and flexible signal adaptivity. As the results demonstrate, this work may find practical applications in high fidelity audio source separation.

*Index Terms*— Time-frequency analysis, Discrete cosine transforms, Source separation, Benchmark, Evaluation

#### 1. INTRODUCTION

Our goal is to tackle the problem of *audio source separation* where the mixtures are *underdetermined* and *instantaneous*. In particular, we aim to estimate J>2 simultanously active sources when the number of mixture channels is two, according to the following model:

$$x(n) = As(n) \tag{1}$$

where  $x(n) = (x_1(n), x_2(n))$  and  $s(n) = (s_1(n), \ldots, s_J(n))$  are the mixture and source vectors respectively,  $A = (a_{i,j})$  is a  $2 \times J$  matrix with real-valued entries  $a_{i,j}$ , and the discrete-time index ranges as  $0 \le n < N$ . In most practical scenarios only x(n) is observed, and little or no information is known about s(n) or s(n) or s(n) (the *blind* case). In benchmarking contexts for algorithm evaluation we assume that both s(n) and s(n) are known (the *oracle* case; see Section 3).

We approach the problem of estimating s(n) in the underdetermined case using the principle of *time-frequency masking* [1,2]. This depends on the assumption that, after transforming x(n) by an appropriate linear, invertible time-frequency (TF) transform (for example, a short-time Fourier transform, STFT), we have at most

two sources active at each TF index m. Denote by  $J'_m$  the estimated number of active (non-zero) source coefficients at the TF index m. We assume that  $J'_m = 2$  as it has been shown that this gives better performance than the simpler  $J'_m = 1$  (binary masking) case [3, 4]. (Efficient source estimation under the general  $J'_m \leq J$  assumption is currently an open research problem.) Let  $X(m) = (X_1(m), X_2(m))$  be the transform of x(n), and  $x(n) = (x_1(m), \dots, x_{N-1}(m))$  be the transform of x(n).

Now we denote by  $\mathcal{J}_m = \{j : S_j(m) \neq 0\}$  the set of all  $J'_m$  sources contributing to X(m), and call it the *local activity pattern* at m. Equation (1) then reduces to a determined system at each m:

$$X(m) = A_{\mathcal{J}_m} S_{\mathcal{J}_m}(m),$$

where  $A_{\mathcal{J}_m}$  is the  $2\times J_m'$  submatrix of A formed by taking columns  $A_j$ , and  $S_{\mathcal{J}_m}(m)$  is the subvector of S(m) formed by taking elements  $S_j(m)$ , whenever  $j\in\mathcal{J}_m$ . Once  $\mathcal{J}_m$  has been estimated for each m we estimate the sources in the TF domain according to the following

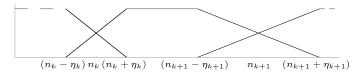
$$\begin{cases} \widehat{S}_{j}(m) = 0 & \text{if } j \notin \mathcal{J}_{m}, \\ \widehat{S}_{\mathcal{J}_{m}}(m) = A_{\mathcal{J}_{m}}^{-1}X(m) & \text{otherwise,} \end{cases}$$
 (2)

where  $A_{\mathcal{J}_m}^{-1}$  is the inverse of  $A_{\mathcal{J}_m}$  [2]. Finally, we invert  $\widehat{S}(m)$  to obtain the estimated source vector in the time domain  $\hat{s}(n)$ .

It has been shown that using *lapped orthogonal transforms* (LOTs) which adapt to the time-varying signal structures in the TF domain has the potential to yield sparser representations and superior performance compared to the commonly used STFT [3–7]. Inspired by MPEG audio coding, our scheme expands on previous work [7] by allowing the LOTs to adapt to the signal flexibly and by decreasing artifacts at window boundaries in order to improve separation performance, whilst drastically decreasing computation time. This work is useful in high fidelity applications, e.g., sampling musical sources in creative or compositional contexts, where the highest possible separation quality is often more important than real-time computation.

The rest of this article is structured as follows. In Section 2 we describe the adaptive LOT framework for fast and flexible TF transforms. Section 3 outlines oracle beenhmarking techniques for algorithm evaluation. We present experimental results for mixtures of three audio sources in Section 4 and discuss these results in Section 5. Finally, in Section 6, we conclude by outlining ideas for further work.

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**Fig. 1.** Schematic representation of window  $\beta_k^{\lambda}$ .

#### 2. ADAPTIVE SIGNAL EXPANSIONS

Adapting a LOT to the mixture channels  $x_i(n)$  entails forming an appropriate partition of their domain [0, N-1], that is, a finite set of ordered pairs

$$\lambda = \{(n_k, \eta_k)\}$$

such that

$$0 = n_0 < n_1 < \cdots < n_k < \cdots < n_{K-1} = N - 1$$
,

where K is the number of partition points. This segments the domain of  $x_i(n)$  into adjacent intervals  $\mathcal{I}_k = [n_k, n_{k+1} - 1]$  which should be relatively long over durations which require good frequency resolution, and relatively short over the durations requiring good time resolution. This is achieved by windowing  $x_i(n)$  with windows  $\beta_k^{\lambda}(n)$ , each of which is supported in  $[n_k - \eta_k, n_{k+1} + \eta_{k+1} - 1]$ , thus partly overlapping with its immediately adjacent windows  $\beta_{k-1}^{\lambda}$  and  $\beta_{k+1}^{\lambda}$  by  $\eta_k$  and  $\eta_{k+1}$  points respectively (see Fig. 1). These bell parameters  $\eta_k$  are thus subject to the constraint

$$n_{k+1} - n_k \ge \eta_{k+1} + \eta_k \,. \tag{3}$$

Previous work [3–6] imposed the constraint that  $\eta_k=\eta$  is constant across all  $k=1,\ldots,K-2$ , whereas we now relax that constraint by allowing the  $\eta_k$  to vary across k. Note that  $\eta_0=\eta_{K-1}=0$  and appropriate border modifications need to be made for this special case [8]. For every partition  $\lambda$  we form its associated windows according to the following function:

$$\beta_k^{\lambda}(n) = \begin{cases} r\left(\frac{n - (n_k - \frac{1}{2})}{\eta_k}\right) & \text{if } n_k - \eta_k \le n < n_k + \eta_k, \\ 1 & \text{if } n_k + \eta_k \le n < n_{k+1} - \eta_{k+1}, \\ r\left(\frac{(n_{k+1} - \frac{1}{2}) - n}{\eta_{k+1}}\right) & \text{if } n_{k+1} - \eta_{k+1} \le n < n_{k+1} + \eta_{k+1}, \\ 0 & \text{otherwise.} \end{cases}$$

where the *bell function* r(t) satisfies  $r^2(t) + r^2(-t) = 1$  for  $-1 \le t \le 1$ , r(t) = 0 for t < -1 and r(t) = 1 for t > 1, where t is real-valued and satisfies various regularity properties [8]. The bell parameters  $\eta_k$  and  $\eta_{k+1}$  determine how quickly the window monotonically rises on its left side and monotonically falls on its right side. Although there are many possible bell functions which satisfy these constraints, in practice we use a sine bell [8]. The local cosine basis associated with the interval  $\mathcal{I}_k$  is then given by modulating  $\beta_k^{\lambda}(n)$  by functions from a cosine-IV basis as follows:

$$\mathcal{B}_k^{\lambda} = \left\{ \beta_k^{\lambda} \sqrt{\frac{2}{n_{k+1} - n_k}} \cos \left[ \pi \left( m + \frac{1}{2} \right) \frac{n - (n_k - \frac{1}{2})}{n_{k+1} - n_k} \right] \right\}$$

where  $m \in [0, n_{k+1} - n_k - 1]$  is the discrete frequency index. This defines the basis  $B^{\lambda}$  for the orthogonal LOT, adapted to the partition

 $\lambda$ , for the space of signals of length N:

$$B^{\lambda} = \bigcup_{k=0}^{K-1} \mathcal{B}_k^{\lambda}.$$

This basis is only one of many possibilities. Since our aim is to find the 'best' basis, we will consider all admissible partitions  $\lambda \in \Lambda$  subject to some relatively lenient constraints, each of which determines a different orthonormal basis. Thus we obtain a *library* of possible cosine packet bases for this space of signals of length N:

$$\mathcal{L} = \bigcup_{\lambda \in \Lambda} B^{\lambda}.$$

### 2.1. Computing the Best Basis

To find that  $B^{\lambda} \in \mathcal{L}$  which gives the 'best' representation of some signal y(n), we aim to minimise its cost C(y), which should be inversely related to our separation performance criterion. We ensure that C(y) is an additive function, for example, the  $\ell^1$  norm [8] in a blind context (where  $y(n) = x_i(n)$ ), or an oracle benchmarking criterion (see Section 3). Past work involves restricting the set of admissible partitions to be dyadic so that each  $n_k$  is proportional to a power of 2 for all m, and also so that all bell parameters  $\eta_k = \eta$ , for k = 1, ..., K - 1, are the same [3,5,6]. This means that we can use computationally efficient, dynamic programming algorithms [8] to determine the best orthogonal basis with minimum cost C(y). On the other hand, this has two major restrictions. Firstly, constraining  $\mathcal{L}$  to admit only dyadic partitions means that the time-varying signal structures may not correspond well to any partition. Secondly, if  $\eta$ is small, which is often the case with previous dyadic partitioning schemes, then window artifacts will be more likely to occur in the estimated sources [5,9].

#### 2.2. Fast and Flexible Partitioning Schemes

To overcome these problems, we have developed several alternative partitioning schemes and associated algorithms, also based on dynamic programming [10, 11]. In previous work [7] we described a flexible segmentation (FS) scheme which admits all possible partitions  $\lambda$  with some 'resolution' L, so that if the signal length N is an integral multiple of L, then each partition point can be written as  $n_k = cL$  for  $c \geq 0$ , and where  $\eta_k$  is subject only to the condition (3). Provided that both L and N are powers of two, any library  $\mathcal L$  admitted by FS is a superset of the library admitted by the less flexible dyadic partitioning scheme.

Although FS gives excellent separation results in the oracle context, its library  $\mathcal L$  is very large due to a combinatorial explosion between the range of allowed interval lengths, interval onsets and bell parameters. Therefore, its computation time is very high. (For example, see Table 1.) As we wish to maintain flexible partitioning on the domain of the signal, yet decrease the time required for estimation of s(n), we are motivated by the corresponding ideas from the MPEG-4 AAC audio coding framework [12] and introduce the following partitioning schemes which call MPEG-like:

**Long-Short (LS)** We restrict the range of allowable partitions to admit intervals  $\mathcal{I}_k$  of only two lengths, that is, a *long interval* of length  $L_L$  and a *short interval* of length  $L_S = L$ , where  $L_L$  is an integral multiple of  $L_S$ , and we admit only bell parameters such that  $2\eta_k \in \{L_L, L_S\}$ . Apart from this restriction of interval lengths and bell parameters, there are no additional constraints, and LS is otherwise the same as FS.

Window Shapes (WS) This is equivalent to LS with the additional constraint that if  $\mathcal{I}_k$  is long, then at most one of  $\eta_k$  and  $\eta_{k+1}$  is short. In other words, the four different window shapes admitted (compared to five in LS) correspond to a long window  $(2\eta_k = 2\eta_{k+1} = L_L)$ , a short window  $(2\eta_k = 2\eta_{k+1} = L_S)$ , a long-short *transition window*  $(2\eta_k = L_L, 2\eta_{k+1} = L_S)$ , and a short-long  $(2\eta_k = L_S, 2\eta_{k+1} = L_L)$  transition window in the MPEG-4 framework.

Onset Times (OT) This is equivalent to LS with the additional constraint if any interval  $\mathcal{I}_k$  is long, then  $n_k$  must satisfy  $n_k = cL_L$  for some  $c = 0, \ldots, \frac{N}{L_L} - 1$ . Although this is equivalent to dyadic partitioning if  $L_L$  is equal to a power of two, it still admits variable bell parameters  $\eta_k$ .

WS/OT This scheme imposes both the WS and OT constraints simultaneously.

WS/OT/Successive Transitions (WS/OT/ST) This scheme imposes the WS/OT constraints in addition to disallowing adjacent transition windows, i.e., a transition window must be adjacent to a long window and a short window. This implements the windowing scheme used by MPEG-4, apart from the choice of the bell function r(t).

Even though the sizes of the libraries become significantly smaller as we impose more constraints, we expect that the MPEG-like partitioning schemes are nevertheless sufficiently flexible that benefits gained in computation time will outweigh any decrease in separation performance.

#### 3. ORACLE ESTIMATION

Oracle estimation allows us to judge the difficulty of estimating the sources s(n) from a given mixture x(n), and to gain insight into the upper performance bounds of our class of separation algorithms [4]. As it depends on knowing the reference source signals s(n) and the mixing matrix A it is intended to be used for algorithm evaluation rather than for practical (semi-)blind separation applications. The aim is to determine those  $\mathcal{J}_m$  and  $B^\lambda \in \mathcal{L}$  which give the best possible separation performance for every time-frequency index m, by minimising the following oracle performance criterion (cost function):

$$C(\hat{s}) = \sum_{n=0}^{N-1} \sum_{j=1}^{J} (\hat{s}_j(n) - s_j(n))^2.$$
 (4)

Minimising (4) is equivalent to maximising the *signal to distortion* ratio (SDR), given by

SDR [dB] = 
$$10 \log_{10} \frac{\sum_{n=0}^{N-1} \sum_{j=1}^{J} (s_j(n))^2}{\sum_{n=0}^{N-1} \sum_{j=1}^{J} (\hat{s}_j(n) - s_j(n))^2},$$

as has already been shown [4]. Moreover, minimising  $C(\hat{s})$  is equivalent to minimising at each m independently, by computing oracle local activity patterns:

$$\widehat{\mathcal{J}}_{m}^{\text{ora}} = \operatorname*{arg\,min}_{\mathcal{J}_{m} \in \mathcal{P}_{m}} \sum_{i=1}^{J} \left( \widehat{S}_{j}(m) - S_{j}(m) \right)^{2},$$

where  $\widehat{S}_j(m)$  on the right hand side is given by (2), and  $\mathcal{P}_m$  is the set of all possible activity patterns subject to  $J_m'=2$ . (As  $J_m'$  is small an exhaustive search over all  $\mathcal{J}_m \in \mathcal{P}_m$  is computationally feasible.) The best orthogonal *oracle* basis is computed by determining  $\widehat{\mathcal{J}}_m^{\text{ora}}$ 

Scheme	$L_L$	$L_S$	Av. SDR [dB]	Av. Time [s]	
FS	-	-	26.3	13183.0	
LS	$2^{10}$	$2^4$	24.9	256.3	
WS	$2^{10}$	$2^4$	24.8	185.6	
OT	$2^{10}$	$2^{9}$	23.8	44.9	
WS/OT	$2^{10}$	$2^{9}$	23.7	40.9	
WS/OT/ST	$2^{10}$	$2^9$	23.7	42.1	
FB	$2^{9}$	$2^{9}$	22.7	25.4	

**Table 1.** Results of oracle estimation. Where applicable, the values of  $L_L$  and  $L_S$  which correspond to the average best SDR are given.

over all  $0 \le m < N$ , for each  $B^{\lambda} \in \mathcal{L}$ , and selecting that  $B^{\lambda}$  corresponding to the activity patterns giving the highest SDR using dynamic programming techniques [10, 11].

#### 4. EXPERIMENTS AND RESULTS

We applied our methods to twenty mixtures in total, each of which had J=3 sources. Ten of the mixtures were music, ten were speech. To simulate a *panned mono* mixing process, we used the following instantantaneous mixing matrix:

$$A = \left( \begin{array}{ccc} 0.2125 & 0.9487 & 0.6430 \\ 0.9772 & 0.3162 & 0.7658 \end{array} \right).$$

The pitched sources in the musical mixtures were harmonically related so that overlapping harmonics between different sources were expected. To ease computation time, we downsampled from 44.1 kHz to 22.05 kHz, keeping a resolution of 16 bits per sample. Each source and mixture channel signal was of length 2<sup>18</sup> samples (approximately 11.9 s).

For each mixture, we performed oracle evaluations of s(n) for each of the LS, WS, OT, WS/OT and WS/OT/ST partitioning schemes (see Section 2.2), with  $L_L=2^c$ , where  $c\in[8,\ldots,11]$ , and  $L_S=2^c$ , where  $n\in[4,\ldots,9]$ . We exclude all long-short combinations with  $L_L\leq L_S$ . This means that short intervals range from 0.73 ms to 23 ms in length, and the long intervals' range is between 12 ms and 93 ms.

A selection of the results is given by Table 1, where each entry is the average over twenty different mixtures corresponding to a particular transform scheme with given block lengths. We compare the MPEG-like schemes to FS and the baseline fixed basis (FB) transform (where  $L_L=L_S$  and  $2\eta_k=L_L$  for all k). Table 2 gives a more extensive presentation for each of the MPEG-like transforms.

#### 5. DISCUSSION

From Table 1 we can see that as the partitioning schemes get more and more restrictive, performance naturally decreases due to their respective libraries becoming smaller. The question is, to what extent is this offset by improvements in computation time? Simply going from FS to LS (with no additional constraints apart from having long and short windows and their corresponding bell parameters) decreases average computation time from 3.7 h to 4.3 min, an approximately 98% improvement in computation time in exchange for a 1.4 dB decrease in average SDR. Blind and oracle performances evolve similarly across changes in interval lengths for adaptive dyadic and fixed basis partition schemes [6], so we expect that proportionally similar changes in computation time and performance

Scheme	$L_L$	$L_S$ and Av. SDR [dB]						
		$2^4$	$2^5$	$2^{6}$	$2^7$	$2^{8}$	$2^{9}$	
LS	$2^{8}$	22.8	22.6	22.4	22.0	-	-	
	$2^{9}$	24.5	24.4	24.2	23.9	23.7	-	
	$2^{10}$	24.9	24.7	24.5	24.4	24.4	24.2	
	$2^{11}$	24.0	23.9	23.8	23.8	24.0	24.0	
WS	$2^{8}$	22.7	22.5	22.3	22.0	-	-	
	$2^{9}$	24.5	24.3	24.1	23.9	23.6	-	
	$2^{10}$	24.8	24.6	24.4	24.3	24.3	24.1	
	$2^{11}$	23.7	23.6	23.6	23.6	23.7	23.9	
OT	$2^{8}$	21.4	21.5	21.5	21.6	-	-	
	$2^{9}$	23.0	23.0	23.1	23.1	23.3	-	
	$2^{10}$	23.2	23.2	23.3	23.4	23.6	23.8	
	$2^{11}$	22.3	22.3	22.4	22.7	23.2	23.6	
WS/OT	$2^{8}$	21.4	21.4	21.5	21.5	-	-	
	$2^{9}$	23.0	23.0	23.0	23.1	23.2	-	
	$2^{10}$	23.2	23.2	23.2	23.4	23.6	23.7	
	$2^{11}$	22.2	22.2	22.3	22.6	23.0	23.5	
WS/OT/ST	$2^{8}$	21.3	21.3	21.4	21.4	-	-	
	$2^{9}$	22.9	22.9	22.9	23.0	23.2	-	
	$2^{10}$	23.1	23.1	23.1	23.3	23.5	23.7	
	$2^{11}$	22.0	22.1	22.2	22.4	22.9	23.4	

**Table 2**. Full table of results for MPEG-like transforms. (Note that results for the FS transform do not appear in this table.)

would be experienced in the blind context with the considered new partitioning schemes. We emphasize that blind estimation typically yields around 12–13 dB for these mixtures [6] and that SDR improvements in the demonstrated range of 1–2 dB dB (in blind and oracle contexts) are significant in high fidelity applications.

As the WS scheme is identical to the LS scheme, apart from the relatively minor additional constraint of admitting only four different window shapes rather than five, it is not surprising that its performance is only 0.1 dB lower, yet it performs faster than the LS scheme by almost 28%. Indeed, this is also an acceptable tradeoff because the 'missing' window is a long window which tapers off with short bell parameters, and such relatively sharp tapers have to been shown to be undesirable, resulting in window border artifacts [5,9].

The OT, WS/OT and WS/OT/ST schemes further improve computation time, however as they are dyadic partitioning schemes, the ranges of results indicate that most of the difference in performance, compared to the FS, LS and WS schemes, is due to dyadic vs non-dyadic partitioning, rather than variation in bell parameters  $\eta_k$ .

Table 2 displays a couple of interesting trends. For the LS and WS schemes, i.e., those which do not impose dyadic partitioning, as  $L_S$  decreases for any fixed  $L_L$ , the average SDR tends to increase by several tenths of a dB. However, for the OT, WS/OT and WS/OT/ST schemes, the reverse is the case; as  $L_S$  increases for any fixed  $L_L$ , the average SDR slightly increases. This further supports our claim that obviating the dyadic partitioning constraint is the primary factor in improving performance.

#### 6. CONCLUSIONS AND FURTHER WORK

We have presented several different schemes for partitioning an audio signal in an adaptive LOT framework and suggest that the LS and WS schemes offer a good tradeoff between performance and computation time. The results highlight the performance advantages of

non-dyadic partitioning of the signal domain.

Further work involves investigating methods for finding the oracle basis for each source individually, rather than for for the mixture as a whole. We expect that this would further improve performance. This would increase the computational complexity of estimating the sources, and one possible approach to tackle this would be to apply efficient, suboptimal, heuristic search algorithms to find orthogonal bases using in a flexible segmentation scheme. Also, we wish to perform listening tests to determine subjective, perceptual differences between the different partitioning schemes.

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