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# Wing shape optimization using FFD and twist parameterization

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Optimization of wing shapes for aerodynamic performance is presented using a combination of particle swarm method and surrogate models. The wing shape deformations are parameterized using free form deformation together with wing twist. The developed strategy is applied to the lift-constrained drag minimization of Onera M6 wing.

**Keywords:** Particle Swarm Optimization, Free Form Deformation, Wing twist parameterization, Surrogate Models, Shape optimization

## 1 Introduction

Numerical shape optimization for aerodynamic problems can lead to improved designs than what is possible by conventional methods. Gradient-based optimization methods require the development of adjoint codes which can be a lengthy exercise and is also not very mature for RANS-based approaches. Furthermore, they may lead to locally optimal solution only, which is not desirable, especially in a preliminary design stage. Gradient-free methods are in this sense attractive and they also have the potential to give globally optimal solutions. The use of Euler/RANS codes for modeling the flow in a design context can be computationally expensive due to the need to evaluate many designs. However, the use of parallel computers and sophisticated surrogate models makes this feasible today.

A shape optimization exercise requires the development and coupling of several elements in an automatic chain. (1) A shape modeling system which converts the design variables into a shape. (2) A grid generation program that generates a surface grid and a volume grid. (3) A CFD solver, and (4) an optimizer.

A shape parameterization system typically involves a CAD tool which must be coupled to a grid generator. Every time the shape design variables are changed, a new grid has to be generated without human intervention. For complex problems and especially involving RANS models, fully automatic grid generation can be difficult or impossible. An alternative approach is

to use a reference shape, usually the starting design, and deform this shape by various techniques. Free form deformation approach falls in this class and is described in subsequent sections. It is necessary to generate a grid for the reference shape which is deformed whenever the shape is deformed, thus avoiding the need to re-generate the grid.

In the present work, we use Particle Swarm Optimization (PSO) method which is a gradient-free method. Surrogate models based on kriging are used to replace the expensive CFD evaluations. In order to construct the surrogate, an initial database of design points is generated and evaluated on the CFD model. This database is then enriched based on certain merit functions which balance the competition between exploration of design space and exploitation of the best solutions. The resulting algorithm is very efficient since it requires few CFD computations.

The rest of the paper describes the FFD technique, our implementation of wing twist as a design variable, optimization method and application of the developed methodology to the shape optimization of Onera M6 wing. In the paper, optimization results with FFD alone are presented, while results including twist variables will be presented in the symposium.

## 2 Free form deformation

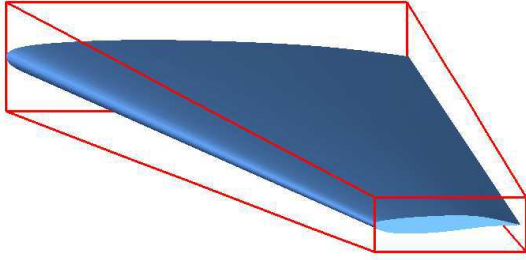


Figure 1: Example of FFD lattice (red) around a wing.

The FFD technique originates from the Computer Graphics field [9]. It allows the deformation of an object in a 2D or 3D space, regardless of the representation of this object. Instead of manipulating the surface of the object directly, by using classical B-Splines or Bézier parameterization of the surface, the FFD technique defines a deformation field over the space embedded in a lattice which is built around the object. By transforming the space coordinates inside the lattice, the FFD technique deforms the object, regardless of its geometrical description. An added advantage

is that the computational grid used for CFD can also be deformed simultaneously to conform to the new shape of the object; this procedure is also independent of the type of grid that is used, making it a very versatile method.

More precisely, consider a three-dimensional hexahedral lattice embedding the object to be deformed. Figure (1) shows an example of such a lattice built around a realistic wing. A local coordinate system  $(\xi, \eta, \zeta)$  is defined in the lattice, with  $(\xi, \eta, \zeta) \in [0, 1] \times [0, 1] \times [0, 1]$ . During the deformation, the displacement  $\Delta q$  of each point  $q$  inside the lattice is here defined by a third-order Bézier tensor product:

$$\Delta q = \sum_{i=0}^{n_i} \sum_{j=0}^{n_j} \sum_{k=0}^{n_k} B_i^{n_i}(\xi_q) B_j^{n_j}(\eta_q) B_k^{n_k}(\zeta_q) \Delta P_{ijk}. \quad (1)$$

$B_i^{n_i}$ ,  $B_j^{n_j}$  and  $B_k^{n_k}$  are the Bernstein polynomials of order  $n_i$ ,  $n_j$  and  $n_k$  (see for instance [5]):

$$B_p^n(t) = C_n^p t^p (1-t)^{n-p}. \quad (2)$$

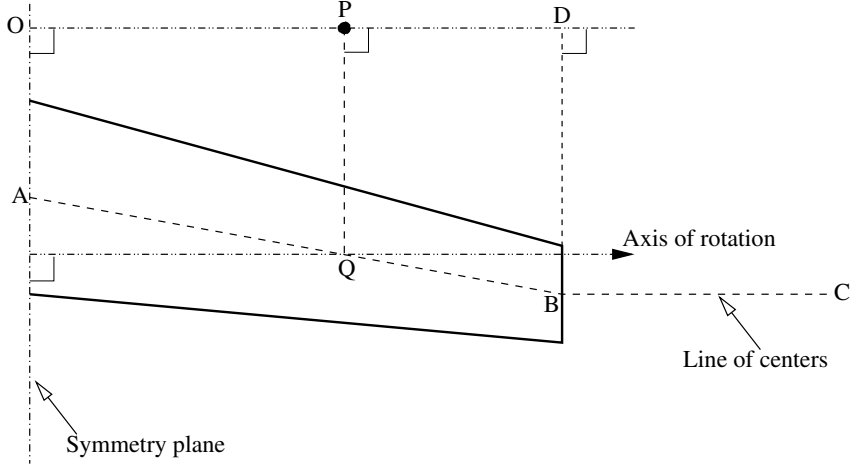


Figure 2: Definition of twist parameters for a swept wing

$(\Delta P_{ijk})_{0 \leq i \leq n_i, 0 \leq j \leq n_j, 0 \leq k \leq n_k}$  are weighting coefficients, or control points displacements, which are used to monitor the deformation and are considered as design variables during the shape optimization procedure.

For the aerodynamic optimization, the FFD lattice is built around the wing with  $\xi$ ,  $\eta$  and  $\zeta$  in the chord-wise, span-wise and thickness directions respectively. The lattice is chosen in order to fit the planform of the wing (see figure 1). Then, the leading and trailing edges are kept fixed during the optimization by freezing the control points that correspond to  $i = 0$  and  $i = n_i$ . Moreover, all control points are only moved vertically. Hence for a parameterization of  $n_i \times n_j \times n_k$ , we obtain  $(n_i - 1) \times (n_j + 1) \times (n_k + 1)$  design variables. In all the test cases in this work, we use  $n_j = n_k = 1$ ; this leads to a linear interpolation of the root and tip airfoil sections over the span.

### 3 Wing twist parameterization

The basic function of introducing wing twist is to induce a smaller angle of attack at the wing tip than at the root, known as washout. This leads to smaller induced drag and also prevents the wing-tip from stalling first, which can be undesirable from stability point of view. Moreover, by adding wing twist as a design variable, we can change the effective angle of attack of the wing which is very useful in lift-constrained drag minimization problems, since it is the angle of attack which has a major influence on lift. Twist can be parameterized as the solid body rotation of all the mesh points about a center and an appropriate axis of rotation. Axis of rotation ( $\vec{n}$ ) can be arbitrarily chosen depending upon the orientation of the geometric model. In the present work, unit vector perpendicular to the symmetry plane of the wing is chosen as the axis of rotation.

Line of centers is the locus of all the centers of rotation. It may be divided into two or more line segments depending upon the shape of the wing. For example, for a double delta wing, the line of centers will be composed of three segments, two inside the wing and one on the outside going upto the outer boundary. In the present work, only a simple swept wing is considered and hence the line of centers ABC consists of two line segments as shown in figure (2): segment AB starting from root section and ending at the wing tip, and the other segment BC starting from

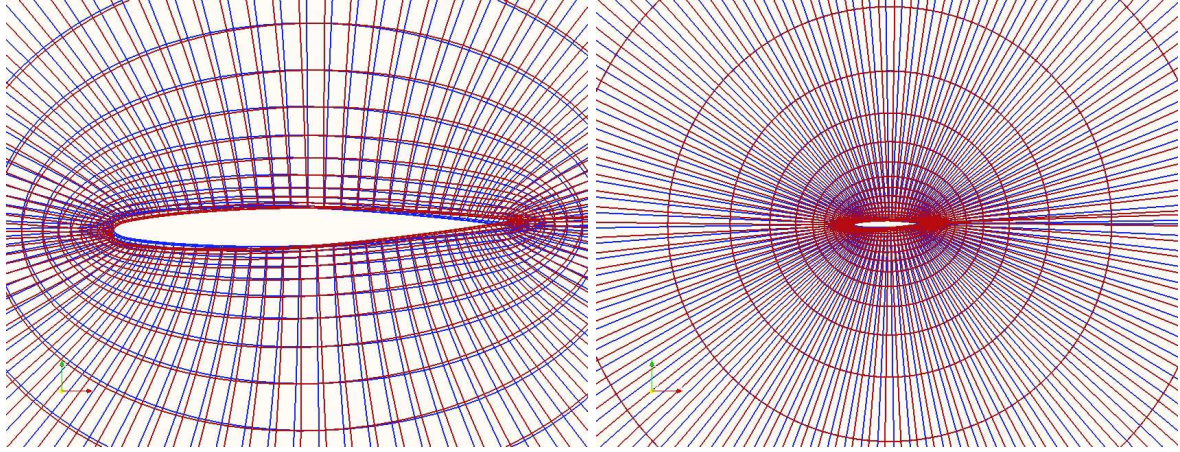


Figure 3: Grid in a plane perpendicular to the wing span: initial grid (blue) and grid after twist (red)

the wing tip and continuing till the outer boundary of the mesh in the direction of the axis of rotation. The location of the centers can be based on quarter-chord points or mid-chord points, this choice being controlled by the user through an input file.

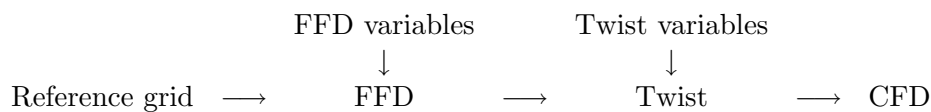
Any point P is rotated about the point Q which is obtained by projecting P onto the line of centers ABC. The angle of rotation is parameterized as

$$\theta(s) = (1 - s)\theta_0 + s\theta_1 \quad (3)$$

where  $\theta_0$  and  $\theta_1$  are the angle of twist at the wing-root and the wing-tip respectively while  $s \geq 0$  is defined as  $s = OP/OD$  with OD being parallel to the axis of rotation. It is also easy to use a higher degree polynomial to parameterize the rotation angle. Note that if Q lies between AB then  $s \in [0, 1]$  while if it is on BC we have  $s > 1$ .

In order to test the twist implementation, we take the case of Onera M6 wing at  $M_\infty = 0.84$ ,  $\alpha = 3.06$  deg. on an inviscid structured grid. A linear twist variation with  $\theta_0 = 0$  and  $\theta_1 = 3$  deg. is used. This causes the wing to pitch down at the tip leading to a reduction in the angle of attack. The initial and rotated grids are shown in figures (3) which shows a smooth grid even after twist. The grid rotation extends upto the outer boundary with an increasing amount of rotation; however since this rotation leads to a smooth deformation it does not degrade the quality of the grid. The flow was computed over the initial and twisted shapes and the pressure contours are shown in figure (4). After twist, the shock strength has been reduced due to the reduction in angle of attack; the lift and drag coefficients decrease as expected indicating the correct effect of wing twist.

The use of FFD and twist parameterization in shape optimization will be effected as a composition of two shape deformations. The reference shape will be first deformed using FFD as explained in the previous section; then the shape will be twisted as detailed in this section. The resulting grid can then be analyzed by the CFD solver. This is schematically illustrated below:



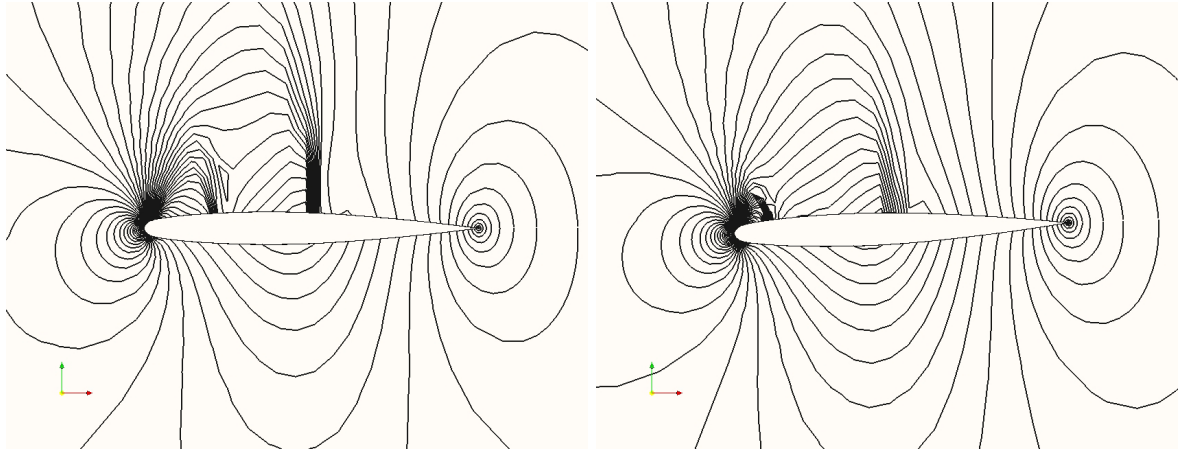


Figure 4: Pressure contours on initial grid (left) and twisted grid (right)

## 4 Surrogate-based PSO

PSO is modeled on the behaviour of a swarm of animals when they hunt for food or avoid predators [6]. Consider the problem of minimizing a function  $J : D \subset \mathbb{R}^d \rightarrow \mathbb{R}$ . A swarm of particles wanders around in the design space  $D$  according to some specified velocity. The position of each particle corresponds to one set of design variables and it has an associated value of the cost function. Each particle remembers the best position i.e., having smallest function value, it has discovered in its entire lifetime (local memory) and also knows the best position discovered by its neighbours and the whole swarm (global memory). The velocity of each particle is such as to pull it towards its own local memory and the global memory of the swarm. Thus the motion of each particle is a compromise between exploring local regions of design space and the region around the global best solution. The particles cooperate in the sense that they all share the information of the global memory and this leads to efficient search for the optimum. While there are many variants of the PSO algorithm, the one we use is described in [4].

PSO is a global search method and has slow convergence property, typically requiring several thousand CFD computations for a realistic problem. In order to reduce the computational cost of PSO, the costly analysis tool (CFD) is replaced with a surrogate model  $\tilde{J}$ . The optimization algorithm is applied to the metamodel  $\tilde{J}$  to predict a better solution. However this cannot be a one-shot process since the metamodel is an approximation, usually very coarse, and the optimum solution predicted by minimizing it may not really be the optimum and/or may not satisfy the constraints. The metamodel must be updated by adding new data points and the optimization applied to the new model. This process is continued until some convergence criterion is satisfied or the computational resources are exhausted. The selection of the new evaluation points is the most crucial aspect of this method. New points must be added in those regions of the design space where there is more likelihood of the existence of an optimum. This is achieved by selecting the new evaluation points as the minimizers of the merit function(s), which are described in [8] together with a complete description of the algorithm.

The surrogate model is built using kriging [8], which not only gives an estimate  $\tilde{J}$  of the exact function  $J$  but also gives an estimate of the error or standard deviation  $\tilde{s}$  in the estimated value. Where the model is less accurate, perhaps due to sparse data, it will predict a large value of  $\tilde{s}$ .

Torczon et al. [3] and Cox and John [2] suggested the use of the lower confidence bound of the prediction as a merit function defined as

$$f_M(x) = \tilde{J}(x) - \kappa \tilde{s}(x) \quad (4)$$

The merit function is minimized and the new evaluation point is the minimizer of the merit function. Several merit functions with different values of  $\kappa$  are minimized which gives a set of new evaluations points. A small value of  $\kappa$  leads to searching around the current minimum of the metamodel. A large value of  $\kappa$  may be expected to give a good estimate of the lower bound of the cost function and leads to better exploration of the search space where the data is less certain or non-existent. According to [1], in practice using four different values of  $\kappa = 0, 1, 2, 4$  is sufficient. In this case, in each optimization iteration, four CFD computations have to be performed and the results added to the database.

## 5 Optimization of Onera M6 wing

The standard Onera M6 wing at transonic flow conditions ( $M_\infty = 0.84$ ,  $\alpha = 3.06$  deg.) is taken as a test case for optimization. An inviscid, finite volume solver [7] based on multi-block, structured grids, Roe fluxes and MUSCL scheme is used to compute the flow, which contains a lambda shock on the upper wing surface as seen in figure (6). The optimization problem is:

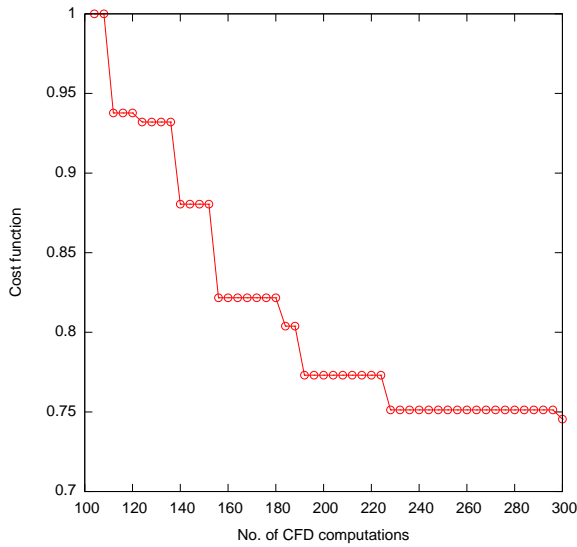


Figure 5: Convergence of optimization iterations

about 25% while the constraints are satisfied. Figure (6) shows that the shock has been considerably weakened as a consequence of shape optimization and this is reflected in reduced drag.

Near the wingtips, the pressure contours show that the shock is still considerably strong. The result can perhaps be improved by including wing twist also as a design variable, which is an ongoing work.

$$\min \frac{C_d}{C_{d_0}} \quad \text{subject to} \quad C_l = C_{l_0} \quad \text{and} \quad V = V_0$$

where the subscript "0" refers to the M6 wing,  $C_d$  is the drag coefficient,  $C_l$  is the lift coefficient and  $V$  is the wing volume. The constraints are enforced by using a penalty function approach. The grid used for CFD consists of  $41 \times 51 \times 201$  nodes with  $35 \times 201$  nodes on the wing surface. The FFD parameterization is of size  $5 \times 1 \times 1$  which leads to 16 design variables. An initial database of 100 design points generated in  $D = [-0.05, +0.05]^{16}$  by latin hypercube sampling is used for constructing the initial database. In each optimization iteration, four merit functions are minimized corresponding to different values of  $\kappa$ . The convergence of the cost function is shown in figure (5); we see that the drag is reduced by

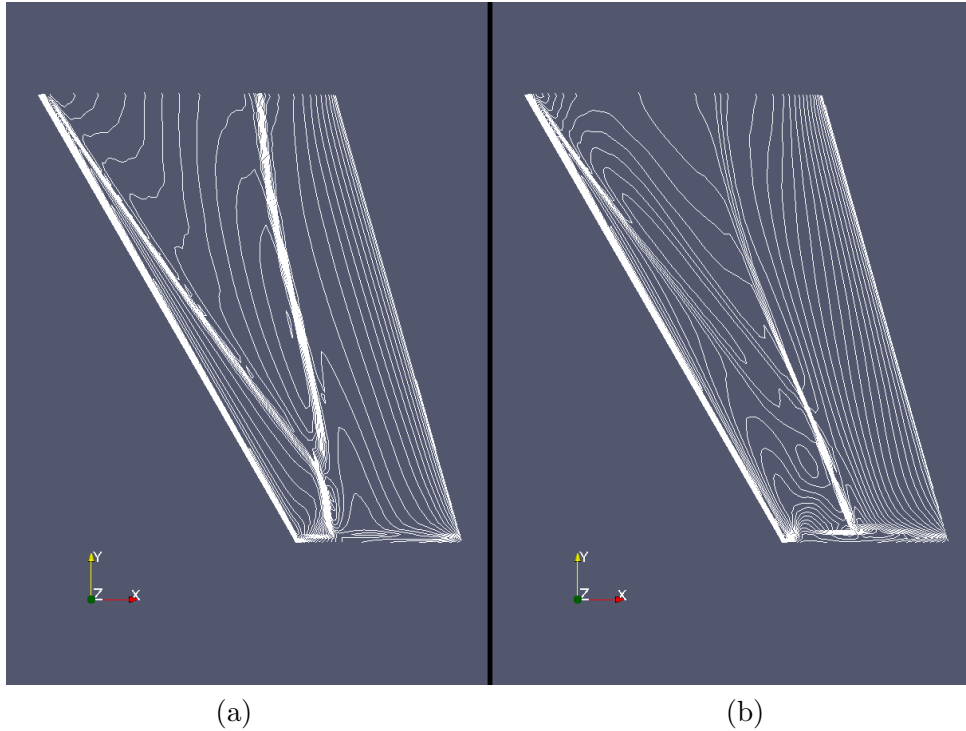


Figure 6: Pressure contours for (a) Onera M6 wing and (b) optimized wing

## 6 Summary and conclusions

A shape optimization framework for global optimization using PSO, surrogate models and FFD is presented. For wings, twist is an important design variable and a strategy is developed for incorporating it together with FFD. The current results with FFD alone show good performance of the optimization tool at a reasonable computational expense in terms of the number of CFD computations required (about 220 in this case), with a 25% reduction in drag coefficient, while the lift and volume constraints were satisfied. We hope to improve the results by using twist also a design variable and the results will be presented in the symposium.

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