Practical Volumetric Sculpting

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Abstract

We present here a *sculpture metaphor* for rapid shape-prototyping. The sculpted shape is the iso-surface of a scalar field spatially sampled. The user can deposit material wherever he desires in space and then iteratively refine it using a freeform tool. The tool shape can be designed inside the application. The tool can add, remove, paint or smooth material, or it can be used as a stamp to make prints on an existing shape. The user can move the scene and/or the tool with a Spacemouse (6D input device), or a 2D mouse using virtual trackball. We also focussed on the rendering quality, exploiting lighting variations, and environment textures that simulate high quality highlights on the surface. Both greatly enhance the shape estimation, which is in our opinion a crucial step during the design process. We also explored some stereo configurations to improve the user's perception of the spatial relationships between the elements of the scene.

Our current implementation based on GLUT allows the application to run both on UNIX-based systems, such as IRIX and Linux, and on Windows systems. We obtain interactive response times, strongly related to the size of the tool. The performances issues and limitations are discussed.

1 Introduction

The general context of our work is 3D freeform design. We deliberately chose a *sculpture metaphor* based on iso-surfaces over a sampled scalar-field.

We propose here a simplified classification based on some major/most recent contributions that came to our knowledge. This classification helps us to present the choices we made, and places our approach in the context of freeform modeling.

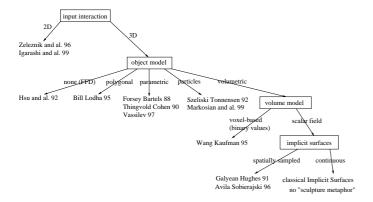


Figure 1: Proposed simplified classification of approaches to rapid prototyping of $3\,D$ -shapes

The first distinction we make concerns the input device used. One possible approach to designing 3D shapes is to use 2Dinput devices, such as a classical mouse or a pen to draw strokes on a screen, and then deduce plausible 3D shapes fitting these silhouettes strokes. Some interesting approaches have been conducted such as the SKETCH system[20] that enabled rapid shape construction using simple primitives (boxes, spheres, cones) that are combined with CSG-like operations and positioned with gestures. This was recently extended with the Teddy system[10] which uses freeform strokes to deduce 3D polygonal model and then simple gestures to extrude, smooth, cut or deform (bend) it. These approaches are very appealing both because of their close relation to the pen and paper interaction, which is natural when roughly sketching ideas in early stages of design, and because of their simplicity in software interface (no sliders, buttons, confusing options) and in hardware interface (simply a pen).

Nevertheless, we preferred 3D input devices (also called *direct* or 6D input devices), as we believe it allows a more precise control over the 3D shape. When considering more complicated devices, such as the Phantom force-feedback articulated arm, the device also allows to feel the surface being modeled, which greatly enhances the surface perception, and consequently its valuation.

The second distinction deals with the underlying model description, which also strongly conditions the range of possibly achievable objects. We only consider here approaches based on direct surface interaction. Free Form Deformation[9] is a powerful method to deform any kind of object. Mixed with a force feedback device[6], it leads to a convincing clay modeling metaphor. However, the serious limitation of this space deformation technique is that the user can not modify the topology of the deformed object. In the polygonal sculpture system proposed in [3], the user may alter the topology, but he has to specify the new connectivity at a triangle level. Moreover, when the user deforms the shape, detecting and handling its self-collisions become very intricate. Another interesting approach was initiated with Hierarchical B-Splines[7], that allowed to add details via overlays locally refining the shape. Intuitive spline manipulation was extended with physical simulation processes such as [16, 17]. But here again, topology changes, especially when auto-intersections occur, are very difficult to handle (and are not handled, to our knowledge). Volumetric models enable one to easily represent 3D shapes of any topology. However, building a sculpting metaphor from classical implicit surfaces seems difficult. Indeed, these surfaces are usually defined as the blending of elementary potential fields generated by individual primitives. The number of these primitives greatly affects the field evaluation cost. Since iterative shape refinement is a key aspect of sculpting, a classical implicit representation would lead to a complexity explosion due to the increasing number of primitives.

In this context a representation of the field function as values stored in a grid seems much more appropriate. Then, whatever the number of editing operations, tri-linear interpolation always evaluates the field value in constant time.

We adopted here this representation, which was already studied in [8, 2].

This paper extends the tools shapes to freeform models that can be designed inside the application. It also proposes a new tool ac-

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tion which allows to use the tool as a stamp printing its shape on the virtual clay.

We also pay attention to the rendering quality, which greatly enhances the perception of the 3D shape, which is a crucial task in the design process.

We firstly describe our application from a user point of view. Then we describe our current implementation through a couple of how does it work sections: the first one dedicated to the potential field storage and update, and the second one dedicated to the tools shapes and actions. Finally, we detail our visual feedback, estimate our system performances on sample cases, and discuss future works.

2 Main features of the system

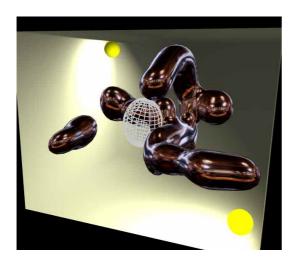


Figure 2: Sample snapshot of our sculpting application. The object being modeled is environment mapped. The tool is displayed in wireframe mode. The two yellow spheres represent the lights and a box representing the workspace is displayed.

Figure 2 shows a typical screen snapshot of our application. We display a box to delimit the workspace. This may also serve as a landmark for the user. This box can be modified to surround the sculpture, or hidden.

During a standard sculpting session the user selects which of the scene, tool or light he wants to move, and the device, either the mouse or the Spacemouse in our current implementation, he wants to use. It's possible for instance to use the mouse to rotate the scene, while controlling the tool's location with the Spacemouse, or the opposite.

The default tool is an ellipsoid which can be resized. It may be hidden, or displayed in transparent or wireframe mode. Its default action is *toothpaste*, which progressively deposits material in space. The user can edit its color, and the speed of the material deposit.

Other possible tool actions are *eraser*, or its progressive counterpart *soft eraser* that remove material in space. Identically, a *painter* and *soft painter* apply the tool color to the existing material. It's also possible to smooth an existing surface. Our particular implementation of these *classical* actions will be discussed in section 4.2. The tool can also be used as a stamp to locally deform a shape. As the user can also design his own tool shapes inside the application, he's able with this tool action to make a print on an existing shape simply by pushing the tool on the surface (see Figure 3) or by shifting the tool onto the surface (see Figure 4). Our implementation of this *printing* action will be discussed in section 4.3.

A crucial feature during the design process is surface appreciation,

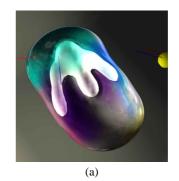




Figure 3: Using a tool designed inside the application as a stamp to make a print on a shape. (a) the tool is displayed in transparent mode. (b) the same view without the tool

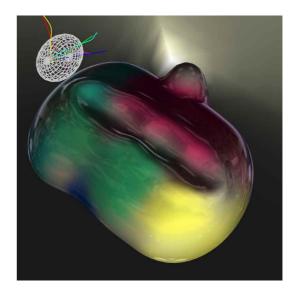


Figure 4: Print made by shifting an ellipsoidal tool

to verify at each modeling step that the resulting shape fits our intention. One possibility to perceive the surface shape is to use different lighting conditions. Here, the user can shift the lights to emphasize some shape features. He can make these light sources either move with the scene, i.e. remain fixed relatively to the sculpture, or move with the viewpoint. The user can also edit the lights color and the sculpture's specular properties. Though this direct shading may suffer from artifacts due to the surface triangulation (a well-known drawback of the marching-cubes process used to extract the isosurface), it enhances the perception of the sculpted shape. Another feature that helps the user to understand the surface's shape is environment mapping. The user can cycle through different modes: no environment texture, opaque texture, semi-transparent texture, and angle dependent transparent texture. An opaque texture completely masks the object colors, and gives it a metallic aspect. The transparent texture imitates a paint layer and gives the object a plastic effect. Both will be discussed in section 5.

The user can also exploit stereo rendering to further enhance his perception of the scene. Our current implementation enables him to use either a head-mounted display (iGlasses from Virtual-IO) or shutter glasses (Crystal Eyes from Stereographics). Our stereo settings will also be detailed in section 5. Though they are very simple at the moment, it greatly improves the scene comprehension.

Finally, it's possible during the sculpting process to save a screen snapshot, or export the triangulated surface as an Inventor object, or save the scene in an internal format which writes the whole field in a file.

3 Discrete potential field storage

We considered the physical size of the sampling grid directly implemented as an array[8, 18, 2] as a limitation: not only because it encloses the model and limits its extension, but also because it wastes memory storing irrelevant sample points where no potential field is defined. We decided to use here a dynamical structure to only store these *relevant* sampling points.

Hash-tables would have been very difficult to use because we have no *a-priori* knowledge of the spatial distribution of the points to store. So it would have been very difficult to design an efficient hash-key: getting closer to the worst case point retrieval would tend to a list-search, and would become very inefficient.

We decided to use balanced binary search trees which are less efficient than hash-table in best case, but have better operation time in worst case configuration.

We firstly describe our data structures, giving the aim of each structure. In section 3.2 we explain how we use these structure, i.e. how we update them and how they interact together.

3.1 Data structures: static description

We call these regularly spaced points that sample the potential field Corners. Each of them stores a potential field value, a color and some cached data, such as the field gradient, and the point location (to avoid its recomputation from the virtual grid indices and sampling steps). We call the balanced binary search tree we build from them Cornerstree. Corners possess a key, so that they can be compared to build the tree. The key we use is simply made up of the indices (i,j,k) of the Corner in the virtual grid implicitly defined by the regular space sampling. Two keys (i_1,j_1,k_1) and (i_2,j_2,k_2) are compared in lexicographical order, which means that we first compare i_1 and i_2 . If they are equal, we then compare j_1 and j_2 , and finally if j_1 equals j_2 , we compare k_1 and k_2 .

Each Corner having a value between an arbitrary minVal and maxVal (arbitrarily set to 0 and 3 in our case) is stored in the CornersTree. A corner whose value becomes less than minVal is removed from the tree and deleted. Values above maxVal are clamped to maxVal. When requesting the value of a Corner not present in the tree, the returned value is minVal.

This regular space sampling divides the space in cubical elements we name Cubes. In a similar manner, each Cube having at least one Corner defined is stored in a CubesTree. The key associated with each Cube is a triplet (i,j,k) that corresponds to the smallest Corner-key of the eight Corners defining it. A Cube is made up of:

- eight pointers to its Corners, one of which is non-null, at least.
- an index deduced from the value of its eight Corners relative to the iso-value, which encodes the Cube/iso-surface intersection configuration. This is a classical decomposition step from the Marching-Cubes algorithm[4, 11, 5].
- twelve pointers to edges.

The Cubes that intersect the iso-surface (depending on their index value) are also inserted into another tree which we call

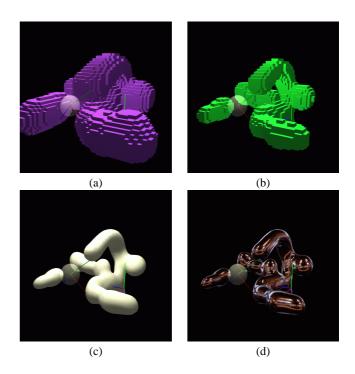


Figure 5: Visualization of some data structures elements: (a) shows all the cubes having at least one corner defined. (b) shows all the cubes that cross the iso-surface. (c) shows the extracted iso-surface. (d) uses environment texture to improve the shape perception

crossList. Figure 5.a shows all the Cubes contained in CubesTree; Figure 5.b shows the cubes crossing the surface (stored in crossList); Figures 5.c and 5.d shows the corresponding isosurface with different rendering modes.

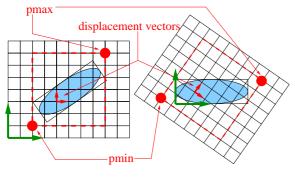
An Edge is created only to compute and store an intersection with the iso-surface. Edges are stored in another balanced binary tree, ordered with a key which is the concatenation of the two Corners keys forming the edge (with the smallest Corner key first to ensure uniqueness of Edge keys). The Edge keys comparison is again achieved in a lexicographical order.

3.2 Applying a tool: data structures update

When a tool is applied, we have to flush its modification in the CornersTree. To this end, we first compute the axis-aligned (grid-aligned) bounding box surrounding the local tool bounding box. Then, we have to walk through this box by:

- 1. transforming from world to local (tool) coordinate only the two extremum points of the box $(P_{min} \text{ and } P_{max})$ and the three displacement vectors (that move from one Corner to the next in each axis direction).
- 2. starting from the P_{min} point, we can reach the next point simply by adding its displacement vector to its current location, and similarly adding its counterpart displacement vector to its counterpart location in local (tool) frame coordinate (see Figure 6). Note that any scaling can be applied to the tool by applying the inverse scaling to the local location we just obtained

For each Corner examined during this walkthrough, we distinguish three cases (see Figure 7.a):



world coordinates

local coordinates

Figure 6: Parallel bounding box walkthrough is conducted both in world and local (tool) coordinates. Only the two points P_{min} and P_{max} , and the three axis-aligned displacement vectors are transformed from world to local coordinates.

- the Corner is in the world bounding box, but outside of the local bounding box. It can be very quickly rejected, since the bounding box containment is a very rapid test in the local frame coordinate. We call these Corners the visited Corners. They appear light grey in Figure 7.
- 2. the Corner is inside the local bounding box, but outside the tool's influence (i.e. the tool's potential field has a null contribution at this point). To identify this case, we must compute the tool's potential value for that point; we call them the computed Corners (meaning that we computed the tool's potential field, but finally the Corner wasn't modified). They appear in grey on Figure 7.
- 3. the last category concerns the Corners whose value was effectively modified. We call them the **dirtied** Corners because they have to be updated (cleaned). They appear in dark grey on Figure 7.

All these **dirtied** Corners are inserted into a temporary tree called modified.

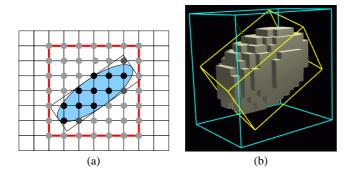


Figure 7: Applying the tool. (a) represents in 2D the virtual grid. Light-grey points represent the Corners **visited**. Grey points represents the Corners **computed**. Dark-grey points represent the corners **dirtied**. (b) shows the axis-aligned (blue) and oriented (yellow) tool bounding boxes. The cubes displayed are the Cubes which possess at least one Corner that has non-null contribution from the tool.

Each time a redisplay is needed, we successively extract (pop) every Corner from the modified tree. For each Corner, we

then have to update the eight Cubes that share it. To avoid multiple Cube examinations, we used either a timestamp-mechanism or another temporary tree to store only once each *dirtied* Cube.

To examine a Cube we compute the index (i.e. a bitmask deduced from the Corners value relative to iso). If the Cube doesn't cross the iso-surface, we're finished with it. If it crosses the iso-surface, its index corresponds to a surface crossing configuration in a precomputed table (classical part of the Marching Cubes process[4, 11, 5]). This configuration tells us which Edges of the Cube are intersected. The corresponding Edges are then updated.

When an Edge is updated (or created), the field gradients of its two extremity Corners are first (re-)computed (with a central difference scheme in our current implementation). Then, the intersection point is obtained by linearly interpolating each Corner attribute (such as the location, gradient and color) weighted by the corresponding potential field value stored. The interpolated gradient serves as surface normal (and is consequently sent to the graphic hardware).

3.3 Undo/redo handling

One key feature to encourage creative explorations is to allow multiple successive tries: the user can experiment whatever he desires without any consequence because he can always return to an earlier configuration.

We achieve the undo/redo process via temporary *undo-files*: each time a tool is applied, we dump all the modified Corners into a new *undo-file*.

In our current implementation, dumping a Corner corresponds to:

- 1. writing its indices in the virtual grid (i.e. the triplet (i, j, k) relative to an arbitrary origin, and an arbitrary step size, arbitrary meaning here semantically empty, as it has no physical meaning/size/dimension).
- writing its previous value and attributes (color only in our case, the other attributes such as the location and gradient are simply caches, and can be computed).
- 3. writing its new value and color after modification.

We arbitrarily limited the number of undo-files to 200. When more than 200 modifications are conducted, we cycle through the existing undo-files (restarting from the beginning). As the filesystems' caching are sufficiently efficient to achieve these dumps at interactive rates (both under IRIX6 and WindowsNT4), the real limitation to this undo/redo process is only disk space.

4 Sculpting tools

A tool is defined by:

- a **potential field**, that defines what we called the *tool contribution* in space. The tool bounding box is in fact the bounding box of this field. This potential field also indirectly (implicitly!) defines the tool's shape, which corresponds to an isovalue of the field.
- an action, that defines the way the tool's potential field is combined with the (possibly) existant object's potential field.

We will in the next section explain what are the possible shapes/potential fields for our tools, focusing also on a particular kind of tool we firstly used. In the next section, we go through the possible tool's actions. We describe how we implemented the classical tool (i.e. the actions already proposed in the previous approaches[8, 18, 2]). Then, we present our method to achieve local deformations that make prints on an existing object.

4.1 Tool shape

4.1.1 Ellipsoidal tools

During our implementation process, we first developed ellipsoidal tools. We simply used either a classical *Wyvill*[19] potential function or a box-shaped function to generate an isotropic (spherical) continuous field around the tool center (see Figure 8). A general ellipsoid is obtained by scaling the tool along its three axes. In

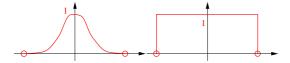


Figure 8: Continous field functions used for the ellipsoidal tool

this particular case, the shape displayed to represent the tool in the workspace is the limit of the influence region.

4.1.2 Freeform tools

We also used the freeform shapes generated inside our application as generalized tools. To achieve this, we duplicate the trees storing the corresponding discrete potential field. The surface displayed corresponds to the iso-surface, which is the same as the one visualized during its design process. The tool can also be scaled along the three axes of its local frame coordinate.

Since applying the tool requires the evaluation of its potential field between its samples' location, we *reconstruct* a continuous potential field by tri-linear interpolation inside the Cube the point falls into: as the Cube stores pointers to its Corners, we save time to retrieve their value (as we avoid the whole CornersTree search for each of the eight values).

4.2 Classical tool actions

The classical tool's actions are, similar to the concepts presented in [8, 2]:

- deposit material, which means that we add the tool's contribution to the (possibly) existing sample point (a Corner, for instance).
- remove material, either smoothly (which means that we substract the tool's contribution to the Corners) or not (which means that we delete all the Corners where the tool has a non-null contribution).
- paint material, again either smoothly or not, depending on if we take into account the respective field value of the Corner being examined to the tool's contribution, or not.
- smooth the shape being modeled, which is indirectly conducted via the local field smoothing. This corresponds to a low-pass filtering operation.

Our implementation of these various tool's actions is very similar to the previously proposed ones[8, 2].

4.3 Local deformation tool: use the tool as a stamp

Our aim here is to produce a visually convincing deformation while avoiding the computation cost and stability problems of a physical simulation of the material displacements. Our method is inspired from an approach developed for classical (continuous) implicit surfaces[13]. It consist in applying a negative field to compress the object in the area where another object penetrates, while creating a bulges to imitate material displacement around this area. The images in Figure 9 were obtained with our implementation of this method inside the iMAGIS-team implicit modeler: *Fabule*[15].

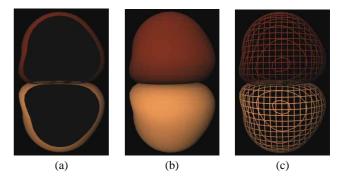


Figure 9:

Though we keep the same underlying ideas:

- 1. direct use of a bulging potential field to achieve *geometric deformations* without any physical simulation.
- 2. use the composite of the potential field of the colliding object (the tool in our case) and an *ad-hoc* deformation function to produce the bulging potential field.

we use a slightly different deformation function, and our use of discrete potential field allows us to obtain plastic deformations which were impossible with the original approach.

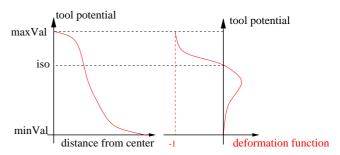


Figure 10: Deformation function principle. On the left, we see the tool potential generated by a spherical tool: this potential varies with the distance from the center of the tool. On the right, we see how the deformation function is mapped onto the tool's potential. Composing the two function relates the deformation function to the distance from the center of the tool.

Concerning the first point, our deformation function comes from simple intuitions: inside the tool, we should remove some material; outside the tool, we should add some material in order to imitate the real material displacement that occurs when a real tool collides with a block of clay. As this inside/outside knowledge is already encoded in the potential field (value greater than iso meaning inside in our case; the lower the potential value, the farther away from the iso-surface), we use the potential field of the tool as input parameter for our deformation function (see Figure 10).

The deformation function parameterization we are currently using appears in Figure 11 (see Figure 12 to identify parameters):

We then set parameter s to our iso-value, and control that the sum s+m+r doesn't bypass maxVal-minVal, otherwise the

$$def(v) = \begin{cases} if(v <= s) & -\frac{(s.k+2)}{s^3}.v^3 + \frac{(s.k+3)}{s^2}.v^2 - 1 \\ if(v <= s+m) & -\frac{(k.m+2.n)}{m^3}.v_0^3 + \frac{(2.k.m+3.n)}{m^2}.v_0^2 - k.v_o \\ & with: \ v_0 \longrightarrow v-s \\ if(v <= s+m+r) & -\frac{2.n}{r^3}.v_0^3 - \frac{3.n}{m^2}.v_0^2 + n \quad with: \ v_0 \longrightarrow v-s-m \\ if(v > s+m+r) & 0 \end{cases}$$

Figure 11: Equation of our deformation function

deformation function

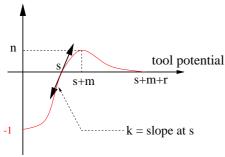


Figure 12: Tunable parameters of the deformation function

domain of definition of the deformation function becomes greater than the potential value variation: the deformation function would be truncated.

To sum up, we evaluate the contribution of a tool at a point P by first computing the value $v_{tool}(P)$ of the tool's potential field at P. The final tool's contribution is the composite of v_{tool} and def:

$$v_{deformTool} = def(v_{tool}(P))$$

Some results can be seen in Figures 3 and 4.

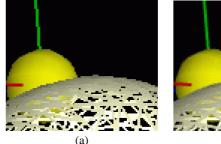
5 Visual feedback

With this test platform, we realized how crucial the visual quality is for the user's comfort, but also for the tool's position perception, and for the object's shape estimation.

One advantage of the *Infinite Reality* graphics card we use is its ability to antialias OpenGL primitives at *no cost* thanks to its hardware support of the multisample extension (see Figure 13).

We also tried some stereo rendering using some *Stereographics* shutter-glasses (*Crystal Eyes* model), and a *virtual-IO* HMD using interlaced rendering (*i-Glasses* model). Both are still in an early stage of development since we do not correctly handle the convergence/zero-parallax problem, and we do not track the head position. Even in this simple configuration, this proved very helpful for the tool placement in space.

Another feature which greatly enhances the shape perception is the use of environment textures that are *sphere-mapped* onto the object. We were first guided in that direction by some methods using textures to simulate high quality highlights. This reveals particularly useful if the surface had degenerated triangles(see Figure 14), which is a typical drawback of the Marching Cubes algorithm. We used classical sphere-mapping with adjustable transparency to be able to see the surface color under the texture layer. We also implemented simplified *ClearCoat*¹ like effect,



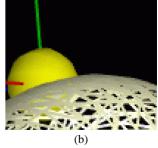


Figure 13: We see a close-up of a snapshot from our system. (a) without the multisample extension and (b) with.

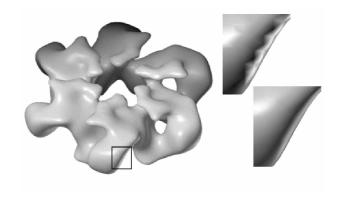


Figure 14: Sample shading artifacts due to the object triangulation, and a proposed solution based on textures to render high quality highlights of infinitely distant light sources (image from [12], pp.273)

i.e. simulating a paint layer, using a texture transparency varying accordingly to the incidence angle between the viewer and the surface.

6 Performances and Results

We obtain interactive response times without the need of any dedicated/specific volume rendering hardware. At the expense of reduced performance and visual quality (no *multisampling* antialiasing, and slower frame rates), our application also runs on a standard PC using OpenGL under WindowsNT.

Galyean[8] used grids from 30^3 up to 60^3 , while Avila[2] reports the use of grids up to 256^3 . Pfister[14] uses special purpose hardware based on his *Cube-4* ASIC to render a 256^3 volume with ray-casting up to 30 frames per second. Here the user is free to resize the workspace's box at any moment, and extend his model wherever he wants, providing *virtually unlimited* grid size. Since the field sampling is regular, two kinds of limitation appear in the current implementation:

 small tool: the sampling points become too distant relatively to the tool size. The tool isn't correctly sampled, and artifacts due to noise appear.

http://www.sgi.com/newsroom/press_releases/1998/september/clearcoat.html

¹information concerning SGI's ClearCoat product may be found at

 large tool: the tool covers so many sample points that their update is no longer possible at interactive rates.

We report in the following table some statistics concerning three differently sized *toothPaste* tools adding some material to the object represented in Figure 2. This object corresponds to 15,573 values stored and cornersTree, cubesTree and edgesTree of respective depth of 14, 16 and 13. The iso-surface displayed has 4,200 vertices and 8,392 triangles. The application runs on an SGI *Onyx2/IR* with 1Gb RAM and a 195MHz R10k processor. For each tool size, we report an average frame rate (wall-clock time) and some results concerning the number of corners and cubes covered in a *best* and *worst* case, depending of the tool's local bounding box orientation.

frames/s	#corners visited	#corners computed	#corners dirtied	#cubes
	visited	computed	airtiea	treated
19-23	216	125	93	184
small	1331	203	110	209
7-8	1452	887	501	751
medium	4352	975	508	771
3-4	2744	2197	1021	1424
large	8316	1919	1003	1407

This shows that as we are able to rapidly reject the corners lying outside of the local tool's bounding box, the tool orientation isn't affecting the field update performance.



Figure 15: Sample sculpture produced with one finger-shaped tool we built during a previous session. This was produced in less than ten minutes, during a debugging stage.

7 Future work

There are still some improvements to conduct concerning the visual quality, such as enhancing the stereo display, or adding some visual cues such as shadows (either with textures, or volumes) or depth of field.

Another key feature that will definitely improve the immersion of the application into reality is force feedback: a first idea was proposed by Avila[2, 1].

An important limitation in our current implementation is the fixed spatial sampling resolution of potential fields. At the moment, we

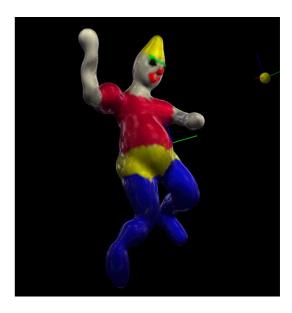


Figure 16: A clown character. He was entirely built using the ellipsoidal tool on an SGI O2 workstation. This was achieved in around one hour and a half including lots of trial and errors.

are planning to use octrees instead of binary search trees to store field values, but a multigrid approach also looks promising.

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²The GLUI User Interface to GLUT can be downloaded from http://www.cs.unc.edu/~rademach/glui



Figure 17: The same clown at an earlier stage

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Figure 18: Design of a new tool using the ellipsoidal tool



Figure 19: A more complicated shape modeled in less than a quarter of hour using the previously designed tool at different scales.

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