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Geometric Feature Extraction by a Multi-Marked Point Process

Florent Lafarge, Georgy Gimel'farb and Xavier Descombes

Abstract—This paper presents a new stochastic marked point process for describing images in terms of a finite library of geometric objects. Image analysis based on conventional marked point processes has already produced convincing results but at the expense of easy parameter tuning, short computing time, and unspecific models. Our more general multi-marked point process has simpler parametric setting, yields notably shorter computing times and can be applied to a variety of applications. Both linear and areal primitives extracted from a library of geometric objects are matched to a given image using a probabilistic Gibbs model, and a Jump-Diffusion process is performed to search for the optimal object configuration. Experiments with remotely sensed images and natural textures show the proposed approach has good potential. We conclude with a discussion about the insertion of more complex object interactions in the model by studying the compromise between model complexity and efficiency.

Index Terms—Object extraction, remote sensing, texture analysis, Stochastic models, Monte Carlo simulations.

1 Introduction

Probabilistic methods are now widespread in image analysis. They have proved to be powerful tools to solve inverse optical problems such as image segmentation or image restoration [1], [2]. Since the mid-nineties, many works have extended the initial pixel based approaches to the concept of object in order to deal with feature recognition problems. In particular, stochastic models have shown good potentialities in extracting rectilinear shapes. Generally, configurations of geometric objects are sampled from probability distributions defined in configuration space, Markov Chain Monte Carlo (MCMC) [3], [4] being one of the most popular families of samplers. In various application domains, from 3D reconstruction [5], [6] to texture modeling [7], [8], [9], the MCMC samplers are efficient for object extraction in large configuration spaces from any type of probability distributions.

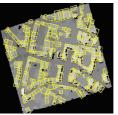
Stochastic models based on marked point processes are among the most efficient approaches and have already led to convincing experimental results in various image analysis applications such as extraction of buildings [11], road markings [13], vascular trees [14], road networks [12], tree crowns [10] or populations of birds [15]. The marked point processes, detailed in [16], exploit random variables whose realizations are configurations of geometrical objects, *e.g.* rectangles [11],

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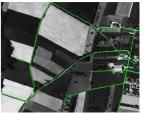


Fig. 1. Results of marked point process based models ©INRIA. Extraction of *(from left to right)* tree crowns [10], building footprints [11], and road networks [12].

[13], segments [12], [14], or ellipses [10], [15]. After a probability distribution measuring the quality of each object configuration is specified, the maximum density estimator is searched for by an MCMC technique based on the birth-and-death sampler [17] coupled with the conventional simulated annealing [18]. Such processes allow the description of complex spatial interactions between the objects. As exemplified in Figure 1, image representations produced by these stochastic models are particularly suitable for solving object recognition problems. However, these models have the following three drawbacks:

- Lack of generality: Each model is associated with only
 a specific application (in all the above mentioned
 works, a marked point process is limited to a single type of objects with simple geometric shape).
 Moreover, the complexity of interactions between
 the objects defined in the model makes it impossible to generalize each particular model to another
 application.
- Lengthy computational time: Although proposition kernels are developed to speed up the process, the birth-and-death sampler remains very slow, especially at low temperatures. For example, the result

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presented in Figure 1-center has been obtained in more than three hours on a 3 GHz processor.

• Trial-and-error parameter tuning: Many parameters (up to ten in most cases) are to be used to define the interactions. They are tuned by trial and error since parameter estimation techniques do not efficiently work with such large configuration spaces. This procedure is long and complex since a Monte Carlo simulation has to be used at each iteration of the tuning.

This paper proposes a new generalized marked point process called by extension a *multi-marked point process*. It provides results that approach by accuracy those obtained with models based on the conventional marked point processes [10], [11], [12], [13], [14], [15], but produces these results in a shorter time and can be applied to a large range of applications without changing the underlying model. Our proposal modifies the conventional marked point processes as follows:

- Joint sampling of multiple objects: The process must jointly sample different types of geometric objects (e.g. linear and areal objects such as segments and polygons) in order to extend the level of generality.
- Constrained object interactions: The interactions between the objects must be simplified and reduced to only the essential ones in order to (i) significantly decrease the number of tuning parameters, (ii) extend the level of generality by avoiding specific interactions, and (iii) use gradient descent based sampling.
- Introducing diffusion dynamics: Diffusion dynamics would allow a significant acceleration of the convergence. The conventional marked point process based models cannot use such a dynamics because the complexity of their probability distributions (usually gradients of their Gibbs energy (see section 2.2) do not satisfy the Lipschitz continuity condition [19]). The Jump-Diffusion processes introduced by Grenander *et al.* [20] represent a class of random samplers which efficiently combine both Monte Carlo techniques and diffusion dynamics.

This paper extends the work we presented in [21] by detailing both the multi-marked point process model and the optimization technique, as well as presenting new results and comments on various remote sensing applications and texture descriptions. The paper is organized as follows. Section 2 overviews the marked point processes and proposes their extension to the multimarked ones that deal with the different object types. Section 3 introduces a Gibbs energy model adapted to different types of geometric objects specified by a chosen mark library. The model is sampled by a Jump-Diffusion process detailed in Section 4. Experimental results for remote sensing and texture description problems are given in Section 5. Section 6 proposes a discussion about the insertion of more complex object interactions in the model by studying the compromise between model

complexity and efficiency. Basic conclusions are outlined in Section 7.

2 POINT PROCESSES AND MARKS

The marked point processes have been introduced in image processing by Baddeley and Van Lieshout [22], and developed and extended further in [16], [23], [24]. These stochastic models can be considered as an extension of conventional Markov random fields [25] such that random variables are associated not with pixel values but with geometrical shapes describing the image. An overview of marked point processes is provided below.

2.1 Point processes

Let X be a *point process* living in a continuous bounded set $K = [0, X_{max}] \times [0, Y_{max}]$ supporting an image. X is a measurable mapping from an abstract probability space $(\Omega, \mathcal{A}, \mathbb{P})$ to the set of configurations of points of K:

$$\forall \omega \in \Omega, x_i \in K, X(\omega) = \{x_1, ..., x_{n(\omega)}\}$$
 (1)

where $n(\omega)$ represents the number of points associated with the event ω . The *homogeneous Poisson process* is the reference point process. Let $\nu(.)$ be a positive measure on K. A Poisson process X with intensity $\nu(.)$ verifies the two following properties:

- For every Borel set $B \in K$, the random variable $N_X(B)$ defining the number of points of X in the Borel set B follows a discrete Poisson distribution with the mean $\nu(B)$, i.e. $P(N_X(B) = n) = \frac{\nu(B)^n}{n!} e^{-\nu(B)}$.
- For every finite sequence of non intersecting Borelian sets $B_1,...,B_l$, the random variables $N_X(B_1),...,N_X(B_l)$ are independent.

The Poisson process induces a complete spatial randomness, given by the fact that the positions are uniformly and independently distributed. Its role is analogous to Lebesgue measures on \mathbb{R}^d .

2.2 Density and Gibbs energy

Complex point processes introducing both consistent measurements with data and interactions between points can be defined by specifying a density with respect to the distribution of a reference Poisson process. Let us consider an homogeneous Poisson process with intensity measure $\nu(.)$, and let h(.) be a non-negative function on the configuration space $\mathbb C$. Then, the measure $\mu(.)$ having a density h(.) with respect to $\nu(.)$ is defined by:

$$\forall B \in \mathcal{B}(\mathcal{C}), \ \mu(B) = \int_{B} h(x)\nu(dx)$$
 (2)

A point process can be specified through a Gibbs energy U(x). The density h(x) of a configuration x is formulated using the Gibbs equation:

$$h(x) = \frac{\exp -U(x)}{Z} \tag{3}$$

where Z is a normalizing constant: $Z=\int_{x\in \mathcal{C}} \exp{-U(x)}$. Generally, a Monte Carlo Markov Chain (MCMC) sampler coupled with a simulated annealing is used to find the maximum density estimator $\widehat{x}=\arg\max{h(.)}$ (this estimator also corresponds to the configuration minimizing the Gibbs energy U(.), i.e. $\widehat{x}=\arg\min{U(.)}$). This optimization technique is particularly interesting since the density h(.) does not need to be normalized, and the complex computation of the normalizing constant Z is then avoided.

2.3 Marked and Multi-marked point processes

In order to model images in terms of geometrical features, it is possible to extend a point process by adding specific *marks* that associate a parametric object to each point. In many cases, the point corresponds to the center of mass of the object. A *marked point process* in $S = K \times M$ is a point process in K where each point is associated with a mark from a bounded set M, for example, a set of radius values in case of disks.

The conventional marked point processes [10], [11], [12], [13], [14], [15] suffer from a lack of generality: they are limited to a single type of objects since the dimension of the mark space M is fixed (e.g. rectangles [11], [13], segments [12], [14], or ellipses [10], [15]). Ortner $et\ al.$ [26] proposed to overcome this drawback by considering two marked point processes each using a different type of objects (rectangles and segments). The two processes are sampled jointly by a Markov Chain Monte Carlo algorithm. However, in this approach, both energy formulations and simulated annealing tunings become too complex to manage since cooperative interactions between both processes must be taken into account. This model cannot be adapted in practice to deal with a large number of object types.

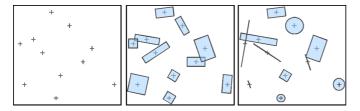


Fig. 2. Realizations of *(from left to right)* a point process, a marked point process of rectangles, and a multi-marked point process of rectangles/segments/circles.

We propose to generalize the conventional marked point process framework in order to jointly sample various types of geometric objects. To do so, we consider a finite library of marks allowing the definition of linear and areal features. The mark space M associated with this library is then specified as a finite union of mark bounded subsets M_q :

$$M = \bigcup_{q=1}^{N_s} M_q \tag{4}$$

where each subset M_q corresponds to one of the N_s specific shape types. In other words, the associated marked point process is able to deal with objects having different numbers of control parameters. Such a process, that we can call by extension a *multi-marked point process*, implies significant changes with respect to the conventional approach such as restrictions on the data term (e.g. the measurement must be independent of the object type), the setting up of general interactions between the various object types, or the introduction of new propositional functions to switch the object type during the sampling.

3 PROBABILISTIC GIBBS MODEL

3.1 Mark library

The library of marks allows the representation of seven simple geometric patterns shown in Figure 3. Segments, lines, and line ends are specific to linear structures whereas rectangles, bands, band ends, and circles correspond to areal descriptors. All the objects have between three and five control parameters, including positional coordinates (c_x, c_y) of the object's center that are specified by the point process in K. The other parameters, detailed in Table 1, represent the marks of the object types (e.g. the radius for circles; the length, width, and orientation for bands and rectangles). The parameters are defined in continuous domains, except for the object orientation defined in a discrete domain. The chosen set includes all basic objects used in the conventional marked point process based models. Thus, it is sufficient to produce detailed representations of a large range of scenes in terms of their linear and areal components.

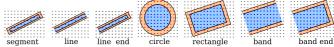


Fig. 3. The library of marks.

TABLE 1 Parameter definition of the marks: s-the length; θ -the orientation angle; r-the radius; L, l-the height and width respectively.

object type	marks	definition domains
segment	s, θ	$[s_{min}, s_{max}] \times [0, \pi]$
line	s, θ	$[s_{min}, s_{max}] \times [0, \pi]$
line end	s, θ	$[s_{min}, s_{max}] \times [0, 2\pi]$
circle	r	$[r_{min}, r_{max}]$
rectangle	L, l, θ	$[L_{min}, L_{max}] \times [l_{min}, l_{max}] \times [0, \pi]$
band	L, l, θ	$[L_{min}, L_{max}] \times [l_{min}, l_{max}] \times [0, \pi]$
band end	L, l, θ	$[L_{min}, L_{max}] \times [l_{min}, l_{max}] \times [0, 2\pi]$

3.2 Gibbs energy

Because the number of objects in any particular scene is unknown, and the objects have different numbers of parameters, the configuration space \mathcal{C} of our problem is defined as an union of subspaces \mathcal{C}_k , each subspace containing fixed numbers of objects of each type. A probability distribution \mathcal{P} on the configuration space \mathcal{C} is defined as a mixture of \mathcal{P}_k distributions on the subspaces \mathcal{C}_k . We assume that unnormalized distributions \mathcal{P}_k on \mathcal{C}_k have Gibbs densities of the form $e^{-U_k(x)}$ where U_k is a Gibbs energy associated with the configuration subspace \mathcal{C}_k (see Section 2.2).

The energy $U_k(x)$ takes into account both the consistency $D_k(x)$ between the objects and the image data and the regularization constraint $R_k(x)$ for the positioning of the objects with no overlaps:

$$U_k(x) = D_k(x) + R_k(x); \quad x \in \mathcal{C}_k \tag{5}$$

3.2.1 The data coherence term

 $D_k(x)$ accumulates the local energy associated with each object x_i of the configuration x:

$$D_k(x) = \sum_i d(x_i) \tag{6}$$

where $d(x_i)$ is a measure of coherence of the object x_i with respect to the data (*i.e.* an image). This measure d(.) must satisfy two important conditions:

- Independence of the object type: In particular, the object area must be taken into account in order to not favor linear or areal object types.
- Selection of "attractive" objects: i.e. the well-fitted objects must have a negative local energy (this feature is very important in the models using birth-and-death processes since it partly defines the object density in the scene).

In addition, d(.) must be differentiable and quickly computable in order to use diffusion dynamics during the optimization. We propose a function that is derived from the Mahalanobis distance and includes a threshold $\theta_{\rm attr} > 0$ that makes some objects attractive if the function is negative:

$$d(x_i) = \begin{cases} \sqrt{\frac{\sigma_{\text{in}}^2 + \sigma_{\text{out}}^2 + \epsilon}{8(m_{\text{in}} - m_{\text{out}})^2}} - \theta_{\text{attr}} & \text{if } m_{\text{in}} \neq m_{\text{out}} \\ \infty & \text{otherwise} \end{cases}$$
 (7)

Here, $(m_{\rm in}, \sigma_{\rm in})$ and $(m_{\rm out}, \sigma_{\rm out})$ represent the mean pixel intensities and standard deviations inside and outside the object, respectively (*i.e.* the blue and red areas on Figure 4). The width of the outside domain is fixed to 2 pixels in practice. \$ is the whole inside and outside area, and $\epsilon>0$ is an infinitesimal value allowing d(.) to be differentiable. The threshold $\theta_{\rm attr}$, being the only parameter of the model, allows to select the attractive objects and tune the sensitiveness of the data fitting. This measure of coherence is based on signal homogeneity criteria inside and outside the object (See Figure 4). It could be improved by taking into account specific information such as contour accuracy or noise modeling. Nonetheless, this measure produces good experimental results as we can see on Figure 5, and the introduction

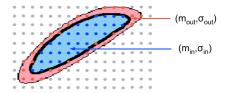


Fig. 4. Coherence measure between the object and the image data.

of additional criteria would strongly increase the computing time.

In addition, two variants of this measure are proposed in order to introduce radiometric information on target objects. By taking $m_{\rm in} > m_{\rm out}$ (respectively $m_{\rm in} < m_{\rm out}$) instead of $m_{\rm in} \neq m_{\rm out}$ in the definition domain of d(.)(see Eq. 7), we can modify the measure in order to favor bright (respectively dark) objects with respect to the background. This variant of d(.) will be called $d_{bright}(.)$ (respectively $d_{dark}(.)$) and used for various experiments in order to obtain a more specific extraction of target objects. Figure 5 shows two sets of signal responses with disks from the d, d_{bright} and d_{dark} measures. The first set corresponds to an ideal signal simulation. The black disk responses are slightly stronger than the white ones since the uniform bright grey background is closer to the white color than the black one. The second set shows the robustness of these measures with respect to noise and

$$d_{bright}(x_i) = \begin{cases} \sqrt{\frac{\sigma_{\rm in}^2 + \sigma_{\rm out}^2 + \epsilon}{8(m_{\rm in} - m_{\rm out})^2}} - \theta_{\rm attr} & \text{if } m_{\rm in} > m_{\rm out} \\ \infty & \text{otherwise} \end{cases}$$

$$d_{dark}(x_i) = \begin{cases} \sqrt{\frac{\sigma_{\rm in}^2 + \sigma_{\rm out}^2 + \epsilon}{8(m_{\rm in} - m_{\rm out})^2}} - \theta_{\rm attr} & \text{if } m_{\rm in} < m_{\rm out} \\ \infty & \text{otherwise} \end{cases}$$

$$(8)$$

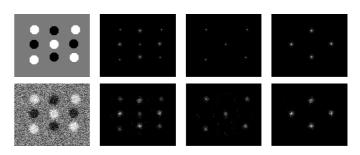


Fig. 5. Responses of (from left to right) d, d_{bright} and d_{dark} measures for a disk object on (top) exact and (bottom) noise and blur corrupted simulations.

3.2.2 The regularization constraint

 $R_k(x)$ introduces prior knowledge on the object layouts by taking into account pairwise interactions between the objects. The conventional marked point processes use strong structural information by defining complex and specific interactions such as inter-connections or mutual alignments of the objects [11], [12], [13], [14]. These complex interactions result in the above-mentioned critical problems (Section 1), such as trial-and-error tuning of many parameters. More generally, the introduction of such structural information in stochastic models requires special learning techniques such as the linear junction model presented in [27] or advanced thresholding methods such as *a contrario* approaches [28].

To avoid these problems, we limit the interactions to the essential ones for developing a general model of the non-overlapping objects. Strong structural information can then be introduced in a subsequent analysis by developing post-processing in order to connect the objects found. This term is expressed as follows:

$$R_k(x) = \sum_{x_i, x_j \in x} (e^{\kappa g(x_i, x_j)} - 1)$$
 (10)

where $g(x_i,x_j)$ taking values in [0,1] quantifies the relative mutual overlap between the objects x_i and x_j , and κ is a big positive real value ($\kappa=100$) which strongly penalizes large overlaps. Under small overlaps between two objects, this prior will weakly penalize the global energy. But if the overlapping is high, this prior will act as a hardcore (*i.e.* a hard constraint: the prior energy takes a very high value), and the configuration will be practically banned.

4 OPTIMIZATION BY JUMP-DIFFUSION

The search for an optimal configuration of objects is performed using the Jump-Diffusion process introduced by Grenander et al. [20], and used successfully in various applications such as target tracking [29], [30] and image segmentation [31]. This process combines the conventional Markov Chain Monte Carlo (MCMC) algorithms [4] and the Langevin equations [19]. Both dynamics play different roles in the Jump-Diffusion process: the former performs reversible jumps between the different subspaces \mathcal{C}_k , whereas the latter conducts stochastic diffusion within each continuous subspace. The global process is controlled by a relaxation temperature T depending on time t and approaching zero as t tends to infinity. The estimation of the simulated annealing parameters are detailed in Section 4.3. The diffusions are interrupted by jumps following a discrete time step Δt (in our experiments, $\Delta t = 50$). At the very low temperature, the diffusion process plays a more important role: the time step is increased ($\Delta t = 100$) to speed up the convergence.

4.1 Jump dynamic

Reversible jumps between the different subspaces are performed according to families of moves called proposition kernels and denoted by Q_m where m represents the family of moves. The jump process performs a move from an object configuration $x \in \mathcal{C}_k$ to $y \in \mathcal{C}_{k'}$ according

to a density $Q_m(x \to y)$. Then the move is accepted with the following probability:

$$\min\left(1, \frac{Q_m(y \to x)}{Q_m(x \to y)} e^{-\frac{(U_{k'}(y) - U_k(x))}{T}}\right) \tag{11}$$

We use two different families of moves in order to jump between the subspaces.

- Birth-and-death kernel Q_{BD} allows for adding or removing an object from a current object configuration. These transformations corresponding to jumps into the spaces of higher (birth) and lower (death) dimension are theoretically sufficient to visit the whole configuration space [16], [17]. In practice, we choose to add or remove an object following a Poisson distribution. If an object is added, its type is randomly chosen and its parameters are chosen according to uniform distributions over the parameter domains.
- Switching kernel Q_S allows us to switch the type of an object (e.g. a circle by a rectangle). Contrary to the previous kernel, this move does not change the number of objects in the configuration. However, the number of parameters can be different (e.g. three parameters for a circle are substituted by five parameters for a rectangle). This kernel creates bijections between the different types of objects [4].

The computation of both the kernels is detailed in Appendix. Usually the jump processes [6], [10], [11], [12], [13], [14], [15] use a perturbation kernel that allows the exploration of each subspace by modifying only parameters of the objects. In our case, this kernel is substituted by a diffusion dynamic which is clearly faster since the exploration of the subspace is directed by the energy gradient.

4.2 Diffusion dynamic

The diffusion process between jumps controls the dynamics of the object configuration in their respective subspaces. Stochastic diffusion (or Langevin) equations driven by Brownian motions depending on the relaxation temperature T are used to explore the subspaces \mathcal{C}_k . If x(t) denotes the variables at time t, then

$$dx(t) = -\frac{dU_k(x)}{dx}dt + \sqrt{2T(t)}dw_t$$
 (12)

where $dw_t \sim N(0, dt^2)$. At high temperature (T >> 0), the Brownian motion is useful in avoiding local pits. At low temperature (T << 1), the role of the Brownian motion becomes negligible and the diffusion dynamics acts as a gradient descent. Details concerning the energy gradient computation are given in Appendix.

4.3 Simulated annealing setting

Simulated annealing theoretically ensures convergence to the global optimum from any initial configuration using a logarithmic decrease of the temperature [32]. In

practice, we use a faster geometric decrease which gives an approximate solution close to the optimum [33]:

$$T_t = T_o.\alpha^t \tag{13}$$

where α and T_0 are, respectively, the decrease coefficient and the initial temperature. The decrease coefficient α can vary and be adapted according to the variation of the energy [34][35]. However, the time savings are usually relatively minor in practice. That is why we prefer using a constant decrease coefficient. (in our experiments, $\alpha \in [0.9999, 0.99999]$). T_0 is estimated through the variation of the energy U on random configurations. More precisely, T_0 is chosen as twice the standard deviation of U at infinite temperature [36]:

$$T_0 = 2.\sigma(U_{T=\infty}) = 2.\sqrt{\langle U_{T=\infty}^2 \rangle - \langle U_{T=\infty} \rangle^2}$$
 (14)

where $\langle U \rangle$ is the means of the energy of the samples (several thousands of samples are necessary to obtain a good estimation - it is negligible with respect to the number of iterations of the optimization process).

5 EXPERIMENTS

The proposed model has been tested on three different types of problems: population counting (tree crown and bird detection from aerial images), structure reconstruction (road network and building extraction from aerial data), and natural texture representation. The remotely sensed images in the two first sets of experiments are the same as in the conventional marked point process based methods [10], [11], [12], [15]. Although the presented results are generally slightly less accurate than those obtained by the specialized marked point processes, the proposed general model allows us to deal uniformly with various problems and in much shorter time.

5.1 Population counting

Figure 6 presents a result of the tree crown extraction by our multi-marked point process model. The main goal in this application is to count trees in large forest scenes for extracting statistics on the density of the stem. Although the shapes of trees are only roughly approximated by circles and rectangles, the trees are accurately detected. Even if no ground truth is available for this application, the accuracy of the tree locations is practically the same as obtained by [10] with elliptical objects to represent the trees. This new model allows the reduction of computational time by almost a factor three compared to [10] (77sec vs 212sec for the 240×350 pixel image in Figure 6).

The evolution of the object configuration during the jump-diffusion process is shown in Figure 7. At the beginning of the algorithm, *i.e.* when the temperature is high (*red*), the process explores the subspaces. Step by step, the configurations with a low energy are favored. At this exploration stage, the jump dynamic plays an important role by specifying both the number and the

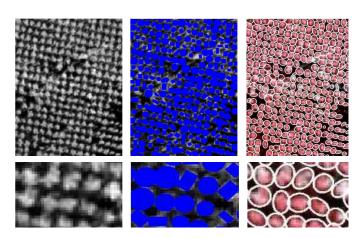


Fig. 6. Tree crown extraction. (the upper row, from left to right) The original aerial image ©IFN, our result, and the result by [10]; (the bottom row) the associated crops.

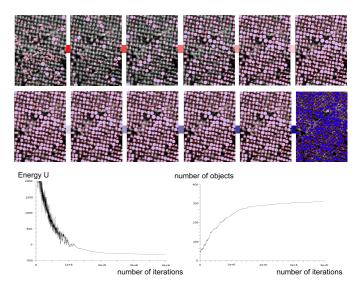


Fig. 7. Optimization process. (the upper row) Evolution of the object configuration from the initial temperature (red) to the final one (blue); (the bottom row) graphs of energy and number of objects in function of the iterations during jump-diffusion process.

type of objects. At low temperature (*blue*), the object configuration belongs to a subspace being close to the optimal one, and the number of objects in the scene does not evolve very much. The diffusion dynamic is useful at this stage mainly to perform a detailed adjustment of the object parameters. This dynamic is clearly faster than a single jump process with a perturbation kernel since the exploration is directed by the gradient of the energy (and not by a random search). Graphs in Figure 7 describe how the energy and the number of objects change in function of the number of iterations.

The bird detection problem is similar to the tree crown extraction: counting Flamingos in large colonies during the breeding season from large aerial images. Figure 8 presents results on a dense bird population which

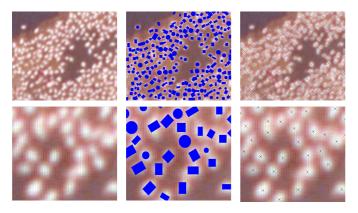


Fig. 8. Bird detection. (the upper row, from left to right) The original aerial image ©Tour du Valat, our result, and ground truth; (the bottom row) the associated crops.

are qualitatively close to those obtained in [15] using a specialized marked point process with elliptical objects. The missed bird rate 3.7%, in Table 2, is comparable to the rate 2.1% obtained by the specialized bird detection model [15]. The missed birds mainly correspond to cases where a proposed object overlaps two close birds as we can see on the cropped result presented in Figure 8. The over-detection rate is quite low (< 3%) in both the models. Our model allows us to gain 25% in terms of computational time compared to [15] that uses an improved Birth-and-Death algorithm specially designed for the population counting problems.

The efficiency of the diffusion dynamics in our model is confirmed by experiments that substitute the diffusion stage by a uniform perturbation kernel added to our jump dynamics. Results in Table 2 underline that the diffusion dynamics is clearly both faster and more accurate than the use of a uniform perturbation kernel.

TABLE 2 Bird extraction evaluation in terms of detection rates and computing time (image size: 560×496 pixels).

	missed	over-detected	computing time
model with	3.7%	2.9%	290 sec
Jump-Diffusion			
model with	6.2%	4.4%	840 sec
Jump			
specialized bird	2.1%	2.0%	380 sec
detection model[15]			

5.2 Structure extraction

Figures 9 and 10 present results of line network and building extractions from aerial images. The obtained structures are globally slightly less accurate than those obtained by the specialized marked point processes. The road network extraction results cannot be considered as a final representation since the detected objects are not connected (contrary to [12] where special complex interactions had been defined to link the segments).

However, the detected objects are mainly lines and bands which are well fitted to roads or rivers. These objects provide a rough pattern of the network and are sufficiently informative to make it possible to extract the global network on the basis of their subsequent analysis (e.g. post-processing based on vectorization in order to connect the objects found). The results in Figure 9 are similar to those obtained by the active contour model presented in [37]. Our method is clearly faster than both the specialized marked point process and active contour models [12], [37] (See Table 3). Moreover, these two models have a sensitive and complex parameter tuning (more than 10 parameters for each one) compared to our algorithm.

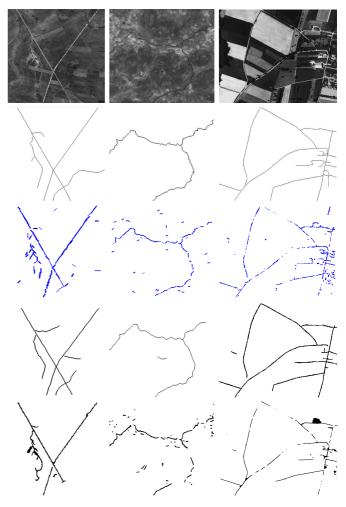


Fig. 9. Line network extraction. (from top to bottom) Aerial images ©CNES/BRGM/IGN, the ground truth, results by our method, by [12], and by [37].

The building extraction is also workable but the object localization remains very rough compared to the specialized model in [11]. This is mainly because of the over simplified data term in Eq. (7) that accounts for signal homogeneity inside and outside the object. Such a term is not relevant to this application since most of the building areas are heterogeneous due to non-flat

TABLE 3
Computing time for the line network extraction results presented on Figure 9 with a 2Ghz processor.

images	our model	mpp model[12]	hoac model[37]
road (left)	235 sec	75 min	30 min
$512 \times 512 \text{ pix}$			
river (middle)	107 sec	45 min	10 min
$364 \times 320 \text{ pix}$			
road2 (right)	380 sec	155 min	60 min
892×652 pix			

roofs. A term based on border discontinuity could be more efficient for this specific application. However, the proposed method detects main elements of the buildings and is clearly faster than the specialized marked point process in [11]: $30 \text{ minutes } vs \ 2 \text{ hours on a } 0.3 \text{ km}^2 \text{ dense}$ urban area using a 3 GHz processor.

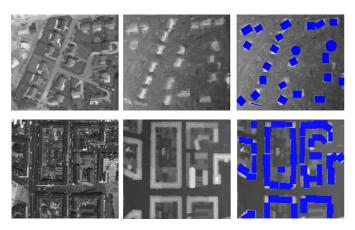


Fig. 10. Building extraction. (from left to right) Peri-urban and dense urban aerial images ©IGN, the associated DEMs, and our results.

5.3 Texture representation

We also tested the proposed method on a number of natural textures in order to evaluate its potentialities for representing them by geometric objects. Representing textures is a partial texture reconstruction where we aim to extract texture components of interest so that they can be visual or/and statistically identified. The choice of the data measure (See Section 3.2.1) is important then for extracting the structures of interest. Such descriptions provide useful information for discriminated textures, even if it remains less detailed than texture synthesis methods [7], [8], [9]. The results (some of them are presented in Figure 11) are quite promising. The obtained descriptions reconstruct the overall rough structure and reveal interesting fine details on a large range of textures. Various spatially homogeneous and heterogeneous textures are successfully represented even with a chosen simple library of objects. Some natural textures perceived under spatially variant illumination and reflectance (see e.g. the metal grid and tile roof examples) are usually difficult to describe, and often

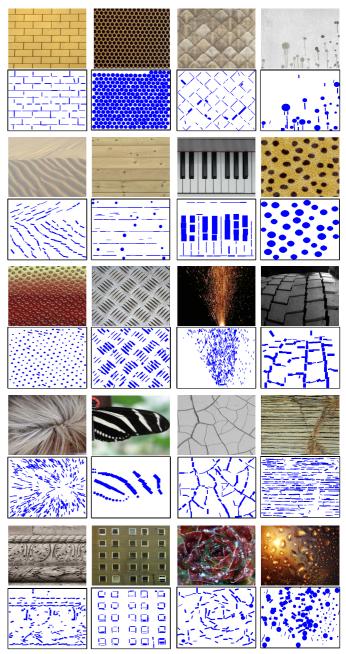


Fig. 11. Examples of natural texture representations in terms of geometrical objects.

require specific advanced techniques such as in [38]. Our method is particularly interesting for representing such textures since the fitting of objects does not depend on illumination effects. Various scales of details can be extracted in the texture structures (see *e.g.* the piano keyboard where the black keys are described by bands and the white key contours are represented by lines). The four last examples in Figure 11 show the limits of our model with respect to structure descriptions. In order to improve such representations, it is necessary to develop a more general energy function taking into account, in particular, typical object deviations and strong noise in

the textures (see *e.g.* the stone ornament and rose results). In terms of occurrence, lines and bands are the most frequent object types in the obtained texture representations. They allow us to describe a large range of linear and areal structures. Rectangles and circles, which are bounded areal descriptors, are mainly selected to describe isolated components of textures. In particular, these two object types lead to convincing results on counting population problems. The three other types are less frequent, and are used in more specific structures such as metal grids.

Figure 12 presents both the result obtained for an image with five different textures and the corresponding evolution of the object configuration during the jumpdiffusion process. Even if the objects are disconnected (see e.g. brick wall or rays) and not correctly selected in some locations (see e.g. some rectangles in the disk grid), the obtained description in terms of objects clearly shows five different object layouts, and underlines good potentialities for subsequent texture discrimination and segmentation. In particular, it would be interesting to combine such object-based representations with Markov Gibbs random field models which are mostly used on the pixel-wise intensities [39] and thus do not explicitly take into account shapes and relative locations of depicted characteristic objects. In order to deal with more complicated textures and have a description level similar to filter bank methods [40], affine-invariant descriptors [41], or wavelet based parametric models [42], the object library has to be extended by introducing new relevant shapes, especially general curved shapes or/and microstructure elements [43]. In this perspective, learning of dominant micro-structure elements such as e.g. in [44] is promising for the automatic selection of relevant objects from training images.

Figure 13 shows a comparison with the multi-layer texton model presented in [8]. Our approach provides a good representation of the textures with few false alarms as we can see for example on the crack image where many small lines have been extracted. However it remains limited in terms of description compared to the multi-layer texton model which allows the complete reconstruction of textures by sampling different layers of texture components. The interesting point consists in comparing both the models on textures composed of a foreground layer and a homogeneous background. In this case, our model can reconstruct the textures (see the third row on Figure 13 where both the extracted objects and background have been colored using the associated intensity means in the texture image), and the obtained results are very satisfactory for a non specialized texture reconstruction model. The localization accuracy we obtained is similar to that of the texton model as we can see for example on the crack results. However, the brick results show that the object connection quality of the texton model is clearly better than the one we obtain. In Section 6, we propose additional object interactions which will allow the improvement of this point. The

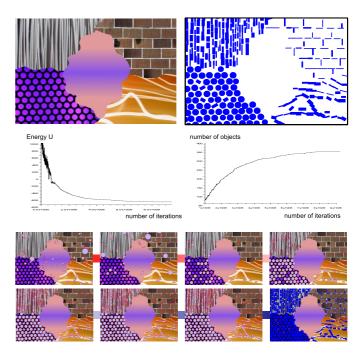


Fig. 12. Texture representation. (the upper row, from left to right) Original image and our result; (the middle row) graphs of energy and number of objects in function of the iterations during jump-diffusion process; (the bottom row) evolution of the object configuration from the initial temperature (red) to the final one (blue).

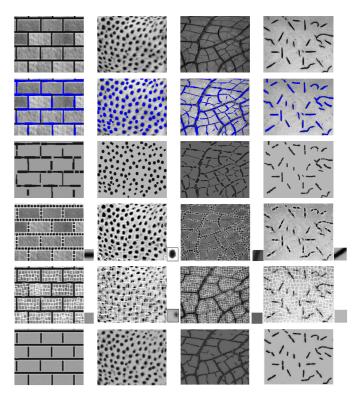


Fig. 13. Comparison with the texton model [8]. (from top to bottom) Textures ©UCLA, our results, our associated reconstructed textures, the foreground and background texton extractions by [8] and the associated reconstructed textures ©UCLA.

cheetah skin results underline the limits of our model when several texton layers are required for describing various texture components (*i.e.* big dark and small grey spots). On the contrary, the texton model leads to an accurate reconstruction on such a multi-component texture.

Figure 14 presents the impact of the model parameter $\theta_{\rm attr}$ on the results. This parameter, which tunes the sensitiveness of data fitting, plays an important role in the final number of objects describing the image. A low value (e.g. 3.5 or 4.5) provides representations containing few accurately localized objects. On the contrary, a high value (such as 6.5 or 7.5) gives much more dense descriptions but with many roughly detected objects. In our experiments, $\theta_{\rm attr}$ has been tuned in the interval [5.1, 5.8] which constitutes a good compromise between the level of details of the representation and the accuracy of the object locations. An automatic estimation of $\theta_{\rm attr}$ from a given image represents a challenging but interesting perspective. Several kinds of information such as the signal to noise ratio or signal co-occurrence repetitiveness in the image could be taken into account for this estimation. Figure 14 also shows results using different data fitting measures.

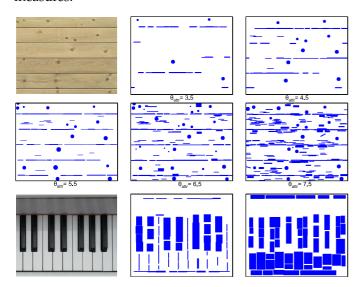


Fig. 14. Impact of the model parameters. (the upper rows) Impact of $\theta_{\rm attr}$ on a natural texture representation; (the bottom row) impact of the d_{bright} and d_{dark} measures.

6 INSERTION OF MORE COMPLEX OBJECT INTERACTIONS

As mentioned in Section 3.2.2, introducing specific regularization constraints directly impacts on three points: (i) more complex parameter tunings, (ii) higher computing times, and (iii) loss of the model generality level. However, such interactions bring helpful structural knowledge in some applications and can allow us to obtain better results by reducing the True Negatives and the False Positives. In this section, we discuss the interest of

inserting new types of object interactions in the energy model (see Eq. 5) and analyze their efficiency on various applications.

6.1 New object interactions

According to the experiments realized in Section 5, some results suffer from both a lack of object connection and an approximated object alignment, especially for line network extraction and texture representation. We propose to introduce these two additional interactions in our energy model in the following.

6.1.1 Inter-connection

Such an interaction type can be efficiently modeled from the non-overlapping constraint defined in Section 3.2.2 by favoring the connected objects in keeping the high overlaps penalize. To to so, we introduce the parameter $\gamma_{attr} > 1$ which makes attractive (respectively repulsive) weak (resp. high) object overlaps. The modified prior is expressed as follows:

$$R_k^c(x) = \sum_{x_i, x_j \in x} (e^{\kappa g(x_i, x_j)} - \gamma_{attr})$$
 (15)

 γ_{attr} controls the balance between attraction and repulsion in function of object overlapping. For example, if we want to favor configurations with an overlap up to 20%, we will take $\gamma_{attr} = \exp 0.2\kappa$.

6.1.2 Mutual alignment

This term aims at penalizing the orientation changes of neighboring elements. It is given by:

$$R_k^a(x) = \sum_{x_i, x_j \in x} (e^{\kappa g(x_i, x_j)} - 1) + \lambda \sum_{x_i, x_j \in x} A(x_i, x_j) \quad (16)$$

where $A(x_i,x_j)$ measures the mutual alignment of the objects x_i and x_j using a $L_{\frac{1}{2}}$ norm. A(.,.) takes values in [0,1] and λ is a parameter weighting the importance of the object alignment with respect to the non-overlapping criterion. When x_i or x_j is a rotation-invariant object (i.e. a circle), we impose $A(x_i,x_j)=a$ where $a\in[0,1]$ is a parameter allowing us to tune the occurrence of rotation-invariant object with respect to non rotation invariant objects. This additional parameter is necessary for modeling alignment constraints when the object library contains rotation-invariant objects.

6.1.3 Inter-connection and mutual alignment association

This prior is a simple combination of both the interaction types detailed above:

$$R_k^{ac}(x) = \sum_{x_i, x_j \in x} \left(e^{\kappa g(x_i, x_j)} - \gamma_{attr} \right) + \lambda \sum_{x_i, x_j \in x} A(x_i, x_j)$$
(17)

These three priors remain more general than those used in the specialized marked point processes and are modeled by less parameters. In addition, they are differentiable which is necessary to perform diffusion dynamics. Compared to the original model presented in Section 3, the new energies are more complex and additional computing time is required to optimize them.

6.2 Model complexity and efficiency

The prior terms detailed above have been tested on various applications. Figure 15 presents the obtained results and comparisons to the initial model and the conventional Canny edge detector [45]. Even if the Canny detector suitably extracts shapes of interest in the presented textures, such an approach is limited to pixel analysis and does not take into account the object concept. Such an edge extraction is interesting to evaluate the complexity of the presented images in terms of boundary accuracy, noise and shape irregularity.

Simulations without data (See first column on Figure 15) show right behaviors of the proposed priors in accordance with the expectation. The inter-connection term, R_k^c , allows us to slightly improve the results by reducing the false alarms but remains insufficient for decreasing the true negative (See the road extraction result for example). This term is clearly not adapted to population counting problems as we can see on the tree extraction result where objects are enlarged to be connected together. On the contrary, the mutual alignment term gives an interesting result for this application and allows us to extract more efficiently such a grid structure by regularizing the object orientation. The interest of R_k^c is quite limited for the others applications. The last term, R_k^{ac} , gives the best results for almost all the tested images. The combination of connection and alignment constraints strongly reduces the number of false positive and true negative as we can see on road and blood vessel extraction. This prior also brings accurate texture representations and allows us to clearly improve the results on complex cases such as the flower. Table 4 evaluates the efficiency of these three priors in terms of parameter tuning and computing time. The term R_k^{ac} , which gives the best results, also corresponds to the most complex parameter tuning and the highest computing time. Depending on the application context, the initial model is preferred since the tuning of the four parameters by trial and error requires time and expertise.

TABLE 4
Prior efficiency evaluation.

interactions	parameters	extra computing time
R_k^c , connection	θ_{attr} , γ_{attr}	32%
R_k^a , alignment and	θ_{attr} , λ , a	48%
non-overlapping		
R_k^{ac} , connection	θ_{attr} , γ_{attr} , λ , a	91%
and alignment		

7 Conclusions

The proposed new approach based on a multi-marked point process model allows the representation of images

in terms of simple geometric features. Although the obtained results are generally slightly less accurate than those provided by the specialized marked point process models, our approach possesses several interesting characteristics. First, it is more general and works efficiently on various applications such as counting population problems, structure reconstruction from remotely sensed images, and natural texture representation whereas the conventional approaches needed to exploit specialized models for each problem. Moreover, we have proposed an efficient Jump-Diffusion algorithm adapted to marked point processes that allows us to strongly reduce computational time with respect to the classical jump techniques. Finally, we have decreased the number of tuning parameters by formulating a global model and have discussed the compromise between model complexity and efficiency by analyzing the impact of additional object interactions in the model.

However, our approach is limited by the content of the mark library: the current set in Figure 3 cannot in principle provide relevant representations of complex structures such as multiple junctions or random curved shapes. In the future, we will extend the mark library and develop probabilistic models and techniques for automatic selection of relevant "basic" objects from a given collection of training images. Another perspective would be to improve the data term of our model by using both a more efficient differentiable and quickly computable measure which takes into account specific information such as noise models or contour accuracy, and to provide an automatic estimation of the data fitting sensitiveness parameter.

APPENDIX

Computation of the birth-and-death kernel

Let us consider a birth, chosen with a probability p_b , from object configurations $x = (x_p)_{p \in [1, n(x)]}$ to $y = x \cup \{x_{n(x)+1}\}$ where $x_{n(x)+1}$ is the new added object chosen randomly on the object space. The ratio of the kernels in the acceptance rate equation (see Eq. 11) is then expressed by:

$$\frac{Q_{BD}(y \to x)}{Q_{BD}(x \to y)} = \frac{p_d}{p_b} \frac{\nu(K)}{n(x) + 1}$$
 (18)

where p_b (respectively, $p_d = 1 - p_b$) is the probability of choosing a birth (respectively, a death), and $\nu(.)$ is the intensity of the reference Poisson process (See Section 2.1). In our model, the probabilities of choosing a birth and a death are the same (*i.e.* $p_d = p_b$).

Let us consider now a death from object configurations $x=(x_p)_{p\in[1,n(x)]}$ to $y=x-\{x_i\}$ where x_i is the removed object chosen randomly in the object configuration x. By the reversible assumption, the kernel ratio of the death is given by:

$$\frac{Q_{BD}(y \to x)}{Q_{BD}(x \to y)} = \frac{p_b}{p_d} \frac{n(x)}{\nu(K)}$$
 (19)

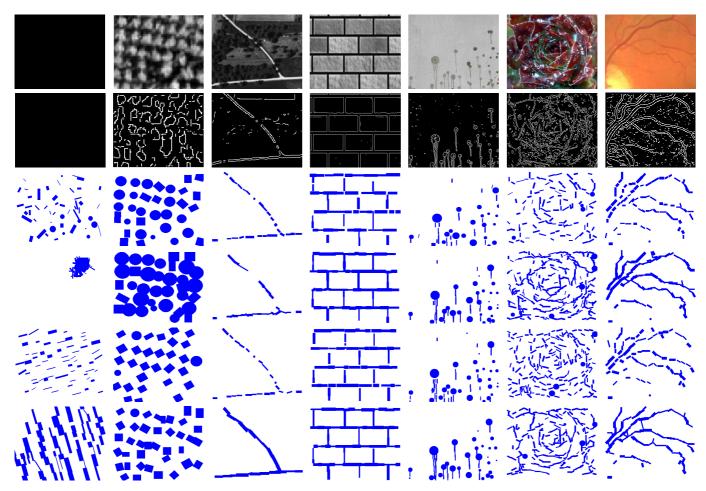


Fig. 15. Efficiency of the various interactions. (*from top to down*) Images, Canny edge detector, results using the original model, the connection, the alignment, and the connection/alignment interaction priors. The number of objects on simulations without data (first column) has been voluntarily upper bounded in order to avoid infinite grouping of objects and then to have comprehensible results.

Computation of the switching kernel

Let us consider a jump from an object x_i of type \mathfrak{T}_m (for example, a circle) to an object $\widehat{x_i}$ of type \mathfrak{T}_n (for example, a rectangle) such that the current object configuration $x=(x_p)_{p\in[1,n(x)]}$ is perturbed into the configuration $y=x-\{x_i\}\cup\widehat{x_i}$. We then create a bijection between the parameter spaces of the object types \mathfrak{T}_m and \mathfrak{T}_n : x_i is completed by auxiliary variables u_{mn} simulated under a law $\varphi_{mn}(.)$ to provide (x_i,u_{mn}) , and $\widehat{x_i}$ by $v_{nm}\sim\varphi_{nm}(.)$ into $(\widehat{x_i},v_{mn})$ such that the mapping Ψ_{mn} between (x_i,u_{mn}) and $(\widehat{x_i},v_{mn})$ is a bijection :

$$(\widehat{x_i}, v_{mn}) = \Psi_{mn}(x_i, u_{mn}) \tag{20}$$

The ratio of the kernels in the acceptation ratio (see Eq. 11) is then expressed by:

$$\frac{Q_S(y \to x)}{Q_S(x \to y)} = \frac{J_{nm}\varphi_{nm}(v_{nm})}{J_{mn}\varphi_{mn}(u_{mn})} \left| \frac{\partial \Psi_{mn}(x_i, u_{mn})}{\partial (x_i, u_{mn})} \right|$$
(21)

where J_{mn} corresponds to the probability of choosing a jump from the object type \mathfrak{T}_m to the object type \mathfrak{T}_n . In our case, the object types are equiprobable. It implies

 $J_{nm}=J_{mn}$. In our experiments, the mark library is composed of seven object types having five different parameter sets shown in Table 1. Then, $5^2-5=20$ bijections and associated completion parameters must be computed.

Let us consider, for example, a jump from a circle (denoted \mathfrak{T}_1) to a rectangle (denoted \mathfrak{T}_2). We move from $x_i=(c_x,c_y,r)$ to $\widehat{x}_i=(c_x,c_y,L,l,\theta)$. The parameters c_x and c_y specifying the center of mass exist in both the object types. Moreover, we can define a linear transformation between the radius $r\in[r_{min},r_{max}]$ of the circle and the length $L\in[L_{min},L_{max}]$ of the rectangle such as $L=\frac{L_{max}-L_{min}}{r_{max}-r_{min}}r+\frac{L_{min}r_{max}-L_{max}r_{min}}{r_{max}-r_{min}}$. Thus, we need to complete the object type \mathfrak{T}_1 by $u_{1\,2}=(l,\theta)$. We then obtain $\widehat{x}_i=\Psi_{1\,2}(x_i,u_{1\,2})$ with

$$\Psi_{12}(X) = \begin{pmatrix}
Id_2 & 0 & 0_{2,2} \\
0_{2,1} & \frac{L_{max} - L_{min}}{r_{max} - r_{min}} & 0_{2,1} \\
0_{2,2} & 0 & Id_2
\end{pmatrix} X + \begin{pmatrix}
0_{1,2} \\
\frac{L_{min}r_{max} - L_{max}r_{min}}{r_{max} - r_{min}} \\
0_{1,2}
\end{pmatrix} (22)$$

where Id_i and $0_{i,j}$ are the identity matrix of size i and the zero matrix of size $i \times j$, respectively. Finally, we have $\left| \frac{\partial \Psi_{1\,2}(x_i,u_{1\,2})}{\partial (x_i,u_{1\,2})} \right| = \frac{L_{max}-L_{min}}{r_{max}-r_{min}}$. The completion parameters $u_{1\,2}$ are chosen following uniform distributions on the parameter spaces.

Computation of the energy gradient

Let p denote a parameter of the object x_i of the object configuration $x \in \mathcal{C}_k$. Then, the energy derivative with respect to p is given by:

$$\frac{dU_{k}(x)}{dp} = \sum_{x_{k} \in x} \frac{dd(x_{k})}{dp} + \sum_{x_{k}, x_{l} \in x} \frac{d(e^{\kappa g(x_{k}, x_{l})} - 1)}{dp}
= d(x_{i})' + \sum_{j \sim i} \kappa g(x_{i}, x_{j})' e^{\kappa g(x_{i}, x_{j})}$$
(23)

where $(.)'=\frac{d\,(.)}{d\,p}$ and the notation $j\sim i$ corresponds to the set of objects x_j such as $g(x_i,x_j)\neq 0$ (i.e. the neighboring objects of x_i). The data term is as follows:

$$d(x_{i})' = \frac{\sigma_{\text{in}}^{2}' + \sigma_{\text{out}}^{2}'}{2\$(d(x_{i}) + \theta_{\text{attr}})(m_{\text{in}} - m_{\text{out}})^{2}} \times \left[1 - \left(\frac{\$'}{\$} + 2\frac{m_{\text{in}}' - m_{\text{out}}'}{m_{\text{in}} - m_{\text{out}}}\right) \frac{\sigma_{\text{in}}^{2} + \sigma_{\text{out}}^{2} + \epsilon}{\sigma_{\text{in}}^{2}' + \sigma_{\text{out}}^{2}'}\right]$$
(24)

If $m_{in} = m_{out}$, a hardcore is associated with the energy which means the object configuration is forbidden. The derivatives of the statistical parameters used in Eq. 24 are given by the following expressions:

$$m_{in}' = -S_{in}' m_{in} + \frac{1}{S_{in}} \int_{\partial \Omega_{in}} I \tag{25}$$

$$m_{out}' = -S_{out}' m_{out} + \frac{1}{S_{out}} \int_{\partial \Omega_{out}} I$$
 (26)

$$\sigma_{\text{in}}^{2'} = -8_{in}'\sigma_{\text{in}}^{2} + \frac{1}{S_{in}} \left[\int_{\partial\Omega_{in}} (I - m_{in})^{2} - 2 \int_{\Omega_{in}} m_{in}' (I - m_{in}) \right]$$
(27)

$$\sigma_{\text{out}}^{2}' = -S_{out}'\sigma_{\text{out}}^{2} + \frac{1}{S_{out}} \times \left[\int_{\partial\Omega_{out}} (I - m_{out})^{2} - 2 \int_{\Omega_{out}} m_{out}' (I - m_{out}) \right]$$
(28)

where I is the intensity of the image, Ω_{in} and Ω_{out} are the inside and outside domain, respectively, and S_{in} and S_{out} are the area of these domains. If we consider the energy derivative with respect to the center of mass and orientation object parameters, the computation is simplified since the area of the object does not depend on these parameters (i.e. $S' = S_{in}' = S_{out}' = 0$).

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