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Investigating the Impact of Sequential Selection in the (1,2)-CMA-ES on the Noisy BBOB-2010 Testbed

[Black-Box Optimization Benchmarking Workshop]

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ABSTRACT

Sequential selection was introduced for Evolution Strategies (ESs) with the aim of accelerating their convergence—performing the evaluations of the different offspring sequentially and concluding an iteration immediately if one offspring is better than the parent. This paper investigates the impact of the application of sequential selection to the (1,2)-CMA-ES on the BBOB-2010 noisy benchmark testbed. The performance of the (1,2^s)-CMA-ES, where sequential selection is implemented, is compared to the baseline algorithm (1,2)-CMA-ES. Independent restarts for the two algorithms are conducted up to a maximum number of $10^4 D$ function evaluations, where D is the dimension of the search space.

The results show a slight improvement of the (1,2^s)-CMA-ES over the baseline (1,2)-CMA-ES on the sphere function with Cauchy noise and a stronger decline on the sphere function with moderate uniform noise. Overall, the (1,2^s)-CMA-ES seems slightly less reliable and we conclude that for the (1,2)-CMA-ES, sequential selection is no improvement on noisy functions.

Categories and Subject Descriptors

G.1.6 [Numerical Analysis]: Optimization—*global optimization, unconstrained optimization*; F.2.1 [Analysis of Algorithms and Problem Complexity]: Numerical Algorithms and Problems

General Terms

Algorithms

Keywords

Benchmarking, Black-box optimization

1. INTRODUCTION

Evolution Strategies (ESs) are robust stochastic search algorithms for black-box optimization where the objective function to be minimized, f , maps the continuous search space \mathbb{R}^D into \mathbb{R} . ESs are using a population of candidate solutions, created by sampling λ independent random vectors following a multivariate normal distribution. Those random vectors are added to a current solution. In the local search (1, λ)-ES, the best of those λ solutions, i.e., the solution having the smallest objective function value, is selected to become the new current solution.

Sequential selection has been recently introduced for Evolution Strategies with the aim of accelerating their convergence [4]. When sequential selection is applied in a (1, λ)-ES, the evaluations are carried out sequentially and the sequence of evaluations is stopped as soon as an offspring turns out to be better than its parent. The parent for the next iteration is then set to this offspring. In this paper, we evaluate the impact of sequential selection on the (1,2)-Covariance-Matrix-Adaptation Evolution-Strategy (CMA-ES) using the BBOB-2010 noisy testbed. The performance of the (1,2^s)-CMA-ES implementing sequential selection is compared to the performance of the (1,2)-CMA-ES. The algorithms as well as the CPU timing experiments are described in a complementing paper in the same proceedings [1].

2. COMPARING THE (1,2) AND THE (1,2^s)-CMA-ES

Results from experiments comparing the (1,2)-CMA-ES and the (1,2^s)-CMA-ES according to [6] on the benchmark functions given in [5, 7] are presented in Figures 1, 2 and 3 and in Table 1. The **expected running time (ERT)**, used in the figures and table, depends on a given target function value, $f_t = f_{\text{opt}} + \Delta f_t$, and is computed over all relevant trials as the number of function evaluations executed during each trial while the best function value did not reach f_t , summed over all trials and divided by the number of trials that actually reached f_t [6, 8]. **Statistical significance** is tested with the rank-sum test for a given target Δf_t (10^{-8} in Figure 1) using, for each trial, either the number of needed function evaluations to reach Δf_t (inverted and multiplied by -1), or, if the target was not reached, the best Δf -value achieved, measured only up to the smallest number of overall function evaluations for any unsuccessful trial under consideration.

Overall, we can say that both the (1,2)-CMA-ES and the (1,2^s)-CMA-ES are not very successful when dealing with noise; 23 out of the 30 functions are not solved, i.e., both algorithms show a success probability of zero to reach a target precision of 10^{-8} . Moreover, the sequentialism of the (1,2^s)-CMA-ES only slightly improves over the (1,2)-CMA-ES on the sphere with Cauchy noise (f_{109} , this is the only statistically significant improvement). At the same time, the (1,2^s)-CMA-ES is much worse than (1,2)-CMA-ES on f_{102} (by a factor of 5, statistically significant) and on f_{130} (factor of 3, not significant) while showing a somewhat smaller success probability in both cases.

Worth to mention is the fact that the (1,2)-CMA-ES performs on par with the overall best algorithm of the BBOB-2009 benchmarking on the Gallagher function with Cauchy noise, f_{130} .

3. CONCLUSIONS

The idea behind the sequential selection scheme introduced in [4] is to finish the iteration as soon as an offspring is evaluated which is better than the current solution and thereby save some of the λ function evaluations per iteration in a (1, λ)-ES. Here, we compared the (1,2^s)-CMA-ES with the corresponding baseline (1,2)-CMA-ES on the noisy BBOB-2010 testbed.

The experiments show that the (1,2)-CMA-ES, despite its small population size, can solve 7 of the functions and performs on the Gallagher function with Cauchy noise (f_{130}) on par with the best algorithm from BBOB-2009. The usage of sequential selection in the (1,2)-CMA-ES is rather detrimental than beneficial here since it seems overall less reliable and delivers only a very moderate speedup in some cases.

Although the experiments suggest that sequential selection has no positive effect, this seems to be true only for the (1,2)-CMA-ES: the (1,4)-CMA-ES with 4 instead of 2 offspring shows significant improvements if the sequential selection is employed on both the noiseless [2] and the noisy BBOB-2010 testbed [3].

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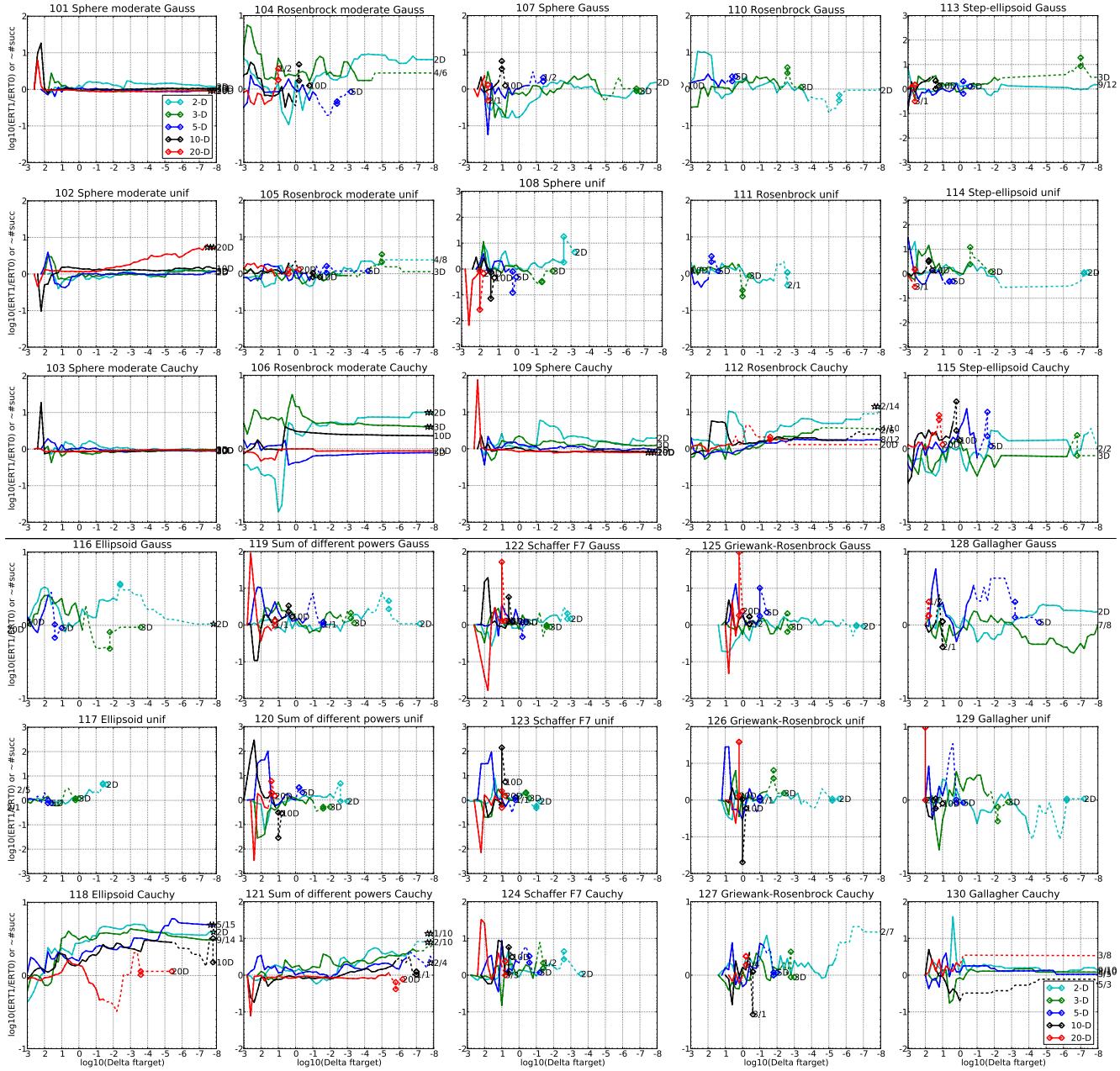


Figure 1: Ratio of the expected running times (ERT) of (1,2^s)-CMA-ES divided by (1,2)-CMA-ES versus $\log_{10}(\Delta f)$ for $f_{101}-f_{130}$ in **2, **3**, **5**, **10**, **20**. Ratios $< 10^0$ indicate an advantage of (1,2^s)-CMA-ES, smaller values are always better. The line gets dashed when for any algorithm the ERT exceeds thrice the median of the trial-wise overall number of f -evaluations for the same algorithm on this function. Symbols indicate the best achieved Δf -value of one algorithm (ERT gets undefined to the right). The dashed line continues as the fraction of successful trials of the other algorithm, where 0 means 0% and the y-axis limits mean 100%, values below zero for (1,2^s)-CMA-ES. The line ends when no algorithm reaches Δf anymore. The number of successful trials is given, only if it was in {1...9} for (1,2^s)-CMA-ES (1st number) and non-zero for (1,2)-CMA-ES (2nd number). Results are statistically significant with $p = 0.05$ for one star and $p = 10^{-\#^*}$ otherwise, with Bonferroni correction within each figure.**

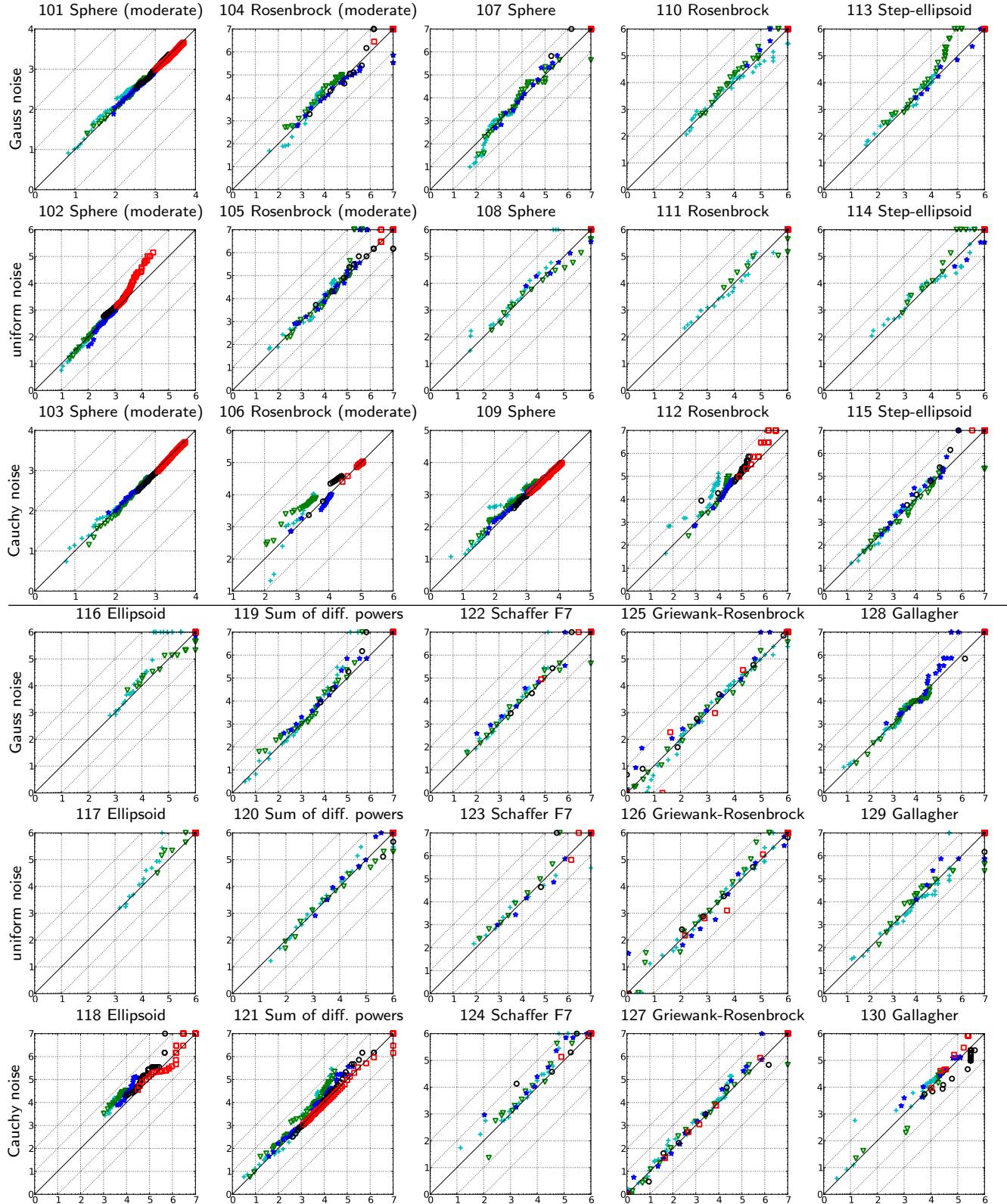


Figure 2: Expected running time (ERT in \log_{10} of number of function evaluations) of $(1,2^s)$ -CMA-ES versus $(1,2)$ -CMA-ES for 46 target values $\Delta f \in [10^{-8}, 10]$ in each dimension for functions $f_{101}-f_{130}$. Markers on the upper or right edge indicate that the target value was never reached by $(1,2^s)$ -CMA-ES or $(1,2)$ -CMA-ES respectively. Markers represent dimension: 2: +, 3: ▼, 5: *, 10: ○, 20: □.

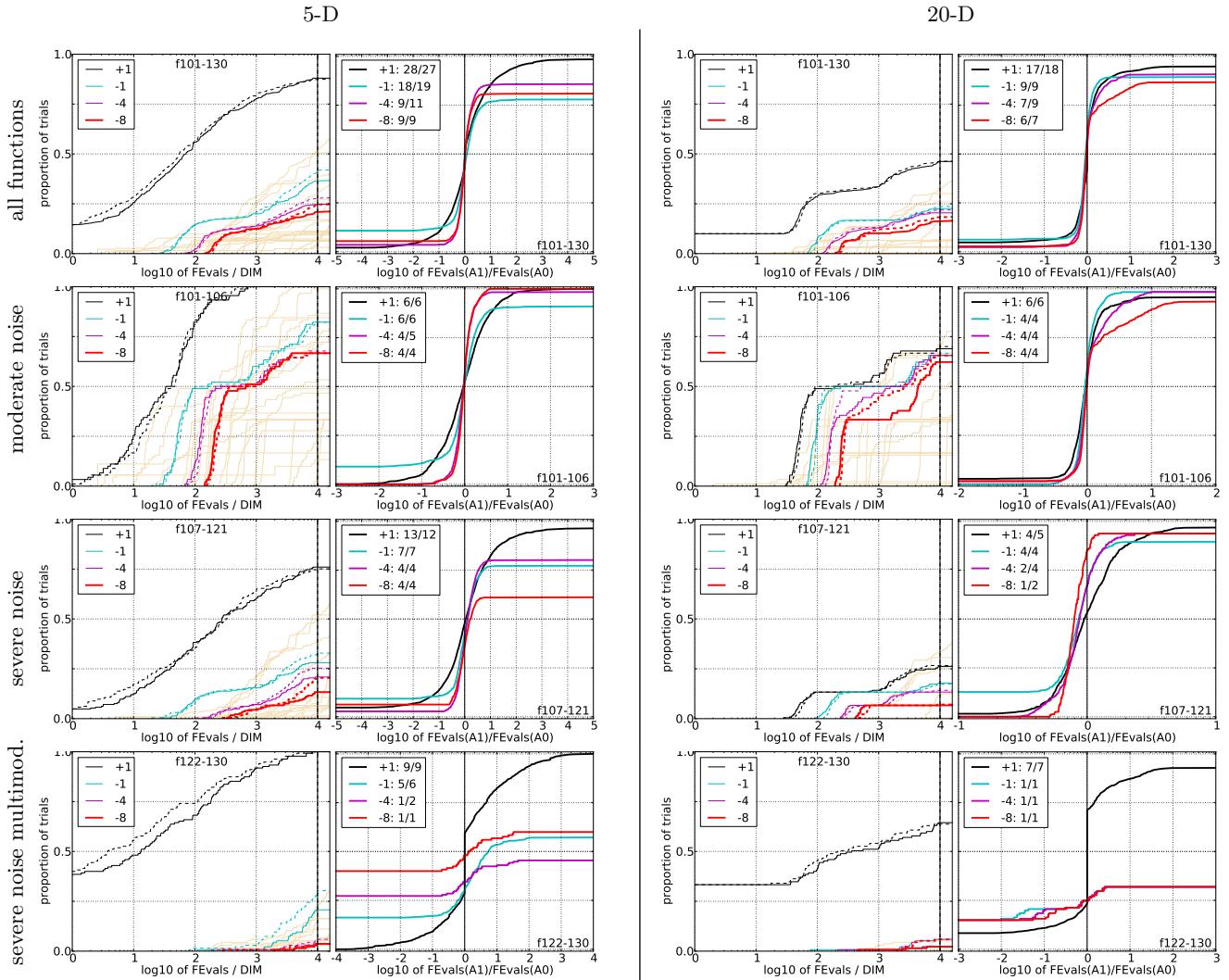


Figure 3: Empirical cumulative distributions (ECDF) of run lengths and speed-up ratios in 5-D (left) and 20-D (right). Left sub-columns: ECDF of the number of necessary function evaluations divided by dimension D (FEvals/D) to reached a target value $f_{\text{opt}} + \Delta f$ with $\Delta f = 10^k$, where $k \in \{1, -1, -4, -8\}$ is given by the first value in the legend, for $(1,2^s)$ -CMA-ES (solid) and $(1,2)$ -CMA-ES (dashed). Light beige lines show the ECDF of FEvals for target value $\Delta f = 10^{-8}$ of all algorithms benchmarked during BBOB-2009. Right sub-columns: ECDF of FEval ratios of $(1,2^s)$ -CMA-ES divided by $(1,2)$ -CMA-ES, all trial pairs for each function. Pairs where both trials failed are disregarded, pairs where one trial failed are visible in the limits being > 0 or < 1 . The legends indicate the number of functions that were solved in at least one trial ($(1,2^s)$ -CMA-ES first).

5-D

Δf	1e+11e+0 1e-1 1e-3 1e-5 1e-7	#succ
f_{101}	11 37 44 62 69 75	15/15
(1,2)-CMA-ES	8.3 4.4 6.3 8.511 13	15/15
(1,2 ^s)-CMA-ES	<i>7</i> 4.7 6.7 7.6 9.7 12	15/15
f_{102}	11 35 50 72 86 99	15/15
(1,2)-CMA-ES	9.2 5.8 6.2 7.7 9.7 11	15/15
(1,2 ^s)-CMA-ES	<i>4.1</i> 5.2 6.4 8 9.3 10	15/15
f_{103}	11 28 30 31 35 120	15/15
(1,2)-CMA-ES	6.2 6.7 9 18 25 10	15/15
(1,2 ^s)-CMA-ES	<i>8.2</i> 7 9.6 16 22 9.2	15/15
f_{104}	170 770 1300 1800 2000 2300	15/15
(1,2)-CMA-ES	3.9 13 54 ∞ ∞ ∞ .5.0e4	0/15
(1,2 ^s)-CMA-ES	<i>3.5</i> 13 50 410 ∞ ∞ .5.0e4	0/15
f_{105}	170 1400 5200 1.0e41.1e4 1.1e4	15/15
(1,2)-CMA-ES	3.1 7.8 19 70 ∞ ∞ .5.0e4	0/15
(1,2 ^s)-CMA-ES	<i>4.9</i> 10 19 ∞ ∞ ∞ .5.0e4	0/15
f_{106}	86 530 1100 2700 2900 3100	15/15
(1,2)-CMA-ES	7.5 13 8.6 4.1 3.9 3.8	15/15
(1,2 ^s)-CMA-ES	<i>8.4</i> 8.5 6.8 3.4 3.4 3.4	15/15
f_{107}	40 230 450 940 1400 1900	15/15
(1,2)-CMA-ES	17 43 330 ∞ ∞ ∞ .5.0e4	0/15
(1,2 ^s)-CMA-ES	<i>12</i> 44 450 ∞ ∞ ∞ .5.0e4	0/15
f_{108}	87 5100 1.4e43.1e45.9e4 8.1e4	15/15
(1,2)-CMA-ES	43 ∞ ∞ ∞ ∞ .5.0e4	0/15
(1,2 ^s)-CMA-ES	<i>90</i> 69 ∞ ∞ ∞ ∞ .5.0e4	0/15
f_{109}	11 57 220 570 870 950	15/15
(1,2)-CMA-ES	5.5 2.8 1.8 1.9 2.5 3.4	15/15
(1,2 ^s)-CMA-ES	<i>5.8</i> 3.5 2 2.2 2.4 3.4	15/15
f_{110}	950 3.4e41.2e55.9e56.0e5 6.1e5	15/15
(1,2)-CMA-ES	32 ∞ ∞ ∞ ∞ .5.0e4	0/15
(1,2 ^s)-CMA-ES	<i>46</i> ∞ ∞ ∞ ∞ .5.0e4	0/15
f_{111}	6900 6.1e58.8e62.3e73.1e7 3.1e7	3/15
(1,2)-CMA-ES	∞ ∞ ∞ ∞ ∞ .5.0e4	0/15
(1,2 ^s)-CMA-ES	∞ ∞ ∞ ∞ ∞ .5.0e4	0/15
f_{112}	110 1700 3400 4500 5100 5600	15/15
(1,2)-CMA-ES	8 9.3 7 7.8 7.4 7.1	12/15
(1,2 ^s)-CMA-ES	<i>6.4</i> 8.6 11 14 13 12	8/15
f_{113}	130 1900 8100 2.4e42.4e4 2.4e4	15/15
(1,2)-CMA-ES	20 51 ∞ ∞ ∞ .5.0e4	0/15
(1,2 ^s)-CMA-ES	<i>21</i> 37 ∞ ∞ ∞ .5.0e4	0/15
f_{114}	770 1.5e45.6e48.3e48.3e4 8.5e4	15/15
(1,2)-CMA-ES	100 ∞ ∞ ∞ ∞ .5.0e4	0/15
(1,2 ^s)-CMA-ES	<i>56</i> ∞ ∞ ∞ ∞ .5.0e4	0/15
f_{115}	64 490 1800 2600 2600 3000	15/15
(1,2)-CMA-ES	5.3 5.7 66 ∞ ∞ ∞ .5.0e4	0/15
(1,2 ^s)-CMA-ES	<i>4.7</i> 11 50 ∞ ∞ ∞ .5.0e4	0/15
f_{116}	5700 1.4e42.2e42.7e43.0e4 3.2e4	15/15
(1,2)-CMA-ES	∞ ∞ ∞ ∞ ∞ .5.0e4	0/15
(1,2 ^s)-CMA-ES	<i>130</i> ∞ ∞ ∞ ∞ .5.0e4	0/15
f_{117}	2.7e47.6e41.1e51.4e51.7e5 1.9e5	15/15
(1,2)-CMA-ES	∞ ∞ ∞ ∞ ∞ .5.0e4	0/15
(1,2 ^s)-CMA-ES	∞ ∞ ∞ ∞ ∞ .5.0e4	0/15
f_{118}	430 1200 1600 2000 2400 2900	15/15
(1,2)-CMA-ES	9.2 6.5 6.4 7.8 8.2 8.8	15/15
(1,2 ^s)-CMA-ES	<i>18</i> 10 16 19 39 44	5/15
f_{119}	12 660 1100 1.0e43.5e4 5.0e4	15/15
(1,2)-CMA-ES	15 7.8 86 ∞ ∞ ∞ .5.0e4	0/15
(1,2 ^s)-CMA-ES	<i>34</i> 10 630 ∞ ∞ ∞ .5.0e4	0/15
f_{120}	16 2900 1.9e47.2e43.3e5 5.5e5	15/15
(1,2)-CMA-ES	77 33 ∞ ∞ ∞ ∞ .5.0e4	0/15
(1,2 ^s)-CMA-ES	<i>51</i> 34 ∞ ∞ ∞ ∞ .5.0e4	0/15
f_{121}	8.6 110 270 1600 3900 6200	15/15
(1,2)-CMA-ES	4.5 2.9 1.9 2.9 4.5 9	4/15
(1,2 ^s)-CMA-ES	<i>5.3</i> 2.9 2.2 5.7 9.4 27	2/15
f_{122}	10 1700 9200 3.0e45.4e4 1.1e5	15/15
(1,2)-CMA-ES	11 30 ∞ ∞ ∞ ∞ .5.0e4	0/15
(1,2 ^s)-CMA-ES	<i>38</i> 40 ∞ ∞ ∞ ∞ .5.0e4	0/15
f_{123}	11 1.6e48.2e43.4e56.7e5 2.2e6	15/15
(1,2)-CMA-ES	75 ∞ ∞ ∞ ∞ .5.0e4	0/15
(1,2 ^s)-CMA-ES	<i>87</i> ∞ ∞ ∞ ∞ .5.0e4	0/15
f_{124}	9.7 200 1000 2.0e44.5e4 9.5e4	15/15
(1,2)-CMA-ES	11 130 700 ∞ ∞ ∞ .5.0e4	0/15
(1,2 ^s)-CMA-ES	<i>96</i> 280 ∞ ∞ ∞ ∞ .5.0e4	0/15
f_{125}	1 1 1 2.4e52.4e5 2.5e5	15/15
(1,2)-CMA-ES	1 120 5.9e4 ∞ ∞ ∞ .5.0e4	0/15
(1,2 ^s)-CMA-ES	<i>1</i> 250 1.0e5 ∞ ∞ ∞ .5.0e4	0/15
f_{126}	1 1 1 ∞ ∞ ∞ 0	0
(1,2)-CMA-ES	1.12e37.4e5 ∞ ∞ ∞ 0	0/15
(1,2 ^s)-CMA-ES	<i>32</i> 580 7.2e5 ∞ ∞ ∞ 0	0/15
f_{127}	1 1 1 3.4e53.9e5 4.0e5	15/15
(1,2)-CMA-ES	1 85 1.4e4 ∞ ∞ ∞ .5.0e4	0/15
(1,2 ^s)-CMA-ES	<i>1</i> 3.60 3.8e4 ∞ ∞ ∞ .5.0e4	0/15
f_{128}	110 4200 7800 1.2e41.7e4 2.1e4	15/15
(1,2)-CMA-ES	4.8 5.9 9.6 29 ∞ ∞ ∞ .5.0e4	0/15
(1,2 ^s)-CMA-ES	<i>9.7</i> 4.8 21 60 ∞ ∞ ∞ .5.0e4	0/15
f_{129}	64 1.1e45.9e42.8e55.1e5 5.8e5	15/15
(1,2)-CMA-ES	170 ∞ ∞ ∞ ∞ ∞ .5.0e4	0/15
(1,2 ^s)-CMA-ES	<i>190</i> 70 ∞ ∞ ∞ ∞ ∞ .5.0e4	0/15
f_{130}	55 810 3000 3.3e43.4e4 3.5e4	10/15
(1,2)-CMA-ES	14 48 23 2.9 2.8 3.6	5/15
(1,2 ^s)-CMA-ES	<i>37</i> 58 41 3.8 3.8 3.8	5/15

20-D

Δf	1e+11e+0 1e-1 1e-3 1e-5 1e-7	#succ
f_{101}	59 360 510 700 740 780	15/15
(1,2)-CMA-ES	17 4 3.7 4 5 5.8	15/15
(1,2 ^s)-CMA-ES	<i>16</i> 3.7 3.2 3.5 4.5 5.4	15/15
f_{102}	230 400 580 920 1200 1400	15/15
(1,2)-CMA-ES	5 4.1 3.7 4.1* 5.3*² 9.8*²	15/15
(1,2 ^s)-CMA-ES	<i>6</i> 4.7 4.4 7.4 18 50	12/15
f_{103}	65 420 630 1300 1900 2500	14/15
(1,2)-CMA-ES	18 3.7 3.1 2.2 2.1 2	15/15
(1,2 ^s)-CMA-ES	<i>15</i> 3.1 2.7 2.1 2 1.9	15/15
f_{104}	2.4e48.6e41.7e51.8e5 1.9e5 2.0e5	15/15
(1,2)-CMA-ES	63 ∞ ∞ ∞ ∞ ∞ .2.0e5	0/15
(1,2 ^s)-CMA-ES	<i>120</i> ∞ ∞ ∞ ∞ ∞ .2.0e5	0/15
f_{105}	1.9e56.1e56.3e56.5e5 6.6e5 6.7e5	15/15
(1,2)-CMA-ES	16 4.9 ∞ ∞ ∞ ∞ .2.0e5	0/15
(1,2 ^s)-CMA-ES	<i>16</i> ∞ ∞ ∞ ∞ ∞ .2.0e5	0/15
f_{106}	1.1e42.2e42.4e2.5e4 2.6e4 2.7e4	15/15
(1,2)-CMA-ES	2.3 3.9 3.9 4.1 4.1 4.1	14/15
(1,2 ^s)-CMA-ES	<i>2.2</i> 3.9 3.9 3.9 3.8 3.8	14/15
f_{107}	8600 1.4e41.6e42.7e4 5.2e4 6.5e4	15/15
(1,2)-CMA-ES	∞ ∞ ∞ ∞ ∞ .2.0e5	0/15
(1,2 ^s)-CMA-ES	∞ ∞ ∞ ∞ ∞ .2.0e5	0/15
f_{108}	5.8e49.7e42.0e54.5e5 6.3e5 9.0e5	15/15
(1,2)-CMA-ES	∞ ∞ ∞ ∞ ∞ .2.0e5	0/15
(1,2 ^s)-CMA-ES	∞ ∞ ∞ ∞ ∞ .2.0e5	0/15
f_{109}	330 630 1100 2300 3600 5000	15/15
(1,2)-CMA-ES	3.6 3.5 2.7 2.4 2.3 2.2	15/15
(1,2 ^s)-CMA-ES	<i>3.4</i> 2.8 2.3 2 1.8 1.8*	15/15
f_{110}	∞ ∞ ∞ ∞ ∞ ∞	0
(1,2)-CMA-ES	∞ ∞ ∞ ∞ ∞ ∞	0/15
(1,2 ^s)-CMA-ES	∞ ∞ ∞ ∞ ∞ ∞	0/15
f_{111}	∞ ∞ ∞ ∞ ∞ ∞	0
(1,2)-CMA-ES	∞ ∞ ∞ ∞ ∞ ∞	0/15
(1,2 ^s)-CMA-ES	∞ ∞ ∞ ∞ ∞ ∞	0/15
f_{112}	2.6e46.4e47.0e47.4e4 7.6e4 7.8e4	15/15
(1,2)-CMA-ES	3.1 8.4 20 40 39 38	1/15
(1,2 ^s)-CMA-ES	<i>3.811</i> 43 ∞ ∞ .2.0e5	0/15
f_{113}	5.0e43.6e55.6e56.5e5 5.9e5 5.9e5	15/15
(1,2)-CMA-ES	∞ ∞ ∞ ∞ ∞ .2.0e5	0/15
(1,2 ^s)-CMA-ES	∞ ∞ ∞ ∞ ∞ .2.0e5	0/15
f_{114}	2.1e51.1e61.4e61.6e6 1.6e6 1.6e6	15/15
(1,2)-CMA-ES	∞ ∞ ∞ ∞ ∞ .2.0e5	0/15
(1,2 ^s)-CMA-ES	∞ ∞ ∞ ∞ ∞ .2.0e5	0/15
f_{115}	2400 3.0e49.2e42.1.3e5 1.3e5 1.3e5	15/15
(1,2)-CMA-ES	1.2e3 ∞ ∞ ∞ ∞ .2.0e5	0/15
(1,2 ^s)-CMA-ES	∞ ∞ ∞ ∞ ∞ .2.0e5	0/15
f_{116}	5.0e56.9e58.9e5 1.0e6 1.1e6 1.1e6	15/15
(1,2)-CMA-ES	∞ ∞ ∞ ∞ ∞ .2.0e5	0/15
(1,2 ^s)-CMA-ES	∞ ∞ ∞ ∞ ∞ .2.0e5	0/15
f_{117}	1.8e62.5e62.6e62.9e6 3.2e6 3.6e6	15/15
(1,2)-CMA-ES	∞ ∞ ∞ ∞ ∞ .2.0e5	0/15
(1,2 ^s)-CMA-ES	∞ ∞ ∞ ∞ ∞ .2.0e5	0/15
f_{118}	6900 1.2e41.8e42.6e4 3.0e4 3.3e4	15/15
(1,2)-CMA-ES	4.610 20 55 98 ∞ ∞ .2.0e5	0/15
(1,2 ^s)-CMA-ES	<i>5.114</i> 13 56 ∞ ∞ .2.0e5	0/15
f_{119}	2800 2.9e43.6e44.1e5 1.4e6 1.9e6	15/15
(1,2)-CMA-ES	∞ ∞ ∞ ∞ ∞ .2.0e5	0/15
(1,2 ^s)-CMA-ES	∞ ∞ ∞ ∞ ∞ .2.0e5	0/15
f_{120}	3.6e41.8e52.8e5 1.6e6 6.7e6 1.4e7	13/15
(1,2)-CMA-ES	∞ ∞ ∞ ∞ ∞ .2.0e5	0/15
(1,2 ^s)-CMA-ES	∞ ∞ ∞ ∞ ∞ .2.0e5	0/15
f_{121}	250 770 1400 9300 3.4e4 5.7e4	15/15
(1,2)-CMA-ES	4.8 3.4 3 1.9 3.8 ∞ .2.0e5	0/15
(1,2 ^s)-CMA-ES	<i>4.5</i> 2.8 2.7 1.5 3.8 ∞ .2.0e5	0/15
f_{122}	690 5.2e41.4e57.9e5 2.0e6 5.8e6	15/1