

Comparison Tables: BBOB 2009 Function Testbed

Anne Auger, Steffen Finck, Nikolaus Hansen, Raymond Ros

▶ To cite this version:

Anne Auger, Steffen Finck, Nikolaus Hansen, Raymond Ros. Comparison Tables: BBOB 2009 Function Testbed. [Technical Report] RT-0383, 2010. inria-00471251v1

HAL Id: inria-00471251 https://inria.hal.science/inria-00471251v1

Submitted on 7 Apr 2010 (v1), last revised 13 Apr 2010 (v2)

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.



INSTITUT NATIONAL DE RECHERCHE EN INFORMATIQUE ET EN AUTOMATIQUE

Comparison Tables: BBOB 2009 Function Testbed

Anne Auger — Steffen Finck — Nikolaus Hansen — Raymond Ros

N° 0383 April 2010 Domaine 1 *Comparing or t te chnique*



INSTITUT NATIONAL

DE RECHERCHE EN INFORMATIQUE ET EN AUTOMATIQUE

Comparison Tables: BBOB 2009 Function Testbed

Anne Auger, Steffen Finck, Nikolaus Hansen, Raymond Ros

Domaine : Mathématiques appliquées, calcul et simulation Équipe-Projet TAO

Rapport technique n° 0383 — April 2010 — 150 pages

Abstract: This document presents the results in the form of tables from the Black-Box Optimization Benchmarking (BBOB) workshop of the Genetic and Evolutionary Computation Conference (GECCO), Montreal Canada, 2009. Each table presents the comparative performances of the algorithms submitted to BBOB 2009 on one problem from the function testbed.

Key-words: continuous optimization, benchmarking

Anne Auger, Nikolaus Hansen and Raymond Ros are affiliated to the TAO team-project, INRIA Saclay - Ile-de-France, Université Paris Sud, LRI, F-91405 Orsay Cedex, France.

Steffen Finck is affiliated to the Research Center PPE, University of Applied Science Vorarlberg, Hochschulstrasse 1, 6850 Dornbirn, Austria.

> Centre de recherche INRIA Saclay – Île-de-France Parc Orsay Université 4, rue Jacques Monod, 91893 ORSAY Cedex Téléphone : +33 1 72 92 59 00

Tables de comparaison: suite de fonctions tests BBOB 2009

Résumé : Ce document présente les résultats sous forme de table du workshop Black-Box Optimization Benchmarking (BBOB) de la conférence Genetic and Evolutionary Computation Conference (GECCO), Montréal Canada, 2009. Chaque table présente les performances des algorithmes soumis à BBOB 2009 pour un problème de la suite de fonctions tests.

Mots-clés : optimisation continue, banc d'essai

This document provides tabular results of the workshop for Black-Box Optimization Benchmarking (BBOB) at GECCO 2009¹. More than 30 algorithms have been tested on 24 benchmark functions in dimensions between 2 and 40. A description of the used objective functions can be found in [14, 9]. The experimental set-up is described in [13].

The performance measure provided in the following tables is the expected number of objective function evaluations to reach a given target function value (ERT, expected running time), divided by the respective value for the best algorithm. Consequently, the best (smallest) value is 1 and the value 1 appears in each column at least once. See [13] for details on how ERT is obtained. All numbers are computed with no more than two digits of precision.

¹see http://coco.gforge.inria.fr/doku.php?id=bbob-2009

	1 Sphere													
	$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$		
	ERT_{best}/D	0.5	0.5	0.9	2.83	2.83	3	3	3	3	3	ERT_{best}/D		
-	ALPS	1	1	2.8	9.7	56	170	290	440	640	970	ALPS [17]		
	AMaLGaM IDEA	1	1.1	2.1	4.4	11	14	23	28	32	46	AMaLGaM IDÉA [4]		
	avg NEWUOA	1	1	1.9	1.1	1.1	1	1	1	1	1	avg NEWUOA [31]		
	BayEDAcG	1	1	1.9	4.2	18	79	110	140	160	210	BayEDAcG [10]		
	BFGS	1	1	3.3	1.2	1.2	1.2	1.2	1.2	1.2	1.2	BFGS [30]		
	Cauchy EDA	1	1	19	15	27	39	50	63	75	100	Cauchy EDA [24]		
	BIPOP-CMA-ES	1	1	3.3	3.8	8.5	13	19	24	29	39	BIPOP-CMA-ES [15]		
	(1+1)-CMA-ES	1	1	3.3	3.6	7.6	11	14	18	22	29	(1+1)-CMA-ES [2]		
	DASA	1	1	39	23	44	52	62	76	95	120	DASA [19]		
	DEPSO	1	1	2.1	12	27	46	51	96	120	170	DEPSO [12]		
	DIRECT	1	1	1	1.4	2.5	9.4	15	20	32	56	DIRECT [25]		
	EDA-PSO	1	1	1.9	5	20	34	53	80	110	210	EDA-PSO [6]		
	full NEWUOA	1	1	2.7	1.2	1.2	1.2	1.2	1.2	1.2	1.2	full NEWUOA [31]		
	G3-PCX	1	1	1.9	6	17	19	24	29	34	46	G3-PCX [26]		
	simple GA	1	1	2.7	7.2	62	310	1100	1800	2600	4500	simple GA [22]		
	GLOBAL	1	1	1.9	5.7	39	50	54	55	56	58	GLOBAL [23]		
	iAMaLGaM IDEA	1	1	2.3	3.8	6.7	12	14	19	22	31	iAMaLGaM IDEA [4]		
	LSfminbnd	1	1	7.8	3.2	3.6	4.1	4.1	4.1	4.1	4.1	LSfminbnd [28]		
	LSstep	1	1	46	34	62	63	68	68	69	69	LSstep [28]		
	MA-LS-Chain	1	1	2.4	7.4	26	40	67	85	92	100	MA-LS-Chain [21]		
	MCS (Neum)	1	1	1	1.5	2.2	2.6	2.6	2.6	2.6	2.6	MCS (Neum) [18]		
	NELDER (Han)	1	1	2.1	1.3	3	3.9	5.1	6.3	7.4	9.8	NELDER (Han) [16]		
	NELDER (Doe)	1	1	1	1.5	2.9	4.1	5.3	6.5	7.6	10	NELDER (Doe) [5]		
	NEWUOA	1	1	2.8	1	1	1	1	1	1	1	NEWUOA [31]		
	(1+1)-ES	1	1	3.5	2.8	6.7	10	14	18	23	30	(1+1)-ES [1]		
	POEMS	1	1	170	80	110	400	680	1100	1300	2100	POEMS [20]		
	PSO	1	1	2.1	5.3	20	59	120	200	250	470	PSO [7]		
	PSO_Bounds	1	1.1	2.4	6	26	89	270	460	770	1200	PSO_Bounds [8]		
	Monte Carlo	1	1	1.5	9.7	49	540	5900	4.8e4	6.8e5	11e-6/1e6	Monte Carlo [3]		
	Rosenbrock	1	1	5.6	3.1	3.9	4.9	6.2	7.6	8.8	11	Rosenbrock [27]		
	IPOP-SEP-CMA-ES	1	1	3.9	5.9	9.5	14	18	24	28	38	IPOP-SEP-CMA-ES [29]		
	VNS (Garcia)	1	1	2.6	8.9	25	33	37	43	48	60	VNS (Garcia) [11]		

Table 1: 02-D, running time excess ERT/ERT_{best} on f_1 , in italics is given the median final function value and the median number	of
function evaluations to reach this value divided by dimension	

4

2 Ellipsoid separable												
Δ ftarget	1e + 03	1e + 02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$	
ERT_{hest}/D	4.93	6.23	8.2	9.47	12.3	12.7	12.9	13.6	14	14.3	ERT_{hest}/D	
ALPS	11	24	58	120	130	160	200	230	260	330	ALPS [17]	
AMaLGaM IDEA	4.9	4.8	6.2	7.6	7.5	9.1	10	11	13	16	AMaLGaM IDEA [4]	
avg NEWUOA	1.2	1.1	1.9	5.6	8.5	10	14	17	20	27	avg NEWUOA [31]	
BayEDAcG	37	62	80	78	82	87	110	110	140	140	BayEDAcG [10]	
BFGS	1.7	1.6	2.5	4	3.7	3.9	4.1	4.1	4.1	4.4	BFGS [30]	
Cauchy EDA	13	17	18	18	18	20	23	24	25	29	Cauchy EDA [24]	
BIPOP-CMA-ES	4	5.4	13	19	18	18	20	20	20	22	BIPOP-CMA-ES [15]	
(1+1)-CMA-ES	4.1	5.1	10	13	13	13	14	14	15	16	(1+1)-CMA-ES [2]	
DASA	21	19	19	22	21	21	23	25	26	31	DASA [19]	
DEPSO	10	16	18	26	27	31	35	40	45	53	DEPSO [12]	
DIRECT	5.9	5.1	7.5	8	7.1	8.5	9.4	12	13	46	DIRECT [25]	
EDA-PSO	8.8	11	13	19	20	26	39	49	65	88	EDA-PSO [6]	
full NEWUOA	1.2	1.2	2.4	5.8	8.3	10	13	15	18	23	full NEWUOA [31]	
G3-PCX	8.6	8.4	14	64	69	76	83	82	82	82	G3-PCX [26]	
simple GA	11	44	130	320	420	540	780	990	1300	1900	simple GA [22]	
GLOBAL	11	19	19	17	13	13	13	13	13	13	GLOBAL [23]	
iAMaLGaM IDEA	2.6	3.8	5.1	9.2	9.1	10	11	12	12	14	iAMaLGaM IDEA [4]	
LSfminbnd	1.4	1.2	1	1	1	1	1	1	1	1	LSfminbnd [28]	
LSstep	14	12	9.5	9.9	7.9	7.9	7.8	7.5	7.3	7.3	LSstep [28]	
MA-LS-Chain	12	14	17	22	20	24	28	28	29	34	MA-LS-Chain [21]	
MCS (Neum)	1.5	1.6	1.4	1.8	1.7	2.6	3.2	3.3	3.7	23	MCS (Neum) [18]	
NELDER (Han)	1.9	1.8	1.7	1.8	1.8	2	2.2	2.4	2.6	3	NELDER (Han) [16]	
NELDER (Doe)	1.6	1.7	1.6	1.9	1.7	1.9	2.2	2.3	2.5	3	NELDER (Doe) [5]	
NEWUOA	1	1	2.2	8.8	12	15	19	23	26	35	NEWUOA [31]	
(1+1)-ES	3.2	2400	8700	4.7e4	1.2e5	3.8e5	74e-3/1e6				(1+1)-ES [1]	
POEMS	140	250	380	420	400	460	510	570	630	780	POEMS [20]	
PSO	7.5	14	56	83	83	98	120	130	160	200	PSO [7]	
PSO_Bounds	6.9	24	54	170	310	360	400	440	530	780	PSO_Bounds [8]	
Monte Carlo	21	50	240	1200	5600	1e5	94e-4/1e6				Monte Carlo [3]	
Rosenbrock	2.6	3.1	2.5	3.7	4.4	5.4	6.3	6.5	6.9	7.9	Rosenbrock [27]	
IPOP-SEP-CMA-ES	4.5	5.4	14	19	16	17	18	18	18	20	IPOP-SEP-CMA-ES [29]	
VNS (Garcia)	8.4	15	22	27	24	25	26	26	26	29	VNS (Garcia) [11]	

Table 2: 02-D, running time excess ERT/ERT_{best} on f_2 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension **2 Ellipsoid separable** $\Delta ftarget$ 1e+03 1e+02 1e+01 1e+00 1e-01 1e-02 1e-03 1e-04 1e-05 1e-07 $\Delta ftarget$

3: 02-D, running	g time exces	s ERT/	ERT _{bes}	t on f_3 , dimens	in ital	lics is g	iven th	e median fi	inal fur	nction v	value and the median			
3 Rastrigin separable														
Δ ftarget	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget			
ERT _{best} /D	0.5	0.7	7.33	135	222	223	225	226	227	232	ERT _{best} /D			
ALPS	1.1	1.6	9.2	6.7	6.4	11	12	15	19	23	ALPS [17]			
AMaLGaM ID	EA 1.1	1.1	3.7	4.6	12	12	12	12	13	13	AMaLGaM IDEA [4]			
avg NEWUO	A 1	2.7	5.1	1.6	3.2	3.2	3.2	3.2	3.2	3.1	avg NEWUOA [31]			
BayEDAcG	1.1	1.2	4.4	4	9.7	18	41	65	65	64	BayEDAcG [10]			
BFGS	1.2	18	14	3.1	10	10	10	10	10	10	BFGS [30]			
Cauchy EDA	1.1	9.6	9.6	3.3	8.4	33	43	43	43	43	Cauchy EDA [24]			
BIPOP-CMA-	ES 1	2.2	3.5	3.5	5.2	6.2	6.4	6.5	6.5	6.7	BIPOP-CMA-ES [15]			
(1+1)-CMA-E	S 1	1.9	6.9	3.8	7.9	7.9	7.9	7.9	7.9	7.8	(1+1)-CMA-ES [2]			
DASA	6.3	22	18	1.8	6.9	7	7.1	7.2	7.4	7.6	DASA [19]			
DEPSO	1.8	2	5.7	2.3	2.7	4	4.5	5	5.4	6.4	DEPSO [12]			
DIRECT	1	1.1	2.7	1	2.4	2.4	2.5	2.6	2.7	3	DIRECT [25]			
EDA-PSO	1.2	1.4	4.8	6.4	14	19	20	20	21	22	EDA-PSO [6]			
full NEWUO.	A 1	4	2.3	1.8	2.2	2.2	2.2	2.1	2.1	2.1	full NEWUOA [31]			
G3-PCX	1.1	2	4.1	7.8	40	40	39	39	39	39	G3-PCX [26]			
simple GA	1	2	8.3	13	19	27	40	55	70	110	simple GA [22]			
GLOBAL	1.1	1.6	7	1.8	3.1	3.1	3.1	3.1	3.1	3.1	GLOBAL [23]			
iAMaLGaM ID	EA 1.1	1.4	1.8	6.3	17	17	17	17	17	17	iAMaLGaM IDEA [4]			
LSfminbnd	2.1	4.7	17	32	43	64	63	63	63	61	LSfminbnd [28]			
LSstep	28	120	24	1.5	1	1	1	1	1	1	LSstep [28]			
MA-LS-Chair	n 1	1.5	5.7	1.7	2.5	2.6	2.7	2.7	2.8	2.9	MA-LS-Chain [21]			
MCS (Neum) 1	1.1	1.5	1.1	1.5	1.6	1.6	2.6	2.6	2.6	MCS (Neum) [18]			
NELDER (Ha	n) 1.2	1.8	1.4	4	13	13	13	13	12	12	NELDER (Han) [16]			
NELDER (Do	e) 1	1	1	1	1.7	1.8	1.8	1.8	1.8	1.8	NELDER (Doe) [5]			
NEWUOA	1.5	2.4	4.8	1.5	4.2	4.2	4.2	4.1	4.1	4.1	NEWUOA [31]			
(1+1)-ES	1.1	2.4	12	5	15	15	15	15	15	14	(1+1)-ES [1]			
POEMS	31	200	42	11	14	20	24	29	32	41	POEMS [20]			
PSO	1.1	1.6	5.1	3.3	3.4	4.7	6	7.2	8.8	11	PSO [7]			
PSO_Bounds	3 1.1	1.8	4.8	5.3	8.3	14	18	22	26	34	PSO_Bounds [8]			
Monte Carlo	1.1	1.5	14	67	460	3100	2.1e4	39e-4/1e6			Monte Carlo [3]			
Rosenbrock	1	16	45	15	26	26	26	26	26	25	Rosenbrock [27]			
IPOP-SEP-CMA	-ES 1	1.5	2.3	3.4	7.6	8.4	9.2	9.4	9.6	9.8	IPOP-SEP-CMA-ES [29]			
VNS (Garcia) 1	1.9	8.8	2.9	4.1	4.2	4.2	4.5	4.7	7.7	VNS (Garcia) [11]			

Comparison Tables: BBOB 2009 Function Testbed

4 Skew Rastrigin-Bueche separable														
Δ ftarget 1e+03 1e+02 1e+01 1e+00 1e-01 1e-02 1e-03 1e-04 1e-05 1e-07 Δ ftarget														
ERT_{hest}/D	0.5	0.5	10.9	172	230	248	261	270	272	283	ERT_{hest}/D			
ALPS	1	2.5	9	7.1	8.3	9.7	12	15	17	20	ALPS [17]			
AMaLGaM IDEA	1	2.2	2.6	5.6	51	48	48	46	47	45	AMaLGaM IDÉA [4]			
avg NEWUOA	1	4.5	6.2	4	14	13	12	12	12	11	avg NEWUOA [31]			
BayEDAcG	1	2.3	4.5	13	62	120	110	10e-1/2e3			BayEDAcG [10]			
BFGS	1	13	11	5.7	12	11	11	10	10	9.8	BFGS [30]			
Cauchy EDA	1	19	6.8	13	75	410	470	450	450	430	Cauchy EDA [24]			
BIPOP-CMA-ES	1	3.8	2.6	6.9	55	97	99	98	99	110	BIPOP-CMA-ES [15]			
(1+1)-CMA-ES	1	2.4	5.2	5.5	27	25	24	23	23	22	(1+1)-CMA-ES [2]			
DASA	1	82	15	2	3.6	3.4	3.3	3.3	3.4	3.4	DASA [19]			
DEPSO	1	2.4	7.2	4.2	6.5	11	17	17	17	35	DEPSO [12]			
DIRECT	1	1	1.8	1.8	6.6	6.1	14	14	16	16	DIRECT [25]			
EDA-PSO	1	2.6	4.2	9.9	18	19	19	19	19	20	EDA-PSO [6]			
full NEWUOA	1	3.8	5.4	3.9	15	14	13	13	13	12	full NEWUOA [31]			
G3-PCX	1	2.1	20	17	76	70	67	65	64	62	G3-PCX [26]			
simple GA	1	2.6	10	16	22	28	37	49	60	100	simple GA [22]			
GLOBAL	1	2.4	8.5	1.2	5.2	4.8	4.6	4.5	4.5	4.3	GLOBAL [23]			
iAMaLGaM IDEA	1	3.8	2.5	9.5	61	57	56	55	55	54	iAMaLGaM IDEA [4]			
LSfminbnd	1	4.6	1	45	120	230	10e-1/4e3				LSfminbnd [28]			
LSstep	1	220	19	1.3	1	1	1	1	1	1	LSstep [28]			
MA-LS-Chain	1	2.3	5.6	1.8	4.4	4.2	4.1	4	4.1	4.1	MA-LS-Chain [21]			
MCS (Neum)	1	1	2	1	2.9	2.7	2.7	2.7	2.7	2.6	MCS (Neum) [18]			
NELDER (Han)	1	3.1	5	5.3	27	25	24	23	23	22	NELDER (Han) [16]			
NELDER (Doe)	1	2.1	1.9	1.4	3.5	3.2	3.1	3	3	3	NELDER (Doe) [5]			
NEWUOA	1	3	5	4.5	18	16	16	15	15	14	NEWUOA [31]			
(1+1)-ES	1	3.1	4.5	5.5	23	21	20	20	20	19	(1+1)-ES [1]			
POEMS	1	240	36	9.8	22	23	29	32	35	41	POEMS [20]			
PSO	1.1	3.2	4	3.3	4.6	5.6	6.4	7.4	8.7	11	PSO [7]			
PSO_Bounds	1	3.3	4.4	6.3	9.6	17	21	24	27	33	PSO_Bounds [8]			
Monte Carlo	1	3.3	8.6	67	620	8200	2.8e4	5.5e4	11e-3/1e6		Monte Carlo [3]			
Rosenbrock	1	71	27	15	52	48	46	44	44	42	Rosenbrock [27]			
IPOP-SEP-CMA-ES	1	3.5	3	8.7	75	180	270	260	260	250	IPOP-SEP-CMA-ES [29]			
VNS (Garcia)	1	2.6	5.1	4.1	8.8	8.2	7.9	8.3	8.8	17	VNS (Garcia) [11]			

Table 4: 02-D, running time excess ERT/ERT_{best} on f_4 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

5 Linear slope													
Δ ftarg	et 1e+03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget		
ERThes	$_{\rm t}/{\rm D}$ 0.5	0.5	1.83	2.2	2.2	2.2	2.2	2.2	2.2	2.2	ERT_{best}/D		
ALP	5 1	1.1	8.8	76	100	100	100	100	100	100	ALPS [17]		
AMaLGaM	IDEA 1	1.1	5.3	16	18	18	18	18	18	18	AMaLGaM IDÉA [4]		
avg NEW	UOA 1	1.2	1.1	1.5	1.6	1.6	1.6	1.6	1.6	1.6	avg NEWUOA [31]		
BayEDA	AcG 1	1	3.3	92	100	100	100	100	100	100	BayEDAcG [10]		
BFG	5 1	1	1.5	2.8	2.8	2.9	2.9	2.9	2.9	2.9	BFGS [30]		
Cauchy 1	EDA 1	1	16	17	17	17	17	17	17	17	Cauchy EDA [24]		
BIPOP-CM	AA-ES 1	1	3.4	5.3	5.7	5.8	5.8	5.8	5.8	5.8	BIPOP-CMA-ES [15]		
(1+1)-CM	IA-ES 1	1	1.9	3.1	3.4	3.4	3.4	3.4	3.4	3.4	(1+1)-CMA-ES [2]		
DASA	A 1	1.9	19	32	40	46	53	60	66	80	DASA [19]		
DEPS	0 1	1	6.1	34	35	36	36	36	36	36	DEPSO [12]		
DIREC	CT 1	1	3.4	2.8	4.2	4.2	4.2	4.2	4.2	4.2	DIRECT [25]		
EDA-P	SO 1	1	5	15	16	17	17	17	17	17	EDA-PSO [6]		
full NEW	UOA 1	1.3	1	1.2	1.4	1.4	1.4	1.4	1.4	1.4	full NEWUOA [31]		
G3-PC	X 1	1.1	4.1	29	31	31	31	31	31	31	G3-PCX [26]		
simple	GA 1	1	4.2	310	2e3	4200	6300	9800	1.5e4	6.8e5	simple GA [22]		
GLOB.	AL 1	1.1	4.4	69	70	70	70	70	70	70	GLOBAL [23]		
iAMaLGaN	I IDEA 1	1	4.6	12	13	13	13	13	13	13	iAMaLGaM IDEA [4]		
LSfmin	ond 1	1	4.9	7.3	8.5	9.1	9.1	9.1	9.1	9.1	LSfminbnd [28]		
LSste	p 1	1.2	59	79	91	91	91	91	91	91	LSstep [28]		
MA-LS-C	Chain 1	1.1	4.7	81	120	130	130	130	130	130	MA-LS-Chain [21]		
MCS (Ne	eum) 1	1	1.2	1	1	1	1	1	1	1	MCS (Neum) [18]		
NELDER	(Han) 1	1	1.8	2.1	2.2	2.2	2.2	2.2	2.2	2.2	NELDER (Han) [16]		
NELDER	(Doe) 1	1	1.3	1.9	1.9	1.9	1.9	1.9	1.9	1.9	NELDER (Doe) $[5]$		
NEWU	OA 1	1	1.1	1.5	1.5	1.5	1.5	1.5	1.5	1.5	NEWUOA [31]		
(1+1)-	ES 1	1	1.9	2.4	2.5	2.6	2.6	2.6	2.6	2.6	(1+1)-ES [1]		
POEM	IS 1	1	140	150	170	180	190	190	190	190	POEMS [20]		
PSO	1	1.1	4.2	18	20	21	21	21	21	21	PSO [7]		
PSO_Bo	unds 1	1	6.1	13	16	16	16	16	16	16	PSO_Bounds [8]		
Monte C	arlo 1	1	4.4	530	4.9e4	22e-3/1e6					Monte Carlo [3]		
Rosenbr	ock 1	1	3.5	3.4	3.5	3.5	3.5	3.5	3.5	3.5	Rosenbrock [27]		
IPOP-SEP-0	CMA-ES 1	1	4	6.6	7.1	7.1	7.1	7.1	7.1	7.1	IPOP-SEP-CMA-ES [29]		
VNS (Ga	rcia) 1	1	6.3	27	27	27	27	27	27	27	VNS (Garcia) [11]		

Table 5: 02-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_5 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

6 Attractive sector													
Δ ftarget	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget		
ERT_{best}/D	0.833	1.4	6.33	11.4	20.5	26.9	33.5	39.9	47.3	62.2	ERT_{best}/D		
ALPS	3.2	3.2	2.2	12	31	50	62	73	80	83	ALPS [17]		
AMaLGaM IDEA	1.1	1.4	2.1	4.5	4.9	5.5	6.2	6.5	6.7	7	AMaLGaM IDEA [4]		
avg NEWUOA	1.4	2.1	3.1	4.7	3.9	4.4	4.4	4.5	4.7	4.6	avg NEWUOA [31]		
BayEDAcG	2.8	1.9	1.5	160	640	72e-2/2e3					BayEDAcG [10]		
BFGS	4.3	4.4	4.2	3.4	2.7	2.4	2	1.9	1.7	1.6	BFGS [30]		
Cauchy EDA	11	10	16	18	17	17	17	17	16	16	Cauchy EDA [24]		
BIPOP-CMA-ES	3.9	3	2	2.8	3.6	3.9	4.2	4.2	4.1	4.3	BIPOP-CMA-ES [15]		
(1+1)-CMA-ES	4.2	3.3	2.1	3	2.3	2.2	2.2	2.3	2.2	2.1	(1+1)-CMA-ES [2]		
DASA	30	29	23	22	18	19	19	18	18	18	DASA [19]		
DEPSO	1.7	1.7	3.8	11	12	14	14	15	16	17	DEPSO [12]		
DIRECT	1.4	1	1.4	7.6	5.8	120	800	1500	1200	970	DIRECT [25]		
EDA-PSO	3.4	2.4	3.1	12	12	15	19	27	29	34	EDA-PSO [6]		
full NEWUOA	1	2.2	3.4	3.7	3.2	3.5	3.7	3.7	4.1	4.5	full NEWUOA [31]		
G3-PCX	2.3	1.5	2.3	4.5	3.7	3.9	3.9	3.8	3.8	4.1	G3-PCX [26]		
simple GA	4.8	3.4	3.5	14	85	1e3	3100	4100	3600	4900	simple GA [22]		
GLOBAL	3.7	2.9	2.3	8.8	7.4	6.2	5.2	4.5	3.9	3.2	GLOBAL [23]		
iAMaLGaM IDEA	2.7	1.9	2.4	3.6	3.8	4	4.1	4.2	4.3	4.4	iAMaLGaM IDEA [4]		
LSfminbnd	19	190	280	370	290	260	210	180	150	120	LSfminbnd [28]		
LSstep	53	330	910	580	380	330	710	1200	17e-4/1e4		LSstep [28]		
MA-LS-Chain	4.4	2.9	2.2	13	14	14	12	12	10	10	MA-LS-Chain [21]		
MCS (Neum)	1.4	190	52	29	19	42	100	110	100	120	MCS (Neum) [18]		
NELDER (Han)	2.1	1.5	1	1	1.1	1.1	1.1	1.1	1.1	1.1	NELDER (Han) [16]		
NELDER (Doe)	1.6	2	1.3	1.3	1	1	1	1	1	1	NELDER (Doe) $[5]$		
NEWUOA	1.2	2.4	4.4	4.7	3.9	4.4	4.7	4.8	5	4.9	NEWUOA [31]		
(1+1)-ES	2.4	2.2	2.5	3.7	3.6	3.6	3.4	3.4	3.3	3.2	(1+1)-ES [1]		
POEMS	200	160	99	130	120	140	130	140	180	180	POEMS [20]		
PSO	1.5	1.1	2.1	4.6	7.9	18	23	29	32	36	PSO [7]		
PSO_Bounds	2.2	1.5	2.6	7	37	77	130	140	140	170	PSO_Bounds [8]		
Monte Carlo	3	2.3	2.7	16	53	780	1.3e4	8.1e4	1.5e5	28e-5/1e6	Monte Carlo [3]		
Rosenbrock	4	3	2.2	2.1	1.8	1.8	1.8	1.8	1.7	1.5	Rosenbrock [27]		
IPOP-SEP-CMA-ES	4.7	3.1	1.7	4.1	3.8	4.5	4.6	4.7	4.6	4.4	IPOP-SEP-CMA-ES [29]		
VNS (Garcia)	2.6	2.7	1.9	7.2	6.9	6.7	6.3	6.3	6.1	5.7	VNS (Garcia) [11]		

Table 6: 02-D, running time excess ERT/ERT _{best}	on f_6 , in italics is	s given the median	final function	value and the media	an number of
function evaluations to reach this value divided by	dimension				

7 Step-ellipsoid													
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$		
ERT _{best} /D	0.5	1	1.6	10.7	30.2	96.7	108	108	108	121	ERT_{best}/D		
ALPS	1.1	1.4	4.1	4.7	12	9.5	11	11	11	13	ALPS [17]		
AMaLGaM IDEA	1.1	1.5	3.4	20	8.1	2.7	2.5	2.5	2.5	2.4	AMaLGaM IDEA [4]		
avg NEWUOA	1.7	2.7	4	3.7	6.8	5	10	10	10	9	avg NEWUOA [31]		
BayEDAcG	1.5	1.7	4.2	3.1	79	85	76	76	76	110	BayEDAcG [10]		
BFGS	1.6	3.7	10	19	34	76e-2/200					BFGS [30]		
Cauchy EDA	5.5	8.4	19	7.6	5.3	2	1.9	1.9	1.9	2.1	Cauchy EDA [24]		
BIPOP-CMA-ES	1.9	1.9	3.2	2.6	3.4	1.5	1.5	1.5	1.5	1.6	BIPOP-CMA-ES [15]		
(1+1)-CMA-ES	1.5	1.4	2.7	1.8	2.8	1	1	1	1	1	(1+1)-CMA-ES [2]		
DASA	30	59	170	170	310	240	440	440	440	390	DASA [19]		
DEPSO	1.7	1.7	6.5	4.8	4.9	2.6	3.1	3.1	3.1	3.6	DEPSO [12]		
DIRECT	1.4	1	2.1	1.3	1	2.7	3	3	3	2.7	DIRECT [25]		
EDA-PSO	1.5	1.8	3.7	3.1	6.2	6.2	9	9	9	14	EDA-PSO [6]		
full NEWUOA	1.9	2.7	2	3.7	3.7	1.7	2.9	2.9	2.9	2.7	full NEWUOA [31]		
G3-PCX	1.3	1.5	4.5	12	35	19	21	21	21	19	G3-PCX [26]		
simple GA	1.6	1.6	5.2	3.9	22	24	47	47	47	67	simple GA [22]		
GLOBAL	1.2	1.8	6.8	4.1	7.5	2.7	4.4	4.4	4.4	3.9	GLOBAL [23]		
iAMaLGaM IDEA	1.8	1.8	3.9	12	4.7	2.8	2.5	2.5	2.5	2.4	iAMaLGaM IDEA [4]		
LSfminbnd	1.3	1.1	6.3	11	66	55	500	500	500	960	LSfminbnd [28]		
LSstep	28	28	260	250	460	1500	29e-3/1e4		•		LSstep [28]		
MA-LS-Chain	1.7	2.3	5.8	3.4	4.7	3.6	4.6	4.6	4.6	4.7	MA-LS-Chain [21]		
MCS (Neum)	1.4	1.4	1	4.1	4.5	2.2	6.5	6.5	6.5	6	MCS (Neum) [18]		
NELDER (Han)	1.5	1.3	2.5	25	18	6.6	6.5	6.5	6.5	5.9	NELDER (Han) [16]		
NELDER (Doe)	1.8	1.6	2.6	1	8.5	5.4	5.2	5.2	5.2	5.4	NELDER (Doe) [5]		
NEWUOA	1.7	2	2.5	9.3	9.3	6	14	14	14	12	NEWUOA [31]		
(1+1)-ES	2.3	3.3	5.6	4.1	4.3	1.8	3.3	3.3	3.3	3	(1+1)-ES [1]		
POEMS	220	210	180	45	41	21	23	23	23	28	POEMS [20]		
PSO	1.5	1.3	4.1	3.5	4.8	3.2	3.6	3.6	3.6	4.4	PSO [7]		
PSO_Bounds	1.3	1.6	6.2	3.4	5.8	5	6.7	6.7	6.7	14	PSO_Bounds [8]		
Monte Carlo	1.7	1.5	4.6	4.5	43	87	150	150	150	950	Monte Carlo [3]		
Rosenbrock	16	42	150	120	170	78	190	190	190	170	Rosenbrock [27]		
IPOP-SEP-CMA-ES	1	2.1	5.5	2.7	2.8	1.2	1.3	1.3	1.3	1.5	IPOP-SEP-CMA-ES [29]		
VNS (Garcia)	1	2.4	3.9	3.8	5.1	2.1	2	2	2	2	VNS (Garcia) [11]		

Table 7: 02-D, running time excess ERT/ERT_{best} on f_7 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

8 Rosenbrock original														
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$														
ERT_{best}/D	0.6	1.6	2.7	6	18.3	23.1	43.2	46.1	47	56	ERT_{hest}/D			
ALPS	2.9	2.8	4.7	19	31	66	54	74	94	130	ALPS [17]			
AMaLGaM IDEA	2.4	4.1	6.2	10	6.8	7	4.4	4.7	5.1	5	AMaLGaM IDEA [4]			
avg NEWUOA	3.9	2.5	2.6	4.6	2.4	2.4	1.4	1.4	1.4	1.3	avg NEWUOA [31]			
BayEDAcG	2.3	2.9	5.6	11	48	350	53e-3 /2e3				BayEDAcG [10]			
BFGS	7.5	4.9	4.1	5.1	2.4	2.2	1.3	1.3	1.3	1.1	BFGS [30]			
Cauchy EDA	15	11	10	24	19	21	12	13	14	13	Cauchy EDA [24]			
BIPOP-CMA-ES	3.1	3.3	3.5	7.1	9.2	11	6.4	6.5	6.7	6.2	BIPOP-CMA-ES [15]			
(1+1)-CMA-ES	6.4	4.3	3.8	11	6.9	7	4.2	4.1	4.3	4	(1+1)-CMA-ES [2]			
DASA	31	33	110	520	480	680	520	580	700	820	DASA [19]			
DEPSO	4	3.3	3.6	14	15	25	28	42	65	76e-7/2e3	DEPSO [12]			
DIRECT	1	1	1.4	5	4.4	8.7	10	16	17	21	DIRECT [25]			
EDA-PSO	1.9	3	5.4	11	50	98	97	140	180	220	EDA-PSO [6]			
full NEWUOA	6.6	3.9	7	7	3.2	2.8	1.6	1.5	1.5	1.3	full NEWUOA [31]			
G3-PCX	2.8	4	5	24	16	18	11	11	11	9.6	G3-PCX [26]			
simple GA	2	2.9	8.4	34	87	170	1300	8900	61e-5/1e5		simple GA [22]			
GLOBAL	4.4	4.5	14	19	8.2	7.2	4.1	3.9	3.9	3.4	GLOBAL [23]			
iAMaLGaM IDEA	2.3	2.8	4.4	12	8	8.4	5	5.2	5.5	5.2	iAMaLGaM IDEA [4]			
LSfminbnd	16	7	420	1500	2300	6300	90e-2/1e4				LSfminbnd [28]			
LSstep	67	51	37	1500	3600	6100	32e-2/1e4				LSstep [28]			
MA-LS-Chain	2.7	3.6	7.2	16	10	15	9	8.8	9	8.5	MA-LS-Chain [21]			
MCS (Neum)	1	1.2	1	1	1	1	1	1	1	1	MCS (Neum) [18]			
NELDER (Han)	1.9	1.4	2.1	3.7	2	2	1.1	1.2	1.2	1.2	NELDER (Han) [16]			
NELDER (Doe)	3	3.2	4.6	6.2	2.9	2.7	1.6	1.5	1.6	1.5	NELDER (Doe) $[5]$			
NEWUOA	3.8	2.8	4.3	7	3.5	3.2	1.9	1.8	1.8	1.6	NEWUOA [31]			
(1+1)-ES	2.3	2.2	47	59	23	34	35	51	70	95	(1+1)-ES [1]			
POEMS	230	110	120	110	76	110	74	91	120	130	POEMS [20]			
PSO	2.7	2.6	6.5	11	16	27	26	37	49	67	PSO [7]			
PSO_Bounds	3.7	4.3	6	19	24	61	69	120	150	200	PSO_Bounds [8]			
Monte Carlo	2.7	3.2	5.8	19	72	670	2200	3.9e4	3.1e5	17e-5/1e6	Monte Carlo [3]			
Rosenbrock	5.8	3.4	4.9	10	5.2	4.8	2.8	2.7	2.8	2.5	Rosenbrock [27]			
IPOP-SEP-CMA-ES	6.4	3.9	5.2	19	17	17	9.5	9.3	9.6	8.7	IPOP-SEP-CMA-ES [29]			
VNS (Garcia)	9.5	4.8	8.1	16	10	11	6.9	6.8	7.2	6.7	VNS (Garcia) [11]			

Table 8: 02-D, running time excess ERT/ERT_{best} on f_8 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

9 Rosenbrock rotated														
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$														
ERT _{best} /D	0.5	0.5	0.5	8.9	15	21.9	33.8	38.5	40.7	46.2	ERT _{best} /D			
ALPS	3.3	7.2	33	19	41	62	64	81	100	140	ALPS [17]			
AMaLGaM IDEA	4.2	13	22	6.3	9.5	9.5	7.5	7.4	7.7	7.6	AMaLGaM IDEA [4]			
avg NEWUOA	7.7	10	22	4.7	4	3.2	2.3	2.1	2	1.9	avg NEWUOA [31]			
BayEDAcG	3.8	11	29	10	99	600	66e-3/2e3				BayEDAcG [10]			
BFGS	4.2	9.2	16	2.4	2.3	1.9	1.4	1.3	1.2	1.1	BFGS [30]			
Cauchy EDA	16	37	59	14	20	19	14	14	14	14	Cauchy EDA [24]			
BIPOP-CMA-ES	2.6	10	19	4.6	7.1	7.5	5.8	5.6	5.8	5.9	BIPOP-CMA-ES [15]			
(1+1)-CMA-ES	3.5	9.9	26	8.8	8	7.3	5.4	5	5	4.9	(1+1)-CMA-ES [2]			
DASA	65	110	320	250	290	330	320	380	550	740	DASA [19]			
DEPSO	2.7	12	58	12	12	20	19	25	45	97	DEPSO [12]			
DIRECT	1	1	1	2	5	5.8	8.3	14	18	25	DIRECT [25]			
EDA-PSO	3.8	12	47	8.5	27	51	78	120	150	200	EDA-PSO [6]			
full NEWUOA	7.1	12	24	2.7	2.2	1.8	1.3	1.2	1.1	1.1	full NEWUOA [31]			
G3-PCX	4.1	10	28	15	20	18	14	13	13	11	G3-PCX [26]			
simple GA	5	15	44	22	90	190	2200	2200	1e4	1.5e4	simple GA [22]			
GLOBAL	3.5	11	30	9.1	11	7.9	5.2	4.7	4.5	4.2	GLOBAL [23]			
iAMaLGaM IDEA	3.1	7.9	29	6	7.2	6.9	5.3	5.1	5.3	5.3	iAMaLGaM IDEA [4]			
LSfminbnd	6.2	15	20	210	670	3100	4100	3600	3400	76e-3/1e4	LSfminbnd [28]			
LSstep	270	610	750	230	670	1800	2100	3800	76e-3/1e4	•	LSstep [28]			
MA-LS-Chain	5	9.5	35	8.6	13	13	11	10	10	11	MA-LS-Chain [21]			
MCS (Neum)	1	1	1	1	1	1	1	1	1	1	MCS (Neum) [18]			
NELDER (Han)	2.7	3.6	10	1.6	2	1.8	1.3	1.2	1.2	1.2	NELDER (Han) [16]			
NELDER (Doe)	4.1	6.9	11	2.3	2.6	2.1	1.5	1.4	1.4	1.4	NELDER (Doe) [5]			
NEWUOA	5.2	8.3	24	3.6	3.3	2.7	1.9	1.8	1.8	1.7	NEWUOA [31]			
(1+1)-ES	4.4	8.1	19	81	120	120	100	110	130	160	(1+1)-ES [1]			
POEMS	360	450	560	65	78	110	98	110	130	160	POEMS [20]			
PSO	4	15	37	8.7	12	24	28	38	49	67	PSO [7]			
PSO_Bounds	3.9	9	48	11	27	96	120	160	200	240	PSO_Bounds [8]			
Monte Carlo	3	10	47	17	110	900	3600	6.9e4	3.7e5	16e-5/1e6	Monte Carlo [3]			
Rosenbrock	8.9	12	22	2.6	3.1	2.9	2.2	2.2	2.2	2.2	Rosenbrock [27]			
IPOP-SEP-CMA-ES	3.1	9.5	16	7.6	15	14	10	9.3	9.4	9	IPOP-SEP-CMA-ES [29]			
VNS (Garcia)	4.8	21	45	14	15	12	9.8	9.4	9.8	10	VNS (Garcia) [11]			

Table 9: 02-D, running time excess ERT/ERT_{best} on f_9 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

10 Ellipsoid													
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$		
ERT _{best} /D	2.9	5.7	14.9	22.9	26.9	30.4	34.2	37.9	40.9	48.8	ERT _{best} /D		
ALPS	22	25	47	69	160	350	780	1600	2100	3200	ALPS [17]		
AMaLGaM IDEA	6.7	5.7	3	3	3.8	4	4.1	4.1	4.3	4.4	AMaLGaM IDEA [4]		
avg NEWUOA	2.6	3.6	3.8	4.8	6.9	7.6	8.8	9.5	9.9	11	avg NEWUOA [31]		
BayEDAcG	17	13	60	190	310	33e-1/2e3					BayEDAcG [10]		
BFGS	2.3	1.5	1	1.4	1.4	1.4	1.4	2.6	6.3	24	BFGS [30]		
Cauchy EDA	14	13	7.4	6.4	7	7	7.4	7.7	8	8.4	Cauchy EDA [24]		
BIPOP-CMA-ES	12	12	7.9	9	8.5	7.9	7.7	7.4	7.3	6.8	BIPOP-CMA-ES [15]		
(1+1)-CMA-ES	7.3	5.8	7.2	6.6	6.3	5.8	5.5	5.3	5.2	4.8	(1+1)-CMA-ES [2]		
DASA	22	15	8900	5.2e4	6.1e4	9.5e4	1.2e5	1.1e5	1e5	8.6e4	DASA [19]		
DEPSO	16	26	80	110	330	310	51e-2/2e3				DEPSO [12]		
DIRECT	3.9	4.3	3.9	9.5	20	68	120	190	220	460	DIRECT [25]		
EDA-PSO	17	26	43	140	330	640	1100	2100	3e3	8600	EDA-PSO [6]		
full NEWUOA	2	3	3.8	4.5	6	6.4	7.1	7.7	8.2	9	full NEWUOA [31]		
G3-PCX	11	9.5	26	39	39	37	34	31	29	25	G3-PCX [26]		
simple GA	27	51	77	700	2800	4300	4.2e4	3.8e4	23e-3/1e5		simple GA [22]		
GLOBAL	18	19	11	7.4	6.4	5.8	5.3	4.9	4.6	4	GLOBAL [23]		
iAMaLGaM IDEA	5.5	4	3.3	3.7	4.1	4.1	4	4.1	4.2	4.1	iAMaLGaM IDEA [4]		
LSfminbnd	1.8	1	770	6300	15e + 0/1e4						LSfminbnd [28]		
LSstep	2.1	1.2	770	2800	15e + 0/1e4						LSstep [28]		
MA-LS-Chain	16	20	13	18	19	20	19	18	18	17	MA-LS-Chain [21]		
MCS (Neum)	1	1.2	1.7	8.7	47	130	520	1100	1300	3700	MCS (Neum) [18]		
NELDER (Han)	3	2.2	1.2	1.1	1.1	1.1	1.1	1.1	1.1	1	NELDER (Han) [16]		
NELDER (Doe)	3.2	2.2	1.2	1	1	1	1	1	1	1	NELDER (Doe) [5]		
NEWUOA	2.3	1.9	3.1	4.3	6.5	7.3	8.5	9.6	10	11	NEWUOA [31]		
(1+1)-ES	6.3	5.3	8700	2.4e4	7.7e4	1.5e5	4.3e5	13e-2/1e6			(1+1)-ES [1]		
POEMS	110	90	300	540	1400	2100	2400	3200	3700	6400	POEMS [20]		
PSO	23	26	180	280	480	650	850	990	1100	1900	PSO [7]		
PSO_Bounds	21	24	530	770	740	830	1500	1900	1900	2100	PSO_Bounds [8]		
Monte Carlo	23	55	110	690	3900	4.4e4	1.3e5	3.8e5	61e-4/1e6		Monte Carlo [3]		
Rosenbrock	4.8	2.8	3.1	3.4	3.2	3	2.9	2.8	3.2	3	Rosenbrock [27]		
IPOP-SEP-CMA-ES	8.3	12	16	14	16	15	13	12	12	11	IPOP-SEP-CMA-ES [29]		
VNS (Garcia)	22	25	17	12	12	11	10	9.4	9.1	8.3	VNS (Garcia) [11]		

Table 10: 02-D, running time excess ERT/ERT_{best} on f_{10} , in italics is given the median final function value and the median	n number of	f
function evaluations to reach this value divided by dimension		

						11 Discus					
Δ ftarget	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{best}/D	4.7	5.67	17.6	22.5	25.2	30.8	33.7	37.6	40.7	48.5	ERT_{best}/D
ALPS	17	40	35	80	200	410	880	1200	1700	3400	ALPS [17]
AMaLGaM IDEA	4.8	5.4	3	3.5	4.2	3.9	4.2	4.4	4.4	4.6	AMaLGaM IDÉA [4]
avg NEWUOA	1.3	1.5	1.5	3.3	5.1	5.4	6.8	7.3	8	8.8	avg NEWUOA [31]
BayEDAcG	9.3	18	31	150	1100	14e-1/2e3					BayEDAcG [10]
BFGS	1.6	1.7	1.2	1.6	2	1.7	1.9	2.7	5.7	36	BFGS [30]
Cauchy EDA	13	15	6.7	7.4	8.1	8	8.3	8.1	8.9	9	Cauchy EDA [24]
BIPOP-CMA-ES	4.7	8.7	7.9	8.8	9.2	8.2	8	7.6	7.5	6.8	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	4.8	5.9	5.8	6.4	6.6	5.7	5.6	5.4	5.1	4.7	(1+1)-CMA-ES [2]
DASA	15	15	9e3	4e4	5.4e4	5.7e4	5.3e4	5e4	4.7e4	4.2e4	DASA [19]
DEPSO	24	34	34	110	45e-2/2e3						DEPSO [12]
DIRECT	3.3	5.1	2.6	5.2	28	49	58	190	270	460	DIRECT [25]
EDA-PSO	8.6	27	96	260	460	990	1900	2900	6500	36e-6/1e5	EDA-PSO [6]
full NEWUOA	1.6	3.5	2.7	4.4	6.2	6.2	7	7.7	8	8.6	full NEWUOA [31]
G3-PCX	9.5	9.1	9.7	25	28	36	35	33	32	27	G3-PCX [26]
simple GA	20	57	53	220	5e3	4.6e4	14e-2/1e5				simple GA [22]
GLOBAL	17	23	9.2	7.5	6.9	5.8	5.4	4.9	4.6	4	GLOBAL [23]
iAMaLGaM IDEA	4.5	6	2.8	3.3	4	3.8	4	3.9	3.9	4	iAMaLGaM IDEA [4]
LSfminbnd	2.1	1.8	500	2900	5500	96e-1/1e4					LSfminbnd [28]
LSstep	1	1	380	1800	2600	81e-1/1e4				•	LSstep [28]
MA-LS-Chain	12	15	11	18	23	21	20	20	20	17	MA-LS-Chain [21]
MCS (Neum)	1	1.1	87	120	170	300	920	1300	2e3	91e-5/3e4	MCS (Neum) [18]
NELDER (Han)	2	2.1	1	1.1	1.1	1	1.1	1.1	1.1	1	NELDER (Han) [16]
NELDER (Doe)	2.2	2.4	1	1	1	1	1	1	1	1	NELDER (Doe) [5]
NEWUOA	1.2	1.5	1.5	3.2	5.5	6.1	6.9	7.7	8.4	11	NEWUOA [31]
(1+1)-ES	4.2	850	7700	2.1e4	6e4	2.3e5	4.4e5	63e-3/1e6		•	(1+1)-ES [1]
POEMS	55	83	1e3	1400	2100	2800	4e3	6500	7900	7100	POEMS [20]
PSO	10	23	480	530	660	670	860	1e3	1300	1900	PSO [7]
PSO_Bounds	11	21	3200	5200	6300	5500	6700	6300	6100	5500	PSO_Bounds [8]
Monte Carlo	16	51	94	870	6300	4.3e4	2.1e5	97e-4/1e6		•	Monte Carlo [3]
Rosenbrock	2.3	2.9	2.4	2.7	3	2.7	2.6	2.5	2.6	2.5	Rosenbrock [27]
IPOP-SEP-CMA-ES	5.4	6.9	13	17	17	14	13	13	12	11	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	8.4	14	12	12	12	11	10	9.7	9.4	8.6	VNS (Garcia) [11]

Table 11: 02-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{11} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension 11 Discus

				v	12 Be	nt ciga	r				
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{host}/D	5	9.17	16.9	23	37.6	47	52.4	62.7	76.3	97.4	ERT_{host}/D
ALPS	19	37	40	51	76	94	130	210	230	370	ALPS [17]
AMaLGaM IDEA	5.4	4.1	5.8	13	17	17	17	18	16	15	AMaLGaM IDEA [4]
avg NEWUOA	1.7	1.1	1	1.6	1.5	1.5	1.5	1.5	1.4	1.4	avg NEWUOA [31]
BayEDAcG	40	26	69	87	67e-2/2e3						BayEDAcG [10]
BFGS	1.8	1.1	1.2	3.2	3.1	2.9	2.8	2.6	2.4	4.2	BFGS [30]
Cauchy EDA	11	9.9	14	24	19	18	18	17	15	14	Cauchy EDA [24]
BIPOP-CMA-ES	6	6.1	7.9	12	9.9	9.1	9	11	9.6	8.2	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	4.9	7	9.4	13	10	8.9	8.7	7.6	6.5	5.6	(1+1)-CMA-ES [2]
DASA	16	64	2700	6800	6100	8800	1.4e4	1.2e4	9700	7900	DASA [19]
DEPSO	17	16	41	55	51	48	45	40	35	45	DEPSO [12]
DIRECT	3	3.3	6.2	35	80	70	160	270	250	290	DIRECT [25]
EDA-PSO	11	24	40	98	160	300	790	1e3	1e3	820	EDA-PSO [6]
full NEWUOA	1.4	1.9	4.6	5.2	3.8	3.4	3.3	3	2.7	2.4	full NEWUOA [31]
G3-PCX	9.1	6.1	12	29	34	34	32	31	29	28	G3-PCX [26]
simple GA	23	39	93	170	580	1e3	2400	2700	2200	1900	simple GA [22]
GLOBAL	11	11	8.1	8.3	7.2	6.3	6.4	5.9	5	4.4	GLOBAL [23]
iAMaLGaM IDEA	4.1	2.5	4.5	7	6.4	6.4	6.4	6	5.8	5.4	iAMaLGaM IDEA [4]
LSfminbnd	1.7	1	590	1200	770	630	570	490	410	330	LSfminbnd [28]
LSstep	500	280	300	230	230	350	720	600	820	640	LSstep [28]
MA-LS-Chain	13	13	12	15	13	12	13	13	12	10	MA-LS-Chain [21]
MCS (Neum)	1	1.1	62	49	32	26	24	28	39	30	MCS (Neum) [18]
NELDER (Han)	1.9	1.4	1	1	1	1	1	1	1	1	NELDER (Han) [16]
NELDER (Doe)	2	1.4	1.1	1.6	1.6	1.7	1.7	1.6	1.4	1.3	NELDER (Doe) [5]
NEWUOA	1.5	1.1	1.9	2.9	2.3	2.1	2	1.8	1.6	1.4	NEWUOA [31]
(1+1)-ES	3.8	1500	6800	1.7e4	2.3e4	5.5e4	1.3e5	2.3e5	1.9e5	25e-3/1e6	(1+1)-ES [1]
POEMS	64	79	83	650	1100	1200	1600	2100	2900	1.5e4	POEMS [20]
PSO	11	12	19	57	110	130	160	180	220	300	PSO [7]
PSO_Bounds	12	19	230	440	390	510	690	630	560	560	PSO_Bounds [8]
Monte Carlo	18	27	97	580	3200	1.6e4	1.4e5	38e-4/1e6			Monte Carlo [3]
Rosenbrock	3.3	2.9	2.5	3.6	3	5.4	5.1	4.5	3.9	3.3	Rosenbrock [27]
IPOP-SEP-CMA-ES	7.4	9.2	7.6	9.5	9.6	8.8	8.5	8.1	7	6.3	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	17	17	15	13	8.8	7.5	7.1	6.4	5.6	4.9	VNS (Garcia) [11]

Table 12: 02-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{12} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

inction evaluations	to reach	i this va	lue divi	ded by (dimensi	lon					
	13 Sharp ridge										
Δ ftarget	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{best}/D	0.5	2.3	11.3	17.6	23.2	30	35.4	41.5	47.4	61.1	ERT_{best}/D
ALPS	1.3	3.2	13	47	100	170	300	1300	3700	2.9e4	ALPS [17]
AMaLGaM IDEA	1.1	3.4	2.6	3.2	3.6	3.7	3.9	4	3.9	4.1	AMaLGaM IDEA [4]
avg NEWUOA	1.8	6.7	6.7	17	38	54	73	130	140	770	avg NEWUOA [31]
BayEDAcG	1.4	2.4	52	140	570	950	11e-1/2e3				BayEDAcG [10]
BFGS	1.2	5	6.8	15	45	74	160	660	580	67e-5/5e3	BFGS [30]
Cauchy EDA	4.1	15	7.3	7.7	7.7	8.2	8.5	8.6	8.5	8.5	Cauchy EDA [24]
BIPOP-CMA-ES	1.3	4.3	3.2	5.4	5.7	5.9	6.4	6.1	6.6	7	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1.1	4.4	5.2	7.3	7	7.3	8.1	7.6	7.9	7.6	(1+1)-CMA-ES [2]
DASA	13	90	540	850	2600	4900	1.6e4	4.7e4	1.4e5	62e-5/1e6	DASA [19]
DEPSO	1.1	6.1	8.4	25	63	120	18e-3/2e3			•	DEPSO [12]
DIRECT	1	1	2.5	4.2	5.1	8.7	24	49	74	120	DIRECT [25]
EDA-PSO	1.4	3.5	6.4	42	180	270	710	4e3	3.1e4	27e-5/1e5	EDA-PSO [6]
full NEWUOA	1.5	5.2	8.5	12	31	76	140	290	760	1800	full NEWUOA [31]
G3-PCX	1.2	3.9	13	30	36	47	50	55	70	61	G3-PCX [26]
simple GA	1.3	3.7	25	170	1100	2.2e4	25e-3/1e5			•	simple GA [22]
GLOBAL	1.3	2.8	9.2	9.3	7.3	6	13	67e-5/400			GLOBAL [23]
iAMaLGaM IDEA	1.1	3.3	2.6	3.1	3.6	3.3	3.6	3.6	3.6	3.7	iAMaLGaM IDEA [4]
LSfminbnd	1	16	52	110	170	470	850	13e-3/1e4			LSfminbnd [28]
LSstep	28	420	280	570	1e3	1500	35e-2/1e4				LSstep [28]
MA-LS-Chain	1.1	3.3	8.7	17	18	21	23	21	19	22	MA-LS-Chain [21]
MCS (Neum)	1	4.7	23	20	170	960	2200	2500	75e-4 /3e4		MCS (Neum) [18]
NELDER (Han)	1.7	1.6	1	1	1	1	1	1	1	1	NELDER (Han) [16]
NELDER (Doe)	1.3	2.2	1.1	1.1	1	1	1	1	1.1	1	NELDER (Doe) [5]
NEWUOA	1.6	2.8	6.3	10	22	25	72	62	91	150	NEWUOA [31]
(1+1)-ES	1.9	31	37	94	210	370	790	4200	8100	3.7e4	(1+1)-ES [1]
POEMS	170	110	48	93	140	330	1100	2300	6300	2.4e4	POEMS [20]
PSO	1.6	3.3	9	27	76	140	330	1100	2900	1.1e4	PSO [7]
PSO_Bounds	1.1	3.8	9.2	43	120	260	620	1200	3e3	93e-7/1e5	PSO_Bounds [8]
Monte Carlo	1.6	5.4	18	280	1.2e4	1.1e5	32e-3/1e6				Monte Carlo [3]
Rosenbrock	3.2	4.8	5.6	7	7.5	18	28	43	70	170	Rosenbrock [27]
IPOP-SEP-CMA-ES	1.1	3.7	13	20	18	15	14	14	13	11	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1.4	3.9	8.8	9.7	9.6	8.8	9.2	9.1	8.6	8.4	VNS (Garcia) [11]

Table 13: 02-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{13} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

14 Sum of different powers											
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget
ERThest/D	0.5	0.5	0.7	3.7	8.1	12.2	18.9	27.8	33.7	45.1	ERT _{best} /D
ALPS	1	1	1.6	2.4	14	60	75	83	130	530	ALPS [17]
AMaLGaM IDEA	1	1.2	1.6	3.3	3.9	4.7	4.2	3.9	3.8	4.2	AMaLGaM IDEA [4]
avg NEWUOA	1	1.4	3.4	2.2	1.4	1.3	1.6	1.8	2.2	6.8	avg NEWUOA [31]
BayEDAcG	1	1	1.9	1.8	10	25	67	98	180	12e-5/2e3	BayEDAcG [10]
BFGS	1	1.4	2.1	2.8	1.8	1.7	1.4	1.1	1	6	BFGS [30]
Cauchy EDA	1	4.6	13	13	12	11	10	8.6	8.9	8.5	Cauchy EDA [24]
BIPOP-CMA-ES	1	1.1	1.9	2.5	3	4.2	4.6	5.3	5.5	7.1	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1.4	1.7	3.1	3.4	3.6	4	3.9	4.4	4.7	(1+1)-CMA-ES [2]
DASA	1	18	22	22	16	18	33	590	9300	3.1e5	DASA [19]
DEPSO	1	1	1.4	5.2	10	16	17	18	55	17e-7/2e3	DEPSO [12]
DIRECT	1	1	1	1.3	2.1	2.8	6	8.6	12	32	DIRECT [25]
EDA-PSO	1	1.2	1.4	2.9	8.2	12	15	74	160	1100	EDA-PSO [6]
full NEWUOA	1	1.4	3.2	1.4	1	1	1	1.1	1.5	3.7	full NEWUOA [31]
G3-PCX	1	1.2	1.8	6.3	6.3	5.9	6.6	7.6	9.1	11	G3-PCX [26]
simple GA	1	1.1	1	4	41	200	280	630	3200	58e-7/1e5	simple GA [22]
GLOBAL	1	1.1	1.7	5.5	13	13	8.8	6.2	8.2	34e-7/300	GLOBAL [23]
iAMaLGaM IDEA	1	1.5	1.6	3.7	3.9	4	3.9	3.4	3.5	3.6	iAMaLGaM IDEA [4]
LSfminbnd	1	1.3	4.7	5.4	3	6.2	76	1500	23e-5/1e4		LSfminbnd [28]
LSstep	1	55	40	73	50	120	1600	5100	23e-4 /1e4		LSstep [28]
MA-LS-Chain	1	1.3	1.7	3.1	9.6	15	13	12	12	17	MA-LS-Chain [21]
MCS (Neum)	1	1	1	1	1.4	1.7	2.8	3.1	23	8200	MCS (Neum) [18]
NELDER (Han)	1	1.5	2.1	1.4	1.4	1.4	1.2	1	1	1.1	NELDER (Han) [16]
NELDER (Doe)	1	1.1	1.3	1.4	1.3	1.3	1.1	1	1	1	NELDER (Doe) $[5]$
NEWUOA	1	1.1	3.7	2.4	1.6	1.5	1.6	1.8	2.1	5.4	NEWUOA [31]
(1+1)-ES	1	1.7	2.3	2.5	2.5	3.4	9.2	160	3400	22e-7/1e6	(1+1)-ES [1]
POEMS	1	140	190	86	73	160	180	180	330	3300	POEMS [20]
PSO	1	1.1	1.4	4.8	13	25	36	48	85	1700	PSO [7]
PSO_Bounds	1	1.1	1.5	2.7	14	45	72	110	180	1200	PSO_Bounds [8]
Monte Carlo	1	1	1.8	2.6	31	560	7200	1.1e5	4.2e5	15e-5/1e6	Monte Carlo [3]
Rosenbrock	1	2.2	4	1.9	1.6	1.6	1.9	1.8	2.4	3	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1.2	1.6	1.8	4.4	4.9	7.4	9.7	10	11	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1	2.1	6.2	10	9.4	9	8.1	8.6	9.3	VNS (Garcia) [11]

Table 14: 02-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{14} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

					15	Rastrig	gin				
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT _{best} /D	0.5	0.6	18.6	146	517	533	556	582	616	706	ERT_{best}/D
ALPS	1.1	1.6	2.7	6.8	3.4	4.8	5.7	7.1	7.9	9.1	ALPS [17]
AMaLGaM IDEA	1.1	2.8	1.1	4.3	2.7	2.8	2.8	2.7	2.6	2.3	AMaLGaM IDEA [4]
avg NEWUOA	1	2.6	2.5	2.5	3.3	3.2	3.1	2.9	2.8	2.4	avg NEWUOA [31]
BayEDAcG	1	2.2	2.1	8.2	7.6	26	16e-2/2e3				BayEDAcG [10]
BFGS	1.2	17	4.2	4.6	7.9	7.7	7.3	7	6.6	5.8	BFGS [30]
Cauchy EDA	9.1	38	4.9	2.9	3.2	11	14	14	13	12	Cauchy EDA [24]
BIPOP-CMA-ES	1.2	2.9	1.1	1.8	2.1	2.2	2.2	2.1	2.1	1.9	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1.2	2.8	22	7.7	7.6	7.4	7.1	6.8	6.5	5.7	(1+1)-CMA-ES [2]
DASA	4.6	22	64	84	64	62	60	57	54	48	DASA [19]
DEPSO	1.1	1.6	2.9	3.8	1.7	2.2	2.5	2.6	3	6.3	DEPSO [12]
DIRECT	1	1	1	1	1	1	1	1	1	1	DIRECT [25]
EDA-PSO	1	3.3	2	9.3	6.1	8.3	8.3	8.5	8.4	8.1	EDA-PSO [6]
full NEWUOA	1.2	3.1	1.5	1.4	3.5	3.4	3.3	3.1	3	2.6	full NEWUOA [31]
G3-PCX	1.1	2.3	7.8	13	22	21	20	19	18	16	G3-PCX [26]
simple GA	1.2	2.3	4.2	18	13	34	96	98	100	120	simple GA [22]
GLOBAL	1.1	2.6	3	1.6	2.6	2.5	2.4	2.3	2.2	2	GLOBAL [23]
iAMaLGaM IDEA	1.1	2.5	1	4.2	5.1	5.1	5	4.8	4.6	4.1	iAMaLGaM IDEA [4]
LSfminbnd	1.1	6.2	3.7	20	36	51	66	210	71e-2/9e3		LSfminbnd [28]
LSstep	1.1	47	170	200	80	79	77	74	71	63	LSstep [28]
MA-LS-Chain	1.1	2	1.7	1.9	1.6	1.5	1.5	1.5	1.4	1.3	MA-LS-Chain [21]
MCS (Neum)	1	1	2.1	3.5	1.4	1.4	1.3	1.3	1.2	1.1	MCS (Neum) [18]
NELDER (Han)	1	1.9	8.4	7.3	9.7	9.4	9	8.6	8.2	7.1	NELDER (Han) [16]
NELDER (Doe)	1	3.2	1.1	1.3	1.4	1.3	1.3	1.2	1.2	1	NELDER (Doe) $[5]$
NEWUOA	1.1	11	4.1	3.4	3.3	3.2	3	2.9	2.7	2.4	NEWUOA [31]
(1+1)-ES	1.4	3.7	1.1	5.3	8.4	8.2	7.9	7.5	7.1	6.3	(1+1)-ES [1]
POEMS	28	120	16	19	18	20	21	21	22	22	POEMS [20]
PSO	1.1	2.4	1.9	4.1	16	16	16	16	16	15	PSO [7]
PSO_Bounds	1.2	2.3	1.7	6.6	3.9	7.3	9.2	11	11	12	PSO_Bounds [8]
Monte Carlo	1.1	2.1	2.4	64	150	1500	5800	1.2e4	50e-4/1e6		Monte Carlo [3]
Rosenbrock	1.3	19	15	9.7	9.5	9.2	8.9	8.5	8	7	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	3.8	1.5	2.9	2.1	2.2	2.2	2.1	2.1	1.9	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	3.3	3.4	1.9	2.4	2.4	2.3	2.4	2.7	3.7	VNS (Garcia) [11]

Table 15: 02-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{15} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	16 Weierstrass										
Δ ftarget	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT _{best} /D	0.5	0.567	4.57	25	87.2	163	179	195	205	269	ERT _{best} /D
ALPS	1	1.3	2.7	5.6	9.1	14	19	25	34	37	ALPS [17]
AMaLGaM IDEA	1	1.2	3.2	3.4	5.1	4.6	4.5	4.2	4.1	3.3	AMaLGaM IDEA [4]
avg NEWUOA	1	12	15	9.1	5.5	6.8	13	21	37	73	avg NEWUOA [31]
BayEDAcG	1	1.4	1.5	9.8	24	39	76	71	68	110	BayEDAcG [10]
BFGS	1	11	40	150	170	270	27e-2/6e3				BFGS [30]
Cauchy EDA	1	4.2	4.5	4.4	6.1	15	29	31	35	27	Cauchy EDA [24]
BIPOP-CMA-ES	1	1	3.1	3.5	3.5	2.5	2.4	2.3	2.3	1.9	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1.2	6	2.3	2.3	5.2	8.8	12	11	12	(1+1)-CMA-ES [2]
DASA	1	9	29	150	180	130	210	250	340	530	DASA [19]
DEPSO	1	1.5	3.9	10	10	9.6	26	38	72	16e-4 /2e3	DEPSO [12]
DIRECT	1	1.4	1.6	1	1	1	1	1.5	2	1.9	DIRECT [25]
EDA-PSO	1	1.8	2.6	4.8	15	200	290	370	410	320	EDA-PSO [6]
full NEWUOA	1	2.5	8.1	5.9	3.9	3.2	5.5	7.6	10	16	full NEWUOA [31]
G3-PCX	1	1.4	2.8	8.9	3.1	4.5	4.8	5	5.3	11	G3-PCX [26]
simple GA	1	1.2	2	4.1	16	42	180	450	690	690	simple GA [22]
GLOBAL	1	1.7	3.9	5.1	2.4	1.4	1.5	1.4	1.7	1.5	GLOBAL [23]
iAMaLGaM IDEA	1	1.1	1	6.9	7.4	9.1	9.2	8.6	8.3	7	iAMaLGaM IDEA [4]
LSfminbnd	1	3.6	5.6	5.7	5.4	8.3	14	33	38	110	LSfminbnd [28]
LSstep	1	1.5	1.6	11	23	63	70	150	200	150	LSstep [28]
MA-LS-Chain	1	1.2	1.3	3.6	4.2	6.4	10	11	10	8.3	MA-LS-Chain [21]
MCS (Neum)	1	1.1	5.1	6.7	2.7	4.3	6.8	10	29	120	MCS (Neum) [18]
NELDER (Han)	1	1.3	1.2	7.6	4.4	4.7	4.3	4	3.8	2.9	NELDER (Han) [16]
NELDER (Doe)	1	1.1	1.6	3.5	1.8	1.1	1.1	1	1	1	NELDER (Doe) [5]
NEWUOA	1	2.4	9	10	6.8	6.9	22	37	44	77	NEWUOA [31]
(1+1)-ES	1	1.7	35	38	35	33	56	73	84	120	(1+1)-ES [1]
POEMS	1	98	71	650	200	110	110	110	110	88	POEMS [20]
PSO	1	1.7	2.5	3.8	6.1	100	94	88	86	69	PSO [7]
PSO_Bounds	1	1.2	2.8	6.4	11	110	120	120	120	100	PSO_Bounds [8]
Monte Carlo	1	1.2	2.3	5	20	140	1200	2.4e4	7.2e4	18e-5/1e6	Monte Carlo [3]
Rosenbrock	1	10	33	36	33	27	79	290	19e-4/8e3		Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1.8	3.2	4.1	2.4	2.9	4	3.8	3.9	3.3	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1.2	4.6	5	4.8	4.9	4.7	4.7	5.6	6.8	VNS (Garcia) [11]

Table 16: 02-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{16} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

			iarao ar	laca oj	17 Sc	haffer F7,	condition	10			
Δ ftarget	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget
ERT _{best} /D	0.5	0.5	1.33	30.4	66.5	138	198	372	543	828	ERT _{best} /D
ALPS	1	1.2	1.5	2.8	16	15	17	12	12	11	ALPS [17]
AMaLGaM IDEA	1	1.5	1.5	1.3	4.8	2.7	4.5	3.3	2.9	2.1	AMaLGaM IDEA [4]
avg NEWUOA	1.1	1.3	12	4.6	13	33	120	75e-4 /5e3			avg NEWUOA [31]
BayEDAcG	1	1.1	1	2	8	7	8.7	8.8	27	87e-6/2e3	BayEDAcG [10]
BFGS	1	6.4	15	16	90	24e-2/2e3					BFGS [30]
Cauchy EDA	1	7.9	18	120	56	28	20	11	16	13	Cauchy EDA [24]
BIPOP-CMA-ES	1	1.2	4.1	1.8	1.5	1	1	1	1.3	1.1	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1	12	3.1	5.9	14	14	14	16	10	(1+1)-CMA-ES [2]
DASA	1	1	21	29	37	52	93	230	340	220	DASA [19]
DEPSO	1	1.3	2.7	1.1	4.3	3.7	3.7	2.8	2.4	2.8	DEPSO [12]
DIRECT	1	1	1.4	1	1	1	1.4	1.2	1	1	DIRECT [25]
EDA-PSO	1.1	1.1	2.6	2	3.9	7.4	9.9	8.2	8	7.1	EDA-PSO [6]
full NEWUOA	1	1.4	8.2	4.4	14	21	53	48	30e-4 /6e3		full NEWUOA [31]
G3-PCX	1	1.1	2.5	4.5	6.2	3.9	3.2	2.6	4.4	3	G3-PCX [26]
simple GA	1	1.2	2.1	5.1	47	61	91	120	150	69e-8/1e5	simple GA [22]
GLOBAL	1	1.2	2.6	4	4.1	3.9	4.4	9.6	75e-4/500		GLOBAL [23]
iAMaLGaM IDEA	1	1.2	1.3	8.8	6.2	4.2	5.1	4.2	4	2.8	iAMaLGaM IDEA [4]
LSfminbnd	1	1.2	5.4	1.2	7.3	55	16e-3/5e3				LSfminbnd [28]
LSstep	1.1	2	42	40	35	44	82	390	10e-4/1e4		LSstep [28]
MA-LS-Chain	1.1	1.3	1.3	2.2	5.3	4.3	4.8	2.8	3.1	2.9	MA-LS-Chain [21]
MCS (Neum)	1	1	1.3	4.3	4.8	5.4	9.2	44	140	130	MCS (Neum) [18]
NELDER (Han)	1	1.5	130	28	20	14	11	12	9.6	6.3	NELDER (Han) [16]
NELDER (Doe)	1	1.5	1.4	1.5	3.3	3	3.1	7	5.9	4	NELDER (Doe) $[5]$
NEWUOA	1	1.9	7.7	6.8	18	33	120	75e-4 /5e3			NEWUOA [31]
(1+1)-ES	1	1.1	2.7	5.9	6.7	4.8	8.5	13	23	15	(1+1)-ES [1]
POEMS	4.5	110	110	18	35	31	32	23	24	21	POEMS [20]
PSO	1.1	1.2	1.9	1.6	5	6.2	8.1	6.2	5.5	5.5	PSO [7]
PSO_Bounds	1	1.3	1.9	1.3	13	15	22	15	21	30	PSO_Bounds [8]
Monte Carlo	1	1.1	1.7	5.2	220	4900	7.4e4	73e-4/1e6	•	•	Monte Carlo [3]
Rosenbrock	1	20	45	83	140	500	350	24e-2/5e3	•	•	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1.9	4	2.2	2.8	2.3	1.8	1.6	1.5	1.4	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1	2.5	5.7	4.7	2.7	2.9	2.6	6.7	32	VNS (Garcia) [11]

Table 17: 02-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{17} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	5 to rea		value ur	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	8 Sch	$\mathbf{F}_{\mathbf{a}}$	ondition 1	000			
Aftarget	10 ± 03	10 ± 02	10 ± 01			$\frac{10.02}{10.02}$		10.04	10.05	10.07	Aftarget
EPT /D	10+03	16	0.5	66.0	222	625	254	1040	1220	1420	EPT /D
	0.5	1.0	9.5	00.9	555	023 F 4	0.04	1040	1220	1430	ALDS [17]
ALPS	1.1	1.3	1.6	6.6	5.5	5.4	6.7	8.1	9.6	13	ALPS [17]
AMALGAM IDEA	1.1	1.3	1.3	4.1	1	1	1.1	1.2	1.1	1.1	AMaLGaM IDEA [4]
avg NEWUOA	1.7	7.9	5.4	9	6.1	62	58e-3/6e3	•	•	•	avg NEWUOA [31]
BayEDAcG	1.4	1.5	2.3	19	19	48	53e-2/2e3	•	•	•	BayEDAcG [10]
BFGS	5.4	11	14	30	110	74e-2/2e3	•	•	•	•	BFGS [30]
Cauchy EDA	2.6	2200	380	55	11	6.4	5	7	7.4	6.7	Cauchy EDA [24]
BIPOP-CMA-ES	1.6	2.4	2.2	6.5	1.9	1.1	1	1	1	1	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	22	6.6	13	17	38	83	140	32e-3/1e4		(1+1)-CMA-ES [2]
DASA	3.3	27	26	91	86	740	1800	4200	5900	5e3	DASA $[19]$
DEPSO	1.3	1	2.7	3.1	2.1	3.3	11	9.4	8.3	75e-4 /2e3	DEPSO [12]
DIRECT	1.4	1.9	1	1	1.1	1.2	3.4	4.8	4.9	11	DIRECT [25]
EDA-PSO	1.3	1.3	2.4	5.4	7.1	9.1	11	12	13	15	EDA-PSO [6]
full NEWUOA	1.2	5	3	16	19	71	58e-3/6e3				full NEWUOA [31]
G3-PCX	1.9	1.1	2	10	21	41	48	72	99	85	G3-PCX [26]
simple GA	1.1	1.5	4.3	15	23	110	280	680	1200	24e-4/1e5	simple GA [22]
GLOBAL	1.3	1.2	2	3.1	2.2	4.8	7.6	58e-3/1e3			GLOBAL [23]
iAMaLGaM IDEA	1.2	1.8	1.4	12	2.9	1.8	2.3	2	2	1.8	iAMaLGaM IDEA [4]
LSfminbnd	2.1	3.6	1.3	2.1	7	33	58e-3 /4e3				LSfminbnd [28]
LSstep	28	18	12	79	60	110	24e-2/1e4				LSstep [28]
MA-LS-Chain	1.7	1.5	1.6	3.2	2.5	3.2	4	3.9	5.8	7	MA-LS-Chain [21]
MCS (Neum)	1.4	3	1.3	2.8	1.7	8.4	140	350	30e-4 /3e4		MCS (Neum) [18]
NELDER (Han)	1.2	1.3	21	44	18	20	38	47	40	34	NELDER (Han) [16]
NELDER (Doe)	1.3	1.3	1.2	3.1	2.4	4.3	5.8	8.7	25	21	NELDER (Doe) [5]
NEWUOA	1.3	13	5.6	12	14	62	98e-3/6e3				NEWUOA [31]
(1+1)-ES	1.5	2.4	63	230	620	1500	4900	1.4e4	75e-4 /1e6		(1+1)-ES [1]
POEMS	100	72	28	120	29	28	23	31	45	42	POEMS [20]
PSO	1.3	1.3	1.7	3.4	2.8	3.2	3.5	5.6	6.5	7.2	PSO [7]
PSO_Bounds	1.4	1.5	1.5	5.3	6.7	8.8	10	12	17	23	PSO_Bounds [8]
Monte Carlo	1.1	1.2	2.2	21	270	1.1e4	24e-3/1e6				Monte Carlo [3]
Rosenbrock	26	54	61	56	200	53e-2/5e3	• •				Rosenbrock [27]
IPOP-SEP-CMA-ES	1.5	4.9	2.1	6.2	2.1	1.3	1.1	1	1.1	1.1	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1.6	3.8	16	5.4	3.6	4.8	8.1	18	150	VNS (Garcia) [11]

Table 18: 02-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{18} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	1000011 0	ino rara	e arriae	19 G	riewar	ik-Ros	enbro	ck F8F2			
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget
ERT_{host}/D	0.5	0.5	0.5	0.5	13.2	108	114	120	126	138	ERT_{host}/D
ALPS	1	1.1	5.5	55	17	12	22	30	41	54	ALPS [17]
AMaLGaM IDEA	1	1.1	6.3	40	6.2	18	18	17	17	16	AMaLGaM IDEA [4]
avg NEWUOA	1	1.3	8	110	13	22	21	20	19	18	avg NEWUOA [31]
BayEDAcG	1	1.1	3.9	44	9.9	13	57	35e-4 /2e3			BayEDAcG [10]
BFGS	1	11	37	310	61	30	29	27	26	24	BFGS [30]
Cauchy EDA	1	1.1	16	110	51	170	860	1300	2800	18e-4/5e4	Cauchy EDA [24]
BIPOP-CMA-ES	1	1	6	31	10	12	12	15	14	14	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1	5.6	87	33	32	31	29	28	26	(1+1)-CMA-ES [2]
DASA	1	7.5	42	760	97	250	250	250	260	270	DASA [19]
DEPSO	1	1	4.4	59	17	18	35	36	69	67	DEPSO [12]
DIRECT	1	1	1	1	4.6	10	9.6	9.1	8.9	59	DIRECT [25]
EDA-PSO	1	1.1	5.2	37	13	17	30	57	62	72	EDA-PSO [6]
full NEWUOA	1	1.3	6.7	88	17	17	17	16	15	14	full NEWUOA [31]
G3-PCX	1	1	5.3	52	37	49	47	45	43	40	G3-PCX [26]
simple GA	1	1.2	4.5	51	20	21	110	360	640	4900	simple GA [22]
GLOBAL	1	1.3	4.3	50	9.4	11	10	10	9.6	8.8	GLOBAL [23]
iAMaLGaM IDEA	1	1.1	5.5	25	63	50	48	48	46	42	iAMaLGaM IDEA [4]
LSfminbnd	1	1.1	9.4	49	10	29	70	120	310	59e-5/5e3	LSfminbnd [28]
LSstep	1	1.9	140	440	27	63	140	580	11e-4/1e4		LSstep [28]
MA-LS-Chain	1	1.1	6.7	60	7.2	15	15	14	14	13	MA-LS-Chain [21]
MCS (Neum)	1	1	1	1	1	1	1	1	1	1	MCS (Neum) [18]
NELDER (Han)	1	1	3.1	380	64	32	30	29	27	25	NELDER (Han) [16]
NELDER (Doe)	1	1.1	4.6	52	10	8.1	7.8	7.4	7.1	6.5	NELDER (Doe) [5]
NEWUOA	1	1.5	6.2	130	16	27	26	25	24	22	NEWUOA [31]
(1+1)-ES	1	1.6	6.2	100	22	23	25	27	30	38	(1+1)-ES [1]
POEMS	1	130	340	550	57	210	200	200	190	190	POEMS [20]
PSO	1	1.1	5.3	34	9.1	4.7	6	8.7	9.9	16	PSO [7]
PSO_Bounds	1	1.5	5.1	40	7.8	11	20	36	47	71	PSO_Bounds [8]
Monte Carlo	1	1.2	4.5	64	16	36	110	310	720	3.2e4	Monte Carlo [3]
Rosenbrock	1	6.9	42	160	34	30	29	28	26	24	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1.5	4.3	29	6.8	19	20	19	19	18	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1.2	2.2	43	12	19	19	20	20	21	VNS (Garcia) [11]

Table 19: 02-D, running time excess ERT/ERT_{best} on f_{19} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	$20 \text{ Schwefel } x^* \sin(x)$										
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{best}/D	1.1	1.6	1.87	30.3	182	183	183	184	185	188	ERT_{best}/D
ALPS	2.1	2.8	3.1	14	6.2	9.2	12	16	20	26	ALPS [17]
AMaLGaM IDEA	2.2	2.5	2.6	26	37	38	38	38	38	38	AMaLGaM IDEA [4]
avg NEWUOA	3	2.2	2.1	9.8	4	4	4	4	4	3.9	avg NEWUOA [31]
BayEDAcG	3.2	4	3.6	9.2	32	25e-2/2e3					BayEDAcG [10]
BFGS	2.5	2.2	2.1	6	2.7	2.7	2.7	2.7	2.7	2.6	BFGS [30]
Cauchy EDA	26	20	18	9.9	31	150	1300	2e3	2e3	1900	Cauchy EDA [24]
BIPOP-CMA-ES	2.9	2.8	2.7	13	9.9	10	11	11	11	11	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	2.2	2	2.1	7.5	8.5	8.6	8.6	8.6	8.6	8.6	(1+1)-CMA-ES [2]
DASA	59	52	49	81	44	45	45	45	45	45	DASA [19]
DEPSO	1.4	1	1	9.9	4.9	5.6	6.4	6.8	8	9.2	DEPSO [12]
DIRECT	5.7	5.9	6.1	1	2.9	3	3.1	3.3	3.7	3.9	DIRECT [25]
EDA-PSO	1.7	3.3	3.2	9	13	21	25	25	26	27	EDA-PSO [6]
full NEWUOA	2.9	2.1	1.8	18	8.3	8.3	8.3	8.3	8.2	8.1	full NEWUOA [31]
G3-PCX	2.9	2.8	2.9	38	7.8	7.8	8	8.1	8.1	8.2	G3-PCX [26]
simple GA	2.7	2.4	2.8	14	15	27	45	65	85	130	simple GA [22]
GLOBAL	1.8	1.9	2.4	11	4.5	4.5	4.5	4.5	4.5	4.5	GLOBAL [23]
iAMaLGaM IDEA	2.1	2.4	2.2	51	26	26	27	27	27	27	iAMaLGaM IDEA [4]
LSfminbnd	6.5	6.7	6.6	150	68e-2/1e4						LSfminbnd [28]
LSstep	94	210	180	120	25	27	30	37	40	50	LSstep [28]
MA-LS-Chain	1.5	1.9	2.4	4.2	1.8	2	2.1	2.2	2.3	2.4	MA-LS-Chain [21]
MCS (Neum)	2.9	6.2	5.7	2.2	1	1	1	1	1	1	MCS (Neum) [18]
NELDER (Han)	1.5	1.3	1.3	36	28	28	28	28	28	27	NELDER (Han) [16]
NELDER (Doe)	1.6	1.7	1.5	3.9	2.8	2.8	2.9	2.9	2.9	2.9	NELDER (Doe) [5]
NEWUOA	3	2.2	2.1	7	5.9	5.9	5.9	5.9	5.8	5.8	NEWUOA [31]
(1+1)-ES	4.1	3.7	3.3	13	9	9.1	9.2	9.2	9.2	9.2	(1+1)-ES [1]
POEMS	190	140	130	25	30	35	42	46	52	61	POEMS [20]
PSO	2.5	2.2	2.5	8.3	5	6.3	8.7	10	12	15	PSO [7]
PSO_Bounds	2.5	2.9	3.7	11	6	13	20	25	30	36	PSO_Bounds [8]
Monte Carlo	2.2	2.8	3.6	21	67	680	5800	8.2e4	80e-5/1e6		Monte Carlo [3]
Rosenbrock	5	4	4	6.8	4.1	4.2	4.2	4.2	4.2	4.2	Rosenbrock [27]
IPOP-SEP-CMA-ES	1.6	1.8	1.8	9.4	15	16	17	18	18	18	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	3.8	4.3	18	9.3	9.6	9.7	9.9	10	13	VNS (Garcia) [11]

Table 20: 02-D, running time excess ERT/ERT_{best} on f_{20} , in italics is given the median final function value and the median number	r of
function evaluations to reach this value divided by dimension	

					21 Gall	lagher	101 p	\mathbf{eaks}				
	$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
	ERT_{best}/D	0.5	0.5	0.833	25.3	87.2	138	145	153	162	165	ERT_{best}/D
-	ALPS	1	1	1.2	2.2	1.8	2.6	4.9	6.4	7.8	12	ALPS [17]
	AMaLGaM IDEA	1	1	1.3	28	17	11	11	10	10	10	AMaLGaM IDEA [4]
	avg NEWUOA	1	1	6.1	6.5	4.6	2.9	2.8	2.7	2.6	2.7	avg NEWUOA [31]
	BayEDAcG	1	1	1.7	1.6	9.3	14	39	57	86	85	BayEDAcG [10]
	BFGS	1	1	2.6	4.8	3	2	1.9	1.8	1.7	1.8	BFGS [30]
	Cauchy EDA	1	1	6	310	93	62	65	62	81	80	Cauchy EDA [24]
	BIPOP-CMA-ES	1	1	1.4	11	10	8.2	9.7	9.3	8.9	8.9	BIPOP-CMA-ES [15]
	(1+1)-CMA-ES	1	1	1.2	12	9.6	6.1	5.9	5.6	5.3	5.3	(1+1)-CMA-ES [2]
	DASA	1	1	13	150	140	88	84	80	77	76	DASA [19]
	DEPSO	1	1	2.1	2.5	1.5	1.8	2.4	2.6	2.9	5.6	DEPSO [12]
	DIRECT	1	1	1.3	1	1	1	1	2	2	2.3	DIRECT [25]
	EDA-PSO	1	1	1	1.8	83	54	53	52	51	52	EDA-PSO [6]
	full NEWUOA	1	1	2.2	3.6	3	1.9	1.8	1.7	1.7	1.7	full NEWUOA [31]
	G3-PCX	1	1	1.4	2.7	2.9	1.9	1.9	1.8	1.8	1.8	G3-PCX [26]
	simple GA	1	1	1.4	1	1.7	4.1	7.7	18	120	270	simple GA [22]
	GLOBAL	1	1	1.5	1.1	1.1	1	1	1	1	1	GLOBAL [23]
	iAMaLGaM IDEA	1	1	1.6	21	12	7.9	7.8	7.5	7.2	7.1	iAMaLGaM IDEA [4]
	LSfminbnd	1	1	2.1	39	20	26	46	60	73	170	LSfminbnd [28]
	LSstep	1	1	18	370	150	100	100	100	120	190	LSstep [28]
	MA-LS-Chain	1	1	1.4	1.1	1.5	1.5	1.7	1.9	1.9	2	MA-LS-Chain [21]
	MCS (Neum)	1	1	1.6	22	14	8.8	8.4	8	7.6	7.5	MCS (Neum) [18]
	NELDER (Han)	1	1	1.8	19	20	13	12	12	11	11	NELDER (Han) [16]
	NELDER (Doe)	1	1	1.4	2.6	2.6	1.7	1.6	1.5	1.5	1.5	NELDER (Doe) [5]
	NEWUOA	1	1	3.5	3.9	4	2.5	2.4	2.3	2.2	2.3	NEWUOA [31]
	(1+1)-ES	1	1	2.8	14	19	12	11	11	10	10	(1+1)-ES [1]
	POEMS	1	1	130	93	890	560	540	520	490	490	POEMS [20]
	PSO	1	1	1.2	1.4	83	53	51	48	46	47	PSO [7]
	PSO_Bounds	1	1	1.5	33	300	190	180	170	170	170	PSO_Bounds [8]
	Monte Carlo	1	1	2	1.8	1.2	3.5	8.8	28	42	640	Monte Carlo [3]
	Rosenbrock	1	1	2.3	5.5	3.9	2.5	2.4	2.3	2.2	2.1	Rosenbrock [27]
	IPOP-SEP-CMA-ES	1	1	1.3	9.6	6.4	6.3	8.5	8.7	8.6	9.2	IPOP-SEP-CMA-ES [29]
	VNS (Garcia)	1	1	1.1	6.1	14	9.1	8.8	8.5	8.4	8.4	VNS (Garcia) [11]

Table 21: 02-D, running time excess ERT/ERT_{best} on f_{21} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\begin{array}{c c c c c c c c c c c c c c c c c c c $												
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$	
ERT_{best}/D	0.5	0.5	2.53	13.4	83.9	109	125	142	144	153	ERT_{best}/D	
ALPS	1	1	1.2	1.3	1	3	5.2	7.1	9.2	15	ALPS [17]	
AMaLGaM IDEA	1	1	1.3	51	18	19	17	15	15	15	AMaLGaM IDEA [4]	
avg NEWUOA	1	1	3	3.8	1.3	1.1	1.1	1.1	1.1	1.3	avg NEWUOA [31]	
BayEDAcG	1	1	1.3	3.3	7.6	11	34	59	200	37e-4 /2e3	BayEDAcG [10]	
BFGS	1	1	5.4	5	1.5	1.2	1.1	1	1	1	BFGS [30]	
Cauchy EDA	1	1	27	610	190	270	390	450	540	510	Cauchy EDA [24]	
BIPOP-CMA-ES	1	1	1	7.3	11	8.7	10	9.2	9.1	8.7	BIPOP-CMA-ES [15]	
(1+1)-CMA-ES	1	1	14	26	7.2	5.7	5	4.5	4.4	4.3	(1+1)-CMA-ES [2]	
DASA	1	1	11	80	22	21	22	28	40	63	DASA [19]	
DEPSO	1	1	2.3	4.7	2.4	4	4.6	5	6.6	9.8	DEPSO [12]	
DIRECT	1	1	1.5	2.1	1.3	1.3	1.4	2.2	4.8	5.1	DIRECT [25]	
EDA-PSO	1	1	1.1	4	1.7	4.2	4.9	8.4	11	25	EDA-PSO [6]	
full NEWUOA	1	1	6.5	6.8	1.5	1.2	1.1	1.1	1.1	1.2	full NEWUOA [31]	
G3-PCX	1	1	2.1	2.2	1.1	1.1	1.1	1.3	1.4	1.6	G3-PCX [26]	
simple GA	1	1	1.2	3	1.3	3.3	7.1	17	280	1900	simple GA [22]	
GLOBAL	1	1	1.7	2.9	1.3	1.5	1.5	1.3	1.4	1.3	GLOBAL [23]	
iAMaLGaM IDEA	1	1	1.5	14	9.9	8.9	8	7.2	7.1	7.3	iAMaLGaM IDEA [4]	
LSfminbnd	1	1	1.4	4.7	5.1	53	49	61	69	460	LSfminbnd [28]	
LSstep	1	1	1	80	140	140	150	280	970	920	LSstep [28]	
MA-LS-Chain	1	1	1	2.8	1.6	1.9	2.2	2.3	2.4	2.4	MA-LS-Chain [21]	
MCS (Neum)	1	1	2.4	40	7.4	6	5.3	4.7	4.8	5.2	MCS (Neum) [18]	
NELDER (Han)	1	1	7.7	39	9.8	7.6	6.6	5.9	5.8	5.5	NELDER (Han) [16]	
NELDER (Doe)	1	1	1.3	8.1	1.8	1.4	1.2	1.1	1.1	1.1	NELDER (Doe) [5]	
NEWUOA	1	1	1.9	6.3	1.2	1	1	1	1	1.1	NEWUOA [31]	
(1+1)-ES	1	1	1.6	46	11	9.8	9.4	9.4	10	12	(1+1)-ES [1]	
POEMS	1	1	64	940	230	190	160	150	150	150	POEMS [20]	
PSO	1	1	1.5	2.7	1	1.8	1.9	2.3	3.8	6.5	PSO [7]	
PSO_Bounds	1	1	1.2	540	87	67	60	56	58	64	PSO_Bounds [8]	
Monte Carlo	1	1	1.3	2.8	1.5	3.1	7.2	24	93	760	Monte Carlo [3]	
Rosenbrock	1	1	12	17	4.5	3.5	3.1	2.7	2.7	2.6	Rosenbrock [27]	
IPOP-SEP-CMA-ES	1	1	1	7.7	4.4	4.1	3.9	3.6	3.8	3.8	IPOP-SEP-CMA-ES [29]	
VNS (Garcia)	1	1	2	1	2.8	3.8	4.8	4.7	5	5.3	VNS (Garcia) [11]	

Table 22: 02-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on	f_{22} , in italics is given	the median final function	value and the median number of
function evaluations to reach this value divided by dime	ension		

	5 10 104	511 01115	value ui	vided by	23	Katsuura	IS				
Δ ftarget	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{host}/D	0.5	0.5	3.9	96.5	117	131	150	157	174	190	ERT_{host}/D
ALPS	1	1	1.4	14	86	140	200	640	4100	2.8e4	ALPS [17]
AMaLGaM IDEA	1	1	1.3	7.5	10	9.8	9	8.9	8.4	8.1	AMaLGaM IDEA [4]
avg NEWUOA	1	1	4.2	6.7	25	100	260	49e-3/6e3			avg NEWUOA [31]
BayEDAcG	1	1	2	11	56e-2/2e3						BayEDAcG [10]
BFGS	1	1	4.8	4.9	28	120	480	460	410	73e-3/5e3	BFGS [30]
Cauchy EDA	1	1	1.8	16	860	14e-2/5e4				•	Cauchy EDA [24]
BIPOP-CMA-ES	1	1	1.8	8.3	15	14	13	13	12	12	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1	2.1	5.1	8.4	8.6	7.7	7.6	6.9	6.6	(1+1)-CMA-ES [2]
DASA	1	1	5.7	17	170	1800	8600	9600	8700	7900	DASA [19]
DEPSO	1	1	2.2	24	96e-2/2e3						DEPSO [12]
DIRECT	1	1	1.5	4.2	290	270	240	230	210	200	DIRECT [25]
EDA-PSO	1	1	2.3	18	1400	13e-2/1e5				•	EDA-PSO [6]
full NEWUOA	1	1	6	1.5	24	46	81	79	71	65	full NEWUOA [31]
G3-PCX	1	1	1.9	1.6	6.1	6	5.8	5.8	5.5	7.4	G3-PCX [26]
simple GA	1	1	1.4	6.6	330	840	3300	41e-4/1e5			simple GA [22]
GLOBAL	1	1	1	2.6	97	21e-2/2e3					GLOBAL [23]
iAMaLGaM IDEA	1	1	1.3	5.3	5.5	5.3	4.9	5	4.7	4.6	iAMaLGaM IDEA [4]
LSfminbnd	1	1	1.3	2.1	30	120	200	190	25e-3/7e3		LSfminbnd [28]
LSstep	1	1	2.6	18	1300	24e-2/1e4	•		•	•	LSstep [28]
MA-LS-Chain	1	1	1.8	5.5	7.4	7.1	6.6	6.7	6.4	7	MA-LS-Chain [21]
MCS (Neum)	1	1	3.4	2.8	6.3	23	210	500	1e3	1900	MCS (Neum) [18]
NELDER (Han)	1	1	1.3	1.6	2.2	2.2	2	1.9	1.8	1.7	NELDER (Han) [16]
NELDER (Doe)	1	1	4.7	1	1	1	1	1	1	1	NELDER (Doe) [5]
NEWUOA	1	1	7.8	3.2	32	89	130	170	500	460	NEWUOA [31]
(1+1)-ES	1	1	2.6	3.7	19	55	240	1e3	2100	6700	(1+1)-ES [1]
POEMS	1	1	14	28	190	180	180	190	180	190	POEMS [20]
PSO	1	1	1.3	9	42	59	73	79	88	95	PSO [7]
PSO_Bounds	1	1	1.7	9.4	260	460	500	690	660	860	PSO_Bounds [8]
Monte Carlo	1	1	1.5	8	1900	46e-3/1e6		·			Monte Carlo [3]
Rosenbrock	1	1	1.9	2.2	9.9	15	17	23	29	66e-7/5e3	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1	2.6	8.1	14	16	14	14	13	12	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1	1.8	8.3	38	67	65	62	56	52	VNS (Garcia) [11]

Table 23: 02-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{23} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

26

					24 Lunac	ek bi-Ras	trigin				
$\Delta ftarget$	1e+03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{best}/D	0.5	0.5	9.13	429	4260	11700	12100	12400	12400	12400	ERT_{hest}/D
ALPS	1	1	1	6.5	4	2.8	2.9	2.9	3	3.2	ALPS [17]
AMaLGaM IDEA	1	1	1.2	35	11	6.7	6.7	6.6	6.6	6.7	AMaLGaM IDEA [4]
avg NEWUOA	1	1	3.3	1.9	1.4	6.2	6	5.9	5.9	5.9	avg NEWUOA [31]
BayEDAcG	1	1	1.9	68	22e-1/2e3						BayEDAcG [10]
BFGS	1	1	3.4	5.1	2.9	42e-2/3e3					BFGS [30]
Cauchy EDA	1	1	3.9	33	170	49e-2/5e4					Cauchy EDA [24]
BIPOP-CMA-ES	1	1	4.6	19	17	13	22	22	22	22	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1	2.7	6.1	4.8	2.9	2.8	2.7	2.7	3.6	(1+1)-CMA-ES [2]
DASA	1	1	10	140	110	61	59	58	58	58	DASA [19]
DEPSO	1	1	3.3	67	24e-1/2e3						DEPSO [12]
DIRECT	1	1	1.9	79	8.7	5	4.9	4.7	4.7	4.8	DIRECT [25]
EDA-PSO	1	1	1.6	100	12	9	9	8.8	8.8	8.9	EDA-PSO [6]
full NEWUOA	1	1	2.8	1	1	1.1	1	1	1	1	full NEWUOA [31]
G3-PCX	1	1	1.2	37	20	10e-2/5e4					G3-PCX [26]
simple GA	1	1	1.6	67	79e-2/1e5						simple GA [22]
GLOBAL	1	1	2.7	3.3	7	51e-2/2e3					GLOBAL [23]
iAMaLGaM IDEA	1	1	1.4	28	9.1	5.4	5.3	5.2	5.3	5.3	iAMaLGaM IDEA [4]
LSfminbnd	1	1	2.8	8.3	37e-2/8e3						LSfminbnd [28]
LSstep	3	3	4.8	29	33	12	12	11e-1/1e4			LSstep [28]
MA-LS-Chain	1	1	2.5	31	34	11e-1/1e4					MA-LS-Chain [21]
MCS (Neum)	1	1	2.5	5.7	1.6	2.7	2.7	2.6	2.6	2.6	MCS (Neum) [18]
NELDER (Han)	1	1	16	7.4	5	6.6	6.4	6.2	6.2	6.2	NELDER (Han) [16]
NELDER (Doe)	1	1	1.5	1.9	1.5	3.2	3.1	3	3	3	NELDER (Doe) [5]
NEWUOA	1	1	3.1	2.8	1.9	2	1.9	1.9	1.9	1.9	NEWUOA [31]
(1+1)-ES	1	1	8	12	11	21	20	19	19	19	(1+1)-ES [1]
POEMS	1	1	28	1500	170	20e-1/1e5					POEMS [20]
PSO	1	1	2.4	470	49	18	17	17	17	17	PSO [7]
PSO_Bounds	1	1	1.3	1500	150	57	55	54	54	54	PSO_Bounds [8]
Monte Carlo	1	1	2.5	14	150	570	49e-3/1e6				Monte Carlo [3]
Rosenbrock	1	1	19	35	15	11	11	11	11	11	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1	1.7	7.2	3.9	3.7	3.7	3.6	3.6	3.6	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1	1.2	5.3	1.7	1	1	1.1	1.9	4.7	VNS (Garcia) [11]

Table 24: 02-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{24} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

1 Sphere											
Δ ftarget	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{best}/D	0.333	0.333	1.2	2.67	2.67	2.67	2.67	2.67	2.67	2.67	ERT_{best}/D
ALPS	1	1	2.6	31	160	280	450	660	860	1200	ALPS [17]
AMaLGaM IDEA	1	1.1	3.1	7.4	16	26	37	45	54	73	AMaLGaM IDEA [4]
avg NEWUOA	1	1.3	2.4	1.1	1.1	1.1	1.1	1.1	1.1	1.1	avg NEWUOA [31]
BayEDAcG	1	1	2.4	9.2	96	120	160	180	280	420	BayEDAcG [10]
BFGS	1	1	2.4	1.1	1.1	1.1	1.1	1.1	1.1	1.1	BFGS [30]
Cauchy EDA	1	1.1	40	36	58	91	110	140	160	210	Cauchy EDA [24]
BIPOP-CMA-ES	1	1	2.8	5.1	11	18	23	29	34	47	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1	1.8	5.2	8.8	12	15	19	23	30	(1+1)-CMA-ES [2]
DASA	1	3.1	37	37	49	63	76	89	100	130	DASA [19]
DEPSO	1	1	2.9	15	36	65	96	120	150	200	DEPSO [12]
DIRECT	1	1	1.2	2	5.7	15	27	38	52	95	DIRECT [25]
EDA-PSO	1	1.1	2.8	10	28	56	120	280	390	690	EDA-PSO [6]
full NEWUOA	1	1.3	2.9	1.4	1.4	1.4	1.4	1.4	1.4	1.4	full NEWUOA [31]
G3-PCX	1	1.3	1.9	12	15	19	24	29	34	47	G3-PCX [26]
simple GA	1	1.1	3.1	26	440	1200	2100	3200	4200	6800	simple GA [22]
GLOBAL	1	1.1	3.1	22	38	41	42	44	45	48	GLOBAL [23]
iAMaLGaM IDEA	1	1.2	2.4	5.5	12	18	24	30	36	49	iAMaLGaM IDEA [4]
LSfminbnd	1	2.5	5.5	4.1	5.3	5.6	5.6	5.8	5.9	5.9	LSfminbnd [28]
LSstep	1	1.2	130	94	100	100	100	100	100	100	LSstep [28]
MA-LS-Chain	1	1.1	2.5	14	36	57	70	75	82	96	MA-LS-Chain [21]
MCS (Neum)	1	1	1	1.6	2	2.4	2.4	2.4	2.4	2.4	MCS (Neum) [18]
NELDER (Han)	1	1.5	1.9	1.8	3.4	5.3	6.7	8.3	9.8	13	NELDER (Han) [16]
NELDER (Doe)	1	1	2	2.4	3.9	5.4	6.9	8.7	10	14	NELDER (Doe) [5]
NEWUOA	1	1	1.8	1	1	1	1	1	1	1	NEWUOA [31]
(1+1)-ES	1	1.3	3.4	4.1	7	11	14	18	22	29	(1+1)-ES [1]
POEMS	1	23	170	110	180	390	1e3	1300	1700	2400	POEMS [20]
PSO	1	1.1	3.2	9.9	44	86	160	230	310	500	PSO [7]
PSO_Bounds	1	1	3.1	13	58	230	430	650	850	1500	PSO_Bounds [8]
Monte Carlo	1	1	3.8	35	1400	3.3e4	1.3e6	15e-4/1e6			Monte Carlo [3]
Rosenbrock	1	1.7	4.5	3.3	4.8	5.9	7.5	8.5	10	13	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1	3.5	5.3	10	14	20	26	31	41	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1	2.6	13	24	31	37	46	50	62	VNS (Garcia) [11]

Table 25: 03-D, running time excess ERT/ERT_{best} on f_1 , in italics is given the median final function value and the median number of	
function evaluations to reach this value divided by dimension	

2 Ellipsoid separable											
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{best}/D	6.04	9.82	12.7	13.8	14.4	14.6	14.8	15.3	15.6	16	ERT_{hest}/D
ALPS	43	49	66	100	130	160	190	220	250	310	ALPS [17]
AMaLGaM IDEA	5.9	5.6	6	8.1	10	12	14	16	17	20	AMaLGaM IDÉA [4]
avg NEWUOA	1	1	1.7	8.2	14	21	30	36	43	57	avg NEWUOA [31]
BayEDAcG	15	15	19	26	29	46	48	55	70	93	BayEDAcG [10]
BFGS	3.4	2.3	3.1	4	4.7	4.9	5	5	5.1	5.2	BFGS [30]
Cauchy EDA	15	17	18	21	25	29	34	36	40	48	Cauchy EDA [24]
BIPOP-CMA-ES	8.9	9.5	13	17	20	21	22	22	23	24	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	6	6.4	8.4	11	12	13	13	13	14	14	(1+1)-CMA-ES [2]
DASA	15	12	11	14	15	18	19	21	23	28	DASA [19]
DEPSO	18	14	15	18	24	29	33	36	40	47	DEPSO [12]
DIRECT	5	4.6	4.5	7.3	8.9	10	12	14	33	38	DIRECT [25]
EDA-PSO	7.8	9.9	13	31	58	84	110	130	150	200	EDA-PSO [6]
full NEWUOA	1	1.1	1.7	4.2	8.2	12	16	19	22	29	full NEWUOA [31]
G3-PCX	16	11	43	87	120	130	170	180	200	230	G3-PCX [26]
simple GA	70	160	280	410	570	780	950	1200	1400	1900	simple GA [22]
GLOBAL	16	11	9	8.9	9	9.3	9.4	9.4	9.5	9.7	GLOBAL [23]
iAMaLGaM IDEA	3.2	3.7	4.4	6.1	7.6	8.9	9.9	11	12	14	iAMaLGaM IDEA [4]
LSfminbnd	1.9	1.3	1	1	1	1	1	1	1	1	LSfminbnd [28]
LSstep	28	17	15	14	14	14	14	13	13	13	LSstep [28]
MA-LS-Chain	12	12	14	19	22	26	30	33	38	44	MA-LS-Chain [21]
MCS (Neum)	1.9	1.1	1.8	1.9	2.2	3.7	4.4	5	5.2	6.9	MCS (Neum) [18]
NELDER (Han)	2.4	2	2.2	3.3	4.3	4.6	4.8	4.9	5.1	5.4	NELDER (Han) [16]
NELDER (Doe)	1.9	1.8	2.3	2.8	3.2	3.6	3.8	3.9	4.2	4.6	NELDER (Doe) $[5]$
NEWUOA	1	1.3	3.4	14	25	33	42	49	56	72	NEWUOA [31]
(1+1)-ES	60	270	5800	2e4	4.1e4	6.6e4	3.2e5	4.8e5	36e-4/1e6		(1+1)-ES [1]
POEMS	270	250	280	320	360	450	500	510	620	720	POEMS [20]
PSO	20	25	46	56	65	83	95	100	120	140	PSO [7]
PSO_Bounds	16	47	150	300	340	510	560	580	640	920	PSO_Bounds [8]
Monte Carlo	66	420	6e3	1.8e5	14e-1/1e6		•	·		•	Monte Carlo [3]
Rosenbrock	2.9	3.2	4.9	16	20	22	24	24	24	26	Rosenbrock [27]
IPOP-SEP-CMA-ES	9	8	9.5	12	13	14	15	15	16	17	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	17	17	21	26	26	27	28	29	29	30	VNS (Garcia) [11]

Table 26: 03-D, running time excess ERT/ERT ₁ , on f_2 , in italics is given the median final function val	alue and the median number of
The set of	dae and the median nameer of
runction evaluations to reach this value divided by dimension	

					3 Rastrigi	n separabl	e				
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{hest}/D	0.333	0.733	12.6	274	277	278	281	282	282	284	ERT_{best}/D
ALPS	1	1	25	6.2	8.9	11	13	15	17	21	ALPS [17]
AMaLGaM IDEA	1	2	3.6	4.2	14	15	15	15	15	15	AMaLGaM IDEA [4]
avg NEWUOA	1	4.4	9.4	5	33	33	33	33	33	32	avg NEWUOA [31]
BayEDAcG	1.1	1.5	32	9.7	70e-2/2e3						BayEDAcG [10]
BFGS	1.3	29	42	25	160	150	150	150	150	150	BFGS [30]
Cauchy EDA	1.1	41	14	7.6	250	2600	10e-2/5e4				Cauchy EDA [24]
BIPOP-CMA-ES	1	3.5	3.2	4.7	25	25	26	26	26	26	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1.8	8.1	4	38	38	37	37	37	37	(1+1)-CMA-ES [2]
DASA	1.3	32	14	1.4	12	12	12	12	12	12	DASA [19]
DEPSO	1	2.4	11	2.7	4.1	4.8	5.6	5.9	7.3	8.6	DEPSO [12]
DIRECT	1	1	4.8	4.1	17	17	17	17	17	17	DIRECT [25]
EDA-PSO	1	1.6	5.6	13	42	44	44	45	46	49	EDA-PSO [6]
full NEWUOA	1	4.5	4.9	3.3	15	15	15	15	15	15	full NEWUOA [31]
G3-PCX	1.1	1.9	73	58	330	330	330	330	330	320	G3-PCX [26]
simple GA	1	2.2	52	15	23	31	41	56	69	100	simple GA [22]
GLOBAL	1.1	2.5	8.2	3.6	12	12	12	12	12	12	GLOBAL [23]
iAMaLGaM IDEA	1.1	1.9	12	12	39	39	39	39	39	39	iAMaLGaM IDEA [4]
LSfminbnd	1	6.9	1	38	54	54	53	53	53	52	LSfminbnd [28]
LSstep	28	150	21	1	1	1	1	1	1	1	LSstep [28]
MA-LS-Chain	1	2.3	6.7	2.3	8.3	8.4	8.4	8.4	8.4	8.5	MA-LS-Chain [21]
MCS (Neum)	1	1	6.8	1.2	10	11	11	12	12	12	MCS (Neum) [18]
NELDER (Han)	1	1.8	25	17	100	100	100	100	100	100	NELDER (Han) [16]
NELDER (Doe)	1	1.7	3	1.5	8.4	8.4	8.3	8.3	8.3	8.3	NELDER (Doe) [5]
NEWUOA	1	2.9	5.7	5	55	54	54	54	53	53	NEWUOA [31]
(1+1)-ES	1	4.3	14	12	69	68	68	67	67	67	(1+1)-ES [1]
POEMS	16	210	26	8.2	23	27	31	35	37	45	POEMS [20]
PSO	1	1.5	7.3	3.5	6.1	7	7.9	8.5	9.6	11	PSO [7]
PSO_Bounds	1	2.2	15	8.6	18	22	25	27	29	41	PSO_Bounds [8]
Monte Carlo	1	1.3	110	5500	5.1e4	10e-1/1e6					Monte Carlo [3]
Rosenbrock	1	42	41	27	410	410	400	400	400	400	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	2.8	3.4	3.7	14	17	17	17	17	17	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1.7	8.4	3.8	7.4	7.4	7.6	8.6	11	17	VNS (Garcia) [11]

Table 27: 03-D, running time excess ERT/ERT_{best} on f_3 , in italics is given the median final function value and the median numbers	ber of
function evaluations to reach this value divided by dimension	

4 Skew Rastrigin-Bueche separable											
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget
ERT_{best}/D	0.333	1.8	13.5	269	289	307	317	330	338	348	ERT_{best}/D
ALPS	1.5	1.7	37	9.6	16	18	19	21	23	27	ALPS [17]
AMaLGaM IDEA	1.3	1.2	23	110	970	950	930	900	880	870	AMaLGaM IDEA [4]
avg NEWUOA	2.9	9.2	11	14	160	150	150	140	140	130	avg NEWUOA [31]
BayEDAcG	1.3	1.3	33	47e-1/2e3							BayEDAcG [10]
BFGS	1.8	20	48	54	30e-1/3e3						BFGS [30]
Cauchy EDA	5.9	20	23	1300	13e-1/5e4						Cauchy EDA [24]
BIPOP-CMA-ES	1.1	1.4	9.5	260	3300	4e3	3900	3800	3700	3600	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	2	1.8	13	21	150	140	140	130	130	130	(1+1)-CMA-ES [2]
DASA	17	29	12	1.2	2	2	2	2.1	2.1	2.3	DASA [19]
DEPSO	2.5	1.5	13	6.8	18	47	46	45	44	43	DEPSO [12]
DIRECT	1	1	4.8	20	26	44	83	170	180	180	DIRECT [25]
EDA-PSO	1.5	1.2	16	24	110	110	100	100	100	100	EDA-PSO [6]
full NEWUOA	2.7	3.5	11	25	170	160	150	140	140	140	full NEWUOA [31]
G3-PCX	1.8	1.3	130	62	430	400	390	380	370	360	G3-PCX [26]
simple GA	1.3	1.4	90	19	24	34	42	54	63	110	simple GA [22]
GLOBAL	1.3	1.7	12	7.9	51	48	46	44	43	42	GLOBAL [23]
iAMaLGaM IDEA	1.3	1.6	12	130	860	820	800	770	760	740	iAMaLGaM IDEA [4]
LSfminbnd	2.1	3.4	1	20e-1/4e3							LSfminbnd [28]
LSstep	54	70	17	1	1	1	1	1	1	1	LSstep [28]
MA-LS-Chain	1.4	2.1	9.6	5.6	60	56	55	53	52	51	MA-LS-Chain [21]
MCS (Neum)	1	1.2	5.9	10	67	63	61	59	57	56	MCS (Neum) [18]
NELDER (Han)	2.3	1.4	33	72	320	300	290	280	270	270	NELDER (Han) [16]
NELDER (Doe)	1.8	1	4.5	7.8	43	40	39	37	37	36	NELDER (Doe) [5]
NEWUOA	2.3	2.2	24	21	300	280	280	260	260	250	NEWUOA [31]
(1+1)-ES	2.5	1.8	31	33	230	210	210	200	190	190	(1+1)-ES [1]
POEMS	89	100	48	13	46	47	48	51	53	57	POEMS [20]
PSO	1.3	1.3	15	6	98	93	91	89	87	87	PSO [7]
PSO_Bounds	1.5	1.1	28	21	28	36	36	38	39	51	PSO_Bounds [8]
Monte Carlo	1.3	1.7	220	1.6e4	14e-1/1e6						Monte Carlo [3]
Rosenbrock	2.2	36	43	44	140	130	130	120	120	120	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1.9	6.3	83	14e-1/1e4						IPOP-SEP-CMA-ES [29]
VNS (Garcia)	2.2	1.8	19	7.6	20	19	19	20	22	50	VNS (Garcia) [11]

Table 28: 03-D, running time excess ERT/ERT_{best} on f_4 , in italics is given the median final function value and the median number of	of
function evaluations to reach this value divided by dimension	

5 Linear slope											
$\Delta ftarget$	1e + 03	1e + 02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{best}/D	0.333	0.333	2.2	2.2	2.2	2.2	2.2	2.2	2.2	2.2	ERT_{hest}/D
ALPS	1	1.3	27	90	98	100	110	110	110	110	ALPS [17]
AMaLGaM IDEA	1	1.1	11	20	21	21	21	21	21	21	AMaLGaM IDEA [4]
avg NEWUOA	1	1.5	1.3	1.5	1.5	1.5	1.5	1.5	1.5	1.5	avg NEWUOA [31]
BayEDAcG	1	1.3	22	360	370	370	370	370	370	370	BayEDAcG [10]
BFGS	1	2.6	1.6	2.4	2.5	2.6	2.6	2.6	2.6	2.6	BFGS [30]
Cauchy EDA	1	13	20	22	23	23	23	23	23	23	Cauchy EDA [24]
BIPOP-CMA-ES	1	1.5	3.6	5.4	5.7	5.8	5.8	5.8	5.8	5.8	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1.1	2.1	2.7	2.8	2.9	2.9	2.9	2.9	2.9	(1+1)-CMA-ES [2]
DASA	1	21	19	31	36	40	44	49	53	62	DASA [19]
DEPSO	1	1.4	15	35	39	39	39	39	39	39	DEPSO [12]
DIRECT	1	1	3.7	4.6	6.2	6.2	6.2	6.2	6.2	6.2	DIRECT [25]
EDA-PSO	1	1.3	8.5	16	17	17	17	17	17	17	EDA-PSO [6]
full NEWUOA	1	2	1.2	1.7	1.8	1.8	1.8	1.8	1.8	1.8	full NEWUOA [31]
G3-PCX	1	1.5	9.4	22	25	25	25	25	25	25	G3-PCX [26]
simple GA	1	1.2	14	1100	3e3	4800	7500	1.1e4	1.5e4	22e-8/1e5	simple GA [22]
GLOBAL	1	1.3	31	47	47	48	48	48	48	48	GLOBAL [23]
iAMaLGaM IDEA	1	1.2	3.5	8.3	8.8	8.8	8.8	8.8	8.8	8.8	iAMaLGaM IDEA [4]
LSfminbnd	1	1.1	7.5	11	11	11	11	11	11	11	LSfminbnd [28]
LSstep	1	28	93	120	120	120	120	120	120	120	LSstep [28]
MA-LS-Chain	1	1.3	25	88	92	92	93	93	93	93	MA-LS-Chain [21]
MCS (Neum)	1	1	1	1	1	1	1	1	1	1	MCS (Neum) [18]
NELDER (Han)	1	1.3	1.6	2.4	2.5	2.5	2.5	2.5	2.5	2.5	NELDER (Han) [16]
NELDER (Doe)	1	1.5	1.4	2.4	2.5	2.5	2.5	2.5	2.5	2.5	NELDER (Doe) $[5]$
NEWUOA	1	1.1	1.1	1.4	1.4	1.4	1.4	1.4	1.4	1.4	NEWUOA [31]
(1+1)-ES	1	1.6	2.3	3	3.1	3.1	3.1	3.1	3.1	3.1	(1+1)-ES [1]
POEMS	1	59	120	150	170	180	180	180	180	180	POEMS [20]
PSO	1	1.1	8.2	16	18	18	18	18	18	18	PSO [7]
PSO_Bounds	1	1.3	6.3	14	15	15	15	15	15	15	PSO_Bounds [8]
Monte Carlo	1	1.2	34	1.8e4	6.5e6	32e-2/1e6					Monte Carlo [3]
Rosenbrock	1	5	3.3	3.6	3.6	3.6	3.6	3.6	3.6	3.6	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1.3	4.1	6.7	7	7.1	7.1	7.1	7.1	7.1	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1	18	20	20	20	20	20	20	20	VNS (Garcia) [11]

Table 29: 03-D, running time excess ERT/ERT_{best} on f_5 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

6 Attractive sector											
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT _{best} /D	1.38	2.53	11.2	18.7	30.1	38.9	49.7	61.3	71.6	88.2	ERT _{best} /D
ALPS	4.9	3.3	9.2	35	46	53	58	61	64	72	ALPS [17]
AMaLGaM IDEA	4.8	4.3	3.7	5.5	5.5	6.3	6.4	6.6	6.9	7.5	AMaLGaM IDEA [4]
avg NEWUOA	1.2	2.3	2.6	2.9	2.9	3.8	3.9	4.1	4.3	4.7	avg NEWUOA [31]
BayEDAcG	4.2	10	130	66e-1/2e3							BayEDAcG [10]
BFGS	3.3	2.2	3.5	3.4	2.9	2.4	2	1.8	1.9	3.1	BFGS [30]
Cauchy EDA	24	33	28	31	28	27	26	25	24	25	Cauchy EDA [24]
BIPOP-CMA-ES	1.6	1.6	2.4	3.2	3.1	3.2	3.2	3.1	3	3.2	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1.4	1.6	1.3	1.6	1.8	1.7	1.6	1.6	1.6	1.6	(1+1)-CMA-ES [2]
DASA	33	58	30	32	30	36	55	56	54	66	DASA [19]
DEPSO	2.4	3.3	6	11	11	13	14	13	13	14	DEPSO [12]
DIRECT	1.4	1.1	3	33	440	1300	2700	23e-3/3e4			DIRECT [25]
EDA-PSO	3.9	3.4	2.7	13	28	42	59	62	66	76	EDA-PSO [6]
full NEWUOA	1.5	3.7	4	5.1	5.1	5.4	5.7	6	6.1	6.9	full NEWUOA [31]
G3-PCX	3	3.2	3.5	3.3	2.9	3.2	3.2	3.5	4.3	4.8	G3-PCX [26]
simple GA	2.4	2.7	9	100	270	4200	4400	3800	4400	1.6e4	simple GA [22]
GLOBAL	2.5	3.7	5.2	5.5	4	3.3	2.8	2.4	2.3	2.3	GLOBAL [23]
iAMaLGaM IDEA	2.4	2	2.1	2.9	3.1	3.7	4.1	4.2	4.3	4.8	iAMaLGaM IDEA [4]
LSfminbnd	14	220	490	810	510	400	310	260	220	190	LSfminbnd [28]
LSstep	240	690	1200	990	1e3	820	670	760	670	1700	LSstep [28]
MA-LS-Chain	3.8	4.6	4.3	10	10	9.6	9.1	8.9	8.3	8.1	MA-LS-Chain [21]
MCS (Neum)	2.1	1.5	3	160	120	140	140	130	150	210	MCS (Neum) [18]
NELDER (Han)	1.6	1.2	1.7	1.5	1.3	1.3	1.2	1.2	1.2	1.3	NELDER (Han) [16]
NELDER (Doe)	1	1	1	1	1	1	1	1	1	1	NELDER (Doe) [5]
NEWUOA	1.4	1.9	2.1	3.4	3.8	4	4.1	4	4.1	4.8	NEWUOA [31]
(1+1)-ES	2.1	3.2	1.7	2	1.8	1.8	2	2	2.1	3	(1+1)-ES [1]
POEMS	160	91	31	74	83	93	100	92	99	110	POEMS [20]
PSO	3.8	4	2.9	8	13	17	18	22	25	28	PSO [7]
PSO_Bounds	2.2	2.3	2.9	12	26	100	120	130	120	120	PSO_Bounds [8]
Monte Carlo	2.8	1.9	7.7	200	8700	1.1e5	26e-3/1e6				Monte Carlo [3]
Rosenbrock	3.9	4	2.1	1.8	1.7	1.7	1.6	1.8	1.7	1.6	Rosenbrock [27]
IPOP-SEP-CMA-ES	4.5	3.6	2.8	3.7	3.3	3.5	3.6	3.6	3.6	3.6	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	2.2	2.3	5.6	5.9	4.8	4.6	4.3	4	3.9	3.8	VNS (Garcia) [11]

Table 30: 03-D, running time excess ERT/ERT_{best} on f_6 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension
7 Step-ellipsoid												
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$	
ERT_{hest}/D	0.333	0.867	3.8	21.6	114	155	161	161	161	178	ERT_{best}/D	
ALPS	1.1	2	6.2	10	7	8.7	9.3	9.3	9.3	11	ALPS [17]	
AMaLGaM IDEA	1.2	2.1	2.6	1.6	2.1	3.1	3	3	3	2.9	AMaLGaM IDEA [4]	
avg NEWUOA	1.3	3.5	1.2	6.8	4.8	19	41	41	41	37	avg NEWUOA [31]	
BayEDAcG	1.4	1	3.6	52	72	85	56e-2/2e3				BayEDAcG [10]	
BFGS	1.8	4.1	17	86	37e-1/100						BFGS [30]	
Cauchy EDA	7.1	16	14	6.1	1.9	1.8	1.9	1.9	1.9	2	Cauchy EDA [24]	
BIPOP-CMA-ES	1	2	3.3	2.8	1.1	1	1	1	1	1	BIPOP-CMA-ES [15]	
(1+1)-CMA-ES	1.4	3.5	2.7	2.1	1	1.4	1.4	1.4	1.4	1.3	(1+1)-CMA-ES [2]	
DASA	24	57	85	260	120	1300	1600	1600	1600	1500	DASA [19]	
DEPSO	1.2	1.7	5.2	6.1	5.9	5.1	5.1	5.1	5.1	5.3	DEPSO [12]	
DIRECT	1	1.4	2.9	2.8	2.1	31	34	34	34	30	DIRECT [25]	
EDA-PSO	1.3	1.9	3.3	3.7	8.8	17	20	20	20	22	EDA-PSO [6]	
full NEWUOA	1.2	3.4	1	1	1.4	2.2	6.8	6.8	6.8	6.2	full NEWUOA [31]	
G3-PCX	1.1	1.5	6.2	8.3	12	16	54	54	54	48	G3-PCX [26]	
simple GA	1.3	2.2	3.3	24	27	130	200	200	200	250	simple GA [22]	
GLOBAL	1.3	2.2	6.2	5.4	4.6	8.8	51	51	51	46	GLOBAL [23]	
iAMaLGaM IDEA	1.2	3.3	2.6	15	8.1	6.1	6	6	6	5.4	iAMaLGaM IDEA [4]	
LSfminbnd	8.7	19	46	68	33	100	290	290	290	260	LSfminbnd [28]	
LSstep	1.6	210	300	320	390	930	22e-2/1e4				LSstep [28]	
MA-LS-Chain	1.3	2.1	6.1	4.3	2.2	3.1	3.9	3.9	3.9	3.9	MA-LS-Chain [21]	
MCS (Neum)	1	1.1	1	5.7	2.4	4.2	4.1	4.1	4.1	8.8	MCS (Neum) [18]	
NELDER (Han)	1.7	3	8	28	20	23	30	30	30	27	NELDER (Han) [16]	
NELDER (Doe)	1.1	1.9	7.5	4.2	4.3	4.2	8.8	8.8	8.8	8.8	NELDER (Doe) $[5]$	
NEWUOA	1.3	2.6	11	12	10	14	39	39	39	35	NEWUOA [31]	
(1+1)-ES	1.1	2.3	2	3.6	3.9	7.7	9.3	9.3	9.3	8.4	(1+1)-ES [1]	
POEMS	170	270	81	29	12	18	21	21	21	20	POEMS [20]	
PSO	1.1	2.2	3.5	5.3	3.1	4.4	5.1	5.1	5.1	5.1	PSO [7]	
PSO_Bounds	1.3	2	4.1	7.3	4.8	9.3	12	12	12	13	PSO_Bounds [8]	
Monte Carlo	1.3	2	5	30	130	3900	1.6e4	1.6e4	1.6e4	55e-4/1e6	Monte Carlo [3]	
Rosenbrock	41	140	97	150	370	79e-2/3e3	•	•		•	Rosenbrock [27]	
IPOP-SEP-CMA-ES	3.2	3.3	2.7	2.9	1.4	1.3	1.3	1.3	1.3	1.4	IPOP-SEP-CMA-ES [29]	
VNS (Garcia)	1	3.2	7.5	4.2	2.6	3	4.1	4.1	4.1	3.9	VNS (Garcia) [11]	

	Table 31: 03-D, running time excess ERT/ERT hest on f_7 , in italics is given the median final function value and the median number of						
	function evaluations to reach this value divided by dimension						
7 Stop allinsaid							

8 Rosenbrock original											
Δ ftarget	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{hest}/D	1.4	4.87	9.07	14.9	50.5	58.5	61.6	64.7	65.9	69.4	ERT_{best}/D
ALPS	2.8	8.5	23	46	33	65	93	120	150	210	ALPS [17]
AMaLGaM IDEA	5.1	2.9	3.8	9.9	5.8	6.3	7	7.5	7.8	8.3	AMaLGaM IDEA [4]
avg NEWUOA	3.1	1.9	1.9	2.6	1	1	1	1	1	1	avg NEWUOA [31]
BayEDAcG	3.7	4.7	11	110	560	73e-2/2e3					BayEDAcG [10]
BFGS	3.3	2.1	1.4	2.7	1.1	1.1	1.1	1	1	1	BFGS [30]
Cauchy EDA	24	18	21	28	14	14	15	15	16	17	Cauchy EDA [24]
BIPOP-CMA-ES	4.8	3.8	3.5	8	4.5	4.9	5.2	5.2	5.4	5.6	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1.7	1.6	1.9	6.3	2.8	2.8	3	3.1	3.2	3.4	(1+1)-CMA-ES [2]
DASA	38	22	15	470	470	750	1200	1500	2e3	2800	DASA [19]
DEPSO	6.7	8.1	7.7	14	11	24	64	62e-4 /2e3			DEPSO [12]
DIRECT	1.5	1.4	2	5	3.5	9.2	15	22	29	42	DIRECT [25]
EDA-PSO	2.9	4	6.8	74	70	110	160	210	260	370	EDA-PSO [6]
full NEWUOA	3.7	1.9	1.4	2.8	1.1	1	1	1	1	1	full NEWUOA [31]
G3-PCX	2.5	4.3	4.2	16	9	9.3	9.3	9.1	9.1	9	G3-PCX [26]
simple GA	2.5	3.4	47	170	400	49e-3/1e5					simple GA [22]
GLOBAL	2.6	9.2	11	8.2	2.8	2.6	2.5	2.5	2.5	2.5	GLOBAL [23]
iAMaLGaM IDEA	2.6	2.4	2.2	8.1	4.5	5	5.1	5.3	5.6	5.9	iAMaLGaM IDEA [4]
LSfminbnd	10	4.4	24	810	2800	2400	2300	2200	96e-2/1e4		LSfminbnd [28]
LSstep	150	70	51	680	2800	2400	2300	2200	2100	73e-2/1e4	LSstep [28]
MA-LS-Chain	4.7	4.5	6.6	14	7.7	9.9	11	11	12	12	MA-LS-Chain [21]
MCS (Neum)	1	1	1	1	7.2	6.3	6.2	6	5.9	5.7	MCS (Neum) [18]
NELDER (Han)	1.6	1	1	2.1	1	1	1.1	1.1	1.1	1.2	NELDER (Han) [16]
NELDER (Doe)	2.1	2.1	1.6	4	1.5	1.4	1.4	1.4	1.5	1.5	NELDER (Doe) [5]
NEWUOA	3.1	1.5	1.4	2.8	1.2	1.2	1.2	1.2	1.2	1.2	NEWUOA [31]
(1+1)-ES	4.5	3.3	2.8	45	20	39	65	91	120	170	(1+1)-ES [1]
POEMS	140	50	37	94	48	69	170	290	330	410	POEMS [20]
PSO	2.9	4.4	9.8	46	52	93	150	210	260	380	PSO [7]
PSO_Bounds	2.5	4	17	60	160	590	740	840	920	1e3	PSO_Bounds [8]
Monte Carlo	2.7	6.9	43	1e3	1e4	1.2e5	38e-3/1e6				Monte Carlo [3]
Rosenbrock	4.2	1.8	1.7	6.9	3	3.1	3.1	3	3.1	3	Rosenbrock [27]
IPOP-SEP-CMA-ES	3.8	1.9	3	8.3	6.2	6.7	7	7	7.1	7.2	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	2.5	9.9	7.7	9.4	5.1	5.4	5.7	5.7	5.9	6.1	VNS (Garcia) [11]

Table 32: 03-D, running time excess ERT/ERT_{best} on f_8 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

9 Rosenbrock rotated											
Δ ftarget	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget
ERT _{best} /D	0.333	0.333	6.93	21.8	42.4	49.7	53.2	54.9	56.3	59.4	ERT _{best} /D
ALPS	7.9	130	30	30	48	83	100	130	170	220	ALPS [17]
AMaLGaM IDEA	15	40	5.4	6.2	6	6.5	7.1	7.7	8.1	8.6	AMaLGaM IDEA [4]
avg NEWUOA	11	20	1.7	1.7	1.2	1.1	1.1	1.1	1.2	1.2	avg NEWUOA [31]
BayEDAcG	15	60	12	110	12e-1/2e3						BayEDAcG [10]
BFGS	9.3	20	1.5	1.5	1.1	1.1	1.1	1.1	1.1	1	BFGS [30]
Cauchy EDA	140	290	24	17	16	17	17	18	19	20	Cauchy EDA [24]
BIPOP-CMA-ES	9.9	30	3.9	4.6	4.4	4.7	4.9	5.1	5.3	5.6	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	8.2	36	2.7	4.5	3.6	3.6	3.7	3.8	3.9	4.1	(1+1)-CMA-ES [2]
DASA	200	390	24	790	720	980	1400	1900	2500	3600	DASA [19]
DEPSO	8	77	15	19	27	55	560	46e-4 /2e3			DEPSO [12]
DIRECT	1	1	1.5	1.7	6.2	9.1	18	27	29	38	DIRECT [25]
EDA-PSO	7	42	7.5	49	69	120	190	260	350	490	EDA-PSO [6]
full NEWUOA	9.4	18	1.6	1.4	1	1	1	1	1	1	full NEWUOA [31]
G3-PCX	11	53	5.4	14	12	12	12	12	12	12	G3-PCX [26]
simple GA	8.4	130	49	100	3800	2.8e4	11e-2/1e5				simple GA [22]
GLOBAL	10	100	14	6.2	3.5	3.2	3.1	3.1	3.1	3.1	GLOBAL [23]
iAMaLGaM IDEA	12	28	3.3	5	4.9	5	5.4	5.8	6	6.4	iAMaLGaM IDEA [4]
LSfminbnd	25	61	4.7	180	310	870	1300	2600	2600	71e-3/1e4	LSfminbnd [28]
LSstep	390	3e3	180	400	3300	2800	56e-2/1e4				LSstep [28]
MA-LS-Chain	12	73	11	9.9	8.7	9.9	11	11	12	13	MA-LS-Chain [21]
MCS (Neum)	1	1	1	1	1	1.1	1.1	1.2	1.2	1.2	MCS (Neum) [18]
NELDER (Han)	5.2	12	1.2	1.2	1	1	1.1	1.1	1.2	1.3	NELDER (Han) [16]
NELDER (Doe)	6.9	18	1.5	1.4	1.1	1.1	1.1	1.1	1.2	1.3	NELDER (Doe) [5]
NEWUOA	7.7	22	1.7	1.7	1.2	1.2	1.2	1.2	1.3	1.3	NEWUOA [31]
(1+1)-ES	11	32	2.6	79	71	88	120	150	180	240	(1+1)-ES [1]
POEMS	650	780	66	69	68	150	250	380	500	910	POEMS [20]
PSO	9.3	75	11	17	34	66	130	200	270	440	PSO [7]
PSO_Bounds	11	59	13	77	370	530	670	780	880	1e3	PSO_Bounds [8]
Monte Carlo	12	71	43	670	1e4	2.9e5	43e-3/1e6				Monte Carlo [3]
Rosenbrock	13	23	1.6	2.6	2.7	2.6	2.7	2.8	2.9	2.9	Rosenbrock [27]
IPOP-SEP-CMA-ES	10	28	3.7	5.6	7.4	8.2	8.1	8.2	8.3	8.4	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	20	140	11	6.8	6	6.2	6.3	6.5	6.7	7	VNS (Garcia) [11]

Table 33: 03-D, running time excess ERT/ERT_{best} on f_9 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

				-	10 Elli	psoid					
Δ ftarget	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{best}/D	9.71	18	38	50.7	55.9	60.2	64.5	68.8	72.8	80.6	ERT_{best}/D
ALPS	23	38	50	120	360	700	1300	1900	2600	7100	ALPS [17]
AMaLGaM IDEA	3.2	3	2	2.3	2.7	2.9	3.2	3.4	3.6	3.8	AMaLGaM IDEA [4]
avg NEWUOA	1.1	1.3	1.9	3.4	5.8	6.9	7.9	8.8	9.5	11	avg NEWUOA [31]
BayEDAcG	88	1600	37e + 1/2e3					•			BayEDAcG [10]
BFGS	1.4	1	1	1.2	1.2	1.2	1.4	1.5	5.9	76	BFGS [30]
Cauchy EDA	13	9.4	6.3	6.2	6.7	7.3	7.8	8.3	8.7	9.5	Cauchy EDA [24]
BIPOP-CMA-ES	8.1	5.6	4.1	4.1	4.6	4.9	4.9	4.9	4.9	4.8	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	4.5	3.1	2.7	2.7	2.7	3	3.1	3	3	3	(1+1)-CMA-ES [2]
DASA	130	180	1.1e4	4.4e4	2.5e5	24e-1/1e6					DASA [19]
DEPSO	13	35	67	110	55e-1/2e3						DEPSO [12]
DIRECT	4.1	8.4	7.6	49	120	160	490	480	1e3	2e3	DIRECT [25]
EDA-PSO	20	66	210	2400	4200	7e3	1.1e4	61e-2/1e5			EDA-PSO [6]
full NEWUOA	1	1.6	1.6	2.6	3.9	4.4	4.9	5.6	6	7.1	full NEWUOA [31]
G3-PCX	8.8	7.2	14	21	28	30	36	39	41	42	G3-PCX [26]
simple GA	30	90	200	2e3	1.2e4	55e-2/1e5					simple GA [22]
GLOBAL	9.9	6	3.3	2.8	2.7	2.6	2.5	2.4	2.3	2.2	GLOBAL [23]
iAMaLGaM IDEA	3.3	2.5	1.8	2.1	2.6	2.9	3	3.1	3.2	3.3	iAMaLGaM IDEA [4]
LSfminbnd	340	480	1700	2800	2500	61e + 0/1e4					LSfminbnd [28]
LSstep	1100	2400	1700	53e + 1/1e4							LSstep [28]
MA-LS-Chain	16	13	9.6	11	12	12	13	12	12	12	MA-LS-Chain [21]
MCS (Neum)	23	14	67	170	820	4100	3800	29e-2/2e4			MCS (Neum) [18]
NELDER (Han)	1.8	1.3	1	1	1	1	1	1	1	1	NELDER (Han) [16]
NELDER (Doe)	2	1.3	1.2	1.1	1.1	1.1	1.1	1.1	1	1.1	NELDER (Doe) [5]
NEWUOA	1.4	1.3	2.8	5.2	8.3	10	12	13	14	16	NEWUOA [31]
(1+1)-ES	28	320	2100	6200	1.2e4	2.3e4	7.6e4	36e-4/1e6			(1+1)-ES [1]
POEMS	49	72	410	1600	5300	1.2e4	51e-2/1e5				POEMS [20]
PSO	9.2	12	59	1100	2400	3600	4800	6700	6500	1.8e4	PSO [7]
PSO_Bounds	13	31	2100	8e3	1.2e4	1.1e4	2.2e4	2.1e4	2e4	1.8e4	PSO_Bounds [8]
Monte Carlo	34	210	2100	6e4	2.5e5	11e-1/1e6					Monte Carlo [3]
Rosenbrock	2.6	3.9	8.5	7.8	7.2	6.8	6.5	6.4	6.9	6.5	Rosenbrock [27]
POP-SEP-CMA-ES	22	17	11	9.8	9.6	9.2	8.8	8.5	8.2	7.8	IPOP-SEP-CMA-ES [29]
UNE (Canaia)	0.2	71	5.0	C	5.0	FO	F 77	FC	F F	F 9	VINC (CL ·) [11]

Table 34: 03-D, running time excess ERT/ERT_{best} on	f_{10} , ir	n italics is given	the median i	final function	value and	the median	number o
function evaluations to reach this value divided by dime	ension						

					11	Discus					
Δ ftarget	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{best}/D	3.13	3.87	22.4	35.1	75.7	87.7	92.5	96.3	101	109	ERT_{best}/D
ALPS	19	48	31	120	250	520	1100	1800	2600	5e3	ALPS [17]
AMaLGaM IDEA	5.5	7	3.1	3	1.7	1.9	2.1	2.3	2.5	2.8	AMaLGaM IDEA [4]
avg NEWUOA	1.9	2.6	2	3.3	2.5	2.7	3.3	3.7	4.3	5	avg NEWUOA [31]
BayEDAcG	10	23	91	810	85e-1/2e3	•					BayEDAcG [10]
BFGS	2.1	1.9	1	1	1	1.4	3.7	11	41	33e-7 / 7e3	BFGS [30]
Cauchy EDA	19	24	7.8	6.5	4.1	4.3	5	5.2	5.6	6.4	Cauchy EDA [24]
BIPOP-CMA-ES	5.7	14	9.5	7.5	4	3.6	3.7	3.7	3.7	3.6	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	4.6	9.8	5.8	4.6	2.7	2.5	2.5	2.5	2.5	2.5	(1+1)-CMA-ES [2]
DASA	15	16	4600	9300	1.4e4	2.2e4	3.3e4	4.3e4	4.2e4	3.9e4	DASA $[19]$
DEPSO	9.8	62	130	270	89e-1/2e3						DEPSO [12]
DIRECT	5.7	6.4	13	28	150	390	770	24e-4 /3e4			DIRECT [25]
EDA-PSO	9.6	28	74	290	490	1100	5100	41e-4/1e5			EDA-PSO [6]
full NEWUOA	2.3	6.9	3.2	3.6	2.5	2.6	3.1	3.5	3.9	4.7	full NEWUOA [31]
G3-PCX	8.7	10	30	93	100	140	180	210	260	320	G3-PCX [26]
simple GA	17	66	74	2100	5600	90e-2/1e5					simple GA [22]
GLOBAL	14	23	5.4	3.9	2	1.8	1.8	1.8	1.7	1.7	GLOBAL [23]
iAMaLGaM IDEA	4.6	6.7	3.1	3.1	1.9	1.9	2	2.1	2.2	2.4	iAMaLGaM IDEA [4]
LSfminbnd	2.1	190	1800	32e + 0/1e4							LSfminbnd [28]
LSstep	2.1	400	2900	36e+0/1e4							LSstep [28]
MA-LS-Chain	13	24	21	22	11	10	10	10	9.9	9.7	MA-LS-Chain [21]
MCS (Neum)	1	1	49	82	100	510	24e-3/2e4				MCS (Neum) [18]
NELDER (Han)	3	3.4	2.2	2.2	1.3	1.2	1.2	1.2	1.2	1.1	NELDER (Han) [16]
NELDER (Doe)	3.2	3.7	2.3	2	1.1	1	1	1	1	1	NELDER (Doe) [5]
NEWUOA	1.7	8.8	3.1	3.4	2.5	2.6	3.2	3.7	4	5.1	NEWUOA [31]
(1+1)-ES	3.7	1300	8400	1.5e4	1.7e4	1.7e5	37e-3/1e6	•			(1+1)-ES [1]
POEMS	79	100	370	1e3	830	1500	1700	2100	2100	3200	POEMS [20]
PSO	12	30	60	150	160	270	360	450	530	990	PSO [7]
PSO_Bounds	9	25	240	740	610	1e3	1600	1600	1600	1700	PSO_Bounds [8]
Monte Carlo	22	52	130	2200	6.1e4	13e-2/1e6					Monte Carlo [3]
Rosenbrock	2.7	2.7	17	12	5.9	5.3	5.1	5	4.9	4.7	Rosenbrock [27]
POP-SEP-CMA-ES	5.2	20	17	15	7.4	6.6	6.6	6.5	6.4	6.1	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	12	30	14	9.6	48	4.5	4.4	4.4	1.1	4.3	VNS (Carcia) [11]

Table 36: function e
Δ ftar

LSstep MA-LS-Chain

NELDER (Han)

MCS (Neum)

NELDER (Doe)

NEWUOA

(1+1)-ES

POEMS

PSO

PSO_Bounds

Monte Carlo

Rosenbrock

IPOP-SEP-CMA-ES

VNS (Garcia)

73

14

1.1

1.4

1.4

1

7200

170

41

280

1.1e4

1.5

5.6

9.9

87

16

1.3

1.5

1.5

1.2

2.7

100

30

110

1700

1.6

5.4

9.3

1400

25

1

 $\mathbf{2}$

1.8

 $\mathbf{2}$

2.8e4

1800

2400

2e3

1.6e5

38

10

13

790

15

1

1.7

1.6

1.6

2.7e4

1600

2700

2200

26e + 0/1e6

19

10

9.5

RT n° 0383

unction evaluations to reach this value divided by dimension											
					12 B	lent cigar					
Δ ftarget	1e+03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{best}/D	9.78	13.2	21.6	55.9	113	134	148	208	232	263	ERT_{best}/D
ALPS	73	85	94	100	170	460	1600	3400	1.4e4	9.3e4	ALPS [17]
AMaLGaM IDEA	5.9	6.4	4.7	4.2	4.8	5.2	5.6	4.9	4.9	5.2	AMaLGaM IDEA [4]
avg NEWUOA	1.1	1.9	4.5	3.2	2.2	2.2	2.2	1.8	1.8	1.9	avg NEWUOA [31]
BayEDAcG	27	26	67	82	120	220	38e-1/2e3				BayEDAcG [10]
BFGS	1.9	1.5	1.7	1.4	1	1	1	2	2.3	43	BFGS [30]
Cauchy EDA	26	26	34	26	17	16	16	13	13	13	Cauchy EDA [24]
BIPOP-CMA-ES	5.2	4.8	7.9	5.7	4.5	4.7	4.8	3.9	4	4.1	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	3.8	4.3	8.5	6.1	4.3	4.2	4.2	3.3	3.6	3.5	(1+1)-CMA-ES [2]
DASA	17	17	3.1e4	3.6e4	3.6e4	81e-1/1e6					DASA [19]
DEPSO	24	25	80	160	260	67e-1/2e3					DEPSO [12]
DIRECT	4.6	4.6	7	6.5	5.7	10	58	53	49	240	DIRECT [25]
EDA-PSO	190	260	960	1700	5900	1.1e4	9500	6800	91e-2/1e5		EDA-PSO [6]
full NEWUOA	1	1.9	2.9	2.2	1.6	1.7	1.7	1.4	1.5	1.6	full NEWUOA [31]
G3-PCX	4.8	4.3	6	11	8.9	9.5	9.9	8	7.9	8.1	G3-PCX [26]
simple GA	200	380	430	2400	1.3e4	1.1e4	11e-1/1e5				simple GA [22]
GLOBAL	11	8.6	5.9	3.1	2	2.4	2.4	2.2	2.8	4	GLOBAL [23]
iAMaLGaM IDEA	4.1	4.4	9.6	8	6.1	6	5.9	4.7	4.7	4.6	iAMaLGaM IDEA [4]
LSfminbnd	6	6.2	700	1200	14e+0/1e4						LSfminbnd [28]

. 34e+0/1e4

11

1.2

1.3

1.2

1.2

1.1e5

5e3

1e4

1.1e4

9.4

9.1

5.6

. 11

2.7

1.3

1.3

1.3

12e-1/1e6

69e-2/1e5

33e-1/1e5

95Ó0

8.9

8.7

5.6

8.8

 $\mathbf{2.5}$

1

1

1

.

. 24e-1/1e5

6.9

6.7

4.6

9.1

4.5

1

1

1.1

.

7.4

7

4.4

8.9

18

1.1

1

1.2

.

.

.

11

6.8

4.4

400

10

1.2

1.3

1.3

1.2

3.9e4

3800

5800

2500

10

8.4

6

Table 36: 03-D, running time excess ER	T/ERT_{best} on f_{12}	$_2$, in italics is given	the median final	function val	lue and the median	number of
function evaluations to reach this value	divided by dimensi	ion				

LSstep [28] MA-LS-Chain [21]

MCS (Neum) [18]

NELDER (Han) [16] NELDER (Doe) [5]

NEWUOA [31] (1+1)-ES [1] POEMS [20] PSO [7] PSO_Bounds [8]

Monte Carlo [3] Rosenbrock [27]

IPOP-SEP-CMA-ES [29]

VNS (Garcia) [11]

Comparison Tables: BBOB 2009 Function Testbed

13 Sharp ridge											
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERThest/D	0.533	5.6	16.4	28.3	36.2	45.3	71.7	84.9	93.8	122	ERT _{best} /D
ALPS	1.5	12	48	66	100	200	410	1600	5400	2.2e4	ALPS [17]
AMaLGaM IDEA	1.4	4.3	3.7	3.9	4.2	4.3	3.4	3.4	3.5	3.4	AMaLGaM IDEA [4]
avg NEWUOA	2.5	1	5.6	14	42	110	160	280	260	36e-4 /8e3	avg NEWUOA [31]
BayEDAcG	1.5	34	45	120	24e-1/2e3					•	BayEDAcG [10]
BFGS	3.5	1.5	1.1	1	1	1	2.1	31	410	25e-6/9e3	BFGS [30]
Cauchy EDA	39	22	14	12	12	12	9.4	9.2	9.6	9.3	Cauchy EDA [24]
BIPOP-CMA-ES	1.6	2.6	3.7	3.8	5	6.1	4.5	4.4	4.8	4.6	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1.9	2.9	4.1	4.5	5.9	6.9	5.9	5.9	6.1	6	(1+1)-CMA-ES [2]
DASA	18	52	320	1100	1600	6100	2e4	4e4	1.5e5	46e-5/1e6	DASA [19]
DEPSO	1.9	9.5	14	60	100	210	11e-2/2e3				DEPSO [12]
DIRECT	1	1.9	2.9	6.8	6.8	16	29	31	61	160	DIRECT [25]
EDA-PSO	1.2	4.7	48	140	400	1400	5800	73e-4 /1e5			EDA-PSO [6]
full NEWUOA	2.2	1	3	10	38	78	120	260	680	51e-5/9e3	full NEWUOA [31]
G3-PCX	1.5	4.8	20	73	97	110	160	220	230	210	G3-PCX [26]
simple GA	2.2	12	150	250	3600	1.5e4	2e4	16e-2/1e5			simple GA [22]
GLOBAL	1.3	9.4	6.6	4.5	6.3	8.4	88	35e-4/400			GLOBAL [23]
iAMaLGaM IDEA	2.2	3.2	2.9	2.7	3.1	3	2.4	2.5	2.6	2.5	iAMaLGaM IDEA [4]
LSfminbnd	5.9	14	120	220	620	1500	39e-2/1e4				LSfminbnd [28]
LSstep	120	150	510	1500	65e-1/1e4						LSstep [28]
MA-LS-Chain	2.2	7.9	9.7	13	17	17	13	12	12	12	MA-LS-Chain [21]
MCS (Neum)	1	1.7	14	130	370	370	710	830	22e-4 /2e4		MCS (Neum) [18]
NELDER (Han)	1.9	1.2	1	1.1	1.2	1.3	1	1	1	1	NELDER (Han) [16]
NELDER (Doe)	1.5	1.3	1	1.1	1.2	1.3	1.2	1.2	1.2	1.1	NELDER (Doe) [5]
NEWUOA	2	1	4.5	9	42	62	200	1200	12e-4 /7e3		NEWUOA [31]
(1+1)-ES	1.7	2.3	16	65	120	290	1e3	1600	3300	5.7e4	(1+1)-ES [1]
POEMS	280	52	73	670	1700	4900	19e-3/1e5				POEMS [20]
PSO	1.2	5.8	19	220	2200	5e3	2e4	1.7e4	1.5e4	71e-3/1e5	PSO [7]
PSO_Bounds	1.5	6.6	980	1400	1200	9e3	9200	42e-3/1e5			PSO_Bounds [8]
Monte Carlo	1.7	13	1300	1.6e5	17e-1/1e6						Monte Carlo [3]
Rosenbrock	4.5	2.9	5	8.6	9.2	20	31	82	130	320	Rosenbrock [27]
IPOP-SEP-CMA-ES	2.6	3	8.6	15	16	13	8.9	8.5	8.3	7.1	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	9.8	7.1	6	7.8	12	8.5	7.8	7.5	7.2	VNS (Garcia) [11]

Table 37: 03-D, running time excess ERT/ERT_{best} on f_1 .	$_{3}$, in italics is	given the median fina	al function valu	ie and the median	number of
function evaluations to reach this value divided by dimensi	sion				

14 Sum of different powers											
Δ ftarget	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget
ERT_{hest}/D	0.333	0.333	0.733	5.76	9.47	14.4	23.8	30.7	36.7	64.8	ERT_{best}/D
ALPS	1	1.2	2.3	10	55	71	69	81	200	2500	ALPS [17]
AMaLGaM IDEA	1	1.2	2.1	2.7	4.5	5	4.5	4.5	4.7	3.6	AMaLGaM IDEA [4]
avg NEWUOA	1	1.2	4.7	1.2	1.1	1.1	1.2	1.6	2.7	6.9	avg NEWUOA [31]
BayEDAcG	1	1.1	1.6	58	120	110	250	280	780	28e-4 /2e3	BayEDAcG [10]
BFGS	1	2.1	3.7	1.5	1.5	1.3	1.1	1	1	29	BFGS [30]
Cauchy EDA	1	1	20	15	17	18	14	14	14	11	Cauchy EDA [24]
BIPOP-CMA-ES	1	1.3	3.1	2.9	3.5	4.2	4.4	6.4	7.1	5.9	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1.1	2.1	1.4	2.2	2.6	2.9	4	4.2	3.6	(1+1)-CMA-ES [2]
DASA	1	13	43	24	20	23	51	400	2900	4.8e4	DASA [19]
DEPSO	1	1	1.5	4.9	12	16	17	26	130	11e-6/2e3	DEPSO [12]
DIRECT	1	1	1.8	1.7	2.7	5.5	17	45	110	480	DIRECT [25]
EDA-PSO	1	1.1	1.8	4.2	11	21	76	130	190	6500	EDA-PSO [6]
full NEWUOA	1	1.3	6.2	1.4	1.2	1	1	1.5	2.3	4.4	full NEWUOA [31]
G3-PCX	1	1.1	2	4	4.6	4.2	4.9	11	45	280	G3-PCX [26]
simple GA	1	1	1.9	10	160	280	320	1600	6e3	25e-6/1e5	simple GA [22]
GLOBAL	1	1	2.5	8.4	11	7.4	5.1	4.8	12	11e-6/300	GLOBAL [23]
iAMaLGaM IDEA	1	1.4	2.7	2.4	3.2	3.7	3.1	3.2	3.6	3.2	iAMaLGaM IDEA [4]
LSfminbnd	1	1	7.2	4.4	3.5	6.1	67	600	31e-5/1e4		LSfminbnd [28]
LSstep	1	29	210	84	70	160	930	22e-4 /1e4			LSstep [28]
MA-LS-Chain	1	1.1	1.8	6.7	11	12	9.8	11	15	13	MA-LS-Chain [21]
MCS (Neum)	1	1	2.5	12	11	7.9	5.7	6	50	20e-7/2e4	MCS (Neum) [18]
NELDER (Han)	1	1.3	1.9	1	1.2	1.3	1.2	1.3	1.3	1	NELDER (Han) [16]
NELDER (Doe)	1	1	2.7	1.1	1.4	1.8	1.5	1.5	1.6	1.2	NELDER (Doe) [5]
NEWUOA	1	1.1	4.1	1.1	1	1	1.2	2.1	3	17	NEWUOA [31]
(1+1)-ES	1	1.1	2.2	1.8	1.9	2.5	5.8	110	2400	16e-7/1e6	(1+1)-ES [1]
POEMS	1	140	250	55	91	110	150	160	220	1e4	POEMS [20]
PSO	1	1.1	1	3.1	14	24	30	45	76	2e3	PSO [7]
PSO_Bounds	1	1	2.7	4	33	62	86	140	280	1100	PSO_Bounds [8]
Monte Carlo	1	1.3	2.1	17	430	1.9e4	6e5	43e-4/1e6			Monte Carlo [3]
Rosenbrock	1	2.5	5.5	1.4	1.3	1.5	2	2.4	3.1	14	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1.1	2.8	2.6	3.6	4.2	4.8	9.9	11	8.3	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1	1	7.1	8.7	8.3	7.5	7.7	8.4	7.2	VNS (Garcia) [11]

Table 38: 03 D supping time every EPT/EPT on f., in italies is given the median final function value and the median number of
Table 56. 05-D, running time excess Erri / Erri hegt of J14, in rance is given the median mai function value and the median number of
unction evaluations to reach this value divided by dimension
anotion cranaations to reach this rando arriada s, annonsion

15 Rastrigin											
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{host}/D	0.333	0.778	40.5	457	2100	2760	2810	2860	2930	3010	ERThost/D
ALPS	1.3	3.3	7.6	5.3	3.9	4.2	4.4	4.6	4.8	5.1	ALPS [17]
AMaLGaM IDEA	1.3	1.8	1.2	5	3.7	3.1	3	3	3	2.9	AMaLGaM IDEA [4]
avg NEWUOA	2	3.4	3.2	3.7	3.1	2.3	2.3	2.2	2.2	2.1	avg NEWUOA [31]
BayEDAcG	1.5	2.4	3.1	11	14	11e-1/2e3					BayEDAcG [10]
BFGS	5.8	27	7.3	17	22	17	16	16	16	15	BFGS [30]
Cauchy EDA	9.2	46	3.9	5.4	27	78e-3/5e4					Cauchy EDA [24]
BIPOP-CMA-ES	1.9	4.4	1.9	1.3	1.7	1.3	1.3	1.3	1.3	1.3	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1.5	3.9	1	5.8	9.5	7.2	7.1	6.9	6.8	6.6	(1+1)-CMA-ES [2]
DASA	9.8	36	56	200	200	150	150	140	140	140	DASA [19]
DEPSO	1.5	1	3.4	6.6	3.3	2.6	2.6	2.6	10e-1/2e3		DEPSO [12]
DIRECT	1	1.4	1	1.5	1	1.7	1.7	1.7	1.7	1.7	DIRECT [25]
EDA-PSO	1.2	1.6	3.8	7.4	9.5	7.4	7.3	7.4	7.4	7.5	EDA-PSO [6]
full NEWUOA	1.3	3.3	2.2	2.8	8.8	6.7	6.5	6.4	6.3	6.1	full NEWUOA [31]
G3-PCX	1.4	2.9	40	28	39	30	29	29	28	27	G3-PCX [26]
simple GA	1.4	3	14	20	62	62	62	64	83	150	simple GA [22]
GLOBAL	1.2	2.3	2.7	3.2	3.9	3	2.9	2.9	2.8	2.7	GLOBAL [23]
iAMaLGaM IDEA	1.4	3	6.2	5.6	4.6	3.6	3.6	3.5	3.5	3.4	iAMaLGaM IDEA [4]
LSfminbnd	1	5.5	4.8	21	20	15	15	15	15	14	LSfminbnd [28]
LSstep	1.2	170	380	140	67	51	50	50	49	48	LSstep [28]
MA-LS-Chain	1.5	3.1	2.6	1.6	3.3	2.5	2.5	2.5	2.4	2.4	MA-LS-Chain [21]
MCS (Neum)	1	1.4	1.8	1	1.8	1.4	1.3	1.3	1.6	1.5	MCS (Neum) [18]
NELDER (Han)	1.3	2.9	2.3	4.6	9.4	7.1	7	6.9	6.7	6.5	NELDER (Han) [16]
NELDER (Doe)	2.3	2.5	1.4	1	2.5	1.9	1.9	1.9	1.8	1.8	NELDER (Doe) [5]
NEWUOA	1.3	2.2	3.5	3.4	4.5	3.4	3.3	3.3	3.2	3.1	NEWUOA [31]
(1+1)-ES	2.2	4.5	3.4	6.2	13	10	10	9.8	9.6	9.3	(1+1)-ES [1]
POEMS	39	190	14	32	77	59	58	57	57	56	POEMS [20]
PSO	1.5	2.8	2.7	4	58	44	44	43	42	41	PSO [7]
PSO_Bounds	1.3	3.8	2.8	27	27	21	22	22	21	22	PSO_Bounds [8]
Monte Carlo	1.5	2.2	29	1500	65e-2/1e6						Monte Carlo [3]
Rosenbrock	5.9	38	11	11	19	15	14	14	14	13	Rosenbrock [27]
IPOP-SEP-CMA-ES	1.7	4.4	2.3	2.2	1.3	1	1	1	1	1	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1.4	2.6	3	3	3.7	2.8	2.8	2.9	2.9	4.5	VNS (Garcia) [11]

Table 39: 03-D, running time excess ERT/ERT_{best} on f_{15} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

16 Weierstrass											
Δ ftarget	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget
ERT_{hest}/D	0.333	0.4	13.6	106	194	263	621	720	1070	1120	ERT_{best}/D
ALPS	1	1.1	1.1	5.9	9.1	13	9	13	10	16	ALPS [17]
AMaLGaM IDEA	1	1.6	1.8	5.2	9.7	11	6	5.3	3.9	3.7	AMaLGaM IDÉA [4]
avg NEWUOA	1	1.3	3.7	6.1	23	59	73	19e-3 / 7e3			avg NEWUOA [31]
BayEDAcG	1	1.4	1.7	25	98e-2/2e3			•			BayEDAcG [10]
BFGS	1	2.8	72	150	14e-1/7e3						BFGS [30]
Cauchy EDA	1	3	5.2	28	1100	14e-2/5e4					Cauchy EDA [24]
BIPOP-CMA-ES	1	1.5	2.1	3.5	4.3	3.3	1.7	1.5	1.1	1.1	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1.2	4.3	4.8	7.9	10	9.9	14	10	18	(1+1)-CMA-ES [2]
DASA	1	8.7	37	130	300	510	1e3	2200	2900	2900	DASA [19]
DEPSO	1	1.3	3.9	5.9	29	15e-2/2e3					DEPSO [12]
DIRECT	1	1.2	1.2	1	1	1	1	1	1.2	1.9	DIRECT [25]
EDA-PSO	1	1.3	1.5	19	110	160	97	93	73	72	EDA-PSO [6]
full NEWUOA	1	1.9	3.3	4.2	9	17	13	69	99	26e-5/8e3	full NEWUOA [31]
G3-PCX	1	1	1	3.2	11	18	13	27	58	100	G3-PCX [26]
simple GA	1	1.4	1	6	61	340	490	940	650	1300	simple GA [22]
GLOBAL	1	1.4	1.6	1.1	1.3	1.6	1.6	1.7	1.3	3.4	GLOBAL [23]
iAMaLGaM IDEA	1	1.1	1.9	1.9	10	9.2	6	5.2	3.5	3.6	iAMaLGaM IDEA [4]
LSfminbnd	1	1.2	1.6	3.5	19	50	100	12e-3/9e3			LSfminbnd [28]
LSstep	1	1.3	4	8.7	94	170	240	210	140	130	LSstep [28]
MA-LS-Chain	1	1.2	1.6	1.6	4.8	5.6	5.7	6.4	6	6.2	MA-LS-Chain [21]
MCS (Neum)	1	1.3	4.1	2.1	11	33	130	18e-4 / 2e4			MCS (Neum) [18]
NELDER (Han)	1	1.3	3.7	7	21	29	13	17	14	14	NELDER (Han) [16]
NELDER (Doe)	1	1.1	1.2	2.8	3.4	3.9	3.2	3.5	2.6	6.3	NELDER (Doe) [5]
NEWUOA	1	2.9	4.5	6.7	12	58	150	130	13e-3/6e3		NEWUOA [31]
(1+1)-ES	1	1.8	8.6	18	40	57	120	200	230	4e3	(1+1)-ES [1]
POEMS	1	120	16	24	71	210	96	84	57	57	POEMS [20]
PSO	1	1.6	1.5	3	41	77	73	66	45	59	PSO [7]
PSO_Bounds	1	1.4	1.8	6.4	58	170	120	120	95	93	PSO_Bounds [8]
Monte Carlo	1	1.3	1.8	7.9	180	4400	2.3e4	80e-4/1e6			Monte Carlo [3]
Rosenbrock	1	3	22	31	93	270	230	23e-2/1e4			Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1.4	2.1	3.5	4	3.5	1.6	1.4	1	1	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1.8	2.3	6.7	5.9	9.5	4.4	4	3	8.4	VNS (Garcia) [11]

Table 40: 03-D, running time excess ERT/ERT_{best} on f_{16} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

					17 Scha	ffer F7, co	ondition 10)			
Δ ftarget	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget
ERT _{best} /D	0.333	0.333	1.2	26.2	93.9	164	378	602	782	1160	ERT _{best} /D
ALPS	1	1.2	2.4	11	13	15	9.2	8.3	8.5	8.8	ALPS [17]
AMaLGaM IDEA	1	1.3	3.3	1.5	1	1	2.6	3.1	3.9	3	AMaLGaM IDEA [4]
avg NEWUOA	1	1.9	3.3	8	13	150	32e-3/5e3	•	•	•	avg NEWUOA [31]
BayEDAcG	1	1.7	2.3	6.7	7.6	17	9.7	16	32e-4 /2e3		BayEDAcG [10]
BFGS	1	2.1	48	44	44e-2/2e3						BFGS [30]
Cauchy EDA	1	4.9	24	7.3	4.1	3.6	2.2	1.8	1.8	1.6	Cauchy EDA [24]
BIPOP-CMA-ES	1	1.2	5.3	4	2.4	2.3	1.5	1.2	1.4	1.1	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1.1	32	7.6	7.9	32	37	75	58	76e-5/1e4	(1+1)-CMA-ES [2]
DASA	1	15	65	49	110	480	900	990	3900	1.2e4	DASA [19]
DEPSO	1	1.3	5.1	4	3.5	3.5	2.3	2.2	2.3	5	DEPSO [12]
DIRECT	1	1	1.2	1	1.2	1.5	1	1	1	1.2	DIRECT [25]
EDA-PSO	1.1	1.3	2.3	4	17	29	20	17	17	16	EDA-PSO [6]
full NEWUOA	1	1.7	3.9	5.5	7.3	31	53	35e-4 /6e3			full NEWUOA [31]
G3-PCX	1	1.3	2.6	33	39	48	47	110	290	640	G3-PCX [26]
simple GA	1	1.1	1.4	30	57	72	72	65	120	58e-8/1e5	simple GA [22]
GLOBAL	1	1.5	3	4.2	7.3	21	98e-3/400				GLOBAL [23]
iAMaLGaM IDEA	1	1.4	2.4	1	3.1	2.7	3.1	4.4	3.6	3	iAMaLGaM IDEA [4]
LSfminbnd	1	1.2	14	8.2	30	140	21e-3/1e4				LSfminbnd [28]
LSstep	1	1.5	71	200	100	880	69e-3/1e4				LSstep [28]
MA-LS-Chain	1	1.4	2.1	3.4	4	4.9	3.1	2.6	2.3	2	MA-LS-Chain [21]
MCS (Neum)	1	1	1	2.5	5.6	16	180	35e-4 /2e4			MCS (Neum) [18]
NELDER (Han)	1	1	62	22	44	95	95	110	250	400	NELDER (Han) [16]
NELDER (Doe)	1	1.2	1.9	3.7	8.5	36	69	12e-4 /2e4			NELDER (Doe) [5]
NEWUÒA	1	1.6	2.7	9	19	140	32e-3 /5e3				NEWUOA [31]
(1+1)-ES	1	2.5	24	33	870	2300	4100	12e-4 /1e6			(1+1)-ES [1]
POÉMS	1	93	140	20	23	28	17	18	16	15	POEMS [20]
PSO	1	1.1	2.8	4.4	80	55	26	18	15	14	PSO [7]
PSO_Bounds	1	1.3	2.5	4.7	14	21	14	13	25	28	PSO_Bounds [8]
Monte Carlo	1	1.1	2.4	30	7200	92e-3/1e6					Monte Carlo [3]
Rosenbrock	1	1.3	81	2200	20e-1 /8e3						Rosenbrock [27]
POP-SEP-CMA-ES	1	1.2	2.8	1.8	2.1	1.8	1.4	1	1.1	1	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1	2.9	2.9	12	17	1 9	<u>່</u>	1.8	18	VNS (Carcia) [11]

RT	
n°	
0383	

Table 42: 03-D, run	nning ti s to rea	me exce	ss ERT, value di	/ERT _{best} c vided by di	on f_{18} , in its mension	alics is give	n the media	n final func	tion value a	and the med	dian number of	Compa
	10 100		varae ar	vided by di	18 Schaffe	r F7. cond	lition 1000					uri
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$	00
ERT _{best} /D	0.333	0.4	13.4	48.2	430	1030	1170	1310	1580	1840	ERT _{best} /D	2
ALPS	1.3	2.6	5	17	5.5	5.2	7.2	13	18	140	ALPS [17]	3
AMaLGaM IDEA	1.2	3.4	1.6	6.1	3.5	3.2	3.1	2.9	2.5	2.5	AMaLGaM IDEA [4]	7
avg NEWUOA	1.3	4.8	11	30	15	89	76e-3/6e3				avg NEWUOA [31]	1 -
BayEDAcG	1.1	3	4.5	9.7	67	20e-2/2e3					BayEDAcG [10]	
BFGS	1	16	33	29e-1 /3e3							BFGS [30]	7
Cauchy EDA	1.3	31	280	80	9.4	4.3	4	8.5	7.3	6.6	Cauchy EDA [24]	J
BIPOP-CMA-ES	1.1	3.4	1.4	3.4	1.8	1.1	1	1	1.1	1.3	BIPOP-CMA-ES [15]	Š
(1+1)-CMA-ES	1.2	3.8	2.7	5	8.3	22	40	16e-3/1e4			(1+1)-CMA-ES [2]	J
DASA	5.6	93	91	980	460	1600	10e-3/1e6				DASA [19]	Э
DEPSO	1.3	2.4	3.8	12	3.4	5.1	12	18e-3/2e3			DEPSO [12]	2
DIRECT	1	1.5	1.1	2.7	1	1	2	2.9	5	8.3	DIRECT [25]	5
EDA-PSO	1	4.5	2.4	28	13	9.3	12	13	14	16	EDA-PSO [6]	н
full NEWUOA	1.1	4.6	4.2	16	13	48e-3 /7e3					full NEWUOA [31]	1
G3-PCX	1.1	3.3	2.4	11	18	63	91e-4 /5e4				G3-PCX [26]	
simple GA	1	3.2	6.3	63	42	420	1200	17e-3/1e5			simple GA [22]	1.
GLOBAL	1.2	2.7	3.9	5.7	4.6	21e-2/500					GLOBAL [23]	
iAMaLGaM IDEA	1.1	1.9	1	1	1.6	3.3	3.7	3.9	3.4	3.8	iAMaLGaM IDEA [4]	_
LSfminbnd	1	4.4	8.7	35	33	10e-2/1e4					LSfminbnd [28]	, i
LSstep	1	25	42	360	330	12e-1/1e4					LSstep [28]	1
MA-LS-Chain	1.1	2.3	3	4.8	5.3	12	11	13	12	11	MA-LS-Chain [21]	1
MCS (Neum)	1	1	4	2.9	20	40e-3/2e4					MCS (Neum) [18]	7
NELDER (Han)	1.1	4.2	25	27	30	45	120	550	98e-5/1e5	•	NELDER (Han) [16]	
NELDER (Doe)	1.1	3.5	1.9	5.4	7	16	72	200	170	63e-4 /2e4	NELDER (Doe) [5]	
NEWUOA	1	5.1	7.2	17	34	12e-2/6e3					NEWUOA [31]	
(1+1)-ES	1.8	9	340	300	2800	1.4e4	1.2e4	83e-3/1e6			(1+1)-ES [1]	
POEMS	42	250	25	180	25	24	50	95	100	170	POEMS [20]	
PSO	1	2.7	2	16	57	77	99	92	110	180	PSO [7]	
PSO_Bounds	1	2.7	2	170	65	57	67	68	69	780	PSO_Bounds [8]	
Monte Carlo	1.1	2.2	4.7	450	26e-2/1e6						Monte Carlo [3]	
Rosenbrock	1.1	160	220	2300	50e-1/8e3						Rosenbrock [27]	
IPOP-SEP-CMA-ES	1.2	4.7	1.2	1.8	2.1	1	1.1	1	1	1	IPOP-SEP-CMA-ES [29	<i>i</i>]
VNS (Garcia)	1.2	3.5	3.2	2.3	4.3	5.3	6.6	13	45	130	VNS (Garcia) [11]	

19 Griewank-Rosenbrock F8F2												
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$	
ERT_{best}/D	0.333	0.333	0.333	0.333	36.5	2250	2460	2460	2470	2480	ERT_{hest}/D	
ALPS	1	1	11	470	46	3	4.6	5.2	5.5	7.1	ALPS [17]	
AMaLGaM IDEA	1	1.2	13	120	36	3.8	5.9	6	6	6	AMaLGaM IDEA [4]	
avg NEWUOA	1	1.5	13	320	120	39	76	76	76	76	avg NEWUOA [31]	
BayEDAcG	1	1.1	9.9	130	43	64e-3/2e3					BayEDAcG [10]	
BFGS	1	37	110	870	160	33	86e-3/5e3				BFGS [30]	
Cauchy EDA	1	2.3	57	540	310	53e-3/5e4					Cauchy EDA [24]	
BIPOP-CMA-ES	1	1.5	13	100	49	2.9	3.2	3.2	3.2	3.3	BIPOP-CMA-ES [15]	
(1+1)-CMA-ES	1	1	6.1	970	160	8.8	17	17	17	17	(1+1)-CMA-ES [2]	
DASA	1	3.3	60	5100	520	230	460	460	460	480	DASA [19]	
DEPSO	1	1	5.4	240	41	43e-3/2e3					DEPSO [12]	
DIRECT	1	1	1	1	1	29	60	60	10e-3/3e4		DIRECT [25]	
EDA-PSO	1	1.4	9.1	370	82	5.8	11	12	13	16	EDA-PSO [6]	
full NEWUOA	1	1.7	25	370	56	11	17	17	17	17	full NEWUOA [31]	
G3-PCX	1	1.1	7.6	920	640	100	95	95	95	94	G3-PCX [26]	
simple GA	1	1.2	7.1	930	100	19	39	50	81	68e-6/1e5	simple GA [22]	
GLOBAL	1	1.1	14	290	46	3.9	94e-3/1e3				GLOBAL [23]	
iAMaLGaM IDEA	1	1.2	10	160	73	7.6	7.7	7.7	7.7	7.7	iAMaLGaM IDEA [4]	
LSfminbnd	1	3	26	270	54	46	38e-3 / 7e3				LSfminbnd [28]	
LSstep	1	2	8.9	650	26	63	28e-3/1e4				LSstep [28]	
MA-LS-Chain	1	1.1	7.6	190	20	1.6	2.2	2.2	2.2	2.3	MA-LS-Chain [21]	
MCS (Neum)	1	1	1	1	11	1	1	1	1	1	MCS (Neum) [18]	
NELDER (Han)	1	1	4.1	1500	120	17	40	40	40	40	NELDER (Han) [16]	
NELDER (Doe)	1	1.1	7.6	150	20	5.4	11	11	11	11	NELDER (Doe) [5]	
NEWUOA	1	1.5	20	1300	280	25	54	54	54	53	NEWUOA [31]	
(1+1)-ES	1	2.3	10	2.1e5	3.1e4	1800	2600	2600	2600	2600	(1+1)-ES [1]	
POEMS	1	130	630	1400	170	40	57	58	58	59	POEMS [20]	
PSO	1	1.1	10	240	24	14	24	25	25	28	PSO [7]	
PSO_Bounds	1	1.1	6.7	250	91	13	26	27	30	35	PSO_Bounds [8]	
Monte Carlo	1	1.1	11	1e3	810	490	2900	6100	6100	79e-4 /1e6	Monte Carlo [3]	
Rosenbrock	1	15	250	3100	850	32	27e-2/1e4				Rosenbrock [27]	
IPOP-SEP-CMA-ES	1	1.1	9.1	190	54	2.6	2.4	2.4	2.5	2.5	IPOP-SEP-CMA-ES [29]	
VNS (Garcia)	1	1.4	23	220	36	4.8	6	6.1	6.3	10	VNS (Garcia) [11]	

Table 43: 03-D, running time excess ERT/ERT_{best} on f_{19} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

a4: 05-D, runnin on evaluations to	reach t	excess E his valu	e divide	d by di	mension	uncs is given	n the media	in inal	Tunctio	m value	e and the median
	1000011 0	ino rara	o antiao	a og an	20 Schwef	el x*sin(x	;)				
Δ ftarget	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{best}/D	1.84	2.6	2.76	128	764	799	827	842	858	925	ERT _{best} /D
ALPS	2.8	4.1	5.1	5	3.9	4.6	5.3	6.2	7.2	8.2	ALPS [17]
AMaLGaM IDEA	2.2	2.2	2.7	20	26	25	25	25	24	23	AMaLGaM IDEA
avg NEWUOA	1.5	1.3	1.3	2.3	9.9	9.5	9.2	9	8.9	8.2	avg NEWUOA
BayEDAcG	3.1	3	3.2	71	13e-1/2e3						BayEDAcG [1
BFGS	1.8	1.7	1.9	1.7	5.5	5.3	5.1	5	4.9	4.6	BFGS [30]
Cauchy EDA	17	18	20	10	460	930	31e-2/5e4				Cauchy EDA [
BIPOP-CMA-ES	2.2	2.1	2.3	8.2	10	10	10	10	10	9.5	BIPOP-CMA-ES
(1+1)-CMA-ES	2.1	2.6	2.7	5.6	9.5	9.1	8.8	8.7	8.5	7.9	(1+1)-CMA-ES
DASA	31	37	37	21	43	41	40	39	38	36	DASA [19]
DEPSO	1.1	4.1	5.9	2.4	4.9	4.8	4.8	4.9	4.8	4.7	DEPSO [12]
DIRECT	3.7	5.2	5.9	1	9	8.7	8.6	8.5	8.5	8.1	DIRECT 25
EDA-PSO	2.3	3.4	3.6	6.7	4.5	4.9	5.1	5.3	5.6	6.1	EDA-PSO [6
full NEWUOA	1.9	1.3	1.2	5.2	9.1	8.7	8.4	8.3	8.1	7.5	full NEWUOA
G3-PCX	1.5	2.8	3.5	17	22	21	21	20	20	19	G3-PCX [26]
simple GA	3.2	4.3	5.1	14	7.1	10	14	17	21	29	simple GA [2
GLOBAL	1.3	2.7	3.4	6	18	17	17	16	16	15	GLOBAL 23
iAMaLGaM IDEA	2.3	2.9	3.7	16	19	18	18	18	17	16	iAMaLGaM IDE
LSfminbnd	6.4	6.1	6.8	9.9	42e-2/1e4						LSfminbnd [2
LSstep	150	180	220	28	180	180	170	170	170	160	LSstep [28]
MA-LS-Chain	2.5	2.3	2.8	2.5	1	1	1	1	1	1	MA-LS-Chain
MCS (Neum)	2.9	2.2	2.3	3.2	3.5	3.4	3.3	3.2	3.1	2.9	MCS (Neum)
NELDER (Han)	1	1	1	19	25	24	23	23	23	21	NELDER (Han)
NELDER (Doe)	1.5	1.5	1.7	3.6	10	10	9.7	9.5	9.4	8.7	NELDER (Doe)
NEWUÒA	1.6	1.4	1.3	1.1	3.9	3.7	3.6	3.5	3.4	3.2	NEWUOA [3]
(1+1)-ES	2.2	3.1	3.1	4.7	9.5	9.1	8.8	8.7	8.5	7.9	(1+1)-ES [1]
POÉMS	110	87	84	7.4	65	63	63	69	69	66	POEMS [20]
PSO	1.4	3.2	3.7	2.6	22	22	21	21	21	20	PSO [7]
PSO_Bounds	2.1	2.7	3.2	5.2	52	78	76	85	84	80	PSO_Bounds [
Monte Carlo	1.3	2.6	3.1	56	1600	94e-3/1e6					Monte Carlo
Rosenbrock	3	2.6	2.5	1.5	10	9.5	9.2	9.1	8.9	8.3	Rosenbrock [2
POP-SEP-CMA-ES	1.7	2.1	2.8	7.9	5.5	5.5	5.4	5.5	5.4	5.2	IPOP-SEP-CMA-E
VNS (Garcia)	3.7	2.8	2.9	4.4	5.5	5.3	5.1	5.1	5.2	5.8	VNS (Garcia)

), running time excess ERT/ERT_{best} on f_{20} , in italics is given the median final function value and the median number of										
ations to reach this value divided by dimension										
20 Schwofel x^* $\sin(x)$										

21 Gallagher 101 peaks											
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{best}/D	0.333	0.333	1.98	61.3	142	146	153	155	156	161	ERT_{best}/D
ALPS	1	1	1.3	2.3	3.7	5.8	7.4	8.8	11	15	ALPS [17]
AMaLGaM IDEA	1	1	2.2	17	41	41	40	40	40	39	AMaLGaM IDÉA [4]
avg NEWUOA	1	1	4	2.5	2.1	2	2	2	2	2	avg NEWUOA [31]
BayEDAcG	1	1	2.1	7.5	94	63e-2/2e3				•	BayEDAcG [10]
BFGS	1	1	2.1	3.3	3.5	3.4	3.3	3.3	3.2	3.2	BFGS [30]
Cauchy EDA	1	1	16	11	240	240	500	650	890	860	Cauchy EDA [24]
BIPOP-CMA-ES	1	1	1.7	6.8	6	6.1	6	6	6.1	6.1	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1	1.9	4.5	8.1	8	7.7	7.6	7.5	7.4	(1+1)-CMA-ES [2]
DASA	1	1	12	93	66	65	62	62	62	61	DASA [19]
DEPSO	1	1	1.2	4.1	3.5	4.6	5.3	6.6	7.1	7.5	DEPSO [12]
DIRECT	1	1	1.9	1	1.4	1.4	1.4	3.8	4.2	5.8	DIRECT [25]
EDA-PSO	1	1	1.4	3.2	54	55	58	59	62	65	EDA-PSO [6]
full NEWUOA	1	1	2.4	3.3	2.8	2.7	2.6	2.6	2.6	2.6	full NEWUOA [31]
G3-PCX	1	1	1.6	8.6	5.7	5.6	5.4	5.4	5.4	5.4	G3-PCX [26]
simple GA	1	1	1.5	2.5	5.3	18	29	43	99	230	simple GA [22]
GLOBAL	1	1	1.8	1.4	1	1	1	1	1	1	GLOBAL [23]
iAMaLGaM IDEA	1	1	1.6	28	20	19	19	18	18	18	iAMaLGaM IDEA [4]
LSfminbnd	1	1	6.1	21	27	26	31	38	39	46	LSfminbnd [28]
LSstep	1	1	15	210	200	190	190	200	200	220	LSstep [28]
MA-LS-Chain	1	1	1.7	1.7	9.7	9.8	9.6	9.7	9.7	9.7	MA-LS-Chain [21]
MCS (Neum)	1	1	6.2	2.1	4.4	4.3	4.1	4.1	4.1	4.2	MCS (Neum) [18]
NELDER (Han)	1	1	1.6	16	26	25	24	23	23	23	NELDER (Han) [16]
NELDER (Doe)	1	1	2	2.8	2.9	2.8	2.7	2.7	2.7	2.6	NELDER (Doe) $[5]$
NEWUOA	1	1	1.6	2.7	3.5	3.5	3.4	3.4	3.4	3.4	NEWUOA [31]
(1+1)-ES	1	1	2	15	17	17	16	16	16	16	(1+1)-ES [1]
POEMS	1	1	95	680	550	540	510	510	510	500	POEMS [20]
PSO	1	1	1.2	120	110	110	100	100	100	100	PSO [7]
PSO_Bounds	1	1	1	120	180	170	170	170	170	170	PSO_Bounds [8]
Monte Carlo	1	1	1.5	2.9	8.3	34	120	980	4500	62e-7/1e6	Monte Carlo [3]
Rosenbrock	1	1	17	8.1	12	11	11	11	11	11	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1	1	4.6	15	17	17	17	17	17	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1	2.1	9.2	11	11	11	11	11	11	VNS (Garcia) [11]

Table 45: 03-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{21} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

22 Gallagher 21 peaks											
Δ ftarget	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget
ERThost/D	0.333	0.333	6.02	56.7	118	121	128	132	134	138	ERT_{host}/D
ALPS	1	1	1.8	2.1	4	8.5	12	17	21	28	ALPS [17]
AMaLGaM IDEA	1	1	1.1	21	56	61	59	58	57	57	AMaLGaM IDEA [4]
avg NEWUOA	1	1	2.8	2	2.9	2.9	2.8	2.9	2.9	3.1	avg NEWUOA [31]
BayEDAcG	1	1	2	11	48	36e-2/2e3					BayEDAcG [10]
BFGS	1	1	3.3	2.6	2.1	2.1	2	2	2	2	BFGS [30]
Cauchy EDA	1	1	12	230	640	1100	2500	2500	2400	2400	Cauchy EDA [24]
BIPOP-CMA-ES	1	1	1.1	6.4	13	14	13	13	13	13	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1	3.5	6.8	11	10	9.8	9.7	9.6	9.4	(1+1)-CMA-ES [2]
DASA	1	1	20	100	69	75	79	88	98	120	DASA [19]
DEPSO	1	1	4.8	4.7	13	14	14	18	26	34	DEPSO [12]
DIRECT	1	1	1.5	1	6.3	6.2	7.4	9.8	15	18	DIRECT [25]
EDA-PSO	1	1	1.2	3.9	5.4	11	16	22	29	42	EDA-PSO [6]
full NEWUOA	1	1	2.3	2	1.8	1.9	1.9	1.9	1.9	2.1	full NEWUOA [31]
G3-PCX	1	1	1.4	4.1	10	10	9.8	9.7	9.7	9.6	G3-PCX [26]
simple GA	1	1	1	3.5	6.5	27	270	950	1600	3100	simple GA [22]
GLOBAL	1	1	1.6	1.6	1	1	1	1	1	1	GLOBAL [23]
iAMaLGaM IDEA	1	1	1.6	21	43	44	43	42	43	42	iAMaLGaM IDEA [4]
LSfminbnd	1	1	14	13	19	66	62	70	77	150	LSfminbnd [28]
LSstep	1	1	64	48	160	240	320	16e-2/1e4			LSstep [28]
MA-LS-Chain	1	1	1.4	3.7	2.7	3.3	3.4	3.5	3.8	4.3	MA-LS-Chain [21]
MCS (Neum)	1	1	3.3	1.6	1.2	1.2	4.6	4.6	4.5	4.6	MCS (Neum) [18]
NELDER (Han)	1	1	5.5	10	13	13	12	12	12	12	NELDER (Han) [16]
NELDER (Doe)	1	1	4.1	2	2.2	2.2	2.1	2	2	2	NELDER (Doe) $[5]$
NEWUOA	1	1	2.8	2.5	5.8	5.8	5.6	5.5	5.5	5.7	NEWUOA [31]
(1+1)-ES	1	1	23	17	17	17	17	18	19	20	(1+1)-ES [1]
POEMS	1	1	42	170	450	450	420	420	410	410	POEMS [20]
PSO	1	1	1.1	130	130	130	120	120	120	120	PSO [7]
PSO_Bounds	1	1	1.5	2.2	64	65	67	69	76	88	PSO_Bounds [8]
Monte Carlo	1	1	1.7	3	4.8	40	200	1500	7100	30e-7/1e6	Monte Carlo [3]
Rosenbrock	1	1	1.7	5.6	5.2	5.3	5.1	5.1	5.1	5	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1	1.7	3.9	13	31	30	30	29	29	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1	1.4	10	12	13	13	14	14	15	VNS (Garcia) [11]

Table 46: 03-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{22} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

23 Katsuuras												
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$	
ERT_{host}/D	0.333	0.333	0.867	136	302	405	738	751	764	798	ERThost/D	
ALPS	1	1	3.7	12	54	200	370	890	6300	3e4	ALPS [17]	
AMaLGaM IDEA	1	1	3.9	6.3	10	8.9	5.1	5.1	5.1	5.1	AMaLGaM IDEA [4]	
avg NEWUOA	1	1	11	2.5	22	85	150	46e-3 /7e3			avg NEWUOA [31]	
BayEDAcG	1	1	3.2	34	11e-1/2e3						BayEDAcG [10]	
BFGS	1	1	17	8.7	110	23e-2/5e3					BFGS [30]	
Cauchy EDA	1	1	4.1	52	51e-2/5e4						Cauchy EDA [24]	
BIPOP-CMA-ES	1	1	4.9	6.4	9.3	7.1	4.2	4.2	4.2	4.2	BIPOP-CMA-ES [15]	
(1+1)-CMA-ES	1	1	3.7	2	11	17	12	12	12	12	(1+1)-CMA-ES [2]	
DASA	1	1	15	71	880	1700	1900	5400	5300	5100	DASA [19]	
DEPSO	1	1	1.9	40	12e-1 /2e3						DEPSO [12]	
DIRECT	1	1	4.7	1.5	31	25	15	16	18	22	DIRECT [25]	
EDA-PSO	1	1	2.9	23	4900	3700	2e3	31e-2/1e5			EDA-PSO [6]	
full NEWUOA	1	1	6.7	2.4	15	40	37	170	170	160	full NEWUOA [31]	
G3-PCX	1	1	4.9	2.1	14	29	17	30	43	42	G3-PCX [26]	
simple GA	1	1	4.3	16	520	3700	88e-3/1e5				simple GA [22]	
GLOBAL	1	1	3.1	1.6	3.1	81e-3/1e3	•	•			GLOBAL [23]	
iAMaLGaM IDEA	1	1	4.4	8.4	9.7	7.5	4.3	4.3	4.3	4.3	iAMaLGaM IDEA [4]	
LSfminbnd	1	1	3.2	7.1	420	31e-2/9e3					LSfminbnd [28]	
LSstep	1	1	5.6	4.9	490	25e-2/1e4					LSstep [28]	
MA-LS-Chain	1	1	4.1	2.1	6.7	5.2	2.9	3.1	3.1	3.1	MA-LS-Chain [21]	
MCS (Neum)	1	1	1	2.7	12	39	330	77e-4 /2e4			MCS (Neum) [18]	
NELDER (Han)	1	1	3.1	1.4	2.3	1.8	1	1	1	1	NELDER (Han) [16]	
NELDER (Doe)	1	1	6.7	1	1	1	1.1	1.4	1.4	1.4	NELDER (Doe) [5]	
NEWUOA	1	1	11	2.7	24	110	68e-3/6e3				NEWUOA [31]	
(1+1)-ES	1	1	21	2.9	13	240	510	1500	1800	3500	(1+1)-ES [1]	
POEMS	1	1	18	22	130	130	73	75	76	79	POEMS [20]	
PSO	1	1	3.2	11	170	360	200	200	200	190	PSO [7]	
PSO_Bounds	1	1	1.9	15	460	570	440	450	930	890	PSO_Bounds [8]	
Monte Carlo	1	1	2.6	13	2.3e4	13e-2/1e6					Monte Carlo [3]	
Rosenbrock	1	1	2.4	1.9	10	88	48	31e-3/5e3			Rosenbrock [27]	
IPOP-SEP-CMA-ES	1	1	4.6	7.1	13	11	5.9	5.9	5.9	5.8	IPOP-SEP-CMA-ES [29]	
VNS (Garcia)	1	1	4.6	6.7	27	41	23	23	24	23	VNS (Garcia) [11]	

Table 47: 03-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{23} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

24 Lunacek bi-Rastrigin													
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$		
ERT_{hest}/D	0.333	0.333	32.2	3460	34200	1.19e5	1.19e5	1.19e5	1.19e5	1.19e5	ERT_{best}/D		
ALPS	1	1.1	7.9	3.5	6.2	2.9	2.9	3	3	3.1	ALPS [17]		
AMaLGaM IDEA	1	1.2	1.5	9.7	10	4.5	4.6	4.7	4.7	5.1	AMaLGaM IDEA [4]		
avg NEWUOA	1	2.6	3.7	1.2	2.4	64e-2/6e3					avg NEWUOA [31]		
BayEDAcG	1	1.3	4.3	40e-1/2e3		•					BayEDAcG [10]		
BFGS	1	1.8	9.3	41e-1/3e3							BFGS [30]		
Cauchy EDA	1.1	1.7	4.2	100	31e-1/5e4						Cauchy EDA [24]		
BIPOP-CMA-ES	1	1	1.3	7.6	7.9	3	4.1	4.9	4.9	4.9	BIPOP-CMA-ES [15]		
(1+1)-CMA-ES	1	1	9.2	3.3	91e-2/1e4						(1+1)-CMA-ES [2]		
DASA	1	1	69	85	420	37e-2/1e6					DASA [19]		
DEPSO	1	1	5.8	48e-1/2e3	•	•					DEPSO [12]		
DIRECT	1	1	2.5	39	30e-1/3e4						DIRECT [25]		
EDA-PSO	1	1.2	6.4	30e-1/1e5	•						EDA-PSO [6]		
full NEWUOA	1	1.7	2.8	1.2	76e-2/6e3						full NEWUOA [31]		
G3-PCX	1	1.1	19	22	10	10e-1/5e4					G3-PCX [26]		
simple GA	1	1.1	18	32e-1/1e5	•						simple GA [22]		
GLOBAL	1	1	3.4	1.1	27e-1/2e3						GLOBAL [23]		
iAMaLGaM IDEA	1	1.5	5.3	5.8	9.9	8.7	8.7	8.7	8.7	8.8	iAMaLGaM IDEA [4]		
LSfminbnd	1	1.1	1.9	6.4	12e-1/1e4						LSfminbnd [28]		
LSstep	3	3.1	6.5	41	35e-1/1e4						LSstep [28]		
MA-LS-Chain	1	1.1	3.7	30e-1/2e4							MA-LS-Chain [21]		
MCS (Neum)	1	1	17	2	1	1	1	1	1	1	MCS (Neum) [18]		
NELDER (Han)	1	1	20	5.2	10	6.3	6.3	6.3	6.3	6.3	NELDER (Han) [16]		
NELDER (Doe)	1	1	2.3	1.5	3.9	2.4	2.4	2.4	2.4	2.4	NELDER (Doe) [5]		
NEWUOA	1	1.5	2.5	1	45e-2/6e3						NEWUOA [31]		
(1+1)-ES	1	2.5	23	13	40	120	120	120	120	120	(1+1)-ES [1]		
POEMS	1	58	16	86	42	12	12	12	12	12	POEMS [20]		
PSO	1	1	4.7	400	31e-1/1e5						PSO [7]		
PSO_Bounds	1	1.1	9.1	410	42	12	12	12	12	12	PSO_Bounds [8]		
Monte Carlo	1	1.3	10	450	10e-1/1e6						Monte Carlo [3]		
Rosenbrock	1	1.1	54	36e-1/1e4							Rosenbrock [27]		
IPOP-SEP-CMA-ES	1	1	1	5	13e-1/1e4						IPOP-SEP-CMA-ES [29]		
VNS (Garcia)	1	1.6	2.9	1.6	110	64	64	64	65	110	VNS (Garcia) [11]		

Table 48: 03-D, running time excess ERT/ERT_{best} on f_{24} , in italics is given the median final function value and the median number of
function evaluations to reach this value divided by dimension

1 Sphere													
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget		
ERT _{bost} /D	0.2	0.2	2.2	2.44	2.44	2.44	2.44	2.44	2.44	2.44	ERThost/D		
ALPS	1	1.6	9.2	140	300	490	680	850	1e3	1400	ALPS [17]		
AMaLGaM IDEA	1	1.5	5.5	16	29	44	58	72	87	120	AMaLGaM IDEA [4]		
avg NEWUOA	1	3.3	1.5	1.3	1.3	1.3	1.3	1.3	1.3	1.3	avg NEWUOA [31]		
BayEDAcG	1	1.2	5.2	46	92	130	170	280	390	560	BayEDAcG [10]		
BFGS	1	3.4	1.2	1.1	1.1	1.1	1.1	1.1	1.1	1.1	BFGS [30]		
Cauchy EDA	1	24	41	90	170	240	310	400	460	600	Cauchy EDA [24]		
BIPOP-CMA-ES	1	2.1	3.2	9	15	21	27	33	40	53	BIPOP-CMA-ES [15]		
(1+1)-CMA-ES	1	1.3	2.3	5.9	9.7	14	17	21	25	32	(1+1)-CMA-ES [2]		
DASA	1	5.2	23	44	59	71	88	110	120	150	DASA [19]		
DEPSO	1	1.3	8.1	26	48	77	110	130	170	220	DEPSO [12]		
DIRECT	1	1	2	7	19	31	44	62	84	150	DIRECT [25]		
EDA-PSO	1	1.1	3.2	20	320	890	1500	2100	2700	3800	EDA-PSO [6]		
full NEWUOA	1	2.9	1.9	1.8	1.8	1.8	1.8	1.8	1.8	1.8	full NEWUOA [31]		
G3-PCX	1	1.5	5.2	12	15	19	25	31	35	45	G3-PCX [26]		
simple GA	1	1.5	8.7	360	1200	2100	2900	4100	5400	8300	simple GA [22]		
GLOBAL	1	1.3	6.8	26	28	30	32	33	35	39	GLOBAL [23]		
iAMaLGaM IDEA	1	1.4	2.5	9.8	19	28	36	47	56	73	iAMaLGaM IDEA [4]		
LSfminbnd	1	2.8	6	6.3	6.7	6.7	6.8	6.8	6.8	6.8	LSfminbnd [28]		
LSstep	1	140	92	120	130	130	130	130	130	130	LSstep [28]		
MA-LS-Chain	1	1.3	7.8	25	47	60	74	90	120	140	MA-LS-Chain [21]		
MCS (Neum)	1	1	1	1.8	2.5	2.6	2.6	2.6	2.6	2.6	MCS (Neum) [18]		
NELDER (Han)	1	1.7	1.5	3.3	5.4	7.2	9.2	11	13	17	NELDER (Han) [16]		
NELDER (Doe)	1	2.3	1.5	3.4	5.6	7.4	9.5	11	13	17	NELDER (Doe) [5]		
NEWUOA	1	2.4	1.1	1	1	1	1	1	1	1	NEWUOA [31]		
(1+1)-ES	1	1.2	2.3	5	8.4	11	15	18	22	28	(1+1)-ES [1]		
POEMS	1	240	110	130	380	760	1200	1600	2100	2900	POEMS [20]		
PSO	1	1.3	3.7	22	55	110	180	240	320	450	PSO [7]		
PSO_Bounds	1	1.2	3.8	41	210	430	730	980	1300	1900	PSO_Bounds [8]		
Monte Carlo	1	1.4	7.5	1700	6.8e5	10e-2/1e6					Monte Carlo [3]		
Rosenbrock	1	2.9	2.9	4.2	5.5	6.8	8.7	10	12	15	Rosenbrock [27]		
IPOP-SEP-CMA-ES	1	1.5	2.8	7	14	18	23	29	34	44	IPOP-SEP-CMA-ES [29]		
VNS (Garcia)	1	1.6	7.4	18	25	31	38	45	50	64	VNS (Garcia) [11]		

Table 49: 05-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_1 ,	italics is given the median final function value and the median number of
function evaluations to reach this value divided by dimensio	

2 Ellipsoid separable													
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$		
ERT_{best}/D	9.71	14.9	16.7	17.5	17.7	17.9	18	18.2	18.4	18.8	ERT_{best}/D		
ALPS	45	55	73	95	120	150	170	190	210	260	ALPS [17]		
AMaLGaM IDEA	5.2	5.3	7.1	10	13	15	17	19	21	24	AMaLGaM IDEA [4]		
avg NEWUOA	1.2	2	6.4	21	41	56	75	92	110	150	avg NEWUOA [31]		
BayEDAcG	32	38	41	46	52	58	64	79	84	95	BayEDAcG [10]		
BFGS	3.3	3.4	3.8	5.6	6.2	6.5	6.6	6.8	6.9	7.1	BFGS [30]		
Cauchy EDA	35	35	42	49	58	71	80	91	100	120	Cauchy EDA [24]		
BIPOP-CMA-ES	11	11	13	16	18	19	20	20	21	22	BIPOP-CMA-ES [15]		
(1+1)-CMA-ES	5.6	6.6	9.4	11	12	13	14	14	14	15	(1+1)-CMA-ES [2]		
DASA	10	8.6	9.7	12	13	15	17	19	21	26	DASA [19]		
DEPSO	11	11	13	16	21	24	28	32	37	44	DEPSO [12]		
DIRECT	4.2	4.3	5.7	7.2	8.4	10	14	16	22	380	DIRECT [25]		
EDA-PSO	8.6	58	140	210	290	360	420	490	550	690	EDA-PSO [6]		
full NEWUOA	1.5	2.7	6.9	19	36	50	69	87	100	130	full NEWUOA [31]		
G3-PCX	15	30	69	150	220	280	340	410	470	620	G3-PCX [26]		
simple GA	180	230	330	460	610	770	1300	1500	2200	2500	simple GA [22]		
GLOBAL	7.1	5.4	6.3	6.9	7.3	7.5	7.8	8	8.2	8.5	GLOBAL [23]		
iAMaLGaM IDEA	4.4	4.7	6.2	8.1	10	12	13	14	15	17	iAMaLGaM IDEA [4]		
LSfminbnd	1.5	1.1	1	1	1	1	1	1	1	1	LSfminbnd [28]		
LSstep	25	17	16	16	16	15	15	15	15	15	LSstep [28]		
MA-LS-Chain	7.9	10	13	16	22	27	32	36	41	49	MA-LS-Chain [21]		
MCS (Neum)	1.3	1	1.1	1.5	2.2	3.2	4.7	5.7	6.5	29	MCS (Neum) [18]		
NELDER (Han)	2.4	2.7	5	6.8	7.4	7.7	7.9	8.1	8.3	8.6	NELDER (Han) [16]		
NELDER (Doe)	2	2.5	4.9	8.1	8.9	9.3	9.6	9.8	10	10	NELDER (Doe) $[5]$		
NEWUOA	1	1.8	5.7	22	45	60	85	100	130	170	NEWUOA [31]		
(1+1)-ES	110	1600	5600	1.6e4	3e4	4.6e4	1.9e5	2.6e5	8e5	19e-4/1e6	(1+1)-ES [1]		
POEMS	150	160	210	270	330	380	440	470	520	630	POEMS $[20]$		
PSO	19	25	32	41	49	59	68	78	89	110	PSO [7]		
PSO_Bounds	47	83	150	190	260	300	400	590	860	1200	PSO_Bounds [8]		
Monte Carlo	1800	1.2e5	11e + 1/1e6								Monte Carlo [3]		
Rosenbrock	2.2	8.6	13	100	140	140	150	190	190	240	Rosenbrock [27]		
IPOP-SEP-CMA-ES	5.4	5.7	7.2	8.5	9.4	10	11	11	12	13	IPOP-SEP-CMA-ES [29]		
VNS (Garcia)	15	14	18	20	24	24	25	26	26	27	VNS (Garcia) [11]		

Table 50: 05-D, running time excess ERT/ERT_{best} on f_2 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

3 Rastrigin separable												
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget	
ERT _{best} /D	0.2	2.92	143	324	327	328	329	330	330	331	ERT _{best} /D	
ALPS	1.5	2	5.7	12	22	24	26	28	29	33	ALPS [17]	
AMaLGaM IDEA	1.5	2.1	4.5	65	480	500	510	520	520	520	AMaLGaM IDEA [4]	
avg NEWUOA	3.3	4.8	3	130	40e-1/6e3						avg NEWUOA [31]	
BayEDAcG	1.2	1.7	2.7	29e-1/2e3							BayEDAcG [10]	
BFGS	7.4	56	110	21e + 0/4e3							BFGS [30]	
Cauchy EDA	35	25	6.7	2200	26e-1/5e4						Cauchy EDA [24]	
BIPOP-CMA-ES	3.5	1.5	1.4	16	140	140	140	140	140	140	BIPOP-CMA-ES [15]	
(1+1)-CMA-ES	2.2	1.3	9.1	440	30e-1/1e4						(1+1)-CMA-ES [2]	
DASA	8.7	18	1.2	1.6	10	10	10	10	10	11	DASA [19]	
DEPSO	1.4	2.9	3.7	29	30	30	30	23e-1/2e3			DEPSO [12]	
DIRECT	1	2.6	45	300	30e-1/2e4						DIRECT [25]	
EDA-PSO	1.4	2.2	12	170	860	860	860	860	870	870	EDA-PSO [6]	
full NEWUOA	4.3	3.7	4.2	160	20e-1 /7e3						full NEWUOA [31]	
G3-PCX	2	3	84	2100	30e-1/5e4			•			G3-PCX [26]	
simple GA	1.1	1.6	19	18	25	34	43	53	110	200	simple GA [22]	
GLOBAL	1.2	2.4	3.3	50e-1/500							GLOBAL [23]	
iAMaLGaM IDEA	1.2	1.4	1.4	33	180	180	180	190	190	190	iAMaLGaM IDEA [4]	
LSfminbnd	11	2.7	1	52	21e-1/4e3						LSfminbnd [28]	
LSstep	81	62	2.2	1	1	1	1	1	1	1	LSstep [28]	
MA-LS-Chain	1	1.3	1	6.4	32	32	32	32	32	32	MA-LS-Chain [21]	
MCS (Neum)	1	1	1.2	24	220	210	210	210	210	210	MCS (Neum) [18]	
NELDER (Han)	1	1.3	5.4	280	1500	1500	1500	1500	1500	1400	NELDER (Han) [16]	
NELDER (Doe)	2.1	1	1.5	33	270	270	270	270	270	270	NELDER (Doe) [5]	
NEWUOA	3	1.5	6.1	230	40e-1/5e3						NEWUOA [31]	
(1+1)-ES	1.8	2.3	16	310	3900	3800	3800	3800	3800	3800	(1+1)-ES [1]	
POEMS	170	70	3.8	9.7	35	39	42	45	47	54	POEMS [20]	
PSO	1.4	1.7	52	55	280	270	280	280	280	280	PSO [7]	
PSO_Bounds	1.5	1.6	7.6	26	38	63	64	65	70	95	PSO_Bounds [8]	
Monte Carlo	1	2.1	6800	83e-1/1e6							Monte Carlo [3]	
Rosenbrock	5.7	39	24	390	70e-1/9e3						Rosenbrock [27]	
IPOP-SEP-CMA-ES	2.2	2.3	1.2	12	96	96	96	97	97	97	IPOP-SEP-CMA-ES [29]	
VNS (Garcia)	1.6	2.5	2.5	5.2	11	11	12	16	22	40	VNS (Garcia) [11]	

Table 51: 05-D, running time excess ERT/ERT_{best} on f_3 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

4 Skew Rastrigin-Bueche separable												
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$	
ERT_{best}/D	0.2	3.77	162	327	338	352	363	370	377	381	ERT_{best}/D	
ALPS	1.1	4.4	7.1	28	59	58	58	58	59	63	ALPS [17]	
AMaLGaM IDEA	1.8	3.4	5.8	2e4	20e-1/1e6						AMaLGaM IDEA [4]	
avg NEWUOA	5.4	10	14	50e-1/8e3	•						avg NEWUOA [31]	
BayEDAcG	1.7	6.3	5.8	69e-1/2e3							BayEDAcG [10]	
BFGS	3	67	170	24e + 0/4e3							BFGS [30]	
Cauchy EDA	7.6	39	85	78e-1/5e4							Cauchy EDA [24]	
BIPOP-CMA-ES	1.1	2.9	2.7	20e-1/4e5							BIPOP-CMA-ES [15]	
(1+1)-CMA-ES	1	1.6	15	460	30e-1/1e4						(1+1)-CMA-ES [2]	
DASA	15	13	1	1.8	5.9	5.7	5.6	5.6	5.7	5.9	DASA [19]	
DEPSO	1.8	5.2	3.3	30e-1/2e3							DEPSO [12]	
DIRECT	1	2.5	190	110	250	11e + 0/2e4					DIRECT [25]	
EDA-PSO	1.1	3.5	14	2e3	20e-1/1e5						EDA-PSO [6]	
full NEWUOA	3.9	2.8	12	30e-1/1e4							full NEWUOA [31]	
G3-PCX	1.5	4.6	76	2200	50e-1/5e4						G3-PCX [26]	
simple GA	1.9	5	18	20	26	33	41	49	58	190	simple GA [22]	
GLOBAL	1.3	4.9	8.3	11e + 0/600							GLOBAL [23]	
iAMaLGaM IDEA	1.7	2.3	3.9	2.1e4	20e-1/1e6						iAMaLGaM IDEA [4]	
LSfminbnd	21	3	7.8	42e-1/5e3							LSfminbnd [28]	
LSstep	320	58	2	1	1	1	1	1	1	1	LSstep [28]	
MA-LS-Chain	1.5	3.8	1.7	35	180	170	160	160	160	160	MA-LS-Chain [21]	
MCS (Neum)	1	2.3	4.1	20e-1/1e4							MCS (Neum) [18]	
NELDER (Han)	3.1	1.4	26	30e-1/1e5							NELDER (Han) [16]	
NELDER (Doe)	1.9	1	7.1	900	870	840	810	790	780	770	NELDER (Doe) [5]	
NEWUOA	4.1	27	27	300	60e-1 /7e3						NEWUOA [31]	
(1+1)-ES	3.3	2	25	3700	2e4	1.9e4	1.9e4	1.8e4	1.8e4	1.8e4	(1+1)-ES [1]	
POEMS	210	67	4.5	17	45	47	47	49	52	57	POEMS [20]	
PSO	1.7	2.7	3	140	4200	4e3	3900	3800	3700	3700	PSO [7]	
PSO_Bounds	1.6	3.2	8	30	64	110	110	110	110	140	PSO_Bounds [8]	
Monte Carlo	1.3	3.4	1.6e4	12e + 0/1e6							Monte Carlo [3]	
Rosenbrock	5.1	33	57	99e-1/1e4							Rosenbrock [27]	
IPOP-SEP-CMA-ES	1.5	2.1	1	37e-1/1e4							IPOP-SEP-CMA-ES [29]	
VNS (Garcia)	2	5.6	2.5	16	39	38	39	50	54	130	VNS (Garcia) [11]	

Table 52: 05-D, running time excess ERT/ERT_{best} on f_4 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

5 Linear slope													
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$		
ERT_{best}/D	0.2	0.293	2	2	2	2	2	2	2	2	ERT_{best}/D		
ALPS	1	1.5	64	130	160	160	160	160	160	160	ALPS [17]		
AMaLGaM IDEA	1	2	19	28	29	29	29	29	29	29	AMaLGaM IDEA [4]		
avg NEWUOA	1	4.1	1.8	1.9	1.9	1.9	1.9	1.9	1.9	1.9	avg NEWUOA [31]		
BayEDAcG	1	1.7	38	76	320	320	320	320	320	320	BayEDAcG [10]		
BFGS	1	5.9	1.9	3	3.1	3.1	3.1	3.1	3.1	3.1	BFGS [30]		
Cauchy EDA	1	29	39	41	41	41	41	41	41	41	Cauchy EDA [24]		
BIPOP-CMA-ES	1	2.5	4.5	6.5	6.6	6.6	6.6	6.6	6.6	6.6	BIPOP-CMA-ES [15]		
(1+1)-CMA-ES	1	2	2.3	3.1	3.2	3.2	3.2	3.2	3.2	3.2	(1+1)-CMA-ES [2]		
DASA	1	45	28	36	40	43	49	52	55	63	DASA [19]		
DEPSO	1	2	22	37	41	41	41	41	41	41	DEPSO [12]		
DIRECT	1	4.5	9.2	12	13	13	13	13	13	13	DIRECT [25]		
EDA-PSO	1	1	10	16	16	16	16	17	17	17	EDA-PSO [6]		
full NEWUOA	1	1.5	2.2	2.4	2.4	2.4	2.4	2.4	2.4	2.4	full NEWUOA [31]		
G3-PCX	1	1.8	14	25	27	28	28	28	28	28	G3-PCX [26]		
simple GA	1	1.9	480	2100	4e3	6300	9200	1.2e4	1.7e4	3.4e4	simple GA [22]		
GLOBAL	1	2.3	32	33	34	34	34	34	34	34	GLOBAL [23]		
iAMaLGaM IDEA	1	1.4	7.1	11	12	12	12	12	12	12	iAMaLGaM IDEA [4]		
LSfminbnd	1	18	13	14	14	14	14	14	14	14	LSfminbnd [28]		
LSstep	1	180	140	160	160	160	160	160	160	160	LSstep [28]		
MA-LS-Chain	1	1.5	53	69	70	71	71	71	71	71	MA-LS-Chain [21]		
MCS (Neum)	1	3	1	1	1	1	1	1	1	1	MCS (Neum) [18]		
NELDER (Han)	1	3.9	2.5	4.1	4.2	4.2	4.2	4.2	4.2	4.2	NELDER (Han) [16]		
NELDER (Doe)	1	3.1	1.9	2.4	2.5	2.5	2.5	2.5	2.5	2.5	NELDER (Doe) $[5]$		
NEWUOA	1	2.9	1.3	1.5	1.5	1.5	1.5	1.5	1.5	1.5	NEWUOA [31]		
(1+1)-ES	1	3	2	2.4	2.5	2.6	2.6	2.6	2.6	2.6	(1+1)-ES [1]		
POEMS	1	350	150	200	210	220	220	220	220	220	POEMS [20]		
PSO	1	1.7	10	14	16	16	16	16	16	16	PSO [7]		
PSO_Bounds	1	1.6	9.2	15	16	16	16	16	16	16	PSO_Bounds [8]		
Monte Carlo	1	1.6	4300	37e-1/1e6		•	·			·	Monte Carlo [3]		
Rosenbrock	1	11	4	4.2	4.2	4.2	4.2	4.2	4.2	4.2	Rosenbrock [27]		
IPOP-SEP-CMA-ES	1	5.7	4.8	6.6	6.8	6.9	6.9	6.9	6.9	6.9	IPOP-SEP-CMA-ES [29]		
VNS (Garcia)	1	2.2	13	15	15	15	15	15	15	15	VNS (Garcia) [11]		

Table 53: 05-D, running time excess ERT/ERT_{best} on .	f_5 , in italics is given	the median final fun	nction value and the media	n number of
function evaluations to reach this value divided by dimen	ension			

6 Attractive sector												
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$	
ERT_{best}/D	2.28	3.2	22.8	42.7	56.2	80.7	116	149	208	266	ERT_{best}/D	
ALPS	31	32	20	28	40	41	39	39	34	37	ALPS [17]	
AMaLGaM IDEA	6.6	5.7	3.2	4.3	5.7	5.7	5.2	5	4.3	4.5	AMaLGaM IDÉA [4]	
avg NEWUOA	1.2	2.6	1.3	1.6	2.6	2.6	2.6	2.6	2.4	2.5	avg NEWUOA [31]	
BayEDAcG	8.8	10	250	13e + 0/2e3							BayEDAcG [10]	
BFGS	2.9	4.9	3	3.3	3.4	3	2.5	2.3	2	7.8	BFGS [30]	
Cauchy EDA	49	230	92	69	68	58	47	43	35	34	Cauchy EDA [24]	
BIPOP-CMA-ES	2.5	5.2	2.3	2.1	2.2	1.9	1.7	1.6	1.3	1.3	BIPOP-CMA-ES [15]	
(1+1)-CMA-ES	1.6	3.3	1.4	1.4	1.6	1.7	1.6	1.5	1.6	1.8	(1+1)-CMA-ES [2]	
DASA	21	21	7.8	9	50	99	110	100	81	150	DASA [19]	
DEPSO	6.3	8.3	5.5	6.4	8	8	7.1	7	6.3	9.7	DEPSO [12]	
DIRECT	2.5	2.2	2.3	28	790	1200	22e-2/2e4				DIRECT [25]	
EDA-PSO	5	4.9	11	51	81	85	79	75	65	68	EDA-PSO [6]	
full NEWUOA	1.5	3.6	1.2	1	1	1	1	1	1	1.4	full NEWUOA [31]	
G3-PCX	7.2	7.1	2.4	3	4.8	5.1	4.7	5.6	5.1	5.5	G3-PCX [26]	
simple GA	60	81	66	150	380	3700	1.2e4	9700	24e-3/1e5		simple GA [22]	
GLOBAL	12	10	2.9	2.1	2	2.9	2.2	2.7	3.6	35	GLOBAL [23]	
iAMaLGaM IDEA	3	3.6	2.1	2.3	3.1	3.1	2.7	2.6	2.2	2.3	iAMaLGaM IDEA [4]	
LSfminbnd	9.1	14	96	110	130	150	110	110	82	65	LSfminbnd [28]	
LSstep	160	200	410	290	300	420	600	490	21e-2/1e4		LSstep [28]	
MA-LS-Chain	12	11	4.8	6.8	7.9	7.4	5.8	5.1	4.1	3.7	MA-LS-Chain [21]	
MCS (Neum)	1	1	2.7	47	41	61	71	63	46	54	MCS (Neum) [18]	
NELDER (Han)	1.7	2.4	1	1.9	2.8	2.6	2.3	2.3	2	2.6	NELDER (Han) [16]	
NELDER (Doe)	2.3	11	5.1	5.6	5.6	4.9	5.3	6.6	5.6	8.5	NELDER (Doe) [5]	
NEWUOA	1.4	2.8	1.7	2.4	3.6	3.6	3.3	3.2	2.7	2.9	NEWUOA [31]	
(1+1)-ES	1.7	3.4	1.6	1.5	1.7	1.5	1.3	1.2	1	1	(1+1)-ES [1]	
POEMS	95	80	27	46	52	50	46	42	37	37	POEMS [20]	
PSO	5.2	5.3	4.7	9	11	12	11	12	10	11	PSO [7]	
PSO_Bounds	4.4	4.4	14	49	85	100	98	92	78	92	PSO_Bounds [8]	
Monte Carlo	290	480	300	5.7e4	14e-1/1e6						Monte Carlo [3]	
Rosenbrock	3	2.6	2.2	2.8	2.4	2.2	4.3	3.8	2.8	2.4	Rosenbrock [27]	
IPOP-SEP-CMA-ES	2.4	7	2.8	2.5	2.7	2.4	2.2	2	1.6	1.5	IPOP-SEP-CMA-ES [29]	
VNS (Garcia)	7.7	12	3.7	2.7	2.9	2.5	2	1.8	1.5	1.4	VNS (Garcia) [11]	

Table 54: 05-D, running time excess ERT/ERT_{best} on f_6 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

7 Step-ellipsoid												
Δ ftarget	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$	
ERT _{best} /D	0.2	1.24	4.72	64.7	234	290	314	314	314	319	ERT _{best} /D	
ALPS	1.1	2.3	33	10	5.7	7.7	9	9	9	9.7	ALPS [17]	
AMaLGaM IDEA	1.3	2.8	5.6	1	1.2	1.8	2.3	2.3	2.3	2.4	AMaLGaM IDEA [4]	
avg NEWUOA	1.1	2.5	4.4	5.9	13	130	17e-3/8e3				avg NEWUOA [31]	
BayEDAcG	1.5	2.4	20	31	120	99	73e-2/2e3				BayEDAcG [10]	
BFGS	3	14	32e + 0/100								BFGS [30]	
Cauchy EDA	10	31	33	4.9	2.4	2.9	2.9	2.9	2.9	3.4	Cauchy EDA [24]	
BIPOP-CMA-ES	1.7	2.2	5	1.5	1	1	1	1	1	1	BIPOP-CMA-ES [15]	
(1+1)-CMA-ES	1	1.6	3.5	5.3	2	2.1	3.1	3.1	3.1	3.1	(1+1)-CMA-ES [2]	
DASA	24	43	230	280	1100	2e4	16e-3/8e5				DASA [19]	
DEPSO	1.2	6.5	14	3	5	7.2	8.3	8.3	8.3	8.5	DEPSO [12]	
DIRECT	1	1	2.8	1.7	120	41e-3/2e4					DIRECT [25]	
EDA-PSO	1.3	1.7	22	24	13	17	18	18	18	19	EDA-PSO [6]	
full NEWUOA	1.7	3.3	1	1.2	4	14	24	24	24	23	full NEWUOA [31]	
G3-PCX	1.3	2.5	19	18	45	150	410	410	410	410	G3-PCX [26]	
simple GA	1.4	3.5	50	35	57	240	520	520	520	520	simple GA [22]	
GLOBAL	1.6	2.9	12	5.7	10	82e-2/400					GLOBAL [23]	
iAMaLGaM IDEA	1.2	2.3	3.8	1.9	3	2.9	3.7	3.7	3.7	3.7	iAMaLGaM IDEA [4]	
LSfminbnd	3.8	17	49	64	100	510	40e-2/1e4				LSfminbnd [28]	
LSstep	28	190	370	700	640	19e-1/1e4					LSstep [28]	
MA-LS-Chain	1.1	3.5	8.4	3.2	13	13	24	24	24	24	MA-LS-Chain [21]	
MCS (Neum)	1	1.3	2.8	5.9	13	140	25e-3/1e4				MCS (Neum) [18]	
NELDER (Han)	1.1	1.6	27	33	56	120	310	310	310	300	NELDER (Han) [16]	
NELDER (Doe)	1.4	1.3	1.4	7.5	15	39	71	71	71	71	NELDER (Doe) [5]	
NEWUOA	1.5	2.2	9.9	13	60	32e-2/6e3					NEWUOA [31]	
(1+1)-ES	1.9	2.6	5.6	6.8	100	370	810	810	810	790	(1+1)-ES [1]	
POEMS	400	180	74	15	9.2	11	21	21	21	22	POEMS [20]	
PSO	1.1	4	11	9.5	590	480	540	540	540	530	PSO [7]	
PSO_Bounds	1.3	2.3	9.4	13	170	140	130	130	130	130	PSO_Bounds [8]	
Monte Carlo	1.3	2.9	39	1200	38e-2/1e6						Monte Carlo [3]	
Rosenbrock	11	220	1200	670	13e+0/3e3						Rosenbrock [27]	
IPOP-SEP-CMA-ES	1.1	2.5	6	1.8	1.2	1.2	1.2	1.2	1.2	1.2	IPOP-SEP-CMA-ES [29]	
VNS (Garcia)	1	3.5	11	1.6	6.8	6.6	7.8	7.8	7.8	7.8	VNS (Garcia) [11]	

Table 55: 05-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on .	f_7 , in italics	is given the	e median final	function	value and	the median	number o	\mathbf{f}
function evaluations to reach this value divided by dimen	nsion							

8 Rosenbrock original											
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget
ERT_{hest}/D	3.56	8.77	14.7	54.6	67.3	74.5	78.2	80.2	82	84.4	ERT_{hest}/D
ALPS	11	32	51	49	100	150	180	210	250	340	ALPS [17]
AMaLGaM IDEA	3.1	4.3	5.2	6.1	7.7	8.1	8.5	8.9	9.1	9.7	AMaLGaM IDEA [4]
avg NEWUOA	1.3	1.6	1.2	1.2	1.1	1.1	1.1	1.1	1.1	1.1	avg NEWUOA [31]
BayEDAcG	5.5	11	140	45e-1/2e3							BayEDAcG [10]
BFGS	2.1	2.4	2.1	1.8	1.6	1.5	1.5	1.5	1.5	1.5	BFGS [30]
Cauchy EDA	24	32	49	31	33	33	34	36	37	40	Cauchy EDA [24]
BIPOP-CMA-ES	2.7	3.6	3.2	3.7	4.5	4.7	4.8	5	5.1	5.4	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	2.1	2.1	2.1	5.1	5	4.9	4.9	4.9	4.9	5	(1+1)-CMA-ES [2]
DASA	16	21	19	160	390	700	1e3	1500	2e3	3300	DASA [19]
DEPSO	4.7	7.2	12	18	23e-2/2e3						DEPSO [12]
DIRECT	2.5	2.8	4.1	5.7	22	56	100	150	190	290	DIRECT [25]
EDA-PSO	3.7	10	72	100	200	300	400	520	620	840	EDA-PSO [6]
full NEWUOA	2.3	2.2	1.6	1	1	1	1	1	1	1	full NEWUOA [31]
G3-PCX	5.5	5.3	4.6	20	18	17	17	16	16	16	G3-PCX [26]
simple GA	8.4	110	190	840	78e-2/1e5						simple GA [22]
GLOBAL	11	7.4	5	2.1	2.1	2.1	2.1	2.1	2.1	2.2	GLOBAL [23]
iAMaLGaM IDEA	2.3	2.8	3.4	7.5	7.6	7.7	7.7	8	8.1	8.4	iAMaLGaM IDEA [4]
LSfminbnd	5.5	9.1	10	290	450	1900	34e-1/1e4				LSfminbnd [28]
LSstep	78	64	64	95	330	910	1800	1800	53e-2/1e4		LSstep [28]
MA-LS-Chain	5.8	7.3	8.7	7.2	9.6	10	11	11	11	12	MA-LS-Chain [21]
MCS (Neum)	1	1.4	1.5	1	1	1	1.1	1.1	1.1	1.1	MCS (Neum) [18]
NELDER (Han)	1.3	1.6	1.6	3.7	3.3	3.2	3.1	3.1	3.1	3.2	NELDER (Han) [16]
NELDER (Doe)	1.1	2.3	2.1	2.4	2.4	2.3	2.3	2.3	2.4	2.4	NELDER (Doe) [5]
NEWUOA	1	1	1	1.1	1.2	1.2	1.2	1.2	1.2	1.2	NEWUOA [31]
(1+1)-ES	2.7	22	15	240	230	240	260	290	320	380	(1+1)-ES [1]
POEMS	67	40	69	180	200	390	750	2100	5500	1.8e4	POEMS [20]
PSO	3.8	7.1	13	150	200	310	470	620	780	1100	PSO [7]
PSO_Bounds	5.1	12	30	470	920	1200	1400	3e3	12e-5/1e5		PSO_Bounds [8]
Monte Carlo	10	220	2e4	64e-1/1e6							Monte Carlo [3]
Rosenbrock	2.3	53	32	23	22	23	25	27	30	36	Rosenbrock [27]
IPOP-SEP-CMA-ES	1.7	2.8	3.5	5.8	6.8	6.7	6.8	6.8	6.9	7.1	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	8.9	5.9	5.1	6.6	7.7	21	46	48	47	46	VNS (Garcia) [11]

Table 56: 05-D, running time excess ERT/ERT _{best}	on f_8 , in	n italics i	s given	the median	final	function	value and	the	median	number	of
function evaluations to reach this value divided by di	mension	1									

9 Rosenbrock rotated											
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{hest}/D	0.2	0.2	6.92	25.4	42.8	52.7	60.1	64.8	67.1	73.8	ERT_{best}/D
ALPS	140	1100	91	92	130	200	260	310	370	560	ALPS [17]
AMaLGaM IDEA	53	140	9.1	23	18	17	16	16	16	15	AMaLGaM IDEA [4]
avg NEWUOA	20	56	2.4	3.1	2.1	1.8	1.7	1.6	1.6	1.5	avg NEWUOA [31]
BayEDAcG	81	350	38	39e-1/2e3							BayEDAcG [10]
BFGS	31	84	3.6	3	2	1.8	1.6	1.5	1.5	1.4	BFGS [30]
Cauchy EDA	400	910	71	54	45	42	41	41	42	43	Cauchy EDA [24]
BIPOP-CMA-ES	28	98	5.8	8.7	7.2	6.7	6.4	6.2	6.3	6.2	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	30	86	4.2	7.7	5.9	5.3	5	4.9	4.9	4.7	(1+1)-CMA-ES [2]
DASA	330	7500	230	6700	4800	4600	4800	5300	6600	8900	DASA [19]
DEPSO	100	370	22	150	10e-1/2e3						DEPSO [12]
DIRECT	1	1	3.2	4.2	48	56	130	140	150	310	DIRECT [25]
EDA-PSO	70	410	250	210	270	470	700	1100	1300	2800	EDA-PSO [6]
full NEWUOA	33	72	2.6	2.7	1.9	1.7	1.5	1.5	1.4	1.3	full NEWUOA [31]
G3-PCX	94	380	14	18	14	12	11	11	10	9.8	G3-PCX [26]
simple GA	100	3800	420	5.6e4	17e-1/1e5						simple GA [22]
GLOBAL	210	340	11	4.6	3.2	3	2.8	2.7	2.7	2.7	GLOBAL [23]
iAMaLGaM IDEA	42	120	7	22	15	14	13	12	12	12	iAMaLGaM IDEA [4]
LSfminbnd	60	330	13	130	180	440	25e-3/1e4				LSfminbnd [28]
LSstep	2e3	1.3e4	520	5600	19e-1/1e4						LSstep [28]
MA-LS-Chain	84	260	18	20	17	17	17	16	16	16	MA-LS-Chain [21]
MCS (Neum)	1	1	1	1	1	1	1	1	1	1	MCS (Neum) [18]
NELDER (Han)	13	62	3.1	13	8.2	6.9	6.2	5.9	5.8	5.4	NELDER (Han) [16]
NELDER (Doe)	21	56	2.4	3.1	2.5	2.3	2.1	2.1	2.1	2	NELDER (Doe) [5]
NEWUOA	16	28	1.8	3.6	2.5	2.1	1.9	1.9	1.9	1.7	NEWUOA [31]
(1+1)-ES	29	64	2.9	100	80	99	130	160	200	270	(1+1)-ES [1]
POEMS	1200	1700	140	130	290	590	1100	1900	1.1e4	39e-6/1e5	POEMS [20]
PSO	66	290	25	940	680	790	1100	1400	2400	2800	PSO [7]
PSO_Bounds	69	360	220	1500	1600	1800	4e3	1.1e4	2.2e4	2e4	PSO_Bounds [8]
Monte Carlo	180	1.3e4	4.1e4	58e-1/1e6							Monte Carlo [3]
Rosenbrock	32	150	5.3	9.8	10	14	14	14	14	14	Rosenbrock [27]
IPOP-SEP-CMA-ES	43	230	9.8	11	9.9	8.8	8.3	8	8	7.7	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	60	250	11	18	14	12	11	11	11	10	VNS (Garcia) [11]

Table 57: 05-D, running time excess ERT/ERT_{best} on f_9 , in italics is given the median final function value and the median number of
function evaluations to reach this value divided by dimension

Table 58: 05-D, ru	nning ti	me excess E	RT/ERT _{bes}	t on f_{10} , in	italics is give	en the medi	an final fur	nction v	alue and th	ne median n	umber of
function evaluation	ns to rea	ch this value	e divided by	dimension							pa
			v		10 Ellip	soid					ris
$\Delta ftarget$	1e+03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget \tilde{S}
ERT_{hest}/D	20.6	34.1	69.9	100	115	121	125	129	166	176	ERT_{hest}/D^{2}
ALPS	29	54	88	320	890	2e3	5300	2e4	21e-5/1e6		ALPS [17]
AMaLGaM IDEA	2.7	2.6	1.9	1.9	2	2.3	2.5	2.7	2.3	2.6	AMaLGaM IDEA [4]
avg NEWUOA	1.2	2.2	3.1	4.6	6.6	8.1	10	12	11	14	avg NEWUOA [31]
BayEDAcG	400	840	28e + 2/2e3						•		BayEDAcG [10]
BFGS	1.7	1.5	1	1	1	1	1	1	1.1	23	BFGS [30]
Cauchy EDA	16	16	11	9	9.4	11	12	13	11	13	Cauchy EDA [24]
BIPOP-CMA-ES	5.1	5.1	3.5	2.9	2.7	2.7	2.8	2.8	2.3	2.4	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	3.2	3.8	2.5	2.2	2	2.1	2.1	2.1	1.7	1.7	(1+1)-CMA-ES [2]
DASA	99	1100	6900	1.8e4	3.9e4	5.9e4	1.2e5	1.1e5	9e4	47e-1/1e6	DASA [19]
DEPSO	18	78	210	88e+0/2e3							DEPSO [12]
DIRECT	8.8	57	110	140	280	15e-2/2e4					DIRECT [25]
EDA-PSO	71	130	890	1400	3900	1.2e4	21e-1/1e5				EDA-PSO [6]
full NEWUOA	1	2	3.6	6.2	8.7	10	13	15	13	17	full NEWUOA [31]
G3-PCX	3.3	7.2	22	27	36	41	49	57	51	64	G3-PCX [26]
simple GA	130	500	2400	15e + 0/1e5							simple GA [22]
GLOBAL	3.8	3	1.9	1.6	1.8	1.9	2	2.2	1.7	1.7	GLOBAL [23]
iAMaLGaM IDEA	2.2	2.2	1.8	1.6	1.7	1.9	2	2.2	1.8	2	iAMaLGaM IDEA [4]
LSfminbnd	160	780	25e+1/1e4								LSfminbnd [28]
LSstep	1200	25e+2/1e4		•					•	•	LSstep [28]
MA-LS-Chain	7.1	9.9	9	9.3	8.6	8.6	8.8	8.7	6.9	6.9	MA-LS-Chain [21]
MCS (Neum)	53	110	280	17e+0/1e4					•	•	MCS (Neum) [18]
NELDER (Han)	1.1	1.2	1.4	1.3	1.4	1.4	1.5	1.5	1.2	1.2	NELDER (Han) [16]
NELDER (Doe)	1	1	1.2	1.3	1.2	1.2	1.2	1.2	1	1	NELDER (Doe) [5]
NEWUOA	1.5	2.6	3.1	5.5	8.1	11	14	17	16	21	NEWUOA [31]
(1+1)-ES	34	130	700	2500	4500	5900	1.4e4	5.8e4	67e-5/1e6		(1+1)-ES [1]
POEMS	41	170	790	2500	45e-1/1e5						POEMS [20]
PSO	15	120	1700	3300	10e + 0/1e5			•			PSO [7]
PSO_Bounds	290	1200	3800	1.5e4	20e+0/1e5						PSO_Bounds [8]
Monte Carlo	990	4.7e4	10e + 1/1e6								Monte Carlo [3]
Rosenbrock	11	25	24	44	40	38	37	36	29	37	Rosenbrock [27]
IPOP-SEP-CMA-ES	10	12	7.4	5.6	5.1	5	5	5	4	3.9	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	6.6	6.2	4.5	3.5	3.4	3.4	3.5	3.5	2.8	2.8	VNS (Garcia) [11]

				v	$11 \mathrm{Dis}$	scus					
Δ ftarget	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget
ERT_{best}/D	2.48	4.88	28.5	40.4	153	195	235	270	293	335	ERT_{best}/D
ALPS	15	23	54	340	300	540	810	1100	1800	2.2e4	ALPS [17]
AMaLGaM IDEA	4.5	5.4	2.1	2.7	1	1	1	1	1	1.1	AMaLGaM IDEA [4]
avg NEWUOA	2.6	11	5.4	7.2	2.7	2.6	2.8	2.9	3.1	3.4	avg NEWUOA [31]
BayEDAcG	9.1	15	160	15e+0/2e3							BayEDAcG [10]
BFGS	2.1	1.8	1	1	1.1	1.9	8.2	21	200	32e-6/8e3	BFGS [30]
Cauchy EDA	25	51	18	17	6	5.5	5.3	5.4	5.6	5.9	Cauchy EDA [24]
BIPOP-CMA-ES	6.4	15	8.4	7.2	2.2	1.8	1.6	1.5	1.4	1.3	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	4	7	6.5	6.6	2.1	1.8	1.5	1.4	1.3	1.2	(1+1)-CMA-ES [2]
DASA	11	12	1900	5200	2300	2800	3200	4200	9700	4.5e4	DASA [19]
DEPSO	11	22	140	10e + 0/2e3	• .					•	DEPSO [12]
DIRECT	5.8	15	87	2200	19e-1/2e4				•	•	DIRECT [25]
EDA-PSO	8.9	30	110	650	970	2400	6200	5500	70e-3/1e5	•	EDA-PSO [6]
full NEWUOA	2.7	20	11	14	5.4	4.9	5.3	5.5	5.9	6.5	full NEWUOA [31]
G3-PCX	7.6	7.9	55	110	45	44	49	52	56	61	G3-PCX [26]
simple GA	15	34	340	7100	9400	21e-1/1e5	•	•		•	simple GA [22]
GLOBAL	13	10	4	5.5	3.5	5.1	5	4.8	5	8.5	GLOBAL [23]
AMaLGaM IDEA	6.1	6.6	3.4	3.8	1.2	1.1	1	1	1	1	iAMaLGaM IDEA [4]
LStminbnd	2.7	320	61e+0/1e4		•		•	•			LSfminbnd [28]
LSstep	3.6	750	4900	73e+0/1e4				· .			LSstep [28]
MA-LS-Chain	7.9	8.7	15	19	6.7	5.6	4.9	4.4	4.2	3.8	MA-LS-Chain [21]
MCS (Neum)	1	1	82	460	13e-1/1e4						MCS (Neum) [18]
NELDER (Han)	2.9	2.7	3.2	5	1.7	1.6	1.5	1.5	1.5	1.6	NELDER (Han) [16]
NELDER (Doe)	4.4	3.4	4.5	4.7	1.5	1.4	1.2	1.4	1.1	1.2	NELDER (Doe) [5]
NEWUOA (1+1) EC	1.7	5.9	3.5	4.7	1.8	1.7	1.8	1.8	2	2.2	$\begin{array}{c} \text{NEWUOA} [31] \\ (1+1) EG [1] \end{array}$
(1+1)-ES	2.8	6700	0400	9300	3700	3800	620	2.8e4	90e-5/1eb		(1+1)-E5 [1] DOEMS [20]
POEMS	00	12	230	310	270	330	160	100	940	2200	POEMS [20]
PSO Pounda	0.4	10	420	∠40 1400	120	140	1100	1600	240 1500	390	PSO Rounda [8]
Monto Corlo	7.4	21	430	1400	110 1 /1-6	169	1100	1000	1000	1400	Monto Carlo [2]
Bosonbrock	(.4 99	3U 19	120	1.160	26	91	18	16	14	13	Rosenbrock [27]
POP SED CMA ES	18	12	120	00	4.2	21	20	26	14 95	10 9 9	IDOD SED CMA ES [20]
VNE (Canaia)	10	34	10	14	4.4	0.4	2.9	2.0	4.0	4.4	11 OI -5EI -OMA-E5 [29]

				a og all	10 E	Pont airon					
A. C.	1 00	1 . 00	1 . 01	1 . 00		sem cigar	1 00	1 04	1 05	1 07	A 51
Δftarget	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δitarget
ERT _{best} /D	13.3	15.9	21.6	53.6	74.1	82.6	92.3	233	261	299	ERT _{best} /D
ALPS	100	120	130	170	540	1400	4200	1.4e4	2.7e4	24e-5/1e6	ALPS [17]
AMALGAM IDEA	8.8	9.2	10	6.7	8.6	9.8	11	4.9	5.1	5.2	AMaLGaM IDEA [4]
avg NEWUOA	1.1	1.8	3.5	2.8	2.8	2.9	3	1.3	1.3	1.4	avg NEWUOA [31]
BayEDAcG	46	46	96	260	390	71e-1/2e3	•	•	•	•	BayEDAcG [10]
BFGS	1.1	1	1.1	1	1	1	1	1.3	2	49	BFGS [30]
Cauchy EDA	66	75	79	41	35	37	38	17	17	17	Cauchy EDA [24]
BIPOP-CMA-ES	5.1	6.3	11	7.4	7.4	7.5	7.7	3.4	3.3	3.3	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	2.8	3.4	4	2.9	3.5	3.9	4.1	1.9	1.9	1.9	(1+1)-CMA-ES [2]
DASA	17	17	1.2e4	5.4e4	5.9e4	1.8e5	32e-1/1e6	•	•	•	DASA [19]
DEPSO	23	33	55	47	120	95e-2/2e3					DEPSO [12]
DIRECT	6.6	8	8.5	8.7	19	39	110	96	380	21e-6/2e4	DIRECT [25]
EDA-PSO	310	390	1100	3e3	8900	21e-1/1e5	•	•	•		EDA-PSO [6]
full NEWUOA	1	1.5	3.7	2.6	2.7	3	3.3	1.6	1.6	1.7	full NEWUOA [31]
G3-PCX	4	4.2	14	11	13	13	12	5.3	5.2	5.1	G3-PCX [26]
simple GA	520	620	930	2400	1.9e4	11e-1/1e5	·	·		•	simple GA [22]
GLOBAL	5.6	5	4.6	2.7	2.4	3	5	3	3.1	3.4	GLOBAL [23]
AMaLGaM IDEA	5.5	6.1	6.9	4.3	4	4.3	4.7	2.1	2.1	2.3	iAMaLGaM IDEA [4]
LSfminbnd	3.4	3.6	310	1200	1900	68e-1/1e4	•		•		LSfminbnd [28]
LSstep	23	26	460	1200	57e-1/1e4	·	•				LSstep [28]
MA-LS-Chain	11	11	11	13	16	15	16	6.9	6.7	6.5	MA-LS-Chain [21]
MCS (Neum)	1.2	1.1	1	18	17	15	22	22	26	56	MCS (Neum) [18]
NELDER (Han)	1.4	1.7	2.3	2.2	2.2	2.2	2.3	1	1	1	NELDER (Han) [16]
NELDER (Doe)	1.6	2.4	4.4	2.9	2.7	2.7	2.7	1.2	1.1	1.2	NELDER (Doe) [5]
NEWUOA	1.1	1.5	3.5	2.6	2.5	2.5	2.6	1.1	1.1	1.1	NEWUOA [31]
(1+1)-ES	2.6	1200	2.1e4	6.1e4	1.9e5	23e-1/1e6			•		(1+1)-ES [1]
POEMS	180	210	1900	2900	8900	17e-1/1e5		•	•	•	POEMS [20]
PSO	28	35	750	3800	5400	7900	1.5e4	<i>41e-1/1e5</i>	•	•	PSO [7]
PSO_Bounds	120	180	1900	2500	5500	1.7e4	46e-1/1e5				PSO_Bounds [8]
Monte Carlo	19e + 3/1e6	•		·	•	·	•	•		•	Monte Carlo [3]
Rosenbrock	1.4	1.4	98	63	91	100	95	46	42	48	Rosenbrock [27]
POP-SEP-CMA-ES	4.6	6.2	12	11	9.1	8.7	8.6	3.7	3.5	3.3	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	6.9	9	19	12	10	9.7	9.4	4	3.8	3.6	VNS (Garcia) [11]

RT	
n°	
0383	

Table 61: 05-D, running time excess ERT/ERT_{best} on f_{13} , in italics is given the median final function value and the median number of	
function evaluations to reach this value divided by dimension	
13 Sharp ridge	

											2
Table 61: 05-D, ru	nning ti	me exce	ss ERT/ER.	Г _{best} о	n f_{13} , in ital	ics is given \uparrow	the median	final function	on value an	d the media	an number of Ξ
function evaluation	ns to rea	ch this y	value divideo	l by din	nension						p_{a}
	10 00 100		and an nace	i og an	13	Sharp ride	re				uri
Aftarget	$1e \pm 0.3$	$1e \pm 02$	$1e \pm 01$	$1e \pm 00$	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Aftarget 0
EBT_1 /D	0.56	8.88	26.4	38.9	50	63.9	262	305	350	451	EBT /D S
best/D	27	43	50	83	280	440	570	2300	3900	760-7/106	ALPS [17]
AMaLGaM IDEA	3.3	5.8	4 2	4.6	49	4.9	1.5	1.5	1 4	1 4	AMaLGaM IDEA [4]
avg NEWIIOA	4	1	4.5	8.1	42	67	68	450	300	150-1/909	avg NEWIIOA [31]
BayEDAcG	1 9	38	170	350	19010/203	01	00	400	550	100-4/505	BayEDAcG [10]
DECS	1.5	1.9	1	1	1	1			140	970 6 /10/	DECG [20]
Cauchy EDA	4.0 54	31	21	24	25	25	4.0	24	7.3	7 3	Cauchy FDA [24]
DIDOD CMA ES	2.4	20	21	24 5.4	2.5	20	1.4	1.5	1.5	1.5	DIDOD CMA ES [15]
(1+1) CMA ES	0.4 9.6	0.0 0 1	3.9	6.2	6.1	6.2	1.0	2.0	2.0	2.1	(1+1) CMA ES [1]
DASA	2.0	2.1 51	200	640	2500	7800	1.9	2.9	020 / /106	0.1	(1+1)-CMA-ES [2]
DASA	04	0.7	200	040	2300	1800	01.1/0.0	1.4e4	23e-4/100	•	DASA [19]
DIPECT	2.1	0.1	7	330	260	240	21e-1/2e3	E 7		10-6/0-1	DIFFOURT [25]
DIRECT EDA DEO	1.6	4.7	150	21	34	140	42	97	120	12e-0/2e4	EDA DEO [6]
EDA-PSO	3.4	47	150	390	2e3	164	04e-3/1e5		•	•	EDA-PSO [6]
full NEWUOA	5.5	I	1.8	6.7	23	85	97	19e-4/1e4			full NEW UOA [31]
G3-PCX	3.3	3.9	14	60	150	340	120	260	590	15e-5/5e4	G3-PCX [26]
simple GA	2.6	120	240	730	4400	2.2e4	20e-2/1e5				simple GA [22]
GLOBAL	3.4	7.4	4.2	6.1	11	19e-2/300			•	•	GLOBAL [23]
iAMaLGaM IDEA	1.9	3.1	2.6	3	3.2	3.3	1	1	1	1	iAMaLGaM IDEA [4]
LSfminbnd	14	15	33	150	540	1100	19e-2/1e4				LSfminbnd [28]
LSstep	250	140	550	1100	2900	22e+0/1e4				•	LSstep [28]
MA-LS-Chain	1.8	9.9	8.3	21	24	19	5.1	4.8	5.3	4.9	MA-LS-Chain [21]
MCS (Neum)	1	1.6	41	210	460	2300	550	21e-2/1e4			MCS (Neum) [18]
NELDER (Han)	2.2	1.2	2	3.8	5.3	4.9	1.3	1.3	1.2	1.3	NELDER (Han) [16]
NELDER (Doe)	2.9	1.7	2.4	2.4	5.3	6.1	1.9	2.5	3.9	5	NELDER (Doe) [5]
NEWUOA	2.6	1.8	3.1	9.3	35	55	54	120	330	17e-4 /8e3	NEWUOA [31]
(1+1)-ES	4.3	11	20	30	110	250	160	350	1500	7200	(1+1)-ES [1]
POEMS	310	57	87	660	5600	1e4	22e-2/1e5				POEMS [20]
PSO	3	8.7	1600	1e4	2.8e4	57e-1/1e5					PSO [7]
PSO_Bounds	1.3	20	350	2400	5700	1e4	5400	81e-2/1e5			PSO_Bounds [8]
Monte Carlo	1.9	960	30e + 0/1e6								Monte Carlo [3]
Rosenbrock	8.6	3.1	7.6	13	26	49	39	56	63	290	Rosenbrock [27]
IPOP-SEP-CMA-ES	3.1	2.9	9	11	12	11	2.8	2.7	2.5	2.3	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1.9	6.2	4.8	5.6	6.6	6.2	1.9	1.9	1.9	2.1	VNS (Garcia) [11]

14 Sum of different powers											
Δ ftarget	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{hest}/D	0.2	0.2	1.96	8.17	11.6	18	27.7	42.2	50.3	95.1	ERT_{best}/D
ALPS	1	1.3	2.5	32	66	72	75	130	390	1e4	ALPS [17]
AMaLGaM IDEA	1	1.5	2.1	4.5	6.1	6.6	5.8	5	5.2	3.8	AMaLGaM IDEA [4]
avg NEWUOA	1	1.7	2.1	1	1	1	1.2	1.8	5	1e3	avg NEWUOA [31]
BayEDAcG	1	1.4	3	100	220	250	1e3	12e-2/2e3			BayEDAcG [10]
BFGS	1	3.4	2.2	1.7	1.8	1.5	1.3	1	1	350	BFGS [30]
Cauchy EDA	1	18	23	29	40	40	33	28	28	19	Cauchy EDA [24]
BIPOP-CMA-ES	1	1.3	1.1	2.8	3.7	4	4.6	4.3	5.4	4.5	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	2.2	1.8	1.9	2.3	2.3	2.6	3.3	4	3.2	(1+1)-CMA-ES [2]
DASA	1	18	19	18	20	21	49	460	3500	12e-7/1e6	DASA [19]
DEPSO	1	1.5	2.6	6.9	8.9	11	17	45	47e-6/2e3		DEPSO [12]
DIRECT	1	1	1	3.7	4.8	7.4	23	370	1900	62e-6/2e4	DIRECT [25]
EDA-PSO	1	1.5	1.4	7.1	96	190	210	190	300	22e-7/1e5	EDA-PSO [6]
full NEWUOA	1	2.8	2.7	1.1	1.1	1	1	1.4	3.2	26	full NEWUOA [31]
G3-PCX	1	1.1	1.7	3.5	3.5	3.6	5	9.7	26	390	G3-PCX [26]
simple GA	1	1.8	2.1	91	270	310	350	3300	13e-5/1e5		simple GA [22]
GLOBAL	1.1	1.7	2.2	7.7	5.9	4.4	3.3	2.6	3.6	59e-7/300	GLOBAL [23]
iAMaLGaM IDEA	1	1.3	1.4	2.7	4.3	4.5	4.1	3.5	3.6	2.7	iAMaLGaM IDEA [4]
LSfminbnd	1	3.7	5.9	4.5	4.3	7.4	70	1700	35e-5/1e4		LSfminbnd [28]
LSstep	1	28	120	96	97	180	35e-4 /1e4				LSstep [28]
MA-LS-Chain	1	1.3	2	7.2	11	11	11	13	16	12	MA-LS-Chain [21]
MCS (Neum)	1	1	1.4	2.8	2.7	2.5	2.8	3.4	230	10e-6/1e4	MCS (Neum) [18]
NELDER (Han)	1	1.3	1.1	1.2	1.5	1.5	1.4	1.2	1.3	1	NELDER (Han) [16]
NELDER (Doe)	1	2.3	1.1	1.1	1.4	1.6	1.7	1.6	1.6	1.3	NELDER (Doe) $[5]$
NEWUOA	1	1.8	1.7	1	1	1	1.2	1.9	5.5	2500	NEWUOA [31]
(1+1)-ES	1	3	2.1	1.8	2.1	2.2	5.6	66	1100	12e-7/1e6	(1+1)-ES [1]
POEMS	1	180	110	42	81	130	140	130	630	31e-7/1e5	POEMS [20]
PSO	1	1.4	1.9	5.6	15	21	30	50	220	90e-8/1e5	PSO [7]
PSO_Bounds	1	1.7	1.9	12	45	74	140	200	410	14e-7/1e5	PSO_Bounds [8]
Monte Carlo	1	1.1	1.2	100	7.6e4	93e-3/1e6	•		·	•	Monte Carlo [3]
Rosenbrock	1	7.9	2.4	1.2	1.3	1.5	4.6	23	26	43	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1.5	1.6	3	3.6	3.6	5.3	9	9.5	6.4	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1.2	3.3	5.5	5.4	5.3	5.3	5.4	7	5.5	VNS (Garcia) [11]

Table 62: 05-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{14} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

Table 63: 05-D, running time excess ERT/ERT _{best} on f_{15} , in italics is given the median final function value and the median number	r of
function evaluations to reach this value divided by dimension	

					15 Rastrig	gın					
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{best}/D	0.2	2.6	102	1860	3870	3950	4010	4080	4150	4270	ERT_{best}/D
ALPS	1.1	1.9	9.2	9	26	26	26	25	25	25	ALPS [17]
AMaLGaM IDEA	1.3	2.7	1.7	2.6	5.3	5.2	5.2	5.1	5.1	5	AMaLGaM IDEA [4]
avg NEWUOA	1.3	2	5.8	46	30e-1/6e3						avg NEWUOA [31]
BayEDAcG	1.2	2.7	4.8	61e-1/2e3							BayEDAcG [10]
BFGS	2.2	46	87	13e+0/3e3							BFGS [30]
Cauchy EDA	8.7	36	12	190	24e-1/5e4						Cauchy EDA [24]
BIPOP-CMA-ES	1	2.3	1.6	1.5	1.2	1.2	1.2	1.2	1.2	1.2	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1.4	2	10	80	30e-1/1e4						(1+1)-CMA-ES [2]
DASA	15	26	230	1700	20e-1/1e6						DASA [19]
DEPSO	1	5.7	7.9	41e-1/2e3							DEPSO [12]
DIRECT	1	1.2	5.4	9.4	99e-2/2e4						DIRECT [25]
EDA-PSO	1.1	2	20	7.5	24	23	23	24	24	24	EDA-PSO [6]
full NEWUOA	1.9	2.9	6.3	55	50e-1 /7e3						full NEWUOA [31]
G3-PCX	1.3	2.2	130	370	50e-1/5e4						G3-PCX [26]
simple GA	1.1	1.9	35	91	370	360	360	350	350	15e-1/1e5	simple GA [22]
GLOBAL	1	2	6	90e-1/500						•	GLOBAL [23]
iAMaLGaM IDEA	1.1	1.8	1	7	9.2	9.1	9	8.9	8.8	8.6	iAMaLGaM IDEA [4]
LSfminbnd	1	4	35	60e-1/1e4							LSfminbnd [28]
LSstep	1.1	80	1400	80	24e+0/1e4						LSstep [28]
MA-LS-Chain	1.1	2.3	2.6	5.3	6	5.9	5.8	5.7	5.6	5.5	MA-LS-Chain [21]
MCS (Neum)	1	1	4	25	38	38	37	36	36	20e-1/1e4	MCS (Neum) [18]
NELDER (Han)	1.7	2.5	20	43	83	81	80	79	77	75	NELDER (Han) [16]
NELDER (Doe)	1.3	5	4.5	20	73	72	71	70	69	67	NELDER (Doe) [5]
NEWUOA	1.9	7.8	5.8	41	30e-1/5e3						NEWUOA [31]
(1+1)-ES	1.3	1.7	28	100	250	240	240	230	230	220	(1+1)-ES [1]
POEMS	1	80	15	130	370	370	360	360	350	340	POEMS [20]
PSO	1.1	1.5	16	220	370	360	350	350	340	330	PSO [7]
PSO_Bounds	1.3	2.3	170	120	20e-1/1e5						PSO_Bounds [8]
Monte Carlo	1.2	1.7	6900	83e-1/1e6							Monte Carlo [3]
Rosenbrock	4.4	190	310	16e + 0/1e4							Rosenbrock [27]
IPOP-SEP-CMA-ES	1.5	1.7	1.6	1	1	1	1	1	1	1	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	3.1	2.4	5.9	680	690	680	690	680	670	VNS (Garcia) [11]

RT n° 0383

				v	16 V	Veierstrass	5				
$\Delta ftarget$	1e+03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT _{best} /D	0.2	0.24	24.1	122	532	2030	2090	2280	2330	2420	ERT _{best} /D
ALPS	1	1.7	2.5	8.6	6.3	6.7	13	60	160	830	ALPS [17]
AMaLGaM IDEA	1	1.4	3	15	12	5	4.9	5.6	5.5	5.4	AMaLGaM IDEA [4]
avg NEWUOA	1	1.2	2.6	12	47	35e-2/8e3					avg NEWUOA [31]
BayEDAcG	1	1.2	5.7	35e-1/2e3	•	•			•		BayEDAcG [10]
BFGS	1	4.2	150	960	49e-1/8e3						BFGS [30]
Cauchy EDA	1	3.4	5.6	1200	15e-1/5e4						Cauchy EDA [24]
BIPOP-CMA-ES	1	1.1	3	3.6	2.6	1.1	1.3	1.3	1.4	1.4	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1	2.5	10	17	21	31	62	60	70e-3/1e4	(1+1)-CMA-ES [2]
DASA	1	6.6	4.8	310	980	1200	24e-3/1e6				DASA [19]
DEPSO	1	1.2	11	42e-1/2e3							DEPSO [12]
DIRECT	1	2	1.2	1.6	3.4	2.1	5.9	10	19	40	DIRECT [25]
EDA-PSO	1	1.4	4.6	210	82	38	53	49	61	61	EDA-PSO [6]
full NEWUOA	1	2.3	2.7	12	29	32	12e-2/1e4				full NEWUOA [31]
G3-PCX	1	1.2	1	22	44	32	350	320	60e-4 /5e4		G3-PCX [26]
simple GA	1	1.3	2.1	84	93	71	150	630	620	600	simple GA [22]
GLOBAL	1	1.3	1.4	1	1	1.3	3.5	7	6.8	6.6	GLOBAL [23]
iAMaLGaM IDEA	1	1.4	1.9	8.6	5.5	4.4	5.9	6.5	6.4	6.8	iAMaLGaM IDEA [4]
LSfminbnd	1	1.3	3.2	28	130	71	37e-2/1e4				LSfminbnd [28]
LSstep	1	1.1	14	280	13e-1/1e4						LSstep [28]
MA-LS-Chain	1	1.1	2.7	8.2	18	11	26	51	50	75	MA-LS-Chain [21]
MCS (Neum)	1	1.8	1.9	18	130	30e-2/1e4					MCS (Neum) [18]
NELDER (Han)	1	1.5	4.4	28	23	25	95	200	300	600	NELDER (Han) [16]
NELDER (Doe)	1	1.3	1.6	4.8	9.8	6.3	13	27	59	120	NELDER (Doe) [5]
NEWUOA	1	1.2	2.1	29	50e-2/7e3						NEWUOA [31]
(1+1)-ES	1	1.1	37	88	340	590	2200	6200	73e-4/1e6		(1+1)-ES [1]
POEMS	1	130	12	74	76	58	57	53	52	54	POEMS [20]
PSO	1	1.2	2.4	6.2	59	55	89	310	300	580	PSO [7]
PSO_Bounds	1	1.2	2.4	36	140	140	320	620	16e-3/1e5		PSO_Bounds [8]
Monte Carlo	1	1.1	3.5	510	30e-2/1e6						Monte Carlo [3]
Rosenbrock	1	1.8	40	1200	36e-1/1e4						Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1.1	2.1	5	3.5	1	1	1	1	1	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1.2	2.8	12	12	9.1	12	16	34	45	VNS (Garcia) [11]

Table 64: 05-D, running time excess ERT/ERT _b	$_{\rm st}$ on f	r ₁₆ , ir	n italics is	s given	the median	final	function	value and	${\rm the}$	median	number	of
function evaluations to reach this value divided \tilde{b}	dimer	nsion										

RT	
n°	
0383	

Table 65: 05-D, ru function evaluation	nning ti is to rea	me exce	ess ERT value di	/ERT _{best} c vided by di	on f_{17} , in its mension	alics is given	n the media	n final func	tion value a	and the med	lian number of	Compc
				· · · · · · · · · · · · · · · · · · ·	17 Schaff	er F7. con	dition 10					sri
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$	108
ERT_{best}/D	0.2	0.2	1.04	43	180	572	734	959	1270	1590	ERT_{best}/D	~
ALPS	1	1.1	2.4	12	8	4.8	7.1	10	21	68	ALPS [17]	3
AMaLGaM IDEA	1	1.1	3.9	1.5	2.7	2.6	2.7	3.5	3.4	3.5	AMaLGaM IDEA [4]	2
avg NEWUOA	1	1.2	3.1	42	410	24e-2/1e4					avg NEWUOA [31]	1
BayEDAcG	1	1.3	2.2	6.7	5.4	4.1	7.5	15	47e-4/2e3		BayEDAcG [10]	
BFGS	1	3.4	120	650	19e-1/4e3						BFGS [30]	Ц
Cauchy EDA	1	1	44	13	7	3.8	4.3	4.3	5.3	13	Cauchy EDA [24]	Э
BIPOP-CMA-ES	1	2.3	3.4	1	1	1	1	1	1	1.2	BIPOP-CMA-ES [15]	2
(1+1)-CMA-ES	1	1.1	4.5	27	110	17e-2/1e4					(1+1)-CMA-ES [2]	J
DASA	1	25	170	380	730	1800	1.9e4	82e-4/1e6			DASA [19]	Э
DEPSO	1	1	7.6	3.5	2.8	3.1	4.5	5.6	12	31e-4 /2e3	DEPSO [12]	5
DIRECT	1	1	1	1.4	1.7	2.7	4.4	6.7	9.5	10	DIRECT [25]	5
EDA-PSO	1	1.1	2.4	27	28	16	18	18	17	19	EDA-PSO [6]	3
full NEWUOA	1	1.1	4.9	25	76	250	13e-2/1e4				full NEWUOA [31]	
G3-PCX	1	1.1	2.2	130	290	60e-3/5e4					G3-PCX [26]	
simple GA	1	1.3	5.4	46	36	52	190	320	550	13e-4 /1e5	simple GA [22]	1.
GLOBAL	1	1.3	3.5	5	47e-2/600						GLOBAL [23]	
iAMaLGaM IDEA	1	1	2.7	1.1	3.8	2.9	4.6	5	6.3	6.8	iAMaLGaM IDEA [4]	_
LSfminbnd	1	1.3	240	64	180	260	16e-2/1e4				LSfminbnd [28]	ļ
LSstep	1	1.1	150	680	26e-1/1e4						LSstep [28]	L.
MA-LS-Chain	1	1.2	3.8	2.8	3.1	4.1	9.3	7.5	7.3	11	MA-LS-Chain [21]	1
MCS (Neum)	1	1	1.9	24	63	87e-3/1e4					MCS (Neum) [18]	J
NELDER (Han)	1	2	55	170	290	2500	54e-3/1e5				NELDER (Han) [16]	
NELDER (Doe)	1	1.1	1.9	10	48	36e-3/2e4					NELDER (Doe) [5]	
NEWUOA	1	1.2	2.3	40	620	32e-2/7e3					NEWUOA [31]	
(1+1)-ES	1	2	1200	7900	3.8e4	48e-2/1e6					(1+1)-ES [1]	
POEMS	1	140	170	15	14	21	19	17	29	41	POEMS [20]	
PSO	1	1.1	3.3	170	140	160	550	420	510	420	PSO [7]	
PSO_Bounds	1	1.1	3.4	7.9	52	35	51	49	61	120	PSO_Bounds [8]	
Monte Carlo	1	1.3	4	840	48e-2/1e6						Monte Carlo [3]	
Rosenbrock	1	1	2700	57e-1/1e4							Rosenbrock [27]	
IPOP-SEP-CMA-ES	1	1.1	3.8	3.4	1.3	1	1	1.1	1.1	1	IPOP-SEP-CMA-ES [29	1
VNS (Garcia)	1	1	6.6	1.6	4.8	4.8	7.9	9.8	18	82	VNS (Garcia) [11]	

				18	Schaffer I	7, conditi	on 1000						
Δ ftarget	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget		
ERT_{best}/D	0.2	0.24	20.7	75.5	794	1690	1860	2080	2180	2490	ERT_{best}/D		
ALPS	1	1.5	8.1	14	3.3	14	49	240	420	53e-7/1e6	ALPS [17]		
AMaLGaM IDEA	1.1	2.1	1.6	1.7	2	1.5	2.4	3.1	3.4	3.1	AMaLGaM IDEA [4]		
avg NEWUOA	1	5.4	10	270	57e-2/3e4						avg NEWUOA [31]		
BayEDAcG	1	2.6	4.4	9.6	11	8.7	14e-2/2e3				BayEDAcG [10]		
BFGS	1.8	100	57	51e-1/4e3							BFGS [30]		
Cauchy EDA	2.5	83	13	12	2.4	2.1	2.7	2.8	3.7	8.6	Cauchy EDA [24]		
BIPOP-CMA-ES	1	2.8	1	3.4	1	1	1	1.1	1.2	1.3	BIPOP-CMA-ES [15]		
(1+1)-CMA-ES	1	2.9	4.9	57	84	37e-2/1e4					(1+1)-CMA-ES [2]		
DASA	1.9	47	270	930	1600	64e-3/1e6					DASA [19]		
DEPSO	1.1	2.4	2.6	5.5	2.2	4.1	57e-3/2e3		•		DEPSO [12]		
DIRECT	1	1	1.4	2.9	1.9	6.2	6.5	8.1	44e-6/2e4		DIRECT [25]		
EDA-PSO	1	1.3	3.6	41	8.8	6.4	17	34	41	58	EDA-PSO [6]		
full NEWUOA	1	8.6	10	84	90	88	78e-2/1e4				full NEWUOA [31]		
G3-PCX	1	1.7	130	800	12e-1/5e4		•				G3-PCX [26]		
simple GA	1.1	2.3	22	59	34	130	15e-3/1e5				simple GA [22]		
GLOBAL	1.1	2.4	3.9	15	14	12e-1/500	•				GLOBAL [23]		
iAMaLGaM IDEA	1.2	2	1.1	1	1.4	1.6	1.9	2.3	3.1	4.8	iAMaLGaM IDEA [4]		
LSfminbnd	1	3.2	64	71	31e-2/1e4						LSfminbnd [28]		
LSstep	1.1	160	150	400	86	60e-1/1e4					LSstep [28]		
MA-LS-Chain	1	1.8	2.5	4.9	1.3	23	88	84	160	140	MA-LS-Chain [21]		
MCS (Neum)	1	1.5	19	150	75e-2/1e4						MCS (Neum) [18]		
NELDER (Han)	1.1	2.9	45	230	320	17e-2/1e5					NELDER (Han) [16]		
NELDER (Doe)	1	2.2	4.3	28	43	15e-2/2e4					NELDER (Doe) [5]		
NEWUOA	1.2	5.7	31	1400	11e-1/2e4						NEWUOA [31]		
(1+1)-ES	1	1.9	3100	3.1e4	22e-1/1e6						(1+1)-ES [1]		
POEMS	41	560	18	24	14	71	150	200	300	570	POEMS [20]		
PSO	1	2.6	2.2	6.6	110	250	53e-3/1e5				PSO [7]		
PSO_Bounds	1.1	2.5	3.8	21	69	72	120	330	10e-3/1e5		PSO_Bounds [8]		
Monte Carlo	1	1.2	18	9.4e4	15e-1/1e6				·		Monte Carlo [3]		
Rosenbrock	1.1	2600	3400	16e + 0/1e4							Rosenbrock [27]		
POP-SEP-CMA-ES	1	3	1.3	5	1.6	1	1	1	1	1	IPOP-SEP-CMA-ES [29]		
VNS (Garcia)	1	1.5	2.2	49	3.6	8.6	26	46	300	1200	VNS (Carcia) [11]		
	19 Griewank-Rosenbrock F8F2												
------------------------	-----------------------------	---------	---------	---------	-----------	-----------	-----------	-----------	-------	-------	----------------------	--	--
Δ ftarget	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$		
ERT _{best} /D	0.2	0.2	0.2	0.2	48.4	21000	24100	24200	24200	24400	ERThest/D		
ALPS	1	1.1	58	5100	500	15	39	40	40	40	ALPS [17]		
AMaLGaM IDEA	1	1.3	38	1100	360	4.5	4.2	4.2	4.2	4.2	AMaLGaM IDEA [4]		
avg NEWUOA	1	1	24	1.6e4	1e3	55e-3/1e5					avg NEWUOA [31]		
BayEDAcG	1	1.1	37	2100	45e-2/2e3						BayEDAcG [10]		
BFGS	1	2.2	1700	2.2e4	1800	62e-2/6e3					BFGS [30]		
Cauchy EDA	1	9.4	300	2.1e4	48e-2/5e4						Cauchy EDA [24]		
BIPOP-CMA-ES	1	1	20	2800	160	1	1	1	1	1	BIPOP-CMA-ES [15]		
(1+1)-CMA-ES	1	1	20	4100	970	19e-2/1e4					(1+1)-CMA-ES [2]		
DASA	1	4.8	290	6.7e4	4.7e4	13e-2/1e6		•			DASA [19]		
DEPSO	1	1	93	3100	71e-2/2e3						DEPSO [12]		
DIRECT	1	1	1	1	1.1	4.2	3.7	16e-3/2e4			DIRECT [25]		
EDA-PSO	1	1.2	37	6700	1600	71	66e-3/1e5	•			EDA-PSO [6]		
full NEWUOA	1	2.7	31	1.1e4	860	6.9	19e-2/1e4				full NEWUOA [31]		
G3-PCX	1	1.1	39	9.5e4	1.4e4	50e-2/5e4					G3-PCX [26]		
simple GA	1	1.1	35	1.2e4	700	68	60	59e-3/1e5		-	simple GA [22]		
GLOBAL	1	1.3	46	7300	10e-1/900					-	GLOBAL [23]		
iAMaLGaM IDEA	1	1.1	28	1100	370	10	12	12	12	12	iAMaLGaM IDEA [4]		
LSfminbnd	1	5.9	54	3e3	38e-2/1e4						LSfminbnd [28]		
LSstep	1	29	910	9500	1500	23e-2/1e4				-	LSstep [28]		
MA-LS-Chain	1	1.2	32	1300	250	8.4	47e-3/2e4			-	MA-LS-Chain [21]		
MCS (Neum)	1	1	1	1	1	16e-3/1e4					MCS (Neum) [18]		
NELDER (Han)	1	1.3	12	2900	590	59e-3/1e5				-	NELDER (Han) [16]		
NELDER (Doe)	1	1.2	12	340	110	14	47e-3/2e4				NELDER (Doe) [5]		
NEWUOA	1	1.9	14	2.7e4	1400	79e-3/1e5				-	NEWUOA [31]		
(1+1)-ES	1	1.3	100	4.1e5	2.9e5	49e-2/1e6				-	(1+1)-ES [1]		
POEMS	1	200	1e3	7200	1.4e4	18e-2/1e5				-	POEMS [20]		
PSO	1	1.1	35	3400	2400	67	60	60	61	61	PSO [7]		
PSO_Bounds	1	1.4	27	1.6e4	2500	70	80e-3/1e5				PSO_Bounds [8]		
Monte Carlo	1	1.3	38	1.4e5	36e-2/1e6						Monte Carlo [3]		
Rosenbrock	1	3.2	1.3e4	7.1e5	38e-1/1e4						Rosenbrock [27]		
IPOP-SEP-CMA-ES	1	1.1	22	1900	160	2.2	3	3	3	3	IPOP-SEP-CMA-ES [29]		
VNS (Garcia)	1	1	55	7600	1300	20	75	81	130	260	VNS (Garcia) [11]		

Table 67: 05-D, running time excess ERT/ERT_{best} on f_{19} , in italics is given the median final function value and the median number	of
function evaluations to reach this value divided by dimension	

20 Schwefel $x*sin(x)$														
Δ ftarget	Δ ftarget 1e+03 1e+02 1e+01 1e+00 1e-01 1e-02 1e-03 1e-04 1e-05 1e-07 Δ ftarget													
ERT _{best} /D	2.71	2.96	3.2	170	7620	10300	10900	10900	11000	11100	ERT _{best} /D			
ALPS	5.3	15	18	7	1.3	1	1	1.1	1.1	1.3	ALPS [17]			
AMaLGaM IDEA	3.2	3.8	3.9	29	24	18	17	17	17	17	AMaLGaM IDEA [4]			
avg NEWUOA	1.2	1.1	1	8.4	12	8.6	8.2	8.1	8.1	8	avg NEWUOA [31]			
BayEDAcG	2.5	4	8	20e-1/2e3							BayEDAcG [10]			
BFGS	1.1	1.5	1.8	2.5	10	7.6	7.2	7.2	7.1	7.1	BFGS [30]			
Cauchy EDA	44	49	48	460	11e-1/5e4						Cauchy EDA [24]			
BIPOP-CMA-ES	2.2	2.9	3.3	8.2	2.8	2.2	2.1	2.2	2.2	2.2	BIPOP-CMA-ES [15]			
(1+1)-CMA-ES	1.5	2.1	2.4	6.4	5.9	4.4	4.1	4.1	4.1	4.1	(1+1)-CMA-ES [2]			
DASA	24	29	32	13	47	35	33	33	33	33	DASA [19]			
DEPSO	3.6	7.7	8.6	3.2	24e-2/2e3						DEPSO [12]			
DIRECT	4.5	4.1	3.8	1.5	47e-2/2e4						DIRECT [25]			
EDA-PSO	3.3	4.9	5.7	13	2.5	2	2	2.1	2.3	2.5	EDA-PSO [6]			
full NEWUOA	1.6	1.5	1.4	6.4	47e-2/6e3						full NEWUOA [31]			
G3-PCX	3.2	7.7	7.4	36	88	66	62	62	61	61	G3-PCX [26]			
simple GA	5.5	22	47	21	1	1	1.3	2.2	2.6	5	simple GA [22]			
GLOBAL	4.8	12	17	18	13e-1/500						GLOBAL [23]			
iAMaLGaM IDEA	2.1	3	3.2	30	25	19	18	18	18	18	iAMaLGaM IDEA [4]			
LSfminbnd	5.8	7	8.2	18	65e-2/1e4						LSfminbnd [28]			
LSstep	110	190	230	41	18	14	13	13	13	13	LSstep [28]			
MA-LS-Chain	2.9	5.6	5.8	4.1	1.4	1.1	1	1	1	1	MA-LS-Chain [21]			
MCS (Neum)	2.5	2.8	2.7	1	9.1	6.8	6.4	6.4	6.4	6.3	MCS (Neum) [18]			
NELDER (Han)	1.1	1.5	1.5	25	24e-2/1e5						NELDER (Han) [16]			
NELDER (Doe)	1.8	2.1	2.2	8.5	37	28	26	26	26	26	NELDER (Doe) [5]			
NEWUOA	1	1	1	3.3	43e-2/6e3						NEWUOA [31]			
(1+1)-ES	3.4	3.9	4	16	43	32	30	30	30	30	(1+1)-ES [1]			
POEMS	83	80	78	8.5	14	10	9.9	9.9	10	10	POEMS [20]			
PSO	2.5	6	8.7	3.1	27	20	19	19	19	18	PSO [7]			
PSO_Bounds	3.1	7	8.1	8.6	21	16	15	15	15	16	PSO_Bounds [8]			
Monte Carlo	6.7	20	29	9200	99e-2/1e6						Monte Carlo [3]			
Rosenbrock	2.6	2.8	2.9	4.6	47e-2/1e4						Rosenbrock [27]			
IPOP-SEP-CMA-ES	2.1	3	3.3	6.6	2.3	1.7	1.7	1.7	1.7	1.7	IPOP-SEP-CMA-ES [29]			
VNS (Garcia)	3.7	11	10	7.8	4.3	3.9	4.3	4.5	4.6	5.7	VNS (Garcia) [11]			

Table 69, 07 Demonstration and the matter of the initialized in the matter of the matter and the matter of the second s
Table 68: 05-D, running time excess $ER1/ER1_{best}$ on J_{20} , in tables is given the median final function value and the median number of
function evaluations to reach this value divided by dimension

21 Gallagher 101 peaks													
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$		
ERT_{best}/D	0.2	0.2	8.2	231	335	338	341	344	346	351	ERT_{best}/D		
ALPS	1	1	3.4	2.2	2.9	3.9	4.7	5.6	6.4	8.1	ALPS [17]		
AMaLGaM IDEA	1	1	3	37	34	35	36	38	38	38	AMaLGaM IDEA [4]		
avg NEWUOA	1	1	1.7	2.5	3.6	3.5	3.5	3.5	3.5	3.5	avg NEWUOA [31]		
BayEDAcG	1	1	4.1	8.6	40	85	84	84	83	82	BayEDAcG [10]		
BFGS	1	1	3.8	1.4	1.9	1.9	1.9	1.9	1.9	2	BFGS [30]		
Cauchy EDA	1	1	20	27	190	430	420	420	420	410	Cauchy EDA [24]		
BIPOP-CMA-ES	1	1	2.3	14	24	25	25	25	25	25	BIPOP-CMA-ES [15]		
(1+1)-CMA-ES	1	1	4.2	4.6	6.6	6.6	6.5	6.5	6.5	6.4	(1+1)-CMA-ES [2]		
DASA	1	1	10	210	320	320	320	310	310	310	DASA [19]		
DEPSO	1	1	4.2	5.5	4.2	4.7	5	5.3	6.2	6.7	DEPSO [12]		
DIRECT	1	1	1	1	1.1	1.8	2.1	2.9	19	19	DIRECT [25]		
EDA-PSO	1	1	4	160	110	110	120	120	120	120	EDA-PSO [6]		
full NEWUOA	1	1	2.4	2.3	2.8	2.8	2.8	2.7	2.7	2.7	full NEWUOA [31]		
G3-PCX	1	1	2.1	4.7	6.8	6.7	6.7	6.7	6.7	6.6	G3-PCX [26]		
simple GA	1	1	4.6	5.5	61	68	70	77	140	290	simple GA [22]		
GLOBAL	1	1	2.3	1.1	1	1	1	1	1	1	GLOBAL [23]		
iAMaLGaM IDEA	1	1	2.2	27	22	22	22	22	22	22	iAMaLGaM IDEA [4]		
LSfminbnd	1	1	30	38	39	45	44	44	44	44	LSfminbnd [28]		
LSstep	1	1	560	120	120	120	130	130	130	130	LSstep [28]		
MA-LS-Chain	1	1	3.6	22	16	16	16	16	16	16	MA-LS-Chain [21]		
MCS (Neum)	1	1	1	3.9	5.1	5.1	5	5	5	5	MCS (Neum) [18]		
NELDER (Han)	1	1	12	8.4	10	10	10	10	9.9	9.8	NELDER (Han) [16]		
NELDER (Doe)	1	1	2.9	1.5	1.2	1.2	1.2	1.2	1.2	1.2	NELDER (Doe) [5]		
NEWUOA	1	1	1.1	2.2	1.8	1.8	1.8	1.8	1.8	1.9	NEWUOA [31]		
(1+1)-ES	1	1	45	19	18	18	18	18	18	18	(1+1)-ES [1]		
POEMS	1	1	34	330	290	290	290	290	290	290	POEMS [20]		
PSO	1	1	2	380	260	260	260	260	260	250	PSO [7]		
PSO_Bounds	1	1	3.5	380	340	340	340	340	340	340	PSO_Bounds [8]		
Monte Carlo	1	1	3.2	8.5	270	1.4e4	14e-3/1e6				Monte Carlo [3]		
Rosenbrock	1	1	9.7	7.9	15	15	15	15	15	15	Rosenbrock [27]		
IPOP-SEP-CMA-ES	1	1	3.6	14	9.9	10	10	10	10	10	IPOP-SEP-CMA-ES [29]		
VNS (Garcia)	1	1	2.4	7.5	6.5	6.6	6.9	7.8	8.3	9.1	VNS (Garcia) [11]		

Table 69: 05-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{21} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	22 Gallagher 21 peaks													
Δ ftarget	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$			
ERT_{best}/D	0.2	0.2	14.2	77.3	188	196	202	205	208	214	ERT_{best}/D			
ALPS	1	1	6.6	9.3	8.8	13	17	21	24	34	ALPS [17]			
AMaLGaM IDEA	1	1	3	19	59	69	69	69	68	67	AMaLGaM IDEA [4]			
avg NEWUOA	1	1	3.4	2.6	2.3	2.3	2.3	2.3	2.4	2.4	avg NEWUOA [31]			
BayEDAcG	1	1	13	75	22e-1/2e3						BayEDAcG [10]			
BFGS	1	1	3.1	2.9	2.1	2.1	2	2	2	2.6	BFGS [30]			
Cauchy EDA	1	1	11	280	780	1700	3500	3400	3400	3300	Cauchy EDA [24]			
BIPOP-CMA-ES	1	1	6.9	20	45	43	42	42	41	40	BIPOP-CMA-ES [15]			
(1+1)-CMA-ES	1	1	2.8	7.1	4.7	4.6	4.5	4.5	4.4	4.4	(1+1)-CMA-ES [2]			
DASA	1	1	96	270	130	130	130	140	140	150	DASA [19]			
DEPSO	1	1	6.5	6.3	7.5	10	11	14	16	32	DEPSO [12]			
DIRECT	1	1	1	1	12	19	22	62	130	400	DIRECT [25]			
EDA-PSO	1	1	6.7	12	89	90	92	95	98	100	EDA-PSO [6]			
full NEWUOA	1	1	4.3	3.7	3	2.9	2.9	3	3	3.1	full NEWUOA [31]			
G3-PCX	1	1	12	15	13	12	12	12	12	12	G3-PCX [26]			
simple GA	1	1	6	18	390	650	1500	6900	6800	24e-3/1e5	simple GA [22]			
GLOBAL	1	1	3.6	1.3	1	1	1	1	1	1	GLOBAL [23]			
iAMaLGaM IDEA	1	1	1.8	22	40	41	41	41	41	40	iAMaLGaM IDEA [4]			
LSfminbnd	1	1	13	47	29	60	62	120	120	220	LSfminbnd [28]			
LSstep	1	1	190	180	380	11e-1/1e4					LSstep [28]			
MA-LS-Chain	1	1	3.3	15	22	22	22	22	22	22	MA-LS-Chain [21]			
MCS (Neum)	1	1	1	1.1	12	11	11	11	11	15	MCS (Neum) [18]			
NELDER (Han)	1	1	19	13	13	13	13	12	12	12	NELDER (Han) [16]			
NELDER (Doe)	1	1	2.5	2.5	2.1	2	2	2	2	2.1	NELDER (Doe) [5]			
NEWUOA	1	1	2.1	2.1	2	2	2.1	2.2	2.3	2.4	NEWUOA [31]			
(1+1)-ES	1	1	21	37	30	29	29	29	29	30	(1+1)-ES [1]			
POEMS	1	1	470	1100	1300	1200	1200	1200	1200	1200	POEMS [20]			
PSO	1	1	2.6	330	470	450	440	430	430	420	PSO [7]			
PSO_Bounds	1	1	510	870	820	820	810	820	820	820	PSO_Bounds [8]			
Monte Carlo	1	1	7.6	73	390	7500	7.1e4	7e4	93e-4/1e6		Monte Carlo [3]			
Rosenbrock	1	1	19	13	10	10	10	10	10	11	Rosenbrock [27]			
IPOP-SEP-CMA-ES	1	1	7.5	23	60	58	57	57	56	55	IPOP-SEP-CMA-ES [29]			
VNS (Garcia)	1	1	5.8	16	18	18	18	18	19	20	VNS (Garcia) [11]			

Table 70: 05-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{22} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

23 Katsuuras												
Δ ftarget	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$	
ERT _{best} /D	0.2	0.2	0.6	104	2850	5580	6330	6480	6610	6850	ERT _{best} /D	
ALPS	1	1	2.2	21	29	100	3100	54e-4/1e6			ALPS [17]	
AMaLGaM IDEA	1	1	1.7	7	1.8	1	1	1	1	1	AMaLGaM IDEA [4]	
avg NEWUOA	1	1	6	2.5	14	15e-2/9e3					avg NEWUOA [31]	
BayEDAcG	1	1	1.8	62	12e-1/2e3	•	•				BayEDAcG [10]	
BFGS	1	1	11	31	69e-2/5e3						BFGS [30]	
Cauchy EDA	1	1	2.2	230	68e-2/5e4						Cauchy EDA [24]	
BIPOP-CMA-ES	1	1	1.7	13	3.7	2.1	1.8	1.8	1.8	1.8	BIPOP-CMA-ES [15]	
(1+1)-CMA-ES	1	1	4.2	3.3	7.5	26	11e-2/1e4				(1+1)-CMA-ES [2]	
DASA	1	1	9	20	360	88e-3/1e6					DASA [19]	
DEPSO	1	1	2	66	15e-1/2e3						DEPSO [12]	
DIRECT	1	1	1.5	3.5	5.7	3.7	6	93e-4/2e4			DIRECT [25]	
EDA-PSO	1	1	2.4	28	59e-2/1e5	•					EDA-PSO [6]	
full NEWUOA	1	1	5.4	2	3.8	87e-3/1e4					full NEWUOA [31]	
G3-PCX	1	1	2.6	2.4	8.6	60	44e-3/5e4				G3-PCX [26]	
simple GA	1	1	1.5	59	49e-2/1e5						simple GA [22]	
GLOBAL	1	1	1.6	1	4.8	23e-2/1e3					GLOBAL [23]	
iAMaLGaM IDEA	1	1	2.6	7.8	2.1	1.3	1.2	1.2	1.1	1.1	iAMaLGaM IDEA [4]	
LSfminbnd	1	1	1.8	11	45e-2/1e4		•				LSfminbnd [28]	
LSstep	1	1	1.4	6.6	51	31e-2/1e4	•				LSstep [28]	
MA-LS-Chain	1	1	2.6	2.5	1.7	4	3.6	3.5	3.4	3.3	MA-LS-Chain [21]	
MCS (Neum)	1	1	3.4	2.4	51	16e-2/1e4					MCS (Neum) [18]	
NELDER (Han)	1	1	2.9	3.5	2.7	3.2	4	4.6	4.6	5.6	NELDER (Han) [16]	
NELDER (Doe)	1	1	1.5	1	1	3.6	15	46	38e-4 /2e4		NELDER (Doe) [5]	
NEWUOA	1	1	6.2	2.4	7.1	20e-2/7e3					NEWUOA [31]	
(1+1)-ES	1	1	3.1	4.8	52	590	14e-3/1e6				(1+1)-ES [1]	
POEMS	1	1	13	23	26	22	25	33	33	32	POEMS [20]	
PSO	1	1	2.2	20	240	15e-2/1e5					PSO [7]	
PSO_Bounds	1	1	2.1	58	240	30e-2/1e5					PSO_Bounds [8]	
Monte Carlo	1	1	2.3	49	38e-2/1e6						Monte Carlo [3]	
Rosenbrock	1	1	1.6	1.8	4.6	13	17e-2/5e3				Rosenbrock [27]	
IPOP-SEP-CMA-ES	1	1	3.1	9.7	3.7	1.9	1.7	1.7	1.7	1.6	IPOP-SEP-CMA-ES [29]	
VNS (Garcia)	1	1	1	9.6	15	26	23	26	25	24	VNS (Garcia) [11]	

Table 71: 05-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{23} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	lo reach	viii vai	ue urvie	24 I	unacek bi	-Rastr	igin				
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{host}/D	0.2	0.2	324	43300	1.27e6	1.92e6	1.92e6	1.92e6	2.57e6	2.57e6	ERT_{host}/D
ALPS	1	5	8.1	9.6	75e-2/1e6						ALPS [17]
AMaLGaM IDEA	1	5.3	3.3	2.4	2.1	3.8	3.7	3.7	5.6	5.6	AMaLGaM IDEA [4]
avg NEWUOA	1	14	2	2.2	30e-1 /7e3						avg NEWUOA [31]
BayEDAcG	1	5.4	15	11e + 0/2e3							BayEDAcG [10]
BFGS	1	160	69	17e+0/3e3							BFGS [30]
Cauchy EDA	1.1	75	30	81e-1/5e4							Cauchy EDA [24]
BIPOP-CMA-ES	1	7.8	2.1	1.6	1	1	1	1	1	1	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	76	6.7	1.7	39e-1/1e4						(1+1)-CMA-ES [2]
DASA	1	79	250	32e-1/1e6						-	DASA [19]
DEPSO	1	5	29	14e + 0/2e3							DEPSO [12]
DIRECT	1	1	7.5	1.9	72e-1/2e4					-	DIRECT [25]
EDA-PSO	1	3.6	9.7	61e-1/1e5							EDA-PSO [6]
full NEWUOA	1	21	2.5	1.1	31e-1/7e3						full NEWUOA [31]
G3-PCX	1	4.9	44	61e-1/5e4							G3-PCX [26]
simple GA	1	7.3	21	54e-1/1e5							simple GA [22]
GLOBAL	1	6.3	4.2	91e-1/1e3					•		GLOBAL [23]
iAMaLGaM IDEA	1	6.3	3.1	2.2	2.2	7.5	7.5	7.5	5.6	5.6	iAMaLGaM IDEA [4]
LSfminbnd	1	30	9.1	63e-1/1e4						-	LSfminbnd [28]
LSstep	3	360	200	15e+0/1e4					•		LSstep [28]
MA-LS-Chain	1	3.8	2.1	52e-1/2e4					•		MA-LS-Chain [21]
MCS (Neum)	1	1	7	3.5	37e-1/1e4					-	MCS (Neum) [18]
NELDER (Han)	1	10	11	5.6	12e-1/1e5						NELDER (Han) [16]
NELDER (Doe)	1	4.3	1	1.4	15e-1/2e4						NELDER (Doe) [5]
NEWUOA	1	12	2.9	2.1	26e-1/6e3						NEWUOA [31]
(1+1)-ES	1	14	31	68	14e-1/1e6						(1+1)-ES [1]
POEMS	1	620	47	70e-1/1e5						-	POEMS [20]
PSO	1	6.5	5.7	63e-1/1e5	•					-	PSO [7]
PSO_Bounds	1	5.2	10	33	60e-1/1e5				•		PSO_Bounds [8]
Monte Carlo	1	4.1	2900	96e-1/1e6							Monte Carlo [3]
Rosenbrock	1	200	210	19e + 0/1e4						-	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	7.5	1.8	1	53e-1/1e4						IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	3.4	3.3	49	13	16	46	200	69e-4 /3e7		VNS (Garcia) [11]

Table 72: 05-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{24} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

1 Sphere												
$\Delta ftarget$	1e+03	1e + 02	1e+01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget	
ERT_{best}/D	0.1	0.1	2.2	2.27	2.29	2.3	2.3	2.3	2.3	2.3	ERT_{best}/D	
ALPS	1	8.9	84	230	410	590	780	950	1100	1500	ALPS [17]	
AMaLGaM IDEA	1	5	18	45	73	100	130	160	190	240	AMaLGaM IDEA [4]	
avg NEWUOA	1	27	1.7	1.7	1.7	1.7	1.7	1.7	1.7	1.7	avg NEWUOA [31]	
BayEDAcG	1	6.5	39	100	230	300	370	440	500	640	BayEDAcG [10]	
BFGS	1	13	1	1	1	1	1	1	1	1	BFGS [30]	
Cauchy EDA	1	240	160	350	510	700	870	1100	1200	1600	Cauchy EDA [24]	
BIPOP-CMA-ES	1	7.8	5.7	12	18	25	31	38	44	58	BIPOP-CMA-ES [15]	
(1+1)-CMA-ES	1	5.3	3.8	7.5	11	15	18	22	25	33	(1+1)-CMA-ES [2]	
DASA	1	110	29	45	59	77	95	110	130	180	DASA [19]	
DEPSO	1	3.2	19	45	84	130	170	220	280	390	DEPSO [12]	
DIRECT	1	1	8.8	31	64	97	140	190	240	400	DIRECT [25]	
EDA-PSO	1	9.2	22	800	1500	2300	3100	3900	4700	6400	EDA-PSO [6]	
full NEWUOA	1	40	3.1	3	3	3	3	3	3	3	full NEWUOA [31]	
G3-PCX	1	4.7	7.9	11	15	20	24	28	33	43	G3-PCX [26]	
simple GA	1	4.4	310	1200	2100	3200	4400	7100	1.2e4	6.1e4	simple GA [22]	
GLOBAL	1	5.3	15	14	14	14	14	14	14	14	GLOBAL [23]	
iAMaLGaM IDEA	1	5.7	8.5	25	41	57	72	87	100	140	iAMaLGaM IDEA [4]	
LSfminbnd	1	39	7.1	8.1	8.3	8.3	8.3	8.3	8.3	8.3	LSfminbnd [28]	
LSstep	1	960	140	150	160	160	160	160	160	160	LSstep [28]	
MA-LS-Chain	1	4.7	12	36	58	80	110	120	140	180	MA-LS-Chain [21]	
MCS (Neum)	1	1	1.2	2	2.1	2.2	2.9	2.9	2.9	2.9	MCS (Neum) [18]	
NELDER (Han)	1	7.1	2.5	6.1	9.5	13	16	19	23	31	NELDER (Han) [16]	
NELDER (Doe)	1	8.3	2.4	5.3	8.1	11	14	17	21	32	NELDER (Doe) $[5]$	
NEWUOA	1	14	1	1	1	1	1	1	1	1	NEWUOA [31]	
(1+1)-ES	1	17	3.9	6.9	10	13	16	19	22	28	(1+1)-ES [1]	
POEMS	1	1600	140	220	620	1e3	1500	2e3	2400	3300	POEMS [20]	
PSO	1	5.8	10	55	100	150	210	280	330	450	PSO [7]	
PSO_Bounds	1	5.7	18	180	700	1400	1700	2100	2500	5300	PSO_Bounds [8]	
Monte Carlo	1	5.4	3e3	35e-1/1e6						•	Monte Carlo [3]	
Rosenbrock	1	37	3.4	4.9	6.5	8.1	9.7	11	13	16	Rosenbrock [27]	
IPOP-SEP-CMA-ES	1	5.3	4.8	11	16	21	26	33	37	48	IPOP-SEP-CMA-ES [29]	
VNS (Garcia)	1	12	12	18	26	32	38	44	51	65	VNS (Garcia) [11]	

Table 73: 10-D, running time excess ERT/ERT_{best} on f_1 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

2 Ellipsoid separable												
Δ ftarget	1e + 03	1e + 02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget	
ERT_{hest}/D	14.6	18.5	18.7	19	19.1	19.1	19.3	19.3	19.4	19.5	ERT_{hest}/D	
ALPS	47	58	80	100	130	150	170	200	220	280	ALPS [17]	
AMaLGaM IDEA	8.7	11	15	20	25	29	32	35	39	46	AMaLGaM IDEA [4]	
avg NEWUOA	2.5	6.1	16	39	67	90	120	160	180	250	avg NEWUOA [31]	
BayEDAcG	32	34	42	57	66	74	81	89	97	110	BayEDAcG [10]	
BFGS	4.7	7.5	10	12	14	14	14	14	15	15	BFGS [30]	
Cauchy EDA	60	72	95	120	140	160	190	210	230	270	Cauchy EDA [24]	
BIPOP-CMA-ES	11	14	20	24	26	27	28	28	29	30	BIPOP-CMA-ES [15]	
(1+1)-CMA-ES	7.9	10	16	20	21	22	23	23	24	25	(1+1)-CMA-ES [2]	
DASA	6.4	6.7	8.6	11	13	15	18	21	25	34	DASA [19]	
DEPSO	8.9	11	16	22	28	34	42	48	55	69	DEPSO [12]	
DIRECT	11	12	15	150	150	160	170	380	410	1e3	DIRECT [25]	
EDA-PSO	200	250	350	440	520	620	710	810	890	1100	EDA-PSO [6]	
full NEWUOA	6.2	18	53	150	300	590	2500	7700	53e-4/1e4		full NEWUOA [31]	
G3-PCX	13	31	89	190	290	370	460	540	640	860	G3-PCX [26]	
simple GA	240	300	820	1400	2700	4400	7e3	1.2e4	7.4e4	53e-4/1e5	simple GA [22]	
GLOBAL	6.5	8.6	12	13	14	14	15	15	15	16	GLOBAL [23]	
iAMaLGaM IDEA	5.9	7.9	11	14	16	18	19	21	23	27	iAMaLGaM IDEA [4]	
LSfminbnd	1.2	1	1	1	1	1	1	1	1	1	LSfminbnd [28]	
LSstep	19	16	16	16	16	16	16	16	16	16	LSstep [28]	
MA-LS-Chain	7	9.6	14	18	23	27	32	37	42	52	MA-LS-Chain [21]	
MCS (Neum)	1	1.3	3.2	4.6	6.5	7.5	10	11	11	110	MCS (Neum) [18]	
NELDER (Han)	3.9	5.1	6.1	7	8.1	8.6	9.2	9.7	10	11	NELDER (Han) [16]	
NELDER (Doe)	4.2	10	22	52	83	100	120	130	130	200	NELDER (Doe) [5]	
NEWUOA	1.2	4.4	13	37	74	100	150	180	220	300	NEWUOA [31]	
(1+1)-ES	280	1300	5600	1.4e4	2.3e4	3.1e4	4.9e4	1.4e5	2.4e5	7.5e5	(1+1)-ES [1]	
POEMS	130	180	220	280	320	380	430	470	540	650	POEMS [20]	
PSO	17	26	41	420	420	430	430	440	440	450	PSO [7]	
PSO_Bounds	120	190	290	420	530	600	890	1200	1500	1800	PSO_Bounds [8]	
Monte Carlo	67e + 2/1e6										Monte Carlo [3]	
Rosenbrock	1.6	3.4	39	100	160	210	220	280	370	650	Rosenbrock [27]	
IPOP-SEP-CMA-ES	4.9	5.6	6.9	7.7	8.5	9.3	9.9	11	11	12	IPOP-SEP-CMA-ES [29]	
VNS (Garcia)	20	24	29	33	37	39	41	43	44	47	VNS (Garcia) [11]	

Table 74: 10-D, running time excess ERT/ERT_{best} on j	f_2 , in italics i	s given the	e median final	function	value and th	e median	number	of
function evaluations to reach this value divided by dimen	nsion							

				3 Kastri	igin separa	able					
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{best}/D	0.1	6.9	174	360	361	364	364	364	365	365	ERT_{best}/D
ALPS	2.6	30	11	40	59	59	61	64	67	81	ALPS [17]
AMaLGaM IDEA	3.7	6.7	4.6	1300	3.9e4	3.9e4	3.8e4	3.8e4	3.8e4	3.8e4	AMaLGaM IDEA [4]
avg NEWUOA	11	16	21e + 0/7e3								avg NEWUOA [31]
BayEDAcG	2.1	18	22e+0/2e3								BayEDAcG [10]
BFGS	30	370	70e + 0/5e3								BFGS [30]
Cauchy EDA	160	69	4100	15e + 0/5e4							Cauchy EDA [24]
BIPOP-CMA-ES	4.5	3.4	3.6	310	5900	5900	5900	5900	5900	5900	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	4.3	14	390	17e + 0/1e4							(1+1)-CMA-ES [2]
DASA	17	7.2	1	11	19	19	19	19	19	20	DASA [19]
DEPSO	1.5	8	170	19e + 0/2e3							DEPSO [12]
DIRECT	1	5.6	87	26e + 0/1e4							DIRECT [25]
EDA-PSO	2.6	34	18	1800	20e-1/1e5						EDA-PSO [6]
full NEWUOA	9.3	14	17e + 0/1e4								full NEWUOA [31]
G3-PCX	1.7	71	20e+0/5e4								G3-PCX [26]
simple GA	2.6	150	26	23	73	140	460	610	830	3900	simple GA [22]
GLOBAL	2.3	6.8	140	34e + 0/2e3							GLOBAL [23]
iAMaLGaM IDEA	2.7	3.6	4.4	270	2300	2300	2300	2300	2300	2300	iAMaLGaM IDEA [4]
LSfminbnd	57	2.2	47	11e + 0/5e3							LSfminbnd [28]
LSstep	1300	46	2.1	1	1	1	1	1	1	1	LSstep [28]
MA-LS-Chain	1.9	5.6	3.9	43	79	79	79	79	79	79	MA-LS-Chain [21]
MCS (Neum)	1	1	11	40e-1/4e3							MCS (Neum) [18]
NELDER (Han)	5.1	31	320	90e-1/1e5							NELDER (Han) [16]
NELDER (Doe)	4.4	1.1	180	11e + 0/2e4							NELDER (Doe) [5]
NEWUOA	5.1	20	23e+0/6e3								NEWUOA [31]
(1+1)-ES	5.9	74	6400	90e-1/1e6							(1+1)-ES [1]
POEMS	470	42	6.7	29	66	68	73	75	79	84	POEMS [20]
PSO	3.9	6.4	150	1800	1800	1800	1800	1800	1800	1800	PSO [7]
PSO_Bounds	2	11	50	44	51	52	54	55	70	95	PSO_Bounds [8]
Monte Carlo	2.4	2900	63e + 0/1e6								Monte Carlo [3]
Rosenbrock	18	330	53e+0/8e3								Rosenbrock [27]
IPOP-SEP-CMA-ES	2.5	2.7	3.1	62	20e-1/1e4						IPOP-SEP-CMA-ES [29]
VNS (Garcia)	2	5.6	3.2	24	190	210	230	230	260	290	VNS (Garcia) [11]

Table 75: 10-D, running time excess ERT/ERT_{best} on f_3 , in italics is given the median final function value and the median number of
function evaluations to reach this value divided by dimension
3 Bastrigin soparable

			4 Sk	ew Rastrig	gin-Bu	eche s	eparat	ole			
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{best}/D	0.1	9.82	223	363	366	370	371	374	374	2880	ERT_{best}/D
ALPS	2.4	39	14	100	170	170	170	180	190	30	ALPS [17]
AMaLGaM IDEA	2.6	8.9	41	50e-1/1e6				•			AMaLGaM IDEA [4]
avg NEWUOA	13	42	27e+0/1e4								avg NEWUOA [31]
BayEDAcG	2.1	28	18e+0/2e3								BayEDAcG [10]
BFGS	89	850	10e+1/5e3					•			BFGS [30]
Cauchy EDA	190	100	31e+0/5e4								Cauchy EDA [24]
BIPOP-CMA-ES	5.8	2.8	6.5	50e-1/3e5							BIPOP-CMA-ES [15]
(1+1)-CMA-ES	3.3	20	33e+0/1e4								(1+1)-CMA-ES [2]
DASA	130	7.8	1	16	52	51	51	51	51	6.8	DASA [19]
DEPSO	3.1	9.4	66	18e + 0/2e3							DEPSO [12]
DIRECT	1	4.2	180	19e + 0/1e4							DIRECT [25]
EDA-PSO	2.5	83	20	50e-1/1e5							EDA-PSO [6]
full NEWUOA	35	13	27e+0/1e4					•			full NEWUOA [31]
G3-PCX	2.9	500	35e+0/5e4								G3-PCX [26]
simple GA	2.7	140	22	26	79	310	1800	84e-4/1e5			simple GA [22]
GLOBAL	2.5	33	57e + 0/2e3								GLOBAL [23]
iAMaLGaM IDEA	3.5	5.5	29	50e-1/1e6				•			iAMaLGaM IDEA [4]
LSfminbnd	56	1.6	21e + 0/6e3								LSfminbnd [28]
LSstep	670	31	1.6	1	1	1	1	1	1	1	LSstep [28]
MA-LS-Chain	2.8	6.1	5.1	290	2e3	2e3	2e3	2e3	2e3	260	MA-LS-Chain [21]
MCS (Neum)	1	1	27	12e+0/4e3				•			MCS (Neum) [18]
NELDER (Han)	5.1	46	3300	17e + 0/1e5							NELDER (Han) [16]
NELDER (Doe)	3.1	2.8	20e+0/2e4								NELDER (Doe) [5]
NEWUOA	11	110	55e+0/7e3								NEWUOA [31]
(1+1)-ES	9.5	120	6.3e4	15e+0/1e6				•			(1+1)-ES [1]
POEMS	570	35	6.4	43	85	89	91	94	97	13	POEMS [20]
PSO	3.3	8.5	120	80e-1/1e5							PSO [7]
PSO_Bounds	3.5	28	37	190	200	200	200	200	210	30	PSO_Bounds [8]
Monte Carlo	2.3	2e4	86e+0/1e6					•			Monte Carlo [3]
Rosenbrock	32	780	70e+0/1e4								Rosenbrock [27]
IPOP-SEP-CMA-ES	6.5	2.7	6.6	60e-1/1e4							IPOP-SEP-CMA-ES [29]
VNS (Garcia)	3.2	5	7.2	2900	2.5e4	2.5e4	2.7e4	2.7e4	2.7e4	4600	VNS (Garcia) [11]

Table 76: 10-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_4 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

5 Linear slope														
Δ ftarget 1e+03 1e+02 1e+01 1e+00 1e-01 1e-02 1e-03 1e-04 1e-05 1e-07 Δ ftarget														
ERT _{best} /D	0.1	1.64	2.02	2.02	2.02	2.02	2.02	2.02	2.02	2.02	ERT _{best} /D			
ALPS	1	7.4	130	190	220	240	250	250	250	260	ALPS [17]			
AMaLGaM IDEA	1	4.6	39	45	46	46	46	46	46	46	AMaLGaM IDEA [4]			
avg NEWUOA	1	1.9	2	2.3	2.3	2.3	2.3	2.3	2.3	2.3	avg NEWUOA [31]			
BayEDAcG	BayEDAcG 1		91	120	140	140	140	140	140	140	BayEDAcG [10]			
BFGS	1	1.3	2.2	2.8	2.8	2.8	2.8	2.8	2.8	2.8	BFGS [30]			
Cauchy EDA	1	24	68	70	72	72	72	72	72	72	Cauchy EDA [24]			
BIPOP-CMA-ES	1	2.2	4.8	6	6.1	6.1	6.1	6.1	6.1	6.1	BIPOP-CMA-ES [15]			
(1+1)-CMA-ES	1	1.1	3.2	3.9	3.9	3.9	3.9	3.9	3.9	3.9	(1+1)-CMA-ES [2]			
DASA	1	13	23	31	36	40	43	47	50	58	DASA [19]			
DEPSO	1	7	33	47	50	50	50	50	50	50	DEPSO [12]			
DIRECT	1	6	36	52	53	53	53	53	53	53	DIRECT [25]			
EDA-PSO	1	2.9	11	17	20	20	21	21	21	21	EDA-PSO [6]			
full NEWUOA	1	2.8	3.6	4	4	4	4	4	4	4	full NEWUOA [31]			
G3-PCX	1	6.8	17	26	27	28	28	28	28	28	G3-PCX [26]			
simple GA	1	5.8	1400	3100	5400	8200	1.1e4	1.5e4	1.9e4	3e4	simple GA [22]			
GLOBAL	1	5.2	17	18	18	18	18	18	18	18	GLOBAL [23]			
iAMaLGaM IDEA	1	2.4	8.8	11	12	12	12	12	12	12	iAMaLGaM IDEA [4]			
LSfminbnd	1	8.3	14	15	15	15	15	15	15	15	LSfminbnd [28]			
LSstep	1	83	170	180	180	180	180	180	180	180	LSstep [28]			
MA-LS-Chain	1	4.7	41	45	49	49	49	49	49	49	MA-LS-Chain [21]			
MCS (Neum)	1	1	1	1	1	1	1	1	1	1	MCS (Neum) [18]			
NELDER (Han)	1	1.6	3.4	4.2	4.3	4.3	4.3	4.3	4.3	4.3	NELDER (Han) [16]			
NELDER (Doe)	1	1.2	3.1	4.1	4.1	4.1	4.1	4.1	4.1	4.1	NELDER (Doe) [5]			
NEWUOA	1	1.3	1.2	1.3	1.4	1.4	1.4	1.4	1.4	1.4	NEWUOA [31]			
(1+1)-ES	1	1.1	2.1	2.6	2.8	2.8	2.8	2.8	2.8	2.8	(1+1)-ES [1]			
POEMS	1	130	190	230	260	270	270	270	270	270	POEMS [20]			
PSO	1	2.9	13	17	19	19	20	20	20	20	PSO [7]			
PSO_Bounds	1	3.1	10	14	15	15	16	16	16	16	PSO_Bounds [8]			
Monte Carlo	1	11	27e + 0/1e6								Monte Carlo [3]			
Rosenbrock	1	3.7	4.1	4.3	4.4	4.4	4.4	4.4	4.4	4.4	Rosenbrock [27]			
IPOP-SEP-CMA-ES	1	2.2	5.4	7.1	7.2	7.3	7.3	7.3	7.3	7.3	IPOP-SEP-CMA-ES [29]			
VNS (Garcia)	1	5.6	9.6	10	11	11	11	11	11	11	VNS (Garcia) [11]			

Table 77: 10 D running time average FPT/FPT. on f, in italies is given the median final function value and the median number of												
Table 11. 10-D, fullning time excess Entr/Entrbest on 55, in mance is given the median multiple of												
function evaluations to reach this value divided by dimension												
F Lincon along												

				, in the second s	6 Attractiv	e secto	or				
$\Delta ftarget$	1e+03	1e + 02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget
ERT_{best}/D	2.79	10.2	39.9	61.5	82.6	104	129	157	184	237	ERT_{best}/D
ALPS	30	24	32	43	51	59	64	67	68	87	ALPS [17]
AMaLGaM IDEA	8	6.1	7.9	9.8	11	12	12	11	11	11	AMaLGaM IDEA [4]
avg NEWUOA	1.5	1.6	1	1	1	1	1.1	1.1	1.1	1.1	avg NEWUOA [31]
BayEDAcG	23	20	360	25e+0/2e3							BayEDAcG [10]
BFGS	2.9	3.7	3.9	4.2	4.5	4.6	4.5	4.4	4.5	66	BFGS [30]
Cauchy EDA	690	550	190	150	140	130	120	110	100	99	Cauchy EDA [24]
BIPOP-CMA-ES	2.2	3.6	2.1	2.1	2	1.9	1.9	1.8	1.7	1.7	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1.7	1.4	1.1	2.6	20	69	150	21e-4 /1e4			(1+1)-CMA-ES [2]
DASA	15	9.9	75	150	350	490	570	620	670	700	DASA [19]
DEPSO	11	5.5	6.8	11	14	24	37	50e-4 /2e3			DEPSO [12]
DIRECT	4.9	3.1	98	34e-1/1e4							DIRECT [25]
EDA-PSO	5.7	14	49	62	68	73	72	71	71	71	EDA-PSO [6]
full NEWUOA	2.4	2.1	1	1	1	1	1	1	1	1	full NEWUOA [31]
G3-PCX	5	2.2	1.7	2.4	3.6	3.8	3.9	4.1	4.5	5.4	G3-PCX [26]
simple GA	160	80	140	4700	28e-1/1e5	•			•		simple GA [22]
GLOBAL	9.3	4.6	3.2	3.3	3.5	3.4	3.4	3.3	4	83	GLOBAL [23]
iAMaLGaM IDEA	3.8	3.8	3.2	4.2	4.8	5.1	5.1	5.1	5	4.9	iAMaLGaM IDEA [4]
LSfminbnd	8.2	85	220	370	300	680	1100	920	790	40e-1/1e4	LSfminbnd [28]
LSstep	120	160	600	2400	24e+0/1e4			•	•		LSstep [28]
MA-LS-Chain	10	4.9	6.6	9.1	9.7	9.5	8.6	7.8	7.3	6.4	MA-LS-Chain [21]
MCS (Neum)	1.8	3.6	19	180	170	280	16e-1/4e3		·		MCS (Neum) [18]
NELDER (Han)	1.8	4.6	4.2	5.3	5.5	5.8	5.7	6.1	6.3	9	NELDER (Han) [16]
NELDER (Doe)	1.3	1.1	3.8	10	15	18	25	58	260	14e-6/2e4	NELDER (Doe) [5]
NEWUOA	1	1.1	2.1	3.3	4	4.9	5.5	5.9	5.9	6.2	NEWUOA [31]
(1+1)-ES	2	2.8	1.8	1.9	2.1	2.5	2.4	2.4	2.4	2.6	(1+1)-ES [1]
POEMS	92	36	30	40	44	46	46	45	44	45	POEMS [20]
PSO	4.9	4.7	400	420	320	260	210	180	160	130	PSO [7]
PSO_Bounds	4.8	5.6	45	120	140	150	140	130	130	160	PSO_Bounds [8]
Monte Carlo	1300	1500	25e+0/1e6						•		Monte Carlo [3]
Rosenbrock	2.5	1	10	38	41	37	34	33	31	29	Rosenbrock [27]
POP-SEP-CMA-ES	3	4.2	2.2	2.3	2.4	2.4	2.4	2.3	2.2	2.1	IPOP-SEP-CMA-ES [29]
VNS (Carcia)	6	6.1	26	9.4	0.0	0.0	0.1	0	10	1.0	VINC (CI ·) [11]

Table 78: 10-D, running time excess ERT/ERT_{best} or	n f_6 , in	italics is given	the median fin	al function	value and the	median numb	er of
function evaluations to reach this value divided by dim	iension						

incluon evaluations to reach this value divided by dimension													
7 Step-ellipsoid													
Δ ftarget 1e+03 1e+02 1e+01 1e+00 1e-01 1e-02 1e-03 1e-04 1e-05 1e-07 Δ fta EBT, /D 0.1 3.29 17.2 161 420 510 514 514 514 539 EBT,													
ERT _{best} /D	0.1	3.29	17.2	161	420	510	514	514	514	539	ERT _{best} /D		
ALPS	1.6	15	25	9.8	25	57	59	59	59	56	ALPS [17]		
AMaLGaM IDEA	1.5	4.9	3.9	1	2.3	2.6	2.6	2.6	2.6	2.5	AMaLGaM IDEA [4]		
avg NEWUOA	3	1.4	16	38	73e-2/1e4						avg NEWUOA [31]		
BayEDAcG	2.4	13	23	47e-1/2e3							BayEDAcG [10]		
BFGS	14	150	13e + 1/100								BFGS [30]		
Cauchy EDA	93	50	31	7.2	4.4	4.7	4.9	4.9	4.9	4.9	Cauchy EDA [24]		
BIPOP-CMA-ES	3.2	2.8	2.3	1.2	1.3	1.3	1.3	1.3	1.3	1.2	BIPOP-CMA-ES [15]		
(1+1)-CMA-ES	2.5	2.1	7.4	5.9	5	20	20	20	20	19	(1+1)-CMA-ES [2]		
DASA	37	33	280	8800	13e-1/6e5						DASA [19]		
DEPSO	2.1	6.6	9.2	21	32	14e-1/2e3					DEPSO [12]		
DIRECT	1	1.7	16	68	70e-2/1e4						DIRECT [25]		
EDA-PSO	1.7	5.6	57	17	130	110	110	110	110	100	EDA-PSO [6]		
full NEWUOA	3.7	2.1	1	7.6	110	51e-2/1e4					full NEWUOA [31]		
G3-PCX	2.1	3.7	21	520	19e-1/2e4						G3-PCX [26]		
simple GA	2.7	23	140	270	680	2900	2800	2800	2800	48e-2/1e5	simple GA [22]		
GLOBAL	1.8	6.1	11	50	45e-1/500						GLOBAL [23]		
iAMaLGaM IDEA	1.8	4	3	1	1	2.1	2.1	2.1	2.1	2	iAMaLGaM IDEA [4]		
LSfminbnd	16	12	95	270	40e-1/1e4						LSfminbnd [28]		
LSstep	110	160	720	93e-1/1e4							LSstep [28]		
MA-LS-Chain	2.7	4.8	7.7	15	110	120	120	120	120	110	MA-LS-Chain [21]		
MCS (Neum)	1	1.3	53	50e-1/4e3							MCS (Neum) [18]		
NELDER (Han)	3	1.4	69	940	11e-1/1e5						NELDER (Han) [16]		
NELDER (Doe)	4.5	1.1	59	400	19e-1/2e4						NELDER (Doe) [5]		
NEWUOA	4.1	1	27	1e3	24e-1/1e4						NEWUOA [31]		
(1+1)-ES	6.3	2.7	190	7e3	85e-2/1e6						(1+1)-ES [1]		
POEMS	1100	88	40	12	74	80	80	80	80	76	POEMS [20]		
PSO	2.2	3.4	10	770	11e-1/1e5						PSO [7]		
PSO_Bounds	1.9	4.2	19	730	3300	13e-1/1e5					PSO_Bounds [8]		
Monte Carlo	2.2	32	6e4	94e-1/1e6							Monte Carlo [3]		
Rosenbrock	150	400	67e + 0/3e3	•							Rosenbrock [27]		
IPOP-SEP-CMA-ES	2.4	2.2	2.5	1.5	1.1	1	1	1	1	1	IPOP-SEP-CMA-ES [29]		
VNS (Garcia)	1.4	8.3	3.2	4.1	19	31	34	34	34	33	VNS (Garcia) [11]		

Table 79: 10-D, running time excess ERT/ERT _{best}	on f_7 , in italics is	given the median fina	l function value and the	median number of
function evaluations to reach this value divided by d	limension			

RT	
n°	
0383	

Table 80: 10-D, ru	nning ti s to rea	ime excess E ch this value	RT/ER	T_{best} on f_8	s, in italics	is given the	median fin	al func	tion value a	and the me	dian number of	omp
	15 10 104	ch this value	uiviaco	a by annen.	8 Rosenbr	ock origin	al					ari
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$	08
ERT _{best} /D	4.23	13.2	32.2	80.6	93.4	101	104	106	108	110	ERT _{best} /D	n
ALPS	53	43	43	120	170	250	330	450	570	3300	ALPS [17]	3
AMaLGaM IDEA	10	7.4	7.4	13	14	14	15	15	15	16	AMaLGaM IDEA [4]	~ 1
avg NEWUOA	1.2	1.2	1	1	1	1	1	1	1	1	avg NEWUOA [31]	1,
BayEDAcG	29	22	75	93e-1/2e3							BayEDAcG [10]	
BFGS	1.9	2.3	1.7	1.7	1.6	1.5	1.5	1.5	1.5	1.5	BFGS [30]	ы
Cauchy EDA	110	82	66	120	110	110	110	110	120	120	Cauchy EDA [24]	Ĕ
BIPOP-CMA-ES	4	2.4	1.9	4.7	5	5.1	5.2	5.3	5.4	5.6	BIPOP-CMA-ES [15]	Š
(1+1)-CMA-ES	3.1	2.9	1.9	6.8	6.7	6.5	6.5	6.6	6.6	6.7	(1+1)-CMA-ES [2]	Э
DASA	18	21	22	200	420	630	900	1200	1400	1900	DASA [19]	Э
DEPSO	11	9	12	54e-1/2e3							DEPSO [12]	2
DIRECT	9.1	7.7	32	550	64e-1/1e4						DIRECT [25]	5
EDA-PSO	65	130	140	220	300	410	530	640	760	46e-8/1e5	EDA-PSO [6]	ы
full NEWUOA	2.8	2	1.3	1.1	1.2	1.2	1.2	1.2	1.2	1.2	full NEWUOA [31]	
G3-PCX	4.6	3.5	2.9	6.9	6.8	6.7	6.7	6.7	6.8	7	G3-PCX [26]	j j
simple GA	280	230	210	53e-1/1e5							simple GA [22]	
GLOBAL	7.7	3.2	2.1	1.7	1.6	1.5	1.5	1.5	1.5	1.5	GLOBAL [23]	-
iAMaLGaM IDEA	6.5	4.7	4	8.4	8.8	8.9	9.1	9.3	9.6	10	iAMaLGaM IDEA [4]	
LSfminbnd	7.2	7.3	19	190	180	440	1300	1400	40e-1/1e4		LSfminbnd [28]	7
LSstep	140	80	63	180	470	1500	12e-1/1e4				LSstep [28]	1.
MA-LS-Chain	7.9	6.7	7.3	13	14	14	15	15	15	15	MA-LS-Chain [21]	1
MCS (Neum)	1.6	1	1	1.6	1.5	1.6	1.6	1.6	1.6	1.6	MCS (Neum) [18]	7
NELDER (Han)	1.6	2.5	2	5.4	5.1	5	5	5.1	5.1	5.2	NELDER (Han) [16]	
NELDER (Doe)	2.2	1.3	1.4	2.5	3.3	3.5	3.7	3.8	4	4.4	NELDER (Doe) [5]	
NEWUOA	1	1.4	1	1.7	1.6	1.6	1.6	1.6	1.6	1.6	NEWUOA [31]	
(1+1)-ES	3.7	13	22	160	150	170	200	240	270	340	(1+1)-ES [1]	
POEMS	80	59	64	470	840	45e-3/1e5					POEMS [20]	
PSO	9.1	10	13	270	350	470	620	790	1500	6700	PSO [7]	
PSO_Bounds	17	44	66	690	750	820	1700	1.4e4	1.4e4	93e-5/1e5	PSO_Bounds [8]	
Monte Carlo	5400	36e + 1/1e6									Monte Carlo [3]	
Rosenbrock	2.1	3.6	12	59	81	110	170	320	430	1300	Rosenbrock [27]	
IPOP-SEP-CMA-ES	3.2	2.4	2.9	7.5	7.5	7.4	7.5	7.5	7.5	7.7	IPOP-SEP-CMA-ES [29)]
VNS (Garcia)	10	5.6	3.5	8.4	8.7	8.6	8.8	8.8	8.9	9	VNS (Garcia) [11]	

 $\overset{\infty}{2}$

9 Rosenbrock rotated													
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$													
ERT_{hest}/D	0.1	0.1	20	64.8	85.7	99.3	107	111	114	119	ERT_{best}/D		
ALPS	1700	5e3	66	320	470	730	1900	3e3	4400	6.1e4	ALPS [17]		
AMaLGaM IDEA 350 700 9.3 17		17	15	15	15	15	15	16	AMaLGaM IDEA [4]				
avg NEWUOA 69 150 1.3 1.8		1.8	1.5	1.4	1.3	1.3	1.2	1.2	avg NEWUOA [31]				
BayEDAcG	860	2500	56	88e-1/2e3							BayEDAcG [10]		
BFGS	88	230	2.1	1.9	1.6	1.4	1.4	1.3	1.3	1.3	BFGS [30]		
Cauchy EDA	4400	1e4	100	150	130	120	110	110	110	120	Cauchy EDA [24]		
BIPOP-CMA-ES	130	350	3.4	6.3	5.9	5.5	5.4	5.4	5.5	5.5	BIPOP-CMA-ES [15]		
(1+1)-CMA-ES	100	350	3.3	7.7	6.6	6.1	5.9	5.8	5.8	5.8	(1+1)-CMA-ES [2]		
DASA	750	1.6e4	160	2200	2e3	2400	2900	3700	4300	5800	DASA [19]		
DEPSO	420	1100	15	70e-1/2e3							DEPSO [12]		
DIRECT	1	1	9.4	350	17e-1/1e4						DIRECT [25]		
EDA-PSO	3200	1.7e4	220	340	540	1500	85e-4/1e5				EDA-PSO [6]		
full NEWUOA	140	250	1.6	2	1.7	1.6	1.5	1.5	1.5	1.4	full NEWUOA [31]		
G3-PCX	190	470	4.7	15	12	11	10	10	10	9.9	G3-PCX [26]		
simple GA	9e3	2.8e4	370	79e-1/1e5							simple GA [22]		
GLOBAL	330	450	2.9	2.2	1.8	1.6	1.5	1.5	1.5	1.4	GLOBAL [23]		
iAMaLGaM IDEA	250	560	6.3	10	9.6	9	8.9	8.9	9.1	9.3	iAMaLGaM IDEA [4]		
LSfminbnd	230	1200	51	120	860	14e-2/1e4					LSfminbnd [28]		
LSstep	5800	3.3e4	420	90e-1/1e4							LSstep [28]		
MA-LS-Chain	290	870	12	36	31	28	27	26	26	25	MA-LS-Chain [21]		
MCS (Neum)	1	1	1	1	1	1	1	1	1	1	MCS (Neum) [18]		
NELDER (Han)	45	240	2.4	3.7	3.4	3.1	3.2	3.2	3.2	3.3	NELDER (Han) [16]		
NELDER (Doe)	49	150	2.7	7.1	6.5	6.1	6	5.9	6	6	NELDER (Doe) [5]		
NEWUOA	39	140	1.7	1.7	1.4	1.3	1.2	1.2	1.2	1.2	NEWUOA [31]		
(1+1)-ES	100	1600	9.5	230	190	190	220	240	280	330	(1+1)-ES [1]		
POÉMS	3100	6200	110	770	1.7e4	18e-2/1e5					POEMS [20]		
PSO	320	1700	24	840	1900	11e-2/1e5					PSO [7]		
PSO_Bounds	770	4.3e4	450	1100	1600	78e-3/1e5					PSO_Bounds [8]		
Monte Carlo	3.7e5	33e+1/1e6									Monte Carlo [3]		
Rosenbrock 79 200 27 77		77	70	87	130	180	12e-5/1e4		Rosenbrock [27]				
IPOP-SEP-CMA-ES 130 780 6.9 10		10	8.9	8.1	7.8	7.7	7.7	7.7	IPOP-SEP-CMA-ES [29]				
VNS (Garcia)	340	580	4.6	9.8	12	13	13	12	12	12	VNS (Garcia) [11]		

Table 81: 10-D, running time excess ERT/ERT _{best}	on f_9 , ir	n italics	is given	the median	final f	function	value and	the	median	number	of
function evaluations to reach this value divided by d	mension	L									

Comparison Tables: BBOB 2009 Function Testbed

Table 82: 10-D. ru	nning time e	excess ERT/	ERThost on	f_{10} , in italic	cs is given th	ne median f	inal fur	nction v	alue and th	ne median r	number of
function evaluation	s to reach th	nis value div	ided by dime	ension	0						ıpc
			lucu by unit	1	10 Ellipsoid	1					uri
Δ ftarget	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget \overset{\infty}{\circ}$
ERT _{best} /D	46.3	104	184	217	245	273	280	308	454	474	ERT_{hest}/D^{2}
ALPS	59	180	850	7800	30e-1/5e5						ALPS [17]
AMaLGaM IDEA	2.9	2.2	1.8	1.9	2	2	2.2	2.2	1.6	1.9	AMaLGaM ÌDÉA [4]
avg NEWUOA	1.3	1.3	1.9	3.5	5.4	6.6	9	9.9	8.1	10	avg NEWUOA [31]
BayEDAcG	16e+3/2e3										BayEDAcG [10]
BFGS	1.8	1.3	1	1	1	1	1	1	1.3	920	BFGS [30]
Cauchy EDA	22	14	10	11	11	12	13	13	10	11	Cauchy EDA [24]
BIPOP-CMA-ES	3.8	2.7	2.3	2.1	1.9	1.8	1.8	1.7	1.2	1.2	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	2.8	2.1	1.7	1.8	1.7	1.6	1.5	1.4	1	1	(1+1)-CMA-ES [2]
DASA	320	1500	7200	2.2e4	6.1e4	76e-1/1e6					DASA [19]
DEPSO	310	19e + 2/2e3									DEPSO [12]
DIRECT	89	37e + 1/1e4									DIRECT [25]
EDA-PSO	300	830	56e + 0/1e5								EDA-PSO [6]
full NEWUOA	1.9	5.3	10	20	33	54	260	240	79e-4/1e4		full NEWUOA [31]
G3-PCX	6.1	6.9	10	19	26	30	37	40	31	38	G3-PCX [26]
simple GA	3500	1.4e4	12e + 2/1e5								simple GA [22]
GLOBAL	2.6	1.6	1.2	1.2	1.3	1.2	1.2	1.2	1.6	29e-7/1e3	GLOBAL [23]
iAMaLGaM IDEA	2.1	1.5	1.2	1.3	1.3	1.3	1.4	1.4	1	1.1	iAMaLGaM IDEA [4]
LSfminbnd	440	14e + 2/1e4									LSfminbnd [28]
LSstep	1600	88e + 2/1e4									LSstep [28]
MA-LS-Chain	10	8	11	11	9.8	9	9	8.3	5.7	5.6	MA-LS-Chain [21]
MCS (Neum)	170	11e + 2/4e3									MCS (Neum) [18]
NELDER (Han)	1.8	2.2	4.1	16	43	100	240	820	1600	27e-5/1e5	NELDER (Han) [16]
NELDER (Doe)	2.7	3.7	9.5	25	34	57	330	970	31e-4/2e4		NELDER (Doe) [5]
NEWUOA	1	1	2.1	3.8	6	7.4	10	11	9.2	12	NEWUOA [31]
(1+1)-ES	43	170	530	1100	1700	2400	3700	9100	1.1e4	43e-5/1e6	(1+1)-ES [1]
POEMS	300	1300	10e + 1/1e5								POEMS [20]
PSO	110	1e3	3900	74e + 0/1e5							PSO [7]
PSO_Bounds	640	2200	12e + 1/1e5								PSO_Bounds [8]
Monte Carlo	72e + 2/1e6										Monte Carlo [3]
Rosenbrock	57	80	120	230	22e+0/1e4						Rosenbrock [27]
IPOP-SEP-CMA-ES	9.3	5.6	4	3.7	3.4	3.2	3.2	2.9	2	2	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	6	3.7	2.8	2.7	2.5	2.3	2.3	2.2	1.5	1.5	VNS (Garcia) [11]

Table 82: 10-D, running time excess ERT/ERT_{best} on f_{10} , in italics is given the median final function value and the median number of

 85

				v	11	Discus					
Δ ftarget	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{best}/D	1.98	2.3	26.6	104	260	295	334	375	409	484	ERT_{best}/D
ALPS	6.3	83	370	460	490	990	4300	14e-4 /5e5		•	ALPS [17]
AMaLGaM IDEA	5.5	14	4.4	1.9	1.1	1.2	1.3	1.4	1.4	1.5	AMaLGaM IDEA [4]
avg NEWUOA	10	220	36	18	9.5	12	14	14	15	15	avg NEWUOA [31]
BayEDAcG	4	58	62e + 0/2e3								BayEDAcG [10]
BFGS	2.2	7.1	1	1	1.7	6	56	12e-4 /8e3			BFGS [30]
Cauchy EDA	37	200	36	13	7	7.5	7.8	8.1	8.3	8.8	Cauchy EDA [24]
BIPOP-CMA-ES	6	82	13	3.8	1.7	1.6	1.5	1.4	1.3	1.2	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	2.2	42	9.9	3.8	1.9	2	1.9	1.8	1.7	1.5	(1+1)-CMA-ES [2]
DASA	5.9	850	1300	1e3	750	1100	1400	1600	2e3	3500	DASA [19]
DEPSO	7.1	140	47e + 0/2e3								DEPSO [12]
DIRECT	1.8	7.9	20e+0/1e4								DIRECT [25]
EDA-PSO	6.7	200	550	990	5700	57e-2/1e5					EDA-PSO [6]
full NEWUOA	15	820	290	31e-1/1e4							full NEWUOA [31]
G3-PCX	5.7	65	40	22	14	16	17	18	19	21	G3-PCX [26]
simple GA	5.3	100	1.6e4	17e + 0/1e5							simple GA [22]
GLOBAL	5	17	2.5	1.7	1.5	8.1	11e-3/2e3	•		•	GLOBAL [23]
iAMaLGaM IDEA	5	25	5.7	2	1	1	1	1	1	1	iAMaLGaM IDEA [4]
LSfminbnd	2.2	9400	13e+1/1e4								LSfminbnd [28]
LSstep	4.3	6.1e4	14e + 1/1e4								LSstep [28]
MA-LS-Chain	7	31	39	14	6	5.6	5.1	4.6	4.3	3.8	MA-LS-Chain [21]
MCS (Neum)	1	1	30e + 0/4e3								MCS (Neum) [18]
NELDER (Han)	3.8	17	15	8.8	6.9	13	37	85	440	24e-6/1e5	NELDER (Han) [16]
NELDER (Doe)	5.2	17	13	7.8	5.4	9.7	17	34	93	32e-6/2e4	NELDER (Doe) [5]
NEWUOA	1.4	41	11	5.5	3.1	3.4	4	4.1	4.3	4.6	NEWUOA [31]
(1+1)-ES	840	2.1e4	5300	2400	1300	1500	1700	1800	1900	3e3	(1+1)-ES [1]
POEMS	86	200	220	200	140	160	210	270	350	1500	POEMS [20]
PSO	6.7	240	220	150	100	130	160	170	190	500	PSO [7]
PSO_Bounds	6.5	670	1400	920	670	1200	1400	3900	3600	12e-2/1e5	PSO_Bounds [8]
Monte Carlo	7.9	120	5.3e5	12e + 0/1e6							Monte Carlo [3]
Rosenbrock	2.3	1e3	5500	1400	570	500	440	390	360	300	Rosenbrock [27]
IPOP-SEP-CMA-ES	5.3	260	29	8.4	3.5	3.2	2.9	2.6	2.4	2.1	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	5.9	160	17	4.7	2	19	17	16	15	13	VNS (Carcia) [11]

				v	12 F	Rent cigar					
Aftarget	1o±03	$1e \pm 02$	1e±01	1e±00	10-01	1e-02	10-03	1e-04	10-05	$1e_{-}07$	Aftarget
EBT, /D	21.2	27.5	51.5	89.6	124	139	157	197	366	515	EBT, /D
ALPS	86	84	57	120	210	1100	5400	1 1e4	1 9e4	13e=1 /5e5	ALPS [17]
AMaLGaM IDEA	14	13	8.5	6.6	6.6	7 9	9.1	9.2	5.9	5.3	AMaLGaM IDEA [4]
avg NEWIJOA	11	17	4 7	8	10	12	12	12	6.9	10	avg NEWIJOA [31]
BayEDAcG	73	72	48	59	71e-1 /2e3	12	12	12	0.0	10	BayEDAcG [10]
BEGS	1.5	1.3	1.3	1.4	1.4	1.3	1.3	2.2	2.6	23	BFGS [30]
Cauchy EDA	100	110	84	69	68	71	74	68	42	34	Cauchy EDA [24]
BIPOP-CMA-ES	3.7	3.3	3.7	4.6	5.3	5.6	5.6	5.2	3.1	2.5	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	2	2.3	4.2	5.5	6.1	7.4	7.2	6.4	3.8	3.5	(1+1)-CMA-ES [2]
DASA	12	10	7100	4.5e4	1.1e5	39e-1/1e6					DASA [19]
DEPSO	19	19	19	42	110	55e-1 /2e3					DEPSO [12]
DIRECT	35	31	29	130	170	340	64e-2/1e4				DIRECT [25]
EDA-PSO	300	290	490	300	810	4800	66e-3/1e5				EDA-PSO [6]
full NEWUOA	1.2	1.4	2.9	4.1	4.6	6.2	6.6	6.2	4.4	4.7	full NEWUOA [31]
G3-PCX	2.5	2.3	2.8	3.7	4	4.4	4.6	4.1	2.5	2	G3-PCX [26]
simple GA	460	490	1300	1900	1.1e4	18e-1/1e5					simple GA [22]
GLOBAL	1.8	1.4	1	1	1	1	1	1	1	2.9	GLOBAL [23]
AMaLGaM IDEA	7.7	7.2	5	4.8	4.9	5.4	5.7	5.5	3.4	3	iAMaLGaM IDEA [4]
LSfminbnd	2.6	2.4	98	170	1100	1e3	890	51e-1/1e4			LSfminbnd [28]
LSstep	74	67	170	730	63e-1/1e4						LSstep [28]
MA-LS-Chain	12	11	8	7.2	9.7	16	25	29	16	12	MA-LS-Chain [21]
MCS (Neum)	1.2	1	3.2	3.9	7	11	13	27	76	110	MCS (Neum) [18]
NELDER (Han)	1.6	1.8	3	4.7	5.3	5.3	5.4	4.8	2.8	2.3	NELDER (Han) [16]
NELDER (Doe)	1.8	1.6	3	6	7.2	7.6	7.7	6.9	4.3	6.5	NELDER (Doe) [5]
NEWUOA	1.1	1	1.9	2	2.1	2.3	2.3	2.1	1.2	1	NEWUOA [31]
(1+1)-ES	1.9	1600	1.5e4	4.8e4	56e-1/1e6						(1+1)-ES [1]
POEMS	160	160	1100	2300	3300	25e-1/1e5					POEMS [20]
PSO	19	20	310	1700	5200	<i>41e-1/1e5</i>					PSO [7]
PSO_Bounds	160	160	580	1800	3300	27e-1/1e5					PSO_Bounds [8]
Monte Carlo	20e+5/1e6			•		•			•		Monte Carlo [3]
Rosenbrock	1	27	38	340	1200	14e-1/1e4					Rosenbrock [27]
POP-SEP-CMA-ES	3	2.9	3	4.5	5.6	6.3	6.3	5.7	3.4	2.7	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	4.4	5.1	4.9	5.6	17	16	15	12	6.9	5.2	VNS (Garcia) [11]

RT	
n°	
0383	

Table 85: 10-D, ru	nning ti	me excess E	RT/ER	T_{best} on f_{13}	, in italics	is given the	median fina	l function v	alue and th	e median n	umber of $\begin{array}{c} C \\ C \\ m \end{array}$
function evaluation	ns to rea	ch this value	e divide	d by dimensi	ion						pa
				v	$13 \ S$	harp ridge	9				ris
Δ ftarget	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget \tilde{S}
ERT_{best}/D	1.18	7.75	38.7	59.6	79.7	101	459	534	621	778	ERT_{best}/D^{2}
ALPS	22	93	53	110	480	830	1100	3e3	54e-5/5e5		ALPS [17]
AMaLGaM IDEA	12	15	6.8	6.9	7	6.8	1.8	1.8	1.8	1.8	AMaLGaM IDEA [4]
avg NEWUOA	3.6	1.4	3	13	30	76	32	70	280	39e-5/1e4	avg NEWUOA [31]
BayEDAcG	17	99	230	26e+0/2e3							BayEDAcG [10]
BFGS	2.8	1.5	1	1	1	1	86	14e-4/1e4			BFGS [30]
Cauchy EDA	160	130	46	43	42	41	11	11	11	11	Cauchy EDA [24]
BIPOP-CMA-ES	4.5	5.3	3.6	4.2	5.6	4.8	1.3	1.3	1.5	1.8	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	3.9	3.3	4.7	5.7	6.9	9.7	3.5	3.7	4.4	6.9	(1+1)-CMA-ES [2]
DASA	24	20	220	380	1200	3600	1800	2900	1.1e4	14e-5/1e6	DASA [19]
DEPSO	8.8	19	58	73e-1 /2e3							DEPSO [12]
DIRECT	2.9	22	62	160	580	28e-2/1e4					DIRECT [25]
EDA-PSO	5.9	300	140	150	990	2900	3100	22e-3/1e5			EDA-PSO [6]
full NEWUOA	6.2	2.1	1.8	12	25	66	40	130	14e-4/1e4		full NEWUOA [31]
G3-PCX	9.8	4.9	13	50	96	160	72	290	820	26e-5/3e4	G3-PCX [26]
simple GA	22	490	480	1.1e4	33e-1/1e5						simple GA [22]
GLOBAL	11	4.9	1.7	1.4	1.3	1.2	5.3	23e-4 /600			GLOBAL [23]
iAMaLGaM IDEA	4.7	9.6	3.9	3.8	3.9	3.8	1	1	1	1	iAMaLGaM IDEA [4]
LSfminbnd	9	16	28	70	180	460	53e-3/1e4				LSfminbnd [28]
LSstep	250	300	470	750	1800	1500	12e + 0/1e4				LSstep [28]
MA-LS-Chain	6.6	19	16	33	140	160	50	43	43	43	MA-LS-Chain [21]
MCS (Neum)	1	4.2	37	44	59	280	86e-3/4e3				MCS (Neum) [18]
NELDER (Han)	2	3.8	4.4	9.1	15	21	5.9	6.2	9	13	NELDER (Han) [16]
NELDER (Doe)	2	2.4	7.2	16	40	76	64	160	480	11e-4/2e4	NELDER (Doe) [5]
NEWUÒA	2.3	1	2	9	20	42	29	69	20e-4 /8e3		NEWUOA [31]
(1+1)-ES	4.4	8.1	11	21	44	99	130	390	940	1.9e4	(1+1)-ES [1]
POÉMS	190	130	270	2e3	5100	31e-1/1e5					POEMS [20]
PSO	6	25	950	1.1e4	1.8e4	1.4e4	44e-1/1e5				PSO [7]
PSO_Bounds	5.2	98	2300	6800	1.8e4	1.4e4	86e-1/1e5				PSO_Bounds [8]
Monte Carlo	25	28e+1/1e6									Monte Carlo [3]
Rosenbrock	5.2	2	3.4	11	15	33	15	42	110	31e-5/1e4	Rosenbrock [27]
IPOP-SEP-CMA-ES	4.2	5.2	8.7	10	9.2	8.4	2.1	1.9	1.8	2	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	13	7.7	4.9	16	20	17	9.4	14	14	20	VNS (Garcia) [11]

				14	Sum	of diffe	erent powe	ers			
Δ ftarget	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{host}/D	0.1	0.1	3.69	9.83	13.3	20.5	39.2	50.5	68.7	430	ERT_{host}/D
ALPS	1	2.7	19	50	74	76	85	320	1400	28e-7/5e5	ALPS [17]
AMaLGaM IDEA	1	3.1	4.7	9	13	12	8.5	8.4	7.5	1.6	AMaLGaM IDEA [4]
avg NEWUOA	1	9.2	1.7	1.3	1.3	1.2	1.1	2.2	7.1	64	avg NEWUOA [31]
BayEDAcG	1	2.5	7.8	75	110	210	11e-3/2e3				BayEDAcG [10]
BFGS	1	11	1.6	1.6	1.6	1.4	1	1	1	11e-7/9e3	BFGS [30]
Cauchy EDA	1	230	71	85	94	88	60	57	51	11	Cauchy EDA [24]
BIPOP-CMA-ES	1	9.2	2.6	3.3	3.8	4.1	4.3	4.9	5.2	1.4	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	4.9	2	1.9	2.3	2.4	2.5	3.7	4.4	1.1	(1+1)-CMA-ES [2]
DASA	1	27	14	13	14	15	80	600	3600	18e-7/1e6	DASA [19]
DEPSO	1.1	2.5	6.6	9.5	15	21	33	35e-5 /2e3			DEPSO [12]
DIRECT	1	1	2.5	11	50	110	500	23e-4/1e4			DIRECT [25]
EDA-PSO	1	4	4.2	130	240	250	170	190	1100	68e-7/1e5	EDA-PSO [6]
full NEWUOA	1	7	3.1	1.8	2	1.7	1.4	2.8	12	37e-8/1e4	full NEWUOA [31]
G3-PCX	1	2.5	3.9	2.8	3	3.1	2.9	5.5	16	120	G3-PCX [26]
simple GA	1	3.2	18	250	370	400	4200	13e-4/1e5			simple GA [22]
GLOBAL	1.1	3.1	8	3.7	3.1	2.3	1.4	1.3	1.1	23e-7/300	GLOBAL [23]
iAMaLGaM IDEA	1.1	3.4	2.2	5	7.2	7	5	5.1	4.5	1	iAMaLGaM IDEA [4]
LSfminbnd	1	45	7.5	5.5	5.6	8.1	52	30e-5/1e4			LSfminbnd [28]
LSstep	1	560	150	120	110	170	29e-4/1e4	•	•		LSstep [28]
MA-LS-Chain	1	2.7	4.4	8.3	12	13	13	15	16	3.6	MA-LS-Chain [21]
MCS (Neum)	1	1	1.1	2.4	2.9	2.8	2.8	6.9	32e-6/4e3		MCS (Neum) [18]
NELDER (Han)	1	3.7	1.2	2.1	2.9	2.9	2.6	3.2	4.2	8.8	NELDER (Han) [16]
NELDER (Doe)	1	4.9	1.1	2.4	2.8	3.5	3.7	4.5	6.3	43	NELDER (Doe) [5]
NEWUOA	1	7.2	1	1	1	1	1	2.3	7.3	570	NEWUOA [31]
(1+1)-ES	1	6.8	2.2	2	2.2	2.3	4.6	44	580	82e-8/1e6	(1+1)-ES [1]
POEMS	110	970	68	50	110	140	120	170	3e3	12e-6/1e5	POEMS [20]
PSO	1.1	2.9	3.2	8.6	17	22	28	140	2100	83e-7/1e5	PSO [7]
PSO_Bounds	1	3.2	3.7	29	93	180	230	560	13e-6/1e5		PSO_Bounds [8]
Monte Carlo	1	2.5	17	15e-1/1e6				•	•		Monte Carlo [3]
Rosenbrock	1	25	2.1	1.3	1.4	1.7	6.3	46	190	96e-7/1e4	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	4.4	3	3.2	3.7	3.9	5.2	9	8.9	2	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	3	7.6	5.3	5.6	5.5	6.1	7.6	7.4	1.8	VNS (Garcia) [11]

Table 86: 10-D, running time excess 1	ERT/ERT _{best}	on f_{14} ,	in italics is	s given t	the median	final fu	unction	value and	the med	an numbe	er of
function evaluations to reach this value	ue divided by d	imensio	n								

Table 87: 10-D, running function evaluations to r	time exc reach this	ess ERT value d	/ERT _{best} ivided by di	on f_{15} , in it imension	talics is	given t	he med	lian fina	l funct	ion v	alue and the median number of
			, i i i i i i i i i i i i i i i i i i i	15 R	astrigi	n					
$\Delta ftarget$	1e + 03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget
ERT, /D	0.1	18.6	477	3020	7360	7470	7580	7670	7780	7980	ERT, /D

Italget	10 ± 00	10+02	16+01	10 ± 00	16-01	16-02	16-03	16-04	16-00	16-07	antarget
ERT _{best} /D	0.1	18.6	477	3920	7360	7470	7580	7670	7780	7980	ERT _{best} /D
ALPS	1.9	12	15	30e-1/5e5							ALPS [17]
AMaLGaM IDEA	1.9	2.5	1	3.5	3.7	3.7	3.7	3.7	3.7	3.6	AMaLGaM IDEA [4]
avg NEWUOA	5.5	4.3	230	25e+0/7e3							avg NEWUOA [31]
BayEDAcG	1.8	7.6	28e+0/2e3								BayEDAcG [10]
BFGS	59	110	70e + 0/4e3								BFGS [30]
Cauchy EDA	80	22	16e+0/5e4								Cauchy EDA [24]
BIPOP-CMA-ES	1.9	1	1	1.7	1.3	1.3	1.3	1.3	1.3	1.3	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1.2	2.9	150	18e + 0/1e4							(1+1)-CMA-ES [2]
DASA	29	270	2.9e4	19e + 0/1e6							DASA [19]
DEPSO	1.6	3.4	37e + 0/2e3								DEPSO [12]
DIRECT	1	2.2	84	17e+0/1e4							DIRECT [25]
EDA-PSO	2.5	23	7	170	190	190	190	180	180	180	EDA-PSO [6]
full NEWUOA	5.4	2.6	300	21e + 0/1e4							full NEWUOA [31]
G3-PCX	1.7	100	1500	24e+0/5e4							G3-PCX [26]
simple GA	1.7	56	27	41e-1/1e5							simple GA [22]
GLOBAL	1.4	13	67e + 0/900	•							GLOBAL [23]
iAMaLGaM IDEA	1.7	1.6	2.6	9.4	10	10	10	10	10	9.9	iAMaLGaM IDEA [4]
LSfminbnd	14	14	29e + 0/1e4								LSfminbnd [28]
LSstep	450	310	74e + 0/1e4	•							LSstep [28]
MA-LS-Chain	1.8	2.3	3.6	23	98	96	95	94	92	90	MA-LS-Chain [21]
MCS (Neum)	1	1.7	24e + 0/4e3								MCS (Neum) [18]
NELDER (Han)	3.3	8.1	240	99e-1/1e5							NELDER (Han) [16]
NELDER (Doe)	2.9	3.7	47	90e-1/2e4							NELDER (Doe) [5]
NEWUOA	5.1	4.5	170	22e + 0/6e3							NEWUOA [31]
(1+1)-ES	5.4	17	2100	99e-1/1e6							(1+1)-ES [1]
POEMS	240	19	320	11e + 0/1e5							POEMS [20]
PSO	1.6	2.1	840	23e+0/1e5							PSO [7]
PSO_Bounds	1.7	5.7	360	11e + 0/1e5							PSO_Bounds [8]
Monte Carlo	1.3	1e3	68e + 0/1e6								Monte Carlo [3]
Rosenbrock	13	710	89e+0/1e4	•							Rosenbrock [27]
IPOP-SEP-CMA-ES	2.3	1	1.2	1	1	1	1	1	1	1	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1.6	1.8	6.5	4300	6200	6100	6e3	5900	5900	7700	VNS (Garcia) [11]

				1	6 Weierst	rass					
Δ ftarget	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{hest}/D	0.1	0.1	42.5	703	1580	4570	5120	6510	6580	7160	ERT_{best}/D
ALPS	1	1.5	8.2	3	56	470	23e-3/5e5				ALPS [17]
AMaLGaM IDEA	1	1.4	8.5	4.9	5.8	4.5	5.1	4.2	4.2	3.9	AMaLGaM IDÉA [4]
avg NEWUOA	1	1.5	3.3	41	13e-1/1e4						avg NEWUOA [31]
BayEDAcG	1	1.3	41	95e-1/2e3							BayEDAcG [10]
BFGS	1	190	18e + 0/1e4								BFGS [30]
Cauchy EDA	1	4.3	400	76e-1/5e4							Cauchy EDA [24]
BIPOP-CMA-ES	1	1.1	3	1	1	1	1	1	1	1	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1.3	5.4	49	12e-1/1e4	•					(1+1)-CMA-ES [2]
DASA	1	1.7	190	3e3	11e-1/1e6						DASA [19]
DEPSO	1	1.2	170	11e + 0/2e3							DEPSO [12]
DIRECT	1	2.2	2.5	1.6	2.4	9.9	21e-3/1e4				DIRECT [25]
EDA-PSO	1	1.5	55	130	190	95	130	100	100	95	EDA-PSO [6]
full NEWUOA	1	1.1	3.6	16	90	99e-2/1e4					full NEWUOA [31]
G3-PCX	1	1.3	4.7	69	75e-2/5e4						G3-PCX [26]
simple GA	1	1.5	28	130	910	91e-2/1e5					simple GA [22]
GLOBAL	1	1.3	1	1.7	11e-1/800		•				GLOBAL [23]
iAMaLGaM IDEA	1	1.2	3.3	1.8	6.5	8.2	9.8	8.6	8.6	8	iAMaLGaM IDEA [4]
LSfminbnd	1	1.4	7.9	28e-1/1e4							LSfminbnd [28]
LSstep	1	2.1	51	47e-1/1e4							LSstep [28]
MA-LS-Chain	1	1.2	2	16	460	30e-2/5e4					MA-LS-Chain [21]
MCS (Neum)	1	2.4	17	86	33e-1/4e3						MCS (Neum) [18]
NELDER (Han)	1	1.5	17	100	75e-2/1e5						NELDER (Han) [16]
NELDER (Doe)	1	1.3	1.4	23	69e-2/2e4						NELDER (Doe) [5]
NEWUOA	1	2.3	4.7	25e-1/9e3							NEWUOA [31]
(1+1)-ES	1	1.6	65	3700	12e-1/1e6						(1+1)-ES [1]
POEMS	1	1	12	4.4	58	61	79	62	62	92	POEMS [20]
PSO	1	1.4	5.2	130	92e-2/1e5						PSO [7]
PSO_Bounds	1	1.5	42	140	260	89e-2/1e5					PSO_Bounds [8]
Monte Carlo	1	1.6	43	31e-1/1e6							Monte Carlo [3]
Rosenbrock	1	2.9	770	12e+0/1e4							Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1.5	2.9	1.2	1.6	1.2	1.3	1.3	1.3	1.2	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1.4	4.1	3.7	28	37	180	370	670	1600	VNS (Garcia) [11]

Table 88: 10-D, running time excess ERT/ERT _{best} o	n f_{16} , i	n italics is	given th	ne median	final f	function	value and	the m	edian 1	umber (of
function evaluations to reach this value divided by dir	nensior	ı									

				[°] 1	7 Schaffer	F7 condit	tion 10				
Δ ftarget	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget
ERTheat /D	0.1	0.1	2.64	42.9	220	633	985	1530	2020	2650	ERT_{host}/D
ALPS	1	1.2	3.5	18	19	130	1100	14e-4 /5e5			ALPS [17]
AMaLGaM IDEA	1	1	2.8	3.8	1.5	1.7	2.3	3.2	4.1	4	AMaLGaM IDEA [4]
avg NEWUOA	1	1.1	2.2	990	10e-1/3e4						avg NEWUOA [31]
BayEDAcG	1	1.3	4	11	6.4	7.3	18e-3/2e3				BayEDAcG [10]
BFGS	1	79	53	36e-1 /8e3							BFGS [30]
Cauchy EDA	1	56	67	35	27	12	9.4	6.9	6.2	6.6	Cauchy EDA [24]
BIPOP-CMA-ES	1	1.4	1.6	1.1	1.7	1	1	1	1	1	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	3.9	14	620	15e-1/1e4						(1+1)-CMA-ES [2]
DASA	1	1	110	2e4	83e-2/1e6						DASA [19]
DEPSO	1	1.5	5.5	6.7	4.9	15	28e-3/2e3				DEPSO [12]
DIRECT	1	1	1.3	3.7	7.2	23	44e-4/1e4				DIRECT [25]
EDA-PSO	1	1.1	2.4	44	22	13	11	9.4	8.8	9.4	EDA-PSO [6]
full NEWUOA	1	2.1	3.1	290	95e-2/1e4						full NEWUOA [31]
G3-PCX	1	1.2	3	5400	15e-1/5e4						G3-PCX [26]
simple GA	1	1.5	4.8	77	45	210	1500	11e-3/1e5			simple GA [22]
GLOBAL	1	1.2	3.9	27e-1/2e3							GLOBAL [23]
iAMaLGaM IDEA	1	1	1.6	1.8	3.3	2.2	3.6	5	8.6	12	iAMaLGaM IDEA [4]
LSfminbnd	1	4.1	35	26e-1/1e4							LSfminbnd [28]
LSstep	1	110	960	73e-1/1e4							LSstep [28]
MA-LS-Chain	1	1.2	2.8	5	8.9	15	21	21	26	53	MA-LS-Chain [21]
MCS (Neum)	1	1	1	1400	18e-1/4e3						MCS (Neum) [18]
NELDER (Han)	1	2.4	19	4200	6600	11e-1/1e5					NELDER (Han) [16]
NELDER (Doe)	1	1.2	1.2	450	77e-2/2e4						NELDER (Doe) [5]
NEWUOA	1	2.9	1.4	2100	14e-1/2e4						NEWUOA [31]
(1+1)-ES	1	1.9	3500	32e-1/1e6							(1+1)-ES [1]
POEMS	1	290	91	23	15	33	58	63	140	250	POEMS [20]
PSO	1	1.3	1.6	5	230	1e3	52e-3/1e5				PSO [7]
PSO_Bounds	1	1.2	1.5	29	320	1e3	1400	71e-3/1e5			PSO_Bounds [8]
Monte Carlo	1	1.3	3.2	21e-1/1e6							Monte Carlo [3]
Rosenbrock	1	1.5e4	8300	12e + 0/1e4							Rosenbrock [27]
POP-SEP-CMA-ES	1	1	1.6	1	1.1	1.3	1.3	1	1	1.1	IPOP-SEP-CMA-ES [29]
VNS (Carcia)	1	1	57	1 /	1	2.2	77	28	330	300 8 1706	UNS (Caraia) [11]

RT	
n°	
0383	

Table 90: 10-D, ru	nning ti	me exce	ess ERT/ER	$\Gamma_{\rm host}$ on f_{18}	, in italics i	is given the	median fina	al function	value and t	he median 1	number of
function evaluation	is to rea	ch this	value divideo	l by dimensi	ion	0					ιpa
				18	Schaffer I	7, conditi	ion 1000				rie
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{best}/D	0.1	0.193	23.8	83.6	701	1590	2750	3160	3720	4270	$ERT_{best}/\mathbb{D}^{\sim}$
ALPS	1	3.2	13	20	60	4700	19e-3/5e5				ALPS [17]
AMaLGaM IDEA	1.2	1.8	2.9	2.8	1.4	1.5	2.2	2.3	2.7	2.4	AMaLGaM IDEA [4]
avg NEWUOA	1	10	73	32e-1 /9e4							avg NEWUOA [31]
BayEDAcG	1	2.3	8.8	13	6.4	19	17e-2/2e3				BayEDAcG [10]
BFGS	1.7	160	5e3	16e + 0/8e3							BFGS [30]
Cauchy EDA	1.1	110	31	24	5.2	3.6	2.8	3	3.1	4.1	Cauchy EDA [24]
BIPOP-CMA-ES	1	3.1	1	1	1	1	1.2	1.1	1.1	1.2	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	4	110	40e-1/1e4							(1+1)-CMA-ES [2]
DASA	1.4	17	1400	8.1e4	19e-1/1e6						DASA [19]
DEPSO	1	4.4	4.3	10	13	19e-2/2e3					DEPSO [12]
DIRECT	1	1	2.3	8.1	4.2	28	38e-3/1e4				DIRECT [25]
EDA-PSO	1	2.1	28	42	9.2	6	7.5	21	79	43e-6/1e5	EDA-PSO [6]
full NEWUOA	1.1	13	120	1700	39e-1/1e4						full NEWUOA [31]
G3-PCX	1.1	1.6	800	51e-1/5e4							G3-PCX [26]
simple GA	1	1	57	85	120	88e-3/1e5					simple GA [22]
GLOBAL	1	1.9	84	90e-1 /2e3							GLOBAL [23]
iAMaLGaM IDEA	1.1	2.1	1.6	3.3	1.4	2.9	3.1	4.8	6.5	9.1	iAMaLGaM IDEA [4]
LSfminbnd	1	15	210	66e-1/1e4							LSfminbnd [28]
LSstep	1.1	230	19e+0/1e4								LSstep [28]
MA-LS-Chain	1.1	3.4	2.5	6.1	12	49	260	13e-3/5e4			MA-LS-Chain [21]
MCS (Neum)	1	1	57	51e-1/4e3							MCS (Neum) [18]
NELDER (Han)	1	3.5	510	8400	32e-1/1e5						NELDER (Han) [16]
NELDER (Doe)	1.1	2.8	72	3500	34e-1/2e4						NELDER (Doe) [5]
NEWUOA	1.1	99	560	51e-1/4e4							NEWUOA [31]
(1+1)-ES	2	10	2.8e5	14e + 0/1e6							(1+1)-ES [1]
POÉMS	2.1	530	19	28	42	130	240	450	24e-3/1e5		POEMS [20]
PSO	1	1.7	3.5	2400	2e3	11e-1/1e5			· .		PSO [7]
PSO_Bounds	1.1	2.5	10	140	580	880	38e-2/1e5				PSO_Bounds [8]
Monte Carlo	1	1.4	3300	72e-1 /1e6							Monte Carlo [3]
Rosenbrock	1	8700	40e+0/1e4								Rosenbrock [27]
IPOP-SEP-CMA-ES	1	3.3	4.4	2.8	1.2	1.1	1	1	1	1	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	2.7	1.7	1.1	1.8	22	93	1500	85e-6/6e6		VNS (Garcia) [11]

Table 90: 10-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{18} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

19 Griewank-Rosenbrock F8F2											
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget
ERT_{best}/D	0.1	0.1	0.1	0.1	1060	98400	1.37e5	1.37e5	1.38e5	1.39e5	ERT_{best}/D
ALPS	1	1	410	7.7e4	550	74e-3/5e5					ALPS [17]
AMaLGaM IDEA	1	1.1	160	7300	83	7.7	8.8	8.7	8.7	8.6	AMaLGaM IDEA [4]
avg NEWUOA	1	1	48	7.1e5	83e-2/1e5						avg NEWUOA [31]
BayEDAcG	1	1.3	210	20e-1/2e3	•		-	-	-		BayEDAcG [10]
BFGS	1	1.7	1.9e4	51e-1/8e3							BFGS [30]
Cauchy EDA	1	6.8	1400	3.4e6	14e-1/5e4						Cauchy EDA [24]
BIPOP-CMA-ES	1	1	52	9400	9.8	1	1	1	1	1	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1	63	8.7e4	55e-2/1e4						(1+1)-CMA-ES [2]
DASA	1	1.1	7100	1.5e7	13e-1/1e6		-	-	-		DASA [19]
DEPSO	1	1	210	29e-1/2e3							DEPSO [12]
DIRECT	1	1	1	1	16	11e-2/1e4	-	-	-		DIRECT [25]
EDA-PSO	1	1.1	130	3.7e5	1300	73e-2/1e5	-	-	-		EDA-PSO [6]
full NEWUOA	1	1.4	150	1.4e5	11e-1/1e4						full NEWUOA [31]
G3-PCX	1	1.1	3.6e4	1.5e6	16e-1/5e4						G3-PCX [26]
simple GA	1	1.1	1e3	1.7e5	290	14e-2/1e5	-	-	-		simple GA [22]
GLOBAL	1	1.2	370	1.2e5	15e-1/2e3		-	-	-		GLOBAL [23]
iAMaLGaM IDEA	1	1	78	2.5e5	370	73	110	110	110	110	iAMaLGaM IDEA [4]
LSfminbnd	1	3.1	200	1.4e6	18e-1/1e4			-	-		LSfminbnd [28]
LSstep	1	55	2700	17e-1/1e4				-	-		LSstep [28]
MA-LS-Chain	1	1.1	120	8600	87	13e-2/5e4					MA-LS-Chain [21]
MCS (Neum)	1	1	1	1	1	16e-3/4e3		-	-		MCS (Neum) [18]
NELDER (Han)	1	1	28	2.8e4	24e-2/1e5						NELDER (Han) [16]
NELDER (Doe)	1	1.1	24	1.2e4	26e-2/2e4						NELDER (Doe) $[5]$
NEWUOA	1	2.1	27	3.2e5	63e-2/1e5						NEWUOA [31]
(1+1)-ES	1	1.5	6500	2.8e7	18e-1/1e6						(1+1)-ES [1]
POEMS	1	380	2500	2.1e5	1400	57e-2/1e5					POEMS [20]
PSO	1	1.3	110	3.7e5	51e-2/1e5						PSO [7]
PSO_Bounds	1	1.1	120	9.2e5	57e-2/1e5		-				PSO_Bounds [8]
Monte Carlo	1	1.1	500	31e-1/1e6				•	•		Monte Carlo [3]
Rosenbrock	1	2.5	6.5e5	24e+0/1e4							Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1	54	1.6e4	17	10e-2/1e4					IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1.4	220	3.1e4	1900	60e-3/5e6					VNS (Garcia) [11]

Table 91: 10-D, running time excess ERT/ERT_{best} on f_{19} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

20 Schwefel x*sin(x)											
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{best}/D	2.58	3	3.19	1540	55000	56700	57300	57600	58100	58900	ERT_{best}/D
ALPS	31	52	61	1.5	10	9.7	9.6	9.6	9.6	9.7	ALPS [17]
AMaLGaM IDEA	8.1	9.6	11	18	270	260	260	260	260	250	AMaLGaM IDEA [4]
avg NEWUOA	1.5	1.3	1.2	37	12e-1 /8e3						avg NEWUOA [31]
BayEDAcG	16	22	30	27e-1/2e3							BayEDAcG [10]
BFGS	1.6	1.9	2.4	1.1	65e-2/1e4						BFGS [30]
Cauchy EDA	110	140	140	21e-1/5e4							Cauchy EDA [24]
BIPOP-CMA-ES	4.4	5.1	5.5	3.6	1	1	1	1	1	1	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	2.9	3.2	3.3	3.3	83e-2/1e4						(1+1)-CMA-ES [2]
DASA	27	29	30	1.9	270	260	260	260	250	250	DASA [19]
DEPSO	11	14	15	1.1	68e-2/2e3						DEPSO [12]
DIRECT	7.2	17	16	14e-1/1e4							DIRECT [25]
EDA-PSO	15	44	92	7.8	3.8	3.7	3.7	3.7	3.7	3.7	EDA-PSO [6]
full NEWUOA	2.6	2.2	2.1	10	10e-1/1e4						full NEWUOA [31]
G3-PCX	5.8	6	6.1	12	85e-2/5e4						G3-PCX [26]
simple GA	130	310	360	3.2	1.8	2	2.6	25	18e-4/1e5		simple GA [22]
GLOBAL	12	11	11	2.6	11e-1/1e3						GLOBAL [23]
iAMaLGaM IDEA	4.8	5.8	6.2	38	24e-2/1e6						iAMaLGaM IDEA [4]
LSfminbnd	9.6	11	13	3.5	81e-2/1e4						LSfminbnd [28]
LSstep	200	250	300	8.3	98e-2/1e4						LSstep [28]
MA-LS-Chain	7.4	8.5	9.3	2.2	1.1	1.1	1.1	1.1	1.1	1.1	MA-LS-Chain [21]
MCS (Neum)	4.8	4.6	4.4	1	77e-2/4e3						MCS (Neum) [18]
NELDER (Han)	1.5	1.9	2.3	16	75e-2/1e5						NELDER (Han) [16]
NELDER (Doe)	1.7	2.1	2.3	5.7	81e-2/2e4						NELDER (Doe) [5]
NEWUOA	1	1	1	1.9	69e-2/1e4						NEWUOA [31]
(1+1)-ES	2.7	3	3.1	7.2	47e-2/1e6						(1+1)-ES [1]
POEMS	95	95	97	1.1	12	12	12	12	12	12	POEMS [20]
PSO	6.8	8.9	10	1.5	57e-2/1e5						PSO [7]
PSO_Bounds	9.4	29	38	2	5.1	7.1	7.1	7.1	7	7.4	PSO_Bounds [8]
Monte Carlo	210	2400	8200	29e-1/1e6							Monte Carlo [3]
Rosenbrock	3	3.1	3.1	1.7	67e-2/1e4						Rosenbrock [27]
IPOP-SEP-CMA-ES	3.4	4.6	4.8	3.1	55e-2/1e4						IPOP-SEP-CMA-ES [29]
VNS (Garcia)	11	11	11	1.2	52	50	50	49	49	51	VNS (Garcia) [11]

Table 92: 10-D, running time excess ERT/ERT_{hest} on f_{20} , in italics is given the median final function value and the median number	of
function evaluations to reach this value divided by dimension	

tion evaluations to	reach t.	ins valu	e urviue	u by un ຈ	1 Collogh	on 101 non	Le				
Afterget	10 ± 02	1 + 0.02	$1 \circ + 01$			1_{10}	10.02	10.04	10.05	10.07	Afterget
EPT /D	0.1	0.1	12	224	420	10-02	469	196	507	1120	EPT /D
	0.1	1	10	224 4 E	439	449 E 0	402	400	007	1130	ALDS [17]
ALF5	1	1	21	4.0	190	0.0	0.0	110	0	4.0	ALES [17]
AMALGAM IDEA	1	1	21	140	120	120	110	110	100	40	AMALGAM IDEA [4]
avg NEW UOA	1	1	3.2	0.2	4.7	4.1	4.0	4.5	4.1	1.9	avg NEW UOA [51]
DECS	1	1	40	21	32	196-1/263		D.C			DECE [20]
DrG5 Caushy EDA	1	1	4.0	2.9	2.0	210	200	2.0	2.0	120	Caushy EDA [24]
DIDOD CMA ES	1	1	79	340	320	310	15	290	260	120	DIDOD CMA ES [15]
(1+1) CMA ES	1	1	0.7	20	10 5 1	10	10	14	14	0.0	(1+1) CMA ES [13]
(I+I)-CMA-ES	1	1	9.7	500	0.1	0 420	4.9	200	4.0	⊿ 170	(1+1)-OMA-ES [2]
DASA	1	1	11	300	430	420	410	190	370	7.0	DASA [19]
DIRECT	1	1	11	20	19	19	10	10	24	1.0	DEFSU [12]
EDA DEO	1	1	2.3	1200	17	30	30 870	00 00	04 800	17	EDA DEO [6]
EDA-F50	1	1	00	1200	920	900	010	030	000	300	EDA-F50 [0]
C2 DCX	1	1	4.4	(.3	4.4	4.3	4.2	4	3.8	1.7	C2 DCX [26]
G5-FCA	1	1	01	15	9	0.0	0.0	0.2	1.0	3.0	G5-FCA [20]
CLOPAL	1	1	91	00 1	95	97	130	120	120	200	CLODAL [22]
AMALCAN IDEA	1	1	3.0	10	14	14	4.9	41	10	10	AMaLCaM IDEA [4]
IAMALGAM IDEA	1	1	3.2	49	44	44	40	41	40	10	IAMaLGaM IDEA [4]
LSIMIDIId	1	1	99	620	170	200	220	200	200	00	LSminbid [26]
MA IS Chain	1	1	7.5	66	42	42	41	20	290	17	MAIS Choin [21]
MCS (Neuro)	1	1	1.5	00	40	42	41	05	0.1	17	MCS (Neuro) [19]
MCS (Neum)	1	1	1	20	10	10	10	9.5	9.1	4.9	MCS (Neum) [16]
NELDER (Hall)	1	1	20	10	27	26	2 E	14 9 /	14 99	0.2	NELDER (Hall) [10]
NEWUOA	1	1	0.4	7.4	3.1	3.0	4.6	J.4	4.9	1.0	NEWLIOA [21]
(1+1) ES	1	1	2.1	20	4.0	4.7	4.0	4.4	4.2	7.1	(1+1) ES [1]
POEMS	1	1	9.0	1800	1500	1500	1400	1200	1200	580	(1+1)-155 [1]
PSO	1	1	1200	510	340	330	330	310	300	130	PSO [7]
PSO Bounds	1	1	560	1200	1500	1500	1400	1300	1300	580	PSO Bounds [8]
Monto Carle	1	1	570	6 304	200 1/106	1000	1400	1300	1000	000	Monto Carlo [3]
Bosophrock	1	1	16	18	12	19	19	11	11		Bosonbrock [27]
IPOP SEP CMA ES	1	1	5.0	14	10	10	0.0	0.5	0.1	4.0	IDOP SEP CMA ES [20]
VNS (Caraia)	1	1	10	14	20	10	5.9	69	69	4.1	VNS (Carrie) [11]
vivo (Garcia)	1	1	10	44	30	40	00	00	00	52	vivo (Garcia) [11]

Table 93: 10-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{21} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	roadii u	iio vara	aiviao			1 1					
				22 0	allagher 2	21 peaks					
Δ ftarget	1e+03	1e + 02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget
ERT_{best}/D	0.1	0.1	9.79	284	635	662	680	692	830	1040	ERT_{best}/D
ALPS	1	1	33	7	12	15	18	24	24	27	ALPS [17]
AMaLGaM IDEA	1	1	8.8	490	4900	4700	4600	4500	3800	3e3	AMaLGaM IDEA [4]
avg NEWUOA	1	1	3.6	2.6	2.1	2.1	2	2	1.7	1.4	avg NEWUOA [31]
BayEDAcG	1	1	62	31	20e-1/2e3						BayEDAcG [10]
BFGS	1	1	6.6	3.1	4.4	4.2	4.2	4.1	3.5	5.7	BFGS [30]
Cauchy EDA	1	1	450	360	20e-1/5e4						Cauchy EDA [24]
BIPOP-CMA-ES	1	1	29	58	200	190	190	180	150	120	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1	9.3	3.7	3.4	3.3	3.2	3.2	2.7	2.2	(1+1)-CMA-ES [2]
DASA	1	1	320	220	190	190	190	190	160	140	DASA [19]
DEPSO	1	1	66	47	51e-1/2e3						DEPSO [12]
DIRECT	1	1	3.5	5.1	69e-2/1e4						DIRECT [25]
EDA-PSO	1	1	1600	980	20e-1/1e5	•					EDA-PSO [6]
full NEWUOA	1	1	3.6	1.1	1.9	1.8	1.8	1.8	1.5	1.3	full NEWUOA [31]
G3-PCX	1	1	9.3	5.6	5.6	5.5	5.4	5.3	4.5	3.7	G3-PCX [26]
simple GA	1	1	130	720	20e-1/1e5						simple GA [22]
GLOBAL	1	1	4.5	1	1	1	1	1	1	1	GLOBAL [23]
iAMaLGaM IDEA	1	1	24	170	1200	1200	1100	1100	930	750	iAMaLGaM IDEA [4]
LSfminbnd	1	1	170	26	48	47	48	49	42	72	LSfminbnd [28]
LSstep	1	1	330	89	230	20e-1/1e4					LSstep [28]
MA-LS-Chain	1	1	55	510	540	520	500	490	410	330	MA-LS-Chain [21]
MCS (Neum)	1	1	1.1	3.2	6.4	6.1	6	5.9	4.9	12	MCS (Neum) [18]
NELDER (Han)	1	1	1	7.4	10	9.6	9.4	9.3	7.8	6.2	NELDER (Han) [16]
NELDER (Doe)	1	1	18	2.5	5	4.9	4.9	4.8	4	3.3	NELDER (Doe) [5]
NEWUOA	1	1	6.7	1.8	2.5	2.4	2.4	2.4	2	1.7	NEWUOA [31]
(1+1)-ES	1	1	47	17	13	13	13	13	11	8.9	(1+1)-ES [1]
POEMS	1	1	4400	1400	1e3	990	960	940	790	640	POEMS [20]
PSO	1	1	3700	1400	2200	2100	2100	2e3	1700	1400	PSO [7]
PSO_Bounds	1	1	740	1400	2200	2100	2100	2100	1700	1400	PSO_Bounds [8]
Monte Carlo	1	1	2500	20e-1/1e6							Monte Carlo [3]
Rosenbrock	1	1	35	5	5.4	5.3	5.3	5.4	4.7	4.1	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1	22	61	220	210	210	200	170	140	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1	39	160	1100	1400	1500	1500	1200	980	VNS (Garcia) [11]

Table 94: 10-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{22} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

function evaluation	s to rea	ch this	value di	vided by dif	23 K	atsuuras					
Aftarget	1e + 03	1e + 02	$1e \pm 01$	$1e \pm 00$	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Aftarget
ERT_{host}/D	0.1	0.1	0.28	91.5	1640	18400	20400	20600	20900	21400	ERT_{host}/D
ALPS	1	1	1.7	42	1e3	14e-2/5e5			ī		ALPS [17]
AMaLGaM IDEA	1	1	1.6	10	1	1	1	1	1	1	AMaLGaM IDEA [4]
avg NEWUOA	1	1	11	2.6	21e-2/1e4						avg NEWUOA [31]
BayEDAcG	1	1	1.3	16e-1/2e3							BayEDAcG [10]
BFGS	1	1	17	130	11e-1/5e3						BFGS [30]
Cauchy EDA	1	1	2.3	1700	11e-1/5e4						Cauchy EDA [24]
BIPOP-CMA-ES	1	1	2	21	2.7	1.3	1.2	1.2	1.2	1.2	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1	3.4	2.9	22e-2/1e4						(1+1)-CMA-ES [2]
DASA	1	1	5	28	4300	15e-2/1e6					DASA [19]
DEPSO	1	1	1.7	18e-1/2e3		•					DEPSO [12]
DIRECT	1	1	2.1	2.1	65e-2/1e4						DIRECT [25]
EDA-PSO	1	1	1.7	590	87e-2/1e5						EDA-PSO [6]
full NEWUOA	1	1	13	2.9	44	19e-2/1e4					full NEWUOA [31]
G3-PCX	1	1	1.8	4.9	98	19e-2/4e4					G3-PCX [26]
simple GA	1	1	1.4	390	85e-2/1e5						simple GA [22]
GLOBAL	1	1	2.1	1	32e-2/700			•			GLOBAL [23]
iAMaLGaM IDEA	1	1	1.8	5.7	3.6	1.1	1	1	1	1	iAMaLGaM IDEA [4]
LSfminbnd	1	1	2.1	26	66e-2/1e4						LSfminbnd [28]
LSstep	1	1	1.2	31	51e-2/1e4						LSstep [28]
MA-LS-Chain	1	1	2	2.3	17	38	35	44e-3/5e4			MA-LS-Chain [21]
MCS (Neum)	1	1	3.4	15	56e-2/4e3						MCS (Neum) [18]
NELDER (Han)	1	1	1	5.7	40	80	59e-3/1e5				NELDER (Han) [16]
NELDER (Doe)	1	1	1.7	1.4	11	97e-3/2e4		•			NELDER (Doe) [5]
NEWUOA	1	1	7.5	3.6	34e-2/7e3			•			NEWUOA [31]
(1+1)-ES	1	1	4.4	7.6	2900	14e-2/1e6					(1+1)-ES [1]
POEMS	1	1	15	31	19	36	69	63e-3/1e5			POEMS [20]
PSO	1	1	1.7	91	42e-2/1e5	•		•			PSO [7]
PSO_Bounds	1	1	1.5	130	67e-2/1e5						PSO_Bounds [8]
Monte Carlo	1	1	1.6	530	61e-2/1e6						Monte Carlo [3]
Rosenbrock	1	1	2.1	2.2	32e-2/5e3						Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1	2.4	17	12	11e-2/1e4					IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1	2.6	18	34	140	420	680	670	650	VNS (Garcia) [11]

Table 95: 10-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{23} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

24 Lunacek bi-Rastrigin											
Δ ftarget	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT _{best} /D	0.1	6.64	9880	1.04e5	7.47e6	7.48e6	7.48e6	7.48e6	7.48e6	7.48e6	ERT _{best} /D
ALPS	1	24	10	44e-1/5e5							ALPS [17]
AMaLGaM IDEA	1	5.5	18	8.3	78e-2/1e6						AMaLGaM IDÉA [4]
avg NEWUOA	1	1.4	21e + 0/8e3								avg NEWUOA [31]
BayEDAcG	1	19	37e + 0/2e3								BayEDAcG [10]
BFGS	1	350	81e + 0/4e3								BFGS [30]
Cauchy EDA	1	51	27e + 0/5e4								Cauchy EDA [24]
BIPOP-CMA-ES	1	2.2	2.7	1	1	1	1	1	1	1	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	8.6	14	20e + 0/1e4							(1+1)-CMA-ES [2]
DASA	1	1300	31e + 0/1e6								DASA [19]
DEPSO	1	6.8	38e + 0/2e3								DEPSO [12]
DIRECT	1	5.9	19e + 0/1e4								DIRECT [25]
EDA-PSO	1	56	23e + 0/1e5			•		•	•		EDA-PSO [6]
full NEWUOA	1	2.6	16e + 0/1e4								full NEWUOA [31]
G3-PCX	1	16	31e + 0/5e4								G3-PCX [26]
simple GA	1	120	14e + 0/1e5								simple GA [22]
GLOBAL	1	7.2	62e + 0/1e3					•			GLOBAL [23]
iAMaLGaM IDEA	1	4.2	4.2	4.2	66e-2/1e6						iAMaLGaM IDEA [4]
LSfminbnd	1	20	33e + 0/1e4								LSfminbnd [28]
LSstep	3	170	49e + 0/1e4								LSstep [28]
MA-LS-Chain	1	5.7	11e + 0/5e4								MA-LS-Chain [21]
MCS (Neum)	1	15	30e + 0/4e3								MCS (Neum) [18]
NELDER (Han)	1	8.2	22	11e + 0/1e5							NELDER (Han) [16]
NELDER (Doe)	1	4.7	2.6	96e-1/2e4							NELDER (Doe) [5]
NEWUOA	1	1	26e + 0/7e3								NEWUOA [31]
(1+1)-ES	1	140	740	17e + 0/1e6							(1+1)-ES [1]
POEMS	1	48	140	19e + 0/1e5							POEMS [20]
PSO	1	8.1	140	20e + 0/1e5							PSO [7]
PSO_Bounds	1	22	140	22e + 0/1e5							PSO_Bounds [8]
Monte Carlo	1	820	60e + 0/1e6								Monte Carlo [3]
Rosenbrock	1	1e4	12e + 1/1e4								Rosenbrock [27]
IPOP-SEP-CMA-ES	1	2.2	1	91e-1/1e4							IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	4.8	3.7	21e-1/8e6							VNS (Garcia) [11]

Table 96: 10-D, running time excess ERT/ERT_{best} on f_{24} , in italics is given the median final function value and the median number of
function evaluations to reach this value divided by dimension
function evaluations to reach this value divided by dimension

1 Sphere											
Δ ftarget	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT _{best} /D	0.05	0.28	2.15	2.15	2.15	2.15	2.15	2.15	2.15	2.15	ERT _{best} /D
ALPS	1	64	150	320	520	710	920	1100	1400	1800	ALPS [17]
AMaLGaM IDEA	1	58	55	130	200	260	320	390	440	550	AMaLGaM IDEA [4]
avg NEWUOA	1	18	2.3	2.3	2.3	2.3	2.3	2.3	2.3	2.3	avg NEWUOA [31]
BayEDAcG	1	49	110	200	310	410	500	610	710	1e3	BayEDAcG [10]
BFGS	1	7.4	1	1	1	1	1	1	1	1	BFGS [30]
Cauchy EDA	1	840	730	1600	2500	3500	4300	5200	6100	7800	Cauchy EDA [24]
BIPOP-CMA-ES	1	9.2	7.9	14	20	26	33	39	45	57	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	12	5.4	9.2	13	17	21	25	29	37	(1+1)-CMA-ES [2]
DASA	1	60	26	45	66	86	120	150	200	300	DASA [19]
DEPSO	1	31	30	81	190	330	560	810	1400	44e-7/2e3	DEPSO [12]
DIRECT	1	8.6	48	110	220	360	490	680	870	1400	DIRECT [25]
EDA-PSO	1	19	450	1100	1700	2300	2900	3600	4200	5400	EDA-PSO [6]
full NEWUOA	1	41	5.4	5.4	5.5	5.5	5.5	5.5	5.5	5.5	full NEWUOA [31]
G3-PCX	1	31	8	13	18	23	27	32	37	48	G3-PCX [26]
simple GA	1	130	880	1900	3200	1.2e4	3.1e4	2e5	6.7e5	74e-5/1e5	simple GA [22]
GLOBAL	1	37	8	8	8	8	8	8	8	8	GLOBAL [23]
iAMaLGaM IDEA	1	13	27	57	88	120	150	180	210	270	iAMaLGaM IDEA [4]
LSfminbnd	1	43	9.3	10	10	10	10	10	10	10	LSfminbnd [28]
LSstep	1	850	160	170	180	180	180	180	180	180	LSstep [28]
MA-LS-Chain	1	19	21	51	78	100	120	140	160	200	MA-LS-Chain [21]
MCS (Neum)	1	1	2.4	6.4	6.8	7	7	7	7	7	MCS (Neum) [18]
NELDER (Han)	1	9.1	5.2	12	19	27	32	36	40	49	NELDER (Han) [16]
NELDER (Doe)	1	6.8	3.3	6.7	11	16	21	27	32	40	NELDER (Doe) [5]
NEWUOA	1	7.5	1	1	1	1	1	1	1	1	NEWUOA [31]
(1+1)-ES	1	11	4.9	8.1	11	15	18	22	25	31	(1+1)-ES [1]
POEMS	1	830	180	400	870	1400	1800	2300	2800	3800	POEMS [20]
PSO	1	16	22	3400	3400	3500	3600	3600	3700	3800	PSO [7]
PSO_Bounds	1	19	120	1500	2100	2800	3300	3800	4500	1.6e4	PSO_Bounds [8]
Monte Carlo	1	170	29e + 0/1e6								Monte Carlo [3]
Rosenbrock	1	19	3.8	5.8	7.2	9.1	11	12	14	17	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	13	7.1	12	18	23	29	34	39	50	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	28	10	17	23	29	36	41	48	60	VNS (Garcia) [11]

Table 97: 20-D, running time excess ERT/ERT _{bost} on f_1 , in	italics is given the median final function value and the median number of
function evaluations to reach this value divided by dimension	

Table 98: 20-D, run function evaluation	nning time o s to reach t	excess E his value	RT/ER e divideo	T _{best} o d by din	n f_2 , in ital nension	lics is given	the mediar	n final funct	ion value a	nd the med	ian number of
					2 Elli	osoid sepa	rable				Ti:
Δ ftarget	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget \Im
ERT_{hest}/D	18.6	19	19.2	19.3	19.3	19.4	19.5	19.5	19.6	19.7	ERT _{best} /D
ALPS	45	66	88	110	140	160	190	220	260	370	ALPS [17]
AMaLGaM IDEA	22	29	35	43	50	56	62	68	76	88	AMaLGaM IDEA [4]
avg NEWUOA	3.5	10	21	43	63	89	120	140	160	200	avg NEWUOA [31]
BayEDAcG	31	42	54	64	76	94	100	34e-5/2e3			BayEDAcG [10]
BFGS	9.1	15	20	24	26	27	27	27	28	28	BFGS [30]
Cauchy EDA	190	310	410	510	610	710	800	900	990	1200	Cauchy EDA [24]
BIPOP-CMA-ES	15	26	35	40	44	45	47	47	48	50	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	14	22	30	37	39	41	41	42	43	44	(1+1)-CMA-ES [2]
DASA	5.6	7.8	10	14	18	23	28	34	39	49	DASA [19]
DEPSO	12	23	42	66	110	500	39e-3 /2e3				DEPSO [12]
DIRECT	38	53	130	470	490	510	540	1200	14e-1/5e3		DIRECT [25]
EDA-PSO	200	270	330	400	470	540	600	670	740	880	EDA-PSO [6]
full NEWUOA	23	94	450	3800	47e-1/1e4						full NEWUOA [31]
G3-PCX	15	47	130	210	320	420	550	650	760	990	G3-PCX [26]
simple GA	300	460	3200	6800	7.3e4	29e-1/1e5					simple GA [22]
GLOBAL	8.4	13	18	23	26	30	33	49	51	63	GLOBAL [23]
iAMaLGaM IDEA	11	17	22	27	30	33	36	40	43	49	iAMaLGaM IDEA [4]
LSfminbnd	1	1	1	1	1	1	1	1	1	1	LSfminbnd [28]
LSstep	17	17	17	17	17	17	17	17	17	17	LSstep [28]
MA-LS-Chain	7.6	11	15	19	23	27	32	36	43	76	MA-LS-Chain [21]
MCS (Neum)	1	2.2	5.4	14	21	41	43	45	45	30e-8/4e3	MCS (Neum) [18]
NELDER (Han)	4.3	6	7	7.8	8.6	9.2	9.7	10	11	12	NELDER (Han) [16]
NELDER (Doe)	5.3	8.5	13	17	19	23	28	32	36	48	NELDER (Doe) [5]
NEWUOA	1.9	6.8	18	42	71	92	130	150	170	220	NEWUOA [31]
(1+1)-ES	270	1800	6900	1.6e4	2.6e4	3.8e4	7.4e4	1.8e5	3.7e5	59e-5/1e6	(1+1)-ES [1]
POEMS	150	190	250	300	340	410	450	500	560	660	POEMS [20]
PSO	16	1900	4600	4600	4600	4600	4500	4500	4500	4500	PSO [7]
PSO_Bounds	120	230	360	530	840	1400	1800	2100	2300	2600	PSO_Bounds [8]
Monte Carlo	12e+4/1e6										Monte Carlo [3]
Rosenbrock	1	1.2	1.4	1.6	5.8	18	29	66	73	73	Rosenbrock [27]
IPOP-SEP-CMA-ES	4.8	6.2	7.5	8.3	9.1	9.7	10	11	11	13	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	35	57	72	82	88	95	97	98	98	99	VNS (Garcia) [11]

3 Rastrigin separable											
Δ ftarget	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{hest}/D	0.05	12.7	253	381	382	382	382	382	382	383	ERT_{best}/D
ALPS	19	54	50	190	230	240	270	310	400	3200	ALPS [17]
AMaLGaM IDEA	17	43	27	40e-1/1e6							AMaLGaM IDEA [4]
avg NEWUOA	88	1e3	97e+0/1e4								avg NEWUOA [31]
BayEDAcG	15	85	73e + 0/2e3								BayEDAcG [10]
BFGS	570	28e + 1/6e3									BFGS [30]
Cauchy EDA	2900	450	69e + 0/5e4								Cauchy EDA [24]
BIPOP-CMA-ES	25	6.7	12	40e-1/3e5							BIPOP-CMA-ES [15]
(1+1)-CMA-ES	37	840	92e + 0/1e4	•							(1+1)-CMA-ES [2]
DASA	210	5.9	1	8.3	35	35	35	35	36	36	DASA [19]
DEPSO	42	130	84e + 0/2e3								DEPSO [12]
DIRECT	1	28	43e + 0/5e3								DIRECT [25]
EDA-PSO	22	150	44	70e-1/1e5							EDA-PSO [6]
full NEWUOA	180	650	88e+0/1e4								full NEWUOA [31]
G3-PCX	24	1.2e4	13e + 1/5e4								G3-PCX [26]
simple GA	26	190	29	3700	21e-1/1e5						simple GA [22]
GLOBAL	19	1400	15e + 1/2e3								GLOBAL [23]
iAMaLGaM IDEA	24	19	38	1.8e4	20e-1/1e6						iAMaLGaM IDEA [4]
LSfminbnd	190	1.3	19e + 0/6e3								LSfminbnd [28]
LSstep	4e3	27	1.5	1	1	1	1	1	1	1	LSstep [28]
MA-LS-Chain	20	12	7	95	160	160	160	160	160	160	MA-LS-Chain [21]
MCS (Neum)	1	1	28	13e + 0/4e3							MCS (Neum) [18]
NELDER (Han)	42	260	81e + 0/1e4	•							NELDER (Han) [16]
NELDER (Doe)	24	71	47e + 0/2e4								NELDER (Doe) [5]
NEWUOA	41	7500	13e + 1/6e3								NEWUOA [31]
(1+1)-ES	360	2.3e4	81e + 0/1e6								(1+1)-ES [1]
POEMS	4e3	43	9.6	69	140	140	150	150	150	160	POEMS [20]
PSO	19	21	21e + 0/1e5								PSO [7]
PSO_Bounds	28	330	120	190	360	360	360	380	400	430	PSO_Bounds [8]
Monte Carlo	32	26e + 1/1e6									Monte Carlo [3]
Rosenbrock	560	23e + 1/7e3									Rosenbrock [27]
IPOP-SEP-CMA-ES	28	5.2	10	60e-1/1e4							IPOP-SEP-CMA-ES [29]
VNS (Garcia)	20	8.1	8.3	340	490	520	560	620	630	630	VNS (Garcia) [11]

Table 99: 20-D, running time excess ERT/ERT_{best} on f_3 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

4 Skew Rastrigin-Bueche separable													
Δ ftarget	$\Delta \text{ftarget} \qquad 1e+03 \qquad 1e+02 \qquad 1e+01 \qquad 1e+00 \qquad 1e-01 \qquad 1e-02 \qquad 1e-03 \qquad 1e-04 1e-05 1e-07 \qquad \Delta \text{ftarget}$												
ERT _{best} /D	0.05	37.3	236	381	383	384	385	386	388	7050	ERT _{best} /D		
ALPS	92	29	150	9800	30e-1/2e5						ALPS [17]		
AMaLGaM IDEA	79	20	14e + 0/1e6								AMaLGaM IDEA [4]		
avg NEWUOA	110	1400	12e+1/2e4								avg NEWUOA [31]		
BayEDAcG	83	40	69e + 0/2e3								BayEDAcG [10]		
BFGS	1700	40e+1/8e3									BFGS [30]		
Cauchy EDA	5100	4300	11e + 1/5e4								Cauchy EDA [24]		
BIPOP-CMA-ES	37	2.4	12e + 0/3e5								BIPOP-CMA-ES [15]		
(1+1)-CMA-ES	46	14e + 1/1e4									(1+1)-CMA-ES [2]		
DASA	290	2.1	1	130	1700	1700	1700	1700	1700	91	DASA [19]		
DEPSO	120	120	10e + 1/2e3								DEPSO [12]		
DIRECT	1	11	88e+0/5e3								DIRECT [25]		
EDA-PSO	20	56	6e3	15e + 0/1e5							EDA-PSO [6]		
full NEWUOA	270	4e3	13e+1/1e4								full NEWUOA [31]		
G3-PCX	79	19e + 1/5e4									G3-PCX [26]		
simple GA	100	80	65	3800	34e-1/1e5						simple GA [22]		
GLOBAL	160	20e + 1/4e3									GLOBAL [23]		
iAMaLGaM IDEA	61	7.1	13e+0/1e6								iAMaLGaM IDEA [4]		
LSfminbnd	280	1.2	49e+0/7e3								LSfminbnd [28]		
LSstep	4400	9.5	1.6	1	1	1	1	1	1	1	LSstep [28]		
MA-LS-Chain	60	6.2	53	30e-1/1e5							MA-LS-Chain [21]		
MCS (Neum)	1	1	21e+0/4e3								MCS (Neum) [18]		
NELDER (Han)	40	13e + 1/1e4									NELDER (Han) [16]		
NELDER (Doe)	35	1600	11e+1/2e4								NELDER (Doe) [5]		
NEWUOA	55	4300	17e + 1/1e4								NEWUOA [31]		
(1+1)-ES	82	3.8e5	13e + 1/1e6								(1+1)-ES [1]		
POEMS	4e3	18	13	140	220	240	250	250	250	14	POEMS [20]		
PSO	44	8.6	5900	23e + 0/1e5							PSO [7]		
PSO_Bounds	66	130	190	290	300	360	360	370	380	21	PSO_Bounds [8]		
Monte Carlo	130	33e + 1/1e6									Monte Carlo [3]		
Rosenbrock	650	20e + 1/8e3									Rosenbrock [27]		
IPOP-SEP-CMA-ES	55	2.5	14e + 0/1e4								IPOP-SEP-CMA-ES [29]		
VNS (Garcia)	110	3.2	27	2.8e4	1.3e5	1.3e5	20e-1/4e6				VNS (Garcia) [11]		

Table 100: 20-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_4 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

Table 101: 20-I	D, running tir	ne exces	s ERT/EI	RT _{best} on	f_5 , in	italics i	is given	the n	nedian f	inal fu	nction	value and the median number of
function evalua	function evaluations to reach this value divided by dimension											
	5 Linear slope											
4	Δ ftarget	1e + 03	1e + 02	1e + 01	1e+00	1e-01	$\overline{1}e-02$	1e-03	1e-04	1e-05	1e-07	Δ ftarget

Δ ftarget	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget
ERT_{best}/D	0.05	1.83	2.03	2.03	2.03	2.03	2.03	2.03	2.03	2.03	ERT_{best}/D
ALPS	1	51	160	210	250	280	300	310	320	330	ALPS [17]
AMaLGaM IDEA	1	34	75	80	80	80	80	80	80	80	AMaLGaM IDEA [4]
avg NEWUOA	1	2.7	2.7	3.2	3.3	3.3	3.3	3.3	3.3	3.3	avg NEWUOA [31]
BayEDAcG	1	67	150	200	200	200	210	210	210	210	BayEDAcG [10]
BFGS	1	1.4	2.4	2.7	2.8	2.8	2.8	2.8	2.8	2.8	BFGS [30]
Cauchy EDA	1	110	160	170	170	170	170	170	170	170	Cauchy EDA [24]
BIPOP-CMA-ES	1	2.7	5.1	6.2	6.3	6.3	6.3	6.3	6.3	6.3	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1.6	3.1	3.6	3.7	3.7	3.7	3.7	3.7	3.7	(1+1)-CMA-ES [2]
DASA	1	14	24	29	34	38	43	47	52	64	DASA [19]
DEPSO	1	16	39	46	48	48	48	48	48	48	DEPSO [12]
DIRECT	1	62	180	220	230	230	230	230	230	230	DIRECT [25]
EDA-PSO	1	5.2	27	34	37	39	39	39	39	39	EDA-PSO [6]
full NEWUOA	1	6.4	6.2	6.5	6.6	6.6	6.6	6.6	6.6	6.6	full NEWUOA [31]
G3-PCX	1	7.5	19	25	26	27	27	27	27	27	G3-PCX [26]
simple GA	1	570	2200	4600	7500	1.1e4	1.4e4	1.8e4	2.2e4	2.3e5	simple GA [22]
GLOBAL	1	9.5	9.9	11	11	11	11	11	11	11	GLOBAL [23]
iAMaLGaM IDEA	1	4.4	9.8	11	11	11	11	11	11	11	iAMaLGaM IDEA [4]
LSfminbnd	1	14	16	16	16	16	16	16	16	16	LSfminbnd [28]
LSstep	1	150	180	190	190	190	190	190	190	190	LSstep [28]
MA-LS-Chain	1	22	41	44	46	46	46	46	46	46	MA-LS-Chain [21]
MCS (Neum)	1	1	1	1	1	1	1	1	1	1	MCS (Neum) [18]
NELDER (Han)	1	3.8	7.4	8.8	9.2	9.2	9.2	9.2	9.2	9.2	NELDER (Han) [16]
NELDER (Doe)	1	2.6	5.2	6.2	6.3	6.4	6.4	6.4	6.4	6.4	NELDER (Doe) [5]
NEWUOA	1	1.2	1.2	1.5	1.6	1.6	1.6	1.6	1.6	1.6	NEWUOA [31]
(1+1)-ES	1	1.6	3.1	3.5	3.6	3.6	3.6	3.6	3.6	3.6	(1+1)-ES [1]
POEMS	1	180	260	310	330	350	350	350	350	350	POEMS [20]
PSO	1	4.7	4.3e4	4.3e4	4.3e4	4.3e4	4.3e4	4.3e4	4.3e4	4.3e4	PSO [7]
PSO_Bounds	1	4.5	160	160	160	160	160	160	160	160	PSO_Bounds [8]
Monte Carlo	1	2.5e6	11e+1/1e6								Monte Carlo [3]
Rosenbrock	1	3.8	4.2	4.3	4.3	4.3	4.3	4.3	4.3	4.3	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	2.9	6.2	7.3	7.7	7.7	7.7	7.7	7.7	7.7	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	4.9	6.8	7.6	7.8	7.8	7.8	7.8	7.8	7.8	VNS (Garcia) [11]

RT	
n°	
0383	

Table 102: 20-D, ru	unning t	time excess I	ERT/ERT _{be}	est on f_6 , in	italics is given	ven the med	lian final fu	nction value	e and the m	edian numb	per of Og
function evaluation	s to rea	ch this value	e divided by	dimension							pa
					6 Attract	tive sector	•				ris
Δ ftarget	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta \mathrm{ftarget}$
ERT _{best} /D	4.03	26	64.7	87.2	123	152	184	219	248	309	$\operatorname{ERT}_{\operatorname{hest}} / \operatorname{D}$
ALPS	59	25	34	54	64	78	100	150	370	14e-7/2e5	ALPS [17]
AMaLGaM IDEA	26	22	19	22	21	22	22	21	22	22	AMaLGaM IDEA [4]
avg NEWUOA	2.3	1.1	1	1	1	1	1	1	1	1	avg NEWUOA [31]
BayEDAcG	46	41	60e + 0/2e3								BayEDAcG [10]
BFGS	2.2	2.7	3.6	4.7	4.7	4.9	5	4.8	4.9	61	BFGS [30]
Cauchy EDA	6200	1500	1e3	1700	17e-1/5e4			•			Cauchy EDA [24]
BIPOP-CMA-ES	2.9	2.2	1.5	1.7	1.6	1.6	1.6	1.5	1.6	1.6	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1.9	4.5	13	180	1200	13e-1/1e4		•	•		(1+1)-CMA-ES [2]
DASA	12	6.8	9.9	19	25	33	49	58	63	74	DASA [19]
DEPSO	11	7.5	12	64	13e-1/2e3			•			DEPSO [12]
DIRECT	18	31	40e + 0/5e3								DIRECT [25]
EDA-PSO	27	46	40	45	44	44	44	44	44	44	EDA-PSO [6]
full NEWUOA	5	1.9	1.5	1.4	1.4	1.4	1.4	1.4	1.4	1.4	full NEWUOA [31]
G3-PCX	4.1	1.4	1.4	2	2.1	2.1	2.2	2.2	2.3	2.4	G3-PCX [26]
simple GA	320	130	2e3	11e + 0/1e5							simple GA [22]
GLOBAL	5	2.9	3.6	4.9	8.5	42e-3/2e3					GLOBAL [23]
iAMaLGaM IDEA	5.1	5.6	5.4	6.8	7.1	7.7	7.8	7.7	8	8.3	iAMaLGaM IDEA [4]
LSfminbnd	9	31	160	760	1100	960	72e-1/1e4				LSfminbnd [28]
LSstep	140	260	2300	59e + 0/1e4							LSstep [28]
MA-LS-Chain	11	4.9	7.5	8.9	8	7.7	7.2	6.7	6.5	6	MA-LS-Chain [21]
MCS (Neum)	1.8	33	42e + 0/4e3								MCS (Neum) [18]
NELDER (Han)	2.2	2.4	2.7	3.3	3.2	3.5	3.5	3.5	4	7.4	NELDER (Han) [16]
NELDER (Doe)	1.5	2.3	9.1	20	28	65	110	430	46e-5/2e4		NELDER (Doe) $[5]$
NEWUOA	1	1	1	1.3	1.4	1.5	1.6	1.6	1.7	1.7	NEWUOA [31]
(1+1)-ES	2	2.2	2.1	2.8	3.9	5.2	6.1	6.5	6.4	6.7	(1+1)-ES [1]
POEMS	89	26	31	37	36	36	36	35	36	37	POEMS [20]
PSO	6.4	280	1100	1400	980	820	710	620	570	790	PSO [7]
PSO_Bounds	9.5	45	120	150	140	140	140	130	160	220	PSO_Bounds [8]
Monte Carlo	2.4e5	48e+1/1e6									Monte Carlo [3]
Rosenbrock	2.1	3.9	31	76	210	230	810	21e-2/1e4			Rosenbrock [27]
IPOP-SEP-CMA-ES	3.2	2.1	1.7	1.9	1.9	1.9	1.9	1.9	2	2	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	5	2.8	1.9	1.9	1.7	1.7	1.7	1.6	1.6	1.6	VNS (Garcia) [11]

Table 102: 20-D, running time excess ERT/ERT_{best} on f_6 , in italics is given the median final function value and the median number of function exclusions to much this exclusion divided by dided by divi
Table 103: 20-D, r function evaluation	Table 103: 20-D, running time excess ERT/ERT_{best} on f_7 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension													
7 Step-ellipsoid														
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$			
ERT_{best}/D	0.53	7.59	67.5	214	475	826	826	826	826	848	ERT _{best} /D			
ALPS	5	26	30	850	930	48e-2/2e5					ALPS [17]			
AMaLGaM IDEA	3	10	3.6	2.1	1.3	1	1	1	1	1	AMaLGaM IDEA [4]			

7 Step-ellipsoid												
Δ ftarget	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$	
ERT_{best}/D	0.53	7.59	67.5	214	475	826	826	826	826	848	ERT_{best}/D	
 ALPS	5	26	30	850	930	48e-2/2e5					ALPS [17]	
AMaLGaM IDEA	3	10	3.6	2.1	1.3	1	1	1	1	1	AMaLGaM IDEA [4]	
avg NEWUOA	7.1	1.4	100	51e-1/2e4							avg NEWUOA [31]	
BayEDAcG	4.3	31	57	11e + 0/2e3							BayEDAcG [10]	
BFGS	69	67e + 1/100									BFGS [30]	
Cauchy EDA	130	130	44	29	18	14	14	14	14	14	Cauchy EDA [24]	
BIPOP-CMA-ES	2.5	2.8	1	4.9	3.5	2.2	2.2	2.2	2.2	2.1	BIPOP-CMA-ES [15]	
(1+1)-CMA-ES	1.6	16	30	54	300	92e-2/1e4					(1+1)-CMA-ES [2]	
DASA	16	49	1.8e4	13e + 0/4e5							DASA [19]	
DEPSO	2.7	7.9	18	77e-1 /2e3							DEPSO [12]	

1.1	1.1	100	0101/204	•	•	•	•	•	•	
4.3	31	57	11e + 0/2e3	•	•					BayEDAcG [10]
69	67e + 1/100									BFGS [30]
130	130	44	29	18	14	14	14	14	14	Cauchy EDA [24]
2.5	2.8	1	4.9	3.5	2.2	2.2	2.2	2.2	2.1	BIPOP-CMA-ES [15]
1.6	16	30	54	300	92e-2/1e4					(1+1)-CMA-ES [2]
16	49	1.8e4	13e + 0/4e5							DASA [19]
2.7	7.9	18	77e-1/2e3							DEPSO [12]
3.5	7	15e + 0/6e3								DIRECT [25]
2.5	65	26	950	15e-1/1e5						EDA-PSO [6]
14	1.9	4.6	700	27e-1/1e4						full NEWUOA [31]
4.7	2.8	760	12e + 0/1e4							G3-PCX [26]
5.8	180	77	32e-1/1e5							simple GA [22]
4.6	2.9	22e+0/700	•							GLOBAL [23]
2	5.8	1.7	1	1	1.3	1.3	1.3	1.3	1.3	iAMaLGaM IDEA [4]
23	21	1e3	15e + 0/1e4							LSfminbnd [28]
230	180	2200	29e + 0/1e4							LSstep [28]
3.4	5.4	4.3	120	360	390	390	390	390	380	MA-LS-Chain [21]
1	57	38e + 0/4e3								MCS (Neum) [18]
4.5	4.6	2200	16e + 0/1e4							NELDER (Han) [16]
2.5	1	370	97e-1/2e4	•	•					NELDER (Doe) [5]
3.6	43	18e + 0/2e4	•							NEWUOA [31]
3.1	1100	27e + 0/1e6								(1+1)-ES [1]
440	55	21	2e3	3100	12e-1/1e5					POEMS [20]
2.5	4.8	430	62e-1/1e5							PSO [7]
3.3	26	9700	22e + 0/1e5							PSO_Bounds [8]
3.2	2.1e5	10e + 1/1e6								Monte Carlo [3]
500	38e + 1/3e3	•								Rosenbrock [27]
3.4	2.8	2.3	4	2.4	1.5	1.5	1.5	1.5	1.5	IPOP-SEP-CMA-ES [29]
1.1	3.7	5.4	78	72	2400	2400	2400	2400	2300	VNS (Garcia) [11]

2400

2400

2400

2400

2300

VNS (Garcia) [11]

DIRECT EDA-PSO full NEWUOA G3-PCX simple GA GLOBAL iAMaLGaM IDEA

LSfminbnd LSstep MA-LS-Chain MCS (Neum)

NELDER (Han) NELDER (Doe) NEWUOA (1+1)-ESPOEMS PSOPSO_Bounds Monte Carlo Rosenbrock IPOP-SEP-CMA-ES

VNS (Garcia)

1.1

3.7

5.4

ancesion evaluations to reach this value divided by dimension													
8 Rosenbrock original													
Δ ftarget	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget		
ERT_{best}/D	5.52	21	97.9	187	202	207	211	215	219	222	ERT_{best}/D		
ALPS	70	51	100	460	600	740	1e3	1200	3100	26e-6/2e5	ALPS [17]		
AMaLGaM IDEA	25	16	20	18	19	20	20	21	21	22	AMaLGaM IDÉA [4]		
avg NEWUOA	2	1.6	1	1	1	1	1	1	1	1	avg NEWUOA [31]		
BayEDAcG	55	35	48e+0/2e3								BayEDAcG [10]		
BFGS	1.9	2	1.9	1.3	1.2	1.2	1.2	1.2	1.2	1.2	BFGS [30]		
Cauchy EDA	360	200	200	180	210	250	260	290	360	550	Cauchy EDA [24]		
BIPOP-CMA-ES	4	2.4	4.2	4.2	4.3	4.5	4.5	4.6	4.6	4.7	BIPOP-CMA-ES [15]		
(1+1)-CMA-ES	2.7	1.8	3.9	6.5	6.6	6.6	6.6	6.7	6.6	6.7	(1+1)-CMA-ES [2]		
DASA	15	26	34	57	120	200	280	350	420	550	DASA [19]		
DEPSO	16	16	17e+0/2e3								DEPSO [12]		
DIRECT	25	82	64e + 0/5e3								DIRECT [25]		
EDA-PSO	220	110	190	220	260	330	410	17e-5/1e5			EDA-PSO [6]		
full NEWUOA	3.4	2.6	1.4	1.6	1.6	1.7	1.7	1.7	1.7	1.7	full NEWUOA [31]		
G3-PCX	3.9	2	2.7	5.6	5.5	5.5	5.5	5.5	5.5	5.7	G3-PCX [26]		
simple GA	480	250	17e + 0/1e5								simple GA [22]		
GLOBAL	4.1	2.4	1.7	1.3	1.2	1.2	1.2	1.2	1.2	1.2	GLOBAL [23]		
iAMaLGaM IDEA	13	6.4	8.6	9.2	9.5	9.8	10	10	10	11	iAMaLGaM IDEA [4]		
LSfminbnd	7.1	17	9.6	120	710	720	40e-1/1e4				LSfminbnd [28]		
LSstep	150	71	25	130	220	350	12e-1/1e4				LSstep [28]		
MA-LS-Chain	12	10	14	13	13	13	14	13	13	14	MA-LS-Chain [21]		
MCS (Neum)	1.4	1.2	1.6	1.8	1.8	1.8	1.8	1.8	1.8	1.8	MCS (Neum) [18]		
NELDER (Han)	3.2	2.9	3.4	3.9	4.1	4.5	4.9	5.1	5.3	5.6	NELDER (Han) [16]		
NELDER (Doe)	3.2	3	2.9	4.9	5.5	6	6.5	7.2	7.7	9.2	NELDER (Doe) [5]		
NEWUOA	1	1	1	1	1	1	1	1	1	1	NEWUOA [31]		
(1+1)-ES	2.5	11	13	120	120	140	160	180	200	240	(1+1)-ES [1]		
POEMS	100	84	590	7600	74e-1/1e5						POEMS [20]		
PSO	15	19	93	320	350	410	470	580	890	3300	PSO [7]		
PSO_Bounds	88	160	540	450	1800	7200	15e-2/1e5				PSO_Bounds [8]		
Monte Carlo	80e+2/1e6				•						Monte Carlo [3]		
Rosenbrock	2	1.1	4	25	28	35	42	55	62	670	Rosenbrock [27]		
IPOP-SEP-CMA-ES	3.5	1.7	5.6	5.6	5.7	5.7	5.8	5.8	5.8	5.8	IPOP-SEP-CMA-ES [29]		
VNS (Garcia)	6	3.1	6	6.3	6.3	6.4	6.4	6.4	6.4	6.4	VNS (Garcia) [11]		

Table 104: 20-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_8 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

9 Rosenbrock rotated											
Δ ftarget	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{hest}/D	0.05	17.8	85.8	155	164	169	173	176	180	186	ERT_{hest}/D
ALPS	4800	37	350	48e-1/2e5							ALPS [17]
AMaLGaM IDEA	2e3	11	22	22	23	24	24	25	25	25	AMaLGaM IDEA [4]
avg NEWUOA	230	1.5	1	1.2	1.2	1.3	1.3	1.2	1.2	1.2	avg NEWUOA [31]
BayEDAcG	4800	27	18e + 0/2e3								BayEDAcG [10]
BFGS	210	1.9	2.2	2.2	2.1	2.1	2	2	2	1.9	BFGS [30]
Cauchy EDA	3.3e4	220	190	270	290	300	310	340	470	630	Cauchy EDA [24]
BIPOP-CMA-ES	390	2.6	4.7	5.7	6	6.1	6.1	6.1	6.1	6.1	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	260	2.4	4.5	6.7	7	7	7	7	7	6.9	(1+1)-CMA-ES [2]
DASA	2e3	77	210	1300	1500	1800	2100	2400	2700	3700	DASA [19]
DEPSO	1400	25	18e + 0/2e3								DEPSO [12]
DIRECT	1	4.7	22e + 0/5e3								DIRECT [25]
EDA-PSO	2.2e4	130	280	450	14e-2/1e5						EDA-PSO [6]
full NEWUOA	460	3	1.8	2.2	2.3	2.3	2.3	2.3	2.3	2.2	full NEWUOA [31]
G3-PCX	410	3.6	2.9	3.8	4	4.1	4.1	4.1	4.1	4.2	G3-PCX [26]
simple GA	4.4e4	270	19e + 0/1e5								simple GA [22]
GLOBAL	420	2	1.7	1.7	1.6	1.6	1.6	1.6	1.6	1.5	GLOBAL [23]
iAMaLGaM IDEA	1400	7.5	9.6	11	12	12	12	12	12	13	iAMaLGaM IDEA [4]
LSfminbnd	740	6.5	52	470	32e-1/1e4						LSfminbnd [28]
LSstep	1.5e4	130	18e + 0/1e4								LSstep [28]
MA-LS-Chain	820	7.3	17	25	27	29	31	31	30	30	MA-LS-Chain [21]
MCS (Neum)	1	1	1	1.3	1.5	1.6	1.6	1.7	1.7	1.6	MCS (Neum) [18]
NELDER (Han)	200	2.3	3.6	6.6	7.2	7.8	8.4	8.6	8.8	8.9	NELDER (Han) [16]
NELDER (Doe)	150	1.4	3.3	6.1	6.6	7	7.5	7.9	8.4	9.4	NELDER (Doe) [5]
NEWUOA	130	1.3	1	1	1	1	1	1	1	1	NEWUOA [31]
(1+1)-ES	260	2.2	12	52	65	86	110	130	160	200	(1+1)-ES [1]
POEMS	1e4	74	2e3	99e-1/1e5							POEMS [20]
PSO	1600	40	670	75e-1/1e5							PSO [7]
PSO_Bounds	8.2e4	650	700	9700	20e-1/1e5						PSO_Bounds [8]
Monte Carlo	68e + 2/1e6										Monte Carlo [3]
Rosenbrock	190	1.2	8.4	31	37	49	63	850	35e-5/1e4		Rosenbrock [27]
IPOP-SEP-CMA-ES	320	2.2	6.9	7	7.2	7.3	7.3	7.3	7.2	7.2	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	510	3.2	6.9	8.2	8.7	8.7	8.7	8.6	8.6	8.5	VNS (Garcia) [11]

Table 105: 20-D, running time excess ERT/ERT_{best} or	f_9 , in	italics is given	the med	dian final	function	value and t	he median	number	of
function evaluations to reach this value divided by dime	ension								

10 Ellipsoid												
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget	
ERT _{best} /D	94	263	371	433	537	682	746	810	854	874	ERT _{best} /D	
ALPS	330	2500	16e + 1/2e5			-					ALPS [17]	
AMaLGaM IDEA	3.9	1.9	1.8	2	1.9	1.7	1.7	1.8	1.8	2.1	AMaLGaM IDEA [4]	
avg NEWUOA	1	1	1.5	2.6	3.1	3.1	3.6	3.9	4.2	5	avg NEWUOA [31]	
BayEDAcG	42e + 3/2e3										BayEDAcG [10]	
BFGS	1.6	1	1	1	1	1.1	1.1	1.3	3.1	77e-8 /5e4	BFGS [30]	
Cauchy EDA	36	21	20	22	20	19	20	21	21	25	Cauchy EDA [24]	
BIPOP-CMA-ES	3.1	1.9	1.9	1.8	1.6	1.3	1.2	1.1	1.1	1.1	BIPOP-CMA-ES [15]	
(1+1)-CMA-ES	2.5	1.7	1.7	1.7	1.4	1.2	1.1	1	1	1	(1+1)-CMA-ES [2]	
DASA	390	1200	3400	72e-1/1e6							DASA [19]	
DEPSO	17e + 3/2e3										DEPSO [12]	
DIRECT	94e + 2/5e3		•	•							DIRECT [25]	
EDA-PSO	480	36e + 1/1e5								•	EDA-PSO [6]	
full NEWUOA	9.9	15	34	67e-1/1e4							full NEWUOA [31]	
G3-PCX	3.1	3.4	6.5	10	12	13	15	16	18	23	G3-PCX [26]	
simple GA	15e + 3/1e5										simple GA [22]	
GLOBAL	1.7	1	1	1.1	1.1	1.2	2	2.6	5.9	19e-6/2e3	GLOBAL [23]	
iAMaLGaM IDEA	2.3	1.3	1.3	1.3	1.2	1	1	1	1	1.1	iAMaLGaM IDEA [4]	
LSfminbnd	290	22e + 2/1e4									LSfminbnd [28]	
LSstep	18e+3/1e4										LSstep [28]	
MA-LS-Chain	11	12	11	13	11	8.5	7.8	7.2	6.9	6.8	MA-LS-Chain [21]	
MCS (Neum)	72e + 2/4e3										MCS (Neum) [18]	
NELDER (Han)	2.9	5.3	390	30e + 0/1e4							NELDER (Han) [16]	
NELDER (Doe)	2.2	4.2	30	57e-1/2e4							NELDER (Doe) [5]	
NEWUOA	1.2	1.1	1.7	2.6	3.3	3.3	4	4.3	4.7	5.8	NEWUOA [31]	
(1+1)-ES	50	110	300	700	1e3	1e3	2200	3500	8700	94e-5/1e6	(1+1)-ES [1]	
POEMS	5100	12e + 2/1e5									POEMS [20]	
PSO	1200	5600	84e + 1/1e5								PSO [7]	
PSO_Bounds	650	41e+1/1e5			•	•					PSO_Bounds [8]	
Monte Carlo	11e+4/1e6										Monte Carlo [3]	
Rosenbrock	27	140	27e + 1/1e4								Rosenbrock [27]	
IPOP-SEP-CMA-ES	7.2	3.8	3.1	2.9	2.4	2	1.8	1.7	1.6	1.6	IPOP-SEP-CMA-ES [29]	
VNS (Garcia)	8.2	5.7	4.8	4.7	4.2	3.4	3.1	2.9	2.8	2.7	VNS (Garcia) [11]	

Table 106: 20-D, running time excess $\mathrm{ERT}/\mathrm{ERT}_{\mathrm{best}}$ on	f_{10} , in italics i	s given the med	dian final function	value and the media:	a number of
function evaluations to reach this value divided by dimen	nsion				

RT	
n°	
0383	

Table 107: 20-D, ru	unning t	time excess E	ERT/ERT _{be}	$_{\rm st}$ on f_{11} , in	italics is gi	ven the mee	lian final fu	nction valu	e and the m	edian numl	ber of
Tunction evaluation	15 10 10a	ich this value	e divided by	umension	11 T	Discus					ari
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftar et$
$ERT_{h and}/D$	1.35	24.1	50.1	111	314	429	488	554	614	742	ERT AL/D
ALPS	5	59	490	980	2200	12e-2/2e5					ALPS [17]
AMaLGaM IDEA	7	3.3	5	3.7	1.9	1.6	1.7	1.8	1.8	1.9	AMaLGaM IDEA [4]
avg NEWUOA	6	11	15	11	5.7	5.1	5.6	5.5	5.8	6.1	avg NEWUOA [31]
BayEDAcG	4.9	250	14e + 1/2e3								BayEDAcG [10]
BFGS	2.9	1	1	1	1.3	2.6	150	31e-4 /1e4			BFGS [30]
Cauchy EDA	100	71	64	44	22	20	22	24	25	26	Cauchy EDA [24]
BIPOP-CMA-ES	4.1	18	10	5.1	1.9	1.5	1.4	1.3	1.2	1	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	2.4	5.6	7	5.1	2.4	2.3	2.4	2.4	2.3	2	(1+1)-CMA-ES [2]
DASA	4.4	120	570	690	420	550	730	810	980	1500	DASA [19]
DEPSO	8.2	110	95e + 0/2e3								DEPSO [12]
DIRECT	2.1	23	76e + 0'/5e3								DIRECT [25]
EDA-PSO	4.3	74	1900	1.3e4	79e-1/1e5						EDA-PSO [6]
full NEWUOA	5	40	57	45	21	18	36	88	75e-5/1e4		full NEWUOA [31]
G3-PCX	4	9.7	18	14	7	6.5	7.1	7.3	7.6	8	G3-PCX [26]
simple GA	4.2	120	2.9e4	20e+0/1e5							simple GA [22]
GLOBAL	5	1.5	1.2	1	1	2.2	74e-4/1e3				GLOBAL [23]
iAMaLGaM IDEA	4.4	5.2	4.4	2.7	1.2	1	1	1	1	1	iAMaLGaM IDEA [4]
LSfminbnd	2	22e+1/1e4							•		LSfminbnd [28]
LSstep	2.4	29e + 1/1e4									LSstep [28]
MA-LS-Chain	2.6	30	63	35	14	12	11	10	9.3	7.8	MA-LS-Chain [21]
MCS (Neum)	1	53	62e + 0/4e3								MCS (Neum) [18]
NELDER (Han)	3.3	5.2	41	290	16e-1/1e4						NELDER (Han) [16]
NELDER (Doe)	4.4	4.4	17	24	74	75e-3 /2e4			•		NELDER (Doe) [5]
NEWUOA	1.5	15	15	13	5.8	5.6	6.1	6.2	6.6	6.5	NEWUOA [31]
(1+1)-ES	2100	1400	1600	1200	580	560	610	620	670	680	(1+1)-ES [1]
POEMS	130	52	440	410	190	190	980	34e-4/1e5			POEMS [20]
PSO	4.1	46	140	190	110	110	130	140	150	2e3	PSO [7]
PSO_Bounds	4.4	210	570	440	220	240	480	660	1200	12e-4/1e5	PSO_Bounds [8]
Monte Carlo	5.5	930	67e + 0/1e6								Monte Carlo [3]
Rosenbrock	2.9	880	11e + 1/1e4								Rosenbrock [27]
IPOP-SEP-CMA-ES	3.1	34	20	10	3.7	2.8	2.5	2.3	2.1	1.8	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	44	23	12	6.2	2.4	1.9	1.8	1.6	1.6	1.4	VNS (Garcia) [11]

Table 107: 20-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{11} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

RT	
n°	
0383	

Table 108: 20-D, ru	unning time	excess I	ERT/ERThe	on f_{12} , ir	ı italics is gi	ven the med	lian final fu	nction valu	e and the m	edian numb	er of
function evaluation	s to reach th	nis value	e divided by	dimension	0						upc
		iib vara	e annaea sy	unnension	$12 \mathrm{Be}$	nt cigar					uri
Δ ftarget	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta \mathrm{ftagget}$
ERT _{best} /D	25.4	29.6	52.1	96.9	137	158	207	321	620	691	ERT_{hest} /D
ALPS	80	90	87	240	840	3500	33e-3/2e5				ALPS [17]
AMaLGaM IDEA	28	29	19	12	13	16	15	12	7.6	8.4	AMaLGaM IDEA [4]
avg NEWUOA	1.4	1.3	11	15	18	24	24	20	12	21	avg NEWUOA [31]
BayEDAcG	55	60	42	77	21e-1/2e3						BayEDAcG [10]
BFGS	1.6	1.6	1.6	1.6	1.6	1.7	1.6	2.2	1.8	45	BFGS [30]
Cauchy EDA	450	520	510	440	420	400	380	360	390	1100	Cauchy EDA [24]
BIPOP-CMA-ES	3	3	3	4	4.5	4.9	4.5	3.3	1.9	2	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1.8	3.1	7.7	9.6	9.9	9.6	8.3	6	3.4	3.6	(1+1)-CMA-ES [2]
DASA	13	16	2.2e4	2.8e4	4.7e4	8.9e4	6.8e4	4.4e4	2.3e4	13e+0/1e6	DASA [19]
DEPSO	39	48	68	77e-1/2e3	•						DEPSO [12]
DIRECT	340	330	420	240	25e+3/5e3						DIRECT [25]
EDA-PSO	230	250	300	260	720	2600	6800	4400	2300	57e-3/1e5	EDA-PSO [6]
full NEWUOA	2.3	6.7	11	15	26	27	38	37	35	100	full NEWUOA [31]
G3-PCX	2.4	2.5	2.7	2.8	3	3.3	2.9	2.1	1.2	1.3	G3-PCX [26]
simple GA	7100	1.5e4	14e + 2/1e5								simple GA [22]
GLOBAL	1.1	1.1	1	1	1	1	1	1	1.1	3.4	GLOBAL [23]
iAMaLGaM IDEA	12	13	8.7	6.6	7.2	8.1	7.8	6	3.6	3.9	iAMaLGaM IDEA [4]
LSfminbnd	2.9	3	97	410	76e-1/1e4						LSfminbnd [28]
LSstep	29	35	230	680	16e+0/1e4			•			LSstep [28]
MA-LS-Chain	11	12	7.4	9.8	130	140	150	97	51	47	MA-LS-Chain [21]
MCS (Neum)	1.3	1.3	1.1	8.4	12	24	43	87	94	16e-4 /4e3	MCS (Neum) [18]
NELDER (Han)	2.7	5.5	19	26	57	78	340	460	54e-4/1e4		NELDER (Han) [16]
NELDER (Doe)	2.3	4.1	13	45	61	400	1400	21e-3/2e4			NELDER (Doe) [5]
NEWUOA	1.3	1.3	3	3	3	3	2.5	1.8	1	1	NEWUOA [31]
(1+1)-ES	1.7	1.7	1.2e4	6.7e4	52e-1/1e6						(1+1)-ES [1]
POEMS	160	170	420	2100	37e-1/1e5						POEMS [20]
PSO	640	550	1700	64e-1/1e5							PSO [7]
PSO_Bounds	240	270	700	3e3	5100	64e-1/1e5					PSO_Bounds [8]
Monte Carlo	28e+6/1e6	-		•	•			•			Monte Carlo [3]
Rosenbrock	1	1	14	56	210	910	70e-2/1e4				Rosenbrock [27]
IPOP-SEP-CMA-ES	2.7	2.8	5.8	6.7	6.4	6.8	5.9	4.3	2.4	2.5	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	3.3	3.4	5.9	5.9	6.6	9.1	8.3	7.4	4.1	4.4	VNS (Garcia) [11]

RT	
n°	
0383	

Table 109: 20-D, ru	unning t	ime excess H	ERT/ERThe	$_{at}$ on f_{13} , in	italics is giv	ven the med	ian final fui	nction v	value and th	e median nu	umber of
function evaluation	is to rea	ch this value	e divided by	dimension	0						npc
	10 00 100	on onis varae	aiviaca og	unnension	13 Sharp	o ridge					uris
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta \mathrm{ftarget} \widetilde{\mathbb{Q}}$
ERT_{best}/D	3.21	8.51	32.6	101	138	175	937	1090	1220	1510	ERT_{best}/D
ALPS	49	130	97	130	420	2700	14e-3/2e5				ALPS [17]
AMaLGaM IDEA	18	41	18	8	8	7.7	1.7	1.7	1.7	1.7	AMaLGaM IDEA [4]
avg NEWUOA	2.1	1.8	1.5	5.3	14	30	14	57	170	67e-5/2e4	avg NEWUOA [31]
BayEDAcG	45	150	910	49e + 0/2e3							BayEDAcG [10]
BFGS	1.2	1.6	1.7	1	1	1	23	87	96e-5/2e4		BFGS [30]
Cauchy EDA	260	410	210	100	100	100	23	23	23	23	Cauchy EDA [24]
BIPOP-CMA-ES	3.6	5.1	4.3	2.7	5.1	6.2	1.5	1.6	2.3	3	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	2.9	3.4	4.9	7.1	10	11	4.2	5.7	6.3	14	(1+1)-CMA-ES [2]
DASA	15	22	380	230	570	1600	670	1200	3700	51e-6/1e6	DASA [19]
DEPSO	11	40	64	53e-1/2e3							DEPSO [12]
DIRECT	15	2400	13e+1/5e3								DIRECT [25]
EDA-PSO	110	330	160	330	1200	12e-2/1e5					EDA-PSO [6]
full NEWUOA	4.1	3.6	1.8	6	18	49	26	40	120	30e-4/1e4	full NEWUOA [31]
G3-PCX	4.3	4.8	9.3	17	43	75	47	110	130	330	G3-PCX [26]
simple GA	290	700	5100	10e + 0/1e5							simple GA [22]
GLOBAL	5.7	3.1	2	1.1	1.1	1.1	4.5	4.2	16e-4/1e3		GLOBAL [23]
iAMaLGaM IDEA	9.2	18	8.7	4.1	4.3	4.4	1	1	1	1	iAMaLGaM IDEA [4]
LSfminbnd	6.2	8.7	19	19	68	150	160	130	53e-3/1e4		LSfminbnd [28]
LSstep	180	310	460	1400	12e + 0/1e4						LSstep [28]
MA-LS-Chain	7.3	22	11	390	700	1800	1500	1300	27e-3/1e5		MA-LS-Chain [21]
MCS (Neum)	1.3	8.4	34	37	61	330	60e-2/4e3				MCS (Neum) [18]
NELDER (Han)	2.3	6.4	11	29	60	180	77	130	35e-3/1e4		NELDER (Han) [16]
NELDER (Doe)	1.5	3.4	12	18	31	87	98	270	36e-4 /2e4		NELDER (Doe) [5]
NEWUOA	1	1	1	3	9.3	37	19	130	43e-4/9e3		NEWUOA [31]
(1+1)-ES	2.5	3.3	7.4	13	26	95	50	110	410	2e3	(1+1)-ES [1]
POEMS	100	200	1700	1.4e4	59e-1/1e5						POEMS [20]
PSO	6.1	1800	6200	6400	1e4	8e3	1500	1300	22e+0/1e5		PSO [7]
PSO_Bounds	12	310	2300	4100	50e-1/1e5						PSO_Bounds [8]
Monte Carlo	1.5e5	92e + 1/1e6									Monte Carlo [3]
Rosenbrock	2.2	2	2.5	4.2	8.3	31	17	43	120	18e-4/1e4	Rosenbrock [27]
IPOP-SEP-CMA-ES	3.6	5	5.8	5.4	7.7	8	1.7	1.9	1.9	2	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	5.8	6.2	4.3	55	120	180	130	320	540	1500	VNS (Garcia) [11]

oest	t on f_{14} , i	n italics is	given the r	nedian fina	al function va	lue and th	e median number of
oy d	limension						
	14 Sum	of differ	ent powers	5			
00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
	15.2	22.5	46.6	66.6	82.4	783	ERT_{best}/D
	78	93	190	1200	34e-6/2e5		ALPS [17]
	30	28	17	15	14	1.9	AMaLGaM IDEA [4]

function evaluation	function evaluations to reach this value divided by dimension													
14 Sum of different powers														
Δ ftarget	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$			
ERT _{best} /D	0.05	0.05	3.75	12	15.2	22.5	46.6	66.6	82.4	783	ERT_{best}/D			
ALPS	1	3.7	41	56	78	93	190	1200	34e-6 /2e5		ALPS [17]			
AMaLGaM IDEA	22	30	28	17	15	14	1.9	AMaLGaM IDEA [4]						
avg NEWUOA	1	38	2.7	1.5	1.6	1.6	1.3	2.7	9.3	26	avg NEWUOA [31]			
BayEDAcG	1	7.2	55	67	150	250	15e-3/2e3				BayEDAcG [10]			
BFGS	1	23	2.7	1.8	2	1.8	1.2	1.1	1.1	18e-7/1e4	BFGS [30]			
Cauchy EDA	1	930	280	270	350	340	210	180	180	25	Cauchy EDA [24]			
BIPOP-CMA-ES	1	7.6	3.9	2.9	3.7	4.3	4.1	5	6.2	1.2	BIPOP-CMA-ES [15]			
(1+1)-CMA-ES	1	18	3.1	1.9	2.3	2.5	2.3	3.4	5.6	1.2	(1+1)-CMA-ES [2]			
DASA	1	93	16	10	12	22	75	560	5200	43e-7/1e6	DASA [19]			
DEPSO	1	13	14	14	25	49	44e-4/2e3				DEPSO [12]			
DIRECT	1	1	8.4	150	290	90e-3/5e3	•				DIRECT [25]			
EDA-PSO	1	3.8	85	140	200	190	130	350	21e-6/1e5		EDA-PSO [6]			
full NEWUOA	1	47	5.9	3	3.6	3.3	2.6	5	20	12e-7/1e4	full NEWUOA [31]			
G3-PCX	1	5.7	4.1	2.4	2.8	3	2.7	4.5	13	59	G3-PCX [26]			
simple GA	1	4.1	280	320	480	2900	72e-4 /1e5				simple GA [22]			
GLOBAL	1	7.5	5	2.2	2.1	1.8	1.1	1	1	28e-7/400	GLOBAL [23]			
iAMaLGaM IDEA	1	4.3	11	9.3	13	12	7.8	6.9	6.9	1	iAMaLGaM IDEA [4]			
LSfminbnd	1	83	8.4	5.2	5.6	9.3	57	31e-5/1e4			LSfminbnd [28]			
LSstep	1	910	190	110	120	210	46e-4/1e4				LSstep [28]			
MA-LS-Chain	1	4.1	7.6	11	13	16	14	23	23	6	MA-LS-Chain [21]			
MCS (Neum)	1	1	1	2.1	3.4	3.7	3.2	15e-5/4e3			MCS (Neum) [18]			
NELDER (Han)	1	23	2.3	3	3.9	3.6	2.9	4.9	36	44e-7/1e4	NELDER (Han) [16]			
NELDER (Doe)	1	11	2	2.1	3.5	3.7	3	5.4	21	26e-7/2e4	NELDER (Doe) [5]			
NEWUOA	1	20	1.5	1	1	1	1	2.3	9.1	43	NEWUOA [31]			
(1+1)-ES	1	17	2.5	1.8	2	2.2	4.8	38	470	71e-8/1e6	(1+1)-ES [1]			
POEMS	1	3100	110	66	120	160	130	2e3	94e-6/1e5		POEMS [20]			
PSO	1	7.2	6.7	12	20	27	54	580	44e-6/1e5		PSO [7]			
PSO_Bounds	1	4.6	23	100	170	240	380	1300	78e-6/1e5		PSO_Bounds [8]			
Monte Carlo	1	5.3	4.5e4	80e-1/1e6							Monte Carlo [3]			
Rosenbrock	1	80	2.4	1.2	1.3	1.8	7.4	97	71e-6/1e4		Rosenbrock [27]			
IPOP-SEP-CMA-ES	1	14	3.3	2.6	3.2	3.7	6.8	8.8	10	1.6	IPOP-SEP-CMA-ES [29]			
VNS (Garcia) 1		3.6	6.4	3.9	4.4	5.1	5	6.4	7.8	1.4	VNS (Garcia) [11]			

Table 110: 20-D, running time excess ERT/ERT_b function evaluations to reach this value divided by

RT n° 0383

	15 Kastrigin													
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$			
ERT_{best}/D	0.06	83.5	1520	7330	15600	15800	16000	16100	22500	23000	ERT_{best}/D			
ALPS	18	10	20e + 0/2e5								ALPS [17]			
AMaLGaM IDEA	12	7.1	1.5	2	1.7	1.7	1.7	1.7	1.2	1.2	AMaLGaM IDÉA [4]			
avg NEWUOA	56	120	95e + 0/1e4								avg NEWUOA [31]			
BayEDAcG	13	23	93e+0/2e3								BayEDAcG [10]			
BFGS	670	25e+1/6e3	•								BFGS [30]			
Cauchy EDA	1700	68	67e+0/5e4								Cauchy EDA [24]			
BIPOP-CMA-ES	17	1.2	1	2	1.4	1.4	1.4	1.4	1	1	BIPOP-CMA-ES [15]			
(1+1)-CMA-ES	33	73	85e+0/1e4								(1+1)-CMA-ES [2]			
DASA	160	3e4	11e + 1/1e6								DASA [19]			
DEPSO	12	12e+1/2e3	•								DEPSO [12]			
DIRECT	1	110	10e+1/5e3								DIRECT [25]			
EDA-PSO	20	22	36	80e-1/1e5							EDA-PSO [6]			
full NEWUOA	120	81	77e + 0/1e4								full NEWUOA [31]			
G3-PCX	21	550	92e+0/5e4								G3-PCX [26]			
simple GA	21	59	25e+0/1e5								simple GA [22]			
GLOBAL	13	25e+1/1e3	•								GLOBAL [23]			
iAMaLGaM IDEA	12	3.1	2.8	14	7.5	7.5	7.4	7.4	5.3	5.2	iAMaLGaM IDEA [4]			
LSfminbnd	130	14e + 1/1e4	•								LSfminbnd [28]			
LSstep	2400	22e+1/1e4	•								LSstep [28]			
MA-LS-Chain	10	3.7	6.9	60e-1/1e5							MA-LS-Chain [21]			
MCS (Neum)	1	70	10e + 1/4e3								MCS (Neum) [18]			
NELDER (Han)	28	54	80e + 0/1e4								NELDER (Han) [16]			
NELDER (Doe)	25	17	54e + 0/2e4								NELDER (Doe) [5]			
NEWUOA	29	1100	12e + 1/6e3								NEWUOA [31]			
(1+1)-ES	340	5400	82e + 0/1e6								(1+1)-ES [1]			
POEMS	2700	23	34e + 0/1e5								POEMS [20]			
PSO	16	92	49e + 0/1e5								PSO [7]			
PSO_Bounds	14	220	51e + 0/1e5								PSO_Bounds [8]			
Monte Carlo	16	26e + 1/1e6									Monte Carlo [3]			
Rosenbrock	7700	35e + 1/1e4									Rosenbrock [27]			
IPOP-SEP-CMA-ES	14	1	1.1	1	1	1	1	1	1.1	6.4	IPOP-SEP-CMA-ES [29]			
VNS (Garcia)	22	1.5	310	60e-1/6e6						•	VNS (Garcia) [11]			

Table 111: 20-D, running time excess ERT/ERT_{best} on f_{15} , in italics is given the median final function value and the median number of										
function evaluations to reach this value divided by dimension										

), rur	ning tin	ne exces	ss ERT
tions	to reach	this va	alue div
	1e + 03	1e+02	1e+
)	0.05	0.05	69
	1	1.2	9.
$\mathbf{E}\mathbf{A}$	1	1.1	14
A	1	1.5	3.
r T	1	1.2	21e+0
	1	140	26e + 0
A	1	3.5	16e + 0
ES	1	1.3	1.
20			0

Table 112: 20-D, running time excess ERT/ERT_{hest} on f_{16} , in italics is given the median final function value and the median number of
function evaluations to reach this value divided by dimension
16 Weierstrass

Δ ftarget	1e+03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget
ERT_{best}/D	0.05	0.05	69.2	1360	3850	6960	9400	9760	9890	11000	ERT_{best}/D
ALPS	1	1.2	9.3	110	78e-2/2e5						ALPS [17]
AMaLGaM IDEA	1	1.1	14	3.3	5.2	5.4	6.2	6.1	6.1	5.7	AMaLGaM IDÉA [4]
avg NEWUOA	1	1.5	3.6	31e-1/2e4							avg NEWUOA [31]
BayEDAcG	1	1.2	21e + 0/2e3	•		•					BayEDAcG [10]
BFGS	1	140	26e + 0/2e4								BFGS [30]
Cauchy EDA	1	3.5	16e + 0/5e4								Cauchy EDA [24]
BIPOP-CMA-ES	1	1.3	1.7	1	1.2	1	1	1	1	1	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1.1	34	53e-1/1e4		•					(1+1)-CMA-ES [2]
DASA	1	2.3	980	44e-1/1e6							DASA [19]
DEPSO	1	1.2	23e + 0/2e3								DEPSO [12]
DIRECT	1	1	8.3	7	12e-1/5e3						DIRECT [25]
EDA-PSO	1	1.3	530	55	380	75e-2/1e5					EDA-PSO [6]
full NEWUOA	1	1.9	4.6	110	25e-1/1e4						full NEWUOA [31]
G3-PCX	1	1.3	17	32e-1/5e4							G3-PCX [26]
simple GA	1	1.3	140	1e3	24e-1/1e5						simple GA [22]
GLOBAL	1	1.2	1	42e-1/600	•						GLOBAL [23]
iAMaLGaM IDEA	1	1.2	3.6	1.7	13	18	29	29	28	26	iAMaLGaM IDEA [4]
LSfminbnd	1	1.1	160	95e-1/1e4							LSfminbnd [28]
LSstep	1	1	240	10e + 0/1e4							LSstep [28]
MA-LS-Chain	1	1.1	19	18e-1/1e5							MA-LS-Chain [21]
MCS (Neum)	1	1	11	75e-1/4e3							MCS (Neum) [18]
NELDER (Han)	1	1.3	17	47e-1/1e4							NELDER (Han) [16]
NELDER (Doe)	1	1.4	7.2	30e-1/2e4							NELDER (Doe) [5]
NEWUOA	1	1.1	16	53e-1/1e4							NEWUOA [31]
(1+1)-ES	1	1.2	1400	72e-1/1e6							(1+1)-ES [1]
POEMS	1	250	15	21	100	58e-2/1e5					POEMS [20]
PSO	1	1.3	110	47e-1/1e5							PSO [7]
PSO_Bounds	1	1.2	130	1e3	25e-1/1e5						PSO_Bounds [8]
Monte Carlo	1	1.3	6.5e4	11e+0/1e6							Monte Carlo [3]
Rosenbrock	1	3.4	29e + 0/1e4								Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1.2	3.1	1	1	1.1	1.4	1.9	1.9	1.7	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1	3.6	9.1	500	72e-3 /3e6	•	•	•	•	VNS (Garcia) [11]

	15 10 10a		value ui		7 Schaffer	F7. condit	tion 10)			
Δ ftarget	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget
ERT_{best}/D	0.05	0.05	3.15	51.5	200	612	1530	2230	2810	4020	ERT_{best}/D
ALPS	1	1.5	19	28	5100	16e-2/2e5					ALPS [17]
AMaLGaM IDEA	1	1.1	14	7.7	4.3	5.1	4.7	3.5	5.1	5.4	AMaLGaM IDEA [4]
avg NEWUOA	1	2.1	2.4	29e-1/4e4							avg NEWUOA [31]
BayEDAcG	1	2	19	19	48	15e-2/2e3			•		BayEDAcG [10]
BFGS	1	350	360	56e-1/2e4							BFGS [30]
Cauchy EDA	1.1	200	260	120	62	30	16	16	23	37e-7/5e4	Cauchy EDA [24]
BIPOP-CMA-ES	1	4	2.2	1	1	1	1.2	1.4	1.3	1.4	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1.9	29	49e-1/1e4		•		•	•	•	(1+1)-CMA-ES [2]
DASA	1	8.5	6.6e4	57e-1/1e6							DASA [19]
DEPSO	1	1.5	8.3	18	150	43e-2/2e3					DEPSO [12]
DIRECT	1	1	1.8	55	55e-2/5e3						DIRECT [25]
EDA-PSO	1	1.3	13	36	20	22	10	8.1	18	21	EDA-PSO [6]
full NEWUOA	1	9.4	13	37e-1/1e4		•					full NEWUOA [31]
G3-PCX	1	1.2	4	35e-1/5e4							G3-PCX [26]
simple GA	1	1.2	57	92	7100	21e-2/1e5					simple GA [22]
GLOBAL	1	1.6	6.2	44e-1/3e3							GLOBAL [23]
iAMaLGaM IDEA	1	1.5	6.4	2.9	1.5	1.4	6.1	22	29	23	iAMaLGaM IDEA [4]
LSfminbnd	1	6.8	990	82e-1/1e4							LSfminbnd [28]
LSstep	1	55	1700	78e-1/1e4		•					LSstep [28]
MA-LS-Chain	1	1.3	3.5	5.1	7.7	10	12	33	59	86	MA-LS-Chain [21]
MCS (Neum)	1	1	1	42e-1/4e3		•					MCS (Neum) [18]
NELDER (Han)	1	1.3	240	62e-1/1e4							NELDER (Han) [16]
NELDER (Doe)	1	4	2.1	46e-1/2e4							NELDER (Doe) [5]
NEWUOA	1	5.1	16	38e-1/8e4							NEWUOA [31]
(1+1)-ES	1	5.7	5.2e4	73e-1/1e6		•					(1+1)-ES [1]
POEMS	1	540	94	25	19	200	270	11e-3/1e5			POEMS [20]
PSO	1	1.1	3.2	2500	10e-1/1e5						PSO [7]
PSO_Bounds	1	1.3	3	830	85e-2/1e5						PSO_Bounds [8]
Monte Carlo	1	1.1	120	50e-1/1e6							Monte Carlo [3]
Rosenbrock	1	1.6e4	2.1e4	19e + 0/1e4							Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1.4	2.8	4	3.1	1.6	1	1	1	1	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1.2	5.3	1.2	1.5	5.8	34	2500	10e-5/4e6		VNS (Garcia) [11]

Table 114: 20- function evaluation	D, running ations to r
$\Delta ftarget$	1e+0
ERT _{best} /D	0.05
ALPS	1.1
AMaLGaM ID	EA 1.2
avg NEWUO	A 1.3
BayEDAcG	1

RT n° 0383

T 1 1 1 1 00 D	• •			e c	, 1.		(1 1.	C 1 C		1 1/1	1: 1 6			
able 114: 20-D, running time excess ER1/ER1 best on J_{18} , in italics is given the median final function value and the median number of														
unction evaluation	inclion evaluations to reach this value divided by dimension													
	18 Schaffer F7, condition 1000													
Δ ftarget	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget			
ERT_{hest}/D	0.05	0.14	31	199	978	1430	3380	4980	6530	7330	ERT_{best}/D			
ALPS	1.1	3.8	15	430	69e-2/2e5						ALPS [17]			
AMaLGaM IDEA	1.2	3.8	7.3	3	1	1	1.7	2.7	2.8	3.7	AMaLGaM IDÉA [4]			
avg NEWUOA	1.3	19	3200	10e + 0/6e4							avg NEWUOA [31]			
BayEDAcG	1	6.4	15	17	95e-2/2e3		•			•	BayEDAcG [10]			
BFGS	1	920	21e+0/2e4								BFGS [30]			
Cauchy EDA	2.5	270	96	42	15	16	12	13	38	25e-6/5e4	Cauchy EDA [24]			
BIPOP-CMA-ES	1	5.3	1	2.4	1.2	1.6	1.1	1.8	1.7	1.6	BIPOP-CMA-ES [15]			
(1+1)-CMA-ES	1	12	4800	16e + 0/1e4	•		•			•	(1+1)-CMA-ES [2]			
DASA	1	60	4.6e5	25e+0/1e6						•	DASA [19]			
DEPSO	1	7.9	7.1	49	16e-1/2e3						DEPSO [12]			
DIRECT	1	6.5	9.1	110	12e-1/5e3		•				DIRECT [25]			
EDA-PSO	1.1	4.2	30	15	5.2	5.4	18	83	220	47e-5/1e5	EDA-PSO [6]			
full NEWUOA	1.1	23	950	12e + 0/1e4			•				full NEWUOA [31]			
G3-PCX	1.1	2.2	7100	14e+0/5e4						•	G3-PCX [26]			
simple GA	1.1	7.8	76	310	73e-2/1e5						simple GA [22]			
GLOBAL	1.1	5.9	17e + 0/4e3								GLOBAL [23]			
iAMaLGaM IDEA	1.2	3.4	2.7	1.2	2.3	3.7	19	18	16	18	iAMaLGaM IDEA [4]			
LSfminbnd	2.2	31	4500	26e + 0/1e4							LSfminbnd [28]			
LSstep	1.1	610	31e+0/1e4								LSstep [28]			
MA-LS-Chain	1.1	5.8	3.6	3.6	26	78	210	43e-4 /1e5			MA-LS-Chain [21]			
MCS (Neum)	1	1	17e + 0/4e3								MCS (Neum) [18]			
NELDER (Han)	1	830	20e+0/1e4								NELDER (Han) [16]			
NELDER (Doe)	1	6.5	4300	14e+0/2e4			•		•	•	NELDER (Doe) $[5]$			
NEWUOA	3.9	320	1.2e4	11e + 0/8e4		•					NEWUOA [31]			
(1+1)-ES	1	2.9e5	24e+0/1e6				•		•	•	(1+1)-ES [1]			
POEMS	5.1	1100	21	140	210	990	38e-2/1e5			•	POEMS [20]			
PSO	1.1	5.2	240	29e-1/1e5	•					•	PSO [7]			
PSO_Bounds	1.1	2.4	69	7100	22e-1/1e5		•	•		•	PSO_Bounds [8]			
Monte Carlo	1.1	7.7	18e + 0/1e6				•		•	•	Monte Carlo [3]			
Rosenbrock	1.4e4	4.8e4	97e + 0/1e4								Rosenbrock [27]			
IPOP-SEP-CMA-ES	1	8.5	1	1	1.1	1.2	1	1	1	1	IPOP-SEP-CMA-ES [29]			
VNS (Garcia)	1	2.5	1.3	1	14	250	40e-4/4e6				VNS (Garcia) [11]			

19 Griewank-Rosenbrock F8F2											
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{hest}/D	0.05	0.05	0.05	0.05	17200	2.34e5	3.11e5	3.33e5	3.34e5	3.37e5	ERT_{best}/D
ALPS	1	1	1200	6.2e5	31e-2/2e5		•				ALPS [17]
AMaLGaM IDEA	1	1.2	740	3.4e4	7.6	4.5	8.8	8.2	8.2	8.1	AMaLGaM IDEA [4]
avg NEWUOA	1	2.9	210	8e6	20e-1/1e5						avg NEWUOA [31]
BayEDAcG	1	1.1	1500	41e-1/2e3		•			•		BayEDAcG [10]
BFGS	1	170	1.2e6	12e + 0/1e4							BFGS [30]
Cauchy EDA	1	3.4	8400	34e-1/5e4							Cauchy EDA [24]
BIPOP-CMA-ES	1	1	170	2.4e4	1.2	1	1	1	1	1	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1	1400	2.8e6	18e-1/1e4	•		•	•	•	(1+1)-CMA-ES [2]
DASA	1	2.1	1.8e6	58e-1/1e6				•			DASA [19]
DEPSO	1	1.1	430	50e-1/2e3		•			•	•	DEPSO [12]
DIRECT	1	1	1	1	21e-2/5e3			•			DIRECT [25]
EDA-PSO	1	1.1	4600	2.8e7	26e-1/1e5						EDA-PSO [6]
full NEWUOA	1	1.3	480	21e-1/1e4				•	•		full NEWUOA [31]
G3-PCX	1	1.1	800	26e-1/5e4					•		G3-PCX [26]
simple GA	1	1.1	1.4e4	6.5e5	44e-2/1e5			•	•		simple GA [22]
GLOBAL	1	1	5600	57e-1/3e3		•	•	•	•	•	GLOBAL [23]
iAMaLGaM IDEA	1	1.1	460	1.8e6	44	72e-3/1e6		•	•		iAMaLGaM IDEA [4]
LSfminbnd	1	2.6	1200	38e-1/1e4				•			LSfminbnd [28]
LSstep	1	130	7800	<i>41e-1/1e4</i>		•	•	•	•	•	LSstep [28]
MA-LS-Chain	1	1.1	280	2.9e4	13	11e-2/1e5	•	•	•	•	MA-LS-Chain [21]
MCS (Neum)	1	1	1	1	1	25e-2/4e3	•	•	•	•	MCS (Neum) [18]
NELDER (Han)	1	1	160	1.4e6	19e-1/1e4	•	•	•	•	•	NELDER (Han) [16]
NELDER (Doe)	1	1	73	4.3e5	96e-2/2e4	•	•	•	•	•	NELDER (Doe) $[5]$
NEWUOA	1	1.1	76	4.3e6	12e-1/1e5						NEWUOA [31]
(1+1)-ES	1	2.5	6.3e6	56e-1/1e6		•	•	•	•	•	(1+1)-ES [1]
POEMS	1	170	6200	1.4e6	94e-2/1e5	•	•	•	•	•	POEMS [20]
PSO	1	1.1	380	32e-1/1e5		•	•	•	•	•	PSO [7]
PSO_Bounds	1	1.1	820	31e-1/1e5		•	•	•	•	•	PSO_Bounds [8]
Monte Carlo	1	1.1	5.9e5	78e-1/1e6		•	•	•	•	•	Monte Carlo [3]
Rosenbrock	1	3.1e4	33e + 0/1e4					•	•	•	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1	150	2.7e4	8.7	29e-2/1e4		•	•	•	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1	330	8.2e4	21e-2/6e6						VNS (Garcia) [11]

Table 115: 20-D, running time excess ERT/ERT_{best} on f_{19} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

netion evaluations to reach this value divided by dimension											
20 Schweiel x^+ sin(x)											
Δ ftarget	1e+03	1e + 02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget
ERT_{best}/D	2.78	3.53	4.09	2310	1.55e5	2.76e5	2.77e5	2.78e5	2.8e5	2.82e5	ERT _{best} /D
ALPS	48	54	53	9.2	47e-2/2e5	•	•	•	•	•	ALPS [17]
AMaLGaM IDEA	20	22	20	88	68e-2/1e6	•	•	•	•	•	AMaLGaM IDEA [4]
avg NEWUOA	1.8	1.4	1.3	110	12e-1/2e4	•	•	•	•	•	avg NEWUOA [31]
BayEDAcG	47	51	49	31e-1/2e3	•	•	•	•	•	•	BayEDAcG [10]
BFGS	1.7	1.9	2.1	5.8	90e-2/2e4	•	•	•	•	•	BFGS [30]
Cauchy EDA	310	330	340	27e-1/5e4			•				Cauchy EDA [24]
BIPOP-CMA-ES	4.7	4.4	4.3	9.2	1	1	1	1	1	1	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	3.5	3.6	3.4	21	11e-1/1e4		•				(1+1)-CMA-ES [2]
DASA	22	21	20	2.1	40e-2/1e6						DASA [19]
DEPSO	15	16	15	21e-1/2e3							DEPSO [12]
DIRECT	17	36	31	18e-1/5e3							DIRECT [25]
EDA-PSO	210	230	230	15	63e-2/1e5		•				EDA-PSO [6]
full NEWUOA	4.2	3.4	3.1	64	12e-1/1e4						full NEWUOA [31]
G3-PCX	5.6	5.4	5	12e-1/5e4							G3-PCX [26]
simple GA	470	520	500	2.8	32e-2/1e5		•				simple GA [22]
GLOBAL	6.6	5.6	5.2	1.6	99e-2/4e3		•				GLOBAL [23]
iAMaLGaM IDEA	14	14	14	240	88e-2/1e6						iAMaLGaM IDEA [4]
LSfminbnd	11	11	11	5.9	97e-2/1e4		•				LSfminbnd [28]
LSstep	230	260	280	11	10e-1/1e4		•				LSstep [28]
MA-LS-Chain	8	9.7	9.4	3.3	4.8	24e-2/1e5	•				MA-LS-Chain [21]
MCS (Neum)	5.9	5.4	4.7	12	12e-1/4e3	•	•	•	•	•	MCS (Neum) [18]
NELDER (Han)	3.1	3.4	3.5	13e-1/1e4			•				NELDER (Han) [16]
NELDER (Doe)	1.9	2.1	2.2	28	11e-1/2e4	•	•	•	•	•	NELDER (Doe) [5]
NEWUOA	1	1	1	15	10e-1/2e4	•	•	•	•	•	NEWUOA [31]
(1+1)-ES	3.4	3.2	3.1	110	88e-2/1e6		•			•	(1+1)-ES [1]
POEMS	130	120	120	1	30e-2/1e5		•				POEMS [20]
PSO	12	15	17	50	11e-1/1e5	•	•	•	•	•	PSO [7]
PSO_Bounds	66	79	86	11	53e-2/1e5	•	•	•	•	•	PSO_Bounds [8]
Monte Carlo	1.7e6	15e + 2/1e6			•	•	•	•	•	•	Monte Carlo [3]
Rosenbrock	3	2.7	2.6	2.9	97e-2/1e4						Rosenbrock [27]
IPOP-SEP-CMA-ES	4.4	4.7	4.5	13	11e-1/1e4						IPOP-SEP-CMA-ES [29]
VNS (Garcia)	8.1	7.7	7.1	1.1	30e-2/1e7				•		VNS (Garcia) [11]

Table 116: 20-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{20} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

function evaluations to reach this value divided by dimension											
21 Gallagher 101 peaks											
$\Delta ftarget$	1e+03	1e+02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{best}/D	0.05	0.05	28.1	327	705	716	732	754	778	879	ERT_{best}/D
ALPS	1	1	14	13	7	7.7	8.3	9.2	9.8	11	ALPS [17]
AMaLGaM IDEA	1	1	51	2400	1500	1500	1500	1500	1400	1300	AMaLGaM IDEA [4]
avg NEWUOA	1	1	3.2	5.7	3.5	3.5	3.4	3.3	3.3	2.9	avg NEWUOA [31]
BayEDAcG	1	1	55	60e-1/2e3							BayEDAcG [10]
BFGS	1	1	1.9	5.5	4.6	4.6	4.5	4.4	4.3	7.3	BFGS [30]
Cauchy EDA	1	1	1e3	32e-1/5e4							Cauchy EDA [24]
BIPOP-CMA-ES	1	1	3.2	55	48	47	46	45	43	39	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1	3.6	7.6	5.8	5.7	5.6	5.4	5.3	4.7	(1+1)-CMA-ES [2]
DASA	1	1	240	100	100	100	99	96	93	83	DASA [19]
DEPSO	1	1	22	13	8.3	8.6	8.9	9.3	19	20e-1/2e3	DEPSO [12]
DIRECT	1	1	3.3	27	19e-1/5e3						DIRECT [25]
EDA-PSO	1	1	35	850	570	560	550	530	520	460	EDA-PSO [6]
full NEWUOA	1	1	7.4	3.4	4.5	4.5	4.4	4.2	4.1	3.7	full NEWUOA [31]
G3-PCX	1	1	12	7.2	5.1	5	4.9	4.8	4.6	4.1	G3-PCX [26]
simple GA	1	1	90	620	400	400	900	890	20e-1/1e5		simple GA [22]
GLOBAL	1	1	1	1	1	1	1	1	1	2.1	GLOBAL [23]
iAMaLGaM IDEA	1	1	10	670	540	540	530	520	540	490	iAMaLGaM IDEA [4]
LSfminbnd	1	1	30	27	20	20	19	19	18	16	LSfminbnd [28]
LSstep	1	1	120	200	200	200	200	190	190	170	LSstep [28]
MA-LS-Chain	1	1	140	310	230	230	220	210	210	180	MA-LS-Chain [21]
MCS (Neum)	1	1	26	32	26	25	25	24	23	32	MCS (Neum) [18]
NELDER (Han)	1	1	7.7	20	24	24	23	23	22	20	NELDER (Han) [16]
NELDER (Doe)	1	1	7.6	4	2	2.1	2.1	2	2	1.8	NELDER (Doe) [5]
NEWUOA	1	1	1.7	2.2	1.2	1.2	1.2	1.1	1.1	1	NEWUOA [31]
(1+1)-ES	1	1	8.3	13	9.4	9.3	9.1	8.8	8.6	7.6	(1+1)-ES [1]
POEMS	1	1	2500	67e-1/1e5							POEMS [20]
PSO	1	1	1800	4300	2e3	2e3	1900	1900	1800	1600	PSO [7]
PSO_Bounds	1	1	560	1200	2e3	2e3	1900	1900	1800	1600	PSO_Bounds [8]
Monte Carlo	1	1	26e+0/1e6								Monte Carlo [3]
Rosenbrock	1	1	7.8	7.6	4.7	4.6	4.5	4.4	4.3	3.8	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1	15	50	58	57	56	54	53	47	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1	11	55	29	29	29	28	27	25	VNS (Garcia) [11]

Table 117: 20-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{21} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

22 Gallagher 21 peaks											
Δ ftarget	1e+03	1e + 02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{best}/D	0.05	0.05	23.3	279	1170	1210	1250	1310	1340	6740	ERT_{best}/D
ALPS	1	1	19	9.7	79	81	86	110	180	130	ALPS [17]
AMaLGaM IDEA	1	1	8.2	1900	69e-2/1e6						AMaLGaM IDEA [4]
avg NEWUOA	1	1	2	5.6	14	13	13	12	12	2.4	avg NEWUOA [31]
BayEDAcG	1	1	34	31	20e-1/2e3						BayEDAcG [10]
BFGS	1	1	2.5	1.8	8.1	7.9	7.7	7.4	9.5	14	BFGS [30]
Cauchy EDA	1.1	1.1	470	1200	51e-1/5e4						Cauchy EDA [24]
BIPOP-CMA-ES	1	1	6.8	13	210	210	200	190	190	37	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1	3.5	4.2	5.6	5.5	5.3	5.1	5	1	(1+1)-CMA-ES [2]
DASA	1	1	34	75	220	210	210	200	200	40	DASA [19]
DEPSO	1	1	20	16	26e-1/2e3						DEPSO [12]
DIRECT	1	1	9.8	16	71e-2/5e3						DIRECT [25]
EDA-PSO	1	1	1600	1e3	26e-1/1e5						EDA-PSO [6]
full NEWUOA	1	1	2.2	12	60	59	57	54	53	11	full NEWUOA [31]
G3-PCX	1	1	11	6.6	23	22	22	21	20	4	G3-PCX [26]
simple GA	1	1	110	1500	20e-1/1e5						simple GA [22]
GLOBAL	1	1	1.1	1	1	1	1	1	1	1.3	GLOBAL [23]
iAMaLGaM IDEA	1	1	8.1	440	69e-2/1e6						iAMaLGaM IDEA [4]
LSfminbnd	1	1	59	16	37	36	36	35	34	7.2	LSfminbnd [28]
LSstep	1	1	280	51e-1/1e4							LSstep [28]
MA-LS-Chain	1	1	3.8	810	20e-1/1e5		•				MA-LS-Chain [21]
MCS (Neum)	1	1	17	20	50	48	47	20e-1/4e3			MCS (Neum) [18]
NELDER (Han)	1	1	17	18	61	59	58	55	54	11	NELDER (Han) [16]
NELDER (Doe)	1	1	5.2	6.5	8.3	8.2	8	7.7	7.5	1.5	NELDER (Doe) $[5]$
NEWUOA	1	1	1	4.9	6.8	6.6	6.4	6.2	6	1.2	NEWUOA [31]
(1+1)-ES	1	1	11	5	11	11	11	10	10	2.1	(1+1)-ES [1]
POEMS	1	1	2300	5e3	51e-1/1e5		•				POEMS [20]
PSO	1	1	5	410	20e-1/1e5	•	•	•	•		PSO [7]
PSO_Bounds	1	1	680	730	1200	1200	1100	1100	1100	210	PSO_Bounds [8]
Monte Carlo	1	1	6.4e5	30e + 0/1e6							Monte Carlo [3]
Rosenbrock	1	1	3.4	4.3	12	12	12	11	11	2.2	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1	6.2	23	69e-2/1e4	•	•		•		IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1	14	67	1300	1200	1200	1200	1100	440	VNS (Garcia) [11]

Table 118: 20-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{22} ,	in italics is given the median final function value and the median number of
function evaluations to reach this value divided by dimension	l

RT	
n°	
0383	

23 Katsuuras											
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT _{best} /D	0.05	0.05	0.16	80.7	3370	18300	24400	25500	40600	41900	ERThest/D
ALPS	1	1	1.9	82	29e-2/2e5				ī		ALPS [17]
AMaLGaM IDEA	1	1	1.7	23	1.1	1	1	1	1	1	AMaLGaM IDEA [4]
avg NEWUOA	1	1	15	4.7	20e-2/2e4						avg NEWUOA [31]
BayEDAcG	1	1	1.6	23e-1/2e3							BayEDAcG [10]
BFGS	1	1	47	300	13e-1 /5e3						BFGS [30]
Cauchy EDA	1	1	1.9	19e-1/5e4							Cauchy EDA [24]
BIPOP-CMA-ES	1	1	4.3	32	1	1.7	2	1.9	1.2	1.2	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1	5.8	9.1	37e-2/1e4						(1+1)-CMA-ES [2]
DASA	1	1	3.4	64	31e-2/1e6						DASA [19]
DEPSO	1	1	1.6	26e-1/2e3							DEPSO [12]
DIRECT	1	1	4.1	52	38e-2/5e3						DIRECT [25]
EDA-PSO	1	1	2.1	16e-1/1e5							EDA-PSO [6]
full NEWUOA	1	1	14	7	44	25e-2/1e4					full NEWUOA [31]
G3-PCX	1	1	2.8	7.8	30e-2/3e4						G3-PCX [26]
simple GA	1	1	1.7	4600	12e-1/1e5						simple GA [22]
GLOBAL	1	1	2.8	1	43e-2/500						GLOBAL [23]
iAMaLGaM IDEA	1	1	1.9	5.4	1.6	2.3	5.1	5.2	3.3	3.2	iAMaLGaM IDEA [4]
LSfminbnd	1	1	4.4	210	10e-1/1e4						LSfminbnd [28]
LSstep	1	1	2.2	81	91e-2/1e4						LSstep [28]
MA-LS-Chain	1	1	1.8	7.1	8.9	61e-3/1e5					MA-LS-Chain [21]
MCS (Neum)	1	1	1.3	120	11e-1/4e3						MCS (Neum) [18]
NELDER (Han)	1	1	2.1	3.3	43	20e-2/1e4					NELDER (Han) [16]
NELDER (Doe)	1	1	1.9	1.4	86	17e-2/2e4					NELDER (Doe) [5]
NEWUOA	1	1	12	3.5	32	39e-2/8e3					NEWUOA [31]
(1+1)-ES	1	1	27	32	31e-2/1e6						(1+1)-ES [1]
POEMS	1	1	23	42	13	59e-3/1e5					POEMS [20]
PSO	1	1	2.2	1600	95e-2/1e5						PSO [7]
PSO_Bounds	1	1	3	8400	12e-1/1e5						PSO_Bounds [8]
Monte Carlo	1	1	2.6	5.5e4	11e-1/1e6						Monte Carlo [3]
Rosenbrock	1	1	1.7	4.6	50e-2/4e3						Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1	4.9	18	3.8	81e-3/1e4					IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1	1	25	10	1700	23e-3 /2e6				VNS (Garcia) [11]

Table 119: 20-D, running time excess ERT/ERT _{best} on f_{23} , in italics is given the median final function value and the median nu	mber of
function evaluations to reach this value divided by dimension	

24 Lunacek bi-Rastrigin											
Δ ftarget	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{hest}/D	0.05	331	66900	3.74e5	2.6e6	2.6e6	2.6e6	2.6e6	2.6e6	2.6e6	ERT_{best}/D
ALPS	1	5.7	22e + 0/2e5	•							ALPS [17]
AMaLGaM IDEA	1.1	4.2	5.1	19	23e-1/1e6						AMaLGaM IDEA [4]
avg NEWUOA	14	3.3	74e+0/1e4		•						avg NEWUOA [31]
BayEDAcG	1	44	11e + 1/2e3								BayEDAcG [10]
BFGS	8	31e+1/6e3								•	BFGS [30]
Cauchy EDA	1.7	76	91e + 0/5e4								Cauchy EDA [24]
BIPOP-CMA-ES	1	5.5	1	1	1	1	1	1	1	1	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	24	90e + 0/1e4					•			(1+1)-CMA-ES [2]
DASA	1.1	16e + 1/1e6				•		•	•		DASA [19]
DEPSO	1.1	14e + 1/2e3						•			DEPSO [12]
DIRECT	1	15e+1/5e3		•							DIRECT [25]
EDA-PSO	1.1	28	86e + 0/1e5			•	•	•	•	•	EDA-PSO [6]
full NEWUOA	3.7	4.5	71e + 0/1e4	•							full NEWUOA [31]
G3-PCX	1.1	190	11e+1/5e4	•							G3-PCX [26]
simple GA	1.1	35	42e + 0/1e5	•							simple GA [22]
GLOBAL	1	21e+1/1e3						•			GLOBAL [23]
iAMaLGaM IDEA	1.1	1.3	2.8	21e-1/1e6							iAMaLGaM IDEA [4]
LSfminbnd	7.1	15e + 1/1e4		•							LSfminbnd [28]
LSstep	3.1	210	19e+1/1e4	•							LSstep [28]
MA-LS-Chain	1.1	2.1	42	25e+0/1e5		•	•	•	•	•	MA-LS-Chain [21]
MCS (Neum)	1	12	10e+1/4e3	•							MCS (Neum) [18]
NELDER (Han)	1	49	10e+1/1e4	•				•			NELDER (Han) [16]
NELDER (Doe)	1	3.7	50e + 0/2e4			•		•	•		NELDER (Doe) [5]
NEWUOA	6.5	4.3	83e+0/8e3	•				•			NEWUOA [31]
(1+1)-ES	4.1	3100	93e + 0/1e6	•							(1+1)-ES [1]
POEMS	2.7	10	46e + 0/1e5	•				•			POEMS [20]
PSO	1	63	60e + 0/1e5	•							PSO [7]
PSO_Bounds	1.1	81	66e + 0/1e5	•		•	•	•	•	•	PSO_Bounds [8]
Monte Carlo	1	26e+1/1e6		•							Monte Carlo [3]
Rosenbrock	1.4	37e + 1/1e4									Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1	1	23e+0/1e4		•	•	•	•	•	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1.8	68	88e-1/1e7							VNS (Garcia) [11]

Table 120: 20-D, running time excess ERT/ERT_{best} on f_{24} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

Table 121: 40-D, running time excess ERT/ERT_{best} on f_1 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

1 Sphere											
$\Delta ftarget$	1e + 03	1e + 02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{best}/D	0.025	2.07	2.08	2.08	2.08	2.08	2.08	2.08	2.08	2.08	ERT_{best}/D
ALPS	1	46	220	420	640	870	1100	1400	1700	2800	ALPS [17]
AMaLGaM IDEA	1	46	150	290	430	560	690	810	970	1200	AMaLGaM IDEA [4]
avg NEWUOA	1	3.2	3.2	3.2	3.2	3.2	3.2	3.2	3.2	3.2	avg NEWUOA [31]
BayEDAcG	1	60	210	350	500	650	790	940	64e-6/2e3		BayEDAcG [10]
BFGS	1	1	1	1	1	1	1	1	1	1	BFGS [30]
BIPOP-CMA-ES	1	3.1	9.6	15	21	28	34	40	45	58	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	3	7	11	15	19	23	27	31	39	(1+1)-CMA-ES [2]
DASA	1	13	33	57	94	130	180	220	260	340	DASA [19]
DEPSO	1	12	65	360	1.4e4	15e-2/2e3					DEPSO [12]
simple GA	1	400	1500	3e3	2.3e4	6.8e5	45e-3/1e5				simple GA [22]
iAMaLGaM IDEA	1	17	73	130	180	240	290	350	410	520	iAMaLGaM IDEA [4]
NELDER (Han)	1	3.9	13	21	28	35	42	49	55	67	NELDER (Han) [16]
NEWUOA	1	1	1	1	1	1	1	1	1	1	NEWUOA [31]
(1+1)-ES	1	2.5	5.8	9.2	13	16	19	23	26	33	(1+1)-ES [1]
Monte Carlo	1	13e + 1/1e6			•						Monte Carlo [3]
IPOP-SEP-CMA-ES	1	3	8.7	14	19	25	30	35	41	51	IPOP-SEP-CMA-ES [29]

Table 122: 40-D, running time excess ERT/ERT_{best} on f_2 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

2 Ellipsoid separable											
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{best}/D	74.3	96.6	118	137	155	172	190	208	221	256	ERT_{best}/D
ALPS	14	15	17	19	20	23	26	32	46	140	ALPS [17]
AMaLGaM IDEA	14	14	14	14	14	14	14	14	14	14	AMaLGaM IDEA [4]
avg NEWUOA	2	4.7	6	9	10	12	12	13	13	14	avg NEWUOA [31]
BayEDAcG	13	13	13	14	33e-2/2e3						BayEDAcG [10]
BFGS	4.3	5.5	6	6.1	5.9	5.6	5.4	5	4.8	4.4	BFGS [30]
BIPOP-CMA-ES	7.7	9.8	11	10	10	9.5	9	8.4	8	7.1	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	6	8.1	9.3	9.5	9.5	9.3	8.7	8.2	7.8	6.8	(1+1)-CMA-ES [2]
DASA	1.7	2.1	2.5	2.8	3	3.3	3.4	3.5	3.7	3.8	DASA [19]
DEPSO	28	310	65e + 1/2e3								DEPSO [12]
simple GA	610	2200	24e + 1/1e5								simple GA [22]
iAMaLGaM IDEA	6.2	7.4	7.7	7.7	7.7	7.6	7.4	7.3	7.4	7.3	iAMaLGaM IDEA [4]
NELDER (Han)	1.1	1	1	1	1	1	1	1	1	1	NELDER (Han) [16]
NEWUOA	1	2.6	4.4	6.4	8.8	9.9	11	12	13	13	NEWUOA [31]
(1+1)-ES	140	630	1500	2500	3400	4400	8900	1.4e4	6.8e4	93e-5/1e6	(1+1)-ES [1]
Monte Carlo	12e + 5/1e6										Monte Carlo [3]
IPOP-SEP-CMA-ES	1.4	1.5	1.5	1.4	1.3	1.3	1.2	1.2	1.2	1.1	IPOP-SEP-CMA-ES [29]

Comparison Tables: BBOB 2009 Function Testbed

Table 123: 40-D, running time excess ERT/ERT_{best} on f_3 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

3 Rastrigin separable											
Δ ftarget	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget
ERT_{best}/D	5.56	116	440	24600	1.59e5	1.59e5	1.59e5	1.59e5	1.59e5	1.59e5	ERT_{best}/D
ALPS	11	32	16e + 0/1e5	•	•	•	•	•	•	•	ALPS [17]
AMaLGaM IDEA	13	16	2800	11e+0/1e6	•				•	•	AMaLGaM IDEA [4]
avg NEWUOA	21	38e+1/1e4	•	•	•				•	•	avg NEWUOA [31]
BayEDAcG	19	24e + 1/2e3								•	BayEDAcG [10]
BFGS	110	64e+1/8e3	•	•	•				•	•	BFGS [30]
BIPOP-CMA-ES	1	1.1	12e + 0/3e5								BIPOP-CMA-ES [15]
(1+1)-CMA-ES	4.1	33e+1/1e4		•	•	•	•		•	•	(1+1)-CMA-ES [2]
DASA	3.5	1	1	1	1	1	1	1	1	1	DASA [19]
DEPSO	3.1	28e + 1/2e3		•	•	•	•		•	•	DEPSO [12]
simple GA	92	39	420	11e + 0/1e5	•	•	•		•	•	simple GA [22]
iAMaLGaM IDEA	4	4.6	770	90e-1/1e6	•	•	•		•	•	iAMaLGaM IDEA [4]
NELDER (Han)	1.9	38e + 1/1e4		•	•	•	•		•	•	NELDER (Han) [16]
NEWUOA	7.7	46e + 1/7e3			•				•	•	NEWUOA [31]
(1+1)-ES	300	42e + 1/1e6		•	•	•	•		•	•	(1+1)-ES [1]
Monte Carlo	1.5e4	87e + 1/1e6		•	•	•	•		•	•	Monte Carlo [3]
IPOP-SEP-CMA-ES	1	1.2	16e+0/1e4	•	•			•	•	•	IPOP-SEP-CMA-ES [29]

Table 124: 40-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_4 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension **4 Skew Rastrigin-Bueche separable**

4 Skew Rastrigin-Bueche separable														
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$			
ERT_{best}/D	11	134	574	1.7e6	nan	nan	nan	nan	nan	nan	ERT_{best}/D			
ALPS	12	66	26e + 0/1e5	•	•						ALPS [17]			
AMaLGaM IDEA	24	18	32e + 0/1e6					•	•		AMaLGaM IDEA [4]			
avg NEWUOA	7.5	36e+1/3e4						•	•		avg NEWUOA [31]			
BayEDAcG	27	25e+1/2e3				•			•		BayEDAcG [10]			
BFGS	1200	97e + 1/1e4									BFGS [30]			
BIPOP-CMA-ES	1.1	3.9	27e + 0/3e5				•				BIPOP-CMA-ES [15]			
(1+1)-CMA-ES	16	54e+1/1e4	•								(1+1)-CMA-ES [2]			
DASA	2.5	1	1	1	20e-1/1e6		•	•			DASA [19]			
DEPSO	3.4	33e + 1/2e3	•		•				•		DEPSO [12]			
simple GA	85	39	2500	17e + 0/1e5			•				simple GA [22]			
iAMaLGaM IDEA	6.4	4.3	34e+0/1e6								iAMaLGaM IDEA [4]			
NELDER (Han)	110	63e+1/1e4	•		•				•		NELDER (Han) [16]			
NEWUOA	14	54e+1/2e4									NEWUOA [31]			
(1+1)-ES	2900	67e + 1/1e6					•				(1+1)-ES [1]			
Monte Carlo	6.3e5	11e + 2/1e6									Monte Carlo [3]			
IPOP-SEP-CMA-ES	1	5.3	30e + 0/1e4			•		•	•		IPOP-SEP-CMA-ES [29]			

mber o

Table 125: 40-D, running time excess ERT/ERT_{best} on f_5	, in italics is gi	ven the median	final function	value and the media	n number of
function evaluations to reach this value divided by dimension	on				

5 Linear slope														
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$														
ERT_{best}/D	0.025	2.13	2.45	2.89	3	3.01	3.01	3.01	3.01	3.01	ERT_{best}/D			
ALPS	1	81	140	160	180	200	210	220	230	230	ALPS [17]			
AMaLGaM IDEA	1	97	120	100	100	100	100	100	100	100	AMaLGaM IDEA [4]			
avg NEWUOA	1	3.1	3.1	3.2	3.4	3.4	3.4	3.4	3.4	3.4	avg NEWUOA [31]			
BayEDAcG	1	140	210	220	220	220	220	220	220	220	BayEDAcG [10]			
BFGS	1	1.4	2.1	2.2	2.2	2.2	2.2	2.2	2.2	2.2	BFGS [30]			
BIPOP-CMA-ES	1	3.2	4.5	4.5	4.4	4.4	4.4	4.4	4.4	4.4	BIPOP-CMA-ES [15]			
(1+1)-CMA-ES	1	1.9	3	3	2.9	3	3	3	3	3	(1+1)-CMA-ES [2]			
DASA	1	12	17	19	23	27	34	41	50	69	DASA [19]			
DEPSO	1	18	29	30	30	31	31	31	31	31	DEPSO [12]			
simple GA	1	1100	3e3	4800	7e3	9500	1.2e4	1.5e4	1.9e4	19e-8/1e5	simple GA [22]			
iAMaLGaM IDEA	1	5.6	8.1	7.4	7.2	7.1	7.1	7.1	7.1	7.1	iAMaLGaM IDEA [4]			
NELDER (Han)	1	9.1	14	13	13	13	13	13	13	13	NELDER (Han) [16]			
NEWUOA	1	1	1	1	1	1	1	1	1	1	NEWUOA [31]			
(1+1)-ES 1 1.8 2.9 3 2.9 2.9 2.9 2.9 2.9 2.9 1.9 $(1+1)$ -ES 1 1.8 1.8 1.9 														
Monte Carlo	1	36e + 1/1e6	•		•				•		Monte Carlo [3]			
IPOP-SEP-CMA-ES	1	3.3	5.2	5.4	5.3	5.2	5.3	5.3	5.3	5.3	IPOP-SEP-CMA-ES [29]			

Comparison Tables: BBOB 2009 Function Testbed

Table 126: 40-D, running time excess ERT/ERT_{best}	on f_6 ,	in italics i	s given	the median	final function	value and	the m	edian 1	number o
function evaluations to reach this value divided by dir	nensio	n							

6 Attractive sector													
$\Delta ftarget$	1e + 03	1e + 02	1e+01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$		
ERT_{best}/D	4.87	46	87.7	138	179	237	288	332	375	481	ERT_{best}/D		
ALPS	56	28	53	93	330	24e-3/1e5					ALPS [17]		
AMaLGaM IDEA	280	67	56	48	47	43	42	41	41	40	AMaLGaM IDEA [4]		
avg NEWUOA	4.7	1.5	1.3	1.3	1.2	1.2	1.1	1.2	1.1	1.1	avg NEWUOA [31]		
BayEDAcG	70	160	13e + 1/2e3								BayEDAcG [10]		
BFGS	1.9	3.3	4.2	4.4	4.6	4.5	4.5	4.6	4.9	18	BFGS [30]		
BIPOP-CMA-ES	6.1	1.9	1.6	1.5	1.5	1.4	1.4	1.4	1.4	1.4	BIPOP-CMA-ES [15]		
(1+1)-CMA-ES	3.6	6.6	360	12e + 0/1e4							(1+1)-CMA-ES [2]		
DASA	9	8.8	18	25	36	41	46	52	56	59	DASA [19]		
DEPSO	12	19	38e + 0/2e3				•			•	DEPSO [12]		
simple GA	350	730	65e + 0/1e5								simple GA [22]		
iAMaLGaM IDEA	26	9.4	10	9.9	11	10	10	11	11	11	iAMaLGaM IDEA [4]		
NELDER (Han)	3.3	2.7	2.7	2.5	2.6	2.8	3.5	5.5	16	68	NELDER (Han) [16]		
NEWUOA	1	1	1	1	1	1	1	1	1	1	NEWUOA [31]		
(1+1)-ES	3.1	1.9	3.2	4.6	6.1	6.8	7.4	8.1	8.6	9	(1+1)-ES [1]		
Monte Carlo	12e + 4/1e6										Monte Carlo [3]		
IPOP-SEP-CMA-ES	6.5	1.9	1.9	1.8	1.9	1.8	1.8	2	2	2	IPOP-SEP-CMA-ES [29]		

Table 127: 40-D, running time excess ERT/ERT_{best} on f_7 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

7 Step-ellipsoid															
$\Delta ftarget$	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$														
ERT_{best}/D	2.64	30.6	267	446	1030	1660	1660	1660	1660	1700	ERT_{best}/D				
ALPS	14	14	2e3	13e + 0/1e5							ALPS [17]				
AMaLGaM IDEA	14	12	2.5	2.2	1.3	1	1	1	1	1	AMaLGaM IDEA [4]				
avg NEWUOA	2.6	5.4	24e+0/4e4								avg NEWUOA [31]				
BayEDAcG	24	23	26e + 0/2e3					•			BayEDAcG [10]				
BFGS	20e + 2/100										BFGS [30]				
BIPOP-CMA-ES	1.5	1	1.2	8.3	4	2.6	2.6	2.6	2.6	2.5	BIPOP-CMA-ES [15]				
(1+1)-CMA-ES	1.8	73	100	12e + 0/1e4							(1+1)-CMA-ES [2]				
DASA	6	2200	76e + 0/2e5					•			DASA [19]				
DEPSO	4.9	7.5	27e + 0/2e3								DEPSO [12]				
simple GA	96	110	36e + 0/1e5								simple GA [22]				
iAMaLGaM IDEA	3.9	4	1	1	1	1.7	1.7	1.7	1.7	1.7	iAMaLGaM IDEA [4]				
NELDER (Han)	1.8	100	70e+0/1e4	•	•						NELDER (Han) [16]				
NEWUOA	1	880	77e+0/6e4					•	•		NEWUOA [31]				
(1+1)-ES	770	24e+1/1e6	•								(1+1)-ES [1]				
Monte Carlo	260	54e + 1/1e6	•								Monte Carlo [3]				
IPOP-SEP-CMA-ES	1.4	1	2.3	5.2	2.5	1.6	1.6	1.6	1.6	1.6	IPOP-SEP-CMA-ES [29]				

Table 128: 40-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_8 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension **8** Bosenbrock original

8 Rosenbrock original													
Δ ftarget	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$		
ERT_{best}/D	15.2	40.4	177	266	275	282	286	289	293	299	ERT_{best}/D		
ALPS	40	84	530	1100	1900	2e3	3200	14e-1/1e5			ALPS [17]		
AMaLGaM IDEA	27	20	47	40	41	42	43	43	43	44	AMaLGaM IDEA [4]		
avg NEWUOA	1.6	1.7	1.2	1.6	1.6	1.6	1.6	1.6	1.6	1.6	avg NEWUOA [31]		
BayEDAcG	38	50	87e+0/2e3					•			BayEDAcG [10]		
BFGS	1.1	1.7	2.4	2.3	2.3	2.3	2.3	2.2	2.2	2.2	BFGS [30]		
BIPOP-CMA-ES	1.8	1.7	7.3	7.7	7.9	7.9	7.9	7.9	7.9	7.8	BIPOP-CMA-ES [15]		
(1+1)-CMA-ES	1.2	1	8.3	8.3	8.6	8.7	8.8	8.8	8.8	8.9	(1+1)-CMA-ES [2]		
DASA	6.6	27	55	61	85	120	150	190	220	290	DASA [19]		
DEPSO	16	130	13e+1/2e3								DEPSO [12]		
simple GA	270	1200	91e + 0/1e5	-							simple GA [22]		
iAMaLGaM IDEA	11	7.5	17	15	15	15	16	16	16	16	iAMaLGaM IDEA [4]		
NELDER (Han)	2.4	4	150	280	550	540	530	530	520	510	NELDER (Han) [16]		
NEWUOA	1	1.4	1	1	1	1	1	1	1	1	NEWUOA [31]		
(1+1)-ES	1	5.5	27	67	73	85	100	120	130	170	(1+1)-ES [1]		
Monte Carlo	87e+3/1e6										Monte Carlo [3]		
IPOP-SEP-CMA-ES	1.6	2	9.7	9.1	9.2	9.1	9.1	9.1	9.1	9	IPOP-SEP-CMA-ES [29]		

Table 129: 40-D, running time excess ERT/ERT_{best} on f_9	, in italics is	given the mediar	final function	value and th	ne median	number o	of
function evaluations to reach this value divided by dimension	on						

9 Rosenbrock rotated														
Δ ftarget 1e+03 1e+02 1e+01 1e+00 1e-01 1e-02 1e-03 1e-04 1e-05 1e-07 Δ ftarget														
ERT_{best}/D	12.7	34.9	153	325	333	337	341	345	348	354	ERT_{best}/D			
ALPS	21	36	28e + 0/1e5						•		ALPS [17]			
AMaLGaM IDEA	28	18	54	32	34	35	35	36	36	37	AMaLGaM IDEA [4]			
avg NEWUOA	1.7	1.3	1.4	1.1	1.1	1.2	1.2	1.2	1.2	1.2	avg NEWUOA [31]			
BayEDAcG	38	26	38e+0/2e3								BayEDAcG [10]			
BFGS	1.1	1.4	2.7	1.6	1.6	1.6	1.6	1.6	1.6	1.6	BFGS [30]			
BIPOP-CMA-ES	1.8	1.5	8.2	6.2	6.4	6.5	6.5	6.5	6.5	6.5	BIPOP-CMA-ES [15]			
(1+1)-CMA-ES	1.2	1.2	9.7	9.7	10	10	10	10	10	10	(1+1)-CMA-ES [2]			
DASA	7.7	12	410	420	520	650	820	980	1100	1600	DASA [19]			
DEPSO	14	110	11e+1/2e3								DEPSO [12]			
simple GA	270	3500	11e+1/1e5								simple GA [22]			
iAMaLGaM IDEA	13	8.5	20	12	13	13	13	13	13	14	iAMaLGaM IDEA [4]			
NELDER (Han)	1.6	2.3	160	230	460	450	440	440	14e + 0/1e4		NELDER (Han) [16]			
NEWUOA	1	1	1	1	1	1	1	1	1	1	NEWUOA [31]			
(1+1)-ES	1.2	1.4	33	91	95	110	120	130	150	170	(1+1)-ES [1]			
Monte Carlo	83e+3/1e6										Monte Carlo [3]			
IPOP-SEP-CMA-ES	1.6	1.2	10	6.9	7.1	7.1	7.1	7.1	7.1	7.1	IPOP-SEP-CMA-ES [29]			

Table 130: 40-D, running time excess ERT/ERT_{best} on f_{10} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

10 Ellipsoid														
$ \Delta \text{ftarget} \qquad 1e+03 \qquad 1e+02 \qquad 1e+01 \qquad 1e+00 \qquad 1e-\overline{01} \qquad 1e-02 \qquad 1e-03 \qquad 1e-04 \qquad 1e-05 \qquad 1e-07 \qquad \Delta \text{ftarget} \\ \text{ERT} \qquad /D \qquad 165 \qquad 402 \qquad 647 \qquad 759 \qquad 920 \qquad 1290 \qquad 1400 \qquad 1520 \qquad 1630 \qquad 1770 \qquad \text{ERT} \qquad /D \\ \end{array} $														
ERT_{best}/D	165	402	647	759	920	1290	1400	1520	1630	1770	ERT_{best}/D			
ALPS 28e+2/1e5 ALPS [17] AMeLCoM UDEA 6.2 2.2 2.4 2.2 1.8 1.0 1.0 2.1 AMeLCoM UDEA [4]														
AMaLGaM IDEA 6.3 3.2 2.4 2.4 2.2 1.8 1.9 1.9 1.9 2.1 AMaLGaM IDEA														
avg NEWUOA 1.3 1.6 1.4 1.9 1.8 1.7 1.8 1.9 1.9 2.1 avg NEV														
BayEDAcG 16e+4/2e3														
BFGS 1.7 1.2 1 1 1 2.1 7.8 34 220 40e-6/1e5 BFGS [30]														
BIPOP-CMA-ES 3.6 2.3 1.9 1.9 1.7 1.3 1.2 1.2 1.1 1 BIPOP-CMA-ES														
(1+1)-CMA-ES	2.8	2	1.7	1.7	1.6	1.3	1.2	1.1	1.1	1	(1+1)-CMA-ES [2]			
DASA	290	1e3	2.3e4	23e+0/1e6							DASA [19]			
DEPSO	14e + 4/2e3										DEPSO [12]			
simple GA	83e+3/1e5	•	-								simple GA [22]			
iAMaLGaM IDEA	2.9	1.9	1.4	1.4	1.3	1	1	1	1	1.1	iAMaLGaM IDEA [4]			
NELDER (Han)	5.9	35e+1/1e4									NELDER (Han) [16]			
NEWUOA	1	1	1.2	1.6	1.8	1.5	1.7	1.8	1.9	2.1	NEWUOA [31]			
(1+1)-ES	46	130	260	430	580	620	1e3	1600	33e-5/1e6		(1+1)-ES [1]			
Monte Carlo	13e + 5/1e6										Monte Carlo [3]			
IPOP-SEP-CMA-ES	IPOP-SEP-CMA-ES 6.2 3.8 2.9 2.7 2.4 1.8 1.7 1.5 1.5 1.4 IPOP-SEP-CMA-ES [29]													

Table 131: 40-D, running time excess ERT/ERT_{best} on f_{11} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

11 Discus													
$\Delta ftarget$	1e+03	1e+02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$		
ERT_{best}/D	1.78	22.6	59.2	121	292	562	674	769	888	1090	ERT_{best}/D		
ALPS	2.7	240	970	33e-1/1e5							ALPS [17]		
AMaLGaM IDEA	2.6	11	9.5	6.8	3.8	2.5	2.4	2.5	2.5	2.5	AMaLGaM IDEA [4]		
avg NEWUOA	3.4	5.5	3.9	2.8	1.5	1	1	1	1	1	avg NEWUOA [31]		
BayEDAcG	2.3	26e + 1/2e3									BayEDAcG [10]		
BFGS	2.8	1	1	1	1	2.5	72	29e-4 /1e4			BFGS [30]		
BIPOP-CMA-ES	99	35	15	8	3.5	1.9	1.6	1.5	1.3	1.1	BIPOP-CMA-ES [15]		
(1+1)-CMA-ES	21	9.8	7.1	5.5	3.1	2.1	2.2	2.3	2.4	2.6	(1+1)-CMA-ES [2]		
DASA	1	230	590	790	500	440	490	540	630	1e3	DASA [19]		
DEPSO	6	24e + 1/2e3			•					•	DEPSO [12]		
simple GA	3.5	820	43e + 0/1e5								simple GA [22]		
iAMaLGaM IDEA	1.8	8.5	5	3.3	1.8	1.1	1.1	1.1	1.1	1.1	iAMaLGaM IDEA [4]		
NELDER (Han)	1.6	88	53e + 0/1e4				•				NELDER (Han) [16]		
NEWUOA	1	18	13	9.9	4.9	3.2	3	3	3	3	NEWUOA [31]		
(1+1)-ES	2300	1100	870	650	350	240	240	240	240	250	(1+1)-ES [1]		
Monte Carlo	2.4	20e + 1/1e6									Monte Carlo [3]		
IPOP-SEP-CMA-ES	130	57	25	13	5.7	3	2.6	2.3	2.1	1.7	IPOP-SEP-CMA-ES [29]		

Table 132: 40-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{12} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

12 Bent cigar													
$\Delta ftarget$	1e + 03	1e + 02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$		
ERT_{best}/D	36	39.9	104	186	229	269	329	526	569	630	ERT_{best}/D		
ALPS	67	81	180	690	8100	83e-2/1e5	•				ALPS [17]		
AMaLGaM IDEA	46	48	21	13	14	16	17	13	14	15	AMaLGaM IDEA [4]		
avg NEWUOA	1.5	6.5	21	24	31	38	42	32	39	86	avg NEWUOA [31]		
BayEDAcG	66	44e+1/2e3			•						BayEDAcG [10]		
BFGS	1	1.1	1	1	1	1	1	4.6	15	660	BFGS [30]		
BIPOP-CMA-ES	2.1	2.8	2.2	2.3	2.5	2.5	2.5	1.8	1.9	1.9	BIPOP-CMA-ES [15]		
(1+1)-CMA-ES	1.4	1.7	2.1	3.1	4.1	4.4	4.6	3.4	3.6	4.1	(1+1)-CMA-ES [2]		
DASA	20	27	3.8e4	3.5e4	22e + 0/1e6						DASA [19]		
DEPSO	12e+4 /2e3										DEPSO [12]		
simple GA	40e+3/1e5										simple GA [22]		
iAMaLGaM IDEA	17	18	8.6	6.4	7	7.3	7.2	5.2	5.4	5.7	iAMaLGaM IDEA [4]		
NELDER (Han)	2.4	2.5	15	24	52	190	42e-3/1e4				NELDER (Han) [16]		
NEWUOA	1	1	1.4	1.4	1.4	1.5	1.4	1	1	1	NEWUOA [31]		
(1+1)-ES	1.2	1300	4800	7700	14e-1/1e6						(1+1)-ES [1]		
Monte Carlo	16e + 7/1e6		-								Monte Carlo [3]		
IPOP-SEP-CMA-ES	1.8	2.8	2.8	3.6	4.2	4.2	3.9	2.7	2.7	2.7	IPOP-SEP-CMA-ES [29]		

Table 133: 40-D, running time excess ERT/ERT_{best} on f_{13} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension 13 Sharp ridge

	10 Sharp Huge													
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget			
ERT_{best}/D	3.73	9.74	50.7	173	218	297	1800	2100	2460	2990	ERT_{best}/D			
ALPS	80	180	130	190	860	85e-3/1e5					ALPS [17]			
AMaLGaM IDEA	88	93	28	12	12	10	2	2	1.9	1.9	AMaLGaM IDEA [4]			
BayEDAcG	100	160	52e + 0/2e3								BayEDAcG [10]			
BFGS	1.2	1.8	1.4	1	1	1	46	73	16e-4/4e4		BFGS [30]			
BIPOP-CMA-ES	4.6	5.1	2.6	2.6	5	17	4.4	5.2	5.3	5.9	BIPOP-CMA-ES [15]			
(1+1)-CMA-ES	3.3	3.3	1.7	4.2	9.5	20	5.6	9.7	18	48	(1+1)-CMA-ES [2]			
DASA	15	24	40	73	150	540	220	940	2900	21e-5/1e6	DASA [19]			
DEPSO	21	1500	12e + 1/2e3								DEPSO [12]			
simple GA	540	6800	91e + 0/1e5								simple GA [22]			
iAMaLGaM IDEA	25	33	11	4.5	4.7	4.8	1	1	1	1	iAMaLGaM IDEA [4]			
NELDER (Han)	4.8	5.9	9.8	20	71	160	41	13e-2/1e4			NELDER (Han) [16]			
NEWUOA	1	1	1	2	3	13	7.3	15	28	88e-5/1e4	NEWUOA [31]			
(1+1)-ES	2.9	3.3	4.7	4.5	18	36	11	37	100	1400	(1+1)-ES [1]			
Monte Carlo	21e+2/1e6										Monte Carlo [3]			
IPOP-SEP-CMA-ES	4.4	4.6	2.1	2.8	6.3	8.2	2.6	2.8	2.8	2.9	IPOP-SEP-CMA-ES [29]			

of

Table 134: 40-D, running time excess ERT/ERT_{best} on f_{14} , in italics is given the median final function value and the median number of
function evaluations to reach this value divided by dimension
14 Sum of different news

14 Sum of different powers													
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget		
ERT_{best}/D	0.025	1.01	7.61	15.7	19.4	27.6	55.2	90.6	121	1440	ERT_{best}/D		
ALPS	1	2.4	38	59	80	140	510	27e-5/1e5			ALPS [17]		
AMaLGaM IDEA	1.1	2.2	44	46	53	50	30	22	20	2.1	AMaLGaM IDEA [4]		
BayEDAcG	1	3.3	74	89	180	63e-3/2e3		•			BayEDAcG [10]		
BFGS	1	2.4	1.7	1.6	1.8	1.7	1.2	1	1	29e-7/2e4	BFGS [30]		
BIPOP-CMA-ES	1	1.1	2.7	2.5	3.1	3.9	4.4	5.4	6.6	1.1	BIPOP-CMA-ES [15]		
(1+1)-CMA-ES	1	2.3	2.1	1.7	2	2.2	2.2	3.2	5.3	1	(1+1)-CMA-ES [2]		
DASA	1	4.8	8.7	8.6	13	22	71	500	4600	58e-7/1e6	DASA [19]		
DEPSO	1.1	1.7	11	28	300	11e-2/2e3					DEPSO [12]		
simple GA	1	3.3	280	390	1.1e4	17e-2/1e5					simple GA [22]		
iAMaLGaM IDEA	1	1	13	15	19	19	12	9.2	8.6	1	iAMaLGaM IDEA [4]		
NELDER (Han)	1	2.9	2.5	2.8	3	3.4	3.4	11	40e-6/1e4		NELDER (Han) [16]		
NEWUOA	1.2	2	1	1	1	1	1	2	8.6	24	NEWUOA [31]		
(1+1)-ES	1.2	2	1.9	1.6	1.8	2.2	5.2	37	400	81e-8/1e6	(1+1)-ES [1]		
Monte Carlo	1.1	1.9	29e + 0/1e6			•				•	Monte Carlo [3]		
IPOP-SEP-CMA-ES	1	1.1	2.4	2.3	2.9	3.7	6.8	8.8	10	1.5	IPOP-SEP-CMA-ES [29]		

Comparison Tables: BBOB 2009 Function Testbed

Table 135: 40-D, running time excess ERT/ERT_{best} on f_{15} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

15 Rastrigin												
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$	
ERT_{best}/D	4.79	190	4700	19700	26200	26600	27000	27300	27700	28400	ERT_{best}/D	
ALPS	12	1100	10e + 1/1e5								ALPS [17]	
AMaLGaM IDEA	13	9.6	1.9	1.5	1.6	1.6	1.6	1.6	1.6	1.7	AMaLGaM IDEA [4]	
BayEDAcG	23	24e + 1/2e3									BayEDAcG [10]	
BFGS	28	53e+1/9e3									BFGS [30]	
BIPOP-CMA-ES	1.2	1	1.4	1	1	1	1	1	1	1	BIPOP-CMA-ES [15]	
(1+1)-CMA-ES	5.1	34e + 1/1e4									(1+1)-CMA-ES [2]	
DASA	640	39e + 1/1e6									DASA [19]	
DEPSO	3.7	35e+1/2e3									DEPSO [12]	
simple GA	100	2200	11e + 1/1e5								simple GA [22]	
iAMaLGaM IDEA	3.9	2.9	9.8	14	11	11	11	11	10	10	iAMaLGaM IDEA [4]	
NELDER (Han)	1.6	33e+1/1e4									NELDER (Han) [16]	
NEWUOA	7.4	37e+1/7e3									NEWUOA [31]	
(1+1)-ES	450	42e + 1/1e6									(1+1)-ES [1]	
Monte Carlo	3.6e4	91e + 1/1e6									Monte Carlo [3]	
IPOP-SEP-CMA-ES	1	1.3	1	3.6	40e-1/1e4						IPOP-SEP-CMA-ÉS [29]	

Table 136: 40-D running time excess EBT/EBT, f_{10} on f_{10} in italics is given the median final function value and the median number of
Table 150. 40 D, running time excess Ditr/Ditr best on J16, in tranes is given the median man function value and the median number of
function evaluations to reach this value divided by dimension

16 Weierstrass												
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$	
ERT_{best}/D	0.025	0.025	131	1800	8040	17800	35200	49300	49700	50500	ERT_{best}/D	
ALPS	1	1.1	11	38e-1/1e5							ALPS [17]	
AMaLGaM IDEA	1	1.1	17	3.4	3.6	4.8	3.4	3.1	3.1	3.8	AMaLGaM IDEA [4]	
BayEDAcG	1	1.3	31e + 0/2e3								BayEDAcG [10]	
BFGS	1	3.7	41e+0/2e4								BFGS [30]	
BIPOP-CMA-ES	1	1.1	1	1	1	1.3	1	1	1	1	BIPOP-CMA-ES [15]	
(1+1)-CMA-ES	1	1.1	550	12e + 0/1e4							(1+1)-CMA-ES [2]	
DASA	1	1.2	1.1e5	13e + 0/1e6							DASA [19]	
DEPSO	1	1.2	35e+0/2e3								DEPSO [12]	
simple GA	1	1.1	260	79e-1/1e5							simple GA [22]	
iAMaLGaM IDEA	1	1.1	3.1	4.3	24	27	17	23	27	27	iAMaLGaM IDEA [4]	
NELDER (Han)	1	1.1	95	10e + 0/1e4							NELDER (Han) [16]	
NEWUOA	1	1.2	17	78e-1/1e4							NEWUOA [31]	
(1+1)-ES	1	1	15e + 0/1e6								(1+1)-ES [1]	
Monte Carlo	1	1.1	22e+0/1e6								Monte Carlo [3]	
IPOP-SEP-CMA-ES	1	1.1	1.8	1.5	1	1	1.4	3	30e-3/1e4		IPOP-SEP-CMA-ES [29]	

Table 137: 40-D, running time excess ERT/ERT_{best} on f_{17} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

17 Schaffer F7, condition 10													
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$		
ERT_{best}/D	0.025	0.025	9.98	106	354	874	1300	2220	3330	6640	ERT_{best}/D		
ALPS	1	1.1	7	3800	12e-1/1e5						ALPS [17]		
AMaLGaM IDEA	1	1.3	13	9.3	4.9	3	2.6	1.9	1.6	4.5	AMaLGaM IDEA [4]		
BayEDAcG	1	1.1	22	14	47e-2/2e3						BayEDAcG [10]		
BFGS	1	5.6	410	68e-1/3e4							BFGS [30]		
BIPOP-CMA-ES	1	1	1	1	1	1	1	1	1	1.4	BIPOP-CMA-ES [15]		
(1+1)-CMA-ES	1	1	67	68e-1/1e4							(1+1)-CMA-ES [2]		
DASA	1	4.2	9.4e4	98e-1/1e6							DASA [19]		
DEPSO	1	1.2	4	31	97e-2/2e3						DEPSO [12]		
simple GA	1	1.3	63	230	89e-2/1e5						simple GA [22]		
iAMaLGaM IDEA	1	1.4	5.2	2.6	1.5	1	54	110	100	62	iAMaLGaM IDEA [4]		
NELDER (Han)	1	1.7	310	77e-1/1e4							NELDER (Han) [16]		
NEWUOA	1	1.9	38	54e-1/1e5							NEWUOA [31]		
(1+1)-ES	1	7.4	5.6e4	80e-1/1e6							(1+1)-ES [1]		
Monte Carlo	1	1.1	2.2e4	91e-1/1e6							Monte Carlo [3]		
IPOP-SEP-CMA-ES	1	1.2	1	2.1	2.4	1.6	1.6	1.3	1.3	1	IPOP-SEP-CMA-ES [29]		

Table 138: 40-D, running time excess ERT/ERT_{best} on f_{18} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

			18	8 Schaffer	F7, condit	tion 10	000				
Δ ftarget	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$
ERT_{best}/D	0.025	0.403	36.1	425	1180	3180	4690	6420	16800	23700	ERT_{best}/D
ALPS	1	1	38	39e-1/1e5							ALPS [17]
AMaLGaM IDEA	1	1.1	18	3.3	1.9	1	2.2	3	2.6	5	AMaLGaM IDEA [4]
BayEDAcG	1	1.1	23	35	16e-1/2e3						BayEDAcG [10]
BFGS	3.7	620	28e+0/3e4								BFGS [30]
BIPOP-CMA-ES	1.1	2.9	1.1	1.1	1.4	1.1	1.1	1.2	1.2	1.1	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	3.1	25e+0/1e4								(1+1)-CMA-ES [2]
DASA	1	13	41e+0/1e6								DASA [19]
DEPSO	1.1	1.5	25	57e-1/2e3							DEPSO [12]
simple GA	1.1	1.3	100	46e-1/1e5							simple GA [22]
iAMaLGaM IDEA	1.1	1.1	4.6	1	1	9	52	54	44	43	iAMaLGaM IDEA [4]
NELDER (Han)	1.1	12	29e + 0/1e4								NELDER (Han) [16]
NEWUOA	1.1	4.2	20e + 0/1e5								NEWUOA [31]
(1+1)-ES	1	100	35e+0/1e6								(1+1)-ES [1]
Monte Carlo	1	1	32e + 0/1e6								Monte Carlo [3]
IPOP-SEP-CMA-ES	1	2.2	1	1.3	1.7	1.1	1	1	1	1	IPOP-SEP-CMA-ES [29]
Table 139: 40-D, running time excess ERT/ERT_{best} on f_{19} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

19 Griewank-Rosenbrock F8F2													
$\Delta ftarget$	1e+03	1e+02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$		
ERT_{best}/D	0.025	0.025	8.79	1410	34800	4.21e5	6.38e5	1.13e6	1.13e6	1.14e6	ERT_{best}/D		
ALPS	1	1.2	6.5	620	16e-1/1e5						ALPS [17]		
AMaLGaM IDEA	1	1	11	2.4	1	2.6	7.4	4.2	4.2	4.2	AMaLGaM IDEA [4]		
BayEDAcG	1	1.1	18	57e-1/2e3							BayEDAcG [10]		
BFGS	1	1	19e + 0/2e4			•	•		•	•	BFGS [30]		
BIPOP-CMA-ES	1	1	1.1	1	1.2	1	1	1	1	1	BIPOP-CMA-ES [15]		
(1+1)-CMA-ES	1	1	16	38e-1/1e4		•	•	•	•	•	(1+1)-CMA-ES [2]		
DASA	1	1	1.6e6	16e + 0/1e6		•	•		•	•	DASA [19]		
DEPSO	1	1.1	3.9	67e-1/2e3		•	•	•	•	•	DEPSO [12]		
simple GA	1	1.1	130	1e3	24e-1/1e5	•	•		•	•	simple GA [22]		
iAMaLGaM IDEA	1	1.1	7	11	46	10e-2/1e6	•	•	•		iAMaLGaM IDEA [4]		
NELDER (Han)	1	1	12	40e-1/1e4		•	•		•	•	NELDER (Han) [16]		
NEWUOA	1	1.2	1	28e-1/1e5		•	•	•	•	•	NEWUOA [31]		
(1+1)-ES	1	1.4	7.7e5	16e + 0/1e6		•	•	•	•		(1+1)-ES [1]		
Monte Carlo	1	1.1	14e + 0/1e6				•		•	•	Monte Carlo [3]		
IPOP-SEP-CMA-ES	1	1	1.1	4.6	84e-2/1e4	•	•	•	•	•	IPOP-SEP-CMA-ES [29]		

ber of

Table 140: 40-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{20} , in italics is given the median final function value and the median number of												
function evaluations to reach this value divided by dimension												
20 Sobword x^{*} sin(x)												

20 Schwefel x*sin(x)												
$\Delta ftarget$	1e + 03	1e+02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$	
ERT_{best}/D	3.12	4.33	5.54	3280	4.03e6	nan	nan	nan	nan	nan	ERT_{best}/D	
ALPS	45	44	40	13e-1/1e5	•	•				•	ALPS [17]	
AMaLGaM IDEA	74	62	52	1400	11e-1/1e6						AMaLGaM IDEA [4]	
BayEDAcG	85	75	64	34e-1/2e3							BayEDAcG [10]	
BFGS	1.6	1.5	1.5	33	11e-1/3e4					•	BFGS [30]	
BIPOP-CMA-ES	5.4	4.6	4.1	22	1	17e-2/6e5					BIPOP-CMA-ES [15]	
(1+1)-CMA-ES	3.6	3.1	2.7	14e-1/1e4			•	•	•	•	(1+1)-CMA-ES [2]	
DASA	18	16	14	1	57e-2/1e6					•	DASA [19]	
DEPSO	20	21	22	30e-1 /2e3						•	DEPSO [12]	
simple GA	630	570	510	2.9	65e-2/1e5					•	simple GA [22]	
iAMaLGaM IDEA	31	28	23	15e-1/1e6			•	•	•	•	iAMaLGaM IDEA [4]	
NELDER (Han)	4.8	4.6	4.1	14e-1/1e4					•		NELDER (Han) [16]	
NEWUOA	1	1	1	310	11e-1/3e4					•	NEWUOA [31]	
(1+1)-ES	3.4	3	2.6	1400	12e-1/1e6						(1+1)-ES [1]	
Monte Carlo	28e + 3/1e6						•	•	•	•	Monte Carlo [3]	
IPOP-SEP-CMA-ES	4.6	4	3.5	16e-1/1e4							IPOP-SEP-CMA-ES [29]	

Table 141: 40-D, running time excess ERT/ERT_{best} on f_{21} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	21 Gallagher 101 peaks													
	Δ ftarget	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$		
]	ERT _{best} /D	0.025	0.025	26.1	529	2520	2530	2530	2540	2550	2560	ERT_{best}/D		
	ALPS	1	1	20	6.5	2.7	3	3.3	3.7	4.2	5.9	ALPS [17]		
AM	aLGaM IDEA	1	1	21	1800	1700	1700	1700	1700	1700	1700	AMaLGaM IDEA [4]		
	BayEDAcG	1	1	37	8	13e-1/2e3						BayEDAcG [10]		
	BFGS	1	1	2.9	2.3	2.1	2.1	2.1	2.1	2.1	9.3	BFGS [30]		
BII	POP-CMA-ES	1	1	2.7	49	110	110	110	110	110	110	BIPOP-CMA-ES [15]		
(1	+1)-CMA-ES	1	1	4.1	1.8	1.7	1.7	1.7	1.7	1.6	1.6	(1+1)-CMA-ES [2]		
	DASA	1	1	46	44	27	27	27	27	27	27	DASA [19]		
	DEPSO	1	1	18	16	12	33e-1 /2e3					DEPSO [12]		
	simple GA	1	1	120	770	560	25e-1/1e5					simple GA [22]		
iAN	IaLGaM IDEA	1	1	38	660	850	850	850	840	840	840	iAMaLGaM IDEA [4]		
NE	ELDER (Han)	1	1	13	14	5.6	5.5	5.5	5.5	5.5	5.5	NELDER (Han) [16]		
	NEWUOA	1	1	1	1	1	1	1	1	1	1	NEWUOA [31]		
	(1+1)-ES	1	1	3.6	5.2	2.8	2.8	2.8	2.8	2.8	2.8	(1+1)-ES [1]		
ľ	Monte Carlo	1	1	69e + 0/1e6								Monte Carlo [3]		
IPOI	P-SEP-CMA-ES	1	1	3.4	19	16	16	16	16	16	16	IPOP-SEP-CMA-ES [29]		

Table 142: 40-D, running time excess ERT/ERT_{best} on f_{22} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

22 Gallagher 21 peaks													
$\Delta ftarget$	1e+03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$		
ERT_{best}/D	0.025	0.025	116	886	16200	16200	16300	16300	16300	16400	ERT_{best}/D		
ALPS	1	1	8.5	12	35	110	69e-2/1e5				ALPS [17]		
AMaLGaM IDEA	1	1	2200	760	69e-2/1e6						AMaLGaM IDEA [4]		
BayEDAcG	1	1	18	10	73e-1/2e3						BayEDAcG [10]		
BFGS	1	1	1	1.5	69e-2/8e3						BFGS [30]		
BIPOP-CMA-ES	1	1	6.4	60	69e-2/1e5						BIPOP-CMA-ES [15]		
(1+1)-CMA-ES	1	1	2.7	1.8	2	2	2	2	2	2	(1+1)-CMA-ES [2]		
DASA	1	1	32	31	45	45	45	45	45	45	DASA [19]		
DEPSO	1	1	7.3	10	26e-1/2e3	•					DEPSO [12]		
simple GA	1	1	87	180	20e-1/1e5	-		-	•	-	simple GA [22]		
iAMaLGaM IDEA	1	1	370	760	69e-2/1e6						iAMaLGaM IDEA [4]		
NELDER (Han)	1	1	4.7	3.8	9	9	9	8.9	8.9	8.9	NELDER (Han) [16]		
NEWUOA	1	1	2.7	1	1	1	1	1	1	1	NEWUOA [31]		
(1+1)-ES	1	1	3.3	2.7	6.6	6.6	6.6	6.6	6.6	6.6	(1+1)-ES [1]		
Monte Carlo	1	1	71e+0/1e6								Monte Carlo [3]		
IPOP-SEP-CMA-ES	1	1	13	6	69e-2/1e4						IPOP-SEP-CMA-ES [29]		

Table 143: 40-D, running time excess ERT/ERT_{best} on f_{23} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

23 Katsuuras												
$\Delta ftarget$	1e + 03	1e + 02	1e + 01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$	
ERT_{best}/D	0.025	0.025	0.237	298	1890	16500	32000	79000	81100	84000	ERT_{best}/D	
ALPS	1	1	1	150	80e-2/1e5						ALPS [17]	
AMaLGaM IDEA	1	1	1.1	12	2.5	1	1	1	1	1	AMaLGaM IDEA [4]	
BayEDAcG	1	1	1.1	37e-1/2e3							BayEDAcG [10]	
BFGS	1	1	58	260	30e-1/5e3						BFGS [30]	
BIPOP-CMA-ES	1	1	5.6	4.8	1	1.6	2	1.4	1.4	1.4	BIPOP-CMA-ES [15]	
(1+1)-CMA-ES	1	1	12	12	82e-2/1e4					-	(1+1)-CMA-ES [2]	
DASA	1	1	1.5	76	68e-2/6e5						DASA [19]	
DEPSO	1	1	1.2	44e-1/2e3							DEPSO [12]	
simple GA	1	1	1.1	440	79e-2/1e5					-	simple GA [22]	
iAMaLGaM IDEA	1	1	1.1	2.3	1.1	3.1	12	8.1	8	7.7	iAMaLGaM IDEA [4]	
NELDER (Han)	1	1	1.3	1	29e-2/1e4						NELDER (Han) [16]	
NEWUOA	1	1	7.1	1.8	46e-2/8e3						NEWUOA [31]	
(1+1)-ES	1	1	24	280	73e-2/1e6						(1+1)-ES [1]	
Monte Carlo	1	1	1.4	22e-1/1e6							Monte Carlo [3]	
IPOP-SEP-CMA-ES	1	1	6.2	4.9	6.3	89e-3/1e4					IPOP-SEP-CMA-ES [29]	

Table 144: 40-D, running time excess ERT/ERT_{best} on f_{24} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	24 Lunacek bi-Rastrigin													
Δ ftarget	1e + 03	1e + 02	1e + 01	1e + 00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta ftarget$			
ERT_{best}/D	2.06	967	1.46e5	2.45e6	7.5e6	7.51e6	7.51e6	7.51e6	7.51e6	7.51e6	ERT_{best}/D			
ALPS	5.8	82	91e + 0/1e5								ALPS [17]			
AMaLGaM IDEA	13	4.2	17	42e+0/1e6	•	•	•	•	•	•	AMaLGaM IDEA [4]			
BayEDAcG	15	28e + 1/2e3						•		•	BayEDAcG [10]			
BFGS	560	89e+1/8e3		•	•		•	•	•	•	BFGS [30]			
BIPOP-CMA-ES	2.3	12	4.6	1	1	1	1	1	1	1	BIPOP-CMA-ES [15]			
(1+1)-CMA-ES	2.3	34e + 1/1e4			•			•	•	•	(1+1)-CMA-ES [2]			
DASA	3200	55e+1/1e6			•	•	•	•	•	•	DASA [19]			
DEPSO	6.6	37e+1/2e3		•	•		•	•	•	•	DEPSO [12]			
simple GA	110	1500	14e + 1/1e5			•					simple GA [22]			
iAMaLGaM IDEA	6.6	1	8.5	10e + 0/1e6	•		•	•	•	•	iAMaLGaM IDEA [4]			
NELDER (Han)	28	64e + 1/1e4						•		•	NELDER (Han) [16]			
NEWUOA	1	25e+1/9e3		•	•		•	•	•	•	NEWUOA [31]			
(1+1)-ES	1700	49e + 1/1e6				•					(1+1)-ES [1]			
Monte Carlo	650	82e + 1/1e6									Monte Carlo [3]			
IPOP-SEP-CMA-ES	2.3	1.5	1	46e+0/1e4							IPOP-SEP-CMA-ES [29]			

References

- Anne Auger. Benchmarking the (1+1) evolution strategy with one-fifth success rule on the BBOB-2009 function testbed. In Rothlauf [32], pages 2447-2452.
- [2] Anne Auger and Nikolaus Hansen. Benchmarking the (1+1)-CMA-ES on the BBOB-2009 function testbed. In Rothlauf [32], pages 2459–2466.
- [3] Anne Auger and Raymond Ros. Benchmarking the pure random search on the BBOB-2009 testbed. In Rothlauf [32], pages 2479–2484.
- [4] Peter A. N. Bosman, Jörn Grahl, and Dirk Thierens. AMaLGaM IDEAs in noiseless black-box optimization benchmarking. In Rothlauf [32], pages 2247–2254.
- [5] Benjamin Doerr, Mahmoud Fouz, Martin Schmidt, and Magnus Wahlström. BBOB: Nelder-Mead with resize and halfruns. In Rothlauf [32], pages 2239–2246.
- [6] Mohammed El-Abd and Mohamed S. Kamel. Black-box optimization benchmarking for noiseless function testbed using an EDA and PSO hybrid. In Rothlauf [32], pages 2263–2268.
- [7] Mohammed El-Abd and Mohamed S. Kamel. Black-box optimization benchmarking for noiseless function testbed using particle swarm optimization. In Rothlauf [32], pages 2269–2274.
- [8] Mohammed El-Abd and Mohamed S. Kamel. Black-box optimization benchmarking for noiseless function testbed using PSO_Bounds. In Rothlauf [32], pages 2275–2280.
- [9] S. Finck, N. Hansen, R. Ros, and A. Auger. Real-parameter black-box optimization benchmarking 2009: Presentation of the noiseless functions. Technical Report 2009/20, Research Center PPE, 2009.
- [10] Marcus Gallagher. Black-box optimization benchmarking: results for the BayEDAcG algorithm on the noiseless function testbed. In Rothlauf [32], pages 2281–2286.
- [11] Carlos García-Martínez and Manuel Lozano. A continuous variable neighbourhood search based on specialised EAs: application to the noiseless BBO-benchmark 2009. In Rothlauf [32], pages 2287–2294.
- [12] José García-Nieto, Enrique Alba, and Javier Apolloni. Noiseless functions black-box optimization: evaluation of a hybrid particle swarm with differential operators. In Rothlauf [32], pages 2231–2238.
- [13] N. Hansen, A. Auger, S. Finck, and R. Ros. Real-parameter black-box optimization benchmarking 2009: Experimental setup. Technical Report RR-6828, INRIA, 2009.
- [14] N. Hansen, S. Finck, R. Ros, and A. Auger. Real-parameter black-box optimization benchmarking 2009: Noiseless functions definitions. Technical Report RR-6829, INRIA, 2009.

- [15] Nikolaus Hansen. Benchmarking a BI-population CMA-ES on the BBOB-2009 function testbed. In Rothlauf [32], pages 2389–2396.
- [16] Nikolaus Hansen. Benchmarking the Nelder-Mead downhill simplex algorithm with many local restarts. In Rothlauf [32], pages 2403–2408.
- [17] Gregory S. Hornby. The age-layered population structure (ALPS) evolutionary algorithm. http://coco.gforge.inria.fr/doku.php?id=bbob-2009-results, July 2009. Noiseless testbed.
- [18] Waltraud Huyer and Arnold Neumaier. Benchmarking of MCS on the noiseless function testbed. http://www.mat.univie.ac.at/~neum/papers.html, 2009. P. 989.
- [19] Peter Korosec and Jurij Silc. A stigmergy-based algorithm for black-box optimization: noiseless function testbed. In Rothlauf [32], pages 2295–2302.
- [20] Jirí Kubalik. Black-box optimization benchmarking of prototype optimization with evolved improvement steps for noiseless function testbed. In Rothlauf [32], pages 2303–2308.
- [21] Daniel Molina, Manuel Lozano, and Francisco Herrera. A memetic algorithm using local search chaining for black-box optimization benchmarking 2009 for noise free functions. In Rothlauf [32], pages 2255–2262.
- [22] Miguel Nicolau. Application of a simple binary genetic algorithm to a noiseless testbed benchmark. In Rothlauf [32], pages 2473–2478.
- [23] László Pál, Tibor Csendes, Mihály Csaba Markót, and Arnold Neumaier. BBO-benchmarking of the GLOBAL method for the noiseless function testbed. http://www.mat.univie.ac.at/~neum/papers.html, 2009. P. 986.
- [24] Petr Pošík. BBOB-benchmarking a simple estimation of distribution algorithm with Cauchy distribution. In Rothlauf [32], pages 2309–2314.
- [25] Petr Pošík. BBOB-benchmarking the DIRECT global optimization algorithm. In Rothlauf [32], pages 2315–2320.
- [26] Petr Pošík. BBOB-benchmarking the generalized generation gap model with parent centric crossover. In Rothlauf [32], pages 2321–2328.
- [27] Petr Pošík. BBOB-benchmarking the Rosenbrock's local search algorithm. In Rothlauf [32], pages 2337–2342.
- [28] Petr Pošík. BBOB-benchmarking two variants of the line-search algorithm. In Rothlauf [32], pages 2329–2336.
- [29] Raymond Ros. Benchmarking sep-CMA-ES on the BBOB-2009 function testbed. In Rothlauf [32], pages 2435–2440.
- [30] Raymond Ros. Benchmarking the BFGS algorithm on the BBOB-2009 function testbed. In Rothlauf [32], pages 2409–2414.

- [31] Raymond Ros. Benchmarking the NEWUOA on the BBOB-2009 function testbed. In Rothlauf [32], pages 2421–2428.
- [32] Franz Rothlauf, editor. Genetic and Evolutionary Computation Conference, GECCO 2009, Proceedings, Montreal, Québec, Canada, July 8-12, 2009, Companion Material. ACM, 2009.



Centre de recherche INRIA Saclay – Île-de-France Parc Orsay Université - ZAC des Vignes 4, rue Jacques Monod - 91893 Orsay Cedex (France)

Centre de recherche INRIA Bordeaux – Sud Ouest : Domaine Universitaire - 351, cours de la Libération - 33405 Talence Cedex Centre de recherche INRIA Grenoble – Rhône-Alpes : 655, avenue de l'Europe - 38334 Montbonnot Saint-Ismier Centre de recherche INRIA Lille – Nord Europe : Parc Scientifique de la Haute Borne - 40, avenue Halley - 59650 Villeneuve d'Ascq Centre de recherche INRIA Nancy – Grand Est : LORIA, Technopôle de Nancy-Brabois - Campus scientifique 615, rue du Jardin Botanique - BP 101 - 54602 Villers-lès-Nancy Cedex Centre de recherche INRIA Paris – Rocquencourt : Domaine de Voluceau - Rocquencourt - BP 105 - 78153 Le Chesnay Cedex Centre de recherche INRIA Rennes – Bretagne Atlantique : IRISA, Campus universitaire de Beaulieu - 35042 Rennes Cedex Centre de recherche INRIA Sophia Antipolis – Méditerranée : 2004, route des Lucioles - BP 93 - 06902 Sophia Antipolis Cedex

> Éditeur INRIA - Domaine de Voluceau - Rocquencourt, BP 105 - 78153 Le Chesnay Cedex (France) http://www.inria.fr ISSN 0249-0803