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# Towards a Generic Framework to Generate Explanatory Traces of Constraint Solving and Rule-Based Reasoning

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Domaine 2 \_\_\_



# Towards a Generic Framework to Generate Explanatory Traces of Constraint Solving and Rule-Based Reasoning

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D om aine : A lgorithm ique, program m ation, logiciels et architectures E quipes-P rojets C ontraintes

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A bstract: In this report, we show how to use the Simple Fluent Calculus (SFC) to specify generic tracers, i.e. tracers which produce a generic trace. A generic trace is a trace which can be produced by di erent im plem entations of a software component and used independently from the traced component.

This approach is used to de ne a method for extending a java based CHR-platform called CHROME (Constraint Handling Rule Online Model-driven Engine) with an extensible generic tracer. The method includes a tracer specication in SFC, a methodology to extend it, and the way to integrate it with CHROME, resulting in the platform CHROME-REF (for Reasoning Explanation Facilities), which is a constraint solving and rule based reasoning engine with explanatory traces.

K ey-words: Trace, CHR, CHR-, CHROME, CHROME REF, Tracer, M eta-Theory, Model Driven Engineering, Tracer Driver, Analysis Tool, Program Analysis, Observational Semantics, Software Component, Debugging, Program ming Environment, Logic Program ming, Validation

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# Towards a Generic Fram ework to Generate Explanatory Traces of Constraint Solving and Rule-Based Reasoning

R esum e: Dans ce rapport, nous montrons com ment utiliser le calcul des uents simple (SFC) pour speci er des traceurs generiques, c'est-a-dire qui produisent des traces generiques. Une trace generique est une trace qui peut être produite par di erentes im plem entations d'un com posant logiciel et être utilisees independam ment du com posant trace.

Cette approche est utilisee pour de nir une methode pour introduire dans une platform e CHR-basee Java et appelee CHROME (Constraint Handling Rule Online Model-driven Engine) un traceur generique extensible. La methode comprend une speci cation du traceur en SFC, une methodologie d'extension, et leur implantation dans CHROME, and obtenir la plateform e CHROME-REF (Raisonnement Explicatif Facilite), qui est un solveur de contraintes et moteur de raisonnement a base de regles avec des traces d'explications.

M ots-cles: trace, CHR, CHR-, CHROME, CHROME-REF, MDE, traceur, m eta-theorie, pilote de tracer, analyseur, outils d'analyse, analyse de program m e, analyse dynam ique, sem antique observationnelle, com posant logiciel, deboggage, environnem ent de program m ation, program m ation en logique, validation

# 1 Introduction

In this report we de ne a method for extending a java based  $CHR^{-1}$  platform called CHROME (Constraint Handling Rule Online Model-driven Engine) with an extensible generic tracer. CHROME is presently developed at the Federal University of Pernam buc [56] with the purpose to allow the developm ent of large software using CHR paradigm.

The m ethod consists of rstly to build a form alspeci cation of a tracer for CHR-, the kernel of the system, and to extend it according to further CHR-extensions. The speci cation de nes a generic trace which is as independent as possible from a particular CHR platform or speci c usages. Then, secondly, it is suggested to use this speci cation as a guideline to extend the MDE scheme development of CHROME, with a tracer scheme development, resulting in the plateform CHROME-REF (REF stands for Reasoning Explanation Facilities), which is a constraint solving and rule based reasoning engine with explanatory traces.

This report is almost based on the internship work of R.O liveira [38]. We introduce rst some contextual aspects of this work.

#### 1.1 The CHRW orld

The language CHR has matured over the last decade to a powerful and elegant general-purpose language with a wide spectrum of application domains [52]. The interest in CHR- stemmed from past research having shown that:

- CHR is simultaneously a Turing-complete declarative program ming language and an expressive knowledge representation language with declarative formal semantics in classical rst-order logic [22];
- CHR integrates and subsumes the three main rule-based program ming and knowledge representation paradigms, i.e., (conditional) term rewrite rules [24], (guarded) production rules [55] and (constraint) logic program ming rules [1];
- A CHR- inference engine can support an unmatched variety of practical autom ated reasoning tasks, including constraint solving with variables from arbitrary domains, satis ability [22], entailment [50], abduction [1], agent action planning [50] and agent belief update [50] and revision [55]. In addition, it support several of these tasks under logical [50], plausibilistic [8] and probabilistic epistem ological [42] assumptions. [10] adds default reasoning to this list, by showing how to represent default logic theories in CHRV. It also discusses how to leverage this representation together with the well-know correspondence between default logic and Negation As Failure (NAF) in logic program ming, to propose an extension CHRV maf of CHRV allowing NAF in the rule heads. And [20] adds concurrency.

The Figure 1 shows the several automatic reasoning services that are subsumed by CHR- and extensions.

For all its above strengths, CHR remained until recently a language for K now ledge R epresentation and Program m ing (KR&P) in the smallm ainly used

<sup>&</sup>lt;sup>1</sup>CHR stands for Constraint H and ling Rule [22], CHR- for CHR with disjunction.

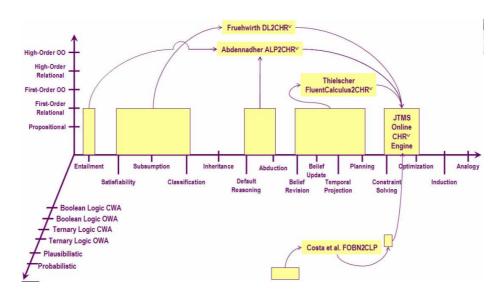


Figure 1: Rule-based Constraint Program m ing and Automated Reasoning Services

to fast prototype intelligent, innovative system s. The ORCAS project  $^2$ , constitutes a rst and prelim inary step towards the long term goal, to turn CHR into a platform for KR&P in-the-large industrial strength, operationally deployed system s. It addressed one key KR&P in-the-large requirement, namely rule base engineering scalability through rule base encapsulation and assembly in reusable software components.

#### 1.2 From CHROME to CHROME-REF

CHROME stands for Constraint Handling Rule Online Model-driven Engine, is a model-driven, component-based, scalable, online, Java-hosted CHR-engine to lay at the bottom of the framework as the most widely reused automated reasoning component. The idea of CHROME is also to demonstrate how a standard set of languages and processes prescribed by MDA can be used to design concrete artefacts, such as: a versatile inference engine for CHR- and its compiler component that generates from a CHR- base the source code of Java classes.

The project CHROME-REF (Constraint Handling Rule Online Model-Driven Engine with Reasoning Explanation Facilities) constitutes a preliminary step, towards extending CHR and CHR engines with a formally founded, exible and user-friendly reasoning explanation facility. The need for exible and user-friendly explanatory reasoning tracing facilities for rule-based systems has been recognized since the initial success of production rule expert systems in the 80s. However, the expressive power of CHR being far superior than that of a mere production system, through the addition of functional terms, rewrite rules and backtracking search, makes debugging a CHR rule base also more complex than debugging a production rule base. In turn, this added complexity makes the

<sup>&</sup>lt;sup>2</sup>http://www.cin.ufpe.br/~jr/mysite/C4RBCPProject.html

need for sophisticated rule engine tracing facilities m ore crucial and the issues in their design and implementation more challenging.

This project is pioneering the investigation of these issues. CHROME assembles CHR base independent run-time components for constraint store management, red ruled history management, constraint entailment, query processing and intelligent search, with optimized components resulting from the compilation of the CHR base. Following the KobrA2 model-driven, component-based, orthographic software engineering method [4,5], CHROME was built by rst specifying a rened Platform-Independent Model (PIM) in the OMG standards UML2/OCL2 (Unied Modeling Language / Object Constraint Language). This PIM was then implemented in Java.

The fact that CHROME compiling a declarative CHR base into imperative Java objects is crucial for its reasoning perform ance. However, it makes tracing far more complex since it introduces a mismatch between, on the one hand, the abstract, high-level rule interpretation operational semantics that the developer follows when conceiving a CHR base, and, on the other hand, the concrete, low-level object method call operational semantics electively executed by the engine. To help the developer debug the rule base, the tracer must thus generate a high-level rule interpretation trace simulation from the low-level object method calls executed by the compiled code.

Our objective here is to integrate the independently constructed tracer architecture within the component-based architecture of CHROME following the K obr $A\ 2$  m ethod.

## 1.3 Towards Generic Trace

Despite the fact that CHR- provides an elegant general-purpose language with a wide spectrum of application domains, a key issue is how easily you can write and maintain programs. Several studies [48, 45] [7] [6] show that maintenance is the most expensive phase of software development: the initial development represents only 20% of the cost, whereas error xing and addition of new features after the rst release represent, each, 40% of the cost. Thus, 80% of the cost is due the to the maintenance phase. Debugging is said to be the least established area in software development: Industrial developers have no clear ideas about general debugging methods or elective and smart debugging tools, yet they debug programs anyway. There are several ways to analyze a program, for instance: program analysis tools help program mers understand programs, type checkers [37] help understand data inconsistencies, slicing tools [30] help understand dependencies among parts of a program. Tracers give insights into program executions.

At present, there exists a number of useful debugging tools for CHR, for example, ECLiPSe Prolog [2], SW IProlog [58] or CHROME [56]. But, these tools were designed and implemented in a specic way for each solver, not all tools bene to from all the existing tool. The Figure 2 shows this current cenario, for each CHR solver a specic implementation of the debugging tool.

This way each implementation results in a set of one-to-one specialized connections between a solver and its tools. If we want to interchange data between each solver, hooks have to be added into the solver code in order to be able to do it. Furthermore, the types of basic information required by a given debugging

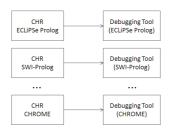
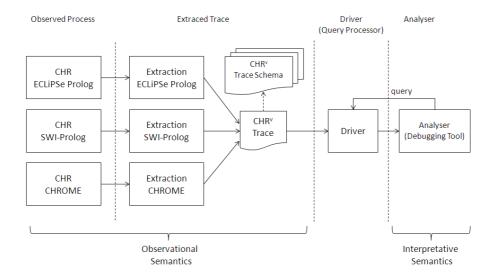


Figure 2: Current situation: each solver is strictly connected to its debugging tool. Figure adapted from [31]



F igure 3:0 ur approach: a generic trace schem a enables w ork and m aintain just one process of debugging

tool is not often m ade explicit and m ay have to be reverse-engineered. This is a non neglectable part of the cost of porting debugging tool from one constraint program m ing platform to another.

In order to solve the above-mentioned problem and improve analysis and maintenance of rule-based constraint programs, like CHR-, there is a need for user-friendly reasoning explanatory facilities that are exible and portable.

G iven this scenario we take advantage of the recent research in trace engineering [16, 14, 15] to propose a generic architecture that produces generic debugging informations for CHR- and potential extensions. In that way, any debugging tool changes its focus to generic traces, instead of to be concerned in speci c platform in plementations.

The Figure 3 illustrates the idea of \generic trace", which is as independent as possible from a particular CHR platform or specic usages. It shows the structure of a tracing process which can be decomposed into three likely \independent" components: trace extraction, full trace litering according to some query, and reconstruction of a sub-trace to be used. It shows also the several aspects which must be specied: a semantics for the generic trace (called 0 b-

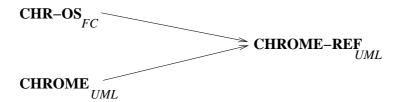


Figure 4: Towards CHROME-REF

servational Sem antics), a query language to select the sub-trace of interest to be used, and a sem antics to interpret the selected trace (called Interpretative Sem antics).

A generic trace needs to be understood independently from the observed process. For this reason it is necessary to be able to give it a semantics as precise as possible. This is the purpose of the O bservational Semantics. It will allow for validation tests and studies of some trace properties before and after in plementing it. In this report we focus on the observational semantics of traces.

The F luent C alculus (FC) is a logic-based representation language for knowledge about actions, change, and causality [54]. As an extension of the classical Situation C alculus [43], F luent C alculus provides a general framework for the development of axiom atic semantics for dynamic domains. It appears to be well suited to describe the O bservational Semantics and, though its F lux implementation [53], to be a likely executable speci cation.

# 1.4 Connecting all the Pieces

The CHROME project focuses on extending CHR with rule-base encapsulation in software components for reuse by assembly across applications. It has as intention to produce the rst domain-independent framework highly reusable debugging tool, supporting a variety of reasoning explanation facilities. The main contribution is to permit any CHR- engine to be extensible with components for comprehensive, exible and e cient reasoning explanation trace generation and user-friendly trace query specication and trace visualization. To achieve this is necessary to integrate design patterns for tracing facilities such as tracer driver with design patterns for Graphical User Interface (GUI) such as Model-View-Controller (MVC) within an overall Model-Driven Architecture (MDA) framework [3]. It will also involve dening a comprehensive trace query language, as well as experiments to empirically evaluate the engineering productivity gains obtained through the use of the tracing components.

In the report we describe the approach illustrated by the Figure 4. It consists rst in an observational sem antics of the extensible generic trace of CHR which is specied in Fluent Calculus. This sem antics is thus mapped into the PIM description of CHROME, leading to a complete PIM of CHROME-REF in UML, the constraint solving and rule based reasoning engine with explanatory traces.

The CHROME-REF environment will be built such an editor as a Eclipse Plugin for rapid prototyping deployed with a GUI to interactively submit requests and inspect solution explanations at various levels of details.

The rest of this report is organized in three main sections.

The Section 2 presents a restricted trace m eta-theory focused on trace production components and composition. It introduces also the observational semantics of a trace and its representation in the simplified uent calculus.

The Section 3 presents the observational sem antics of CHR- in uent calculus including tracer and extraction schemes.

The Section 4 shows the introduction of the tracer in the PIM of CHROME using the KobrA2 method and resulting in a PIM of CHROME-REF with a very rst implementation.

Four annexes give respectively a description of the O bservational Sem antics of CHR in SFC, the XML scheme of a generic trace of CHR-, a short example of trace produced by the java compiled CHROME-REF, and the OS of an application.

 $<sup>^2</sup>$ http://www.eclipse.org/

# 2 Specifying Tracers

The Trace M eta-Theory (TM T) [15] provides a set of de nitions about how to design a trace for a speci c dom ain of observation.

A trace may be interpreted as a sequence of communication actions that may take place between an observer and an observed process. It consists of nite unbounded sequences trace events. There is also the tracer that means the generator of trace. A coording to [14], the TMT focuses particularly on providing sem antics to tracers and the produced traces as independent as possible from those of the processes or from the ways the tracers produce them .

There are two concepts of trace [14] (cf. the Figure 5 and the Section 2.2). The rst one is the virtual trace, it represents a sequence of events showing the evolution of a virtual state which contains all that one can or wants to know about the observed process. The second one is called actual trace, it represents the generated trace in the form of some encoding of the current virtual state. Finally, there is the idea of full trace if the parameters chosen to be observed about the process represent the totality of useful know ledge regarding it (explicitly or in plicitly).

# 2.1 Components of Trace Generation and Use

The Figure 6 shows the dierent components related to a unique trace. We distinguish 5 components, in this order.

# 1.0 bserved process

The observed process is assumed more or less abstracted in such a way that his behavior can be described by a virtual trace, that is to say, a sequence of (partial) states. A formal description of the process, if possible, can be considered as a formal semantics, which can be used to describe the actual trace extraction.

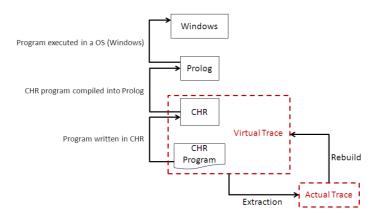


Figure 5: Virtual and Actual Trace.

# 2. Extractor

This component is the extraction function of the actual trace from the virtual trace. From a theoretical point of view, we can see it as a speci c

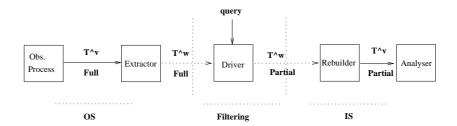


Figure 6: Components of the TMT

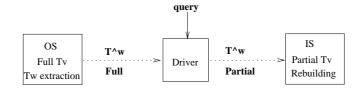


Figure 7: Form al concepts related to the generation and use of a trace

com ponent, but in practice it corresponds to the tracer whose realization, in the case of a program ming language, usually requires modifying the code of the process.

#### 3. Filter

The role of the lter component, or driver [32], is to select a useful subtrace. This component requires a specic study. It is assumed here that it operates on the actual trace (that produced by the tracer). The fact of making it as a proper component corresponds to the specic approach adopted here, which implies that the extracted actual trace is full. The ltering depends on the specic application, implying that the full trace already contains all the information potentially needed for various uses.

#### 4. Rebuilder

The reconstruction component performs the reverse operation of the extraction, at least for a subpart of the trace, and then reconstructs a sequence of partial virtual states. If the trace is faithful (i.e. no information is lost by the driver) [15], this ensures that the virtual trace reconstruction is possible. In this case also, the separation between two components (rebuilder and analyzer) is essentially theoretical; these two components may be in practice very entangled.

# 5. Analyzer

The component using a trace m ay be a trace analyzer or any application.

W ith these components it may be associated three main speci cation steps, as illustrated on the Figure 7.

#### - Observational Semantics (OS)

The 0 S describes form ally the observed process (or a fam ily of processes) and the actual trace extraction. This aspect will be studied deeper in the Section 2.2. The intention here is to express the 0 S using simple uent calculus.

#### - Querying

Due to the separation in several components, the actual trace may be expressed in any language. We suggest using XM L. This allows to use standard querying techniques dened for XM L. This aspect will not be developed here, but we chose to express the trace in XM L and give in the Appendix B the corresponding XM L schema.

#### - Interpretative Sem antics (IS)

The interpretation of a trace, i.e. the capacity of reconstructing the sequence of virtual states from an actual trace, is form ally described by the Interpretative Sem antics. In the TM T no particular application is de ned; its objective is just to make sure that the original observed sem antics of the process has been fully communicated to the application, independently of what the application does.

# 2.2 Contiguous Full Traces

We introduce here the two traces which may be associated to a single process equipped with a tracer. We recall here the de nitions used in [15].

# 2.2.1 Virtual Trace

A full virtual trace is de ned on a dom ain of states. Given P a nite set of (nam es) of param eters  $p_i$  de ned on the dom ains  $P_i$ . The  $P_i$  are dom ains of objects of any kind. They may also have relations (functional or otherwise) between them and they can be in nite in size.

A dom ain of states S is de ned on the Cartesian product of the parameter dom ains: S P  $_1$   $\,:::$  P  $_n$  .

De nition 1 (Contiguous Full V irtual Trace) A contiguous full virtual trace is a sequence of trace events of the form  $e_t:(t;r_t;s_t);t$  1, where:

- t: is the chrono, speci c time of the trace. It is an integer increased by one unit in each successive event. To point a particular value of the chrono, we will talk about moment of the trace.
- $\bullet$   $r_t\colon$  an identi er of action characterizing the type of actions undertaken to make the transition from state  $s_t$  , to state  $s_t$  .
- $s_t$ : is an element of the state domain.  $s_t = p_{1;t}$ ; ...;  $p_{n,t}$  is the current state reached at moment t, and the  $p_{i,t}$  are values of the parameters  $p_i$  at moment t.  $s_t$  is the current full virtual state.

A nite virtual trace over t (t > 0) events will be denoted  $T_t^v = < s_0; \overline{e_t} >$ , where  $s_0$  is the initial full virtual state and  $\overline{e_t}$  represents the sequence  $e_1 ::: e_i ::: e_t$ . The full virtual trace is contiguous insofar as all the moments in the interval [1::t] are present in the trace  $T_t^v = < s_0; \overline{e_t} >$ .

#### 2.2.2 Actual Trace

The full virtual trace represents what we want or what is possible to observe of a process. It describes the development stages of this process in the form of the evolution of a state which contains the observables. As the current virtual state of a process can be fully represented in this trace, one cannot expect neither to produce it nor to communicate it e ciently. In practice we will perform a kind of \compression" of the information conveyed by the virtual states and their evolution, transmitted or communicable to the process observers, and one shall ensure that these processes are able to \decompress" it. This actually communicated information is the actual trace.

An actual full trace is de ned on an actual state dom ain. Let A be a nite set of (nam es of) attributes  $a_i$  de ned on dom ains of attributes  $A_i$ . The attributes may have relationships (they are not necessarily independent) and they can be in nite in size.

An actual state dom ain A is de ned on the C artesian product of attributes dom ains: A A  $_{\rm 1}$   $\,$  ::: A  $_{\rm n}$  .

De nition 2 (Contiguous Full Actual Trace) An actual trace is a sequence of trace events of the form  $w_t$ :  $(t;a_t)$ ; t=1, where:

t is the chrono and  $a_t$  2 A denotes a nite sequence of attributes values,  $a_t$  is the current actual state. The number of attributes of a trace event is bound by n. Each state  $a_t$  contains at most n attributes whose number depends exclusively on the type of action which produced it.

An actual trace with t (t > 0) events is denoted  $T_t^w = \langle s_0; \overline{w_t} \rangle$ , where  $s_0$  is the initial virtual state comm on to both traces and  $\overline{w_t}$  represents the sequence  $w_1; \ldots w_i; \ldots w_t$ .

## 2.3 Generic Trace and Composition

We study here the methodology of generic full trace development for a multilayer based application.

# 2.3.1 Generic Trace of a Familly of Observed Processes

Consider again the Figure 3 in the introduction. It illustrates the fact that dierent in plementations of CHR can be abstracted by a unique simpler model. This common model is used to specify the unique virtual and actual traces of these implementations. This illustrates the way we will proceed to get a generic trace of CHR: starting from an abstract theoretical, general but su ciently rened, semantics of CHR which is (almost) the same implemented in all CHR platforms.

# 2.3.2 Composition of Traces

Now we consider the case of an application written in CHR. It may be for example a particular constraints solver like CLP (FD). In this case there exists already a generic trace called GenTra4CP [12]. This trace is generic form ost of the CLP (FD) existing constraints solvers. Therefore a tracer of CLP (FD) solver implemented in CHR should also produce this trace. But we may be interested

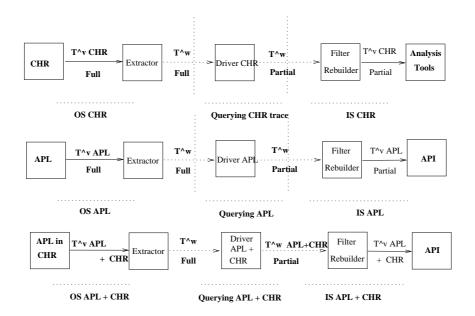


Figure 8: Composition of Generic Full Traces for a two Layers Application

in re ning the trace considering that there are two layers: the layer of the application (CLP (FD)) and the layer of the language in which it is in plemented (CHR). The most rened trace will then be the trace in the GenTra4CP form at extended with elements of the generic full trace of CHR alone. The generic full trace of CLP (FD) on CHR is an extension of the application trace taking into account details of lower layers.

This is illustrated by the Figure 8 in the case of two layers: an application (like CLP (FD) for example) in plemented in CHR. This method can be generalized to applications with several layers of software. The Figure 5 shows in fact at least 4 layers.

In our components based approach it means that we may de ne separately and independently specic generic full traces for each layer, and, so in this case for the application (APL) and the under-layer of CHR. The generic full trace APL on CHR is a kind of composition of traces and will be obtained by some merging of both generic full traces into a unique one. The result may not exactly be a union of all actions, parameters and attributes, but it is not our purpose here to study more deeply this aspect. For more details see [15].

# 2.4 Observational Semantics

The Observational Sem antics (OS) is a description of a possibly unbounded data ow without explicit reference to the operational sem antics of the process which produced it [16]. The OS may be considered as a abstract model of process, in the case of a single observed process or it can be an abstraction of the sem antics to several processes. It is defined as a Labelled Transition Systems (LTS) [25].

## 2.4.1 Representation of the Observational Sem antics

The Observational Semantics has two parts: a state transition function and a trace extraction function.

The rst part is a form alm odel on the way successive events of the virtual trace are related. It is a virtual trace sem antics in the sense that, given a full virtual trace

 $T_t^v = \langle s_0; \overline{e_t} \rangle$ , it explains the sequence of events  $e_t$  by a transition function<sup>3</sup> recursively applied from an initial virtual state.

The second part, the function of extraction, produces what is actually \broad-casted" outside from the observed process. This function has as arguments the current state and the type of action, and produces the attributes of the actual trace.

De nition 3 (Observational Sem antics (OS)) An Observational Sem antics is de ned by the tuple < S;R  $_{0}$ ;A;E;T;S $_{0}$ >, where

- S is a virtual state domain, where each state is described by a set of parameters.
- $\bullet$  R  $_{\rm O}$  is a nite set of action types, set of identi ers used as labels for transitions.
- A is a actual state domain, where each state is described by a set of attributes.
- E is the local extraction function of the actual state a, perform ed by transition of action type r issued from state s, E:RxS!A, which satis es by de nition: E(r;s) = a (a 2 A, set of actual states). More precisely, the set of attributes  $a_t$  of the event t of the actual trace is derived from the current state at moment t 1 of the virtual trace and the transition labelled by the action type  $r_t$ , i.e.

$$E(r_t; s_{t 1}) = a_t$$

• T state transition function T:Rx! S, i.e.

$$T(r_t; s_{t-1}) = s_t$$

• S<sub>0</sub> S, set of initial states.

The 0 S m ay be represented by \rules", one for each action, describing the transition and the actual trace event extraction corresponding to the action. A rule has 4 item s.

- AType: an action identi err2 Ro
- A C ond: f some auxiliary computations on the current virtual state and condition for executing the action corresponding to the transition: a rst-order logic formula using predicates on the parameters g

 $<sup>^{3}\,\</sup>mathrm{It}$  is fact a relation since the transitions m ay be nondeterm in istic.

- V SE ect: f the e ect of the action r on the current state s, resulting in a new state  $\rm s^0$ , and som e auxiliary com putations relative to the attributes of the trace event q
- E trace: f the attributes of the trace event produced by the action r: a, new extracted actual trace event g

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Exam ple 2.1: the Fibonacci Function Idealized (biologically unrealistic) rabbit population.
```

The OS < S;If;R<sub>0</sub>;A;E;T;S<sub>0</sub> >, describes the determ inistic transition function  $T_1$ .

 $S:N_+$  (positive integers list),  $s_t$  is the complete evolution of the population from m om ent 0 until m om ent  $t+1:s_t=$  [popu<sub>0</sub>;:::;popu<sub>t</sub>;popu<sub>t+1</sub>]

```
R_0: fm gg (m onthly growing)
```

 $A: N_+$ ,  $a_t$  is the population at m om ent t+1 (popu (t+1)).

 $E : E \ (m \ q; s) = plast(s) + last(s)$ . There is one rule only to describe E.

 $T_1$ : T (m g;s) = s o [plast(s) + last(s)] (respectively before last and last elements of the list ss, o denote lists concatenation). The new virtual state t is the previous state to which the sum of the two last elements is appended.

```
S_0: s_0 = [1;1].
A Type: m g
A C ond: f trueg
V SE ect: f v plast(s) + last(s) ^ s^0 so [v] g
E trace: fvg

Traces:
T_5^v = < [1;1]; [(1;m g; [1;1;2]); (2;m g; [1;1;2;3]); :::;
(4;m g; [1;1;2;3;5;8]); (5;m g; [1;1;2;3;5;8;13])] > T_5^w = < [1;1]; [(1;2); (2;3); (3;5); (4;8); (5;13)] >
```

# 2.4.2 Sim ple Fluent Calculus

The Fluent Calculus (FC) is a logic-based representation language for knowledge about actions, change, and causality [54]. As an extension of the classical Situation Calculus [43], Fluent Calculus provides a general fram ework for the development of axiom atic semantics for dynamic domains.

The simple uent calculus (SFC) has the following appealing qualities:

- Simplication of the description, since the notions of virtual state and actual trace are \naturally" embedded in the uent calculus (the situation corresponding to a state can be viewed as a representation of the actual trace).
- Reasoning on transitions may be simpler, as it supports handling partial virtual states (with appropriate axiom atisation). Form alproofs become simpler in the SFC (less deductions, at least for \direct closed" e ects, see [54, 51]). It follows that properties like \faithfulness" [16] should be easier to prove form ally. The Symmetry of \state axioms" allows forward and backward reasoning. With the simplicity of the representation of state changes, this should make such proofs simpler.

- The description in SFC makes such speci cation potentially executable in Flux. There is some limits to the executability, related to the partial axiom attisation of the observational semantics and executability of formal speci cation in general. However such framework may facilitate some simulations.

The Fluent Calculus is a sorted logic language with four standard sorts: FLUENT, STATE, ACTION, and SIT (which stands for situation). A uent describes a single state property that may change by the means of the actions of some agent. A state is a collection of uents. A dopted from Situation Calculus, the standard sort SIT describes sequences of actions.

The pre-de ned constant; :STATE stands for the empty state. Each term of sort FLUENT is also an (atom ic) STATE, and the function :STATE STATE  $\P$  STATE, written in in x notation, represents the composition of two states. The following abbreviation H olds (f;z) is used to express that uent f holds in state z:

Holds(f;z) = 
$$_{def}$$
 (9z<sup>0</sup>)f  $z^{0}$  = z (1)

The behavior of function  $\$  " is governed by the foundational axioms of Fluent Calculus, which essentially characterize states as sets of uents.

$$(z_1 \quad z_1) \quad z_1 = z_1 \quad (z_1 \quad z_1) \tag{2}$$

$$z_1 \quad z_2 = z_2 \quad z_3 \tag{3}$$

$$z \quad z = z$$
 (4)

$$z_1 \quad \mathbf{;} = z \tag{5}$$

$$H ext{ olds}(f; f_1 ext{ z}) ext{ } f_1 ext{ } H ext{ olds}(f; z) ext{ } (6)$$

States can be updated by adding and/or rem oving one or more uents. Addition of a sub-state z to a state  $z_1$  is  $sim p \lg y$  expressed as  $z_2 = z_1 - z$ , and rem oval is defined by

$$z_2 = z_1 \quad z =_{\text{def}} (\text{H olds}(f; z_2)) \quad \text{H olds}(f; z_1) \quad \text{H olds}(f; z_2)) \quad (7)$$

The standard predicate Poss: ACTION STATE in Fluent Calculus is used to axiom atize the conditions under which an action is possible in a state, i.e., the situations in which the pre-condition of this actions is satis ed.

The pre-de ned constant  $S_0:SIT$  is the initial (i.e., before the execution of any action) situation. The function Do:ACTION SIT 7 SIT denotes the addition of an action to a situation. The standard function State:SIT 7 STATE is used to denote the state, i.e., the uents that hold in a situation, after a sequence of actions. This allows to extend m acro Holds and predicate Poss to SITUATION arguments as follows.

$$H ext{ olds}(f;s) = def H ext{ olds}(f;State(s))$$
 (8)

$$P oss(a;s) = def P oss(a;S tate(s))$$
 (9)

In a F luent C alculus A xiom atization, beyond the de nition of the dom ain sorts, functions and predicates, we can de ne a set of axiom s that must follow three pre-de ned axiom schem as: the precondition axiom s, the state update axiom s and the state constraint axiom s.

De nition 4 (Pure State Formula) A Pure State Formula is a First Order formula (z)

- There is only one free state variable z
- It is composed of atom ic form ulas in the form:

```
Holds(;z), where is of the sort FLUENT
```

atom s which do not use any reserved predicate of F luent C alculus

De nition 5 (Precondition Axiom) A precondition axiom follows the schema: P oss(A(x);z) (x;z), where (x;z) is a Pure State Formula.

This kind of axiom states that the execution of the action A with the param eters x is possible in the state z if and only if  $_{A}$  (x;z) is true.

```
De nition 6 (State U pdate A xiom ) A state update axiom follows the schema: Poss(A(x);State(s))^ (x;State(s)) (State(Do(A(x);s));State(s)) where (State(Do(A(x);s));State(s)) = State(Do(A(x);s)) = State(s) # # where
```

# and # are partial states.

# 2.4.3 Observational Semantics in Simple Fluent Calculus

A virtual state of the observed process corresponds to a state in SFC described by a set of uents (this correspondence must be explicitly specied).

Each type of action in the 0 S is an action name in the SFC. A particular action is denoted R in the following.

A ctual states are elements of the Cartesian product of attribute domains (this domain must be explicitly specied).

Transition and extraction function (or relation) are described using both fundam ental following schemes (fundam ental axioms of the Fluent calculus)

1. Pre-Condition Axioms:

```
P oss(R;x;z) (x;z)
```

2. State U pdate A xiom s:

```
P oss(R;x;State(s)) ^ (x x;State(s))
_{R} (State(D o(R;w(x x;State(s));s));State(s))
```

where w (x, y; S tate(s)) is an actual trace event associated with the transition, and derived from the current state (using local variables too).

Nota: a situation s contains the sequence of actions in the OS executed to reach the current virtual state z=S tate(s), and also the sequence of extracted actual trace events such that  $T^{\,_{V}}=E$  ( $T^{\,_{V}}$ ).

```
An actual trace T^w is the sequence of w_i, w ith chrono, found in the situation s = D \circ (R_n; x_n; w_n; D \circ (R_{n-1}; x_{n-1}; w_{n-1}; ...; S_0) ...) It may be computed according to the following axiom s: Extraction (0; S) = S
Extraction (n + 1; D \circ (R; x; w; s)) = ((n + 1) w) Extraction (n; s)
```

Exam ple 2.2: OS for Fibonacci

The virtual state contains only one uent F ib=1 of type List(Int) > F luent, and there is only one type of action M g. The actual state contains just 2 attributes, respectively of type S tring and Int. A vector is represented by a sequence (P rolog list syntax).

```
S_0 = F ib([1;1]) P oss(M g; [1;p1];z) \quad H olds(F ib([1;p1]x]);z) P oss(M g; [1;p1];S tate(s)) \land v = 1 + p1 S tate(D o(M g; M g;v];s)) = S tate(s) \quad F ib([v;1;p1]x]) \quad F ib([1;p1]x])
```

# 2.5 Trace Query and Analysis Tools

Trace query and analysis tools are considered here as separate components, as illustrated in the Figure 6. Although they are part of the CHROME-REF project, they are not studied more deeply here. Instead, we propose a rst representation of the actual CHR trace using XML. The XML schema is given in the Appendix B, and an example of produced trace in the XML form at in the Appendix C.

# 3 Tracing Rule-Based Constraint Program ming

Constraint Handling Rules emerges in the context of Constraint Logic Program ming (CLP) as a language for describing Constraint Solvers. In CLP, a problem is stated as a set of constraints, a set of predicates and a set of logical rules. Problems in CLP are generally solved by the interaction of a logical inference engine and constraint solving components. The logical rules (written in a host language) are interpreted by the logical inference engine and the constraint solving tasks are delegated to the constraint solvers.

# 3.1 CHR by Example

The following rule base handles the less-than-or-equal problem:

This CHR program speci es how leq simpli es and propagates as a constraint. The rules in plement re exivity, antisymmetry, idempotence and transitivity in a straightforward way. CHR reflexivity states that leq(X; Y) simplies to true, provided it is the case that X = Y. This test forms the (optional) guard of a rule, a precondition on the applicability of the rule. Hence, whenever we see a constraint of the form leq(X; X) we can simplify it to true.

The rule antisym m etry m eans that if we nd leq(X;Y) as well as leq(Y;X) in the constraint store, we can replace it by the logically equivalent X = Y. Note the different use of X = Y in the two rules: in the reflexivity rule the equality is a precondition (test) on the rule, while in the antisym m etry rule it is enforced when the rule res. (The re exivity rule could also have been written as reflexivity@leq(X;X) <=> true:)

The rules ref lexivity and antisym metry are simplication CHR. In such rules, the constraint found are removed when the rule applies and res. The rule idem potence is a simpagation CHR, only the constraint in the right part of the head will be removed. The rule says that if we not leq(X; Y) and another leq(X; Y) in the constraint store, we can remove one.

Finally, the rule transitivity states that the conjunction leq(X;Y); leq(Y;Z) implies leq(X;Z). Operationally, we add leq(X;Z) as (redundant) constraint. without removing the constraints leq(X;Y); leq(Y;Z). This kind of CHR is called propagation CHR.

The CHR rules are interpreted by a CHR inference engine by rewriting the initial set of constraints by the iterative application of the rules. Its extension with disjunctive bodies, CHR- boosts its expressiveness power, turning it into a general program ming language (with no need of an host language).

# 3.2 Observational Sem antics of CHR

The observational semantics of a tracer is based on a simplied abstract semantics of the observed process. In the case of CHR-, we suggest to use an

adaptation of the re ned theoretical sem antics of CHR as presented in [17]. To start with, we show how to build an observational sem antics for CHR based on the theoretical operational sem antics  $!_t$  [22]. The description of  $!_t$  in SFC is borrowed from [9].

# 3.2.1 Theoretical Operational Sem antics $!_t$ of CHR

We do not T as the constraint theory which do not the sem antic of the built-in constraints and thus models the internal solver which is in charge of handling them. We assume it supports at least the equality built-in. We use [H  $\mbox{\it JT}$ ] to indicate the rst (H) and the remaining (T) terms in a list, ++ for sequence concatenation and [] for empty sequences.

We use the notation  $a_0; \ldots; a_n$  for both bags and sets. Bags are sets which allow repeats. We use [ for set union and ] for bag union, and fg to represent both the empty bag and the empty set. The identied constraints have the form c#i, where c is a user-de ned constraint and i a natural number. They dierentiate among copies of the same constraint in a bag. We also assume the functions chr(c#i) = c and id(c#i) = i.

An execution state is a tuple hQ;U;B;Pin, where Q is the Goal, a bag of constraints to be executed; U is the UDCS (User De ned Constraint Store), a bag of identi ed user de ned constraints; B is the BICS (Built-In Constraint Store), a conjunction of constraints; P is the Propagation History, a set of sequences, each recording the identities of the user-de ned constraints which red a rule; n is the next free natural used to number an identi ed constraint.

The initial state is represented by the tuple hQ; []; true; []i $_n$ . The transitions are applied non-determ inistically until no transition is applicable or the current built—in constraint store is inconsistent. These transitions are defined as follows:

```
Solve hfcg ] Q;U;B;Pin 7 hQ;U;c^B;Pin where c is built-in Introduce hfcg] Q;U;B;Pin 7 hQ;fc# ng] U;B;Pin+1 where c is user-de ned constraint Apply hQ;H1] H2] U;B;Pin 7 hC]Q;H1]U;e^B;Pin where exists a rule r@H1nH2, gbC and a matching substitution e, such that chr(H1) = e(H1);chr(H2) = e(H2) and CT \ni B 9(e^g); and the sequence id(H1) + + id(H2) + + id(H2) + + id(H2) + + id(H2) + + id(H2)
```

Exam ple 3.1 The following is a (term inating) derivation under  $!_t$  for the query leq(A;B); leq(B;C); leq(C;A) executed on the leq program in Example 3.1. For brevity, P have been removed from each tuple.

Nomore transition rules are possible, so this is the nal state.

#### 3.2.2 Theoretical Operational Semantics ! to f CHR in SFC

The following is the description of the theoretical operational semantics  $!_t$  in terms of the sorts, relations, functions and axioms of the simple uent calculus.

#### (a) Domain Sorts

- NATURAL, natural num bers;
- RULE, the sort of CHR rules and RULE\_ID the sort of the rule identiers;
- CONSTRAINT, the sort of constraints, with the following subsorts: BIC (the built-in constraints), with the subsort EQ (constraints in the form x=y), and UDC (the user-de ned constraints), with the following subsort: IDENTIFIED (constraints in the form c# i). In short:

```
EQ < BIC < CONSTRAINT and
IDENTIFIED < UDC < CONSTRAINT;
```

- PROPHISTORY = Seq(NATURAL) RULE, the elements of the Propagation History, tuples of a sequence of natural numbers and a rule;

For each de ned sort X, three new sorts:  $S \exp(X)$ ,  $S \exp(X)$  and  $B \exp(X)$  containing the sequences, the sets and the bags of elements of X. W e use [] for the empty sequence and fg for the empty set and the empty bag.

- C H RACTION < ACTION , the subsort of ACTION containing only the actions in the CHR sem antics.

# (b) Predicates

- Query: Bag(CONSTRAINT), Query(q) holds i q is the initial query;
- Consistent:STATE, holds i the BICS of the state is consistent (i.e., if it does not entail false).
- M atch ( $h_k$ ;  $h_R$ ;  $u_1$ ;  $u_2$ ; e; z) holds i (i)  $u_1$  and  $u_2$  are in the UDCS of z and (ii) the set of m atching equations e is such that chr( $u_1$ ) = e( $h_k$ ) and chr( $u_2$ ) = e( $h_R$ );
- -Entails: Set(BIC) Set(EQ) Bag(BIC), Entails(b;e;g) holds if  $CT \neq b! 9(e^g)$ .

#### (c) Functions

- -#:UDC NATURAL 7 IDENTIFIED, de nes the syntactic sugar for de ning identi ed constraints in the form c#i;
- -makeRule:
  - RULEID Bag(UDC) Bag(UDC) Bag(UDC) 7 RULE,
  - m akes a rule from its components. We do no the syntactic sugar for rules as  $r_{id}$  @  $h_k nh_R$  \$ gjb= m akeRule( $r_{id}$ ; $h_k$ ; $h_R$ ;g;b);
- -Bics:STATE 7 Set(BIC), where Bics(z) = fcfd olds(InBics(c);z)g;
- id:Set(UDC) 7 Set(NATURAL), where id(H) = i; # i2 H
- The usual set, sequence and bag operations: 2 for element, [ for set union, ] for bag union, ++ for sequence concatenation, j for sequence head and tail (Ex: [head tail]) and n for set subtraction.

#### (d) Fluents

- -Goal:Bag(UDC) 7 FLUENT, Goal(q) holds i q is the current goal;
- Udcs:Bag(IDENTIFIED) 7 FLUENT, Udcs(u) holds i u is the current UDCS;
- InBics:BIC 7 FLUENT, InBics(c) holds i c is in the current BICS;
- InPropH istory: PROPH ISTORY 7 FLUENT, InPropH istory(p) holds i p is in the current Propagation H istory;
- N extId: NATURAL 7 FLUENT, N extId(n) holds i n is the next natural number to be used to identify a identi ed constraint.

#### (e) Actions

- Solve : B IC 7 CHR\_ACTION , D o(Solve(c);s) executes the Solve transition with the built—in constraint c;
- Introduce: UDC 7 CHR\_ACTION, Do(Introduce(c);s) executes the Introduce transition with the user-de ned constraint c;
- Apply: RULE Bag(UDC) Bag(UDC) 7 CHR\_ACTION, Do(Apply(r;  $u_1$ ;  $u_2$ ); s) executes the Apply transition matching the constraints  $u_1$  and  $u_2$  in the UDCS with the kept and removed heads of r.

# (f) Axioms

- Query (q)! State (S0) = Goal(q) Udcs(fg) NextId(1), The Initial State Axiom states that in the initial state, the goal contains the constraints in the query, the user de ned constraint store is empty and the next ID for identied constraints is 1;

#### Solve

- Poss(Solve(c);z) (9q) (Holds(Goal(q);z) ^ c2 q)
The Solve Precondition Axiom states that the only precondition for the Solve action on the built-in constraint c is that this constraint should be in the goal.

```
S tate(D \circ (S \circ lve(c); s)) = S tate(s) G \circ al(q) InB ics(c)
    Goal(q] fcq)
 The Solve State Update Axiom states that the result of the Solve action
 over the constraint c is that this constraint is removed from goal and
 added to InB ics list in current state;
 Introduce
-Poss(Introduce(c);z) (9q)(Holds(Goal(q);z) ^ c2 q)
- Poss(Introduce(c);s) ^ Holds(Goal(q] c);State(s))^
    Holds(Udcs(u);State(s)) ~ Holds(NextId(n);State(s))
     S tate(D \circ (Introduce(c);s)) = S tate(s) G \circ al(q) U dcs(u ] c#n)
 N = xtId(n + 1)
    Goal(q] fcg) Udcs(u) NextId(n)
 Apply
- Poss (Apply (r@hknhR $ gjd;u_1;u_2);z)
     (9e) (9b) (M atch (h_k;h_R;u_1;u_2;e;z)^
    : H olds (InP ropH istory (id (u_1); id (u_2);r);z)^B ics (b;z)^E ntails (b;e;g))
- Poss(Apply(r@hknhR $gjd;u_1;u_2);State(s))^
    H 	ext{ olds (U dcs (u_1 ] u_2 ] u); S tate (s)) } H 	ext{ olds (G oal(q); S tate (s))}
    M atch (h_k; h_R; u_1; u_2; e; z)
    State (D o (Apply (r@ hknhR $ g\dot{g}(u_1;u_2);s)) = State(s) Goal(d] q)
   Udcs(u1]u) InBics(e) InBics(g) InInPropHistory(id(u2);r)
    Goal(q) Udcs(u1]u2]u)
```

# 3.2.3 Observational Sem antics of CHR based on $!_t$

- Poss(Solve(c);s) ^ Holds(Goal(q] fcg);State(s))

The following is the description of the observational sem antics of CHR using the simple uent calculus with modified axioms of the Section 2.4.3. Sorts, Predicates, Functions and Fluents are the same as in the previous section; there is on additional item for the attributes.

The actions are now constants and we make explicit 4 actions: Init; Solve; Introduce; Fail.

# (e) Actions

- Init: 7 CHR\_ACTION, Do(Init; [goal(q)ja]; s) executes the top-level initial transition (starting the resolution) with some query q in the current state (a stands for other attributes list in the associated trace event);
- Solve: 7 CHR\_ACTION, Do(Solve; [bic(c)ja]; s) executes the Solve transition with the built-in constraint c;
- Introduce: 7 CHR\_ACTION, Do(Introduce; [udc(c)ja];s) executes the Introduce transition with the user-de ned constraint c;
- Apply: 7 CHR\_ACTION,
  Do(Apply; [rule(r)];s) executes the Apply transition with rule rm atching the constraints in the UDCS with the kept and removed heads;

-Fail: 7 CHR\_ACTION, Do(Fail; [goal(q)ja]; s) if no Apply is possible.

There are also 5 attributes in the actual trace: goal; udc; bic; hind; rule.

#### (f) Attributes

- goal: CONSTRAINTS 7 ATTRIBUTE, is the set of constraints in the current Goal;
- udc:CONSTRAINTS 7 ATTRIBUTE, is the set of constraints in the current User De ned Constraints Store;
- bic: CONSTRAINTS 7 ATTRIBUTE, is the set of constraints in the current Built-In Constraints Store;
- hind: In TEGER, is the new propagation history index (incremented by Introduce);
- rule: RULE 7 ATTRIBUTE, is the rule applied to reach this state.

#### Apply

We just comment the adaptation of one rule, the full description is in Appendix A .

(g) A xiom s of the O bservational Sem antics

The observational sem antics of CHR- can be form alized similarly with 11 actions (hence 11 dierent kinds of trace events),

in itS tate; solve; activate; reactivate; drop; sim plify; propagate; derive;
clean; split; fail,

using the re ned operational semantics  $!_{r}$ , according to [17, 9].

## 3.3 Towards Full Generic Trace of CHR-

As suggested in the Section 2.3.2, a full trace will be progressively obtained by composing several layers of traces and several potential applications in such a way that as many as possible of potential uses can be satisfied by such a trace. The Figure 5 suggests 4 levels of renements corresponding to 4 layers of implementations, i.e. from bottom to top: environment of execution (W indows/Linux/M ac...), implementation language (most of CHR are implemented in Prolog), CHR, and application written in CHR. There may be other lower levels, like WAM abstract machine implemented in Java for the Prolog level, etc... Even if each layer has its own level of abstraction and most of the CHR users don't care about lower software layers, it may be interesting to keep some trace of them in the \full" trace.

If we consider the point of view of debugging some application written in CHR, here are some information which could be usefully found in a trace used by a debugging tool.

- Execution environment: activation of system commands during interactions
- Im plem entation languages (there may be several layers): specic local error m essages, activated layer, ...
- CHR: nam e of used rules

We mean here that, at some point, it may be useful to not in the trace of the application some information regarding dierent layers of implementation in order a debugging tool to be able to \understand" some bugs.

Let us consider an example of application. In the Annex D we give the observationalsem antics in SFC of a simple application of [53]. This OS species possible traces of actions performed by robots (here there is only one). We may assume that this smallworld is program med in CHR and therefore the trace of the whole system is a kind of combination of both traces: the one of the robot and the trace corresponding to the CHR program execution. The resulting full trace corresponds to the trace composition described in the Section 2.3.2 (comprehensively treated in [15]).

If one wants just to follow what the robots are doing, then the sub-trace consisting of the trace events regarding the robot's actions is su ciently relevant. But, at least at the stage of debugging, som e dysfunction observed in the robot's trace (for exam ple crossing a closed door) can be understood only by looking at a more complete trace which includes events related to the CHR layer behaviour.

Finally there is one more level, which corresponds to the speci city and versatility of CHR: the many extensions and applications which are embedded in CHR with CHR as implementation language, quoted as the \CHR world" in the introduction. Here are some of them [22]: Boolean algebra for circuit analysis, resolution of linear polinomial equations – CLP (R) $^4$  – with application in nances and non linear equations, nite domain solvers – CLP (FD) – with applications in puzzles, scheduling and optimisation, but many others as quoted at the beginning of the report.

 $<sup>^4\,\</sup>mathrm{C\,LP}\,$  stands for C onstraint Logic P rogram m ing.

A full CHR- trace should probably include traces related to several extensions like CLR (X ) where X stands for some constraint domain, and CHR  $^{\rm V}$  maf for example. This is possible, but there is still a need to specify an observational sem antics for several of these extensions.

# 4 Towards CHROME-REF

This section details the architecture of CHROME-REF, the extensible implementation of a generic tracer for Constraint Solving and Rule-Based Reasoning. Each component of the CHROME-REF is described in terms of UML2.1 according the KobrA2m ethodology [4,5]. We extensive a brief overview of CHROME.

#### 4.1 CHROME

CHROME stands for Constraint Handling Rule Online Model-driven Engine, is a model-driven, component-based, scalable, online, Java-hosted CHR-engine to lay at the bottom of the framework as the most widely reused automated reasoning component. The idea of CHROME is also to demonstrate how a standard set of languages and processes prescribed by MDA can be used to design concrete artefacts, such as: a versatile inference engine for CHR- and its compiler component that generates from a CHR- base the source code of Java classes.

# 4.1.1 Goals and Design Principles

The main goal of CHROME if to take CHR engines a step beyond, by designing a new CHR- engine and a corresponding compiler using a component-based model-driven approach. CHROME is a CHR- engine with an ecient and complete search algorithm (e.g. the conict-directed backjumping algorithm), the rst versatile rule-based engine, integrating production rules, rewrite rules, its built-in belief revision mechanism (reused for handling disjunctions) and CLP rules to run on top of a mainstream Object Oriented (OO) platform (Java). Because it is a rule-based engine following a component-based model-driven approach, it allows easy port to other OO platforms such as Python, JSP, C++ and others. Finally the compiler is the rst that uses a model transform ation pipeline to transform from a source relational-declarative language into a OO imperative paradigm language.

The CHROME architecture is divided into two main sub-components (see the Figure 9):

- i) The ATL-pipeline compiler (CHR Compiler component) that takes as input a relational declarative CHR-base and produces an e-cient constraint handling imperative object-oriented component assembly.
- ii) The CHROME run-time engine (shown in the Figure 9 as the QueryProcessor component) that provides the services and data structures necessary to execute a CHR- base given a particular query (collection of constraints).

The Figure 10 shows the complete MOF metamodel of CHR-. At this abstract syntax levelallCHR- rules are generalized as simpagation rules. The meta-associations keep and del from the CHR- meta-class to the Constraint meta-class respectively represent the propagated and simplied heads of the rule. The heads must be instances of RDCs (Rule De ned Constraints). A guard of a rule must be a collection of BICs (BuiltIn Constraints). Both RDCs and BICs are specializations of Constraint meta-class.

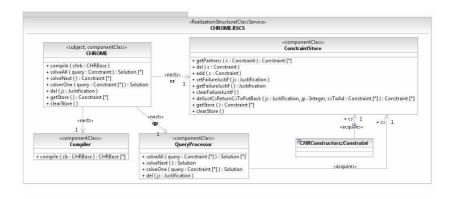


Figure 9: CHROME

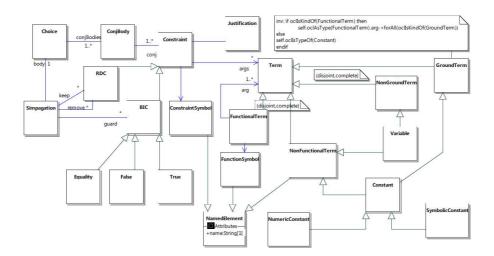


Figure 10: M eta-m odel of CHR- and CHR data structures.

The body of a CHR- rule is a collection of alternative conjunctions. Conjunctions are composed by both RDC or BIC, e.g. a collection of instances of meta-class Constraint. The original CHR- base has a special RDC (OR) to indicate disjunctions in the body. The collection of all rules of a CHR program is a CHR Base.

Each constraint is composed by a constraint symbol and a collection of zero or more arguments, e.g. a collection of terms (meta-class Term). A Term further specializes into: functional terms, non-functional terms, ground terms and non-ground terms. A Constant is both a non-functional term and a ground term and a Variable is a non-ground term and a non-functional term. Finally a functional term is further composed by a Function Symbol and a collection of zero or more arguments, which are in turn recursively dened as instances of meta-class Term. The constraint domain meta-class aggregates all terms ymbols allowed.

The m etam odel displays also the internal structures of the engine, namely: the constraint store and the constraint queue. The rst stores the constraints added by ring rules, the second is a processing queue that tracks which is the next constraint to be processed.

# 4.1.2 Strengths and Lim itations

CHROME is the rst Java CHR- engine: none of the related CHR Java engines allow disjunctive rules. Compilation in Java makes it easier to reuse and deploy full CHR- bases in applications in need of automated reasoning services. It is one of the largest case study to date to integrate MDE technology with model transformations (4358 ATL lines) and components. It however su ers some limitations, as it provides only three built-in constraints: the syntactical equality, true and false, and it has no visual tracing IDE. This makes practical applications still too cumbersome to implement, being tracing a fundamental part of large automated reasoning development.

# 4.2 CHROME-REF Components

The Figure 11 shows a object-oriented representation of the observational semantics of CHR- as described in the Section 3.2.1. It contains we sort of extracted trace events (ETrace): an initial state (EInitialState), user-de ned contraint store introduced (EIntroduce), built-in introduced (ESolve), rule applied (EApply) and rule failed (EFail).

The top-level CHROME-REF component encapsulates all sub-components that compose the CHROME environment. The Figure 12 shows the main component and its three sub-components as dened in what follows. They provide methods to compile a rule base, to solve a query (displaying one or more solutions for such query), to adapt a solution when a given set of justified constraints is deleted and to clear the constraint store for processing a new query.

The D river component is a intermediator between CHROME and Analyzer, its function is to manager the communication of trace event sent by the engine and liter the requested information to the analyzer. Finally, the Analyzer component, in our case, is a debugging tool for CHR.

The next sub-sections describe each component.

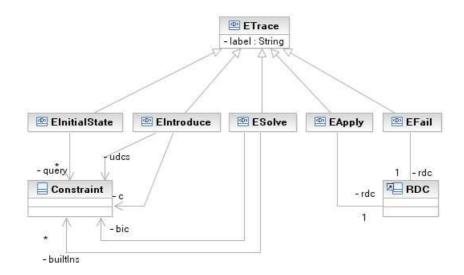


Figure 11:00 Representation of the OS of the CHR-Tracer

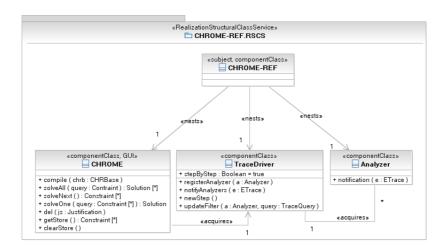


Figure 12: CHROME-REF three main Components

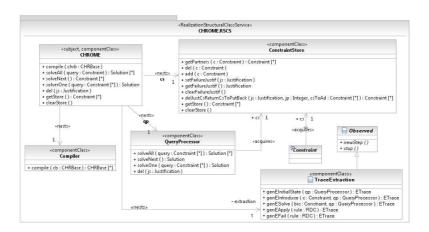


Figure 13: Insertion of the Trace Extraction Component into CHROME

## 4.2.1 Extraction

The Figure 13 shows the CHROME component with a new component called TraceExtraction, which implements the generic CHR trace as described in the Section 3.2.3.

We have added two improvements to the CHROME to integrate with our proposal: a new componente called Trace Extraction that receives as input some parameters (Constraint; QueryProcessorandRDC) and produces the trace events (ETrace); and, we included new rules into the CHROME compiler to send the previous parameters to the Trace Extraction during the execution of a CHR program.

The following 0 CL rules explain how a trace event will be produced from received param eters:

```
context TraceExtraction::genEInitialState(qp:QueryProcessor): -
   Etrace
post:
   let eInitialState:EInitialState = oclIsNew()
   in
        eInitialState.query = qp.goal and
        result = eInitialState
context TraceExtraction::genEIntroduce(c:Constraint, qp: -
   QueryProcessor):Etrace
post:
   let eIntroduce :EIntroduce = oclIsNew()
   in
        eIntroduce.c = c and
        eIntroduce .udcs = qp.cs.getStore() and
        result = eIntroduce
context TraceExtraction::genESolve(bic:Constraint, gp: -
   QueryProcessor):Etrace
post:
   let eSolve:ESolve = oclIsNew()
   in
        eSolve.bic = bic and
        eSolve.builtIns = qp.allVars and
```

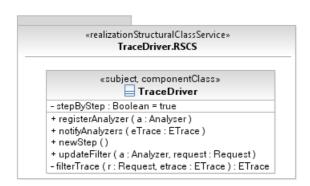


Figure 14: Trace Driver Meta-model

```
result = eSolve

context TraceExtraction::genEApply(rule:RDC):Etrace
post:
    let eApply:EApply = oclIsNew()
    in
        eApply.rule = rule and
        result = eApply

context TraceExtraction::genEFail(rule:RDC):Etrace
post:
    let eFail:EFail = oclIsNew()
    in
        eFail.rule = rule and
        result = eFatil
```

# 4.2.2 Driver

The Trace Driver component is an intermediator between a process and an analyzer. It component has the following functions (Figure 14):

- to decide whether the underlying process (in our case CHROME) will send trace events step by step or all at once. This information is represented by means of the ag stepByStep;
- to register an analyzer that will watch the trace events from the underlying process;
- to notify all connected analyzers soon after a trace event to be produced;
- to ask for a new trace event (only if the ag stepB yS tep is true); and,
- to Iter a trace event by means of a trace query sent from a analyzer.

The following OCL rules describe the post-condition of each method:

```
context TraceDriver ::registerAnalyzer(a:Analyzer)
post: analyzer > includes(d)
context TraceDriver ::notifyDriver(eTrace:ETrace)
```

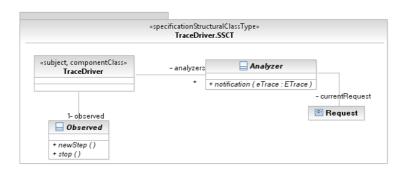


Figure 15: Meta-model of the Analyzer and Communication with the Driver

As said before, the Trace D river component is a intermediator that receives trace events from a process and sends it to the analyzer. The Figure 15 shows the relationships between these components.

A trace driver is connected to an observed process which sends the trace events, and it has a list of analyzers to which to the trace events. Each analyzer is associated to a query, which says which information the driver will send to the analyzer.

# 4.2.3 Analyzer

The trace analyzer speci es to the driver which events are needed by means of queries. The requests that an analyzer can send to the tracer driver are of three kind. Firstly, the analyzer can ask for additional data about the current event. Secondly, the analyzer can modify the query to be checked by the driver. Thirdly, the analyzer can notify the driver to pause, continue or end the process execution.

In this project, in order to exemplify the whole proposed framework, we have created two simple views to show a pretty-printing of a CHR execution. The Figure 16 presents these two kind of analyzers: the Trace View shows the evolution of the CHR parameters (Goal, Constraint Store, Built-ins, etc), dened in the generic trace; and the Program View is just to focus in a specie rule when this rule is triggered.

We illustrate these views with an execution of the LEQ example.

```
reflexivity @ leq(X,Y) <=> X=Y j true. antisymetry @ leq(X,Y) , leq(Y,X) <=> X=Y. idempotence @ leq(X,Y) n leq(X,Y) <=> true. transitivity @ leq(X,Y) , leq(Y,Z) <=> leq(X,Z). with the query:
```

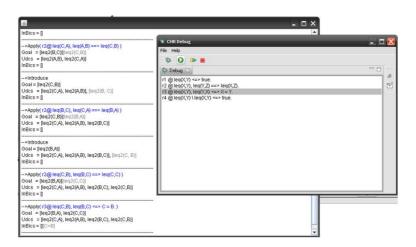


Figure 16: A Simple GUI to Analyze a Program Execution Looking at its Trace

```
leq(A,B), leq(B,C), leq(C,A).
```

Finally, we get the XML instance produced by CHROME for this example (see complete trace with all attributes in the Appendix C).

```
< ?xml version= "1.0" encoding= "UTF 8"?>
< chrv
    xmlns="http://orcas.org.br/chrv"
    xmlns:xsi="http://www.w3.org/2001/XM LSchem a instance"
    xsi:schemaLocation=
        "http://orcas.org.br/chrv chrv.xsd">
    < event chrono= "1">
        <initialState>
           < goal > leq(A,B), leq(B,C), leq(C,A) < /goal >
        </initialState>
    </event>
    < event chrono= "2">
        <introduce>
            <udc>leq(A,B)</udc>
            < goal > leq(B,C), leq(C,A) < / goal >
        </introduce>
    </event>
    < event chrono= "3">
        <introduce>
            <udc>leq(A,B), leq(B,C)</udc>
            < goal> leq(C,A)</goal>
</chrv>
```

At this stage of the implementation, such views are principally helpful to help to develop the generic trace.

## 5 Conclusion

In this report we have presented an ongoing work as a roadm ap towards CHROME-REF, and we have de ned the methods and tools to reach this goal. They consists of a formal speci cation (called observational semantics - OS) of a generic tracer for CHR- using an adaptation of the simple uent calculus (SFC) which we have presented, and its implementation, over and inside CHROME, using the KobrA 2 method, and resulting in a PIM of CHROME-REF.

We have tested the approach with a small trace pretty printing GUI. We also indicated how to work on extensions of the very rst trace we presented (using the simple!  $^{\rm t}$  sem antics of CHR), before including other actions and attributes inspired by more rened sem antics of CHR – and various CHR domains extensions.

Several other issues however remain to be explored.

First the use of the SFC to describe the observational sem antics of tracers. As quoted in the report, we may expect several advantages of its use: facilitation of trace extension speci cation, or re nement, by merging observational sem antics of several CHR extensions or sublayers, and facilitation of veri cation of form alproperties of the trace. We did not reach the point to be in condition to simulate production of traces trying to execute this OS using Flux. Such execution would require some implementation of complex functions or predicates. Since the OS may be a smooth abstraction of a family of solvers, it is in principle possible to develop some simulation producing supersets of possible traces. This can be useful to analyse some properties of the traces to improve their design. However it will become worth and more interesting when a more re ned full trace will be ready.

A nother point which remains unsolved is the way to relate the observational semantics of the tracer and the design of the CHROME-REF PIM. Both are forms of partial formal speci cation. The OS because it is an abstraction of the semantics of the observed process—hence a partial speci cation—, the later because it is a partially formal speci cation. Even if it is clear that the description of the tracer in SFC is a clear requirement which serves as guideline to design this PIM , there is no way to guarantee a formal correspondence.

One proposed approach is to map the logical model of SFC used here into an 0 bject-0 riented (00) model (00 SFC), and to limit the \implementation step" to a merging of PIMs. This way to proceed is illustrated on the Figure 17. This approach aims at reducing the complexity of mapping between the two dierent descriptions, by introducing a intermediary step denoted CHR-0 S<sub>00SFC</sub>.

We have started to specify the OS in OOSFC  $\beta$ 9], but this question is still open whether this step is really helping, or whether the construction of the tracer part of the CHROME-REF PIM in UML is better achieved just using the SFC speci cation of the OS. It could be also interesting to compare several approaches of extending existing codes, like pluging aspects in the CHROME java code. In any cases the question of the relationships with the speci cation is still worth posing.

Finally a third unsolved point concerns the validation of the implementation. Considering the design and implementation used method, there is now ay to make formal proof of adequation between the speci cation and the imple-

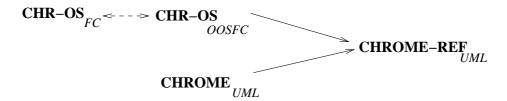


Figure 17: An Interm ediate Step towards CHROME-REF

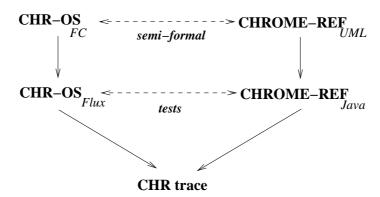


Figure 18: Validating di erent operational sem antics

m entation, but this point need more study. At this stage, we are limited to perform tests. The Figure 18 illustrates this point.

- Sem i-form alproof: It is to show that CHR-OS<sub>FC</sub> is equivalent to the CHROME-REF<sub>UML</sub>. But, as UML is a sem i-form allanguage [33], so that, UML is not strictly form alin sense of a purely syntactic derivation using a very precise and circum scribed form alset of rules of inference, no form alproof can be performed.
- Test-based validation: Let CHR-O  $S_{FC}$  with its equivalent in plem entation CHR-O  $S_{Flux}$  in Flux, and CHROME-REF<sub>UML</sub> with its equivalent im plem entation in Java CHROME-REF<sub>Java</sub>, the method consists of comparing the produced traces to check whether they are equivalent.

There is still a long way to get a full generic trace for CHR. Indeed, as quoted in the Section 3.3, such goal in plies the existence of generic traces for several CHR extensions. Since we already have some (for nite domain solvers, or for Prolog under-layer for example), we are far to cover all existing extensions of CHR quoted at the beginning of this paper. But the composition of traces and the method of implementing tracer presented here give a possible road towards a full generic trace for CHR- and many of its extensions.

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## A Appendix - Observational Sem antics of CHR

The following is the description of the observational sem antics of CHR based on its theoretical operational sem antics !  $_{\rm t}$  and the simple uent calculus with modi ed axiom s of the Section 2.4.3.

### (a) Domain Sorts

- NATURAL, natural num bers;
- RULE, the sort of CHR rules and RULE\_ID the sort of the rule identiers;
- CONSTRAINT, the sort of constraints, with the following subsorts: BIC (the built-in constraints), with the subsort EQ (constraints in the form x=y), and UDC (the user-de ned constraints), with the following subsort: IDENTIFIED (constraints in the form c# i). In short:

```
EQ < BIC < CONSTRAINT and
IDENTIFIED < UDC < CONSTRAINT;
```

- PROPHISTORY = Seq(NATURAL) RULE, the elements of the Propagation History, tuples of a sequence of natural numbers and a rule. For each dened sort X, three new sorts: Seq(X), Set(X) and Bag(X) containing the sequences, the sets and the bags of elements of X. We use
- [] for the empty sequence and fg for the empty set and the empty bag.  $\mbox{CHRACTION} < \mbox{ACTION}, \mbox{ the subsort of ACTION} \mbox{ containing only the actions in the CHR sem antics.}$

#### (b) Predicates

- Query: Bag(CONSTRAINT), Query(q) holds i q is the initial query;
- Consistent:STATE, holds i the BICS of the state is consistent (i.e., if it does not entail false);
- M atch  $(h_k; h_R; u_1; u_2; e; z)$  holds i (i)  $u_1$  and  $u_2$  are in the UDCS of z and (ii) the set of m atching equations e is such that  $chr(u_1) = e(h_k)$  and  $chr(u_2) = e(h_R)$ ;
- Entails : Set(BIC) Set(EQ) Bag(BIC), Entails(b;e;g) holds if CT  $\neq$  b! 9(e^g).

## (c) Functions

- -#:UDC NATURAL 7 IDENTIFIED, de nes the syntactic sugar for de ning identi ed constraints in the form c#i;
- -makeRule:
  - RULEID Bag(UDC) Bag(UDC) Bag(UDC)  $\mathbb{7}$  RULE, makes a rule from its components. We denote the syntactic sugar for rules as  $r_{id} \in h_k nh_R$ \$ gp = m akeRule( $r_{id}$ ; $h_k$ ; $h_R$ ;g;b);
- -Bics:STATE 7 Set(BIC), where Bics(z) = fcfH olds(InBics(c);z)g;
- id:Set(UDC) 7 Set(NATURAL), where id(H) = i;c#i2 H

- The usual set, sequence and bag operations: 2 for pertinence, [ for set union, ] for bag union, ++ for sequence concatenation, j for sequence head and tail (Ex: [head tail]) and n for set subtraction.

#### (d) Fluents

- Query: Bag(UDC) FLUENT, Query(q) holds i q is the initial toplevel goal;
- -Goal:Bag(UDC) 7 FLUENT, Goal(q) holds i q is the current goal;
- U dcs : B ag(ID E N T IF IE D ) 7 F L U E N T , U dcs(u) holds i u is the current U D C S;
- InBics: BIC 7 FLUENT, InBics(c) holds i c is in the current BICS;
- InPropH istory: PROPH ISTORY 7 FLUENT, InPropH istory(p) holds i p is in the current Propagation H istory;
- N extId: NATURAL 7 FLUENT, N extId(n) holds in is the next natural number to be used to identify a identied constraint.

#### (e) Actions

- Init: 7 CHR\_ACTION, Do(Init; [goal(q)ja];s) executes the toplevel initial transition (starting the resolution) with some query q in the current state (a stands for other attributes list in the associated trace event);
- Solve :7 CHR\_ACTION, Do(Solve; [bic(c)ja];s) executes the Solve transition with the built-in constraint c;
- Introduce: 7 CHR\_ACTION, Do(Introduce; [udc(c)ja];s) executes the Introduce transition with the user-de ned constraint c;
- Apply: 7 CHR\_ACTION,
  Do(Apply; [rule(r)t];s) executes the Apply transition with rule r m atching the constraints in the UDCS with the kept and rem oved heads;
- Fail: 7 CHR\_ACTION, Do(Init; [goal(q)ja]; s) executes the toplevel initial transition (starting the resolution) with some query q in the current state (a stands for other attributes list in the associated trace event);

## (f) Attributes

- goal: CONSTRAINTS  $\Tilde{7}$  ATTRIBUTE, is the set of constraints in the current Goal;
- udc: CONSTRAINTS 7 ATTRIBUTE, is the set of constraints in the current User De ned Constraints Store;
- bic : CONSTRAINTS 7 ATTRIBUTE, is the set of constraints in the current Built–In Constraints Store;
- hind: IN TEGER, is the new propagation history index (incremented by Introduce);
- rule : RULE 7 ATTRIBUTE, is the rule applied to reach this state.

(g) A xiom s of the O bservational Sem antics

```
Init
```

- Poss(Init; [q];z) Holds(Query(q);z)
- $\label{eq:condition} $$ P oss(Init; [q]; S tate(s)) \quad S tate(D o(Init; [initState; goal(q); hind(1)]; s)) = $$ S tate(s) \quad U dcs(fg) \quad G oal(q) \quad N extId(1) $$ Q uery(q) $$$

The Initial State Axiom states that in the initial state, the goal contains the constraints in the query, the user de ned constraint store is empty and the next ID for identied constraints is 1;

#### Solve

- Poss(Solve; [c]; z) (9q) (Holds(Goal(q] fcg); z)

The Solve Precondition Axiom states that the only precondition for the Solve action on the built—in constraint c is that this constraint should be in the goal.

- Poss(Solve; [c];s)

```
S tate(D o(S olve; [solve; bic(c); goal(q)]; s)) =
```

State(s) Goal(q) InBics(c) Goal(q] fcg)

The Solve State Update Axiom states that the result of the Solve action over the constraint c is that this constraint is removed from goal and added to InB ics list in current state;

## Introduce

- Poss(Introduce; [c];z) (9q) (Holds(Goal(q);z) ^ c2 q)
- Poss(Introduce; [c]; State(s)) ^ Holds(Udcs(u); State(s))^

H olds(N extId(n);State(s))

State(Do(Introduce; [introduce; udc(c); goal(q); hind(n + 1)]; s)) =

State(s) Goal(q) Udcs(u] c#n) NextId(n+1)

Goal(q] fcg) Udcs(u) NextId(n)

### Apply

- Poss(Apply; [r; $h_k$ ; $h_R$ ;g; $u_1$ ; $u_2$ ];z)

(9e) (9b) (M atch ( $h_k$ ;  $h_R$ ;  $u_1$ ;  $u_2$ ; e; z)^

: H olds (InP ropH istory (id  $(u_1)$ ; id  $(u_2)$ ;r);z) ^ B ics (b;z)^

Entails(b;e;g))

- Poss(Apply; [r; $h_k$ ; $h_R$ ;g; $u_1$ ; $u_2$ ]; State(s))^

H olds (U dcs ( $u_1$  ]  $u_2$  ] u); S tate(s))  $^H$  olds (G oal(q); S tate(s))  $^H$ 

M atch  $(h_k; h_R; u_1; u_2; e; z)$ 

State (Do(Apply;

 $[apply, rule (r@\ h_k nh_R\ \$\ gjd; u_1; u_2); goal(d]\ q); udc(u1]\ u); bic(g)]; s)) =$ 

State(s) Goal(d] q) Udcs(u1] u) InBics(e) InBics(g)

InP ropH istory (id  $(u_1)$ ; id  $(u_2)$ ; r)

```
Goal(q) Udcs(u1] u2] u)

Fail

- Poss(Fail; [q]; z) Holds(goal(q); z)^ @Poss(Apply; [r; h_k; h_R; g; u_1; u_2]; z)

- Poss(Fail; [q]; s)

State(Do(Fail; [fail; goal(q)]; s)) = State(s)
```

# B Appendix - XM L schem a for Generic CHR Trace

```
< ?xm l version="1.0" encoding="UTF 8"?>
 < xs:schem a xm lns:xs= "http://www.w3.org/2001/XM LSchem a"</pre>
    targetN am espace= "http://orcas.org.br/chrv" xm lns= "http://orcas -
         .org.br/chrv"
    elem entForm D efault= "qualified">
  < xs:elem ent nam e= "chrv">
   < xs:com plexT ype>
    < xs:sequence>
      < xs:elem ent nam e= "event" m in0 ccurs= "0" m ax0 ccurs= "unbounded" -</pre>
       < xs:com plexT ype>
        < xs:choice>
         < xs:elem ent nam e= "initialState" m inO ccurs="1" m axO ccurs=" -</pre>
              1">
          < xs:com plexT ype>
            < xs:sequence>
             < xs:elem ent nam e= "goal" type= "xs:string" />
< xs:elem ent nam e= "hind" type= "xs:integer" />
           </xs:sequence>

<p
         < xs:elem ent nam e= "introduce" m in0 ccurs= "1" m ax0 ccurs= "1">
           < xs:com plexT ype>
            < xs:sequence>
             < xs:elem ent nam e= "udc" type= "xs:string" />
             < xs:elem ent nam e= "goal" type= "xs:string" />
             < xs:elem ent nam e= "hind" type="xs:integer" />
           </xs:sequence>
          </r></r></ra>
         < xs:elem ent nam e= "solve" m in0 ccurs= "1" m ax0 ccurs= "1">
           < xs:com plexT ype>
            < xs:sequence>
             < xs:elem ent nam e= "bic" type= "xs:string" />
             < xs:elem ent nam e= "goal" type= "xs:string" />
           </xs:sequence>
          </r></r></ra>
          < xs:elem ent nam e= "apply" m in0 ccurs= "1" m ax0 ccurs= "1">
           < xs:com plexT ype>
            < xs:sequence>
             < xs:elem ent nam e= "rule" type= "xs:string" />
             < xs:elem ent nam e= "goal" type= "xs:string" />
< xs:elem ent nam e= "udc" type= "xs:string" />
             < xs:elem ent nam e= "bic" type= "xs:string" />
            </xs:sequence>
           </r></re>/xs:elem ent>
           < xs:elem ent nam e= "fail" m inO ccurs= "1" m axO ccurs= "1">
            < xs:com plexT ype>
             < xs:sequence>
              < xs:elem ent nam e= "rule" type= "xs:string" />
             </r></r></ra>
          </xs:choice>
```

## C Appendix - LEQ Example Execution Trace

Here is the trace of execution of the LEQ the Example 3.1 executed in CHROME-REF.

```
< ?xm l version="1.0" encoding="UTF 8"?>
< chrv
    xm lns="http://orcas.org.br/chrv"
    xm lns:xsi="http://www.w3.org/2001/XMLSchemainstance"
    xsi:schem aLocation=
         "http://orcas.org.br/chrv chrv2.xsd">
    < event chrono= "1">
        < in itialState>
            < goab leq(A,B), leq(B,C), leq(C,A) </ goab
            < hind> 1 < /hind>
        / in itialState>
    </event>
    < event chrono= "2">
        < introduce>
            <udc> leq(A,B) </udc>
             <goab leq(B,C), leq(C,A) </goab</pre>
            < h ind> 2 < / h ind>

    </event>
    < event chrono= "3">
        < introduce>
            <udo leq(A,B), leq(B,C) </udo
            <goab leq(C,A)) </goab
<hind> 3 </hind>
        </event>
    < event chrono= "4">
        < apply>
            < rule > r40 leq(A,B), leq(B,C) ==> leq(A,C) < / rule >
            < goal leg(C,A), leg(A,C) </goal
        < / apply>
    </event>
    < event chrono= "5">
        < introduce>
            <udc> leq(A,B), leq(B,C), leq(A,C) < /udc>
            < goab leq(C,A) < / goab
            < hind> 4 < /hind>
        </introduce>
    </event>
    < event chrono= "6">
        < introduce>
            <ud> leq(A,B), leq(B,C), leq(A,C), leq(C,A) </ud>
            < goab </goab
            < hind> 5 < / hind>
        / introduce>
    </event>
    < event chrono= "7">
        < apply>
            < rule > r2@ leq(A,C), leq(C,A) ==> A=C < / rule >
            <goab </goab
            < ud > leq(C,B), leq(B,C) < /ud >
            < bic> A= C < / bic>
        < / apply>
    </event>
    < event chrono= "8">
        < apply>
```

Nomore LEQ program rule may apply.

U sing a representation where attributes have the functional form used in the O bservational Sem antics, it corresponds to the trace (attributes with empty argument are omitted):

See Appendix A for the meaning of the attributes.

```
initialState goal((leq(A,B), leq(B,C), leq(C,A))))
                   hind(1)
2
     introduce
                   udc((leq(A, B)))
                   goal((leq(B,C), leq(C,A)))
                   hind(2)
                   udc((leq(A,B), leq(B,C)))
3
     introduce
                   goal((leq(C,A)))
                   hind(3)
4
     apply
                   rule((r4@ leq(A,B), leq(B,C) \Longrightarrow leq(A,C)))
                   goal((leq(C,A), leq(A,C)))
5
     introduce
                   udc((leq(A,B), leq(B,C), leq(A,C)))
                   goal((leq(C,B)))
                   hind(4)
6
                   udc((leq(A,B), leq(B,C), leq(A,C), leq(C,A)))
     introduce
7
     apply
                   rule((r2@ leq(A,C), leq(C,A) \Longrightarrow A=C)),
                   udc(leq(C,B), leq(B,C))
                   bic((A=C))
                   rule((r2@ leq(C,B), leq(B,C) \Longrightarrow C=B)),
8
     apply
                   bic((A=C, C=B))
```

## D Appendix - OS of a Robots Application in SFC

This world consists of agents (the robots) moving in a space structured by rooms connected by doors, able to carry objects they and in the rooms. A requisition is an order to seek for objects and carry them from some place to an other one. The scene description at some moment is the current state and consists of a set of facts. A \situation" corresponds to a succession of trace events. The current state corresponding to a given situation is obtained here by the reconstruction function (interpretation semantics).

In uent calculus, facts are named  $\setminus$  uents" and requisitions (or requests) are  $\sin$  ilar to Prolog goals. The way the requisitions are  $\cos$  puted is not described by the observational  $\sec$  antics. The requests are thus treated as in uence factors.

We describe a simplied version of the example of [53] with 3 rooms. The simplied robot's world is depicted on Figure 19.

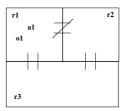


Figure 19: A simple robot world

Initially there is one object and one robot both located in the same room, and the door  ${\tt d}12$  is locked. The robot has its key.

We present an implementation of the OS in Flux. A current state is described by a set of atoms.

## ACTIONS TYPES

pickup pick an object (if any) drop drop the carried object (if any) gotodoor go to the quoted door (if any) enteroom enter the quoted room (if the door is open) open open the door (if it is closed)

## TRACE EVENTS [attributes]

Attribute a stands for \agent"
Attribute o stands for \ob ject"
Attribute r stands for \room "
Attribute d stands for \door"

pickup a o r drop a o r walk a d walk ar open ad

## • Domains

D om ain Sorts				
AGENT	A 1			
ROOM	R1;R2;R3			
DOOR	D 12 <b>;</b> D 13			
OBJECT	01;02;03			

## • Param eters

Param eters versus F luents				
param eter	type	m eaning		
AgentInRoom	AGENT ROOM V FLUENT	the agent is in room r		
AtD oor	AGENT DOOR 7 FLUENT	the agent is at door d		
C losed	DOOR 7 FLUENT	door d is closed		
C arries	AGENT OBJECT 7 FLUENT	agent carries ob ject o		
HasKeyCode	AGENT DOOR 7 FLUENT	agent has the key code for door d		
0 bjectInR com	OBJECT ROOM 7 FLUENT	the object is in room r		
Request	ROOM OBJECT ROOM 7 FLUENT	there is a request to deliver		
		object o from room r1 to room r2		

 ${\bf E}$  ach param eter  ${\bf m}$  ay be represented by several uents. (Request is treated as external)

The initial state is form alized by this term below.

H olds (A gentInR oom (A1;R2);S0)^H olds (O bjectInR oom (O1;R3);S0)^ H olds (O bjectInR oom (O2;R1);S0)^H olds (O bjectInR oom (O3;R2);S0)^

H olds (C losed (D 12); $S_0$ ) ^ H olds (H asK eyC ode (A 1;D 13); $S_0$ ) ^ H olds (R equest(R 3;O 1;R 2); $S_0$ ) ^ H olds (R equest(R 1;O 2;R 3); $S_0$ ) ^ H olds (R equest(R 2;O 3;R 1); $S_0$ ) ^ (8x): H olds (C arries (A 1;x); $S_0$ )

## • Auxiliary Predicates

A uxiliary P redicates				
predicate	type			m eaning
C onnects	ROOM	DOOR	ROOM	doord connects rooms $r_1$ and $r_2$

### • A ctions and A ctual state A ttributes

A ctions					
action	attri	attributes			action meaning
P ickup	pickup	AGENI	OBJECT F	ROOM	pick up object o
D rop	drop	AGENT	DOOR ROOI	M	drop object o
GoToDoor	walk	AGENT	DOOR		go to door d
EnterRoom	walk	AGENT	ROOM		enter room r
0 pen	open	DOOR			open door d

The parameters of the actions in a condition are just used for communication of particular values and thus avoid rewriting of  $\H$  olds" conditions in the following axiom.

```
Observational Sem antics
Pickup
Poss(Pickup; [a;o;r];s)
   Holds (AgentInRoom (a;r);s) ^ Holds (ObjectInRoom (o;r);s)^
   : H olds (C arries (a; o)))
Poss(Pickup; [a;o;r];s)
   State(Do(Pickup; [pickup;a;o;r];s)) = State(s) Carries(a;o)
Drop
Poss(Drop;[a;o;r];s)
   Holds(Carries(a;o)) ^ Holds(AgentInRoom(a;r);s)
Poss(Drop;[a;o;r];s)
   State(Do(Drop; [drop;a;o;r];s)) = State(s) Carries(a;o)
GoToDoor
Poss(GoToDoor; [a;d;r];s) Holds(AgentInRoom (a;r);s)^
    (9r^{0})C onnects (r;d;r^{0}) ^{:} (9d^{0})H olds (AtD oor (a;d^{0});s)
Poss(GoToDoor; [a;d;r];s)
   State(Do(GoToDoor; [walk;a;d];s)) = State(s) AtDoor(a;d)
EnterRoom
Poss (EnterRoom; [a;r;d;r^{0}];s) Holds (AgentInRoom(a;r))^{^{\wedge}}
   H 	ext{ olds (A tD oor(a;d);s) } C 	ext{ onnects (r;d;r}^0) : H 	ext{ olds (C losed (d);s))}
Poss(EnterRoom;[a;r;d;r<sup>0</sup>];s)
  State (D o (E nterRoom; [walk;a;r^0];s)) = State(s) AgentInRoom (a;r^0)
   AgentInRoom (a;r)
Open
Poss(Open; [a;d];s)
   Holds (AtDoor(a;d);s) ^ Holds (HasKeyCode(a;d);s)^
   Holds (C losed (d);s)
Poss(Open;[a;d];s)
   State (Do(Open; [open;a;d];s)) = State(s) Closed(d)
```

## Exam ple of trace:

1	pickup	a1	01	r1
2	walk	a1	d12	
3	open	a1	d12	
4	walk	a1	r2	
5	walk	a1	d12	
6	walk	a1	r1	
7	drop	a1	01	r1
8	pickup	a1	01	r1
9	drop	a1	01	r1
10	walk	a1	d13	

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