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Benchmarking a BI-Population CMA-ES on the BBOB-2009 Noisy Testbed

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ABSTRACT

We benchmark the BI-population CMA-ES on the BBOB-2009 noisy functions testbed. BI-population refers to a multistart strategy with equal budgets for two interlaced restart strategies, one with an increasing population size and one with varying small population sizes. The latter is presumably of little use on a noisy testbed. The BI-population CMA-ES could solve 29, 27 and 26 out of 30 functions in search space dimension 5, 10 and 20 respectively. The time to find the solution ranges between 100D and $10^5 D^2$ objective function evaluations, where D is the search space dimension.

Categories and Subject Descriptors

G.1.6 [Numerical Analysis]: Optimization—global optimization, unconstrained optimization; F.2.1 [Analysis of Algorithms and Problem Complexity]: Numerical Algorithms and Problems

General Terms

Algorithms

Keywords

Benchmarking, Black-box optimization, Direct search, Evolutionary computation, CMA-ES

1. INTRODUCTION

The covariance matrix adaptation evolution strategy (CMA-ES) [2, 6, 7] is a stochastic, population-based search method in continuous search spaces, aiming at minimizing an objective function $f : \mathbb{R}^D \to \mathbb{R}$ in a black-box scenario. In this paper, the $(\mu/\mu_w, \lambda)$ -CMA-ES is applied in a multistart strategy and benchmarked on 30 noisy functions. The multistart consists of two interlacing strategies, one with increasing population size, the other with varying small population size. The algorithm is given in a complementing paper in the same proceedings [3].

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2. ALGORITHM AND PARAMETER SET-TINGS

The algorithm and all parameters are described in [3]. The following parameters have been chosen differently, where λ denotes the offspring population size.

- $MaxIter = 1000 + 500(D + 3)^2/\sqrt{\lambda}$ has been chosen ten times larger, as the noisy functions are expected to be more difficult to solve.
- $c_1 = \frac{0.4}{(D+1.3)^2 + \mu_{\rm W}}$ and $c_{\mu} = \min\left(1 c_1, 0.4 \frac{\mu_{\rm W} 2 + 1/\mu_{\rm W}}{(D+2)^2 + \mu_{\rm W}}\right)$, the learning rates for the covariance matrix have been chosen five times smaller than by default. With default learning rates, the learning of the covariance matrix is the algorithm component that is most susceptible to uncertainties in the selection. Surprisingly, this change did not produce a striking improvement, but slightly more consistent results (e.g. f_{105} , f_{108} and f_{117} are solved also in 40-D).

Restarts are launched until $10^6 D$ function evaluations are exceeded. The stagnation termination criterion

Stagnation: terminate a run, if the median of the 20 newest values is not smaller than the median of the 20 oldest values, respectively, in the two arrays containg the best function values and the median function values of the last $[0.2 t + 120 + 30D/\lambda]$ iterations, where t denotes the iteration counter,

turns out to be crucial for the noisy testbed. Most other standard termination criteria regularly fail. We presume that restarts with small population size are less valuable on a noisy testbed, which leaves yet room for improvement.

The same parameter setting is used for all functions and therefore the crafting effort according to [4] is CrE = 0.

3. SUCCESSFUL POPULATION SIZE

We investigate the population sizes of the final successful runs. In Table 1 minimal, median (the larger in case of even data) and maximal population size are given for 10-D and 20-D. Functions solved with default offspring population size, $\lambda = 10$ and 12, are the sphere function with moderate noise and about half of the functions with Cauchy noise (function numbers in *italics*). Otherwise is the typical population size 10D or larger.

Table 2 tabulates mininal, median (the larger in case of even data) and maximal initial step-size σ^0 of the final successful runs, whenever $\sigma^0 < 2$ in at least one successful case.

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Table 1: Final, successful population sizes. If less than three successful trials included restarts, only the median (default population size) is given

		D = 10)	D =	= 20	
f	\min	med	\max	\min	med	max
101		10			12	
102		10			12	
103		10			12	
104	20	20	40	96	96	192
105	40	80	80	192	192	384
106		10			12	
107	20	20	20	24	24	48
108	80	160	160	192	192	384
109		10			12	
110	-	-	-	-	-	-
111	-	-	-	-	-	-
112		10			12	
113	40	80	320	192	384	384
114	160	320	640	286	768	768
115	40	80	160	185	192	384
116	80	160	160	192	384	384
117	160	320	640	768	768	768
118		10			12	
119	160	160	160	384	384	384
120	320	640	1280	1536	1536	1536
121		10			12	
122	80	160	320	384	768	768
123	640	1280	1280	_	_	-
124	40	80	160	96	192	192
125	640	1280	2560	3072	6144	6144
126	-	-	-	-	-	-
127	239	640	1280	384	1536	3072
128	11	40	320	37	192	768
129	80	118	1280	1301	3072	6144
130	10	26	166	12	24	192

Table 2: Initial step-size σ^0 of successful restarts for functions, where $\sigma^0 < 2$ was successful at least once

	D =	= 10			D =	= 20	
f	\min	med	\max	f	\min	med	max
115	0.126	2.0	2.0	114	1.06	2.0	2.0
125	0.72	2.0	2.0	115	0.068	2.0	2.0
127	0.158	2.0	2.0	122	0.2	2.0	2.0
128	0.28	1.8	2.0	128	0.64	1.56	2.0
129	0.8	2.0	2.0	129	1.42	2.0	2.0
130	0.06	0.64	2.0	130	0.042	0.38	2.0

The data neither rule out nor suggest that f_{130} might benefit from a small initial step-size. Overall, as expected, the small initial step-size is of little use and, if anything, rather disadvantageous on the BBOB-2009 noisy testbed.

4. RESULTS AND DISCUSSION

The results of CPU timing experiments are given in [3]: using Matlab, about $2-3 \times 10^{-4}$ seconds per function evaluation are needed on the BBOB-2009 f_8 function for up to 40-D. Results from the performance experiments according to [4] on the benchmarks functions given in [1, 5] are presented in Figures 1 and 2 and in Tables 3 and 4.

The number of solved functions are 30, 30, 29, 27, 26 and

 $24 \ {\rm out} \ {\rm of} \ 30 \ {\rm functions} \ {\rm in} \ 2, \ 3, \ 5, \ 10, \ 20 \ {\rm and} \ 40 \ {\rm D}, \ {\rm respectively}.$

The typical scaling of the running time (number of function evalutions) is quadratic with the dimension (see Figure 1). With the moderate noise models and with the Cauchy noise model the sphere function can be solved in linear time. More severe noise impairs the scaling behavior by one order of magnitude to quadratic. Similarly, on the Rosenbrock function the severe noise impairs the scaling by one order from roughly quadratic to roughly cubic. Here, the observed failure is presumably due to a too small maximum number of function evaluations allowed.

The expected running times appear rather uniform on the log-scale between 100D and 10^5D^2 function evaluations (upper figures in Figure 2). The graphs suggest that, in higher dimension, with more function evaluations even more functions can be solved.

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Figure 1: Expected Running Time (ERT, •) to reach $f_{opt} + \Delta f$ and median number of function evaluations of successful trials (+), shown for $\Delta f = 10, 1, 10^{-1}, 10^{-2}, 10^{-3}, 10^{-5}, 10^{-8}$ (the exponent is given in the legend of f_{101} and f_{130}) versus dimension in log-log presentation. The ERT(Δf) equals to $\#FEs(\Delta f)$ divided by the number of successful trials, where a trial is successful if $f_{opt} + \Delta f$ was surpassed during the trial. The $\#FEs(\Delta f)$ are the total number of function evaluations while $f_{opt} + \Delta f$ was not surpassed during the trial from all respective trials (successful and unsuccessful), and f_{opt} denotes the optimal function value. Crosses (×) indicate the total number of successful trials. Annotated numbers on the ordinate are decimal logarithms. Additional grid lines show linear and quadratic scaling.

f_{101} in 5-D, N=15, mFE=93	0 f101 in 20-D. N=15. mFE=3014	f102 in 5-D. N=15, mFE=882	f102 in 20-D. N=15, mFE=3122
$\Delta f \# \text{ERT} 10\% 90\% \text{RT}_{em}$	# ERT 10% 90% RT _{succ}	$\Delta f \# \text{ERT} 10\% 90\% \text{RT}_{\text{succ}}$	# ERT 10% 90% RTsucc
10 15 3.5e1 2.9e1 4.2e1 3.5e	15 3.6e2 3.4e2 3.8e2 3.6e2	10 15 3.0e1 2.5e1 3.6e1 3.0e1 1	15 3.7e2 3.5e2 3.9e2 3.7e2
1 15 1.1e2 1.0e2 1.2e2 1.1e	2 15 6.5e2 6.3e2 6.7e2 6.5e2	1 15 1.1e2 9.6e1 1.2e2 1.1e2 1	L5 6.5e2 6.3e2 6.6e2 6.5e2
1e-1 15 2.0e2 1.9e2 2.1e2 2.0e	2 15 9.4e2 9.2e2 9.5e2 9.4e2	1e-1 15 2.0e2 1.9e2 2.1e2 2.0e2	15 9.4e2 9.2e2 9.6e2 9.4e2
1e-3 15 3.8e2 3.6e2 3.9e2 3.8e	2 15 1.5e3 1.4e3 1.5e3 1.5e3	1e-3 15 3.7e2 3.6e2 3.8e2 3.7e2	15 1.5e3 1.5e3 1.5e3 1.5e3
1e-5 15 5.6e2 5.4e2 5.7e2 5.6e	2 15 2.0e3 2.0e3 2.0e3 2.0e3	1e-5 15 5.4e2 5.3e2 5.6e2 5.4e2 1	15 2.0e3 2.0e3 2.1e3 2.0e3
1e-8 15 8.2e2 8.0e2 8.3e2 8.2e	2 15 2.8e3 2.8e3 2.9e3 2.8e3	1e-8 15 8.0e2 7.8e2 8.2e2 8.0e2 1	15 2.9e3 2.8e3 2.9e3 2.9e3
f103 in 5-D, N=15, mFE=994	f103 in 20-D, N=15, mFE=3386	f104 in 5-D, N=15, mFE=7644	f104 in 20-D, N=15, mFE=668758
$\Delta f \# \text{ ERT} 10\% 90\% \text{ RT}_{succ}$	# ERT 10% 90% RT _{succ}	Δf # ERT 10% 90% RT _{succ} #	≠ ERT 10% 90% RT _{succ}
10 15 3.8e1 3.0e1 4.7e1 3.8e1	15 3.6e2 3.4e2 3.7e2 3.6e2	10 15 2.5e2 2.4e2 2.7e2 2.5e2 1	5 2.4e5 2.0e5 2.8e5 2.4e5
1 15 1.3e2 1.2e2 1.4e2 1.3e2	$15 \ 6.6 \ e^2 \ 6.4 \ e^2 \ 6.7 \ e^2 \ 6.6 \ e^2$	1 15 1.4e3 1.2e3 1.7e3 1.4e3 1	5 2.8e5 2.3e5 3.3e5 2.8e5
1e-1 15 2.2e2 2.1e2 2.3e2 2.2e2	$15 \ 9.5 e2 \ 9.3 e2 \ 9.6 e2 \ 9.5 e2$	1e-1 15 2.5e3 2.3e3 2.8e3 2.5e3 1	5 2.9e5 2.4e5 3.4e5 2.9e5
1e-3 15 4.0e2 3.9e2 4.1e2 4.0e2	15 1.6e3 1.5e3 1.6e3 1.6e3	1e-3 15 3.5e3 3.3e3 3.8e3 3.5e3 1	5 3.0e5 2.5e5 3.5e5 3.0e5
1e-5 15 5.9e2 5.8e2 6.1e2 5.9e2	15 2.2e3 2.2e3 2.2e3 2.2e3	1e-5 15 3.9e3 3.6e3 4.2e3 3.9e3 1	5 3.0e5 2.5e5 3.5e5 3.0e5
1e-8 15 9.1e2 8.9e2 9.2e2 9.1e2	15 3.2e3 3.1e3 3.2e3 3.2e3	1e-8 15 4.3e3 4.0e3 4.6e3 4.3e3 1	5 3.1e5 2.6e5 3.6e5 3.1e5
f105 in 5-D, N=15, mFE=19372	f105 in 20-D, N=15, mFE=1.28e6	f106 in 5-D, N=15, mFE=11108	f106 in 20-D, N=15, mFE=86380
Δf # ERT 10% 90% RT _{succ}	# ERT 10% 90% RT _{succ}	Δf # ERT 10% 90% RT _{succ}	# ERT 10% 90% RT _{succ}
10 15 2.8e2 2.6e2 2.9e2 2.8e2	15 5.3e5 4.4e5 6.1e5 5.3e5	10 15 3.0e2 2.8e2 3.3e2 3.0e2	15 1.2e4 1.1e4 1.3e4 1.2e4
1 15 5.2e3 4.4e3 6.2e3 5.2e3	15 6.1e5 5.2e5 7.1e5 6.1e5	1 15 2.3e3 1.6e3 3.0e3 2.3e3	15 2.9e4 2.3e4 3.5e4 2.9e4
1e-1 15 8.9e3 7.8e3 1.0e4 8.9e3	15 6.3e5 5.3e5 7.3e5 6.3e5	1e-1 15 3.3e3 2.6e3 4.1e3 3.3e3	15 3.3e4 2.7e4 3.9e4 3.3e4
1e-3 15 1.0e4 9.2e3 1.2e4 1.0e4	15 6.5e5 5.5e5 7.5e5 6.5e5	1e-3 15 4.4e3 3.6e3 5.2e3 4.4e3	15 3.7e4 3.1e4 4.3e4 3.7e4
le-5 15 1.1e4 9.7e3 1.2e4 1.1e4	15 6.6e5 5.7e5 7.6e5 6.6e5	1e-5 15 4.8e3 4.0e3 5.6e3 4.8e3	15 3.9e4 3.3e4 4.5e4 3.9e4
1e-8 15 1.1e4 1.0e4 1.3e4 1.1e4	15 0.8e5 5.8e5 7.8e5 0.8e5	1e-8 15 5.3e3 4.5e3 6.2e3 5.3e3	15 4.0e4 3.5e4 4.6e4 4.0e4
f107 in 5-D, N=15, mFE=3162	J_{107} in 20-D, N=15, mFE=141332	f108 in 5-D, N=15, mFE=200594	J108 in 20-D, N=15, mFE=3.02 e6
$\Delta J = \pm \text{EKT} = 10\% = 90\% \text{ RT}_{succ}$	# ERI 10% 90% RTsucc	$\Delta J = ERT 10\% 90\% RT_{succ}$	# EKT 10% 90% RT _{succ}
10 15 7.0e1 4.6e1 9.6e1 7.0e1	15 8.6e3 6.9e3 1.0e4 8.6e3	10 15 5.3e2 3.1e2 7.7e2 5.3e2	15 5.8e4 5.1e4 6.5e4 5.8e4
1 15 2.3e2 1.9e2 2.7e2 2.3e2	15 1.4e4 1.1e4 1.0e4 1.4e4	1 15 5.4e3 4.2e3 5.5e3 5.4e3	15 9.7e4 8.3e4 1.1e5 9.7e4
1e-1 15 4.5e2 4.0e2 5.1e2 4.5e2	15 1.6e4 1.4e4 1.9e4 1.6e4	1e-1 15 1.4e4 1.2e4 1.8e4 1.4e4	15 2.0e5 1.7e5 2.3e5 2.0e5
1e-3 15 9.4e2 8.8e2 1.0e3 9.4e2	15 2.764 2.464 5.064 2.764	1e-5 15 5.1e4 2.0e4 5.0e4 5.1e4	15 4.5e5 5.9e5 5.0e5 4.5e5
$1e = 8$ 15 2 2 e^3 2 0 e^3 2 3 e^3 2 2 e^3	15 6 9 e4 5 7 e4 8 2 e4 6 9 e4	1e-3 15 0 7e4 8 3e4 1 1e5 0 7e4	15 1 4e6 1 1e6 1 6e6 1 4e6
f100 in 5-D N=15 mEE=1022	f_{100} in 20-D N=15 mEE=6878	f110 in 5-D N=15 mEE=1 33e6	fillo in 20-D N=15 mEE=3.09e7
$\Delta f = \frac{1}{2} EBT = 10\% = 10\% BT_{max}$	# EBT 10% 90% BT	Δf # EBT 10% 90% BT	# EBT 10% 90% BT
10 15 3 8e1 3 2e1 4 4e1 3 8e1	$\frac{4}{7}$ Eff. 10/0 50/0 ft1succ	10 15 9 5e2 4 1e2 1 5e3 9 5e2	$\frac{4}{7}$ Entr 10% 50% Hisucc
10 10 5.001 5.201 4.401 5.001	15 7 5e2 7 2e2 7 8e2 7 5e2	10 10 3.002 4.102 1.000 3.002	0 1/2/0 1/2/0 1/2/0 1.50/
1e - 1 15 2 4e2 2 3e2 2 7e2 2 4e2	15 1 3e3 1 2e3 1 3e3 1 3e3	1e - 1 15 4 5e5 3 3e5 5 7e5 4 5e5	
1e-3 15 6.2e2 5.9e2 6.6e2 6.2e2	15 2.6e3 2.5e3 2.7e3 2.6e3	1e-3 15 5.9e5 4.9e5 7.0e5 5.9e5	
1e-5 15 1.0e3 9.5e2 1.1e3 1.0e3	15 3.9e3 3.8e3 4.1e3 3.9e3	1e-5 15 6.0e5 5.0e5 7.1e5 6.0e5	
1e-8 15 1.5e3 1.5e3 1.6e3 1.5e3	15 6 0 e3 5 8 e3 6 1 e3 6 0 e3	10-8 15 6 205 5 105 7 305 6 205	
	10 01000 01000 01100 01000	10 0.200 0.100 1.500 0.200	
f111 in 5-D, N=15, mFE=1.11e7	f_{111} in 20-D, N=15, mFE=2.51e7	f_{112} in 5-D, N=15, mFE=9378	f112 in 20-D, N=15, mFE=187012
$\Delta f \begin{vmatrix} f_{111} & \text{in } 5\text{-}\text{D}, \text{ N}=15, \text{ mFE}=1.11\text{ e}_{7} \\ \# \text{ ERT } 10\% & 90\% \text{ RT}_{\text{SUCC}} \end{vmatrix}$	$\begin{array}{c} f_{111} \text{ in } 20\text{-}\text{D}, \text{ N}{=}15, \text{ mFE}{=}2.51\text{e}7\\ \# \text{ ERT } 10\% 90\% \text{ RT}_{\text{SUCC}} \end{array}$	$\begin{array}{c} f_{112} \text{ in } 5\text{-D}, \text{ N=15, mFE=9378} \\ \Delta f & \# \text{ ERT } 10\% 90\% \text{ RT}_{\text{succ}} \end{array}$	$ \begin{array}{c} \textbf{f_{112 in 20-D, N=15, mFE=187012}} \\ \# \text{ ERT } 10\% 90\% \text{ RT}_{\text{SUCC}} \end{array} $
$ \begin{array}{c c} f111 \text{ in } 5\text{-D}, \text{ N=15, mFE=1.11e7} \\ \hline f & \text{ # ERT } 10\% 90\% \text{ RT}_{\text{succ}} \\ \hline 10 & 15 6.9e3 4.4e3 9.5e3 6.9e3 \\ \end{array} $	$ \begin{array}{c} \textbf{f111 in 20-D, N=15, mFE=2.51e7} \\ \# \ \text{ERT} \ 10\% \ 90\% \ \text{RT}_{\text{succ}} \\ 0 \ 18e+0 \ 17e+0 \ 18e+0 \ 1.8e7 \end{array} $	$ \begin{array}{c} f_{112} \text{ in 5-D, N=15, mFE=9378} \\ f_{112} \text{ in 5-D, N=15, mFE=9378} \\ \underline{\Delta f} \ \# \ \text{ERT} \ 10\% \ 90\% \ \text{RT}_{\text{succ}} \\ \hline 10 \ 15 \ 4.3e2 \ 2.6e2 \ 6.1e2 \ 4.3e2 \end{array} $	$\begin{array}{c} f_{112} \text{ in } 20\text{-}\text{D}, \text{ N=15}, \text{ mFE=187012} \\ \# \text{ ERT } 10\% 90\% \text{ RT}_{\text{succ}} \\ 15 2.6 \text{e4} 2.4 \text{e4} 2.7 \text{e4} 2.6 \text{e4} \end{array}$
$ \begin{array}{c c} f_{111} \text{ in } 5\text{-} \text{D}, \text{ N} = 15, \text{ mFE} = 1.11 \text{ er} \\ \hline \Delta f & \# \text{ ERT } 10\% & 90\% & \text{RT}_{\text{SUCC}} \\ \hline 10 & 15 & 6.9 \text{e3} & 4.4 \text{e3} & 9.5 \text{e3} & 6.9 \text{e3} \\ 1 & 14 & 1.5 \text{e6} & 9.3 \text{e5} & 2.2 \text{e6} & 1.1 \text{e6} \\ \end{array} $		$ \frac{f_{112} \text{ in 5-D}, \text{ N=15}, \text{ mFE=9378}}{f_{11} \text{ ERT} 10\% 90\% \text{ RT}_{\text{succ}}} \\ \frac{\Delta f}{10} \frac{\# \text{ ERT} 10\% 90\% \text{ RT}_{\text{succ}}}{115 4.3 \text{ e2} 2.6 \text{ e2} 6.1 \text{ e2} 4.3 \text{ e2}} \\ \frac{1}{15 1.7 \text{ e3} 1.4 \text{ e3} 2.0 \text{ e3} 1.7 \text{ e3}} \\ \frac{1}{15 1.7 \text{ e3} 1.4 \text{ e3} 2.0 \text{ e3} 1.7 \text{ e3}} \\ \frac{1}{15 1.7 \text{ e3} 1.4 \text{ e3} 2.0 \text{ e3} 1.7 \text{ e3}} \\ \frac{1}{15 1.7 \text{ e3} 1.4 \text{ e3} 2.0 \text{ e3} 1.7 \text{ e3}} \\ \frac{1}{15 1.7 \text{ e3} 1.4 \text{ e3} 2.0 \text{ e3} 1.7 \text{ e3}} \\ \frac{1}{15 1.7 \text{ e3} 1.4 \text{ e3} 2.0 \text{ e3} 1.7 \text{ e3}} \\ \frac{1}{15 1.7 \text{ e3} 1.4 \text{ e3} 2.0 \text{ e3} 1.7 \text{ e3}} \\ \frac{1}{15 1.7 \text{ e3} 1.4 \text{ e3} 2.0 \text{ e3} 1.7 \text{ e3}} \\ \frac{1}{15 1.7 \text{ e3} 1.4 \text{ e3} 2.0 \text{ e3} 1.7 \text{ e3}} \\ \frac{1}{15 1.7 \text{ e3} 1.4 \text{ e3} 2.0 \text{ e3} 1.7 \text{ e3}} \\ \frac{1}{15 1.7 \text{ e3} 1.4 \text{ e3} 2.0 \text{ e3} 1.7 \text{ e3}} \\ \frac{1}{15 1.7 \text{ e3} 1.4 \text{ e3} 2.0 \text{ e3} 1.7 \text{ e3}} \\ \frac{1}{15 1.7 \text{ e3} 1.4 \text{ e3} 2.0 \text{ e3} 1.7 \text{ e3}} \\ \frac{1}{15 1.7 \text{ e3} 1.4 \text{ e3} 2.0 \text{ e3} 1.7 \text{ e3}} \\ \frac{1}{15 1.7 \text{ e3} 1.4 \text{ e3} 2.0 \text{ e3} 1.7 \text{ e3}} \\ \frac{1}{15 1.7 \text{ e3} 1.4 \text{ e3} 2.0 \text{ e3} 1.7 \text{ e3}} \\ \frac{1}{15 1.7 \text{ e3} 1.4 \text{ e3} 2.0 \text{ e3} 1.7 \text{ e3}} \\ \frac{1}{15 1.7 \text{ e3} 1.4 \text{ e3} 2.0 \text{ e3} 1.7 \text{ e3}} \\ \frac{1}{15 1.7 \text{ e3} 1.4 \text{ e3} 2.0 \text{ e3} 1.7 \text{ e3}} \\ \frac{1}{15 1.7 \text{ e3} 1.4 \text{ e3} 2.0 \text{ e3} 1.7 \text{ e3}} \\ \frac{1}{15 1.7 \text{ e3} 1.4 \text{ e3} 2.0 \text{ e3} 1.7 \text{ e3} 1.7 \text{ e3} 1.7 \text{ e3}} \\ \frac{1}{15 1.7 \text{ e3} 1.4 \text{ e3} 2.0 \text{ e3} 1.7 e3$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c} \textbf{f111 in 20-D, N=15, mFE=2.51e7} \\ \textbf{\# ERT 10\% 90\% RT_{succ}} \\ 0 \ 18e+0 \ 17e+0 \ 18e+0 \ 1.8e7 \\ $	$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c} \textbf{f111 in 20-D, N=15, mFE=2.51e7} \\ \# \ \text{ERT} \ 10\% \ 90\% \ \text{RT}_{\text{succ}} \\ 0 \ 18e+0 \ 17e+0 \ 18e+0 \ 1.8e7 \\ . \\ . \\ . \\ . \\ . \\ . \\ . \\ . \\ . \\ $	$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c} f_{112} \text{ in } 20\text{-}D, \ N=15, \ \text{mFE}=187012 \\ \# \ \text{ERT} \ 10\% \ 90\% \ \text{RT}_{\text{Succ}} \\ 15 \ 2.6e4 \ 2.4e4 \ 2.7e4 \ 2.6e4 \\ 15 \ 6.9e4 \ 5.6e4 \ 8.1e4 \ 6.9e4 \\ 15 \ 7.9e4 \ 6.7e4 \ 9.1e4 \ 7.9e4 \\ 15 \ 8.6e4 \ 7.4e4 \ 1.0e5 \ 8.6e4 \end{array} $
$ \begin{array}{c c} f_{111} \ in \ 5\text{-D}, \ \text{N=15}, \ \text{mFE=1.11e7} \\ \hline \Delta f & \# \ \text{ERT} & 10\% & 90\% & \text{RT}_{\text{succ}} \\ \hline 10 & 15 & 6.9e3 & 4.4e3 & 9.5e3 & 6.9e3 \\ 1 & 14 & 1.5e6 & 9.3e5 & 2.2e6 & 1.1e6 \\ \hline \text{le-1} & 8 & 8.8e6 & 6.3e6 & 1.3e7 & 4.8e6 \\ \hline \text{le-3} & 4 & 2.3e7 & 1.4e7 & 5.1e6 \\ \hline \text{le-5} & 3 & 3.1e7 & 1.8e7 & 8.8e7 & 6.8e6 \\ \end{array} $	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{ccccccc} f_{112} \ in \ 20\text{-D}, \ N=15, \ mFE=187012 \\ \# \ ERT \ 10\% \ 90\% \ RT_{Succ} \\ 15 \ 2.6e4 \ 2.4e4 \ 2.7e4 \ 2.6e4 \\ 15 \ 6.9e4 \ 5.6e4 \ 8.1e4 \ 6.9e4 \\ 15 \ 6.9e4 \ 5.6e4 \ 8.1e4 \ 7.9e4 \\ 15 \ 8.6e4 \ 7.4e4 \ 1.0e5 \ 8.6e4 \\ 15 \ 9.0e4 \ 7.7e4 \ 1.0e5 \ 9.0e4 \\ \end{array} $
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	f111 in 20-D N=15, mFE=2.51e7 # ERT 10% 90% RT _{succ} 0 18e+0 17e+0 18e+0 1.8e7 	$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	f111 in 20-D, N=15, mFE=2.51e7 # ERT 10% 90% RT _{succ} 0 18e+0 17e+0 18e+0 1.8e7 . . </td <td>$\begin{array}{c c c c c c c c c c c c c c c c c c c$</td> <td>$\begin{array}{c} f_{112} \ in \ 20\text{-D}, \ N=15, \ mFE=187012 \\ \# \ ERT \ 10\% \ 90\% \ RT_{Succ} \\ 15 \ 2.6e4 \ 2.4e4 \ 2.7e4 \ 2.6e4 \\ 15 \ 7.9e4 \ 6.7e4 \ 9.1e4 \ 7.9e4 \\ 15 \ 7.9e4 \ 6.7e4 \ 9.1e4 \ 7.9e4 \\ 15 \ 8.6e4 \ 7.4e4 \ 1.0e5 \ 8.6e4 \\ 15 \ 9.0e4 \ 7.7e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.3e4 \ 8.0e4 \ 1.1e5 \ 9.3e4 \\ 15 \ 9.3e4 \ 8.0e4 \ 1.1e5 \ 9.3e4 \\ \end{array}$</td>	$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c} f_{112} \ in \ 20\text{-D}, \ N=15, \ mFE=187012 \\ \# \ ERT \ 10\% \ 90\% \ RT_{Succ} \\ 15 \ 2.6e4 \ 2.4e4 \ 2.7e4 \ 2.6e4 \\ 15 \ 7.9e4 \ 6.7e4 \ 9.1e4 \ 7.9e4 \\ 15 \ 7.9e4 \ 6.7e4 \ 9.1e4 \ 7.9e4 \\ 15 \ 8.6e4 \ 7.4e4 \ 1.0e5 \ 8.6e4 \\ 15 \ 9.0e4 \ 7.7e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.3e4 \ 8.0e4 \ 1.1e5 \ 9.3e4 \\ 15 \ 9.3e4 \ 8.0e4 \ 1.1e5 \ 9.3e4 \\ \end{array} $
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c} \textbf{f111 in 20\text{-}D, N=15, mFE=2.51e7} \\ \# \ ERT \ 10\% \ 90\% \ RT_{succ} \\ \hline 0 \ 18e+0 \ 17e+0 \ 18e+0 \ 1.8e7 \\ \hline . & . & . \\ \hline . & . & . \\ f113 \ \textbf{in 20\text{-}D, N=15, mFE=795352} \\ \# \ ERT \ 10\% \ 90\% \ RT_{succ} \\ \end{array} $	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$ f112 in 20-D, N=15, mFE=187012 \\ \# ERT 10\% 90\% RT_{Succ} \\ 15 2.6e4 2.4e4 2.7e4 2.6e4 \\ 15 6.9e4 5.6e4 8.1e4 6.9e4 \\ 15 6.9e4 5.6e4 8.1e4 7.9e4 \\ 15 8.6e4 7.4e4 1.0e5 8.6e4 \\ 15 8.6e4 7.4e4 1.0e5 9.0e4 \\ 15 9.0e4 7.7e4 1.0e5 9.0e4 \\ 15 9.3e4 8.0e4 1.1e5 9.3e4 \\ f114 in 20-D, N=15, mFE=2.53e6 \\ \# ERT 10\% 90\% RT_{succ} \\ $
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c} \textbf{f111 in 20-D, N=15, mFE=2.51e7} \\ \# \ \ \textbf{ERT} \ \ 10\% \ \ 90\% \ \ \textbf{RT}_{\texttt{succ}} \\ \hline 0 \ \ 18e+0 \ \ 17e+0 \ \ 18e+0 \ \ 1.8e7 \\ \hline . \ . \ . \ . \ . \ . \ . \ . \ . \ .$	$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c} \textbf{f111 in 20-D, N=15, mFE=2.51e7} \\ \# \ \ \textbf{ERT} \ \ 10\% \ \ 90\% \ \ \textbf{RT}_{\text{succ}} \\ \hline 0 \ \ 18e+0 \ \ 17e+0 \ \ 18e+0 \ \ 1.8e7 \\ \hline \cdot \$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c} \textbf{f_{112} in 20-D, N=15, mFE=187012} \\ \# \ ERT \ 10\% \ 90\% \ RT_{Succ} \\ 15 \ 2.6e4 \ 2.4e4 \ 2.7e4 \ 2.6e4 \\ 15 \ 6.9e4 \ 5.6e4 \ 8.1e4 \ 6.9e4 \\ 15 \ 6.9e4 \ 5.6e4 \ 8.1e4 \ 6.9e4 \\ 15 \ 8.6e4 \ 7.4e4 \ 1.0e5 \ 8.6e4 \\ 15 \ 9.0e4 \ 7.7e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.3e4 \ 8.0e4 \ 1.1e5 \ 9.3e4 \\ 115 \ 9.3e4 \ 8.0e4 \ 1.1e5 \ 9.3e4 \\ \hline \textbf{f_{114} in 20-D, N=15, mFE=2.53e6} \\ \# \ ERT \ 10\% \ 90\% \ RT_{Succ} \\ 15 \ 2.1e5 \ 1.8e5 \ 2.4e5 \ 2.1e5 \\ 15 \ 1.1e6 \ 9.5e5 \ 1.3e6 \ 1.1e6 \\ \end{array} $
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$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c} f_{112} \mbox{ in } 20\mbox{-}D, \mbox{ N=15}, \mbox{ mFE=187012} \\ \# \ ERT \ 10\% \ 90\% \ RT_{\rm Succ} \\ 15 \ 2.6e4 \ 2.4e4 \ 2.7e4 \ 2.6e4 \\ 15 \ 6.9e4 \ 5.6e4 \ 8.1e4 \ 6.9e4 \\ 15 \ 6.9e4 \ 5.6e4 \ 8.1e4 \ 6.9e4 \\ 15 \ 8.6e4 \ 7.4e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.0e4 \ 7.7e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.0e4 \ 7.7e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.0e4 \ 7.7e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.0e4 \ 7.7e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.0e4 \ 7.7e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.0e4 \ 7.7e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.0e4 \ 7.7e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.0e4 \ 7.7e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.0e4 \ 7.7e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.0e4 \ 7.7e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.0e4 \ 7.7e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.1e5 \ 1.3e6 \ 1.4e5 \ 1.3e6 \ 1.1e6 \\ 1.5 \ 1.4e6 \ 1.3e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.7e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.7e6 \ 1.4e6 \ 1.9e6 \ 1.7e6 \\ 1.7e6 \ 1.7e6 \ 1.7e6 \ 1.7e6 \\ 1.7e6 \ 1.7e6 \ 1.7e6 \ 1.7e6 \ 1.7e6 \ 1.7e6 \\ 1.7e6 \ 1.7e6 $
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$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c} \textbf{f111 in 20-D, N=15, mFE=2.51e7} \\ \# \ ERT \ 10\% \ 90\% \ RT_{succ} \\ \hline 0 \ 18e+0 \ 17e+0 \ 18e+0 \ 1.8e7 \\ \hline$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
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$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c} f{111 in 20-D, N=15, mFE=2.51e7} \\ \# \ ERT \ 10\% \ 90\% \ RT_{succ} \\ \hline 0 \ 18e+0 \ 17e+0 \ 18e+0 \ 1.8e7 \\ \hline$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
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$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c} \textbf{f112 in 20-D, N=15, mFE=187012} \\ \# \ ERT \ 10\% \ 90\% \ RT_{succ} \\ \hline \textbf{f12 2.6e4 2.4e4 2.7e4 2.6e4 } \\ 15 2.6e4 2.4e4 2.7e4 2.6e4 \\ 15 6.9e4 5.6e4 8.1e4 6.9e4 \\ 15 7.9e4 6.7e4 9.1e4 7.9e4 \\ 15 8.6e4 7.4e4 1.0e5 8.6e4 \\ 15 9.0e4 7.7e4 1.0e5 9.0e4 \\ 15 9.3e4 8.0e4 1.1e5 9.3e4 \\ \hline \textbf{f114 in 20-D, N=15, mFE=2.53e6} \\ \# \ ERT \ 10\% \ 90\% \ RT_{succ} \\ \hline \textbf{f12 166 9.5e5 1.3e6 1.1e6} \\ 15 1.4e6 1.3e6 1.6e6 1.4e6 \\ 15 1.6e6 1.4e6 1.8e6 1.6e6 \\ 15 1.6e6 1.4e6 1.8e6 1.6e6 \\ 15 1.6e6 1.4e6 1.8e6 1.6e6 \\ 15 1.6e5 1.4e6 1.9e6 1.7e6 \\ \hline \textbf{f116 in 20-D, N=15, mFE=1.69e6} \\ \# \ ERT \ 10\% \ 90\% \ RT_{succ} \\ \hline \textbf{f15 8.6e5 7.5e5 9.7e5 8.6e5} \\ \hline \textbf{5 1.9c5 8.7e5 1.1e6 9.7e5} \\ 15 0.0e6 9.3e5 1.1e6 1.0e6 \\ \hline \textbf{5 1.0e6 15 1.1e6 1.2e6 1.1e6 } \\ \hline \textbf{f16 in 20-D, N=15, mFE=1.69e6} \\ \hline \textbf{f16 in 20-D, N=15, mFE=1.61e6 \\ \hline \textbf{f16 in 20-D, N=15 \\ \hline \textbf{f16 in 20-D, N=15 } \\ \hline \textbf{f16 in 20-D, N=15 \\ \hline \textbf{f16 in 20-D, N=15 \\ \hline \textbf{f16 in 20-D, N=15 } \\ \hline f16 in 20-D, N=15 \\ \hline \textbf{f16 in 20-D, N=15 \\ \hline \textbf{f16 in 20-D, N=15 \\ $
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c} f_{112} \mbox{ in } 20\mbox{-}D, \mbox{ N=15}, \mbox{ mFE=187012} \\ \# \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c} f_{112} \mbox{ in } 20\text{-}D, \ N=15, \ mFE=187012 \\ \# \ ERT \ 10\% \ 90\% \ RT_{succ} \\ 15 \ 2.6e4 \ 2.4e4 \ 2.7e4 \ 2.6e4 \\ 15 \ 6.9e4 \ 2.4e4 \ 2.7e4 \ 2.6e4 \\ 15 \ 9.0e4 \ 2.4e4 \ 2.4e5 \ 2.6e4 \\ 15 \ 9.0e4 \ 7.7e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.3e4 \ 8.0e4 \ 1.1e5 \ 9.3e4 \\ \hline 15 \ 9.3e4 \ 8.0e4 \ 1.1e5 \ 9.3e4 \\ \hline f_{114} \ in \ 20\text{-}D, \ N=15, \ mFE=2.53e6 \\ \# \ ERT \ 10\% \ 90\% \ RT_{succ} \\ 15 \ 2.1e5 \ 1.8e5 \ 2.4e5 \ 2.1e5 \\ 15 \ 1.4e6 \ 1.3e6 \ 1.4e6 \ 1.4e6 \\ 15 \ 1.6e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.6e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.7e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.7e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.7e6 \ 1.4e5 \ 9.7e5 \ 8.3e5 \ 7.1e5 \\ 15 \ 8.6e5 \ 7.5e5 \ 9.7e5 \ 8.3e5 \ 7.1e5 \\ 15 \ 9.7e5 \ 8.7e5 \ 1.1e6 \ 9.7e5 \\ 15 \ 9.7e5 \ 8.7e5 \ 1.1e6 \ 9.7e5 \\ 15 \ 1.0e6 \ 9.3e5 \ 1.1e6 \ 1.0e6 \\ 15 \ 1.1e6 \ 9.7e5 \ 1.2e6 \ 1.1e6 \\ 15 \ 1.1e6 \ 1.3e6 \ 1.1e6 \\ 15 \ 1.1e6 \ 1.3e6 \ 1.1e6 \\ 1.1e6 \ 1.1e6 \ 1.3e6 \ 1.1e6 \\ 1.1e6 \ 1.1e6 \ 1.3e6 \ 1.1e6 \\ 1.6e6 \ 1.5 \ 1.1e6 \ 1.8e6 \ 1.1e6 \\ 15 \ 1.1e6 \ 1.8e6 \ 1.1e6 \ 1.8e6 \ 1.1e6 \\ 15 \ 1.1e6 \ 9.7e5 \ 1.2e6 \ 1.8e6 \ 1.1e6 \\ 15 \ 1.1e6 \ 1.3e6 \ 1.1e6 \ 1.8e6 \ 1.1e6 \\ 15 \ 1.1e6 \ 1.3e6 \ 1.1e6 \ 1.8e6 \ 1.1e6 \\ 15 \ 1.1e6 \ 1.8e6 \ 1.8e6 \ 1.8e6 \ 1.8e6 \ 1.8e6 \\ 1.6e6 \ 15 \ 1.1e6 \ 1.8e6 \ 1.8e6 \ 1.8e6 \ 1.8e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.1e6 \ 9.7e5 \ 1.2e6 \ 1.8e6 $
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c} f_{112} \mbox{ in } 20\mbox{-}D, \mbox{ N=15}, \mbox{ mFE=187012} \\ \# \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c} f_{112} \mbox{ in } 20\text{-}D, \ N=15, \ mFE=187012 \\ \# \ ERT \ 10\% \ 90\% \ RT_{\rm succ} \\ 15 \ 2.6e4 \ 2.4e4 \ 2.7e4 \ 2.6e4 \\ 15 \ 6.9e4 \ 2.4e4 \ 2.7e4 \ 2.6e4 \\ 15 \ 9.0e4 \ 2.6e4 \ 9.1e4 \ 7.9e4 \\ 15 \ 9.3e4 \ 8.0e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.3e4 \ 8.0e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.3e4 \ 8.0e4 \ 1.1e5 \ 9.3e4 \\ \hline f_{114} \ in \ 20\text{-}D, \ N=15, \ mFE=2.53e6 \\ \# \ ERT \ 10\% \ 90\% \ RT_{\rm succ} \\ 15 \ 2.1e5 \ 1.3e6 \ 1.4e6 \ 1.3e6 \ 1.4e6 \\ 15 \ 1.6e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.6e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.6e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.6e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.6e5 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.6e5 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.6e5 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.6e5 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.6e5 \ 7.5e5 \ 9.7e5 \ 8.3e5 \ 7.1e5 \\ 15 \ 8.6e5 \ 7.5e5 \ 9.7e5 \ 8.3e5 \ 7.1e5 \\ 15 \ 9.7e5 \ 8.7e5 \ 1.1e6 \ 9.7e5 \\ 15 \ 1.0e6 \ 9.3e5 \ 1.1e6 \ 9.7e5 \\ 15 \ 1.0e6 \ 9.3e5 \ 1.2e6 \ 1.1e6 \\ 15 \ 1.1e6 \ 1.0e6 \ 1.3e6 \ 1.1e6 \\ 15 \ 1.1e6 \ 1.0e6 \ 1.3e6 \ 1.1e6 \\ 15 \ 1.1e6 \ 1.2e6 \ 1.2e6 \ 1.1e6 \\ 15 \ 1.1e6 \ 1.2e6 \ 1.2e6 \ 1.1e6 \ 1.1e6 \\ 15 \ 1.1e6 \ 1.2e6 \ 1.2e6 \ 1.2e6 \ 1.2e6 \ 1.1e6 \\ 15 \ 1.1e6 \ 1.2e6 \ 1.2e6 \ 1.2e6 \ 1.2e6 \ 1.1e6 \ 1.2e6 \$
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c} \textbf{f112 in 20-D, N=15, mFE=187012} \\ \# ERT 10\% 90\% RT_{Succ} \\ 15 2.6e4 2.4e4 2.7e4 2.6e4 \\ 15 6.9e4 5.6e4 8.1e4 6.9e4 \\ 15 7.9e4 6.7e4 9.1e4 7.9e4 \\ 15 8.6e4 7.4e4 1.0e5 8.6e4 \\ 15 9.0e4 7.7e4 1.0e5 9.0e4 \\ 15 9.3e4 8.0e4 1.1e5 9.3e4 \\ \hline \textbf{f114 in 20-D, N=15, mFE=2.53e6} \\ \# ERT 10\% 90\% RT_{Succ} \\ 15 2.1e5 1.8e5 2.4e5 2.1e5 \\ 15 1.4e6 1.3e6 1.6e6 1.4e6 \\ 15 1.6e6 1.4e6 1.8e6 1.6e6 \\ 15 1.6e6 1.4e6 1.8e6 1.6e6 \\ 15 1.6e5 1.4e5 1.9e5 8.3e5 7.1e5 \\ 15 8.6e5 7.5e5 9.7e5 8.6e5 \\ 15 9.3e5 1.1e6 9.7e5 1.1e6 9.7e5 \\ 15 9.3e5 1.1e6 9.7e5 1.1e6 9.7e5 \\ 15 9.7e5 8.7e5 1.1e6 9.7e5 \\ 15 9.7e5 8.7e5 1.1e6 9.7e5 \\ 15 9.7e5 8.7e5 1.1e6 9.7e5 \\ 15 1.0e6 9.3e5 1.1e6 1.0e6 \\ 15 1.1e6 1.0e6 1.3e6 1.1e6 \\ 15 1.1e6 1.0e5 1.8e5 \\ 1.1e6 1.9e5 1.2e6 1.1e6 \\ 15 1.1e6 9.7e5 1.1e6 9.7e5 \\ 1.1e6 1.9e5 1.2e6 1.1e6 \\ 15 1.1e6 1.0e5 1.3e6 1.1e6 \\ 15 1.1e6 1.0e5 1.3e6 1.1e6 \\ 15 1.1e6 1.0e5 1.3e4 1.2e4 1.3e4 \\ 15 2.1e4 2.0e4 2.2e4 2.1e4 \\ 15 2.8e4 2.7e4 2.9e4 2.8e4 \\ \end{array}$
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c} f_{112} \mbox{ in } 20\text{-}D, \ N=15, \ mFE=187012 \\ \# \ ERT \ 10\% \ 90\% \ RT_{succ} \\ 15 \ 2.6e4 \ 2.4e4 \ 2.7e4 \ 2.6e4 \\ 15 \ 6.9e4 \ 2.4e4 \ 2.7e4 \ 2.6e4 \\ 15 \ 9.0e4 \ 2.4e4 \ 2.7e4 \ 2.6e4 \\ 15 \ 9.0e4 \ 7.7e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.0e4 \ 7.7e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.0e4 \ 7.7e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.0e4 \ 7.7e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.0e4 \ 7.7e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.3e4 \ 8.0e4 \ 1.1e5 \ 9.3e4 \\ f_{114} \ in \ 20\text{-}D, \ N=15, \ mFE=2.53e6 \\ \# \ ERT \ 10\% \ 90\% \ RT_{succ} \\ 15 \ 2.1e5 \ 1.8e5 \ 2.4e5 \ 2.1e5 \\ 15 \ 1.4e6 \ 1.3e6 \ 1.4e6 \ 1.4e6 \\ 15 \ 1.6e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.6e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.7e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.7e6 \ 1.4e6 \ 1.8e5 \ 7.1e5 \\ 15 \ 8.6e5 \ 7.5e5 \ 9.7e5 \ 8.3e5 \ 7.1e5 \\ 15 \ 9.7e5 \ 8.7e5 \ 1.1e6 \ 9.7e5 \\ 15 \ 9.7e5 \ 8.7e5 \ 1.1e6 \ 9.7e5 \\ 15 \ 1.0e6 \ 9.3e5 \ 1.1e6 \ 1.0e6 \\ 15 \ 1.1e6 \ 9.7e5 \ 1.2e6 \ 1.1e6 \\ 15 \ 1.1e6 \ 9.7e5 \ 1.2e6 \ 1.1e6 \\ 15 \ 1.1e6 \ 9.7e5 \ 1.2e6 \ 1.1e6 \\ 15 \ 1.1e6 \ 9.7e5 \ 1.2e6 \ 1.1e6 \\ 15 \ 1.1e6 \ 9.7e5 \ 1.2e6 \ 1.1e6 \\ 15 \ 1.1e6 \ 1.3e6 \ 1.1e6 \\ 1.5 \ 1.1e6 \ 1.3e6 \ 1.1e6 \\ 1.5 \ 1.1e6 \ 1.3e6 \ 1.1e6 \\ 1.5 \ 1.1e6 \ 1.3e6 \ 1.1e6 \ 1.3e6 \ 1.1e6 \\ 15 \ 1.1e6 \ 1.3e4 \ 1.2e4 \ 1.2$
$\begin{array}{c c c c c c c c c c c c c c c c c c c $		$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	$ \begin{array}{c} f_{112} \mbox{ in } 20\text{-}D, \ N=15, \ mFE=187012 \\ \# \ ERT \ 10\% \ 90\% \ RT_{\rm succ} \\ 15 \ 2.6e4 \ 2.4e4 \ 2.7e4 \ 2.6e4 \\ 15 \ 6.9e4 \ 2.6e4 \ 2.7e4 \ 2.6e4 \\ 15 \ 6.9e4 \ 5.6e4 \ 8.1e4 \ 6.9e4 \\ 15 \ 7.9e4 \ 6.7e4 \ 9.1e4 \ 7.9e4 \\ 15 \ 8.6e4 \ 7.4e4 \ 1.0e5 \ 8.6e4 \\ 15 \ 9.0e4 \ 7.7e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.3e4 \ 8.0e4 \ 1.1e5 \ 9.3e4 \\ \hline f_{114} \ in \ 20\text{-}D, \ N=15, \ mFE=2.53e6 \\ \# \ ERT \ 10\% \ 90\% \ RT_{\rm succ} \\ 15 \ 2.1e5 \ 1.8e5 \ 2.4e5 \ 2.1e5 \\ 15 \ 1.4e6 \ 1.3e6 \ 1.6e6 \ 1.4e6 \\ 15 \ 1.6e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.6e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.6e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.7e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.7e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.7e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.7e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.7e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.7e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.7e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.7e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.7e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.6e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.7e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.6e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.6e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.6e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.6e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.1e6 \ 1.0e6 \ 1.3e6 \ 1.1e6 \\ 15 \ 1.1e6 \ 1.0e6 \ 1.3e6 \ 1.1e6 \\ 15 \ 1.1e6 \ 1.0e6 \ 1.3e6 \ 1.1e6 \\ 15 \ 1.1e6 \ 1.2e4 \ 1.2e4 \ 1.8e4 \ 1.3e4 \\ 15 \ 2.8e4 \ 2.7e4 \ 2.2e4 \ 2.1e4 \\ 15 \ 2.8e4 \ 2.7e4 \ 2.8e4 \ 2.8e4 \\ 15 \ 4.0e4 \ 3.9e4 \ 4.1e4 \ 4.0e4 \\ 15 \ 4.7e4 \ 4.6e4 \ 4.8e4 \ 4.7e4 \ 4.7e4 \ 1.8e4 \ 1.7e4 \ 1.7e6 \ 1.$
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c c c c c c c c c c c c c c c c c c c $
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $		$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c} f_{112} \mbox{ in } 20\text{-}D, \ N=15, \ mFE=187012 \\ \# \ ERT \ 10\% \ 90\% \ RT_{\rm succ} \\ 15 \ 2.6e4 \ 2.4e4 \ 2.7e4 \ 2.6e4 \\ 15 \ 6.9e4 \ 2.6e4 \ 2.7e4 \ 2.6e4 \\ 15 \ 6.9e4 \ 5.6e4 \ 8.1e4 \ 6.9e4 \\ 15 \ 7.9e4 \ 6.7e4 \ 9.1e4 \ 7.9e4 \\ 15 \ 8.6e4 \ 7.4e4 \ 1.0e5 \ 8.6e4 \\ 15 \ 9.0e4 \ 7.7e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.0e4 \ 7.7e4 \ 1.0e5 \ 9.0e4 \\ 15 \ 9.3e4 \ 8.0e4 \ 1.1e5 \ 9.3e4 \\ f_{114} \ mbox{ in } 20\text{-}D, \ N=15, \ mFE=2.53e6 \\ \# \ ERT \ 10\% \ 90\% \ RT_{\rm succ} \\ 15 \ 2.1e5 \ 1.8e5 \ 2.4e5 \ 2.1e5 \\ 15 \ 1.1e6 \ 1.3e6 \ 1.6e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.6e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.6e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.6e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.7e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.7e6 \ 1.4e6 \ 1.8e6 \ 1.6e6 \\ 15 \ 1.7e5 \ 8.7e5 \ 8.3e5 \ 7.1e5 \\ 5 \ 9.7e5 \ 8.7e5 \ 8.1e6 \ 5.1e6 \\ 5 \ 1.1e6 \ 9.7e5 \ 1.1e6 \ 9.7e5 \ 1.1e6 \\ 15 \ 1.1e6 \ 1.0e6 \ 1.3e6 \ 1.1e6 \\ 15 \ 1.1e6 \ 1.0e6 \ 1.3e6 \ 1.1e6 \\ 15 \ 1.1e6 \ 1.0e6 \ 1.3e6 \ 1.1e6 \\ 15 \ 1.1e6 \ 1.2e4 \ 1.2e4 \ 1.4e4 \ 1.3e4 \\ 15 \ 2.8e4 \ 2.7e4 \ 2.9e4 \ 2.1e4 \ 1.3e4 \\ 15 \ 2.8e4 \ 2.7e4 \ 2.9e4 \ 2.8e4 \\ 15 \ 4.0e4 \ 3.9e4 \ 4.1e4 \ 4.0e4 \\ 15 \ 4.2e4 \ 1.6e4 \ 4.8e4 \ 4.7e4 \ 1.5 \ 5.2e4 \ 5.1e4 \ 5.3e4 \ 5.2e4 \\ f_{120} \mbox{ in } 20\text{-}N=15, \ mFE=2.35e7 \ 7.1e5 \ 5.2e4 \ 5.1e4 \ 5.2e4 \ $
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c} f_{112} \mbox{ in PE=187012} \\ \# \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	f112 in 20-D, N=15, mFE=187012 # ERT 10% 90% RT _{SUCC} 15 2.6e4 2.4e4 2.7e4 2.6e4 15 6.9e4 5.6e4 8.1e4 6.9e4 15 7.9e4 6.7e4 9.1e4 7.9e4 15 9.0e4 7.7e4 1.0e5 8.6e4 15 9.0e4 7.7e4 1.0e5 9.0e4 15 9.3e4 8.0e4 1.1e5 9.3e4 15 9.3e4 8.0e4 1.1e5 9.3e4 15 9.3e4 8.0e4 1.1e5 9.3e4 15 9.3e5 1.3e6 1.1e6 15 2.1e5 1.8e5 2.4e5 2.1e5 15 1.1e6 9.5e5 1.3e6 1.1e6 15 1.6e6 1.4e6 1.8e6 1.6e6 15 1.6e6 1.4e6 1.8e6 1.6e6 15 1.6e5 1.4e6 1.8e6 1.6e6 15 1.7e6 1.4e6 1.8e5 7.1e5 15 8.6e5 7.5e5 9.7e5 8.3e5 7.1e5 15 8.6e5 7.5e5 9.7e5 8.6e5 15 1.0e6 9.3e5 1.1e6 1.0e6 15 1.1e6 1.0e6 1.3e6 1.1e6 15 1.1e6 1.2e4 1.2e4 1.1e4 15 1.2e4 1.2e4 1.4e4 1.3e4 15 2.8e4 2.7e4 2.2e4 2.1e4 15 2.8e4 2.7e4 2.9e4 2.8e4 15 3.2e4 5.1e4 5.3e4 5.2e4 15 4.6e4 4.8e4 4.7e4 15 5.2e4 5.1e4 5.3e4 5.2e4 15 2.1e4 5.3e4 5.2e4 15 2.1e4 5.3e4 5.2e4
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	f112 in 20-D, N=15, mFE=187012 # ERT 10% 90% RT _{succ} 15 2.6e4 2.4e4 2.7e4 2.6e4 15 6.9e4 5.6e4 8.1e4 6.9e4 15 7.9e4 6.7e4 9.1e4 7.9e4 15 8.6e4 7.4e4 1.0e5 8.6e4 15 9.0e4 7.7e4 1.0e5 9.0e4 15 9.3e4 8.0e4 1.1e5 9.3e4 f114 in 20-D, N=15, mFE=2.53e6 # ERT 10% 90% RT _{succ} 15 2.1e5 1.8e5 2.4e5 2.1e5 15 1.1e6 9.5e5 1.3e6 1.1e6 15 1.6e6 1.4e6 1.8e6 1.6e6 15 1.6e6 1.4e6 1.8e6 1.6e6 15 1.6e5 9.7e5 8.3e5 7.1e5 15 7.1e5 5.9e5 8.3e5 7.1e6 15 7.1e5 5.9e5 8.3e5 7.1e6 15 7.1e5 5.9e5 8.3e5 7.1e6 15 1.6e6 1.9e6 1.1e6 15 1.1e6 9.7e5 1.1e6 9.7e5 15 7.1e5 5.9e5 8.3e5 7.1e6 15 7.1e5 8.7e5 1.1e6 9.7e5 15 1.0e6 9.3e5 1.1e6 1.0e6 15 1.1e6 1.0e6 1.3e6 1.1e6 15 1.1e6 1.0e6 1.3e6 1.1e6 15 1.3e4 1.2e4 1.4e4 1.3e4 15 2.1e4 2.0e4 2.2e4 2.1e4 15 2.2e4 5.1e4 2.9e4 2.8e4 15 4.0e4 3.9e4 4.1e4 4.0e4 15 5.2e4 5.1e4 5.3e4 5.2e4 15 4.0e4 4.8e4 4.7e4 15 4.2e4 1.6e4 3.8e4 4.7e4
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	f112 in 20-D, N=15, mFE=187012 # ERT 10% 90% RTsucc 15 2.6e4 2.4e4 2.7e4 2.6e4 15 6.9e4 5.6e4 8.1e4 6.9e4 15 7.9e4 6.7e4 9.1e4 7.9e4 15 9.3e4 7.7e4 1.0e5 8.6e4 15 9.3e4 8.0e4 1.1e5 9.3e4 15 9.3e4 8.0e4 1.1e5 9.3e4 15 9.3e4 8.0e4 1.1e5 9.3e4 f114 in 20-D, N=15, mFE=2.33e6 # ERT 10% 90% RTsucc 15 1.4e6 1.3e6 1.6e6 15 1.6e6 1.4e6 1.8e6 1.6e6 15 1.6e6 1.4e6 1.8e6 1.6e6 15 1.7e6 1.4e6 1.8e6 1.6e6 15 1.7e6 1.8e5 7.9e5 8.3e5 7.1e5 15 8.6e5 7.5e5 9.7e5 8.6e5 15 9.7e5 8.7e5 1.1e6 1.0e6 15 1.1e6 9.7e5 1.2e6 1.1e6 15 1.1e6 9.7e5 1.2e6 1.1e6 15 1.1e6 9.7e5 1.2e6 1.1e6 15 1.2e4 2.0e4 2.2e4 2.1e4 15 2.1e4 2.0e4 1.2e4 1.4e4 15 2.1e4 2.0e4 1.3e4 1.4e4 15
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $		$\begin{array}{c c c c c c c c c c c c c c c c c c c $	fil2 in 20-D, N=15, mFE=187012 # ERT 10% 90% RT _{SUCC} 15 2.6e4 2.4e4 2.7e4 2.6e4 15 6.9e4 5.6e4 8.1e4 6.9e4 15 7.9e4 6.7e4 9.1e4 7.9e4 15 8.6e4 7.4e4 1.0e5 8.6e4 15 9.0e4 7.7e4 1.0e5 9.0e4 15 9.3e4 8.0e4 1.1e5 9.3e4 fil4 in 20-D, N=15, mFE=2.53e6 # ERT 10% 90% RT _{SUCC} 15 2.1e5 1.8e5 2.4e5 2.1e5 15 1.4e6 1.3e6 1.6e6 1.4e6 15 1.6e6 1.4e6 1.8e6 1.6e6 15 1.6e6 1.4e6 1.8e6 1.6e6 15 1.7e6 1.4e6 1.8e6 1.6e6 15 1.7e6 1.4e6 1.8e5 7.1e5 15 8.6e5 7.5e5 8.3e5 7.1e5 15 8.6e5 7.5e5 8.7e5 8.6e5 15 1.1e6 9.7e5 1.2e6 1.1e6 15 1.2e4 2.0e4 2.2e4 2.1e4 15 2.8e4 2.7e4 2.9e4 2.8e4 15 4.0e4 3.9e4 4.1e4 4.0e4 15 4.7e4 4.6e4 4.8e4 4.7e4 15 5.2e4 5.1e4 5.3e4 5.2e4 15 4.6e4 2.7e4 2.9e5 2.8e5 15 3.6e4 2.7e4 2.9e5 2.8e5 15 3.6e4 2.7e4 4.5e4 3.6e4 15 4.7e4 4.6e4 4.8e4 4.7e4 15 4.7e4 4.6e4 4.8e4 4.7e4 15 4.7e4 4.6e4 4.8e4 4.7e4 15 4.7e4 4.6e4 4.8e4 4.7e4 15 4.8e5 1.5e5 2.1e5 1.8e5 15 3.6e4 2.7e4 2.9e5 2.8e5 15 3.6e4 2.7e4 2.9e5 2.8e5 15 2.8e5 2.5e5 3.2e5 2.8e5 15 2.8e5 2.5e5 3.2e5 2.8e5 15 2.8e5 2.5e5 3.2e5 2.8e5 15 5.6.7e6 6.0e6 7.4e6 6.7e6 13 1.8e7 1.6e7 2.1e7 1.6e7

Table 3: Shown are, for functions $f_{101}-f_{120}$ and for a given target difference to the optimal function value Δf : the number of successful trials (#); the expected running time to surpass $f_{opt} + \Delta f$ (ERT, see Figure 1); the 10%-tile and 90%-tile of the bootstrap distribution of ERT; the average number of function evaluations in successful trials or, if none was successful, as last entry the median number of function evaluations to reach the best function value (\mathbf{RT}_{succ}). If $f_{opt} + \Delta f$ was never reached, figures in *italics* denote the best achieved Δf -value of the median trial and the 10% and 90%-tile trial. Furthermore, N denotes the number of trials, and mFE denotes the maximum of number of function evaluations executed in one trial. See Figure 1 for the names of functions.



Figure 2: Empirical cumulative distribution functions (ECDFs), plotting the fraction of trials versus running time (left subplots) or versus Δf (right subplots). The thick red line represents the best achieved results. Left subplots: ECDF of the running time (number of function evaluations), divided by search space dimension D, to fall below $f_{opt} + \Delta f$ with $\Delta f = 10^k$, where k is the first value in the legend. Right subplots: ECDF of the best achieved Δf divided by 10^k (upper left lines in continuation of the left subplot), and best achieved Δf divided by 10^{-8} for running times of D, 10 D, 100 D... function evaluations (from right to left cycling black-cyan-magenta). Top row: all results from all functions; second row: moderate noise functions; third row: severe noise functions; fourth row: severe noise and highly-multimodal functions. The legends indicate the number of functions that were solved in at least one trial. FEvals denotes number of function evaluations, D and DIM denote search space dimension, and Δf and Df denote the difference to the optimal function value.

	f121 in 5-D, N=15, mFE=17658	f_{121} in 20-D, N=15, mFE=164174	f122 in 5-D, N=15, mFE=226165	f_{122} in 20-D, N=15, mFE=1.55e7
Δf	# ERT 10% 90% RT _{succ}	# ERT 10% 90% RT _{succ}	Δf # ERT 10% 90% RT _{succ}	# ERT 10% 90% RT _{succ}
10	15 2.3e1 1.6e1 3.0e1 2.3e1	15 2.9e2 2.6e2 3.2e2 2.9e2	10 15 2.2e1 1.2e1 3.3e1 2.2e1	15 1.2e3 4.7e2 2.0e3 1.2e3
1	$15 \ 1.2 e2 \ 1.1 e2 \ 1.4 e2 \ 1.2 e2$	15 8.1e2 7.7e2 8.4e2 8.1e2	1 15 1.7e3 1.3e3 2.2e3 1.7e3	15 5.2e4 4.5e4 5.9e4 5.2e4
$1\mathrm{e}-1$	15 2.7e2 2.5e2 2.9e2 2.7e2	15 1.7e3 1.6e3 1.8e3 1.7e3	1e-1 15 9.2e3 7.1e3 1.1e4 9.2e3	15 1.4e5 1.2e5 1.6e5 1.4e5
1e-3	15 1.8e3 1.6e3 2.0e3 1.8e3	15 1.1e4 1.0e4 1.1e4 1.1e4	1e-3 15 3.0e4 2.6e4 3.4e4 3.0e4	15 7.9e5 6.5e5 9.5e5 7.9e5
$1\mathrm{e}-5$	15 7.6e3 7.3e3 7.9e3 7.6e3	15 4.6e4 4.5e4 4.7e4 4.6e4	1e-5 15 5.4e4 4.6e4 6.1e4 5.4e4	15 2.0e6 1.8e6 2.2e6 2.0e6
$1\mathrm{e}-8$	$15 \ 1.7 e4 \ 1.6 e4 \ 1.7 e4 \ 1.7 e4$	15 1.5e5 1.4e5 1.5e5 1.5e5	1e-8 15 1.2e5 1.0e5 1.3e5 1.2e5	15 7.5e6 6.2e6 8.9e6 7.5e6
	f123 in 5-D, N=15, mFE=5.43e6	f123 in 20-D, N=15, mFE=2.56e7	f124 in 5-D, N=15, mFE=403943	f124 in 20-D, N=15, mFE=1.12e6
Δf	# ERT 10% 90% RT _{succ}	# ERT 10% 90% RT _{succ}	$\Delta f \# \text{ ERT } 10\% 90\% \text{ RT}_{succ}$	# ERT 10% 90% RT _{succ}
10	15 9.1e1 3.5e1 1.6e2 9.1e1	15 6.1e3 4.8e3 7.3e3 6.1e3	10 15 1.5e1 1.1e1 1.9e1 1.5e1	15 2.0e2 1.8e2 2.3e2 2.0e2
1	15 1.6e4 1.3e4 1.9e4 1.6e4	15 5.3e5 4.2e5 6.4e5 5.3e5	1 15 2.2e2 2.0e2 2.4e2 2.2e2	15 2.0e3 1.7e3 2.3e3 2.0e3
$1\mathrm{e}-1$	15 8.2e4 6.6e4 9.8e4 8.2e4	15 1.5e6 1.2e6 1.8e6 1.5e6	1e-1 15 1.0e3 7.3e2 1.4e3 1.0e3	15 4.1e4 3.2e4 5.0e4 4.1e4
$1\mathrm{e}-3$	15 3.4e5 2.8e5 4.0e5 3.4e5	15 5.3e6 4.6e6 6.0e6 5.3e6	1e-3 15 2.2e4 1.7e4 2.6e4 2.2e4	15 1.3e5 1.1e5 1.5e5 1.3e5
$1\mathrm{e}-5$	15 6.7e5 5.7e5 7.8e5 6.7e5	10 2.7e7 2.3e7 3.4e7 1.9e7	1e-5 15 5.4e4 4.5e4 6.5e4 5.4e4	15 3.9e5 3.1e5 4.7e5 3.9e5
$1\mathrm{e}-8$	15 2.6e6 2.1e6 3.1e6 2.6e6	0 36e-7 61e-9 16e-6 2.0e7	1e-8 15 9.8e4 7.0e4 1.3e5 9.8e4	15 8.7e5 7.8e5 9.6e5 8.7e5
	f125 in 5-D, N=15, mFE=555113	f125 in 20-D, N=15, mFE=3.35e7	f126 in 5-D, N=15, mFE=6.03e6	f126 in 20-D, N=15, mFE=1.24e7
Δf	# ERT 10% 90% RT _{succ}	# ERT 10% 90% RT _{succ}	Δf # ERT 10% 90% RT _{succ}	# ERT 10% 90% RT _{succ}
10	15 1.1e0 1.0e0 1.1e0 1.1e0	15 1.0e0 1.0e0 1.0e0 1.0e0	10 15 1.0e0 1.0e0 1.0e0 1.0e0	15 1.0e0 1.0e0 1.0e0 1.0e0
1	15 1.7e1 1.3e1 2.2e1 1.7e1	15 3.8e2 3.1e2 4.6e2 3.8e2	1 15 1.6e2 4.0e1 2.8e2 1.6e2	15 5.8e3 4.6e3 6.9e3 5.8e3
1e - 1	15 3.4e3 2.6e3 4.4e3 3.4e3	15 9.8e6 8.2e6 1.1e7 9.8e6	1e-1 15 1.3e4 1.0e4 1.6e4 1.3e4	0 30e-2 24e-2 32e-2 5.6e6
				,
$1\mathrm{e}-3$	15 2.4e5 2.0e5 2.8e5 2.4e5	10 2.5e7 1.9e7 3.4e7 1.5e7	1e-3 0 67e-4 13e-4 98e-4 2.8e6	
${}^{1\mathrm{e}}_{-3}_{1\mathrm{e}}_{-5}$	15 2.4e5 2.0e5 2.8e5 2.4e5 15 2.4e5 2.0e5 2.8e5 2.4e5	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	
$_{1e-3}^{1e-3}_{1e-8}$	15 2.4e5 2.0e5 2.8e5 2.4e5 15 2.4e5 2.0e5 2.8e5 2.4e5 15 2.4e5 2.0e5 2.8e5 2.4e5 15 2.5e5 2.1e5 2.9e5 2.5e5	10 2.5e7 1.9e7 3.4e7 1.5e7 4 8.0e7 5.3e7 1.6e8 2.3e7 4 8.1e7 5.2e7 1.7e8 2.3e7	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	
1e-3 1e-5 1e-8	15 2.4e5 2.0e5 2.8e5 2.4e5 15 2.4e5 2.0e5 2.8e5 2.4e5 15 2.4e5 2.0e5 2.8e5 2.4e5 15 2.5e5 2.1e5 2.9e5 2.5e5 f127 in 5-D , N=15, mFE=1.03e6	10 2.5e7 1.9e7 3.4e7 1.5e7 4 8.0e7 5.3e7 1.6e8 2.3e7 4 8.1e7 5.2e7 1.7e8 2.3e7 f127 in 20-D , N=15, mFE=1.60e7	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	f128 in 20-D, N=15, mFE=2.37e7
1e-3 1e-5 1e-8 Δf	15 2.4e5 2.0e5 2.8e5 2.4e5 15 2.4e5 2.0e5 2.8e5 2.4e5 15 2.4e5 2.0e5 2.8e5 2.4e5 15 2.5e5 2.1e5 2.9e5 2.5e5 f127 in 5-D, N=15, mFE=1.03e6 # ERT 10% 90% RTsucc	10 2.5e7 1.9e7 3.4e7 1.5e7 4 8.0e7 5.3e7 1.6e8 2.3e7 4 8.1e7 5.2e7 1.7e8 2.3e7 f127 in 20-D , N=15, mFE=1.60e7 # ERT 10% 90% RTsucc	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	f128 in 20-D, N=15, mFE=2.37e7 # ERT 10% 90% RT _{succ}
$\begin{array}{c} 1e-3\\ 1e-5\\ 1e-8\\ \hline \Delta f\\ 10 \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	f128 in 20-D, N=15, mFE=2.37e7 # ERT 10% 90% RT _{succ} 15 1.4e5 8.7e4 2.0e5 1.4e5
$\begin{array}{c} 1e-3\\ 1e-5\\ 1e-8\\ \hline \Delta f\\ 10\\ 1\end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	f128 in 20-D, N=15, mFE=2.37e7 # ERT 10% 90% RT _{succ} 15 1.4e5 8.7e4 2.0e5 1.4e5 10 1.3e7 8.2e6 2.0e7 8.9e6
1e-3 1e-5 1e-8 Δf 10 1 1e-1	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	f128 in 20-D, N=15, mFE=2.37e7 # ERT 10% 90% RTsucc 15 1.4e5 8.7e4 2.0e5 1.4e5 10 1.3e7 8.2e6 2.0e7 8.9e6 9 1.7e7 1.1e7 2.5e7 1.2e7
1e-3 1e-5 1e-8 Δf 10 1 1e-1 1e-3	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$		$ \begin{array}{c} f_{128} \text{ in } 20\text{-D}, \text{N=15}, \text{mFE=2.37e7} \\ \# \text{ERT} 10\% 90\% \text{RT}_{\text{succ}} \\ 15 1.4e5 8.7e4 2.0e5 1.4e5 \\ 10 1.3e7 8.2e6 2.0e7 8.9e6 \\ 9 1.7e7 1.1e7 2.5e7 1.2e7 \\ 9 1.7e7 1.2e7 2.5e7 1.2e7 \end{array} $
$\begin{array}{c} 1e-3 \\ 1e-5 \\ 1e-8 \\ \hline \Delta f \\ 10 \\ 1 \\ 1e-1 \\ 1e-3 \\ 1e-5 \\ \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c} f_{128} \mbox{ in 20-D}, \ \mbox{N=15}, \ \mbox{mFE=}2.37e7\\ \# \ \mbox{ERT} \ \ \mbox{10\%} \ \ \mbox{MFSucc}\\ 15 \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ $
$\begin{array}{c} 1e-3 \\ 1e-5 \\ 1e-8 \\ \hline \Delta f \\ 10 \\ 1 \\ 1e-1 \\ 1e-3 \\ 1e-5 \\ 1e-8 \\ \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$		$ \begin{array}{c} f_{128} \text{ in } 20\text{-D}, \ \text{N=15}, \ \text{mFE=2.37e7} \\ \# \ \text{ERT} & 10\% & 90\% & \text{RT}_{\text{succ}} \\ 15 \ 1.4e5 & 8.7e4 & 2.0e5 & 1.4e5 \\ 10 \ 1.3e7 & 8.2e6 & 2.0e7 & 8.9e6 \\ 9 \ 1.7e7 & 1.1e7 & 2.5e7 & 1.2e7 \\ 9 \ 1.7e7 & 1.2e7 & 2.5e7 & 1.2e7 \\ 9 \ 1.7e7 & 1.2e7 & 2.6e7 & 1.2e7 \\ 9 \ 1.7e7 & 1.2e7 & 2.6e7 & 1.2e7 \\ \end{array} $
$\begin{array}{c} 1e-3 \\ 1e-5 \\ 1e-8 \end{array}$ $\begin{array}{c} \Delta f \\ 10 \\ 1 \\ 1e-1 \\ 1e-3 \\ 1e-5 \\ 1e-8 \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$		$ \begin{array}{c} f_{128} \mbox{ in } 20\mbox{-}D, \mbox{ N=15}, \mbox{ mFE=2.37e7} \\ \# \ \mbox{ ERT } 10\% \ \ 90\% \ \ \mbox{ RT}_{succ} \\ f_{15} \ \ 1.4e5 \ \ 8.7e4 \ \ 2.0e5 \ \ 1.4e5 \\ 10 \ \ 1.3e7 \ \ 8.2e6 \ \ 2.0e7 \ \ 8.9e6 \\ 9 \ \ 1.7e7 \ \ 1.1e7 \ \ 2.5e7 \ \ 1.2e7 \\ 9 \ \ 1.7e7 \ \ 1.2e7 \ \ 2.5e7 \ \ 1.2e7 \\ 9 \ \ 1.7e7 \ \ 1.2e7 \ \ 2.5e7 \ \ 1.2e7 \\ 9 \ \ 1.7e7 \ \ 1.2e7 \ \ 2.6e7 \ \ 1.2e7 \\ 9 \ \ 1.7e7 \ \ 1.2e7 \ \ 2.6e7 \ \ 1.2e7 \\ 9 \ \ 1.7e7 \ \ 1.2e7 \ \ 2.6e7 \ \ 1.2e7 \\ 9 \ \ 1.7e7 \ \ 1.2e7 \ \ 2.6e7 \ \ 1.2e7 \\ 9 \ \ 1.7e7 \ \ 1.2e7 \ \ 2.6e7 \ \ 1.2e7 \\ 9 \ \ 1.7e7 \ \ 1.2e7 \ \ 2.6e7 \ \ 1.2e7 \\ 9 \ \ 1.7e7 \ \ 1.2e7 \ \ 2.6e7 \ \ 1.2e7 \\ 9 \ \ 1.7e7 \ \ 1.2e7 \ \ 2.6e7 \ \ 1.2e7 \\ \end{array}$
$\begin{array}{c} 1e-3 \\ 1e-5 \\ 1e-8 \end{array}$ $\begin{array}{c} \Delta f \\ 10 \\ 1 \\ 1e-1 \\ 1e-3 \\ 1e-5 \\ 1e-8 \end{array}$ Δf	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c} f_{128} \mbox{ in } 20\mbox{-}D, \ \mbox{N=15}, \ \mbox{mFE=2.37e7} \\ \# \ \ \mbox{ERT} \ \ \ 10\% \ \ \ 90\% \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$
$\begin{array}{c} 1e-3\\ 1e-5\\ 1e-8\\ \hline \Delta f\\ 10\\ 1\\ 1e-1\\ 1e-3\\ 1e-5\\ 1e-8\\ \hline \Delta f\\ 10\\ \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$		$ \begin{array}{c} f_{128} \text{ in 20-D}, \ N=15, \ \mathrm{mFE}=2.37\mathrm{e7} \\ \# \ \mathrm{ERT} & 10\% & 90\% & \mathrm{RT}_{\mathrm{succ}} \\ 15 & 1.4\mathrm{e5} & 8.7\mathrm{e4} & 2.0\mathrm{e5} & 1.4\mathrm{e5} \\ 10 & 1.3\mathrm{e7} & 8.2\mathrm{e6} & 2.0\mathrm{e7} & 8.9\mathrm{e6} \\ 9 & 1.7\mathrm{e7} & 1.1\mathrm{e7} & 2.5\mathrm{e7} & 1.2\mathrm{e7} \\ 9 & 1.7\mathrm{e7} & 1.1\mathrm{e7} & 2.5\mathrm{e7} & 1.2\mathrm{e7} \\ 9 & 1.7\mathrm{e7} & 1.2\mathrm{e7} & 2.5\mathrm{e7} & 1.2\mathrm{e7} \\ 9 & 1.7\mathrm{e7} & 1.2\mathrm{e7} & 2.6\mathrm{e7} & 1.2\mathrm{e7} \\ 9 & 1.7\mathrm{e7} & 1.2\mathrm{e7} & 2.6\mathrm{e7} & 1.2\mathrm{e7} \\ 1.2\mathrm{e7} & 1.2\mathrm{e7} & 2.6\mathrm{e7} & 1.2\mathrm{e7} \\ f_{130} \text{ in 20-D}, \ N=15, \ \mathrm{mFE}=1.62\mathrm{e7} \\ \# \ \mathrm{ERT} & 10\% & 90\% \ \mathrm{RT}_{\mathrm{succ}} \\ 15 & 9.1\mathrm{e3} & 4.2\mathrm{e3} & 1.4\mathrm{e4} & 9.1\mathrm{e3} \\ \end{array} $
$\begin{array}{c} 1e-3\\ 1e-5\\ 1e-8\\ \end{array}\\ \begin{array}{c} \Delta f\\ 10\\ 1\\ 1e-1\\ 1e-3\\ 1e-5\\ 1e-8\\ \end{array}\\ \begin{array}{c} \Delta f\\ 10\\ 1\\ \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$		$ \begin{array}{c} f_{128} & 120\text{-D}, \ N=15, \ mFE=2.37e7 \\ \# \ ERT & 10\% & 90\% \ RT_{succ} \\ 15 & 1.4e5 & 8.7e4 & 2.0e5 & 1.4e5 \\ 10 & 1.3e7 & 8.2e6 & 2.0e7 & 1.4e5 \\ 10 & 1.3e7 & 8.2e6 & 2.0e7 & 1.2e7 \\ 9 & 1.7e7 & 1.1e7 & 2.5e7 & 1.2e7 \\ 9 & 1.7e7 & 1.2e7 & 2.5e7 & 1.2e7 \\ 9 & 1.7e7 & 1.2e7 & 2.6e7 & 1.2e7 \\ 1.3e1 & 10\text{-D}, \ N=15, \ mFE=1.62e7 \\ \# \ ERT & 10\% & 90\% \ RT_{succ} \\ 15 & 3.1e6 & 1.5e6 & 5.1e6 & 3.1e6 \\ \end{array} $
$\begin{array}{c} 1e-3\\ 1e-5\\ 1e-8\\ \end{array}\\ \begin{array}{c} \Delta f\\ 10\\ 1\\ 1e-1\\ 1e-3\\ 1e-5\\ 1e-8\\ \end{array}\\ \begin{array}{c} \Delta f\\ 10\\ 1\\ 1e-1\\ \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$		$\begin{array}{c} f_{128} \ \mbox{in} 20\mbox{-}D, \ \mbox{N=15}, \ \mbox{mFE=}2.37\mbox{e7}\\ \# \ \ \mbox{Err} \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ $
$\begin{array}{c} 1\mathrm{e}\!-\!3\\ 1\mathrm{e}\!-\!5\\ 1\mathrm{e}\!-\!5\\ 1\mathrm{e}\!-\!8\\ \hline \Delta f\\ 10\\ 1\\ 1\mathrm{e}\!-\!3\\ 1\mathrm{e}\!-\!5\\ 1\mathrm{e}\!-\!8\\ \hline \Delta f\\ 1\\ 1\\ 1\mathrm{e}\!-\!1\\ 1\mathrm{e}\!-\!3\end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	$\begin{array}{c} f_{128} \text{ in } 20\text{-D}, \text{N=15}, \text{mFE=2.37e7} \\ \# \text{ERT} & 10\% & 90\% & \text{RT}_{succ} \\ 15 & 1.4e5 & 8.7e4 & 2.0e5 & 1.4e5 \\ 10 & 1.3e7 & 8.2e6 & 2.0e7 & 8.9e6 \\ 9 & 1.7e7 & 1.1e7 & 2.5e7 & 1.2e7 \\ 9 & 1.7e7 & 1.2e7 & 2.5e7 & 1.2e7 \\ 9 & 1.7e7 & 1.2e7 & 2.6e7 & 1.2e7 \\ 9 & 1.7e7 & 1.2e7 & 2.6e7 & 1.2e7 \\ f_{130} \text{ in } 20\text{-D}, \text{N=15}, \text{mFE=1.62e7} \\ \# \text{ERT} & 10\% & 90\% & \text{RT}_{succ} \\ \# \text{ERT} & 10\% & 90\% & \text{RT}_{succ} \\ 15 & 9.1e3 & 4.2e3 & 1.4e4 & 9.1e3 \\ 15 & 3.1e6 & 1.8e6 & 5.3e6 & 3.6e6 \\ 15 & 3.6e6 & 1.8e6 & 5.3e6 & 3.6e6 \\ 15 & 3.6e6 & 1.9e6 & 5.3e6 & 3.6e6 \\ \end{array}$
$\begin{array}{c} 1\mathrm{e}\!-\!3\\ 1\mathrm{e}\!-\!5\\ 1\mathrm{e}\!-\!5\\ 1\mathrm{e}\!-\!8\\ \hline \Delta f\\ 10\\ 1\\ 1\mathrm{e}\!-\!3\\ 1\mathrm{e}\!-\!5\\ 1\mathrm{e}\!-\!8\\ \hline \Delta f\\ 10\\ 1\\ 1\mathrm{e}\!-\!1\\ 1\mathrm{e}\!-\!3\\ 1\mathrm{e}\!-\!5\\ 1\mathrm{e}\!-\!5\\ \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$		$\begin{array}{l} f_{128} \mbox{ in } 20\mbox{-}D, \ \mbox{N=15}, \ \mbox{mFE=}2.37\mbox{e7}\\ f_{\rm E} \mbox{Err} & 10\% & 90\% \mbox{RT}_{\rm succ}\\ 15 & 1.4\mbox{e5} & 8.7\mbox{e4} & 2.0\mbox{e5} & 1.4\mbox{e5}\\ 10 & 1.3\mbox{e7} & 8.2\mbox{e6} & 2.0\mbox{e7} & 1.4\mbox{e5}\\ 10 & 1.3\mbox{e7} & 1.2\mbox{e7} & 2.5\mbox{e7} & 1.2\mbox{e7}\\ 9 & 1.7\mbox{e7} & 1.2\mbox{e7} & 2.5\mbox{e7} & 1.2\mbox{e7}\\ 9 & 1.7\mbox{e7} & 1.2\mbox{e7} & 2.5\mbox{e7} & 1.2\mbox{e7}\\ 9 & 1.7\mbox{e7} & 1.2\mbox{e7} & 2.5\mbox{e7} & 1.2\mbox{e7}\\ 9 & 1.7\mbox{e7} & 1.2\mbox{e7} & 2.5\mbox{e7} & 1.2\mbox{e7}\\ 9 & 1.7\mbox{e7} & 1.2\mbox{e7} & 2.5\mbox{e7} & 1.2\mbox{e7}\\ 9 & 1.7\mbox{e7} & 1.2\mbox{e7} & 2.5\mbox{e7} & 1.2\mbox{e7}\\ 9 & 1.7\mbox{e7} & 1.2\mbox{e7} & 2.5\mbox{e7} & 1.2\mbox{e7}\\ 9 & 1.7\mbox{e7} & 1.2\mbox{e7} & 2.5\mbox{e7} & 1.2\mbox{e7}\\ 9 & 1.7\mbox{e7} & 1.2\mbox{e7} & 2.5\mbox{e7} & 1.2\mbox{e7}\\ 9 & 1.7\mbox{e7} & 1.2\mbox{e7} & 2.5\mbox{e7} & 1.2\mbox{e7}\\ 9 & 1.7\mbox{e7} & 1.2\mbox{e7} & 2.5\mbox{e7} & 1.2\mbox{e7}\\ 9 & 1.7\mbox{e7} & 1.2\mbox{e7} & 2.5\mbox{e7} & 1.2\mbox{e7}\\ 15 & 3.1\mbox{e6} & 1.5\mbox{e6} & 5.4\mbox{e6} & 3.6\mbox{e6}\\ 15 & 3.6\mbox{e6} & 5.4\mbox{e6} & 5.4\mbox{e6} & 3.6\mbox{e6}\\ 15 & 3.6\mbox{e6} & 1.2\mbox{e6} & 5.4\mbox{e6} & 3.6\mbox{e6}\\ 15 & 3.6\mbox{e6} & 1.2\mbox{e6} & 5.4\mbox{e6} & 3.6\mbox{e6}\\ 15 & 3.6\mbox{e6} & 1.2\mbox{e6} & 5.4\mbox{e6} & 3.6\mbox{e6}\\ 15 & 3.6\mbox{e6} & 1.2\mbox{e6} & 5.4\mbox{e6} & 3.6\mbox{e6}\\ 15 & 3.6\mbox{e6} & 1.2\mbox{e6} & 5.4\mbox{e6} & 3.6\mbox{e6}\\ 15 & 3.6\mbox{e6} & 1.2\mbox{e6} & 5.4\mbox{e6} & 3.6\mbox{e6}\\ 15 & 3.6\mbox{e6} & 1.2\mbox{e7} & 1.2\mbox{e7}\\ 10 & 1.2\mbox{e7} & 1.2\mb$
$\begin{array}{c} 1\mathrm{e}-3\\ 1\mathrm{e}-5\\ 1\mathrm{e}-8\\ \end{array}\\ \underline{\Delta f}\\ 10\\ 1\\ 1\mathrm{e}-3\\ 1\mathrm{e}-5\\ 1\mathrm{e}-8\\ \end{array}\\ \underline{\Delta f}\\ 10\\ 1\\ 1\mathrm{e}-1\\ 1\mathrm{e}-3\\ 1\mathrm{e}-5\\ 1\mathrm{e}-8\\ \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$		$\begin{array}{c} f_{128} \text{ in } 20\text{-D}, \ N=15, \ \mathrm{mFE}=2.37\mathrm{e7} \\ \# \ \mathrm{ERT} & 10\% & 90\% \ \mathrm{RT}_{\mathrm{succ}} \\ 15 & 1.4\mathrm{e5} & 8.7\mathrm{e4} & 2.0\mathrm{e5} & 1.4\mathrm{e5} \\ 10 & 1.3\mathrm{e7} & 8.2\mathrm{e6} & 2.0\mathrm{e7} & 8.9\mathrm{e6} \\ 9 & 1.7\mathrm{e7} & 1.1\mathrm{e7} & 2.5\mathrm{e7} & 1.2\mathrm{e7} \\ 9 & 1.7\mathrm{e7} & 1.2\mathrm{e7} & 2.5\mathrm{e7} & 1.2\mathrm{e7} \\ 9 & 1.7\mathrm{e7} & 1.2\mathrm{e7} & 2.5\mathrm{e7} & 1.2\mathrm{e7} \\ 9 & 1.7\mathrm{e7} & 1.2\mathrm{e7} & 2.5\mathrm{e7} & 1.2\mathrm{e7} \\ 9 & 1.7\mathrm{e7} & 1.2\mathrm{e7} & 2.5\mathrm{e7} & 1.2\mathrm{e7} \\ 130 & \mathrm{in} & 20\text{-D}, \ \mathrm{N=15}, \ \mathrm{mFE}=1.62\mathrm{e7} \\ \# \ \mathrm{ERT} & 10\% & 90\% \ \mathrm{RT}_{\mathrm{succ}} \\ 15 & 3.1\mathrm{e6} & 1.3\mathrm{e6} & 3.1\mathrm{e6} \\ 15 & 3.6\mathrm{e6} & 1.8\mathrm{e6} & 5.3\mathrm{e6} & 3.6\mathrm{e6} \\ 15 & 3.6\mathrm{e6} & 1.8\mathrm{e6} & 5.3\mathrm{e6} & 3.6\mathrm{e6} \\ 15 & 3.6\mathrm{e6} & 1.9\mathrm{e6} & 5.4\mathrm{e6} & 3.6\mathrm{e6} \\ 15 & 3.6\mathrm{e6} & 1.9\mathrm{e6} & 5.4\mathrm{e6} & 3.6\mathrm{e6} \\ 15 & 3.6\mathrm{e6} & 1.9\mathrm{e6} & 5.4\mathrm{e6} & 3.6\mathrm{e6} \\ 15 & 3.6\mathrm{e6} & 1.9\mathrm{e6} & 5.4\mathrm{e6} & 3.6\mathrm{e6} \\ \end{array}$

Table 4: Shown are, for functions f_{121} - f_{130} and for a given target difference to the optimal function value Δf : the number of successful trials (#); the expected running time to surpass $f_{opt} + \Delta f$ (ERT, see Figure 1); the 10%-tile and 90%-tile of the bootstrap distribution of ERT; the average number of function evaluations in successful trials or, if none was successful, as last entry the median number of function evaluations to reach the best function value (\mathbf{RT}_{succ}). If $f_{opt} + \Delta f$ was never reached, figures in *italics* denote the best achieved Δf -value of the median trial and the 10% and 90%-tile trial. Furthermore, N denotes the number of trials, and mFE denotes the maximum of number of function evaluations executed in one trial. See Figure 1 for the names of functions.