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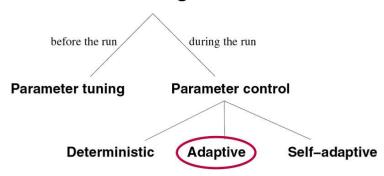
Learning and Intelligent Optimization Conference - LION 3
January 15th, 2009



Conclusions

Parameter Setting in EAs

Parameter Setting in EAs



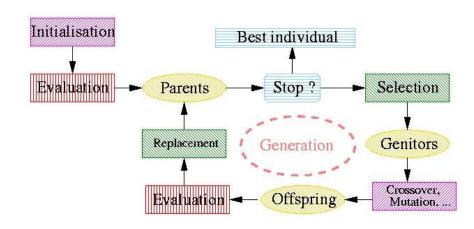
(from [Eiben et al., 2007])



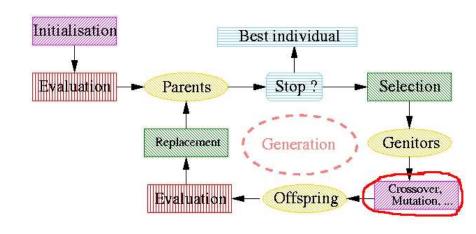
Evolutionary Algorithms

AOS

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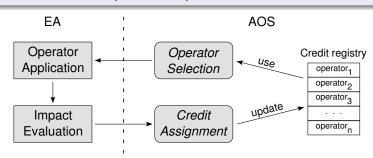
Evolutionary Algorithms



Adaptive Operator Selection

Objective

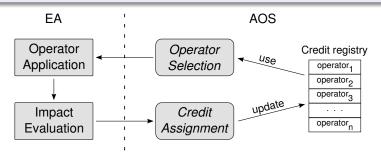
Autonomously select the operator to be applied amongst available ones, based on its impact in the past.



Adaptive Operator Selection

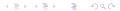
Objective

Autonomously select the operator to be applied amongst available ones, based on its impact in the past.



This work:

- Operator selection: Dynamic Multi-Armed Bandits
- Credit Assignment: Extreme Value Based



AOS: A (kind of) Multi-Armed Bandit problem

Multi-Armed Bandits



At time t, gambler plays arm j

reward at
$$t$$
: $r_t = \left\{ egin{array}{ll} 1 & ext{with prob} &= p_j \\ 0 & ext{with prob} &= 1 - p_j \end{array} \right.$

Goal: maximize cumulated reward

AOS: A (kind of) Multi-Armed Bandit problem

Multi-Armed Bandits



At time t, gambler plays arm j

reward at
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: $r_t = \begin{cases} 1 & \text{with prob } = p_j \\ 0 & \text{with prob } = 1 - p_j \end{cases}$

Goal: maximize cumulated reward

State-of-the-art: UCB1 [Auer et al., 2002]

• At time t, choose arm j maximizing:

$$\hat{r}_{j,t} + \sqrt{\frac{2\log\sum_k n_{k,t}}{n_{j,t}}}$$
, where $\begin{cases} \hat{r}_{j,t} & \text{,estimated reward for arm } j \\ n_{j,t} & \text{,chosen times for arm } j \end{cases}$



AOS with Multi-Armed Bandits: the true story I

Scaling

AOS

MAB framework:

• $\hat{r}_{i,t} \in [0,1]$;

AOS framework:

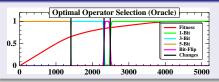
• $\hat{r}_{i,t} \in [a,b]$ (e.g. fitness improvement)

UCB1's EvE balance is broken, **Scaling** is needed:

$$\hat{q}_{i,t} = \mathcal{C} * \hat{r}_{j,t} + \sqrt{\frac{2 \log \sum_k n_{k,t}}{n_{j,t}}}$$

AOS with Multi-Armed Bandits: the true story II

AOS is a dynamic context

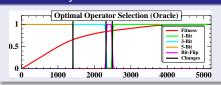


UCB1: too long to recover.

- Detect change;
- Restart the MAB.

AOS with Multi-Armed Bandits: the true story II

AOS is a dynamic context



UCB1: too long to recover.

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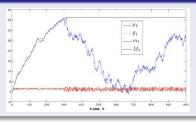
How to detect a change in a distribution?

[Page-Hinkley test, 1954]

$$m_t = \sum_{i=1}^t (r_i - \bar{r}_i + \delta),$$

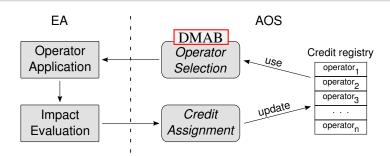
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$$M_t = \max\{|m_i|, i = 1...t\}$$

• Return
$$(M_t - |m_t| > \lambda)$$



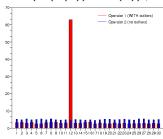
DMAB: UCB1 + Scaling + Page-Hinkley

- Proposed by other members of our group [Hartland, 2007]
- Won the Pascal Network challenge on "On-line Trading of Exploration and Exploitation" (OTEE)



Credit Assignment: Extreme Value-Based (EVB)

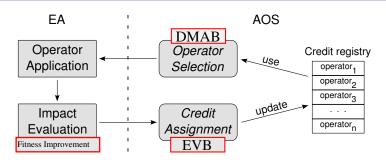
• Fitness improvement: $(\mathcal{F}(o(x)) - \mathcal{F}(x))_+$



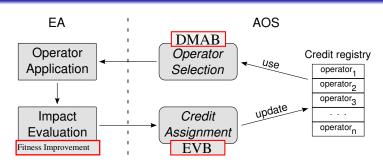
- Outlier operators are rarely considered smaller expectation.
- EC: Focus on extreme, rather than average events
 - Complex systems, e.g. epidemic propagation, financial markets
- Extreme Value-Based (EVB) Credit Assignment.
 - $\mathcal{R} = \underline{\mathsf{Extreme}}$ value over a $\underline{\mathsf{Window}}$



Ex-DMAB Adaptive Operator Selection



Ex-DMAB Adaptive Operator Selection



Meta-Parameters

AOS

- Operator selection (DMAB):
 - \bullet C, for scaling;
 - λ and δ , for the PH test ($\delta \equiv 0.15$)
- Credit assignment (EVB):
 - \bullet \mathcal{W} , the size of the sliding window



Experimental Conditions

AOS

- (1+50)-EA applied to: One-Max; Long k-Path
- Mutation Operators:
 - 1-bit, 3-bit, 5-bit
 - 1/n bit-flip (and also k/n bit-flip for the 2nd problem)
- Initial individual is set to (0, ..., 0)
- Meta-parameters tuned off-line
 - One-Max: complete DOE campaign
 - Long k-Path: F-RACE [Birattari et al., 2002], a Racing technique using the Friedman's 2-way ANOVA by ranks

Extreme-DMAB versus

- Probability Matching and Adaptive Pursuit [Thierens, 2007]
- Average-DMAB *
- Naive (uniform) and Optimal operator selection *

References

The One-Max Problem

• 10⁴ bits

AOS

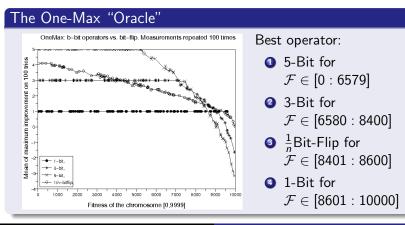
- Fitness is the number of "1"s in the bitstring
- Very simple unimodal problem, the "drosophila of EC"

The One-Max Problem

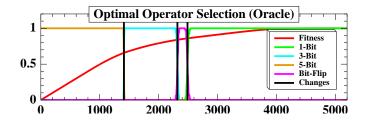
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Results Extreme - DMAB on the One-Max



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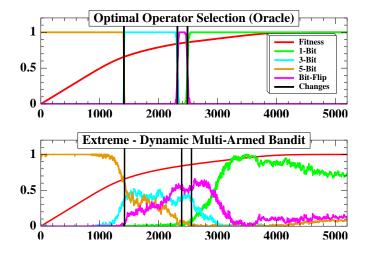


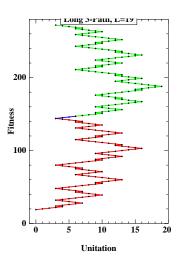
Figure: Extreme - DMAB behavior averaged over 50 runs.

AOS	Conf.	Gens. to Optimum
Extreme - DMAB	$C = 1, \gamma = 250$	5467 \pm 513
Average - DMAB	$C = 10, \gamma = 25$	7727 ± 642
Optimal Strategy	Given by "Oracle"	5069 ± 292
Best Naive	$\mathcal{U}(1\text{-Bit}+5\text{-Bit})$	6793 ± 625
Complete Naive	<i>U</i> (4 ops.)	7813 ± 708

Table: Results on the 10k bits One-Max problem (over 50 runs).

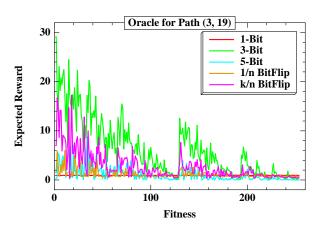
Long k-Path Problems

- Unimodal, very long path to the optimum
 - Path length grows exponentially with size of the bitstring (n)
 - Hamming distance between two consecutive points is 1
 - Any other point at distance 1 is off the path
- "Shortcuts" require at least k bit-flips

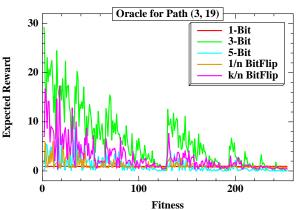




The Long K-Path Oracle



The Long K-Path Oracle



N	Length	
43	\sim 65 K	
49	\sim 262 K	
55	$\sim 1~{\sf M}$	
61	\sim 4 M	

	DMAB - $\mathcal{W}(\mathcal{C},\lambda)$			
N	Extreme	Average	Optimal	Uniform
	500 (100; 100)	50 (50; .5)		
43	2910/1771	= 3039/2234	> 2134/2414	= 3462/2174
49	4407/2698	< 5950/3694	= 3590/3327	= 5201/3461
55	6257/4535	< 8366/5991	=4858/5669	< 9778/5245
61	14586/9345	= 16222/8608	> 8608/9907	= 12243/10043

Table: Average/Std. Deviation number of generations to optimum out of 50 runs, using the optimal AOS parameters found by F-Race over ALL instances. Comparison validated by applying both unsigned Wilcoxon rank sum and Kolmogorov-Smirnov non-parametric tests.



Comparative Results on the Long K-Path Problem II

N	DMAB - $\mathcal{W}(\mathcal{C},\lambda)$		Optimal	Uniform
	Extreme	Average	Орина	Offition
43	2457/1945	= 2815/1908	= 2134/2414	< 3462/2174
	500(50; 50)	50(.5; 100)		
49	3670/2485	< 5759/3696	= 3590/3327	< 5201/3461
	500(100; 500)	50(.1; 1000)		
55	6257/4535	< 8303/5945	= 4858/5669	< 9778/5245
	500(100; 100)	50(50; .1)		
61	12380/9733	= 14521/8945	= 8608/9907	= 12243/10041
	500(50; 25)	50(.5; 50)		

Table: Average/Std. Deviation number of generations to optimum out of 50 runs, using the optimal AOS parameters found by F-Race over EACH instance. Comparison validated by applying both unsigned Wilcoxon rank sum and Kolmogorov-Smirnov non-parametric tests.

Conclusions and Perspectives

Efficiency

AOS

- Demonstrated on 2 benchmark problems.
- Still expensive. Real problems no optimal behavior.
- Better than fixed, naive and known adaptive approaches.



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Deepen our understanding on meta-parameters

- High sensitivity.
 - DMAB's $\mathcal C$ and λ affect the EvE balance.
- Self-Adaptation? Off-line? Learning?

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- Demonstrated on 2 benchmark problems.
- Still expensive. Real problems no optimal behavior.
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Deepen our understanding on meta-parameters

- High sensitivity.
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- Self-Adaptation? Off-line? Learning?

Generalization

- Rank-based rewarding (aware of fitness variance)
- Consider different measures (e.g. diversity)
 - Current work on SAT problems (Université d'Angers)

References I

AOS



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- Da Costa, L., Fialho, A., Schoenauer, M., and Sebag, M. (2008). Adaptive operator selection with dynamic multi-armed bandits. In *Proc. GECCO'08*.
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References II

AOS









Dynamic Multi-Armed Bandits and Extreme Value Rewards for Adaptive Operator Selection in Evolutionary Algorithms

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