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MERGING SENSOR DATA FROM MULTIPLE TEMPERATURE SCENARIOS FOR VIBRATION MONITORING OF CIVIL STRUCTURES

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Merging sensor data from multiple temperature scenarios for vibration monitoring of civil structures

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 $\mathbf{F}_{\mathbf{r}}$ based structural health monitoring SHM approaches for civil engineering struc tures. This paper addresses the issue of discriminating changes in modal parameters due to damages and changes in modal parameters due to temperature effects. A non parametric damage detection algorithm is proposed which only assumes that several datasets are recorded on the safe structure at different and unknown temperatures. and smoothes out the temperature effect using an averaging operation.

Kev-words: Subspace identification, damage detection, sensor data fusion, keywords-beneficient products and the second control of the second c vibration-based monitoring, civil engineering structures, temperature effect.

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Fusion de donn-ees provenant de scenarii de temp-erature multiples pour la surveillance vibratoire de structures de g-enie civil

Resume - Leet de la temperature ambiante limite lecacite des methodes de surveillance d'intégrité de structures basées sur leurs vibrations. Cet article étudie la discrimination entre changements de param-etres modaux dus aux endommage ments et changements de param-etres modaux dus aux eets de temperature Un algorithme non-paramétrique de détection d'endommagement est proposé, qui suppose seulement que l'on dispose d'enregistrements des vibrations de la structure saine sous différentes températures inconnues, et utilise une opération de moyennisation pour éliminer l'effet de la température.

Mots cles - Identication par sous
espaces detection dendommagement fusion de données délivrées par des capteurs, surveillance vibratoire, structures de génie civil, effet de la température.

Introduction

As argued in $[1, 2, 3]$ and references therein, automatic global vibration-based monitoring techniques have been recognized as useful alternatives to visual inspections or local non destructive evaluations performed manually. It is also widely recognized that the ambient temperature effect on civil engineering structures may result in limitations of such SHM approaches Actually the dynamics of those structures is affected by the ambient temperature and other environmental effects $[4, 5, 6]$. Hence both temperature variations and damages affect the modal parameters (modal frequencies, and associated damping values and mode-shapes) which characterize the dynamics of the structure. This raises the issue of discriminating between changes in modal parameters due to damages and changes in modal parameters due to tem perature effects.

A parametric damage detection algorithm based on a residual associated with a $\rm covarianter\, or\, linearly defined in terms of a linearly independent.$ on that residual has been proposed in This subspace
based residual uses the left null space of a particular matrix capturing the nominal (safe) state of the structure The purpose of this paper is to propose an extension of a non parametric version of this damage detection algorithm, to cope with the temperature effect. This new algorithm only assumes that several datasets are recorded on the safe structure at different and unknown temperatures. The temperature effect is smoothed out using a particular averaging operation

The paper is organized as follows. In section 2, the subspace-based damaged detection algorithm is summarized, under both its parametric and non parametric versions. In section 3, the issue of merging multiple measurements setups is addressed, of which the joint handling of measurements recorded at different temperatures is a particular case A new detection algorithm is proposed which extends the non parametric version. The results obtaining when applying both the original and the new detection algorithms on two application examples are reported in section 4. The examples are a simulated bridge deck and a laboratory test-case composed of a clamped beam within a climatic chamber Finally some conclusions are drawn in section

2 Subspace-based detection

The subspace-based detection algorithm proposed and investigated in [7, 8, 9] handles a residual which exploits the left null space of appropriate matrices This is briefly recalled now.

The use of state
space representations for vibration
based structural monitoring is well known $[11, 12]$: structural monitoring boils down to monitoring the eigenstructure of the state transition matrix F of a linear dynamic system:

$$
\begin{cases}\nX_{k+1} = F X_k + V_{k+1} \\
Y_k = H X_k\n\end{cases} \n\tag{1}
$$

 max_{i} and pairs (i, j, j, λ) dened by:

$$
\det(F - \lambda I) = 0, \ (F - \lambda I) \ \varphi_{\lambda} = 0, \ \Phi_{\lambda} \stackrel{\text{def}}{=} H \ \varphi_{\lambda} \tag{2}
$$

Let

$$
\theta \stackrel{\text{def}}{=} \left(\begin{array}{c} \Lambda \\ \text{vec}\Phi \end{array} \right) \tag{3}
$$

be the modal parameter where is the vector whose elements are the -s is the matrix whose columns are the - λ -, the columns the columns column stating operators.

The considered residual, which is associated with a covariance-driven outputonly subspace identification algorithm, exploits the following basic although simple factorization property. Let $R_i \stackrel{\text{def}}{=} (\mathbf{E} Y_k Y_{k-i}^T)$, where **E** is the expectation operator, be the output covariance matrix. Let also

$$
\mathcal{H}_{p+1,q} \stackrel{\text{def}}{=} \begin{pmatrix} R_0 & R_1 & \vdots & R_{q-1} \\ R_1 & R_2 & \vdots & R_q \\ \vdots & \vdots & \vdots & \vdots \\ R_p & R_{p+1} & \vdots & R_{p+q-1} \end{pmatrix} \stackrel{\text{def}}{=} \text{Hank}(R_i) \tag{4}
$$

be the theoretical Hankel matrix. Let also $G \stackrel{{\mathrm {def}}}{=} \left({\mathbf E} \; X_k \; Y_k^T \right)$ be the cross-covariance between the state and the observed outputs. Direct computations of the R_i 's from the Equations in (1) lead to

$$
R_i = H \ F^i \ G \tag{5}
$$

and consequently to the well known factorization

$$
\mathcal{H}_{p+1,q} = \mathcal{O}_{p+1}(H,F) \mathcal{C}_q(F,G) \tag{6}
$$

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where
$$
\mathcal{O}_p(H, F) \stackrel{\text{def}}{=} \begin{pmatrix} H \\ HF \\ \vdots \\ HF^{p-1} \end{pmatrix}
$$
 and $\mathcal{C}_q(F, G) \stackrel{\text{def}}{=} (G \ F G \ \cdots \ F^{q-1} G)$ are the observ-

ability and controllability matrices, respectively.

From Equation (2), we know that the knowledge of the pair (H, F) is sufficient for recovering the modal parameters. Now it results from Equation (6) that the left $f_{\rm acc, 1.4}$ and $f_{\rm acc, 1.0}$ matrix $f_{\rm eff, 0.00}$ are $f_{\rm eff, 0.000}$ and $f_{\rm eff, 0.000}$ and $f_{\rm acc, 0.000}$ by the excitation. Thus the modal parameter θ can be recovered from matrix \mathcal{O}_p only

Parametric test

The modal parameter vector θ can be characterized as follows. Assume that the eigenvectors of F are chosen as the basis for the state space of the system in Equation $\mathbf{v} = \mathbf{v}$ and basis matrix operations of \mathbf{v} is the contract of \mathbf{v}

$$
\mathcal{O}_{p+1}(\theta) = \begin{pmatrix} \Phi \\ \Phi \Delta \\ \vdots \\ \Phi \Delta^p \end{pmatrix} \tag{7}
$$

where diagonal matrix $\Delta = \text{diag}(\Lambda)$, and Λ and Φ are as in Equation (3) above. From Equation (6) it results that whether a nominal modal parameter θ_0 is in agreement with a given output covariance sequence $(R_j)_j$ is characterized by:

$$
\mathcal{O}_{p+1}(\theta_0) \text{ and } \mathcal{H}_{p+1,q} \text{ have the same left null space. } (8)
$$

This property can be checked as follows From computer $\{0,1,\ldots,m\}$ From $\{0,1,\ldots,0\}$, where $\bigcap_{n\geq 0}$ is a following $\bigcap_{n\geq 0}$ T , and perform every component value of the strategies of \sim , \sim defining its left null space, namely for extracting an orthonormal matrix S such that $S^T S = I_s$ and:

$$
S^T(\theta_0) \mathcal{O}_{p+1}(\theta_0) = 0 \tag{9}
$$

Matrix S depends implicitly on θ_0 . Although not unique, - two such matrices are related through a post-multiplication with an orthonormal matrix U – it can be treated as a function $S(\theta_0)$ [7]. Then the characteristic property in Equation (8) writes

$$
S^{T}(\theta_0) \mathcal{H}_{p+1,q} = 0 \tag{10}
$$

Now, the damage detection problem is to decide whether a new data sample $(Y_k)_{k=1,...,n}$ from the (possibly damaged) system is still well described by a reference parameter θ_0 (identified on data recorded on the undamaged reference system) or not. Let $\pi_{p+1,q}$ be the empirical counterpart or Equation (4) computed with the new data:

$$
\widehat{\mathcal{H}}_{p+1,q} \stackrel{\text{def}}{=} \text{Hank}\left(\widehat{R}_i\right) , \quad \widehat{R}_i = \frac{1}{n} \sum_{k=1}^n Y_k Y_{k-i}^T \tag{11}
$$

For checking whether the new data agree with the reference modal parameter θ_0 , the following residual is introduced in the \mathbf{r}

$$
\zeta_n(\theta_0) \stackrel{\text{def}}{=} \sqrt{n} \, \text{vec}\left(S^T(\theta_0) \, \hat{\mathcal{H}}_{p+1,q}\right) \tag{12}
$$

 \mathcal{L} it can be deduced that \mathcal{L} is called that \mathcal{L} is a series of \mathcal{L} is a series of \mathcal{L} in \mathcal{L} θ , and nonzero mean if a change occurs. Thus it plays the role of a residual.

For deciding that the residual $\zeta_n(\theta_0)$ is *significantly* different from zero, a particular asymptotic statistical framework is assumed where the changes to occur are supposed to be small $[7]$. Under convenient assumptions, the residual is asymptotically Gaussian, and manifests itself the damage by a change in its own mean value. In other words, let $\mathcal{J}(\theta_0)$ and $\Sigma(\theta_0)$ the residual sensitivity and covariance matrices, respectively. Then, provided that $\Sigma(\theta_0)$ is positive definite:

$$
\zeta_n(\theta_0) \xrightarrow[n \to \infty]{} \begin{cases} \mathcal{N}(\ 0, \ \Sigma(\theta_0)) & \text{in case of no change} \\ \mathcal{N}(\ \mathcal{J}(\theta_0) \ \delta\theta, \ \Sigma(\theta_0)) & \text{in case of a small deviation } \delta\theta \text{ in } \theta \end{cases}
$$
(13)

The generalized likelihood ratio (GLR) test, resulting from the maximization w.r.t. $\delta\theta$ of the ratio of the two Gaussian distributions in (13), provides us with the folfowing χ -test statistics built on the residual (12).

$$
\chi_n^2(\theta_0) \stackrel{\text{def}}{=} \zeta_n^T(\theta_0) \widehat{\Sigma}^{-1}(\theta_0) \widehat{\mathcal{J}}(\theta_0) \left(\widehat{\mathcal{J}}^T(\theta_0) \widehat{\Sigma}^{-1}(\theta_0) \widehat{\mathcal{J}}(\theta_0) \right)^{-1} \widehat{\mathcal{J}}^T(\theta_0) \widehat{\Sigma}^{-1}(\theta_0) \zeta_n(\theta_0)
$$
\n(14)

which should be compared to a threshold. In Equation (14), $J(00)$ and $\Delta(00)$ are consistent estimates of the sensitivity and covariance matrices of $\zeta_n(\theta_0)$ [7].

-Non-parametric test

In some cases it may be of interest to replace this parametric approach with a non parametric one, based on an *empirical* null space computed on a reference data set and not on a reference modal signature. Such a null space may result from a SVD of the empirical Hankel matrix built on the reference data set (indexed with $s = s$ superscript $s = s$

$$
\widehat{S}_0^T \ \widehat{\mathcal{H}}_{p+1,q}^{(0)} = 0 \tag{15}
$$

Such a non parametric detection approach is used e.g. in $[13, 14]$.

Based on new data from the (possibly damaged) system, the empirical Hankel $max_{p+1,q}$ is computed and the residual then writes.

$$
\widehat{\zeta}_n \stackrel{\text{def}}{=} \sqrt{n} \ \text{vec}\left(\widehat{S}_0^T \ \widehat{\mathcal{H}}_{p+1,q}\right) \tag{16}
$$

Let Δ be the covariance matrix of ζ . Then, provided that Δ is positive definite.

$$
\hat{\zeta}_n \xrightarrow[n \to \infty]{} \begin{cases} \mathcal{N} \left(\begin{array}{c} 0, \Sigma \end{array} \right) & \text{in case of no change} \\ \mathcal{N} \left(\begin{array}{c} \delta \Upsilon, \Sigma \end{array} \right) & \text{in case of a small deviation } \delta \Upsilon \text{ in } \hat{\zeta} \end{cases} \tag{17}
$$

The GLR test, resulting from the maximization w.r.t. $\delta \Upsilon$ of the ratio of the two Gaussian distributions in (17), provides us with the following χ -test statistics built on the residual

$$
\hat{\chi}_n^2 \stackrel{\text{def}}{=} \hat{\zeta}_n^T \hat{\Sigma}^{-1} \hat{\zeta}_n \tag{18}
$$

which should also be compared to a threshold. In Equation (10), ω is a consistent estimate of the covariance matrix of ζ_n .

3 Merging multiple measurements setups

It has been shown both experimentally and theoretically that covariance
driven sub space identification algorithm tend to factor out the non stationarities in the excitation, thanks to the averaging operations in Equation (11) and the key factorization property in Equation (6) [15, 16, 17]. The Hankel matrix factorization property in Equation (6) has also proven key to the extension of that algorithm to the simultaneous processing of *multiple measurements setups* recorded at different times and under different excitation conditions $[18, 17]$. When the sensors setups are all identical (same number and locations of sensors), this extended algorithm boils down to process the *empirical average* of the individual Hankel matrices associated with each sensor setup

Hence, when J reference data sets are available, as e.g. when handling the temperature effect, a global empirical Hankel matrix is computed by averaging the

empirical Hankel matrices corresponding to each reference data set

$$
\overline{\mathcal{H}}_{p+1,q}^{(0)} \stackrel{\text{def}}{=} \frac{1}{J} \sum_{j=1}^{J} \overline{\mathcal{H}}_{p+1,q}^{(0),j} \tag{19}
$$

Using a SVD as above, a global empirical null space \overline{S}_0 can then be obtained:

$$
\overline{S}_0^T \ \overline{\mathcal{H}}_{p+1,q}^{(0)} = 0 \tag{20}
$$

For handling the temperature effect, the idea proposed in this paper consists in assuming that ^J reference data sets are available for the undamaged structure at different *unknown temperatures*, and in using the trick in Equations (19)-(20) as the entry for the non parametric subspace
based detection algorithm in Equations $(16)-(18)$. It should be clear, however, that the situation with those J data sets is basically *different* from that of reference data sets recorded for the *same* structure subject to different excitations. Here, because of the temperature effect on the dynamics of the structure, the reference data sets actually correspond to different states of the undamaged structure

The proposed algorithm runs as follows Compute the global empirical null \mathbf{r} in Equation (1) reference data sets at the J reference data sets at the distribution of the J reference data sets at the distributio temperatures. Based on new data from the (possibly damaged) system, fill the empirical Hankel matrix $\pi_{p+1,q}$ and compute the residual:

$$
\overline{\zeta}_n \stackrel{\text{def}}{=} \sqrt{n} \text{ vec } (\overline{S}_0^T \; \widehat{\mathcal{H}}_{p+1,q}) \tag{21}
$$

with Δ an estimate of the covariance matrix of ζ , the corresponding χ -test statistics writes

$$
\overline{\chi}_n^2 \stackrel{\text{def}}{=} \overline{\zeta}_n^T \overline{\Sigma}^{-1} \overline{\zeta}_n \tag{22}
$$

This damage detection algorithm is expected to smooth out the temperature effect thanks to the averaging operation in Equation (19) .

Application

Both algorithms in Equations (14) and (22) have been experimented on two cases: a simulated bridge deck provided by LMSSMat and a vertical clamped beam within a climatic chamber, a test-case provided by LCPC.

 \lceil A similar idea is used in [19, 20].

-Simulation: simple bridge deck

In this section, a simulated bridge deck is described, with controlled temperature variations. The temperature effect on the modal parameters and on the test results is discussed

4.1.1 The test-case

In order to outline the temperature effect and to test the validity of the proposed damage detection algorithm with temperature rejection a simulated bridge deck has been simulated

This simplified bridge model consists of 28 supports and a deck which is $3m$ m and the shown in Figure as shown in Figure . The Structure in Figure 1 (2001), the Structure in Structure and tural Dynamics Toolbox [21] was used to develop and implement the finite element model of this bridge The whole bridge span is modeled using standard
node isoparametric volume elements and 13668 nodes. At both ends, the span motion is blocked in the y and z directions while a nominal stimulus while a nominal stimulus while a nominal stimulus w the bridge x direction, to simulate a blocking condition.

The temperature variations are modeled using either one of two fields: a uniform temperature elevation and a linear variation with z from 25° C on the deck to 15° C at the bottom. The vertical thermal gradient field and the induced axial strain σ_{xx} state are depicted on Figure 2. The warmer deck tends to expand while the cooler bottom contracts. The figure also clearly shows edge effects where the springs are used to model attachment conditions near the piles

The damage is simulated as the reduction in the stiffness of some elements. More precisely, the damaged elements, whose location is $16.5m$ from the end, are modeled as a reduction of the material model model with α , which is a vertex defining an extent of the damaged area o consists of two sections, each of which includes 48 elements. But, as displayed in Figure 1 (Right), only 44 of those elements are simulated as damaged, so there are 88 damaged elements altogether within the bridge model. Figure 1 also shows the location of the simulated damaged sections and elements in the bridge

Simulation scenarios for both the undamaged case, which serves as the reference signal for subsequent damage detection, and the damaged case are considered. For each case, 21 temperature scenarios are undertaken, and each scenario is repeated 50 times. The output data are simulated under white noise excitations. 21 sensors are uniformly distributed along the bridge to measure the vertical displacement, and the sensors location is also shown in Figure 1. The sampling frequencies for all sensors are the Hz and the Hz

Figure 3 displays how the first frequency is affected by a uniform temperature decrease, under safe and damaged conditions, and how the corresponding partial χ -test focussed on that frequency is affected.

4.1.2 Numerical results

The reference parameter θ_0 , the null space $S(\theta_0)$ in Equation (9) and matrices $J(0,1,2,0,0)$ for the test in Equations (12)-(14) are estimated on the first scenario where is no present space α in Equation () and matrix α $\overline{\Sigma}$ for the non parametric test in Equations (21)-(22) are estimated are estimated on the whole set of realizations of the scenarios for the undamaged case

On Figures 4-5, the values of the original subspace-pased χ -test in Equation $f(14)$ for the 21 scenarios are displayed on the left hand side, and the values of the μ ew χ -test in Equation (22) are displayed on the right hand side. On Figure 4 are displayed all the test values obtained for the repetitions of the scenarios These results are condensed in Figure 5 where each test value is the empirical mean

On Figure 4 (Left), it is possible to discriminate between the damaged and the undamaged values for the test in Equation (14) . Whereas on Figure 4 (Right), it is possible to set a threshold for separating the values of the new test for the damaged and safe scenarii. Figure 5 (Right) provides us with the same information about the dispersion of the test values, which are much higher in the damaged case, as theoretically predicted. These results show that, for the present experiment, either the mean test value in Figure 5 (Right) or any single test value in Figure 4 (Right) is sufficient to detect the damage when the temperature T varies.

-Laboratory test-case: clamped beam within a climatic chamber

4.2.1 The test-case

The experimental device is depicted in Figure 6. A vertical beam is clamped at both ends on a workbench made of four vertical thick columns and two horizontal decks. This workbench is made of steel, whereas the beam is made of aluminum. The whole apparatus is set inside a climatic chamber with controlled ambient tem perature. Because steel and aluminum have different thermal expansion coefficients $(11.7e - 0)$ and $25.4e - 0$ Λ , respectively), a temperature change naturally induces a signicant axial prestress inside the beam constant along the beam in the absence of external forces

The test beam is instrumented with four accelerometers located at nodes of the 5th flexural mode in order to avoid nodes of modes 1 to 4 (a truncation up to the 4th mode has been performed for the analysis reported in $[22]$). A pair of aluminum strain gauges with thermal compensation is also bonded on the beam The half sum of both strains gives a direct measure of the actual axial prestress (divided by Young's modulus), without requiring any temperature measurement. This measurement, not useful for the present detection method, it is of primary importance for the method in $[22]$. Some temperature sensors have also been used in order to check that gage measurements are closely related to thermal variations

Tests are carried out inside the climatic chamber, first by stabilizing the ambient temperature for 1 hour, and then cooling down for 17 hours with a slope of $-1^{\circ}C$ per hour The beam is acoustically excited by a loudspeaker with a white noise in put. Strains and temperatures measurements are saved every seconds. Acceleration . In the contract \mathbb{R}^n are also triggered every trial \mathbb{R}^n and \mathbb{R}^n are \mathbb{R}^n . The seconds with \mathbb{R}^n sampling frequency is such that is such that for modes is such that for modes in the three modes is the three modes in the thre is below the contract of the contract of \mathbf{H}

An example of experimental results is given in Figure 7 (undamaged case). It clearly shows that prestress and thus frequencies increase as temperature decreases with time (note that prestress is taken positive when tensile). At the end of the test, the first frequency has been increased by about 15% . Modes 2, 3 and 4 (not shown here) have been increased by about $8, 5$ and 3% , respectively. Axial prestress has thus a stronger effect for lower frequencies, which is coherent with known results $\left[23\right]$.

Finally, two sets of experiments are performed, for the safe and damaged cases respectively. In each set, 37 temperature scenarios are undertaken, and each scenario is repeated in the extreme of an interest of an interesting to an interest of an interesting property of an interest attached to the beam plays the role of a local non destructive damage This damage may be tuned by increasing the stiffness and/or the height of the spring. In this experiment, the spring is located at $L/3$ and its stimess is about $\kappa = 4000$ *N.m.* This choice has been designed from a finite element model in order to give slight (less than 1%) deviations from the no-spring "safe" case. Experimental deviations of modes in the above are about the species of the second contract of the second con ations for modes 3 and 4 are a bit odd, but may result from a mechanical coupling of the beam with the workbench and the spring bracket. Figure 8 shows how the first frequencies are affected by the temperature scenarios, under both safe (blue) and damaged (red) conditions.

4.2.2 Numerical results

The reference parameter θ_0 , the null space $S(\theta_0)$ in Equation (9) and matrices $J(\nu_0), \Delta(\nu_0)$ for the test in Equations (12)-(14) are estimated on the TO realizations of the rst scenario corresponding to a thermal constraint about The Ω in Equation () in Equation () in Equation () is the non-parametric test in Γ equations (e.g. (e.g. are estimated on the scenarios of the scenarios of the scenarios of the scenario for the undamaged case

In Figures y -IV, the values of the original subspace-based χ -test in Equation (14) for the 25 scenarios corresponding to thermal constraints $\varepsilon_x - \alpha \delta T$ ranging approximately between and are displayed on the left hand side and the values of the new χ -test in Equation (22) are displayed on the right hand side. On Figure are displayed all the test values obtained for the repetitions of the scenaries is the condensed in Figure is the complete in Figure is the condensed in the condense is the condense empirical mean of realizations of the same scenario It should be obvious that is too small a number for clearing out possible outliers; this is confirmed on Figure 10 $(Right)$.

On Figure 9 (Left), it is not possible to discriminate between the damaged and the undamaged values for test in Equation (14) . Whereas on Figure 9 (Right), it is possible to set a threshold for separating the test values of the damaged and safe scenarii Figure Right provides us with the same information about the disper sion of the test values, which are much higher in the damaged case, as theoretically predicted. These results also show that, for the present experiment, either the mean test value in Figure Right or any single test value in Figure Right is sucient to detect the damage when the temperature T varies.

$\overline{5}$ Conclusion

The problem of handling the temperature effect in vibration-based monitoring of civil engineering structures has been addressed A non parametric approach has been proposed, based on a global empirical null space merging reference data sets recorded at unknown temperatures and plugged into a statistical subspace damage detection algorithm The relevance of the proposed algorithm has been illustrated on two examples : a simulated bridge deck model and a laboratory test-case made of a clamped beam within a climatic chamber

Issues for future research encompass validation on structures in
operation and extension to the non stationary excitation case Actually computing the test co variance matrix for each scenario, as performed in $[22]$, would increase if not ensure the robustness of the approach w.r.t. changes in the excitation.

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