## Harmonic skeleton for realistic character animation

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## Skeletal animation

Building an animated 3D character requires to:
(1) Create a 3D mesh
(2) Set the 3D position and hierarchy of skeleton joints
(3) Set the 3D orientation of skeleton joints
(4) Create high-level controllers for animation (IK, constrains)
(5) Define skinning weights


## Skeleton computation

- Nowadays:
- By hand
- By experts
- Automatic methods:
- Little control over the result
- Provide noisy skeletons (unwanted joints)
- Rely only on the geometry of the shape
$\rightsquigarrow$ not the anatomy of the model (bone structure)

[Liu PG'03]

[Lien SPM'06]




## Our idea

## Control of the extrema thanks to a harmonic function

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$$
\begin{aligned}
& \Downarrow \\
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\end{aligned}
$$

Automatic association of semantic information to nodes/joints


## Our idea

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Adapted refinement to match handmade IK skeletons


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Adapted refinement to match handmade IK skeletons
$\rightsquigarrow$ Help for both experts and non-experts

## Contributions

A skeleton generation algorithm with the following properties:

- Semantic decomposition of both skeleton and shape
- Specialized heuristics for bipeds and quadruped mammals
- Robustness (pose+deformation: see paper)
- Fast and almost no user intervention, but control is possible



## Algorithm overview



Mesh

+ source vertex



Harmonic graph

## Reeb graph

Reeb graph of $f=M / \sim$
$x_{1} \sim x_{2} \Longleftrightarrow\left\{\begin{array}{l}f\left(x_{1}\right)=f\left(x_{2}\right) \\ \text { and } x_{1} \text { and } x_{2} \text { belong to the same } \\ \text { connected component of } f^{-1}\left(f\left(x_{1}\right)\right)\end{array}\right.$

$f$

mesh

level sets


Reeb graph

## Harmonic function

Laplace equation with boundary conditions:

$$
\begin{cases}\triangle f(x)=0 & \forall x \in M \\ f(x)=g(x) & \forall x \in B_{M}\end{cases}
$$

- $B_{M}=$ set of vertices: extrema of the graph
- $g(x)=$ approx. geodesic distance to source vertex

height

distance to source

harmonic


## Harmonic graph computation

(1) Extrema selection

- Automatic or not
- Source vertex on the head (by hand)


## Harmonic graph computation

(1) Extrema selection
(2) Harmonic function $f$ computation


## Harmonic graph computation

(1) Extrema selection
(2) Harmonic function $f$ computation
(3) Reeb graph computation

- In $O(n \log n)$ time
[Cole McLaughlin SoCG'03]



## Harmonic graph computation

(1) Extrema selection
(2) Harmonic function $f$ computation
(3) Reeb graph computation
(4) Graph filtering

- Small (for $f$ ) edges removal
- Related to persistence [Edelsbrunner FOCS'00]
- Can be done automatically [Pascucci SIGGRAPH'07]
$\Rightarrow$ morphology recovered


## Algorithm overview



Mesh

+ source vertex



Harmonic graph

## Symmetry axis detection

- Symmetry of the morphology (2 arms, 2 feet, ...)
- Finding symmetries on a graph: NP-complete
- Assumptions:
- Source node on the symmetry axis
- No cycle
- 2 subtrees isomorphic $\Longleftrightarrow$ same depth + same degree for root nodes



## Simple embedding

Not straightforward solution for saddle nodes

- Insert regular nodes
- Use the symmetry axis





## Joint hierarchy and orientation

Hierarchy:

- Use symmetry axis: e.g. last joint = root joint

Orientation:

- Use the direction of the embedding of the symmetry axis

Skeleton refinement:

- Add regular nodes on the graph
- Embedding: center of mass of their connected component for $f$



## Algorithm overview



Mesh

+ source vertex



Harmonic graph

## Bipeds and quadrupeds

The symmetry axis gives semantic information!


New nodes inserted:

- Edges subdivided
- New extremum for the jaw (biped)/the top of the head (quadruped)

Reference frame
(Spine, $\frac{P_{1} P_{2}}{\left\|P_{1} P_{2}\right\|}$, Spine $\times \frac{P_{1} P_{2}}{\left\|P_{1} P_{2}\right\|}$ )

## Heuristics

- Some nodes are shifted along one of the directions of the reference frame
- New nodes:
- mean Euclidean position
- or mean value for $f$
- or fitting some geometric features [Tierny PG'06]


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Example: spine joints, quadruped case

- SP divided into 4 edges
- All joints lifted up along Spine $\times \frac{P_{1} P_{2}}{\left\|P_{1} P_{2}\right\|}$
- $J_{\text {new }}=J_{\text {simple }}+c .\left\|J_{\text {simple }} B\right\|$ Spine $\times \frac{P_{1} P_{2}}{\left\|P_{1} P_{2}\right\|}$
- $c=0.8 / 0.76 / 0.72 / 0.64, S$ so that Spine not modified



## Results



14,000 faces, 0.8 s


4,000 faces, 0.2 s


296,000 faces, 36 s


7,000 faces, 0.6 s


850 faces, 0.05 s


38,000 faces, 3s

## Video: use for animation



## Conclusion

## Input:

- Manifold mesh
- Source vertex (on the head)
- A priori knowledge about character's real anatomy

Output:

- IK skeleton closely matching handmade skeleton
- Semantic information attached to joints (symmetry axis, anatomy)


Computed


Handmade (previous)

## Future work

- Enhancement
- Robust feature extraction [Zhang ToG'05]
- Reeb graph for non-manifold meshes [Pascucci SIGGRAPH'07]
- Skinning
- Use $f$ values : vertices $\leftrightarrow$ joints
- Use joint semantics to define adapted weights


## Questions?



