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An Adaptive Algorithm for Incremental Evaluation of Production Rules in Databases

Françoise FABRET Mireille REGNIER Eric SIMON

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PROGRAMME 1 -

Architectures parallèles, Bases de données, Réseaux et Systèmes distribués



Un Algorithm Adaptif pour l'Evaluation Incrementale des Programmes de Règles de Production pour les Bases de Données

Françoise Fabret, Mireille Régnier and Eric Simon INRIA - 78153 Le Chesnay-Cédex, FRANCE

Résumé

Plusieurs algorithmes de calcul incrémental ont été proposés pour évaluer les programmes de règles de production pour les bases de données. Ils sont tous dérivés d'algorithmes, tels RETE et TREAT, qui ont été conçus pour les systèmes à bases de règles développés dans le cadre de l'Intelligence Artificielle. Dans ce papier, nous étudions un problème crucial soulevé par ces algorithmes : quelles données est il profitable de matérialiser et de maintenir pour accélérer l'évaluation d'un programme? Nous montrons que la réponse relève d'un compromis entre les facteurs opposés espace et temps. Notre contribution est de proposer un algorithme adaptatif qui prend en entrée un programme de règles et retourne, pour chaque règle, l'ensemble des expressions relationnelles dont le maintien conduit à un bon compromis espace temps. Notre algorithme peut être utilisé aussi bien pour des règles ayant une sémantique ensembliste que pour celles dont la sémantique set tuple à tuple. Nous comparons notre algorithme avec des algorithmes existants qui sont dédiés au calcul incrémental des programmes à base de règles de production pour les bases de données.

Mots Clés : algorithmes de calcul incrémental, règles de production, évaluation des langages de règles de production pour les bases de données, optimisation des règles de production.

An Adaptive Algorithm for Incremental Evaluation of Production Rules in Databases

Abstract

Several incremental algorithms have been proposed to evaluate database production rule programs. They all derive from existing incremental algorithms, like RETE and TREAT, developed for rule-based systems in the framework of Artificial Intelligence. In this paper, we address a specific but crucial problem that arises with these incremental algorithms: how much data should be profitably materialized and maintained in order to speed-up program evaluation? We show that the answer exposes to a well known space-time tradeoff. Our major contribution is to propose an adaptive algorithm that takes as input a program of rules and returns for each rule, the set of most profitable relational expressions that should be maintained, in order to obtain a good space-time compromise. A notable feature of our algorithm is that it works for both set-oriented and instance-oriented rules. We compare our algorithms with existing incremental algorithms for database production rule programs.

1 Introduction

Production rules have demonstrated to be a powerful programming paradigm to specify queries, views, integrity constraints and triggers in a database system [DE88], [SLR88], [KdMS90], [SKdM92], [SJGP90], [Han89], [WCL91]. However, the problem of efficiently supporting rules in a database system still constitutes a major challenge to establish the viability of rule-based technology. A few papers have addressed this problem by adapting algorithms that were designed by AI researchers to optimize OPS5 rule programs in a main memory environment.

Most database rule systems (see [HW92]) follow a recognize-act-cycle similar to that of OPS5 [BFKM85]. A production rule consists of an action that must be executed whenever a condition over the database holds. In active database rule languages, an event can be associated with the (condition, action) pair. Usually, the action is a set of operations on the database that is insertions, deletions, and updates. Executing a rule program proceeds by (i) evaluating rule's conditions against the database, (ii) choosing one rule instantiation whose condition is satisfied, (iii) executing the action of the selected rule, and repeating the cycle until a fixed-point is reached (if any). The set of tuples that satisfies a rule condition in a given database state is called a satisfying rule instantiation.

A critical part of rule evaluation is the match phase (phase (i) above) where satisfying rule instantiations are computed. A naive algorithm would execute the query associated with each rule's condition against the entire database on each cycle. This approach rapidly becomes intractable as soon as the number of rules and facts gets large. To overcome this problem, *incremental* algorithms that maintain state information from cycle to cycle have been proposed by AI researchers. The two main known algorithms that fall into this class are RETE [For82] and TREAT [Mir87].

The RETE algorithm maintains the result of the first matching phase into an ad-hoc data structure called a discrimination network. In this structure, the result of each select and join operation that occurs in every rule's condition is recorded and stored in some node. Results of selections are stored in alpha-memory nodes and form the input portion of the discrimination network. The results of joins are stored in beta-memory nodes. Nodes corresponding to the select and join operations that occur in the same rule's condition are connected together in the form of a dataflow network. Satisfying rule instantiations are stored in the output nodes of the network.

RETE transforms the recognize-act-cycle above as follows. Phase (i) is removed from the cycle and becomes an *initialization* phase during which the discrimination network is built. A new phase is then inserted in the cycle after phase (iii). It propagates every change to the database done by a rule's action, (expected to be very small compared to the size of the database), towards the appropriate alpha and beta-memories. Thus, the set of rule instantiations is *incrementally* (or differentially) maintained. The TREAT algorithm essentially differs from RETE by the fact that it does not maintain beta-memory nodes. TREAT only maintains alpha-nodes and the set of all the satisfying rule instantiations.

Our starting point for this research is that incremental algorithms have an inherent space-time tradeoff. Intuitively, maintaining some node N in a discrimination network is profitable if the work spent in computing the changes to the operands involved in the expression that computes N and in updating the current value of N from its previous value is less than that spent in computing it directly from its operands. The three important factors in this type of improvement are, (1) the ability to efficiently compute the differential change to N for arbitrary expressions, (2) the boundedness of this differential, and (3) the number of times N is used with regard to the number of times N is changed.

In a sense, RETE and TREAT are two opposite answers to this tradeoff. RETE must do as much work to maintain memory nodes whenever tuples are deleted from the database as it does to maintain memory nodes whenever tuples are inserted. TREAT does much less work when tuples are deleted from the database since it does not have to update the intermediate join results. Only the final set of rule instantiations has to be updated. But TREAT does do more work than RETE when tuples are inserted because rule conditions have to be reevaluated for these new tuples. In some situations, the tradeoff favors TREAT([Mir87], [WH92]). In others, RETE performs better.

The purpose of this paper is to systematically investigate this problem of profitability of incremental algorithms for rule-based programs. Our main contribution is to propose an adaptative algorithm that given a rule program chooses the better compromise of discrimination network in between RETE and TREAT. Following previous work on the design of incremental algorithms in the framework of high-level programming languages such as SETL ([PK82], [Pai83]), our algorithm relies on a heuristic-based characterization of the notion of profitability. More, our algorithm is based on a careful analysis of the migration flow of data in a rule program.

Usually, a rule language has either set-oriented (e.g., Ariel, RDL, Starburst) or instance-oriented rules (e.g., OPS5, RPL, PRSII). We show that this difference of semantics greatly influences the choice of a good discrimination network. A notable feature of our algorithm is that it works for both set-oriented and instance-oriented rules.

This paper is structured as follows. Section 2 presents our rule language, introduces useful terminology, and relates our language to OPS5. In Section 3, we describe RETE and TREAT algorithms and exhibit their inherent space-time tradeoff. In Section 4, we first characterize expressions, called autonomous expressions, that can be easily differentiated with respect to some changes to their operands. Then, we define when a relation is profitable to maintain and give an algorithm that extracts maximal profitable relations from a given conjunctive formula. Section 5 presents our main adaptative algorithm, which given a set of rules determines the better discrimination network to build. Section 6 compares our work with other related work. Indeed, we show that our results are complementary to previous results on the efficient implementation of RETE and TREAT in a database system. Finally, Section 7 concludes the paper.

2 The Rule Language

In order to make the presentation of our algorithms general and independent from a particular rule-based language syntax, we shall use a Datalog-like notation for rules. From a semantic point of view, we distinguish set-oriented rules from instance-oriented rules.

2.1 Terminology

We briefly review some terminology. A fact over a predicate Q of arity n is an expression $Q(a_1, ..., a_n)$ where each a_i is a constant. A database schema is a finite set of predicates. A (database) instance over a schema S is a finite set of facts over predicates in S. If I_k is a set of facts and Q a predicate in S, $Q^{(k)}$ denotes the set of facts over Q in I_k . A literal is an expression of the form $(\neg)Q(x_1, ..., x_m)$ where $m \ge 0$, Q is a predicate of arity m and each x_i is either a variable or a constant. An eq-literal is an expression of the form $(\neg)x_1 = x_2$ where x_1, x_2 are variables or constants. We shall use letters x, y, z, \ldots to denote variables, and greek letters to denote constants.

Definition 2.1 A rule is an expression of the form

$$B_1, \ldots, B_n - A_1, \ldots, A_k \ (k \ge 1, n \ge 0),$$

where each A_j is a literal and each B_i is a literal or an eq-literal. A rule program is a finite set of rules.

We consider that there may exist a partial ordering between rules where $r \leq r'$ means that if r and r' are both firable at the same time, then r has priority over r'. This ordering is assumed to be available at any time during program execution. We denote (Γ, \leq) a rule program with a priority ordering between rules.

2.2 Set-oriented Rules

A rule can be interpreted using either an instance-oriented or a set-oriented semantics. We start with the last one.

Effect of a rule on a database instance: Let r be a rule: $body \rightarrow A_1, ..., A_p, \neg B_1, ..., \neg B_n$, and I a set of facts. Let r' be a ground instance of r such that (i) each literal of the body of r' is a fact in I and each eq-literal in the body of r' holds, and (ii) each variable is valuated to some constant occurring in I. Then r' is said to be a satisfying instance of r in I. Now, the set of ground literals in the heads of all the satisfying instances of r in I is called the effect of r on I, denoted $effect_r(I)$.

Intuitively, the effect of rule r on I is the global effect obtained by considering the actions of all the satisfying instances of r in I.

Definition 2.2 A rule r is said to be *firable* in a state I if there exists a fact A such that either

- $A \in effect_r(I)$, $\neg A \notin effect_r(I)$ and $A \notin I$, or
- $\neg A \in effect_r(I), A \notin effect_r(I) \text{ and } A \in I$

Thus, a rule is firable if its firing would produce a net change to the current database state.

Semantics of a rule program: Let (Γ, \leq) be a rule program. This program defines a relation among database instances as follows. For each state I, J is reachable from I using Γ if there is a firable rule r in Γ such that no other firable rule has priority over r, and J consists of the facts A such that:

- A is in $I \cup effect_r(I)$ and $\neg A$ is not in $effect_r(I)$ or
- A is in I and A, $\neg A$ are both in $effect_r(I)$.

If a sequence of reachable states has a limit, it is called a *fixpoint* of the program. Notice that a program may have several fixpoints or no fixpoint at all.

Definition 2.3 Given a rule program and a state I, the conflict set is defined to be the set of all the firable rules in I.

2.3 Instance-oriented Rules

A set-oriented rule is fired for all its instantiations in one step whereas an instance-oriented rule is fired for one instantiation in one step. Thus, the difference is that we consider the effect of a satisfying rule instance alone. If r' is a satisfying instance of r, we denote the effect of r' on I by $effect_{r'}(I)$. We define r as a firable rule if there exists a satisfying firable instance r' of r that obeys the conditions of Definition 2.2., where $effect_r(I)$ is replaced by $effect_{r'}(I)$. Then, the semantics of a rule program is defined as for set-oriented rules except that r is replaced by a satisfying instance r' and $effect_r(I)$ is replaced by $effect_{r'}(I)$. Finally, the conflict set is defined to be the set of all the firable satisfying instances of rules in a state I.

2.4 Comparisons with OPS5-like Languages

OPS5 [BFKM85] is the underlying language for which RETE and TREAT have initially been designed. Compared to OPS5, our language has three main differences.

First, in OPS5, all facts are associated with a unique identifier called a timestamp. If firing a rule has for effect to insert a fact A in the database then even if A already exists, it will be inserted again with a different timestamp. Hence, a rule that has a satisfying instance is always firable. Instead, we used a purely value-based data model, that is when a fact A is inserted by a rule it does not get a new timestamp that will distinguish it from an existing fact A. The use of a value-based semantics induces an extra-cost to evaluate the net effect of a rule, i.e., to determine if a rule is firable or not. Second, OPS5 uses a refraction-based semantics. Refraction prevents a ground rule from being fired twice during a program execution. Last, we assume a static priority ordering between rules whereas OPS5 uses a dynamic conflict resolution strategy.

In spite of these differences of semantics, our final algorithm is applicable to OPS5-like languages. The main reason is that we seek to optimize the specific phase of matching rules against the database, which is common to all rule-based languages [HW92]. Furthermore, the semantics of rules (set-oriented or instance-oriented) can be passed as a parameter to our algorithm.

3 Incremental Computation Algorithms

In this section, we illustrate the use of RETE and TREAT. We assume that rules are instance-oriented (as in OPS5). Our main goal is to exhibit the inherent space-time tradeoff of incremental algorithms.

3.1 RETE in Action

Consider the following rule:

$$r1: A(x,\alpha,z), B(x,y,\beta), C(\gamma,y,w) \rightarrow C(\gamma,x,w), \neg C(\gamma,y,z).$$

This rule is compiled by RETE in the dataflow network depicted in Figure 1. The network has three alpha-nodes n1, n2, n3, and two beta-nodes p1, p2, where:

$$n1 = \sigma_{A,2=\alpha}A$$
, $n2 = \sigma_{B,3=\beta}B$, and $n3 = \sigma_{C,1=\gamma}C$
 $p1 = \prod_{\{n1,1,n2,2,n1,3\}} (n1 \bowtie_{n1,1=n2,1} n2)$, and $p2 = \prod_{\{p1,1,p1,2,p1,3,n3,3\}} (p1 \bowtie_{p1,2=n3,2} n3)$

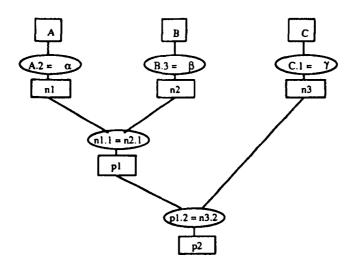


Figure 1: RETE network for rule r1

and σ , Π , and \bowtie respectively denote relational select, project and join.

The incremental evaluation procedure of a rule program proceeds essentially as follows:

Compared to the original evaluation procedure used by RETE and TREAT, there is one main difference. Since we assume statically-defined priorities between rules, there is no need to construct the whole conflict set before entering the while loop. We only need to find one firable rule (step †). Thus, selecting a firable rule in step ‡ may require to match some non-already tried rules against state in order to compute their set of satisfying instances and hence, to expand the discrimination network.

Suppose the initial database, called I_0 , is as shown on Table 1.

¹If rules have instance_oriented semantics, then r is a firable satisfying instance

A	В	Ĉ
0 α 1	0 2 β	γ 2 1
$2 \alpha 0$	20β	$\gamma 03$
3 α 1	3 2 B	
	43β	

n1	n2	n3	n1.1 = n2.1	p1.2 = n3.2
0 α 1	023	γ 2 1	0 2 1	0 2 1 1
200	20β	$\gamma 0 3$	$2\ 0\ 0$	2003
3 0 1	32β		3 2 1	3 2 1 1
	433			

Table 1: state I_0

Table 2: Network in state I_0

Then, the values of the network's nodes in I_0 are shown on Table 2. Each tuple of $p2^2$ represents a firable satisfying instance of r_1 . Suppose that r_1 is fired with variable instantiation (x/3, y/2, z/1, w/1), then $C(\gamma \ 3 \ 1)$ is inserted and fact $C(\gamma \ 2 \ 1)$ is deleted. We call I_1 the resulting instance. The propagation of these two updates to C is done as follows. Starting with the deletion, tuple $t = C(\gamma \ 2 \ 1)$ is deleted from n_3 . Then p_1 is joined with t to discover which tuples must be deleted from p_2 . Tuples $p_2(0\ 2\ 1\ 1)$ and $p_2(3\ 2\ 1\ 1)$ are returned and deleted. Now, for the insertion into C, tuple $C(\gamma \ 3 \ 1)$ is first inserted into n_3 and since there are no successful matchings with p_1 , propagation stops. The network in state I_1 is shown on Table 3. Now, r_1 can be fired with instantiation (x/2, y/0, z/0, w/3) and the process continues until the conflict set becomes empty.

n1	n2	n3	n1.1 = n2.1	p1.2 = n3.2
0 a 1	023	γ 3 1	0 2 1	
2 α 0	20 B	703	200	2003
3 a 1	3 2 3		3 2 1	
	433			

Table 3: Network in state I_1

3.2 TREAT in Action

We now describe the execution of TREAT on the same rule. TREAT compiles rule r1 in the dataflow network of Figure 2. The only difference with RETE's network is that the result of the join between n_1 and n_2 is not kept. On the other hand, TREAT maintains for each rule its set of satisfying instances. This coincides with node p_2 in RETE's network, but here we call this node p. Thus, we have

$$p = \prod_{\{n1,1,n2,2,n1,3,n3,3\}} \{n1 \bowtie_{n1,1=n2,1} n2 \bowtie_{n2,2=n3,2} n3)\}.$$

In fact, TREAT also remembers in p the tuple identifiers of the matching tuples.

When the rule first fires, tuple $C(\gamma \ 3 \ 1)$ is inserted and tuple $C(\gamma \ 2 \ 1)$ is deleted. These updates are propagated in the network. The deletion only requires to search into p for all tuples where the identifier of the deleted tuple occurs. There are two such tuples that are deleted from p. Then, the insertion into C is propagated. Tuple $C(\gamma \ 3 \ 1)$ is first inserted into n_3 . Then the join between n_1 and n_2 is computed and the result is joined with the new n_3 tuple yielding two new tuples that are inserted into p. This process continues until the conflict set becomes empty.

²In the original RETE and TREAT algorithms, p2 exactly represents the conflict set because of the particular semantics of OPS5 (timestamps and refraction)

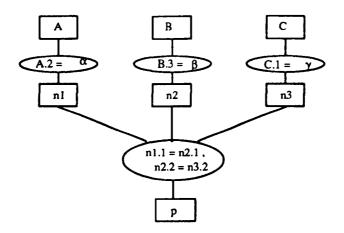


Figure 2: TREAT network for rule r1

3.3 Tradeoff Between RETE and TREAT

The main question raised by the previous example is: "is it worthwhile to keep node p_1 ?". To answer, we need to compare the work done by each algorithm at each cycle.

RETE does an extra work to maintain p_2 when a deletion to n_3 occurs. But, some implementations of RETE optimize it by recording tuple identifiers in the nodes (as TREAT does). On the other hand, TREAT does an extra work to propagate insertions because the join betwen n_1 and n_2 needs to be recomputed at each cycle. Clearly, on this example, the tradeoff will favor RETE (even if RETE does not optimize the maintenance of p_2 with tuple identifiers).

Now, suppose that the action part of the rule is changed, yielding the following rule:

$$r2: A(x,\alpha,z), B(x,y,\beta), C(\gamma,y,w) - \neg B(y,z,\beta)$$

Since the body of r_2 is the same as r_1 , the networks respectively built by RETE and TREAT for r_2 are as the networks for r_1 . But this time, TREAT outperforms RETE because the only effect of the rule is to delete facts and these deletions require less work with TREAT. Indeed, RETE will update nodes n_2 , p_1 and p_2 whereas TREAT will update n_2 and p_3 .

The above examples hopefully make two points. One, there is an inherent space-time tradeoff in incremental algorithms. Maintaining information may help for computing new rule instantiations but may hurt performance when rule instantiations are deleted from the conflict set. In general, a rule program has a non-monotonic behavior with respect to its conflict set and solving the tradeoff depends on the particular rule program to treat. Second, an important factor in rule's analysis is the effect of a rule's action on the satisfaction of the condition parts of the other rules.

4 Computation of Profitable Relations

Ideally, an algorithm that chooses a discrimination network for a set of rules should consider two important factors:

1. the ability to efficiently compute the differential change to every node in the network associated with a relational expression, given the net changes to its predecessor nodes,

2. the *profitability* of maintaining a node in the network for speeding calculations that will follow the materialization of the node.

Both conditions must be met to decide to maintain a node in the network. The first problem is addressed in Sections 4.1 and 4.2, while the second one is addressed in Section 4.3. We conclude by presenting an algorithm that given a safe conjunction of literals Φ and a set of changes to the predicate's instances occurring in Φ , determines a set of maximal profitable relations that are useful to maintain in order to efficiently maintain the relation defined by Φ .

4.1 Autonomous Expressions

The problem addressed by our algorithm is not totally new. Previous work (e.g., [BCL89]) has addressed the problem of determining which data are useful to maintain in order to speed-up the maintenance of a materialized view when base relations change. In particular, an interesting case is when the new value of the view can be computed from its previous (stored) value and the differential changes applied to its operand relations. The view is said to be autonomously computable.

Following this line, we generalize the notion of autonomously computable view introduced in [BCL89] and provide three criteria to syntactically detect autonomous expressions that consist of a conjunction of literals.

In what follows, a change to a predicate instance is either an insertion or a deletion of tuples. The sign of a predicate in a conjunction of literals indicates if it occurs positively or negatively. We also denote $\Phi^{(k)}$ the relation defined 3 by a conjunction of literals $\Phi(\vec{x})$ in state I_k . Without loss of generality, we only consider formulas Φ where each predicate occurs only once (this may be achieved by renaming).

Definition 4.1 Let Φ be a (safe) conjunction of literals and c a change to a predicate P occurring in Φ . Then Φ is autonomous for P wrt c if for any k, $\Phi^{(k+1)}$, can only be computed from $\Phi^{(k)}$ and c.

This definition is generalized to a set of changes.

Definition 4.2 Let Φ be a (safe) conjunction of literals and $\mathcal{C}_{\mathcal{P}}$ a set of changes to P. Φ is autonomous for P wrt $\mathcal{C}_{\mathcal{P}}$ if Φ is autonomous for P wrt every change of $\mathcal{C}_{\mathcal{P}}$. Let \mathcal{C} be a set of changes to some predicates of Φ . Φ is autonomous wrt \mathcal{C} if for each predicate P and for each change c of \mathcal{C} , either c has no effect on P, or Φ is autonomous for P wrt c.

Our criteria to detect autonomous expressions are presented below. We shall use the following notations. Let Φ be a (safe) conjunction of literals and P a predicate in Φ . We partition the variables of Φ into three sets: SV contains variables shared by P and some other predicate of Φ , PV contains variables that occur solely in P, and RV contains the remaining variables.

First and Second Autonomy Criteria: Let I_k be a state and I_{k+1} the state obtained after applying a change c to $P^{(k)}$.

³In the sense of [Ull88], p. 107

1. If P is positive and c is a delete, then Φ is autonomous for P wrt c and the relation defined by Φ in state I_k is defined by:

$$\begin{cases}
\Delta \Phi^{(k)} = \Phi^{(k)}(SV, PV, RV) \bowtie \Delta P^{(k)}(SV, PV), \\
\Phi^{(k+1)} = \Phi^{(k)} - \Delta \Phi^{(k)}
\end{cases} (1)$$

where $\Delta P^{(k)} = P^{(k)} - P^{(k+1)}$

2. If P is negative and c is an insert, then Φ is autonomous for P w.r.t c and the relation defined by Φ in state I_k is defined by formula (1), in which $\Delta P^{(k)} = P^{(k+1)} - P^{(k)}$.

Before introducing the third criteria, we need another definition.

Definition 4.3 Let $P(A_1, ..., A_n)$ be a relational schema and S be a subset of $\{A_1, ..., A_n\}$. We say that $\Pi_S P$ is *stable* wrt a set of changes C, if for any state I_k , C has no effect on $\Pi_S P^{(k)}$.

For instance, P is stable on $\{x\}$ wrt the changes induced by rule $r: R(x,z), P(x,y) \rightarrow P(x,z)$.

Third Autonomy Criteria:

If P is positive, c is an insert and $\Pi_{SV}P$ is stable wrt Γ , then Φ is autonomous for P w.r.t c and the relation defined by Φ in state I_k is defined by

$$\begin{cases} \Delta \Phi^{(k)} &= (\Pi_{\{SV,RV\}} \Phi^{(k)}(SV,PV,RV)) \bowtie \Delta P^{(k)}(SV,PV), \\ \Phi^{(k+1)} &= \Phi^{(k)} \cup \Delta \Phi^{(k)} \end{cases}$$
(2)

where $\Delta P^{(k)} = P^{(k+1)} - P^{(k)}$.

Example 4.1: Take $\Phi = R(x, z) \bowtie P(x, y)$ and rule $R(x, z), P(x, y) \longrightarrow P(x, z)$. Given a state I_k , when r fires, the set of tuples $\Delta P^{(k)}$ inserted into $P^{(k)}$ is such that $\Pi_{\{x\}} \Delta P^{(k)} \subseteq \Pi_{\{x\}} P^{(k)}$. By the third autonomy criteria. Φ is autonomous for P wrt the changes induced by r, and $\Phi^{(k+1)}$ can be easily computed using formula (2).

Remark however, that if r has a set-oriented semantics then the rule can only be fired once because after the first firing no new tuples can be inserted into P. Thus, maintaining $\Phi^{(k)}$ will not be profitable. On the other hand, if r has an instance-oriented semantics then r can be fired many times before reaching a fixpoint. Hence, maintaining $\Phi^{(k)}$ will be profitable. We shall elaborate on this point in Section 5.

4.2 Producer-filter Decomposition of an Expression

In this section, we make use of the notion of producer-filter view initially introduced in [Bry89]. We provide a different definition of a producer-filter and relate this notion to the previous concept of autonomous expression. We first use a motivating example.

Example 4.2: Take the expression:

$$\Phi_1 = A(x,y), B(y,z), C(x,u), \neg D(z,x), \neg E(z,y)$$

and suppose we have a set of changes C consisting of deletions from A, insertions into C that keep $\Pi_{\{C,1\}}C$ invariant, insertions into D, and insertions and deletions to E. According to the three autonomy criteria, Φ_1 is autonomous wrt all changes of C but deletions from E. Now, take formula:

$$\Phi_2 = A(x,y), B(y,z), C(x,u), \neg D(z,x)$$

 Φ_2 is clearly autonomous wrt to C. Suppose that T(x,y,z,u) is the relation defined by Φ_2 , and let us define $\tilde{T}(x,y,z,u,f_E)$ as: $(T \bowtie E) \times \{true\} \cup (T \supset \bowtie E) \times \{false\}$. The relation defined by Φ_1 is simply computed by $\Pi_{\{x,y,z,u,\}}(\sigma_{f_E=false} \tilde{T})$. Furthermore, when a tuple t is deleted from E then all tuples of \tilde{T} that match with t have their f_E attribute set to false.

Thus, maintaining relation \tilde{T} is easy when deletions to E occur and can be profitable to compute the relation defined by Φ_1 .

Definition 4.4 Let Φ be a (safe) conjunction of literals. Assume that $\Phi = \phi \wedge \psi$, where ϕ is safe and all ψ variables are bound by positive literals in ϕ . Then ϕ (resp. ψ) is said to be a *producer* (resp. a filter) for Φ , and (ϕ, ψ) is said to be a *producer-filter* decomposition.

Definition 4.5 Let (ϕ, ψ) be a producer-filter decomposition of a formula Φ . Let $\psi = (\neg)B_1(\vec{x}_1)$, ..., $(\neg)B_n(\vec{x}_n)$, and $T(A_1,...A_k)$ the relation defined by ϕ . We define the relation \tilde{T} with schema $\{A_1,...A_k\} \cup \{f_1,...,f_n\}$, where $Dom(f_i) = \{true, false\}$ as:

$$\tilde{T} = T \quad \overline{\bowtie} \quad B_1 \dots \quad \overline{\bowtie} \quad B_n$$

where kernetes the semi-outer join operator.

Intuitively, for each tuple t of T (the producer), there is a tuple in \tilde{T} that indicates whether t satisfies the condition of the filter (formula ψ).

Proposition 4.1 Let (ϕ, ψ) be a producer filter decomposition of Φ and \tilde{T} the associated relation. Let P be a predicate of Φ and C a set of changes. If either P occurs in ψ , or Φ is autonomous Φ for P wrt Φ then Φ is autonomous for P wrt Φ .

In the previous example, $(\Phi_2, \neg E)$ is a *producer filter* decomposition of Φ_1 which is autonomous wrt the set of changes we considered.

4.3 Algorithm to Compute Profitable Relations

We now characterize profitable relations and provide an algorithm that computes the maximal profitable relations from a given conjunction of literals.

Definition 4.6 A relation R is said Φ -profitable with respect to a set of changes C if:

- R is defined by a subexpression ϕ of Φ that is autonomous wrt C, or R is an autonomous relation associated with a producer-filter decomposition of Φ wrt C,
- no cartesian product is used to build R.

⁴ for a sake of simplicity we shall abusively use the word autonomous for a relation

Given a formula, there may be many profitable subexpressions but not all of them will be interesting to maintain. Take $\Phi = A(x,y)$, B(y,z), C(z,x), and assume that the set of changes C consists of insertions into A that keep $\Pi_{A,2}A$ invariant, deletions from B, and insertions into C that keep $\Pi_{C,1}C$ invariant. Then A, B, C, $A \bowtie B$, $B \bowtie C$ are all Φ -profitable subexpressions wrt C. Nevertheless, memorizing and maintaining all these relations is clearly not a good space-time compromise (although some implementations of RETE suggest to do it [SLR88]). Our algorithm only selects maximal relations. In our case, it will randomly choose to maintain either A and $B\bowtie C$, or C and $A\bowtie B$.

```
Maximal Profitable Relations Algorithm
   input: a safe conjunction of literals \Phi, and a set of changes \mathcal C
   output: A = a set of \Phi-profitable relations such that every operand relation belongs to
            only one expression;
   \mathcal{M} \leftarrow \emptyset; /* a set of autonomous expressions */
    build a connection graph \mathcal{G} where vertices are literals of \Phi and there is an edge
   between literals P_1 and P_2 if they have at least a variable in common;
   step 2:
   repeat
            P \leftarrow choose\_source(\phi, \mathcal{G}, \mathcal{C}):
            /* return a literal of \Phi that is non-marked in \mathcal{G}^*/
            mark P in G:
            g \leftarrow choose\_max\_subexpression(\mathcal{G}.\mathcal{C}.P.P);
            /* construct a maximal autonomous expression from P^*/
            \mathcal{M} \leftarrow \mathcal{M} \cup \{g\}:
   until all nodes of G with positive literals are marked:
   \mathcal{F} \leftarrow \{\text{unmarked literals in } \mathcal{G}\} \cup \{f \in \mathcal{M} \text{ s.t. } f \text{ is a singleton and there is some } p \text{ in } \mathcal{M} \text{ s.t.}
            (p,f) is a producer-filter decomposition of p \wedge f and its associated relation
            is autonomous wrt C };
   \mathcal{P} \leftarrow make\_producer(\mathcal{M}-\mathcal{F});
   /* an element of \mathcal{P} is a producer-filter decomposition (p, f) s.t. p is in \mathcal{M}-\mathcal{F} and f is
   initialized with 0. */
    for f in \mathcal{F} do
            (p, f') \leftarrow select\_producer-filter(f, \mathcal{P}, \mathcal{C});
            f'(p,f') \in \mathcal{P} s.t. (p,f) is a producer-filter decomposition and its associated relation
            is autonomous wrt C. When several elements of P are candidate, we choose
            the most selective one; if none p is randomly selected.*/
             if p exists then add f to f':
   od
   step 4:
   A \leftarrow 0;
    for (p, f) in \mathcal{P} do
           if f \neq \emptyset or p is not a single literal then add the relation associated with (p, f) to A;
   od
   returns A;
```

At Step 2 of the algorithm, we choose a node, called the source, in the predicate connection graph and then construct a maximal autonomous expression from this node. Note that there may

be several autonomous expressions that can be built from a given node. The heuristics used to choose the source and compute the *preferred* autonomous expression is detailed in Appendix A. In general, we are interested in the selectivity of a literal (some arguments can be constants) because we want to compute a profitable relation with the smallest size.

At the end of Step 2, \mathcal{M} contains a set of autonomous expressions but some nodes of \mathcal{G} may remain unmarked (negative literals). In Step 3, \mathcal{F} is constructed with potential filters to some autonomous expressions of \mathcal{M} . Each autonomous expression that is not in \mathcal{F} becomes a producer-filter decomposition in \mathcal{P} . Then, we try to integrate every literal of \mathcal{F} within the filter of some producer-filter decomposition in \mathcal{P} .

In the last step of the algorithm, we output relations that are associated with *interesting* producer-filter decompositions, i.e., those where the filter is not empty or the producer is not reduced to a single literal.

5 The COSMA Algorithm

5.1 Output Token Relations

Before presenting our algorithm we need to define specific relations, called *output token* relations, that play a key role in the computation of a rule program. Intuitively, given a rule r and a literal $l = (\neg)P(\vec{x})$ in its head, the output token relation associated with r and l records the net effect of r on the instance of P, for a particular database state. Such relations are essential because they enable to know if a rule is firable: at least one of its output token relations must be not empty. More, when a rule fires, output token relations serve to compute the effect of the rule.

The definition of an output token relation varies according to the semantics of rules.

Definition 5.1 Let r be a set-oriented rule, $l = (\neg)P(\vec{x})$ a literal in the head of r, and I a database state. The output token relation, noted OT(r,l), associated with r and l is the set of ground instances of P in $effect_r(I)$ that represent a net change to I(P).

For instance-oriented rules, the definition slightly differs because we have to identify to which satisfying rule instance is associated each tuple of OT. In fact, every tuple in the relation defined by the body of a rule, represents a satisfying instance of that rule. This is what we exploit in the next definition.

Definition 5.2 Let r be an instance-oriented rule, $l = (\neg)P(\vec{x})$ a literal in the head of r, and I a database state. Each tuple in OT(r,l) is the concatenation of two tuples, t and t' where t is a tuple in the relation defined by the body of r that corresponds to a satisfying instance r' of r, and t' is a ground instance of P in $effect_{r'}(I)$ that represents a net change to I(P).

5.2 Migration Flow of Data in a Program

As we mentioned before, our algorithm relies on the knowledge of the changes to any predicate that are induced by the program at a particular point in time. Extracting this knowledge from a rule program requires to perform a careful analysis of the migration flow of data within the rule program. Because, we assume statically-defined priorities between rules, this analysis can be done statically.

In order to capture the migration flow of data, we construct a labelled directed graph \mathcal{I} called an *Influence graph*. Rules are the vertices of \mathcal{I} and there is an arc from r to r' if there are predicates occurring in the head of r that also occur in r'. In the following, we say that r has an *influence* over r'. The label associated with (r,r') is a set of expressions of the form l θ l' where l (resp. l') is a literal of the head of r (resp. head of r') and θ is in $\{+,-\}$. The expression l+l' (resp. l-l') means that when r fires, its effect wrt l has for consequence to add (resp. to remove) tuples into (resp. from) OT(r,l').

Example 5.1: Consider the following program Γ :

Table 5.1 below represents the Influence graph of program Γ :

	r_1	r_2	r_3	r_4
r_1		$\{C+D\}$	$\{C + \neg C\}$	$\{C + \neg A, C + F\}$
r_2		$\{D+D\}$	$\{D-D,D-\neg C\}$	$\{D+\neg A,D+F\}$
r_3	$\{\neg C + C\}$	$\{D+D\}$	$\{D-D,D-\neg C\}$	$\{\neg C - \neg A, C - F, D + \neg A, D + F\}$
r4	$\{\neg A - C\}$			$\{\neg A - \neg A, \neg A - F, F + \neg A, F + F\}$

Table 5.1: Influence graph of F

Definition 5.3 Let \mathcal{I} be the influence graph of a program Γ and $r_0r_1\cdots r_n$ a path in \mathcal{I} . If there exists a sequence $(l_0\ \theta_0\ l_1)(l_1\ \theta_1\ l_2)\dots(l_{n-1}\ \theta_{n-1}\ l_n)$ where $(l_i\ \theta_i\ l_{i+1})$ is an expression in the label of (r_i,r_{i+1}) , then this sequence is said to be a propagation path from r_0 to r_n . If for each $i\in\{0,\dots,(n-1)\}$, $\theta_i=+$, then the propagation path is positive. If $\theta_{n-1}=-$, then the propagation path is negative.

The priority ordering between rules enables to simplify an influence graph by removing some labels. Assume for instance that r_1 , r_2 and r_3 have priority over r_4 in the previous example. Rule r_4 can only be fired when no other rule is firable. Since $OT(r_4, \neg A)$ has not yet been computed any firing of r_1 , r_2 and r_3 has no effect on $OT(r_4, \neg A)$. Furthermore, if r_4 fires, neither r_1 or r_2 or r_3 becomes firable. Thus, r_4 has no effect on $OT(r_1, C)$. Hence, the labels of the arcs (r_1, r_4) , (r_2, r_4) , (r_3, r_4) and (r_4, r_1) are irrelevant and can be discarded, thereby changing the propagation paths in \mathcal{I} . This is formalized below.

Definition 5.4 Let (Γ, \leq) be a program, \mathcal{I} its influence graph, and $p = l \theta l'$ an element of the label of (r, r'). Then p is relevant iff

- r and r' are not comparable wrt \leq , or
- r' has priority over r and p is a positive propagation path from r to r', or
- r has priority over r' and there exist a rule r'' that has not priority over r' and a positive propagation path, p', from r'' to r, such that p' p is a propagation path from r'' to r'.

Irrelevant portions of the labels can be discarded from the influence graph. To illustrate, Table 5.2 represents the Influence graph of (Γ, \leq) where irrelevant label expressions have been discarded.

	r_1	r_2	r_3	
r_1		$\{C+D\}$	$\{C + \neg C\}$	
r_2		$\{D+D\}$	$\{D-D,D-\neg C\}$	
<i>r</i> ₃	$\{\neg C + C\}$	$\{D+D\}$	$\{D-D,D-\neg C\}$	
r_4				$\{\neg A - \neg A, \neg A - F, F + \neg A, F + F\}$

Table 5.2: Simplified Influence Graph

5.3 The Algorithm

Given a program (Γ, \leq) , with either an instance-oriented or a set-oriented semantics, COSMA is a one-pass algorithm which produces for each rule, which relations should be materialized, how to compute these relations and how to differentially maintain them.

COSMA incrementally builds an influence graph and simultaneously computes the relevant label expressions. When all the labels of the edges ending at some rule r are fully computed, the influence graph provides the necessary knowledge about the possible set of changes, say C, to the predicates occurring in r. Then, r is annotated with two specific sets noted Effect and Subexp using the $Annotate_Rule$ algorithm.

COSMA Algorithm:

```
input: a program (Γ, ≤) with a set-oriented or instance-oriented semantics;
output: Γ where each rule has been annotated;
Step 1:
I ← ∅;
/* Initialisation of the influence graph */
Step 2:
while there exists a non annotated rule in Γ do
M ← {r ∈ Γ s.t. ∀ r' ∈ Γ if r' has priority over r then r' is annotated}
for r in M do
N ← { rules that have an influence over r };
for r' in N do
expand I with edge (r', r);
compute the relevant label expressions of (r', r);
od;
Annotate_Rule (I, r);
od;
od;
```

An element of Subexp is a pair $(E, \partial E/\partial C)$ such that E is a subexpression of the expression associated with OT(r, l), for some l in the head of r, and $\partial E/\partial C$ denotes the differential expression that incrementally maintain the relation defined by E wrt a set of changes C. All the relations defined by the E-expressions of Subexp will be materialized. A differential expression consists itself of a pair $(\partial E^+/\partial C, \partial E^-/\partial C)$, where the first (resp. second) element computes tuples that must

be added (resp. deleted) to the relation defined by E, say T. If no insertions (resp. deletions) can occur to T then the first (resp. second) element is said to be *undefined*.

For every literal l in the head of r, there is a triple $(E, \partial E/\partial C, \text{Mat})$ in Effect. In each triple, E represents the expression that computes OT(r,l) in terms of the materialized relations defined in Subexp and other (non-materialized) relations. If OT(r,l) is materialized then $\partial E/\partial C$ is the differential expression that maintains OT wrt C. In this case, the differential will consist of a pair $(\partial E^+/\partial C, \partial E^-/\partial C)$ as we mentioned before. Otherwise, $\partial E/\partial C$ is the expression that computes the new value of OT in terms of the differential changes to its operand relations. Here, the differential consists of a single expression. Finally, Mat is a boolean that indicates if OT(r,l) is materialized.

- Steps 2 and 3 of the Annotate_Rule algorithm compute Subexp. Given a rule r and a literal l in its head, our algorithm uses the following simple rule to decide which subexpressions should be computed in Subexp.
 - R1. If OT(r, l) is not autonomous wrt C then memorizing maximal OT(r, l)-profitable relations is useful.

The rationale for this heuristic rule is that when OT(r,l) is not autonomous wrt C, OT(r,l) needs to be computed more than once whatever the semantics of the rule is. Thus, it is useful to memorize subexpressions that may speed up repetitive computations of OT(r,l).

- Step 4 of the algorithm computes the second part of the annotation, Effect. An important decision taken by the algorithm is to decide if an output token relation must be materialized. We use the following heuristic rule:
 - R2. If a rule r is instance-oriented then memorizing OT(r, l) is useful for every literal l in the head of r.

With instance-oriented rules, when a rule fires, only one instantiation, say r', i.e., one tuple of OT is used. Intuitively, the effect of the rule may have for consequence to add new instantiations in OT and/or to invalidate previous instantiations of OT. If OT is not materialized then it has to be entirely recomputed at each firing of r because the next instantiations cannot be computed solely in terms of r' and its consequences. Thus, OT represents the most recent computation that can be differentiated before the choice of an instantiation to fire. On the other hand, with set-oriented rules, the OT relations are emptied after each firing of the rule and hence there is no need to materialize them. Furthermore, for set_oriented rules, we have:

Proposition 5.1 Let (Γ, \leq) be a program with set oriented semantics, r a rule, $l = (\neg)P(\vec{x})$ a literal in the head of r. If the formula associated with OT(r,l) is autonomous wrt the changes to P induced by the program, then OT(r,l) will be computed once. Furthermore, if this is the case for every literal in the head of r, then r is fired at most once.

```
Annotate_Rule Algorithm:
   input: an influence graph I and a rule r;
   output: r is annotated with two sets: Effect and Subexp;
   Step 1:
        C \leftarrow \{\text{changes on predicates occurring in } r\};
         /* C is easily derived from I */
   Step 2:
         H \leftarrow \emptyset;
         /* H contains output token expressions which are not autonomous wrt C */
         for each literal l of the head of r do
             \Psi \leftarrow expression associated with OT(r, l):
             if \Psi is not autonomous wrt C then add \Psi to H;
         od ;
    Step 3:
         if H \neq \emptyset then
             if H is a singleton \{\Psi\} then \Phi = \Psi
             else \Phi = expression associated with the body of r;
             \mathcal{A} \leftarrow \text{Maximal\_Profitable\_Relation}(\Phi, \mathcal{C});
             Subexp \leftarrow \{(E, \partial E/\partial C) \text{ s.t. } E \in A\}:
         else Subexp - 0;
    Step 4:
         Effect \leftarrow \emptyset:
         for each literal l of the head of r do
             E = expression associated with OT(r, l) in terms of relations defined by expressions in Subezp;
             if r is instance_oriented then
                 calculate \partial E/\partial C for maintaining OT(r, l); Mat — true;
             else
                 Mat \leftarrow false:
                 if E is not autonomous wrt \mathcal C
                 then calculate \partial E/\partial C for computing the new value of OT(r,l)
                 else \partial E/\partial \mathcal{C} - \emptyset:
                     /* OT(r,l) is computed once only */
             add (E, \partial E/\partial C) to Effect:
         od:
```

5.4 An Example

We apply COSMA algorithm to the program (Γ, \leq) of section 5.2. We assume that rules are setoriented and that r_1 , r_2 and r_3 have priority over r_4 . The rule annotations returned by COSMA are as follows:

```
\begin{array}{c} r_1: \ \mathsf{Subexp}: \\ e1 = \Pi\{x,z\} (\ \sigma_{A.2=\alpha}A(x,.,y)) \bowtie (\sigma_{B.2=\beta}B(y,.,z)) \bowtie (\sigma_{E.3=\gamma}E(z,v,.)) \\ \neg \bowtie \ F(x,z) \ \bowtie \ C(x,z) \\ /^*\ T1 \ \mathsf{is} \ \mathsf{the} \ \mathsf{relation} \ \mathsf{defined} \ \mathsf{by} \ \mathsf{el}\ ^*/\\ \partial e1^+/\partial C = (\Pi_{\{x,z\}}\ T1 \ \bowtie \ \Delta^-C(x,z)) \times \mathsf{false} \\ \partial e1^-/\partial C = T1 \ \bowtie \ \Delta^-C(x,z) \end{array} Effect:
```

```
e2 = \Pi_{\{x,z\}}(\sigma_{f_C=false} e1)
                \partial e^2/\partial C = \Pi_{\{x,z\}} \Delta^+ T^1
       Materialize: false
r_2: Effect:
                e3 = \prod_{\{z,u,x\}} (C(x,y) \bowtie D1(y,z,u)) \neg \bowtie D2(z,u,x)
                \partial e3/\partial C = \prod_{\{z,u,x\}} (\Delta^+ C(x,y) \bowtie D1(y,z,u)) \supset \bowtie D2(z,u,x)
                \partial e3/\partial D = \prod_{\{z,u,x\}} (C(x,y) \bowtie \Delta^+ D1(y,z,u)) \supset \bowtie D2(z,u,x)
       Materialize: false
r_3: Subexp:
                e4=(\sigma_{B,3=\beta}(B(x,y,-)) \neg \bowtie (\sigma_{D,1=\delta} D1(-,y,x)) \bowtie E(z,u,x) \bowtie C(y,x)
                 /* T2 is the relation defined by e4 */
                  \partial e4^+/\partial C = (\Pi_{\{x,z\}} T2 \bowtie \Delta^+C(y,x)) \times true
                  \partial e4^{-}/\partial C = T2 \bowtie \Delta^{+}C(y,x)
       Effect:
                e5 = \Pi_{\{y,x\}}(\sigma_{f_C=true} T2)
                \partial e5/\partial C = \Pi_{\{y,x\}} \Delta^+ T2
                e6 = \prod_{\{z,x\}} ((\sigma_{B,3=\beta}(B(x,y,.)) \neg \bowtie (\sigma_{D,1=\delta} D1(.,y,x)) \bowtie E(z,u,x))
                          \neg \bowtie (\sigma_{D,2=\delta} D2(-z.x))
                \partial e5/\partial C = undefined
       Materialize: false
r_4: Effect:
                e7 = \prod_{\{y,t,x\}} (A1(x,y,z) \bowtie (\sigma_{D,1=\delta}D(-x,y)) \bowtie C(z,t) \bowtie F1(z,w)) \bowtie A2(y,t,x)
                e8 = \prod_{\{z,y\}} (A1(x,y,z) \bowtie (\sigma_{D,1=\delta}D(z,x,y)) \bowtie C(z,t) \bowtie F1(z,w)) \neg \bowtie F2(z,y)
       Materialize: false
```

In Figure 3, we represent the discrimination network for every output token relation associated with a rule of program. In each diagram, there is one input node per literal in the rule and one output token relation. Circle boxes denote relational expressions, square boxes denote materialized relations, and other nodes denote non-materialized relations.

Take rule r_1 , the only changes on its predicates consist of deletions from C according to the influence graph of table 5.2. The expression associated with $OT(r_1, C)$ is $\Psi = A(x,\alpha,y)$, $B(y,\beta,z)$, $E(z,v,\gamma)$, $\neg F(x,z)$, $\neg C(x,z)$. Step 2 of the Annotate-Rule algorithm detects that Ψ is not autonomous wrt deletions in C. Step 3 computes the maximal OT-profitable relations wrt changes to C and returns the relation defined by e1 which is the relation associated with the producer-filter decomposition of $\Psi((A(x,\alpha,y), B(y,\beta,z), E(z,v,\gamma), \neg F(x,z)).(\neg C(x,z)))$. Then $\partial e1^+/\partial C$ and $\partial e1^-/\partial C$ are computed. Next, Step 4 proceeds. Since the rule is set-oriented, its output token relation is not materialized. The expression that computes the initial value of $OT(r_1, C)$ in terms of T1 (the relation defined by e1) is calculated and yields e2.

Subsequent values of $OT(r_1, C)$ are then computed in terms of T1 and Δ^-C using $\partial e2/\partial C$, where Δ^-C represents the delta relation containing deletions to C that occurred since last firing of r_1 . When deletions occur in C, they are propagated to T1. Deletions to T1 are directly performed to T1 while insertions to T1 are recorded separately into Δ^+T1 . In fact Δ^+T1 is a delta relation, in the sense of [SKdM92], representing the net additions to T1.

For rule r_1 , only one delta relation has to be maintained: Δ^-C . Similarly, for the other rules, our algorithm enables to detect which delta relations are necessary to maintain. In addition to

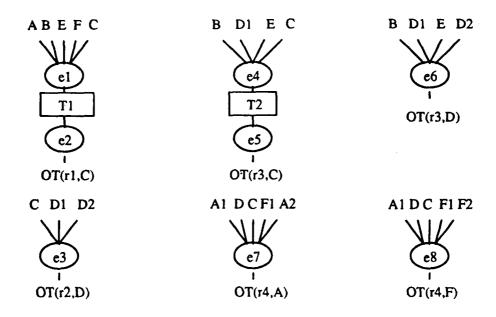


Figure 3: Discrimination network for rules of example 5.1

enable an incremental computation of the rules, these relations play the role of logs. Indeed, delta relations enable to implement a deferred update strategy for processing the rules. The idea is that updates to the input level of a rule network can be logged into delta relations and their propagation into the network can be delayed until the rule is tried to fire. As shown in [Rou91], deferred update strategies can be very effective for incremental evaluation of relational expressions.

6 Related Work

A few incremental algorithms have been proposed to evaluate production rules in a database system. The A_TREAT algorithm [Han92] is derived from TREAT and assumes that rules are set-oriented. DBCond [SLR90] is derived from RETE and also assumes that rules are set-oriented. Finally, Rule Materialization in [SZ91] is also derived from RETE but does not make any assumption on the semantics of rules. In the following, we compare these algorithms with our COSMA algorithm.

A_TREAT [Han92] uses a TREAT-like discrimination network to record the result of matching rule bodies against the database. However, in order to save memory space, A_TREAT only memorizes the results of selection predicates in α _memory nodes when the selectivity of the selection is high. If the selectivity the selection is low, A_TREAT replaces the corresponding α _memory by a virtual α _memory where it memorizes the selection predicate of the node instead of the result of the selection itself. When a set of changes is performed to some relation R, the changes are filtered through the discrimination network. Joins occurring in rule bodies are processed with the α _memory nodes. For virtual α _memory nodes, joins are processed with the input relations to which the selection predicates are applied. The relation defined by a rule body is ultimately materialized and used to compute the actions of the rule. When a rule is fired, this relation is emptied and recomputed in terms of the input nodes and their differential changes. Much attention has been devoted to the efficient calculation of the new value of the relation defined by a rule body by taking advantage of

the query optimizer and the use of attribute indexes. On the other hand, our algorithm focuses on choosing which appropriate discrimination network should be built. With regard to this problem A_TREAT only question the profitability of maintaing a selection node based on its selectivity.

DBCond [SLR90] maintains a RETE discrimination network into a flattened data structure. Take a rule $r: A(x, \alpha, z), B(x, y, \beta), C(\gamma, y, z) - head$, and relations $A(A_1, A_2, A_3), B(B_1, B_2, B_3)$ and $C(C_1, C_2, C_3)$. Then, DBcond will maintain one relation per literal in the body of r, called COND relations. For instance, COND - A will contain the projections $\Pi_{B_1}(B)$ and $\Pi_{C_3}(C)$, as well as the projection on B_1 and C_3 of tuples in the join between B and C. The main feature of this algorithm is that when a change occurs to A then COND - A suffices to determine if rule r is firable (although it does not compute the effect of the rule). However, all affected COND-relations have to be maintained upon a change to A (in our case, COND - B and COND - C relations). Thus, the space-time tradeoff pointed out earlier in this paper applies exactly as for RETE. Our algorithm is able to choose a better discrimnation network which could then be implemented using the DBCond technique.

In [SZ91], the authors propose an efficient technique to materialize the relation defined by a rule body. Suppose that the rule body is an expression: $E = Q_1 \bowtie \cdots, \bowtie Q_n$. Then the relation, say T, defined by E has one attribute for every surrogate attribute of Q_i plus all Q_i -join attributes that occur in E. The result of every intermediate join is stored into T. For instance, the result of the join between Q_1 and Q_2 will yield tuples in T where the value of every attribute that is neither a Q_1 or Q_2 surrogate attribute or a join attribute between Q_1 and Q_2 is a null value. It is worth noting that such a relation is autonomous wrt any change to the Q_i 's. Here again, our algorithm can be used to reduce the size of T by retaining only those intermediate results that are profitable to maintain.

In order to compare COSMA with the other algorithms in more concrete terms, we consider again rule r_1 of the previous example in Section 5.4. Incremental algorithms that are derived from RETE, such as DBCond and Rule Materialization, would materialize the following data in the discrimination network of r_1 : $f_1 = \prod\{x,y\}$ ($\sigma_{A,2=o}A(x,-,y)$), $f_2 = \prod\{x,z\}$ ($\sigma_{B,2=\beta}B(y,-,z)$), $f_3 = \prod\{z,v\}$ ($\sigma_{E,3=\gamma}E(z,v,-)$), $f_4 = f_1 \bowtie f_2$, $f_5 = f_2 \bowtie f_3$, $f_6 = f_1 \bowtie f_2 \bowtie f_3$, $f_7 = f_1 \bowtie F(x,z)$, $f_8 = f_2 \bowtie F(x,z)$, $f_9 = f_3 \bowtie F(x,z)$, $f_{10} = f_4 \bowtie F(x,z)$, $f_{11} = f_5 \bowtie F(x,z)$, Even if these data are stored in a compact form (e.g., in a flattened data structure or a single specific relation), too many data are retained.

On the other hand, A_TREAT would only retain f1, f2, and f3 in the discrimination network if their selectivity is high, plus the relation associated with the body of r_1 . Thus, $\Delta C \bowtie f1 \bowtie f2 \bowtie f3 \bowtie F(x,z)$ will have to be recomputed every time the rule is fired.

7 Conclusions

We have presented an original adaptive algorithm that takes as input a program of rules and returns a discrimination network representing a expected good space-time compromise. The discrimination network is then used to perform an incremental evaluation of the rule program. In order to decide if a subexpression must be materialized as a node in the discrimination network, our algorithm analyzes two main factors:

1. the ability to efficiently compute the differential change to this node, given the net changes to its predecessor nodes induced by the rule program,

2. the *profitability* of maintaining a node in the network for speeding calculations that will follow its materialization.

Our algorithm works for set-oriented and instance-oriented rules which are the two most common kinds of rules used in database rule languages. More, it is clear from the presentation of the algorithm that it can be adapted to many variants of rule language semantics such as the use of refraction and timestamps.

We believe that our algorithm fills a hole in the literature on incremental algorithms for production rule languages in databases. As we said before, most algorithms are derived either from RETE or TREAT. Specific implementation techniques have been designed to efficiently process a RETE or TREAT discrimination network, but we are not aware of any previous work that questioned the pertinence of building a RETE or TREAT network. Our algorithm does so and capitalizes on various database algorithms, in particular in the area of maintenance of materialized views. Our work was also inspired by algorithms developed in the framework of high-level programming languages, and particularly [FU76], [PK82], [RF87].

We consider the algorithm presented in this paper as a first step. We wish to implement it in the framework of the A-RDL active database system ([SKdM92]) and perform real measurements. Doing this, we will integrate implementation techniques for discrimination networks such as those of [SZ91] or [Han92].

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Appendix

```
choose_source Algorithm
   input: a conjunction \Phi, its predicate connexion graph \mathcal{G}, and a set of changes \mathcal{C};
   output: P = a positive literal of \Phi st its vertex is not marked in \mathcal{G};
   let P denote an unmarked positive literal;
   let C_{\mathcal{P}} denote the set of changes to P in C;
   apply the ordered list of statements until one P is found:
         /* searches for an invariant wrt C */
         1. return the most selective P (henceforth, m.s.) s.t. C has no effect on P;
         /* seek for a literal whose defined relation is stable on some attributes */
         2. return m.s. P s.t. \Phi is autonomous for P wrt \mathcal{C}_{\mathcal{P}} by 3^{rd} autonomy criterium;
         /* seek for a literal whose defined relation can only decrease due to C */
         3. return m.s. P s.t. \Phi is autonomous for P wrt \mathcal{C}_{\mathcal{P}} by 1^{st} autonomy criterium;
         4. return m.s. P s.t. \Phi is autonomous for P wrt \mathcal{C}_{\mathcal{P}} by any criteria;
         5. return m.s. P;
choose_max_subexpression Algorithm
    input: a conjunction \Phi, its predicate connexion graph \mathcal{G}, a set of changes \mathcal{C}, P a literal of \Phi, and
        g an autonomous expression wrt \mathcal{C}:
    output: g = an autonomous expression wrt C:
        /* the literals of g are marked in \mathcal{G} */
    if P is positive then
        compute \mathcal{V}_{\mathcal{P}} = \{\text{unmarked literal V st V node is connected to } P \text{ in } \mathcal{G} \text{ and } g \land V \text{ is} \}
           autonomous wrt C;
        while V_P \neq \emptyset do
        1. choose an adjacent vertex V in \mathcal{V}_{\mathcal{P}}:
           let C_{\mathcal{V}} denote the set of changes to V in \mathcal{C}:
           apply the ordered list of statements until one V is found:
               1. return negative V s.t. C has no effect on V:
               2. return m.s. positive V s.t. C has no effect on V;
               3. return m.s. V s.t. \Phi is autonomous for V wrt C_V by 2^{nd} autonomy criterium;
               4. return m.s. V s.t. \Phi is autonomous for V wrt \mathcal{C}_{\mathcal{V}} by 1^{st} autonomy criterium;
               5. return m.s. V s.t. \Phi is autonomous for V wrt C_{\nu} by 3^{rd} autonomy criterium;
               6. return m.s. V;
        2. extend g with V and mark V;
        3. visit G from V and expand g:
           g \leftarrow g \land choose\_max\_subexpression (\Phi, \mathcal{G}, \mathcal{C}, V, g);
           update V_{\mathcal{P}} according to g;
        od
    endif
    return g;
```



Unité de Recherche INRIA Rocquencourt Domaine de Voluceau - Rocquencourt - B.P. 105 - 78153 LE CHESNAY Cedex (France)

Unité de Recherche INRIA Lorraine Technopôle de Nancy-Brabois - Campus Scientifique
615, rue du Jardin Botanique - B.P. 101 - 54602 VILLERS LES NANCY Cedex (France)
Unité de Recherche INRIA Rennes IRISA, Campus Universitaire de Beaulieu 35042 RENNES Cedex (France)
Unité de Recherche INRIA Rhône-Alpes 46, avenue Félix Viallet - 38031 GRENOBLE Cedex (France)
Unité de Recherche INRIA Sophia Antipolis 2004, route des Lucioles - B.P. 93 - 06902 SOPHIA ANTIPOLIS Cedex (France)

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