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# UNITÉ DE RECHERCHE INRIA-ROCQUENCOURT

Institut National de Recherche en Informatique et en Automatique

Domaine de Voluceau
Rocquencourt
B.P.105
78153 Le Chesnay Cedex
France
Tél.(1) 39 63 5511

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# BASILE-MAPLE INTERFACE: A LINK BETWEEN CACSD PACKAGE AND COMPUTER ALGEBRA SYSTEM

Claude GOMEZ
Georges LE VEY
Christine ROUGERIE

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BASILE-MAPLE Interface: a Link between CACSD Package and Computer Algebra System

Interface BASILE-MAPLE : Un lien entre système de CAO pour l'automatique et système de calcul formel

Claude Gomez\*

Georges Le Vey<sup>†</sup>

Christine Rougerie<sup>‡</sup>

<sup>\*</sup>Projet META2, INRIA, Domaine de Voluceau, Rocquencourt, B.P. 105, 78153 Le Chesnay Cédex, France. †SIMULOG S.A., 1 rue James Joule, 78182 Saint Quentin en Yvelines Cédex, France.

<sup>&</sup>lt;sup>‡</sup>IBSI, 122 Avenue de Hambourg, 13008 Marseille, France.

#### Abstract

BASILE is a CACSD package of great efficiency for numerical computations. On another hand, automatic control is a field in which a lot of mathematical objects have to be manipulated in a symbolic way. For that, powerful computer algebra systems such as MAPLE exist. We describe in this paper an interface between BASILE and MAPLE, allowing various data communication and combining in this way the respective powerfulness of numerical and symbolic computations.

#### Résumé

BASILE est un système de CAO pour l'automatique qui réalise principalement des calculs numériques. Pour résoudre les problèmes d'automatique, il est très souvent nécessaire d'effectuer des manipulations symboliques. Le but de l'interface présentée est de relier numérique et symbolique en permettant l'échange de données entre BASILE et le système de calcul formel MAPLE. Ainsi, l'utilisateur a la possibilité de mélanger la puissance du calcul symbolique et l'efficacité du calcul numérique.

#### 1 Specifications

#### 1.1 Introduction

BASILE (see [1]) is a CACSD package, essentially doing numerical computations. However, in many cases, one needs to do some symbolic computations, particularly in automatic control but also while dealing with general mathematical quantities, exact differentiation or integration. We will show, through a few examples, how such needs appear when trying to solve problems with BASILE. Among the numerous implications of computer algebra towards numerical purposes, let us mention first the symbolic differentiation as one of major interest for BASILE. Another interest, as we shall see in the sequel, is the possibility to automatically generate numerical codes (FORTRAN, C) from a formal description of dynamical systems, for simulation purposes (for example see [2]). We use MAPLE as the computer algebra system.

#### 1.2 Examples

We present now some practical examples, and we will identify which data must be transferred between BASILE and MAPLE.

#### 1.2.1 Example 1: derivative computation

BASILE knows how to numerically integrate explicit or semi-explicit differential systems. For that, the user must supply, through a FORTRAN program or a BASILE macro, the right member of the system under study. Moreover, it may be of interest to simultaneously give the derivative of the function with respect to the state vector (the jacobian matrix). Of course, such computations may be derived by hand but it is quite obvious that with a dozen of equations and variables, the preceding computations become tedious and always need precise verifications, for the symbolic manipulations and while writing the numerical code. So, we would like to use a computer algebra system for such derivative computations. Such computations appear in optimal control problems too, to calculate the gradient of a functional with respect to the control, by the state adjoint method. In such situations, we would like to transfer BASILE macros to MAPLE and to load a BASILE macro after processing by MAPLE. Let us give a simple example.

Suppose we have loaded into BASILE the macro describing the following function:

$$f(x) = \sin(x_1 + x_2) - 3(x_1x_2 + e^{x_3})/(x_2 + x_3)$$

The corresponding BASILE macro is the following:

```
//<f>=f(x)
f=sin(x(1)+x(2))-3*(x(1)*x(2)+exp(x(3)))/(x(2)+x(3));
//end
```

As we mentioned previously, all the computations could be done by hand, or derived separately with MAPLE; we could have written then the desired BASILE macro. Nevertheless, an automatic procedure would be of great value for bigger applications. In the example, we want to transfer the body of the BASILE macro to MAPLE, do symbolic differentiation of the function and load into BASILE the macro giving the derivative:

```
//<out>=grad(x) 
out=\cos(x(1)+x(2))-3*x(2)/(x(2)+x(3)),\cos(x(1)+x(2))-3*x(1)/(x(2)+x(3)...)
))+3*(x(1)*x(2)+exp(x(3)))/(x(2)+x(3))**2,-3*exp(x(3))/(x(2)+x(3))+3*(...x(1)*x(2)+exp(x(3)))/(x(2)+x(3))**2>
//end
```

#### 1.2.2 Example 2: change of variables

Change of variables is a frequent operation while dealing with mathematical problems. For example it may occur in order to reduce the size of a system or to give a better condition number. BASILE does not know how to do such an operation, except for a limited class of data. On the other hand, it is very easy to perform it with MAPLE. In that case, the data we want to transfer to MAPLE is again the body of a BASILE macro (description of a system of equations). Then the desired substitutions are done with MAPLE and we want to get a new BASILE macro describing the system after the relevant change of variable.

The following system describes the evolution of a simple planar pendulum in a normal coordinates system.  $\lambda$  is the tension of the pendulum, L is the length of the pendulum and g is the gravitational constant.

$$\begin{aligned}
 \dot{x}_1 &= x_2 \\
 \dot{x}_2 &= -\lambda x_1 \\
 \dot{x}_3 &= x_4 \\
 \dot{x}_4 &= -\lambda x_3 - g \\
 0 &= x_1^2 + x_3^2 - L^2
 \end{aligned}$$

It is well known that eliminating the constraints leads to the following system of equations:

$$\dot{\phi}_1 = \phi_2 
\dot{\phi}_2 = g/L \sin \phi_1$$

where:

$$x_1 = L\sin\phi_1$$

$$x_3 = -L\cos\phi_1$$

The BASILE macros describing the two systems are as follows:

For the first system:

```
//<res>=chvar(t,x,xd)
r=-xd(1)+x(2);
r=<r;-xd(2)-lambda*x(1)>;
r=<r;-xd(3)+x(4)>;
r=<r;-xd(4)-lambda*x(3)-g>;
//end
    For the second system:
//<phid>=chvar2(t,phi)
phid(1)=phi(2);
phid(2)=g/l*sin(phi(1));
//end
```

Starting from the first as input, we want the second as an output. This example is similar to that in 1.2.1, as far as the data to be transferred between BASILE and MAPLE are concerned. Only the symbolic manipulations change.

#### 1.2.3 Example 3: analytical expression of integrals or solution of particular O.D.E's

In a number of situations, it may be useful to get the exact expression of an indefinite integral. If a program evaluates a great number of times such an integral, much computing time may be saved as opposed to the numerical evaluation of the integral each time. Another interesting application is the exact solution (when it exists) of some differential equations or systems of equations, for example through the Laplace Transform. In such situations, the data to be transferred are again macros, for the description of the function to integrate or the equation to solve.

#### 1.2.4 Example 4: unknown data types in BASILE

Suppose you want to study a transfer matrix  $\frac{p_{ij}(s)}{q_{ij}(s)}$ , depending on a formal parameter  $\alpha$ . This data type does not exist in *BASILE*. We could plot a parameterized Bode plot the following way. First, let us compute  $\frac{p_{ij}(s)}{q_{ij}(s)}$  as a function of  $\alpha$  in MAPLE; in a second step, we can compute and plot the frequency response in *BASILE*. In that case, the data to be transferred is a list that gives the rational matrix (remember that rational matrices are given as lists in *BASILE*).

#### 1.3 Conclusion

The preceding examples allow the distinction of:

• Several data types that we need to transfer from BASILE to MAPLE:

macros
polynomials or lists representing rationals
numerical data (scalars, vectors, matrices).

• Several ways to get back the relevant information into BASILE:

macros to load into BASILE (mainly for non linear functions description) polynomials or rationals (BASILE lists) numerical data (scalars, vectors, matrices).

As we can see from this list, all the essential data types of BASILE are to be transferred to MAPLE.

### 2 User's Guide

#### 2.1 Main features

In the sequel, the data transfer between the two packages BASILE and MAPLE will be held through files, transparently for the user.

For a comfortable use, the user should activate BASILE and MAPLE simultaneously on his workstation, with his favorite window manager. The two processes run each in a window. But a sequential use of the two processes is possible too when no multiple window terminal is available.

The following BASILE functionalities are given to the user:

tomaple to send data to MAPLE

frmaple to get data from MAPLE.

The following MAPLE functionalities are given to the user:

tobasile to send data to BASILE

frbasile to get data from BASILE.

The precise definitions of those functions are given hereunder.

#### 2.2 Main functions of the interface

#### 2.2.1 BASILE Functions

tomaple(var, string) takes a BASILE variable var as input and writes its MAPLE syntax translation into a temporary file. string is a character string.

If the BASILE variable var is the name of a BASILE macro, a MAPLE procedure with string as its name and the MAPLE syntax translation of the macro as its body is generated. Else, a MAPLE variable with string as its name and the value of the BASILE expression as its value is generated.

MAPLE expressions generated this way may be loaded into MAPLE by the MAPLE command frbasile(). The temporary file is destroyed after the execution of this command.

Successive calls to the function tomaple are possible, allowing several expressions to be stored in the temporary file. Each activation of frbasile() destroys the temporary file.

frmaple() loads BASILE macros generated by tobasile() from MAPLE and destroys the corresponding temporary file.

clmaple() destroys the temporary file where BASILE to MAPLE translations have been stored.

A complete description appears in table 1.

#### 2.2.2 MAPLE Procedures

tobasile(exp,name{,arglist}) takes as input a MAPLE expression exp (it may be a procedure name) and writes the BASILE macro translation into a temporary file. The argument name is the name of the generated BASILE macro. The argument arglist is the argument list of the BASILE macro and is optional. If arglist is not given and exp is a procedure name, the arguments of the BASILE macro and those of the procedure are the same, else the argument list of the BASILE macro is empty.

The BASILE macros generated may be loaded into BASILE with the BASILE command frmaple(). The temporary file is destroyed with the activation of this command.

Successive calls to the function tobasile are possible, allowing several BASILE macros to be stored in the temporary file. Each activation of frmaple() destroys the temporary file.

frbasile() reads in MAPLE expressions generated with the commands tomaple() from BASILE and then destroys the corresponding temporary file.

clbasile() destroys the temporary file where MAPLE to BASILE translations have been stored.

basile(exp,file,{,arglist}) takes a MAPLE expression exp as input (it may be a procedure) and translates it into BASILE syntax.

This supplementary procedure gives the possibility of adding new functionalities for translating MAPLE expressions into BASILE; but, strictly speaking, it is not part of the interface.

```
Expression to be translated: a=1+x**2

• tomaple(a,'a');
    Contents of the temporary file:

a := 1+x*(x) ;

Loading into MAPLE with: frbasile()

Macro to be translated: deff('<out>=f(x)','out=x+log(x)')

• tomaple(f,'f');
    Contents of the temporary file:

f := proc(x)
    out :=(x+log(x));
    out;
    end;

Loading into MAPLE with: frbasile()
```

Table 1: Translating BASILE expressions into MAPLE

This procedure is able to treat several cases.

If exp is a MAPLE procedure name, the translation results in a BASILE macro. If the argument file is terminal, the macro definition (using the BASILE function deff) is printed on the terminal screen. If the argument file is different from terminal, a macro with name file, is written into the file file. This BASILE macro may then be loaded into BASILE with the BASILE command getf. The argument arglist is the argument list of the BASILE macro and is optional. When omitted, the arguments of the BASILE macro are those of the procedure.

If exp is a MAPLE expression and if the argument file is terminal, the BASILE syntax translation of the expression is printed on the terminal screen. If the argument file is not terminal, a BASILE macro with file as its name and the BASILE syntax translation of the MAPLE expression as its body is written into a file with file as its name. This BASILE macro may then be loaded into BASILE with the BASILE command getf. The argument arglist is the argument list of the BASILE macro. When omitted, the BASILE macro has an empty argument list.

While entering the command basile(exp,terminal), we can decide to store the result in a file and then to load the translated expression into BASILE with the BASILE command exec. This is obtained with the following sequence of MAPLE commands:

```
writeto(file);
basile(exp,terminal);
writeto(terminal);
```

All the preceding functionalities are summarized in tables 2 and 3. One simple way of doing things is to use tobasile solely.

#### 2.3 Types of translated expressions

Table 4 shows which expressions the interface can translate.

In this paragraph, we describe some of the limitations of the BASILE -MAPLE interface and we introduce the new MAPLE function &ev.

#### 2.3.1 Translating from BASILE to MAPLE

Presently, the interface does not know how to translate BASILE control structures (loops, conditional expressions). Moreover, it translates the BASILE expression a(...) into a(...), because it has no means to distinguish between a functional expression and an element of a matrix. These limitations will be relaxed in the next version of the interface.

#### 2.3.2 Translating from MAPLE to BASILE

MAPLE procedures are translated as such into BASILE macros. The interface considers that the name of the output variable is out. A user must define explicitly out as output variable for a correct execution of the generated macro (see the examples in section 3). Only one value may be returned from a MAPLE procedure, so if multiple values are needed, a list of the relevant values has to be returned from the procedure and this list is translated into a BASILE list.

```
Expression to be translated: a:=1+x^2;
   • tobasile(a,'a');
     Contents of the temporary file:
     //<out>=a ()
     out=1+x**2
     //end
     Loading into BASILE with: frmaple()
   • tobasile(a,'a',[x]);
     Contents of the temporary file:
     //<out>=a (x)
     out=1+x**2
     //end
     Loading into BASILE with: frmaple()
  • basile(a,toto);
     Contents of the file toto:
     //<out>=toto()
     out=1+x**2
     //end
     Loading into BASILE with: getf('toto')
  • writeto(toto); basile(a, terminal); writeto(terminal);
     Contents of the file toto:
     1+x**2
     Loading into BASILE with: exec('toto')
```

Table 2: Translating MAPLE expressions into BASILE

```
Procedure to be translated: f:=proc(x,y) local out; out:=y+log(x) end;
   • tobasile(f,'f');
     Contents of the temporary file:
     //<out>=f(x,y)
     out=y+log(x),
     //end
     Loading into BASILE with: frmaple()
   tobasile(f,g,[x]);
     Contents of the temporary file:
     //<out>=g(x)
     out=y+log(x),
     //end
     Loading into BASILE with: frmaple()
   • basile(f,toto);
     Contents of the file toto:
     //<out>=f(x,y)
     out=y+log(x),
     //end
     Loading into BASILE with: getf('toto')
   writeto(toto);basile(f,terminal);writeto(terminal);
     Contents of the file toto:
     deff('<out>=f(x)',<'out=x+log(x),'>)
     Loading into BASILE with: exec('toto')
```

Table 3: Translating MAPLE procedures into BASILE

#### $MAPLE \iff BASILE$

integer, float, complex numbers constants  $\pi$ , e, i algebraic expressions matrices, arrays, indexed names lists trigonometric functions

# $MAPLE \Longrightarrow \overline{BASILE}$

functions of linalg package:
 add, inverse, multiply, transpose
in the body of procedures:

if with boolean expressions (comparison
 operators, true, false, and, or, not)
for except the for in form
 special function &ev
evalm is not translated

#### $BASILE \Longrightarrow MAPLE$

macros defining no matrix expressions in the body of these macros:

operators +, \*, -, /, \, \*\*
trigonometric functions
if, for and select are not translated
strings are not translated

Table 4: Expressions translated by the interface

x

#### 2.3.3 The MAPLE function &ev

The function **&ev** is a new MAPLE function created for the needs of the interface. When used in a MAPLE procedure, it replaces its argument (which must be a variable name) by the evaluation of its name. This functionality is very useful when an expression is defined in MAPLE and we want to use it inside a generated BASILE macro.

We show hereunder an example of its use.

The following MAPLE program will be translated into a BASILE macro in which the array a is multiplied by n!. The array a is introduced into the BASILE macro with the help of &ev(a).

```
with(linalg):
a:=array([[expand((1+x)^10),x],[1-x,2-x^2]]);
f:=proc(n,na)
  local fac;
  fac:=1;
  for i to n do fac := fac*i od;
  out := &ev(a);
  out := fac * out;
end;
   After loading into MAPLE, we get the following in BASILE:
 <>frmaple()
 <>disp(f);
<out>=f(n,na)
fac=1,
for i=1:1:n,
fac=fac*i,
end,
out=<1+10*x+45*x**2+120*x**3+210*x**4+252*x**5+210*x**6+120*x**7+45*x**8+10*x**9
+x**10,x;1-x,2-x**2>,
out=fac*out,
 <>x=poly(0,'x')
```

```
<>f(4,2)
 ans
         colonne
į
                      2
                               3
                                                        6
                                                5
ļ
    24 + 240x + 1080x + 2880x + 5040x + 6048x + 5040x + 2880x + 1080x
į
            + 240x + 24x
!
    24 - 24x
                     2
         colonne
•
    24x
•
            2!
    48 - 24x !
```

## 3 Examples

Let us first do the preliminary remark that it is often easier to define in MAPLE expressions to be used and then to translate them into BASILE with the help of the BASILE -MAPLE interface.

#### 3.1 Derivative computation

```
We treat the example given in section 1.2.1.
```

In a first step, we load into MAPLE the following program:

```
with(linalg);
f:=sin(x[1]+x[2])-3*(x[1]*x[2]+exp(x[3]))/(x[2]+x[3]);
gf:=grad(f,[x[1],x[2],x[3]]);
tobasile(f,'f',[x]);
tobasile(gf,'grad',[x]);
   Then we just have to execute the following sequence of instructions:
   <>frmaple()
   <>disp(f)

<out>=f(x)
out=sin(x(1)+x(2))-3*(x(1)*x(2)+exp(x(3)))/(x(2)+x(3)),
```

```
<>disp(grad)
<out>=grad(x)
out = \langle \cos(x(1)+x(2))-3*x(2)/(x(2)+x(3)), \cos(x(1)+x(2))-3*x(1)/(x(2)+x(3))+3*(x(1)+x(2))-3*x(1)/(x(2)+x(3))+3*(x(1)+x(2))-3*x(2)/(x(2)+x(3)) \rangle
*x(2)+exp(x(3)))/(x(2)+x(3))**2,-3*exp(x(3))/(x(2)+x(3))+3*(x(1)*x(2)+exp(x(3)))
/(x(2)+x(3))**2>,
    Change of variables
Here we treat the example exposed in section 1.2.2.
   We first load into MAPLE the following program:
with(linalg):
e1:=-diff(x1(t),t)+x2(t);
e2:=-diff(x2(t),t)-lambda*x1(t);
e3:=-diff(x3(t),t)+x4(t);
e4:=-diff(x4(t),t)-lambda*x3(t)-g;
e:=[e1,e2,e3,e4];
eb:=subs([diff(x1(t),t)=xd[1],diff(x2(t),t)=xd[2],diff(x3(t),t)=xd[3],
  diff(x4(t),t)=xd[4]],e);
eb:=subs([x1(t)=x[1],x2(t)=x[2],x3(t)=x[3],x4(t)=x[4]],eb);
tobasile(convert(eb,array),chvar,[t,x,xd]);
ee:=eval(subs([x1(t)=l*sin(phi1(t)),x3(t)=-l*cos(phi1(t))],e));
ee:=eval(subs([x2(t)=solve(ee[1],x2(t)),x4(t)=solve(ee[3],x4(t))],
  {ee[2],ee[4]}));
ee:=eval(subs([diff(phi1(t),t)=dphi1,diff(phi1(t),t,t)=dphi2],ee));
ss:=simplify(solve(ee,{dphi1,dphi2})[1]);
assign(ss);
dphi2:=subs(phi1(t)=phi[1],dphi2);
dphi1:=phi[2];
res:=[dphi1,dphi2];
tobasile(convert(res,array),chvar2,[t,phi]);
   Then the following instructions are entered in BASILE:
 <>frmaple()
 <>disp(chvar);
```

#### 3.3 Help to curve plotting

We may be faced with the problem of plotting the graph of a function defined by an implicit equation such as: f(t,y) = 0. This cannot be done in this form in BASILE. To be able to plot the graph of y, we make use of the implicit functions theorem, in order to compute the derivative of y with respect to t. The derivative computation is done in MAPLE. The corresponding differential equation is then numerically solved in BASILE. The resulting solution is plotted using BASILE.

Let us take the simple example  $f(t, y) = y - t^2$ .

First we load into MAPLE the following program:

```
f:=y-t^2;
d:=-diff(f,t)/diff(f,y);
tobasile(d,kdot,[t,y]);

Then the following sequence of BASILE commands gives the desired result:
<>frmaple()
<>disp(kdot)
<out>=kdot(t,y)
out=2*t,
<>tt=<0,1,2,3,4,5,6,7,8,9,10>;
<>yt=ode(0,0,tt,kdot);
<>plot(tt,yt)

The macro kdot describes the differential equation: dy/dt = - \frac{\partial f}{\partial t} \frac{\partial f}{\partial y}.
tt is the sequence of time samples where the numerical solution is computed.
```

The call to the BASILE solver ode gives the desired result. Then the graph is plotted.

The inverted pendulum

3.4

The system equations are more complex here but the symbolic manipulations are of derivative type and of no particular difficulty.

A first MAPLE procedure, of general use, linearizes a system:

$$\begin{cases} \dot{X} = f(X, U) \\ Y = g(X, U) \end{cases}$$

into:

$$\begin{cases} \dot{X} = AX + BU \\ Y = CX + DU \end{cases}$$

The corresponding MAPLE procedure is as follows:

```
# x[1..nx], u[1..nu], y[1..ny], xdot[1..nx]
# x0[1..nx], u0[1..nu]
with(linalg):
lin:=proc(xdot,y,x,u,x0,u0)
  local a,b,c,d,jac,fmat0;
  fmat0:=proc(mat) map(eval,subs(x=x0,u=u0,op(mat))) end;
  jac:=jacobian(xdot,x); a:=fmat0(jac);
  jac:=jacobian(xdot,u); b:=fmat0(jac);
  jac:=jacobian(y,x); c:=fmat0(jac);
  jac:=jacobian(y,u); d:=fmat0(jac);
  [map(simplify,op(a)),
   map(simplify,op(b)),
   map(simplify,op(c)),
   map(simplify,op(d))]
end;
```

where xdot (resp. y) is an array representing  $\dot{X}$  (resp. Y), x and u are the corresponding arrays for the variables X and U; x0 and u0 define the point where the linearization is done.

Let us recall briefly the goal of this problem (see figure 1): a control has to be designed so that the pendulum, in an inverted position on a moving chariot, keeps its equilibrium.

The differential system governing the pendulum evolution is:

$$\begin{cases} \dot{x}_1 &= x_2 \\ \dot{x}_2 &= \frac{u_1 + \sqrt{m_b} \left( \sin(x_3) x_4^2 - \cos(x_3) D_4 \right)}{m_b + m_c} \\ \dot{x}_3 &= x_4 \\ \dot{x}_4 &= D_4 \end{cases}$$

$$\begin{cases} y_1 &= x_1 \\ y_2 &= x_3 \end{cases}$$

with

$$q_m = \frac{m_b}{m_b + m_c}$$

$$d = \frac{4}{3} - q_m \cos(x_3)^2$$

$$D_4 = \frac{-\sin(x_3)\cos(x_3)q_m x_4^2 + \frac{2\sin(x_3)m_b g - q_m \cos(x_3)u_1}{m_b l}}{d}$$
E program computing the tangent linear system is:

The MAPLE program computing the tangent linear system is:

read lin:

```
x:=array(1..4); u:=array(1..1);
```

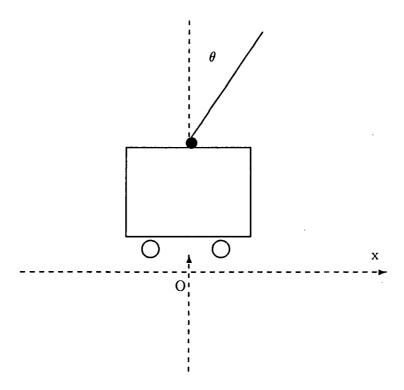


Figure 1: The inverted pendulum on a moving chariot

```
qm:=mb/(mb+mc);
cx3:=cos(x[3]);
sx3:=sin(x[3]);
d:=4/3-qm*cx3*cx3;
xd4:=(-sx3*cx3*qm*x[4]**2+2/(mb*1)*(sx3*mb*g-qm*cx3*u[1]))/d;
axdot:=array([x[2],
      (u[1]+mb*(1/2)*(sx3*x[4]**2-cx3*xd4))/(mb+mc),
      x[4],
      xd4]);
ay:=array([x[1],x[3]]);
x0:=array([0,0,0,0,0]); u0:=array([0]);
res:=lin(axdot,ay,x,u,x0,u0):
va:=res[1];
vb:=res[2];
vc:=res[3];
vd:=res[4];
u[1]:=u;
g:=9.81;
lres:=[''lss'',op(va),op(vb),op(vc),op(vd),op(x0),''c''];
tobasile(lres,'sys');
```

ay gives the original system equations, x0 is the point where to linearize, res is the tangent linear system in  $(x_0, u_0)$  and lres is the construction of the BASILE list for correct description of the linear system.

We can now get the wanted result in BASILE:

```
<>frmaple()
<>disp(sys)
<out>=sys()
\frac{1}{mb+4*mc}, 0>, <0; \frac{4}{mb+4*mc}; 0; -6/1/(mb+4*mc)>, <1,0,0,0; 0,0,1,0>, <0; 0>, <0,0,0
,0,0>,'c'),
<>mb=0.1;mc=1;l=0.3;
<>ssprint(sys());
   1 0
                   0 1
                         10
    0
       0 -0.7178049
                   0 1
                         1 0.9756098 I
x = 1
                   1 \mid x +
                         10
   10
         52.639024 0 |
                         1-4.8780488
   1
       0
          0
            0 |
```

# 4 Implementation

#### 4.1 Data communication through files

Using files for data transfer between BASILE and MAPLE implies the designation of two temporary files that BASILE and MAPLE must know.

In the case of BASILE, these two files have two be defined in the system file basile.star with the BASILE names b\_2\_m (for "basile to maple") and m\_2\_b (for "maple to basile").

This definition is machine dependent. For instance, in UNIX, it could be:

```
b_2_m='/tmp/b_2_m'
m_2_b='/tmp/m_2_b'
```

In the case of MAPLE, the two files must be defined in the system file init (usually in the src directory of the MAPLE library), with the MAPLE variable names \_tmpin et \_tmpout.

This definition is machine dependent. For instance, in UNIX, it could be:

```
_tmpin := '/tmp/b_2_m':
_tmpout := '/tmp/m_2_b':
```

The files defined for BASILE and MAPLE must have the same names, of course. In the presented implementation, it is important to point out that only one user can use the BASILE -MAPLE interface (to avoid overwriting of the temporary files). However, a slight modification can relax this restriction, for example by appending a user identification to the names of the temporary files.

#### 4.2 Initializing BASILE and MAPLE

Practically, one BASILE function (frmaple) and two BASILE macros (tomaple, clmaple) are given to the user of the interface.

The function frmaple is resident (via the initial link edition of BASILE). For a correct access to the two macros tomaple and clmaple, the user has to load the file tomaple.bas with the BASILE command getf. It can be done automatically by inserting the command in the BASILE initialization file startup.bas. The directory containing the file tomaple.bas is machine dependent.

To get correct access to the MAPLE procedures tobasile, frbasile, clbasile and basile, the user must first execute the following command in MAPLE:

```
read ''.libname.'/map2bas.m':
```

and again this can be done in the user MAPLE initialization file .mapleinit.

#### 4.3 BASILE Functions

The new BASILE functionalities are mainly given by macros.

#### 4.3.1 Function frmaple

This function is a FORTRAN program linked to BASILE. It is defined in the file frmaple.f. Its purpose is simply to execute getf from the temporary file.

#### 4.3.2 The macro clmaple

This macro destroys the temporary file. It is defined in the file tomaple.bas.

#### 4.3.3 The macro tomaple

Considering the translation from BASILE to MAPLE two situations have to be considered:

- 1. The translation is applied to simple data types such as matrices (real or complex numbers, polynomials, rationals), lists or character strings. In that case, the data transfer is done inside the macro tomaple.
- 2. We want to translate BASILE macros into MAPLE procedures. This situation would imply the use of a lexical analyzer and of a translator, leading to the writing of a BASILE expression parser. Instead, we have used the BASILE parser, taking the compiler output and translating it into MAPLE syntax. This is done by the FORTRAN subroutine tramac linked to BASILE during the initial link edition.

The BASILE macro tomaple is defined in the file tomaple.bas and the function tramac in the file tramac.f.

#### 4.4 MAPLE procedures

MAPLE procedures are stored in the file map2bas. For the translation of a MAPLE expression into BASILE we took the ideas from the MAPLE function fortran. For the translation of MAPLE procedures into BASILE macros, we used their decompilation with the help of the MAPLE procedure procedure.

## References

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