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1	Characteristics of submesoscale compensated/reinforced fronts in the
2	northern Bay of Bengal
3	
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11	

12	Key Points:
13	• The submesoscale salinity (temperature) fronts are pronounced at surface
14	(subsurface), and they tend to be compensated.
15	• Subsurface layer is featured with more compensation than surface layer, and this
16	subsurface compensation is more submesoscale-selective.
17	• The slump of salinity-controlled compensated fronts will result in temperature
18	inversion and the retaining of barrier layer.
19	
20	
21	
22	ABSTRACT
23	Fronts in the Bay of Bengal (BoB) are active and can potentially impact the regional
24	dynamics such as temperature variability, salinity distribution and oceanic circulation.
25	Based on the high resolution model output LLC4320, this study investigates the
26	characteristics of submesoscale fronts in the northern BoB and associated
27	compensation/reinforcement effects. At sea surface, horizontal gradients of salinity
28	and density are remarkable in the northern BoB, and they are nearly 3 times larger
29	than temperature gradients. As the depth deepens, temperature gradients increase and
30	become comparable to salinity gradients, while density gradients decrease a lot due to
31	the increasing effects of compensation at subsurface. Statistical results show the
32	dominance of salinity-controlled fronts over temperature-controlled fronts, and
33	compensated fronts over reinforced fronts. The surface cooling/heating results in
34	significant temporal variation of compensation at surface, but this variation is limited
35	at subsurface by the block of mixed layer base. The submesoscale-selective feature of
36	compensation is much more pronounced at subsurface layer than surface layer. From
37	statistical analysis and idealized numerical model, we found the slump of salinity-
38	controlled compensated fronts are important in generating temperature inversion and
39	maintaining barrier layer. This study validates the compensation theories originating
40	from observations, and further illustrates the importance of subsurface compensated
41	fronts with spatially continuous, regionally extended, and longer-term model output.
42	The subsurface-intensified submesoscale-selective compensation is proved for the
43	first time in this study.
44	

#### **Plain Language Summary**

46 With cold, fresh water on the one side and warm, salty water on the other side, roles of temperature and salinity in changing density are opposed across fronts, and they are 47 referred to as compensated fronts. Otherwise, the front is reinforced by temperature 48 and salinity. The strength of compensated fronts are thwarted to some extent 49 compared to reinforced fronts, thus the existence of compensation effects are not 50 favorable for forming a sharp front and associated instability processes. The statistics 51 of submesoscale compensated/reinforced fronts in the northern BoB 52 are comprehensively analyzed in this study. Concerning the amount of freshwater input, 53 fronts are dominated by salinity gradients instead of temperature gradients over the 54 northern BoB, and compensated fronts are more likely to form during winter with the 55 existence of both large salinity gradients and heat losses. Both statistical analysis and 56 idealized model simulation suggest that when the salinity front compensated by 57 58 temperature collapses, a reversed vertical temperature gradient (temperature inversion) 59 is favored to form.

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# 62 **1. Introduction**

The Bay of Bengal (BoB) is a semi-enclosed basin in the northeastern Indian Ocean. 63 The thermohaline structure in the BoB is very unique among the world's ocean basins. 64 65 A freshwater plume exists in the northern Bay of Bengal (nBoB) due to freshwater input from oceanic monsoon precipitation and associated continental river discharge 66 (Varkey et al., 1996, Sengupta et al., 2006; Papa et al., 2012). Freshwater input 67 creates a strong salinity stratification in the upper ocean of the nBoB, forming a 68 barrier layer (where halocline deeper than thermocline) and temperature inversion 69 layer (where warm water between colder water above and below) in this region 70 71 (Lucks and Lindstrom, 1991; Sprintall and Tomczak, 1992; Thadathil et al., 2002). Temperature inversion layer and barrier layer usually coexist, and they are crucial in 72 73 modulating local air-sea momentum and heat exchange, and thus impacting climate 74 and post-monsoon tropical cyclones (Thadathil et al., 2016).

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Fronts are ubiquitous in the ocean and are characterized by sharp horizontal variations in temperature, salinity, density or other material concentrations, with horizontal scales ranging from meters to kilometers (McWilliams, 2021). For example, the Kuroshio, Gulf Stream, and Antarctic Circumpolar Current are known for their prominent horizontal temperature gradients across their major axes (Wunsch, 1998; Clayton et al., 2014; Wenegrat et al., 2020) and they are largely constrained by Earth's rotation.

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84 Submesoscale fronts with horizontal scales of  $0.1 \sim 10$  km and time scales of hours ~ days are widely distributed over the global ocean (McWilliams, 2016). These fronts 85 are associated with relatively large Rossby numbers (O  $\sim$  (1)) and are thus less 86 constrained by the geostrophic effect (Thomas et al., 2008). The generation 87 88 mechanisms of submesoscale fronts and filaments (considered as dual fronts) are illustrated by previous researchers: strain-induced frontogenesis (Hoskins and 89 90 Bretherton, 1972), mixed layer instability (Boccaletti et al., 2007), horizontal convergence motion (Barkan et al., 2019) and boundary layer turbulence 91 92 (McWilliams et al., 2015). Vertical velocities around submesoscale fronts are 93 typically large due to the development of ageostrophic secondary circulation, making them instrumental in influencing oceanic biogeochemical processes (Mahadevan, 94

2016; Lévy et al., 2018) and marine pollutant distributions (Poje et al., 2014). Besides,
submesoscale fronts provide a connection between mesoscale and small scale
processes for energy cascade (Barkan et al. 2021; Balwada et al., 2022; Naveira
Garabato et al., 2021).

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Although the small spatiotemporal scale of submesoscale fronts makes them difficult 100 to resolve observationally, several studies have observed submesoscale fronts in the 101 BoB using advanced observational means. For example, Sengupta et al. (2016) 102 103 observed high-frequency salinity variations in the nBoB based on a long time series of mooring observations. They suggested that a salinity jump with magnitude of 0.2-1.2 104 PSU occurs when submesoscale salinity fronts moving pass the mooring. Based on a 105 high-resolution radiator survey in the central BoB from the Air-Sea Interactions in the 106 Northern Indian Ocean (ASIRI) - Ocean Mixing and Monsoons (OMM) project 107 (Wijesekera et al., 2016), abundant submesoscale temperature and salinity fronts were 108 observed by Ramachandran et al. (2018). They believed that these submesoscale 109 fronts are important in modulating the ocean vertical stratification. More recently, 110 using the Monsoon Intraseasonal Oscillations in the Bay of Bengal (MISO-BOB) 111 112 observations, Mckie et al. (2024) suggested that the submesoscale frontal instability and temperature inversion are closely related in the BoB. 113

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High-resolution numerical modelling is a powerful tool for studying submesoscale 115 fronts. Based on outputs from a high-resolution air-ocean-wave coupled model, 116 Jensen et al. (2018) found that the submesoscale salinity front can evolve into 117 submesoscale currents in the mixed layer through frontal instabilities. Using Large 118 Eddy Simulation (LES) results, Sarkar et al. (2016) suggested that the submesoscale 119 salinity fronts in the nBoB are associated with a variety of instability processes (e.g., 120 symmetric instability and Kelvin-Helmholtz shear instability), and further 121 development of the instability processes can alter the ocean stratification. Based on 122 LES, Pham and Sarkar (2019) found that strong salinity fronts are prone to shear 123 instability, which drives the generation of ageostrophic secondary circulations, 124 leading to the formation of barrier and temperature inversion layers on both sides of 125 the front, and enhancing local mixing. 126

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Compensating/opposing (these two terms are used interchangeably in this study) 128 effects are common across oceanic fronts when the roles of salinity and temperature 129 in density variation are opposite (i.e., warm but salty water on one side and cold but 130 fresh water on the other) (Rudnick and Martin, 2002). Horizontal density fronts at ~ O 131 (10 km) scales tend to be compensated in many regions (Drushka et al., 2019), and the 132 universality of the compensation in the North Pacific Ocean (Rudnick and Ferrari, 133 1999) and the Gulf of Mexico (Barkan et al., 2017) has been captured by cruise 134 observations and model simulations, respectively. Lin et al. (2023) used towed 135 136 measurements to reveal the mechanism of scale-dependent compensation in the Taiwan Strait. They suggested that the compensation effect at submesoscale is larger 137 (smaller) in salinity (temperature) dominated frontal zones compared to larger scales. 138 In the BoB, Spiro Jaeger and Mahadevan (2018) investigated the temperature-salinity 139 compensation effect across fronts using ship-based observations and model 140 simulations. They proposed that the restratification effect resulting from submesoscale 141 frontal instability could transform lateral gradients into mixed-layer stratification. 142 Consequently, when cooled by the atmosphere, the sea surface temperature (SST) 143 decreases more significantly on the restratified side of the salinity-controlled front 144 145 owing to the shallower mixed layer. This leads to the occurrence of temperaturesalinity compensation. 146

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The above-mentioned studies of submesoscale fronts are based on either observations 148 149 or idealized numerical models. However, the spatial coverage (both horizontal and vertical) and the time span of the observations are limited, and idealized models are 150 151 limited to describe the real oceanic fronts. Besides, a general conclusion on temperature-salinity compensation or reinforcement across fronts is still lacking. In 152 this study, a comprehensive analysis of submesoscale fronts and the associated 153 compensation/reinforcement effect is performed in the BoB using a spatially 154 continuous, regionally extended, and longer-term model output. 155

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The remainder of the manuscript is structured as follows: Data and methods are described in Section 2. Model outputs are validated in Section 3. Statistics of submesoscale fronts in the BoB are presented in Section 4. Compensation and reinforcement effects across submesoscale fronts are illustrated in Section 5. The relationship between compensated fronts and vertical stratification is shown inSection 6. Discussion and conclusions are given in Section 7.

163

## 164 **2. Data and Method**

#### 165 2.1 Numerical Model output

A high resolution primitive equation model is used to provide high resolution 166 thermohaline data in the BoB (3°N-23°N, 76°E-99°E). This model is the 167 Massachusetts Institute of Technology General Circulation Model (MITgcm) on a 168 latitude-longitude polar cap (LLC) grid (Menemenlis et al., 2008) for a period of 14 169 170 months from September 13, 2011 to November 14, 2012. The model simulation used here is the so-called LLC4320, which has a horizontal grid spacing of  $1/48^{\circ}$  (~ 2 km 171 172 in BoB). The vertical resolution of this model is refined at surface layer: grid space increases from 1 m at surface to 380 m at bottom, with 22 layers in the upper 100 m. 173 The temporal resolution of the model output is one hour, and the daily averaged data 174 are selected for analysis in order to remove the tidal signals. 175

176

The model is forced with six-hourly surface atmospheric fields (including momentum 177 and buoyancy flux) from the European Centre for Medium-Range Weather 178 Forecasting (ECMWF) atmospheric operational model analysis (with a horizontal 179 180 resolution of  $0.14^{\circ}$ ). The climatological river discharge over the BoB is included in the surface freshwater flux. Full luni-solar tidal constituents are also included in this 181 simulation as additional atmospheric pressure forcing. The vertical subgrid mixing 182 183 scheme used in the model is the K-Profile Parameterization (KPP). This model output has been successfully used in submesoscale studies (e.g. Rocha et al. 2016; Su et al., 184 2018; Dong et al., 2021; Cheng et al., 2023; Zhou et al., 2024). In this study, a period 185 of one full year (October 1, 2011 ~ September 30, 2012) is chosen for the analysis. 186

187

## 188 2.2 Multisource Data

We use several observational data sets to validate the numerical model. Sea surface
salinity (SSS) and temperature (SST) data with a 7-day interval are obtained from Soil
Moisture and Ocean Salinity SMOS/SMAP OI L4 maps product (SMOS for short)
provided and supported by the CNES CATDS and CNES TOSCA SMOS OCEAN
projects (Kolodziejczyk et al., 2021). Daily SST data are from the Group of High-

Resolution Sea Surface Temperature (GHRSST) product with a 0.01°×0.01° resolution (Dash et al., 2012). We also use SST data from Aqua Moderate Resolution Imaging Spectroratiometer (MODIS, Savtchenko et al., 2004) with a resolution of 4 km. The World Ocean Atlas 2018 (WOA18) provides vertical thermohaline data (Locarnini et al., 2018; Zweng et al., 2018). The time period for all data is from October 2011 to September 2012, except that WOA18 is monthly climatology. Detailed information about these data can be found in Table 1.

201

Table. 1. Observations and reanalysis data used in this study

Data	Time Resolution	Spatial Resolution	Variable
SMOS	7 Days	0.25°×0.25°	SSS
GHRSST	Daily	0.01°×0.01°	SST
MODIS	Daily	4 km	SST
WOA18	Monthly	0.25°×0.25°	Salinity, Temperature

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203

## 204 **2.3 Idealized numerical model**

The Coastal and Regional Ocean COmmunity model (CROCO, Auclair et al., 2022), is used to set up frontal experiments to corroborate the findings from statistical analysis (see Section 6 for detail). The fronts we set are in a channel measuring 60 km (along front)  $\times$  60 km (cross front) and 25 m (vertically), with a horizontal resolution of 2 km and a vertical resolution of 1 m. The frontal axes are along the y-direction with a hyperbolic function along the x-direction. Temperature and salinity across the fronts are set to be similar with that of Pham and Sarkar (2019) by:

$$\begin{split} T(x,z) &= \frac{\nabla T_x|_{max}L}{60\alpha g} \Big\{ T_0 \\ &+ 0.25 \left[ 1 + tanh \ tanh \ \left( x - \frac{L}{2} \right) \frac{12}{L} \right] \left[ 1 + tanh \ tanh \ \left( \frac{z + H}{2} \right) \right] \Big\} \\ &- \frac{0.5}{\alpha g} \{ \left[ N_{m,T}^2 + N_{p,T}^2 \right] z + 2(N_{m,T}^2 - N_{p,T}^2) log[\frac{\cosh((z + H)/2)}{\cosh(H/2)} \right] \} \\ &S(x,z) &= \frac{-\nabla S_x|_{max}L}{60\beta g} \Big\{ S_0 \\ &+ 0.25 \left[ 1 + Sgn * tanh \ tanh \ \left( x - \frac{L}{2} \right) \frac{12}{L} \right] \left[ 1 + tanh \ tanh \ \left( \frac{z + H}{2} \right) \right] \Big\} \\ &- \frac{0.5}{\beta g} \{ \left[ N_{m,S}^2 + N_{p,S}^2 \right] z + 2(N_{m,S}^2 - N_{p,S}^2) log[\frac{\cosh((z + H)/2)}{\cosh(H/2)} \right] \} \end{split}$$

where  $\nabla T_x|_{max} = 2 \times 10^{-6} s^{-2}$  are the maximum values of the lateral gradients of 212 temperature;  $L = 60 \ km$  is the frontal width;  $\alpha = 2 \times 10^{-4} \ \text{°C}^{-1}$  is the thermal 213 expansion coefficient and  $\beta = 8 \times 10^{-4} psu^{-1}$  is the haline contraction coefficient; 214  $T_0 = 26$  is a parameter to make the temperature close to reality;  $N_{m,T}^2 = -2 \times$ 215  $10^{-5}s^{-2}$  and  $N_{p,T}^2 = -2 \times 10^{-4}s^{-2}$  are the temperature stratification in the mixed 216 layer and the pycnocline;  $N_{m,S}^2 = 4 \times 10^{-4} s^{-2}$  and  $N_{p,S}^2 = 2 \times 10^{-3} s^{-2}$  are the 217 salinity stratification in the mixed layer and pycnocline. These values are set to 218 constant, so that the temperature structure is the same for all fronts (see first column 219 in Fig. 13). 220

221

On the other hand, we change the following parameters according to the values of the Turner angle (see Section 5 for detailed definition): 1) the maximum values of the lateral gradients of temperature( $\nabla S_x|_{max}$ ); 2) parameter to adjust the salinity close to reality ( $S_0$ ); and 3) a sign function (Sgn). This results in different salinity structures for different fronts (see second column in Fig. 13). The values of these parameters are listed in Table 2, and the way to classify a front (TCSR, SCTR, SCTO and TCSO) is described in Section 5.

229

 Table. 2. Parameter setups for different fronts

Parameter	TCSR	SCTR	SCTO	TCSO
$\nabla S_x _{max}$	$1 \times 10^{-6} s^{-2}$	$6 \times 10^{-6} s^{-2}$	$6 \times 10^{-6} s^{-2}$	$1 \times 10^{-6} s^{-2}$
S <sub>0</sub>	-230	-39	-39	-230
Sgn	1	1	-1	-1

230

231

# 232 **3. Model validation**

233 (a) Surface temperature/salinity

We first validate the ability of the LLC4320 to simulate oceanic properties in the BoB. Although there are small discrepancies, the seasonal cycles of SSS and SST in LLC4320 agree quite well with the observed SSS (from SMOS) and SST (from GHRSST) (Fig. 1). The spatio-temporal distribution of hydrological properties in the BoB is well represented in this simulation. The largest variations in SST/SSS are located in the northern bay (boxes in Fig. 1, 16°N-22.5°N, 83°E-95°E, hereafter region R1), partly due to the large input and/or variations in heat/freshwater fluxes in



this region (Fig. S1).



Fig. 1. Geographical distribution of model seasonal SST (first column, °C), GHRSST
seasonal SST (second column, °C), model seasonal SSS (third column, PSU), and
SMOS seasonal SSS (last column, PSU) during October 2011-September 2012. Black
boxes refer to region R1.

#### 248 (b) Vertical thermohaline

The vertical thermohaline distribution of the model is evaluated through comparing it with observations. We focus on region R1, which is subject to the largest SSS/SST variability (Fig. S1). The model reproduces the seasonal cycles of the subsurface thermohaline distribution well compared with the WOA18 monthly climatology data (Figs. 2a-2d). In particular, both model and observations capture the strong surface layer cooling in winter and warming in spring/summer (Fig. 2e). In addition, the upper ocean freshening event due to the increasing freshwater flux in late summer and autumn (Fig. 2f) is well captured by the model.

257

The barrier layer is well known in the ocean, especially in the BoB, for its climatic 258 effect, and the barrier layer thickness (BLT) is a good indicator to describe the ocean 259 salinity stratification. The BLT is calculated based on the variable density threshold 260 method following De Boyer Montegut et al. (2004): First, we define a reference depth 261  $(Z_{ref} = 0 m)$  and find the depth at which the temperature decreases by  $0.5^{\circ}C$ 262 compared to the temperature at  $Z_{ref}$ , which gives us the isothermal layer depth (ILD). 263 Then we calculate the density variation from  $Z_{ref}$  with a constant salinity and a 0.5°C 264 temperature decrease ( $\delta \rho$ ). Finally, we search for the depth at which the density 265 266 increase from  $Z_{ref}$  is equal to  $\delta \rho$ , and this depth is defined as the mixed layer depth (MLD). The layer between the MLD and the ILD is defined as the BLT. 267 268

The BLT corresponds to the layer between the black line (MLD) and the blue line 269 (ILD) in Figs. 2a-2d. The seasonal variation of the BLT in the model agrees well with 270 the WOA18 data, with a maximum in winter and a minimum in spring. During winter, 271 when the barrier layer is thickest and heat exchange between the surface and 272 subsurface layers is blocked, both WOA18 and LLC4320 capture a subsurface 273 temperature inversion at a depth of 40-60 m. These validations confirm the robust 274 275 thermohaline representation of the model and provide substantial credibility for conducting further analyses. 276



277

Fig. 2. Depth-time plot of (a) temperature (°C) and (b) salinity (PSU) averaged over
region R1 based on LLC4320 during October 2011-September 2012. (c) and (d) are
the thermohaline structure from WOA18 monthly climatology data. (e) Regional
mean heat flux in the model (upward, positive value means surface cooling, W/m<sup>2</sup>). (f)
Regional mean freshwater flux in the model (upward, positive value means losing
freshwater, cm/day). Black lines in (a-d) represent the MLD and blue lines in (a-d)
represent the ILD. The layer in between is the barrier layer.

## 286 (c) Typical length of submesoscale

Based on the theory of baroclinic instability (Boccaletti et al., 2007; Dong et al., 287 2020), the upper bound of the mixed layer baroclinic instability wavelength is L =288  $6\frac{N_{ML}H_{ML}}{f}$ , where  $N_{ML}$  is the mixed layer stratification,  $H_{ML}$  is the mixed layer depth, 289 and f is the Coriolis parameter. The value of L in the study area is within the range of 290 15~50 km (Fig. 3), so the submesoscale fronts can be at least partially resolved by 291 292 LLC4320 with its grid resolution of O (~2 km). The regional mean L over the nBoB is 293 about 28 km, so hereafter the submesoscale fronts are defined as fronts with scales ~O (10-30 km). 294



Fig. 3. Spatial distribution of annual mean (a) mixed layer stratification  $(s^{-1})$ , (b) mixed layer depth (m), (c) Coriolis parameter  $(s^{-1})$  and (d) upper bound of mixed layer baroclinic instability wavelength (km). Black box in (d) refers to region R1.

# **4. Statistics of submesoscale fronts in the BoB**

# 301 (a) Observed submesoscale fronts

Ocean fronts are characterized by large horizontal gradients of tracers. A snapshot of SST from MODIS (Fig. 4a) on a typical winter day shows amounts of temperature fronts in the Bay of Bengal with horizontal scales of ~ O (1) km, which can be considered as submesoscale fronts (Sengupta et al., 2016; Li et al, 2022). These submesoscale fronts are also obvious in LLC4320 (Fig. 4b).



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Fig. 4. Snapshots of SST (°C) on December 31, 2011 from (a) MODIS and (b)
LLC4320 over the BoB region. Missing data in (a) are cloud covered regions.

310

#### 311 *(b) Lateral gradients for tracers*

To represent the frontal characteristics in the BoB, the zonal and meridional gradients of temperature, salinity and density scaled by their respective coefficients are calculated as:

315 
$$\nabla T_{x} = -g\alpha \,\partial T/\partial x; \quad \nabla T_{y} = -g\alpha \,\partial T/\partial y \quad (3.1)$$
  
316 
$$\nabla S_{x} = g\beta \,\partial S/\partial x; \quad \nabla S_{y} = g\beta \,\partial S/\partial y \quad (3.2)$$
  
317 
$$\nabla \rho_{x} = \nabla T_{x} + \nabla S_{x}; \quad \nabla \rho_{y} = \nabla T_{y} + \nabla S_{y} \quad (3.3)$$

where *T*, *S* and  $\rho$  are temperature, salinity and density, respectively.  $\alpha$  is the thermal expansion coefficient and  $\beta$  is the haline contraction coefficient. *x* and *y* are the zonal and meridional direction, respectively. These scaled gradients are adjusted to have the same unit ( $s^{-2}$ ), facilitating easier comparison. Hereafter we will simply refer to the "scaled gradients" of temperature, salinity, and density as "gradients".

323

Spice is a passive tracer that combines the gradients of temperature and salinity on isopycnal surfaces (Spiro Jaeger et al., 2020). BoB region is a typical "*spicy sea*" suggested by MacKinnon et al. (2016), which represents a region in which there is significant temperature salinity (T-S) variability along an isopycnal. The scaled spice gradients are calculated as:

329

$$\nabla \gamma_x = \nabla S_x - \nabla T_x; \qquad \nabla \gamma_y = \nabla S_y - \nabla T_y \tag{3.4}$$

330

The results that will be discussed below are based on the zonal (x direction) gradients, while the results based on meridional (y direction) gradients are shown in Supplementary Materials for comparison. It can be seen that most of the results are statistically independent of direction. Hereafter we use "gradients" as a shortening for "scaled zonal gradients".

336

The annual mean amplitude of gradients at the sea surface for temperature, salinity, and density in the BoB are shown in Figures 5a-5c. Spatially, the largest gradients of salinity and density are visible in region R1 (black boxes). The region receives large amounts of freshwater from precipitation and river runoff (Fig. S1), and large

gradients are formed by the stirring of ocean currents. Large salinity and density 341 gradients are also visible in the coastal regions (i.e., east coast of India, coast of Sri 342 Lanka, west coast of Myanmar, Andaman Islands, and southern part of Sumatra). 343 These regions have very shallow water depths (shoreward of the 200 m isobaths in 344 Fig. 5), so the ocean-land interaction can induce large gradients. The surface 345 temperature gradients are much smaller compared to that of salinity and density. (Fig. 346 5a). From Eq (3.3), the horizontal density gradients are exactly the sum of the 347 temperature gradients and the salinity gradients, so that at sea surface most of the 348 349 density gradients are caused by salinity rather than temperature. This salinitycontrolled feature is also obvious in the surface temperature-salinity diagram (Fig. 350 351 S2a).



352

Fig. 5. Spatial distribution of annual mean (October 2011-September 2012) sea surface (0 m) (a)  $|\nabla T_x|$ , (b)  $|\nabla S_x|$  and (c)  $|\nabla \rho_x|$  in the BoB, multiplied by 10<sup>-7</sup>. (d-f) are subsurface (50 m) values. Units are  $s^{-2}$ . The black boxes refer to region R1 and the black contours indicate the 200 m isobaths from ETOPO2.

357

The gradients at subsurface are quite different from those at surface. Here the depth for subsurface is chosen as 50 m, i.e., the depth just below the mixed layer depth (Fig.

2). The values of  $|\nabla T_x|$  in the subsurface are much larger than those at surface (Fig. 360 5d), while  $|\nabla S_x|$  and  $\nabla \rho_x$  are smaller than those at surface (Figs. 5e-5f). In particular, 361  $|\nabla \rho_x|$  in the subsurface is much smaller than  $|\nabla S_x|$  and  $|\nabla T_x|$ , and large values 362 of  $|\nabla \rho_x|$  are mostly confined to the coastal region. In other words, most of the  $|\nabla T_x|$ 363 and  $|\nabla S_x|$  are opposed in the subsurface, producing small  $|\nabla \rho_x|$ . Compared to the 364 surface, the salinity-controlled features are much reduced in the subsurface (see also 365 Fig. S2b). Note that over the southeastern BoB region, subsurface gradients of 366 temperature and density are also remarkable. This region is featured with relative 367 shallow water depth, so the topography may be crucial in generating large gradients. 368 However, this is beyond the scope of the current study and will be addressed in future 369 370 research.

371

Obviously, large tracer gradients are not just confined to the surface layer. The depth-372 time plots for laterally averaged  $|\nabla T_x|$ ,  $|\nabla S_x|$  and  $|\nabla \gamma_x|$  over region R1 are shown in 373 374 Figure 6 in order to get a vertical view. Values of  $|\nabla T_x|$  are relatively small in the mixed layer and reach a maximum below the MLD (Fig. 6a), which may be related to 375 the intermittent tilting of the isotherms. In contrast, large  $|\nabla S_x|$  are mostly confined to 376 the mixed layer and decrease with depth (Fig. 6b). The density gradients are mostly 377 smaller than the salinity gradients, indicating that the effects of temperature and 378 salinity on the density gradients are counteracted. On the contrary, the value of  $|\nabla \gamma_x|$ 379 380 is larger than all other tracer gradients, suggesting a large variation of thermohaline properties along isopycnals. Clearly,  $|\nabla \gamma_x|$  acts in the opposite direction to  $|\nabla \rho_x|$ , 381 and large magnitudes of  $|\nabla \gamma_x|$  can be considered as a sign of temperature-salinity 382 compensation. 383



384

Fig. 6. Depth-time plot of lateral averaged (a)  $|\nabla T_x|$ , (b)  $|\nabla S_x|$ , (c)  $|\nabla \rho_x|$  and (d)  $|\nabla \gamma_x|$ during October 2011 and September 2012 over region R1. The black lines in each panel show the mixed layer depth.

# 389 (c) Selection of submesoscale fronts

Since fronts are characterized by particularly large gradients, strong submesoscale 390 391 frontal regions are defined here as locations with remarkable horizontal gradients. The probability density function (PDF) for  $|\nabla T_x|$ ,  $|\nabla S_x|$  and  $|\nabla \rho_x|$  at surface and 392 subsurface are shown in Figure 7 (solid lines). The dashed lines represent the largest 5% 393 (8% or 10% doesn't make large differences, not shown) magnitude for each gradient, 394 where the PDF slopes flatten (Barkan et al., 2017; Spiro Jaeger and Mahadevan, 2018; 395 Lin et al., 2023). At the surface (blue lines in Fig. 7), the  $|\nabla T_x|$  threshold is about 396 three times smaller than those of  $|\nabla S_x|$  and  $|\nabla \rho_x|$ , while at the subsurface (red lines 397 in Fig. 7), the  $|\nabla T_x|$  threshold is nearly identical to that of  $|\nabla S_x|$  and larger than that 398 of  $|\nabla \rho_x|$ . Meanwhile, the magnitudes of top 5% of surface  $|\nabla S_x|$  and  $|\nabla \rho_x|$  are larger 399 than at subsurface, while the top 5% of  $|\nabla T_x|$  at subsurface are larger than at surface 400 (Figs. 7d~7f). 401



402

**Fig. 7.** Probability density function (PDF) for (a)  $|\nabla T_x|$ , (b)  $|\nabla S_x|$  and (c)  $|\nabla \rho_x|$  in the BoB, denoted by solid lines (blue for 0 m and red for 50 m). Dashed lines represent the top 5% magnitude of each gradient. (d-f) are the corresponding PDF in logarithmic scale.

# **5. Compensated and reinforced fronts in the nBoB**

409 (a) Quantify the role of compensation/reinforcement

410 The density ratio  $(R_x)$  and Turner angle  $(Tu_x)$  are widely used to quantify the 411 compensation/reinforcement effect (Ferrari and Rudnick, 2000). They are calculated 412 by:

413 
$$R_x = -\nabla T_x / \nabla S_x \qquad (4.1)$$
414 
$$Tu_x = \operatorname{arctan} R_x \qquad (4.2)$$

where the negative sign means that the density decreases with temperature but increases with salinity. Since  $R_x$  can be very small (large) due to very small  $\nabla T_x$  ( $\nabla S_x$ ), it is more convenient to use  $Tu_x$  within a finite range ( $-\pi/2 < Tu_x < \pi/2$ ), as was done by Spiro Jaeger and Mahadevan (2018) and Drushka et al. (2019). A snapshot of  $Tu_x$  on April 29, 2012 in region R1 is shown in Fig. 8a. Positive and negative  $Tu_x$  appear alternately in the nBoB, indicating the role of compensation and reinforcement, respectively. Here, we classified the fronts into four types according to the value of  $Tu_x$ : Temperature Controlled Salinity Reinforcing (TCSR) with  $-\pi/2 <$  $Tu_x \le -\pi/4$ ; Salinity Controlled Temperature Reinforcing (SCTR) with  $-\pi/4 <$  $Tu_x \le 0$ ; Salinity Controlled Temperature Opposing (SCTO) with  $0 < Tu_x \le \pi/4$ ; Temperature Controlled Salinity Opposing (TCSO) with  $\pi/4 < Tu_x < \pi/2$ .



427

Fig. 8. (a) Snapshot of normalized surface  $Tu_x$  on April 29, 2012 in region R1. (b-f) are the SST and SSS structure from the black boxes in (a): (b) TCSR front, (c) SCTR front, (d) SCTO front, (e) TCSO front and (f) cold filament. Note that the color shadings in (b-f) are for temperature (°C) and the contours are for salinity (PSU).

432

Several examples of each type of front in terms of horizontal temperature and salinity 433 structure are shown in Figures 8b~8f from the  $Tu_x$  snapshot. The TCSR front is 434 featured with warm/fresh water on the southeastern side and cold/salty water on the 435 northwestern side (Fig. 8b). The SCTR front is featured with warm/fresh water on the 436 eastern side and cold/salty water on the western side (Fig. 8c). The SCTO front is 437 438 featured with warm/salty water on the southwestern side and cold/fresh water on the northeastern side (Fig. 8d). The TCSO front is featured with warm/salty water on the 439 western side and cold/salty water on the eastern side (Fig. 8e). Figure 8f shows a 440

special cold filament structure (Gula et al., 2014), which is a combination of SCTO
and TCSR fronts. It is featured with cold water lying in the middle of warm water,
and salinity increasing northwestward.

444

# 445 (b) Statistics of compensated/reinforced fronts

Since there is a large discrepancy in horizontal gradients between the coastal (< 200 m) and offshore (> 200 m) regions, as well as between the surface and subsurface layers (Fig. 5), the statistics of  $Tu_x$  are analyzed here using the conditional PDF method, and the 5% thresholds are used here to separate the frontal regions (Fig. 9). Hereafter we focus only on these frontal regions in region R1.

451

452 For regions with top 5% of  $|\nabla T_x|$  (Figs. 9a and 9b), we can first expect that no  $Tu_x$  are near zero because of the large value of  $|\nabla T_x|$ . At the surface (blue lines), there is a 453 peak of  $Tu_x$  located in  $(0, \pi/4)$  for both coastal and offshore regions as SCTO fronts. 454 In other words, regions with top 5% magnitudes of  $|\nabla T_x|$  are featured with even larger 455  $|\nabla S_{x}|$ . Apart from the SCTO fronts, the probabilities of the remaining three types of 456 457 fronts at surface are almost identical. At subsurface (red lines), large  $|\nabla T_x|$  are more likely to be fully compensated by  $|\nabla S_x|$  with a peak near  $\pi/4$ , especially far from the 458 459 coast.

- 460
- 461



**Fig. 9.** Conditional PDF of  $Tu_x$  at (a) coastal regions with top 5% of  $|\nabla T_x|$ , (b) offshore regions with top 5% of  $|\nabla T_x|$ , (c) coastal regions with top 5% of  $|\nabla S_x|$ , (d) offshore regions with top 5% of  $|\nabla S_x|$ , (e) coastal regions with top 5% of  $|\nabla \rho_x|$  and (f) offshore regions with top 5% of  $|\nabla \rho_x|$ . Blue lines for surface  $Tu_x$  and red lines for subsurface  $Tu_x$ .

462

The condition for top 5% of  $|\nabla S_x|$  are quite different from that of  $|\nabla T_x|$  in terms of the conditional PDF of  $Tu_x$  (Figs. 9c and 9d). No values of  $Tu_x$  are near  $\pm \pi/2$  for large  $\nabla S_x$ . Almost all the values of  $Tu_x$  are concentrated at  $(-\pi/4, \pi/4)$ , showing the predominance of salinity. The shape of the PDF at surface is characterized by a peak near 0, but there are still more positive (compensation)  $Tu_x$  than negative (reinforcement) ones. At subsurface, the peak of  $Tu_x$  is close to  $\pi/4$ , which is similar to the subsurface  $|\nabla T_x|$ , suggesting the tendency to be fully compensated.

476

The shape of the  $Tu_x$  PDF for the top 5% of  $|\nabla \rho_x|$  at surface is similar to that of | $\nabla S_x$ | (Figs. 9e and 9f). It is not possible for density fronts to be fully compensated, so no values of  $Tu_x$  are near  $\pi/4$ . At subsurface, there are more negative  $Tu_x$ (reinforcement effect) distributed over the coastal region, and this can help explain the large values of coastal  $|\nabla \rho_x|$  in Figure 5f.

482

# 483 (c) Seasonality of compensated fronts versus reinforced fronts

According to the frontal classification method, we can further evaluate the seasonal 484 variation of compensated fronts versus reinforced fronts over the study region. The 485 486 ratios of compensation (dark colors) to reinforcement (light colors) effects for the top 5% of  $|\nabla T_x|$ ,  $|\nabla S_x|$  and  $|\nabla \rho_x|$  during different seasons are shown in Fig. 10. Overall, 487 the seasonal variations are more pronounced at surface than at subsurface, considering 488 that the surface layer is directly influenced by the seasonal atmospheric fluxes. 489 Surface compensation is most likely to occur during winter, especially for  $|\nabla T_x|$  and 490  $|\nabla S_x|$  (more than 80%). The fresher side of a front is characterized by shallow MLD, 491 so the temperature on this side will decrease more than on the saltier side when the 492 ocean surface loses heat. As a result, there will be colder/fresher water on the one side 493 and warmer/saltier water on the other side, and they will be compensated. This 494 cooling-induced compensation has been revealed by Spiro Jaeger and Mahadevan 495 496 (2018) and is further validated here.



497

498 Fig. 10. Seasonal ratio (%) of compensated (dark color bars) and reinforced fronts

(light Scolor bars) in region R1 for (a) surface top 5% of  $|\nabla T_x|$ , (b) surface top 5% of  $|\nabla_x|$ , (c) surface top 5% of  $|\nabla \rho_x|$ . (d-f) are the same as (a-c) but for subsurface.

501

At the subsurface, the compensation ratio is also largest in winter, indicating the 502 penetration of cooling-induced compensation to the subsurface. However, the effects 503 of atmospheric flux are apparently reduced in terms of its weaker seasonal variation at 504 subsurface. Moreover, the dominance of compensation over reinforcement at 505 subsurface is present during all seasons. In spring, when the ocean is heated, the 506 surface fronts are less compensated, while the subsurface fronts are almost as 507 compensated as in winter. This enhanced subsurface compensation cannot be 508 explained by the cooling-induced effect. Other factors must be responsible for this 509 phenomenon. In the next subsection, we will briefly explain the subsurface spring 510 compensation. 511

512

#### 513 *(d) Scale-dependent compensation*

The aforementioned compensation effect is actually composed of different spatial scales of compensation. The submesoscale-selective compensation has been revealed in the BoB (Spiro Jaeger and Mahadevan, 2018) and Taiwan Strait (Lin et al., 2023) by using ship-based observations, respectively. Here, we attempt to validate whether this submesoscale selective character is robust in the model data.

519

By choosing different horizontal sampling intervals from the model data, we can 520 calculate the tracer gradients at different scales, and compare the results with the 521 model scale of ~4 km (central difference, so 2 times of grid space). The time-depth 522 compensation ratio for ~4 km and ~100 km scales are shown in Figures 11a~11b. 523 Here the compensation ratio is defined as the ratio of the compensated grids over total 524 grids for each day at each depth. In general, the compensation effect is weaker at 525 larger scales. Strong compensation signals (>70%) almost disappear at ~100 km at 526 527 subsurface, suggesting that the compensation effect at subsurface is submesoscaleselective, as pointed out by Spiro Jaeger and Mahadevan (2018). 528

529

530 The compensation effects at surface and subsurface have some similarities. As the 531 surface layer is better mixed by atmospheric turbulence, the surface compensation ratio is in general smaller than that of subsurface (Fig. 11c). The expected subsurface compensation ratio (surface value adds 8%, blue dashed line in Fig. 11c) agrees well with the real value (blue solid line in Fig. 11c), except during spring/early summer which is featured with a rapid shallowing of mixed layer depth. While the surface compensation during spring/early summer is much reduced by surface warming, large value of subsurface compensation still holds because of the block effects of mixed layer base.

539

540 A more accurate analysis between compensation ratio and sample interval is done, and the compensation at subsurface is shown to be very sensitive to the spatial scale 541 all the time (Fig. 11e). During autumn and spring, for example, the grid scale (~4 km) 542 compensation is quite obvious at subsurface, but it gets weaker quickly toward scales 543 larger than 20~40 km. In comparison, at surface the phenomenon that compensation 544 rapidly diminishes toward larger scales only occurs during early winter (Fig. 11d), 545 which is the period of the observational data in Spiro Jaeger and Mahadevan (2018). 546 Large discrepancies of scale dependency of compensation are visible from the annual 547 mean compensation ratios at surface and subsurface (Fig. 11f). It is suggesting that a 548 549 more detailed observation with a longer time span is needed to verify the robustness of submesoscale-selective compensation at surface. 550



551

Fig. 11. Time-depth plots of ratio (%) of compensation in region R1 for spatial scales 552 of (a) ~4 km and (b) ~100 km. (c) Monthly mean and regional mean time series of 553 compensation ratio at 0 m (red solid line), 50 m (blue solid line) and expected value at 554 555 50 m (blue dashed line) for model grid scale. Compensation ratio as a function of scale and time at (d) 0 m depth and (e) 50 m depth. (f) Annual mean compensation 556 ratio for different scales at 0 m (red line) and 50 m (blue line). Green lines in (a) and 557 (b) show the mixed layer depth. White contours in (a), (b), (d) and (e) show the 70% 558 559 compensation ratio.

# **6. Stratification induced by compensated fronts**

562 (a) Statistical relation

As mentioned in Section 3, the barrier layer is thick in winter and thin in spring (Fig. 2), together with the occurrence of subsurface temperature inversion in winter. Compensated fronts also prevail during winter, as seen in Section 5. Atmospheric cooling seems to play a dominant role, but oceanic processes are also significant. To illustrate the statistical relationship between atmospheric forcing, oceanic fronts and
vertical stratification, several variables are selected for comparison: a) ratio of
compensation; 2) regional mean barrier layer thickness (BLT); 3) regional mean
inversion layer thickness (ILT, defined as the layer where the vertical temperature
gradient is negative); and 4) regional mean heat flux.

572

Here the surface, SCTO, density fronts are chosen as a representation of the compensation ratio for several seasons. First, SCTO fronts are much more popular over the nBoB region than TCSO fronts. Second, the density fronts are more appropriate than salinity/temperature fronts, as density is directly related to the pressure gradients and thus ocean movement. Last but not least, surface fronts are characterized by more obvious seasonal variations than subsurface fronts.

579

The mutual correlation between all variables is quite good, with all peaks in winter 580 and troughs in late spring/summer (Fig. 12). The ocean loses heat during winter and 581 gains heat during late spring and summer. Under the condition of horizontal salinity 582 gradients, compensated fronts are most prominent in winter due to the cooling-583 584 induced compensation effect. Meanwhile, the cooling effect forms a deeper thermocline than the halocline and creates a thick barrier layer. The barrier layer can 585 586 limit the winter cooling to the shallow surface layer, and warm water can be trapped in the subsurface layer, creating a temperature inversion. 587



588

Fig. 12. Time series of ratio of SCTO (black), regional average heat flux (red), ILT
(green) and BLT (blue) over region R1. All values are normalized by their mean
values and standard deviations.

592

593 Numerical studies have shown that temperature inversions can also form when the

compensated fronts collapse (Spiro Jaeger and Mahadevan, 2018; Pham and Sarkar et al., 2019; Ramachandran and Tandon, 2020). Thus, in addition to the atmospheric cooling effect, oceanic frontal dynamics may also be responsible for the vertical stratification in frontal regions. Considering that there are four types of fronts (TCSR, SCTR, SCTO and TCSO), the resulting stratification may be quite different for different fronts. To illustrate the specific frontal processes for different fronts, idealized frontal experiments are conducted in the next section.

601

#### 602 (b) Idealized numerical model

In this subsection, four sets of frontal experiments with different types of fronts using
CROCO are conducted, and the model setups are described in Section 2. The models
are run for 2.5 days, and the initial state and final states are selected for comparison.

606

Regardless of the frontal type, the isopycnals are tilted (third column in Fig. 13), so the fronts will slump due to the gravitational effect. The frontal types are indicated by the initial values of  $Tu_x$  (fourth column in Fig. 13). The values of the Turner angle in the vertical direction  $(Tu_z)$  are also shown (last column in Fig. 13).  $Tu_z$  is calculated by:

612

$$Tu_z = \arctan(-\nabla T_z / \nabla S_Z) \tag{6.1}$$

613 It represents the effects of vertical compensation/reinforcement. In the initial state, the 614 warm/fresh water is in the surface and the cold/salty water is in the subsurface, so  $Tu_z$ 615 is negative everywhere (reinforcement).



**Fig. 13.** The cross front temperature (first column), salinity (second column), density (third column),  $Tu_x$  (fourth column) and  $Tu_z$  (last column) for TCSR front (first row), SCTR front (second row), SCTO front (third row), and TCSO front (last row) of the initial state. Black lines represent the MLD and red lines represent the ILD. The layer in between is the barrier layer.

616

The final state after 2.5 days of running is shown in Figure 14. As the lighter waters are located on the right side of the TCSR, SCTR and TCSO fronts (third column in Fig. 13), they all tend to slump to the left, and the warm water tends to rise above the cold water (first column in Fig. 14). No temperature inversion is formed and the barrier layer is reduced more or less by the slump of the isotherms. The values of  $Tu_z$ remain negative for these three fronts (last column in Fig. 14).

629

The evolution of the SCTO front is quite different from other fronts (third row in Fig. 14). In this case, the lighter waters are on the left side of the front. When the front slumps, the fresh waters tend to be above the salty waters, but the warm waters tend to be below the cold waters due to the tilt of the isotherms. Also, the ILD remains deep, so the barrier layer remains thick. The values of  $Tu_z$  become positive around the temperature inversion region, indicating the vertical compensation effect. These results may help to further explain why SCTO fronts and temperature inversion layers



637 / barrier layer are collocated.



**Fig. 14.** The same as Fig. 13, but after 2.5 days of model running.

640

641 **7. Discussion and conclusions** 

642 In this study, we used high-resolution model output (LLC4320) to investigate the characteristics of compensated/reinforced submesoscale fronts in the northern BoB. 643 The model is shown to describe the main temperature and salinity features in the 644 study region realistically. Large surface horizontal temperature, salinity and density 645 gradients occur over the northern bay, with salinity/density gradients nearly 3 times 646 larger than temperature gradients. At subsurface, temperature gradients are apparently 647 increased compared to that at surface, while density gradients are much reduced due 648 to the increasing counteracting effect between temperature and salinity. 649

650

Probability density functions of gradients tend to flatten at magnitudes of the largest 5% of each gradient, and regions where gradients larger than these thresholds are considered as submesoscale frontal regions. The roles of compensation and reinforcement across fronts are quantified using the Turner angle. Based on the value of the Turner angle, submesoscale fronts are classified into 4 types: SCTO (salinitycontrolled fronts compensated by temperature), SCTR (salinity-controlled fronts
reinforced by temperature), TCSO (temperature-controlled fronts compensated by
salinity), and TCSR (temperature-controlled fronts reinforced by salinity).

659

The statistics of different types of fronts are analyzed. Surface fronts are mostly 660 controlled by salinity and partly compensated by temperature, while subsurface fronts 661 are controlled by both temperature and salinity and tend to be fully compensated. 662 Seasonal variations for surface fronts are more pronounced than for subsurface fronts, 663 664 with SCTO fronts being most pronounced in winter, due to the combined effects of the existence of strong salinity fronts and heat losses of the ocean. The subsurface 665 layer has more compensation than the surface layer, and the submesoscale-selective 666 compensation is proved by choosing different horizontal sampling intervals. The 667 SCTO fronts are suggested to be closely related to the vertical barrier layer and 668 temperature inversion, and this is further confirmed by idealized models. The 669 intermittent appearance of the temperature inversion layer and the barrier layer in the 670 BoB region may be related to the formation and dissolution of compensated 671 submesoscale fronts. 672

673

The subsurface compensation is shown to be an inherent feature in the ocean. When 674 675 the idealized fronts (Section 6) slumps, a lot of compensation signals occur at subsurface (5-15 m in this case) for different types of fronts. Zonal sections of  $Tu_r$ 676 and  $Tu_z$  from LLC4320 for a typical spring day are shown in Figure 15. Positive  $Tu_x$ 677 are mostly confined at subsurface (compensation), while negative  $Tu_z$  are dominated 678 except at surface layer in order to stay vertical stable. At subsurface,  $Tu_z$  is combined 679 680 with positive values (compensation) and small negative values (weak reinforcement). Under a small disturbance, the vertical weak reinforcement is easy to change its sign 681 682 to compensation, and the vertical compensation can easily convert to horizontal compensation when the isopycnals tilt. At surface, although large vertical 683 compensation exists, the surface wind stirs and homogenizes this layer, so 684 compensation is less prevailing. This subsurface layer is the so called pycnocline by 685 Spiro Jaeger et al. (2020), which is featured with most remarkable spice variation, and 686 can be proved from the submesoscale (10-30 km) power spectrum density (PSD) for 687  $\nabla T_x$  and  $\nabla S_x$  (Fig. 15c). This can help to explain why subsurface compensation is 688





Fig. 15. Zonal section of (a)  $Tu_x$  and (b)  $Tu_z$  from LLC4320 for a typical spring day. (c) Annual mean and regional averaged power spectrum density (PSD) of  $\nabla T_x$  and  $\nabla S_x$ at submesoscale range (10-30 km) in logarithmic scale.

690

A front is either compensated or reinforced. Compensated fronts are characterized 695 with a density gradient at least smaller than either temperature gradient or salinity 696 gradient, while reinforced fronts are featured with larger density gradient than both 697 698 temperature and salinity gradient. Compensated fronts with smaller density gradients are thus not favorable for frontal instability and associated energy transfer and 699 700 transformation compared to reinforced fronts. In an ideal ocean without any forcing, temperature and salinity always tend to be fully compensated in order to get a 701 completely stable state. But in the real ocean, this is never the truth thanks to the 702 omnipresent disturbance. 703

704

There are still some limitations of the model data. For example, the temporal 705 706 frequency and the way to include river run-off in the model may impact the submesoscale fronts, especially the coastal regions close to the river mouth. The 707 model is using climatological river discharge and converting it to freshwater flux, and 708 the season variation of river discharge is not included. As a result, the model 709 710 overestimates freshwater in spring and underestimates freshwater in autumn. Additionally, converting river freshwater into surface flux may omit the river 711 712 diffusion processes, which could generate some small scale processes. The submesoscale salinity fronts captured by the model may be underestimated. A real 713 river forcing with relative high frequency is needed to better understand the 714

submesoscale frontal dynamics around the river mouth.

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725

# 726 **Open Research**

## 727 Data Availability Statement

- 728 The authors declare that the data supporting the findings of this study are available
- within the article and the multisource data used in this study can all be found online.
- 730 The LLC4320 model output used for analysis can be directly accessed from the
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- 741 model outputs for different types of fronts are available at
- https://doi.org/10.5281/zenodo.13235434. Figures were made with Matplotlib version
- 3.9.0 at https://doi.org/10.5281/zenodo.11201097 and available under the Matplotlib
- 744 license at https://matplotlib.org/ (Hunter, 2007).
- 745
- 746

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Figure 01.



Figure 02.



Figure 03.



Figure 04.



Figure 05.



Figure 06.







Figure 07.



Figure 08.





Figure 09.



Figure 10.



Figure 11.



Figure 12.



Figure 13.



Figure 14.



Figure 15.

