



Statistical inference for Same Data Meta-Analysis (SDMA) for neuroimaging multiverse analyzes



OHBM 2024
JUNE 23~27, SEOUL, KOREA



Jeremy
Lefort-Besnard



Thomas
Nichols



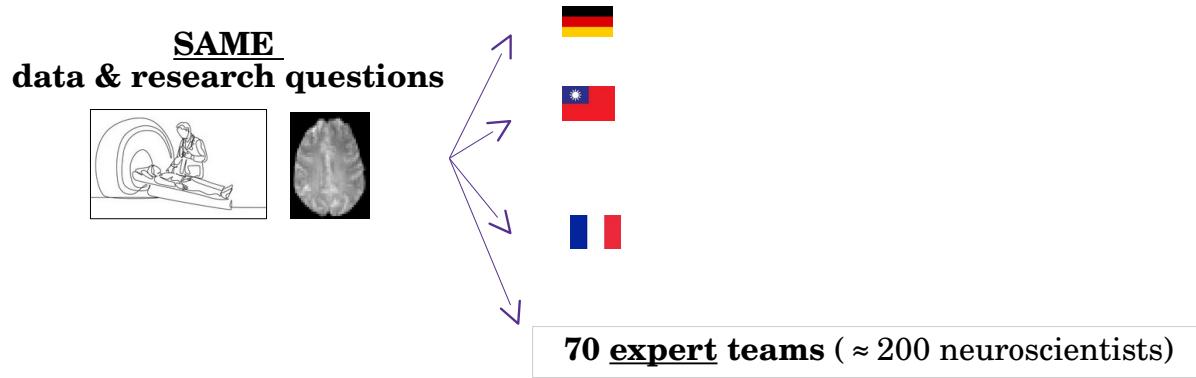
Camille
Maumet





Same Data Meta-Analysis - Introduction

NARPS study (Rotem Botvinik-Nezer et al. Variability in the analysis of a single neuroimaging dataset by many teams. *Nature*, 2020)



Same Data Meta-Analysis - Introduction



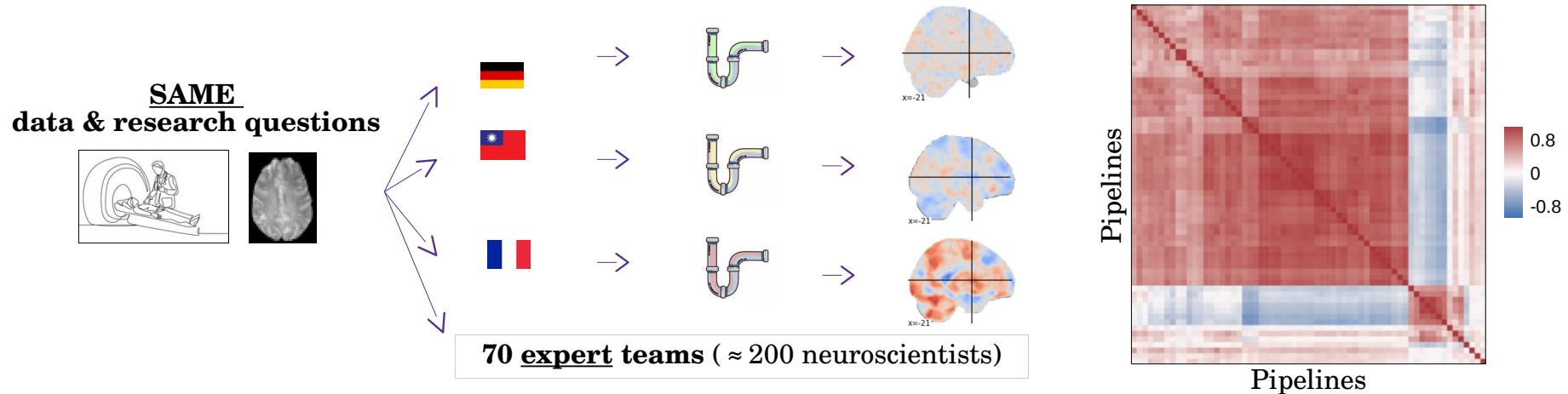
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Same Data Meta-Analysis - Introduction



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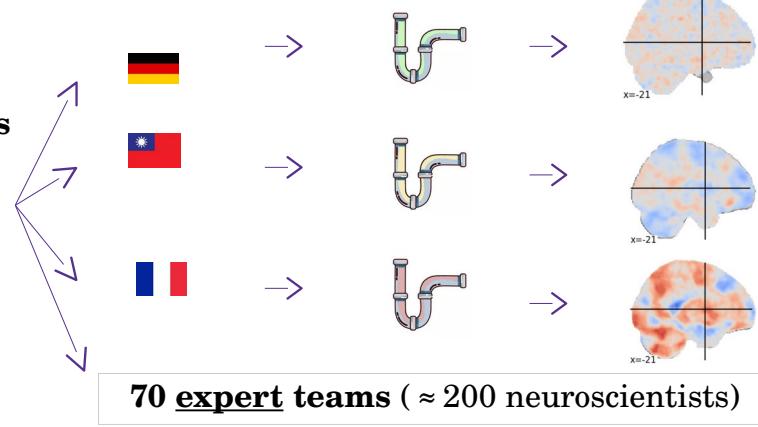
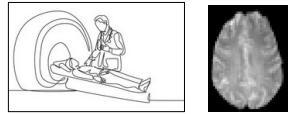


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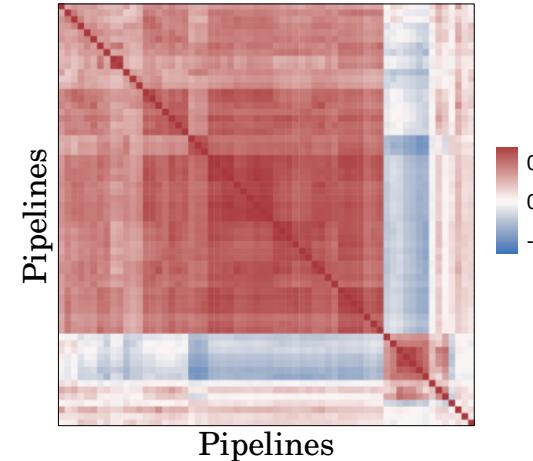


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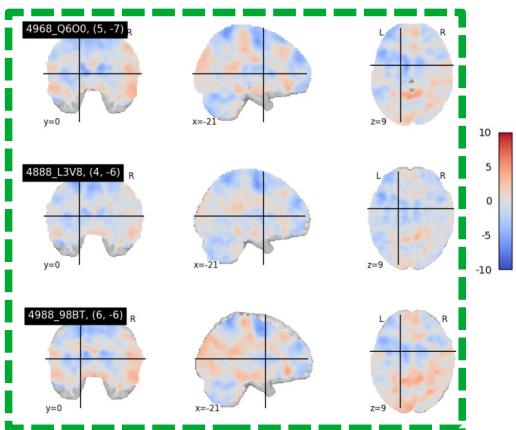
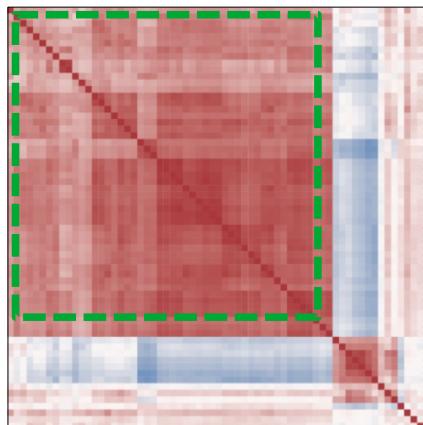
SAME
data & research questions



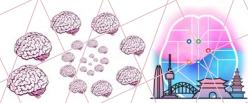
70 expert teams (≈ 200 neuroscientists)



Pipelines

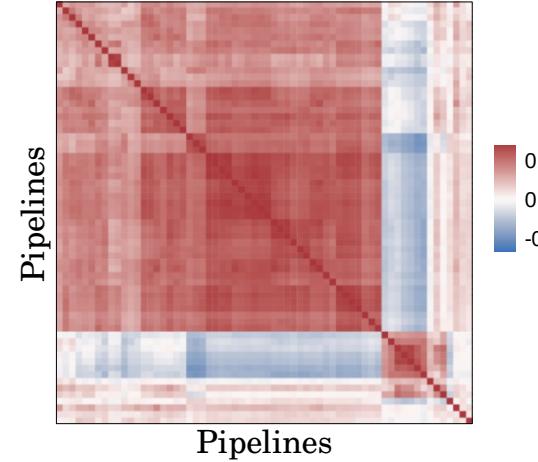
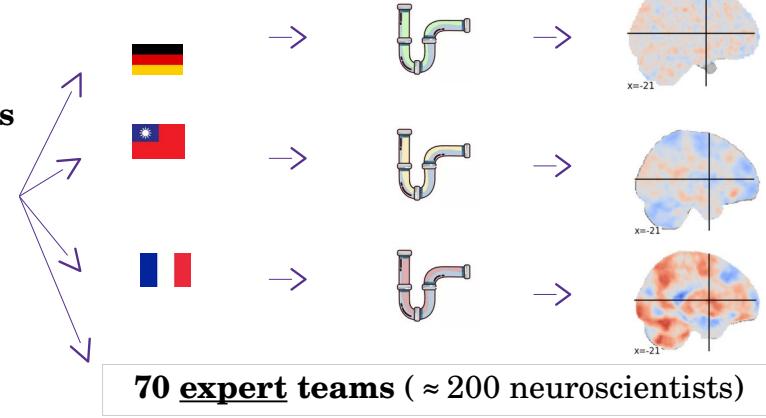
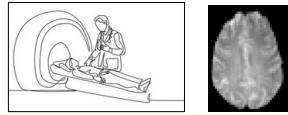


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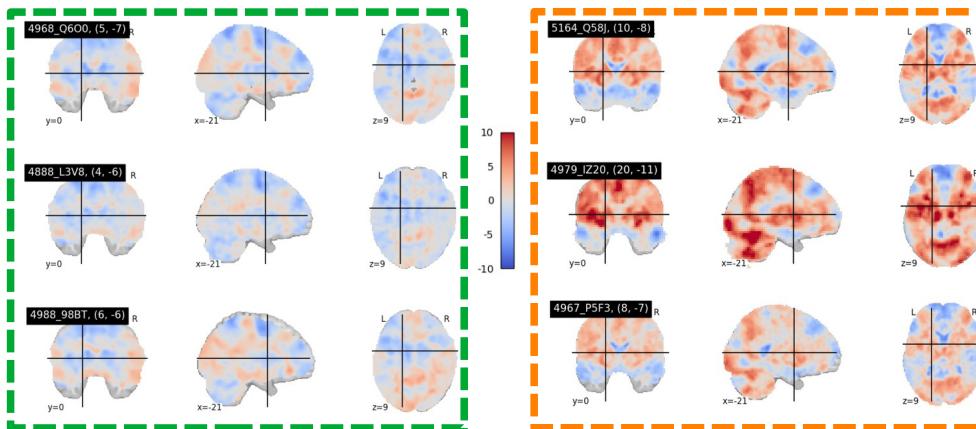
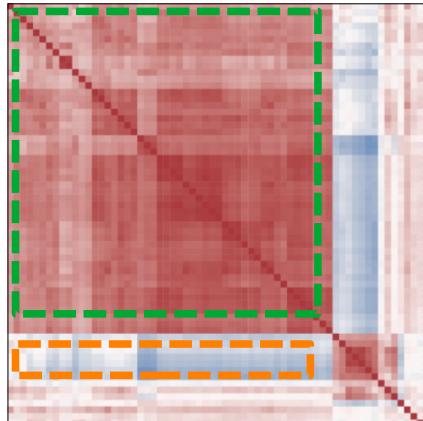


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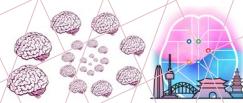
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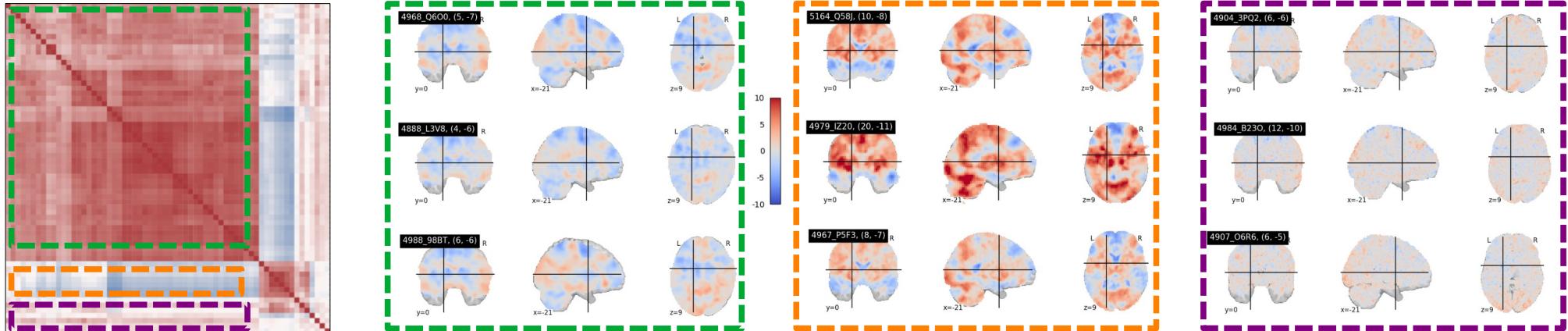
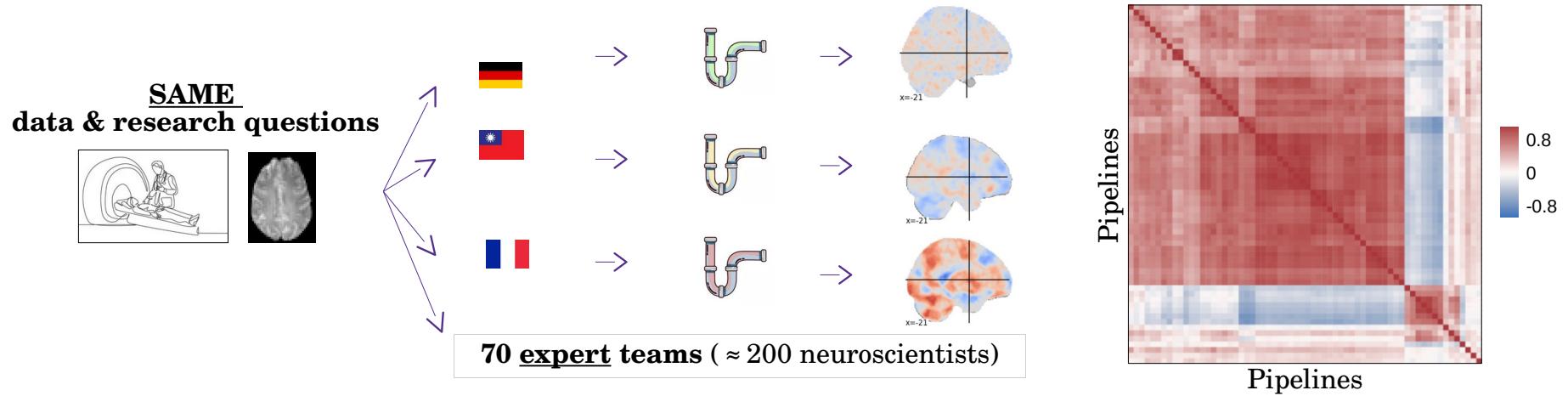
Pipelines



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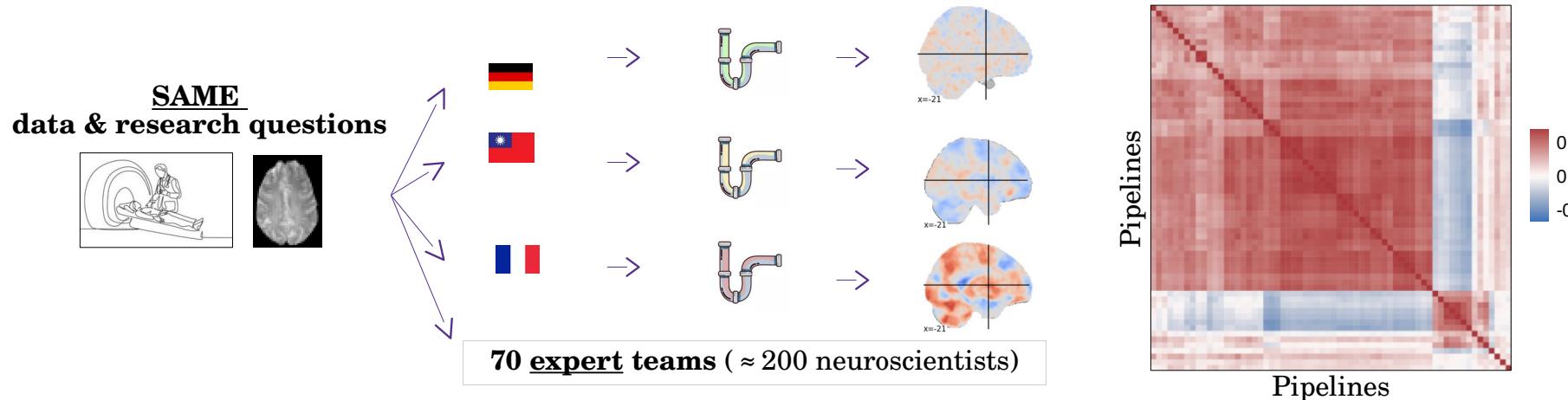
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Same Data Meta-Analysis - Introduction

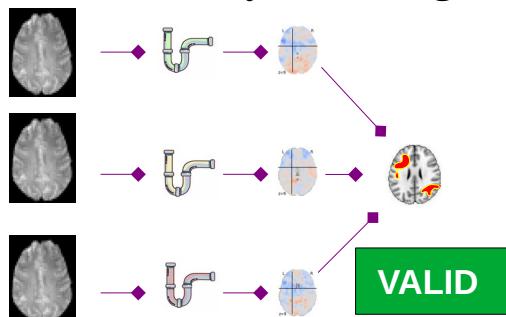


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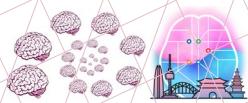


Classical meta-analysis methods in :

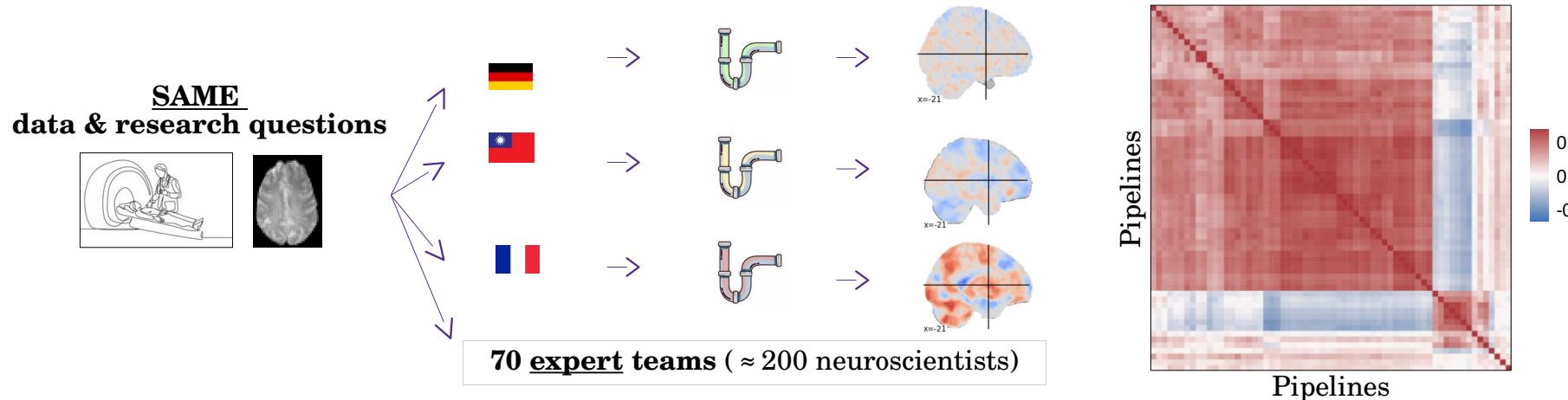
Traditional analysis setting



Same Data Meta-Analysis - Introduction

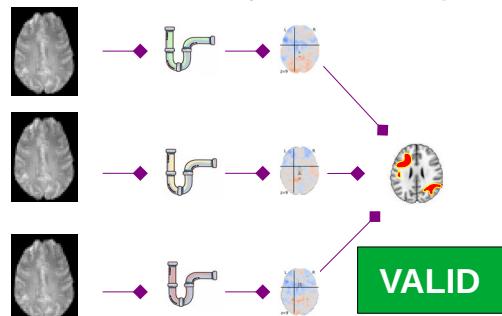


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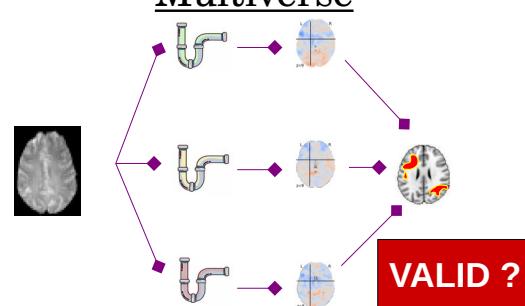


Classical meta-analysis methods in :

Traditional analysis setting



Multiverse





Same Data Meta-Analysis - Methods

CLASSICAL Meta-Analysis

Stouffer

$$Z_j^S = \frac{\bar{Y}_j}{\sqrt{1/K}}$$

Average standardized

SDMA Stouffer

$$Z_j^{SS} = \frac{\bar{Y}_j}{\sqrt{\mathbf{1}_k^\top \mathbf{Q} \mathbf{1}_k / K^2}}$$

Average standardized
accounting for
dependence

SAME DATA Meta-Analysis

Lefort-Besnard, Nichols*, and Maumet*. (2024). Statistical inference for Same Data Meta-Analysis for neuroimaging multiverse analyzes. *In prep.*



Same Data Meta-Analysis - Methods

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SAME DATA Meta-Analysis

Consensus SDMA Stouffer

$$Z_j^{CSS} = Z_j^{SS} - \langle Z^{SS} \rangle + \mu_C$$

Average standardized
accounting for
dependence,
and shifted empirically

Lefort-Besnard, Nichols*, and Maumet*. (2024). Statistical inference for Same Data Meta-Analysis for neuroimaging multiverse analyzes. *In prep.*



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Average standardized accounting for dependence

SAME DATA Meta-Analysis

Consensus SDMA Stouffer

$$Z_j^{CSS} = Z_j^{SS} - \langle Z^{SS} \rangle + \mu_C$$

Average standardized accounting for dependence, and shifted empirically

Consensus Average

$$Z_j^{CA} = \frac{\bar{Y}_j - \langle \bar{Y} \rangle}{\sqrt{\langle \langle \bar{Y} \rangle \rangle}} \sigma_C + \mu_C$$

Average, scaled and shifted empirically

Lefort-Besnard, Nichols*, and Maumet*. (2024). Statistical inference for Same Data Meta-Analysis for neuroimaging multiverse analyzes. *In prep.*



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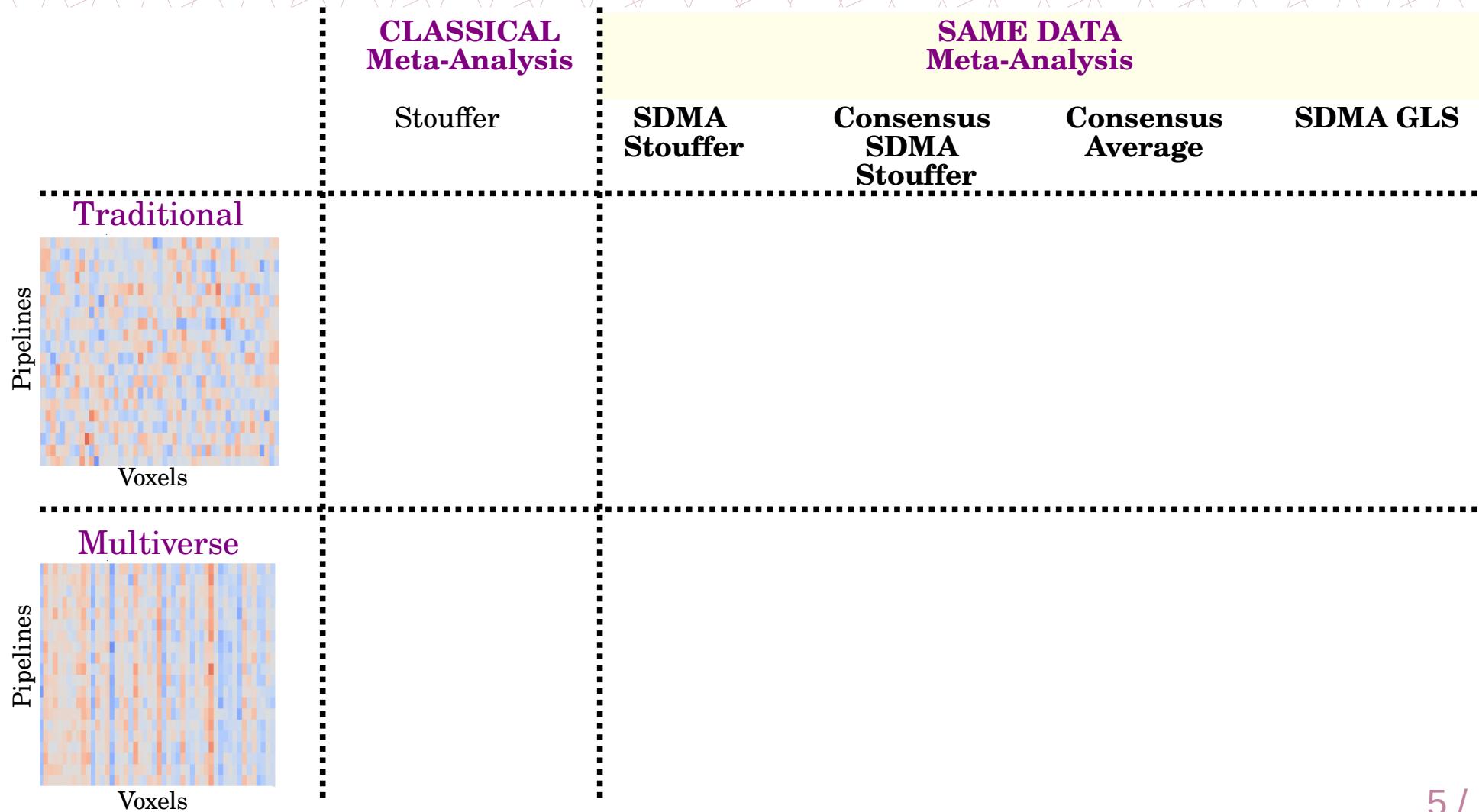
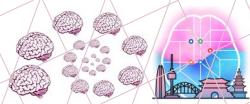
SDMA GLS

$$Z_j^{SG} = \frac{\mathbf{1}^\top \mathbf{Q}^{-1} \mathbf{Y}_j}{\sqrt{\mathbf{1}^\top \mathbf{Q}^{-1} \mathbf{1}}}$$

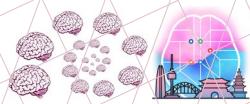
Optimal average,
standardised

Lefort-Besnard, Nichols* and Maumet*. (2024). Statistical inference for Same Data Meta-Analysis for neuroimaging multiverse analyzes. *In prep.*

Same Data Meta-Analysis - Results in simulations

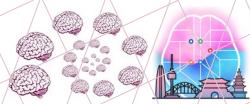


Same Data Meta-Analysis - Results in simulations



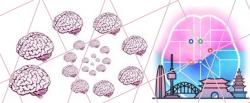
		CLASSICAL Meta-Analysis		SAME DATA Meta-Analysis		
		Stouffer	SDMA Stouffer	Consensus SDMA Stouffer	Consensus Average	SDMA GLS
Pipelines	Traditional					
	Voxels	VALID 4.7 %				
Pipelines	Multiverse	$\alpha = 5\% \text{ nominal}$				
	Voxels					

Same Data Meta-Analysis - Results in simulations



		CLASSICAL Meta-Analysis		SAME DATA Meta-Analysis		
		Stouffer	SDMA Stouffer	Consensus SDMA Stouffer	Consensus Average	SDMA GLS
Pipelines	Traditional					
	Voxels	VALID 4.7 %				
Pipelines	Multiverse	$\alpha = 5\% \text{ nominal}$				
	Voxels	INVALID 30.1 %				

Same Data Meta-Analysis - Results in simulations



		CLASSICAL Meta-Analysis		SAME DATA Meta-Analysis		
		Stouffer	SDMA Stouffer	Consensus SDMA Stouffer	Consensus Average	SDMA GLS
Pipelines	Traditional					
	Voxels	VALID 4.7 %	VALID 4.7 %	VALID 4.8 %	VALID 4.8 %	VALID 4.4 %
Pipelines	Multiverse	$\alpha = 5\% \text{ nominal}$				
	Voxels	INVALID 30.1 %	VALID 4.9 %	VALID 5.0 %	VALID 5.0 %	VALID 4.9 %



SAME DATA Meta-Analysis

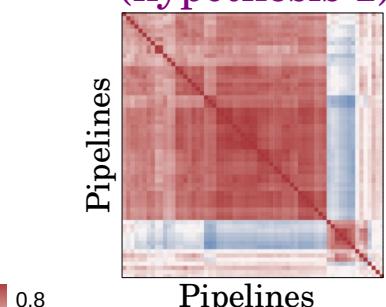
SDMA
Stouffer

Consensus
SDMA
Stouffer

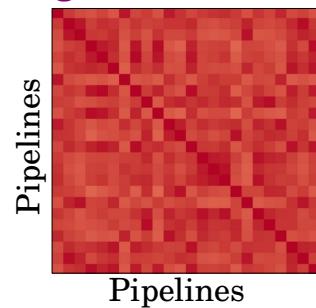
Consensus
Average

SDMA GLS

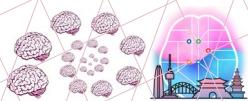
NARPS
(hypothesis 1)



HCP Young Adult
(Right hand contrast)



Same Data Meta-Analysis - Results in real data



SAME DATA Meta-Analysis

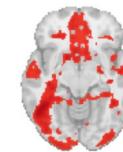
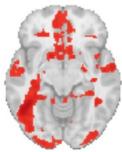
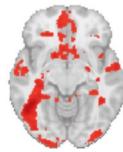
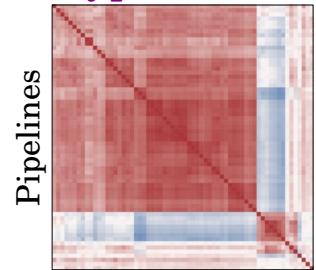
SDMA
Stouffer

Consensus
SDMA
Stouffer

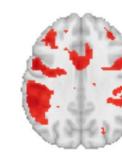
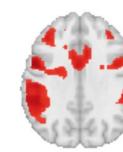
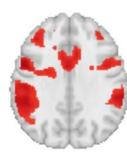
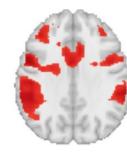
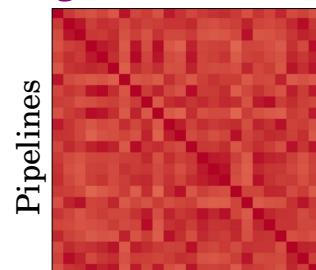
Consensus
Average

SDMA GLS

NARPS
(hypothesis 1)

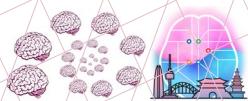


HCP Young Adult
(Right hand contrast)

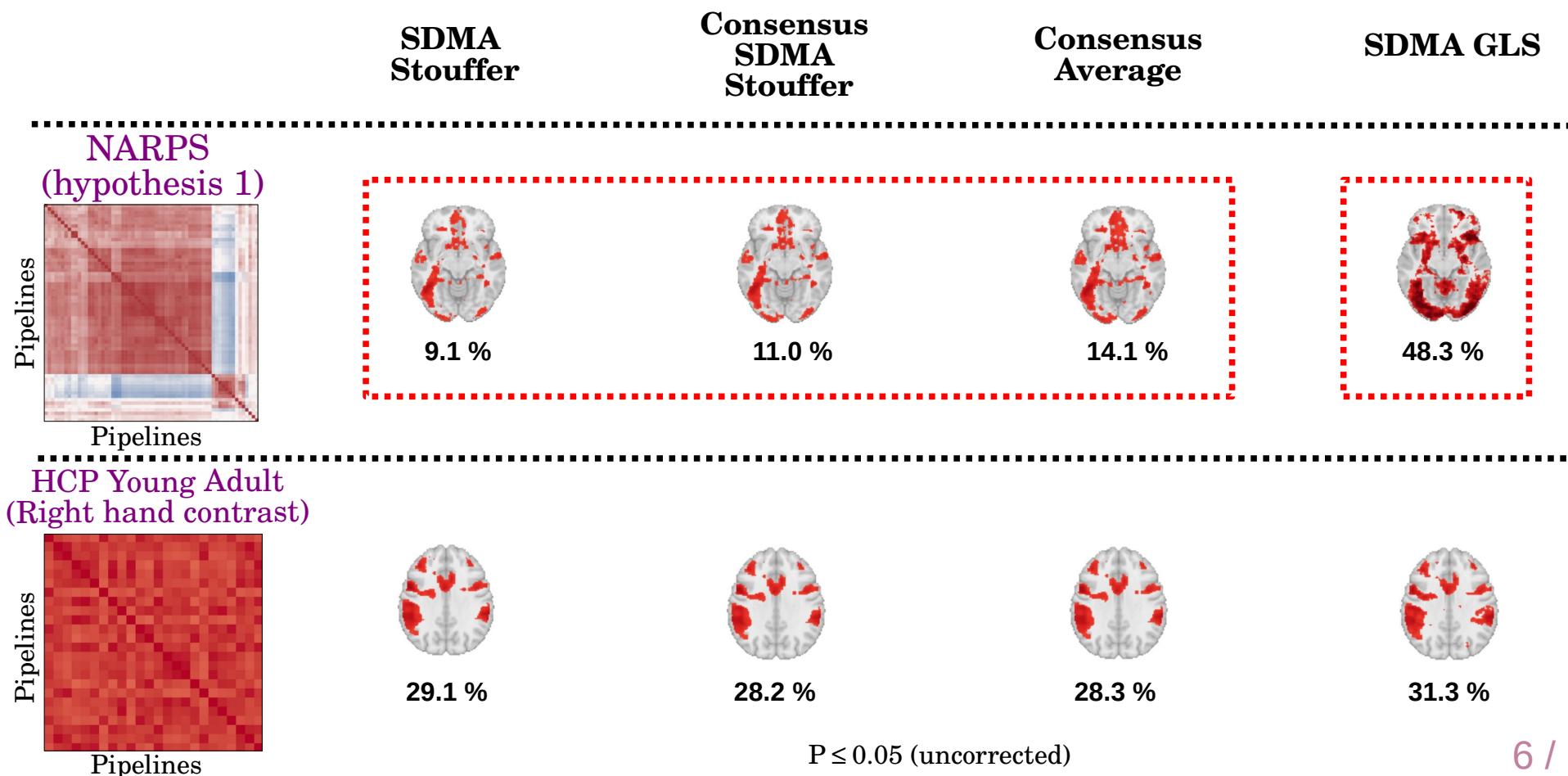


$P \leq 0.05$ (uncorrected)

Same Data Meta-Analysis - Results in real data



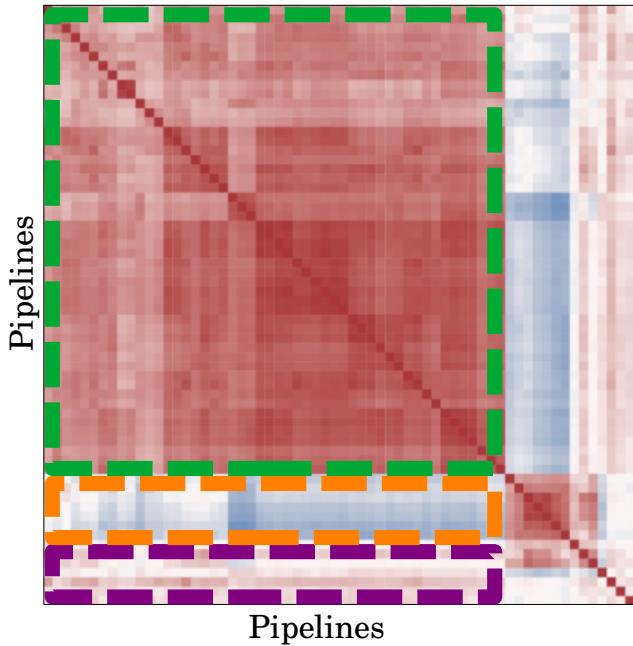
SAME DATA Meta-Analysis



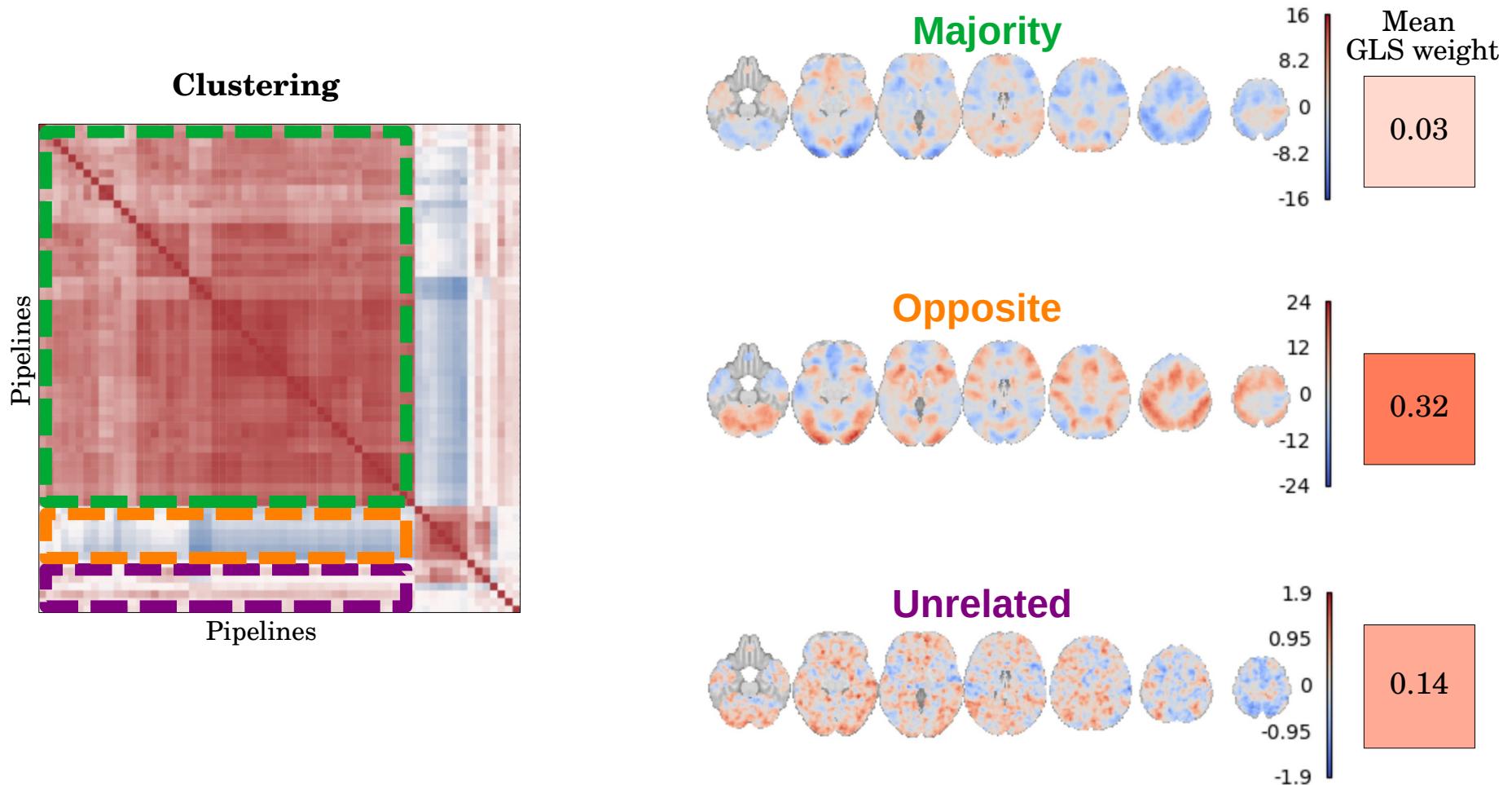


Same Data Meta-Analysis - Interpretability of SDMA GLS

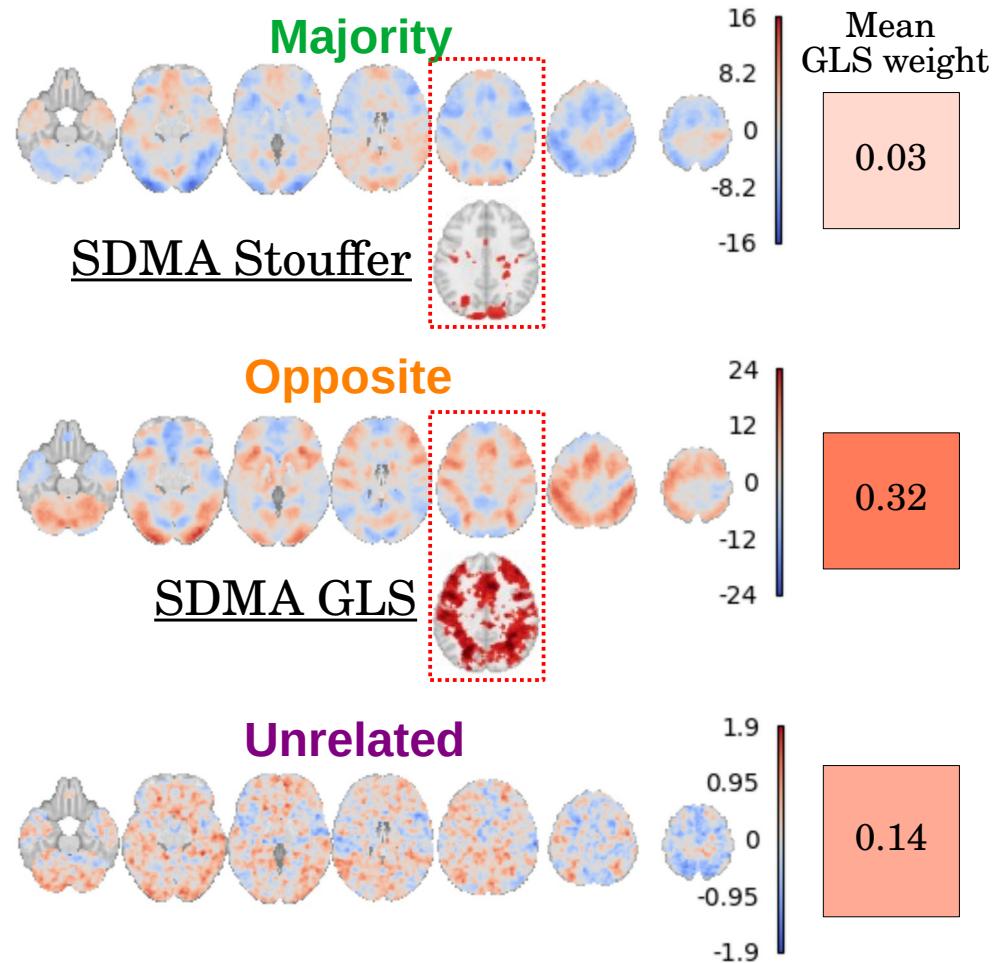
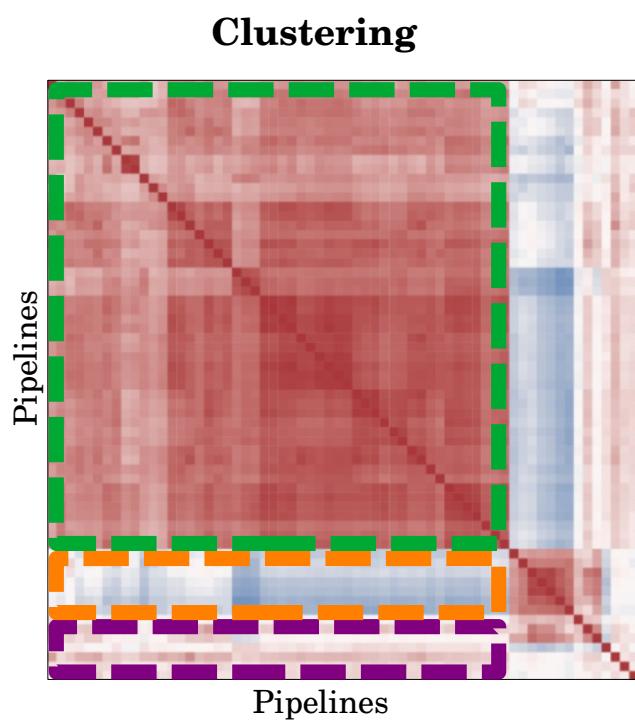
Clustering



Same Data Meta-Analysis - Interpretability of SDMA GLS



Same Data Meta-Analysis - Interpretability of SDMA GLS





Take-home message:

SDMA Stouffer

$$Z_j^{\text{SS}} = \frac{\bar{Y}_j}{\sqrt{\mathbf{1}_k^\top \mathbf{Q} \mathbf{1}_k / K^2}}$$

Average standardized accounting for dependence

Consensus SDMA Stouffer

$$Z_j^{\text{CSS}} = Z_j^{\text{SS}} - \langle Z^{\text{SS}} \rangle + \mu_C$$

Average standardized accounting for dependence, and shifted empirically

Stable

Consensus Average

$$Z_j^{\text{CA}} = \frac{\bar{Y}_j - \langle \bar{Y} \rangle}{\sqrt{\langle \langle \bar{Y} \rangle \rangle}} \sigma_C + \mu_C$$

Average, scaled and shifted empirically

SDMA GLS

$$Z_j^{\text{SG}} = \frac{\mathbf{1}^\top \mathbf{Q}^{-1} \mathbf{Y}_j}{\sqrt{\mathbf{1}^\top \mathbf{Q}^{-1} \mathbf{1}}}$$

Optimal average, standardised

Though theoretically optimal, unstable in heterogeneous sample



Thank you !



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Jeremy
Lefort-Besnard



Thomas
Nichols



Camille
Maumet

OHBM 2024

Université
de Rennes

Inria

Inserm
Institut national de la santé et de la recherche médicale

CNRS

IRISA

BIG DATA
INSTITUTE

UNIVERSITY OF
OXFORD

EMPENN