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# Numerical Simulation of Turbulent Flows using the SST-SAS Model

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*Abstract:* - Turbulent flows play a crucial role in various engineering and scientific applications, and the accurate prediction of these flows remains a challenging task. This review explores the application of the Shear Stress Transport Scale-Adaptive Simulation (SST-SAS) turbulence model for solving incompressible turbulent flows, with a specific focus on unsteady wakes behind bluff bodies. Providing a concise overview of the model's formulation and its advantages, this article highlights the efficacy of the SST-SAS model in simulating the intricate dynamics in different configurations of circular cylinders. The present study affirms that the SST-SAS model can be considered a highly viable alternative for simulating unsteady flows around bluff bodies due to the good predictive quality of the resulting simulations.

*Key-Words:* - SST-SAS turbulence model, unsteady flow, interference effects, wall proximity, tandem circular cylinders, staggered tube bundle, wall-mounted cylinder.

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## 1 Introduction

It is widely acknowledged that for quite a broad range of flow configurations, the Reynolds-Averaged Navier-Stokes (RANS) approach can yield relatively satisfactory results for mean flow quantities at a moderate computational cost. However, in scenarios of flows largely dominated by large-scale separation, the standard RANS methodology finds rapidly its limits. Under such conditions, the intricate nature of turbulent flows

calls for alternative modeling techniques to obtain more accurate numerical predictions. In the last decade, significant strides have been made in Large Eddy Simulation (LES) models but their systematic application to specific industrial flows at very high Reynolds and Rayleigh numbers remains quite a challenge, [1]. The hybridization of LES with RANS is one possibility that permits to strike a balance between the results' accuracy and computational efficiency, [2]. Revisiting the RANS

framework and reevaluating the derivation of its governing equations was another option followed in [3], to develop an unsteady RANS (URANS) model called the scale-adaptive simulation (SAS) approach. More specifically, the SAS version called SST-SAS [4], and based on the  $k-\omega$  SST RANS model, [5], became quite a popular choice when it comes to selecting a turbulence model. Indeed, a search through the literature of the last ten-year period with the keyword “SST-SAS” in the title or the abstract returns more than one hundred references. The diversity of flow configurations dealt with is quite impressive, a glimpse of it is given by the references listed below:

- Canonical configurations: flows over a backward-facing step [6]; the periodic hill [7]; flows past a circular cylinder [8], [9], [10], [11], [12]; flows past two circular cylinders [13]; the flow past a prismatic bluff body [14]; twin impinging jets [15].
- Systems of practical interest: the flow around a high-speed train [16], the flow past an airfoil [17]; the flow over a wall mounted array of cubes [11]; the flow in a tube bundle [18], [19]; flows in centrifugal pumps [7], [20]; the flow in a pressure wave exchanger [21]; the filling of a tank [22]; a ship air wake [23]; flows in Francis turbines [24], [25], [26].

In the above-listed studies, the SST-SAS method was employed either with commercial codes (ANSYS-FLUENT, CFX, STAR-CCM+) or with the open-source library OpenFOAM or in-house codes. But, regardless of the kind of numerical set-up used, the SST-SAS turbulence model is generally praised for its capability of well-predicting on relatively coarse meshes the mean flow properties while being able to resolve a significant portion of the flow temporal fluctuations. It should be noted though that in most of these studies, the assessment of the quality of the model is largely based on visual comparisons with experimental data and not on the recourse to objective criteria. Some studies are performing such a comparison on integral flow quantities but only two studies are using objective criteria to compare experimental and numerical data sets, [14], [18]. The context regarding the use of the SAS approach being now recalled, the objective of the present contribution is i) to review published applications of the SST-SAS model to the simulation of incompressible unsteady flow over cylinder(s) and ii) to present new results obtained for the configuration of the flow over a wall-mounted cylinder. Such configurations hold

practical relevance in various engineering applications, including heat exchangers, pipelines used in fuel storage and distribution chains, and offshore and ocean structures like subsea pipelines, marine risers, and platform legs. The paper is organized as follows: Section 2 describes the governing equations and the SST-SAS turbulence model. In Section 3, the reviewed cases are analyzed and discussed. Section 4 presents recent experimental and numerical results for the flow around a wall-mounted cylinder. Finally, Section 5 presents the concluding remarks along with some axes of future activity.

## 2 Background

### 2.1 Flow Model Formulation

The behavior of fluids in motion is comprehensively described by the Navier-Stokes and continuity equations. The ensemble averaging of these equations, considering a constant density, isothermal, and incompressible body force-free flow, yields the Unsteady Reynolds-Averaged Navier-Stokes (URANS) equations. In the Cartesian coordinate system ( $O, x_1, x_2, x_3$ ), these equations can be expressed as follows:

$$\frac{\partial \langle u_i \rangle}{\partial x_i} = 0 \quad (1)$$

$$\frac{\partial \langle u_i \rangle}{\partial t} + \frac{\partial \langle u_i \rangle \langle u_j \rangle}{\partial x_j} = \frac{1}{\rho} \frac{\partial \langle p \rangle}{\partial x_j} + \frac{\partial}{\partial x_j} \left[ \nu \left( \frac{\partial \langle u_i \rangle}{\partial x_j} + \frac{\partial \langle u_j \rangle}{\partial x_i} \right) - \langle u_i' u_j' \rangle \right] \quad (2)$$

where  $\langle u_i \rangle$  is the ensemble average component of the velocity in the direction  $x_i$ ,  $\rho$  is the density of the fluid,  $\langle p \rangle$  is the ensemble average pressure,  $\nu$  is the kinematic viscosity and  $\langle u_i' u_j' \rangle$  is the Reynolds stress tensor. To complete this URANS system, the Reynold stress tensor, representing turbulence effects through nonlinear terms, is modeled through a Boussinesq-like relation, namely:

$$\langle u_i' u_j' \rangle = -\nu_t \left( \frac{\partial \langle u_i \rangle}{\partial x_j} + \frac{\partial \langle u_j \rangle}{\partial x_i} \right) + \frac{2}{3} k \delta_{ij} \quad (3)$$

where the turbulent eddy viscosity  $\nu_t$  and the turbulence kinetic energy  $k$  are calculated thanks to the recourse to the SST-SAS turbulence model.

## 2.2 SST-SAS Two-Equation Turbulence Model

Menter and co-authors developed the Scale Adaptive Simulation (SAS) method [3], [27], [28] to simulate turbulent flows by using a two-equation model. When the SAS approach is coupled with the  $k-\omega$  SST model [5], it yields the SST-SAS turbulence model [3], [4], [29], [30]. The resulting equations for  $k$  and  $\omega$  are given by:

$$\frac{\partial k}{\partial t} + \langle u_j \rangle \frac{\partial k}{\partial x_j} = P_k - \beta^* k \omega + \frac{\partial}{\partial x_j} \left[ \Gamma_k \frac{\partial k}{\partial x_j} \right] \quad (4)$$

$$\begin{aligned} \frac{\partial \omega}{\partial t} + \langle u_j \rangle \frac{\partial \omega}{\partial x_j} &= \frac{\gamma}{\mu_t} P_k - \beta \omega^2 + \frac{\partial}{\partial x_j} \left[ \Gamma_\omega \frac{\partial \omega}{\partial x_j} \right] \\ + (1 - F_1) \frac{2}{\sigma_{\omega,2}} \frac{1}{\omega} \frac{\partial k}{\partial x_j} \frac{\partial \omega}{\partial x_j} &+ Q_{SAS} \end{aligned} \quad (5)$$

where  $F_1$  is a blending function and  $P_k$  is the production term of turbulence kinetic energy given by  $P_k = \nu_t S^2$  with  $S = \sqrt{2S_{ij}S_{ij}}$  and

$$S_{ij} = \frac{1}{2} \left( \frac{\partial \langle u_i \rangle}{\partial x_j} + \frac{\partial \langle u_j \rangle}{\partial x_i} \right). \text{ The constant } \beta^* \text{ is taken}$$

equal to 0.09 and  $\sigma_{\omega,2} = 1.168$  while the turbulent

diffusivities are expressed as  $\Gamma_k = \left( \nu + \frac{\nu_t}{\sigma_k} \right)$  and

$$\Gamma_\omega = \left( \nu + \frac{\nu_t}{\sigma_\omega} \right) \text{ where the value of } \sigma_k \text{ and } \sigma_\omega, \text{ just}$$

like  $\beta$ , result from a mix between the constants of the  $k-\varepsilon$  and  $k-\omega$  models. The SST-SAS model differs from the original SST model by the addition of the source term ( $Q_{SAS}$ ) in the transport equation for the turbulence eddy frequency  $\omega$ . In contrast, the equation for the turbulence kinetic energy  $k$  remains unchanged. The additional source term ( $Q_{SAS}$ ) is given as:

$$\begin{aligned} Q_{SAS} &= \max \left[ \xi_2 \kappa S^2 \left( \frac{L}{L_{vK}} \right)^2 \right. \\ &\left. - C_{SAS} \frac{2\rho k}{\sigma_\Phi} \max \left( \frac{1}{\omega^2} \frac{\partial \omega}{\partial x_j} \frac{\partial \omega}{\partial x_j}, \frac{1}{k^2} \frac{\partial k}{\partial x_j} \frac{\partial k}{\partial x_j} \right), 0 \right] \end{aligned} \quad (6)$$

where the model parameters are given by  $\xi_2 = 3.51$ ,  $\sigma_\Phi = 2/3$ ,  $C_{SAS} = 2$ ,  $\kappa$  is the von Karman constant. The turbulence length scale ( $L$ ) is calculated as:

$$L = \frac{\sqrt{k}}{0.25 \frac{c_\mu}{\omega}} \quad (7)$$

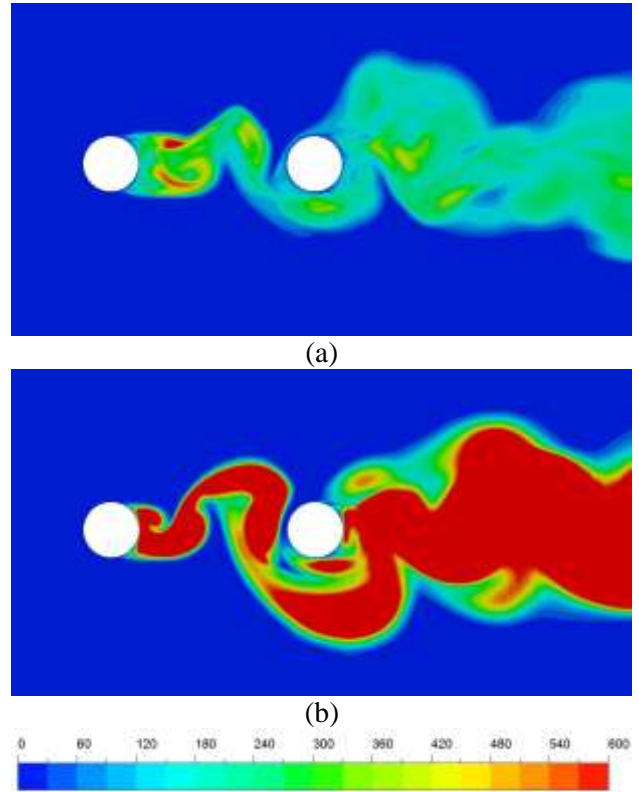


Fig. 1: Airflow past two circular cylinders arranged in tandem ( $Re = 1.66 \times 10^5$ ) - 2D contours snapshots of  $(\nu_t/\nu)$ : a) SST-SAS turbulence model and b)  $k-\omega$  SST turbulence model

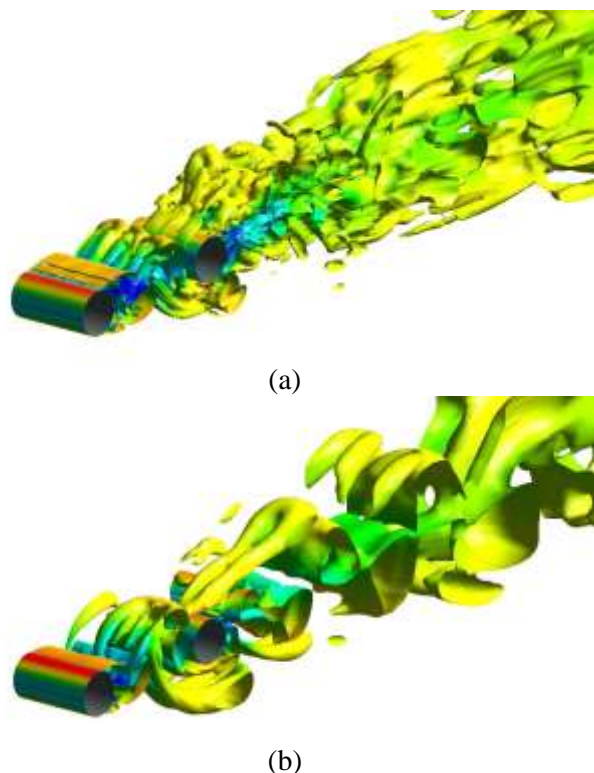


Fig. 2: Airflow past two circular cylinders arranged in tandem ( $Re = 1.66 \times 10^5$ ) - Snapshots of the  $Q$ -criterion iso-surface ( $Q = 1s^{-2}$ ) applied to the resolved velocity field: a) SST-SAS turbulence model and b)  $k-\omega$  SST turbulence model

The von Karman length-scale  $L_{vK}$  acts as a sensor to detect the flow unsteadiness susceptibility of the resolved velocity field, which is defined as:

$$L_{vK} = \kappa \frac{\frac{\partial \langle u_i \rangle}{\partial x_j} \frac{\partial \langle u_j \rangle}{\partial x_i}}{\left( \frac{\partial^2 \langle u_i \rangle}{\partial x_j^2} \right) \left( \frac{\partial^2 \langle u_j \rangle}{\partial x_i^2} \right)} \quad (8)$$

In flow regions where  $Q_{SAS}$  is sufficiently large thanks to large values of  $\left( \frac{L}{L_{vK}} \right)^2$ , the turbulent viscosity  $\nu_t \propto k/\omega$  experiences a dramatic reduction driven by the concomitant increase (resp. decrease) of  $\omega$  (resp.  $k$ ). This behavior is illustrated in Figure 1 for the flow past two cylinders in tandem at non-dimensional distance  $L/D = 3.7$  (see section 3.2 for an in-depth analysis of such a flow configuration). It can be seen that when compared to the level obtained with a simulation based on the

use of the sole  $k-\omega$  model (Figure 1-(b)), an almost sixfold decrease in the maximum level of the turbulent eddy viscosity is obtained when using the SST-SAS model (Figure 1-(a)). The direct consequence of this reduction is the presence of a significantly broader range of structures in the cylinder's wakes when using the SST-SAS model. This phenomenon can be qualitatively illustrated by displaying representative iso-surfaces of the  $Q$ -criterion ( $Q = 1/2(\Omega^2 - S^2)$ , where  $S$  is the strain rate and  $\Omega$  is the vorticity) obtained by processing two individual snapshots of the resolved flow fields. As depicted in Figure 2-(a), the presence of small-scale structures in the flow field is clearly visible in the snapshot of the resolved field obtained with the SST-SAS model whereas these small-scale structures are absent on the snapshot taken from the simulations with the standard  $k-\omega$  SST turbulence model (Figure 2-(b)).

### 3 Case Analysis and Discussion

Despite the great simplicity of its geometry, the configuration obtained by uniformly flowing at a velocity  $U_\infty$  a fluid of kinematic viscosity  $\nu$  past a circular cylinder of diameter  $D$  features quite a fascinating diversity of flow patterns and related dynamics as suggested by [31]. Since the beginning of the twentieth century, a great deal of studies focused on the characterization of the different flow regimes whose onset proved to be driven by the value of the Reynolds number defined as  $Re = U_\infty D/\nu$ . Still relevant today, the extensive review published in 1991 by [32] provided quite a complete panorama regarding the complexity of such a flow configuration. As recalled by [33], there exists three different flow regimes when progressively increasing  $Re$ : the subcritical regime ( $Re \leq 1.5-2 \times 10^5$ ), the supercritical regime ( $4-5 \times 10^5 \leq Re \leq 4-5 \times 10^6$ ) and the transcritical regime ( $Re \geq 4-5 \times 10^6$ ). [32], split the subcritical regime into not less than seven different sub-regimes and thanks to visualizations they explained the different underlying and differentiating mechanisms that led to such a classification of the subcritical regime. The interested reader is referred to the review by, [32] and the references therein for further explanations regarding the mechanisms at work in this kind of flow configuration. If additional complexity comes into play such as with the presence of confinement, [34], or of additional cylinders, then what was observed for the isolated 1-cylinder flow configuration has to be revisited to account for new mechanisms of interference. This is precisely such kind of situations that call for

numerical simulations to help explain and predict the outcome of such complex interference. Along these lines, the objective of this section is to highlight the capability of numerical simulations (in particular with the SST-SAS turbulence model) to help investigate three different flow past cylinder(s) configurations characterized by the specific nature of the interference to be dealt with, namely: a circular cylinder in proximity to a plane wall, circular cylinders in a free stream arranged in tandem and the flow through a staggered tube bundle.

### 3.1 The Flow over a Circular Cylinder in the Vicinity of a Plane Wall

A notable feature of the flow past a circular cylinder in the subcritical regime is the unsteadiness of the cylinder wake. Taking the form of a periodic vortex shedding, it leads to the continuous application of fluctuating forces exerted on the cylinder. However, when the cylinder is positioned close to a plane wall at a distance of  $G$ , the flow dynamics become more complex. In such a configuration, distinct changes in aerodynamic drag and lift forces are observed. There exists a critical gap ratio  $((G/D)_{crit})$  for which the suppression of vortices takes place. This phenomenon is primarily controlled by three key parameters: the Reynolds number ( $Re$ ), the boundary layer thickness ( $\delta$ ), and the gap ratio ( $G/D$ ). Various computational fluid dynamics methods employed to investigate such a flow configuration are now discussed. Let's start with [35], who studied the conditions for observing the suppression of the vortex shedding for a Reynolds number  $Re$  ranging from 80 to 1000. They solved the 2D Navier–Stokes equations by using a finite difference method. Their results showed that the critical gap ratio  $((G/D)_{crit})$ , at which the vortex shedding was suppressed was a decreasing function of the Reynolds number. [36], solved also the 2D Navier–Stokes equations but using a stream-function/vorticity formulation. For  $Re = 1200$  and  $G/D = 0.5$  and  $1.5$ , they found the calculated lift and drag coefficients and the predicted vortex shedding behavior match well with available experimental results. [37], employed the 2D Unsteady Reynolds-Averaged Navier Stokes (URANS) equations with the standard high Reynolds number  $k-\epsilon$  model at  $Re$  ranging from  $1 \times 10^4$  to  $4.8 \times 10^4$  with  $\delta/D = 0.14-2$ . They reported an under-prediction of hydrodynamic quantities ( $C_d$ ,  $C_l$ ,  $St$ , and  $C_p$ ) and attributed this to the intrinsic limitations of the  $k-\epsilon$  model for such a flow configuration. In a subsequent study, [38], investigated near-bed flow mechanisms around a marine pipeline close to a flat seabed at  $Re = 3.6 \times$

$10^6$ . The predicted hydrodynamic quantities were in satisfactory agreement with published experimental data. In their simulations at  $Re = 2 \times 10^4$ , [39], selected the  $k-\omega$  model. Their results exhibited good qualitative agreement with published experimental data. However, detailed comparisons with experimental results and discussions for  $G/D < 0.4$  were not provided. [40], used both URANS and the Detached-Eddy Simulation (DES) to simulate the flow around a circular cylinder positioned near a moving plane wall at  $Re = 4 \times 10^4$ . They found that DES proved superior to URANS in predicting the disappearance of vortex shedding as well as the time-averaged drag coefficients, the separation angles, and the velocity profiles in the near-wake region. The SST-SAS turbulence model was selected by [12], to conduct two-dimensional (2D) simulations around a circular cylinder positioned near a plane wall. The simulations considered factors such as wall proximity, boundary layer effects, and the variation of Reynolds number. Furthermore, three-dimensional (3D) simulations were also carried out to assess the importance of three-dimensional effects, [10]. Comparative analyses demonstrated a superior performance of the 3D simulations concerning the prediction of aerodynamic characteristics, and vortex shedding as well as the prediction of the critical values of  $((G/D)_{crit})$  at which the suppression of vortex shedding occurred. [41], shared a similar perspective, suggesting that 3D Large Eddy Simulation (LES) offers distinct advantages over the widely used 2D Reynolds-Averaged Navier-Stokes (RANS)  $k-\epsilon$  model [42], as well as over 2D LES. The 3D LES results offer more reliable integrated forces and better capture flow details for different values of  $G/D$ . Additionally, in [11], the results obtained with the SST-SAS turbulence model showed that  $(G/D)_{crit}$  decreased as  $Re$  was increased from  $8.6 \times 10^4$  to  $2.77 \times 10^5$ , a trend similar to that observed by [38]. However, in [10], the change in  $(G/D)_{crit}$  was associated more with the shift in flow regimes (from subcritical to critical) than with a change in the Reynolds number itself. On the other hand, the critical gap was not overly sensitive to the incident boundary layer thickness ( $\delta$ ) since for  $Re = 1.89 \times 10^5$ , the results showed that  $(G/D)_{crit}$  decreased from 0.3 to 0.2 when  $\delta/D$  was increased from 0.1 to 1.1. This trend was echoing the findings by [43] and [44].

### 3.2 Circular Cylinders Arranged in Tandem in a Free Stream

Placing more than one cylinder within the fluid stream leads to the so-called flow interference

regime. The tandem configuration corresponds to the case of two cylinders arranged in line in a crossflow. The wake of the upstream cylinder modifies the incoming flow conditions for the downstream cylinder, while this second cylinder interferes with the wake dynamics and vortex formation region of the upstream cylinder. [45], described this reciprocal impact as 'wake interference'. Depending on the distance between the cylinders, different flow behaviors occur around both cylinders that have significant effects on the vortice detachment and the resulting loads on the cylinders. The distance between the cylinders called the spacing is expressed as the ratio of the center-to-center distance  $L$  to the cylinder diameter, denoted as  $L/D$ . Particularly crucial is the critical spacing  $(L/D)_{crit}$  associated with the onset of the vortex shedding from the upstream cylinder.

Many computational studies of tandem cylinders in steady cross-flow have been undertaken. [46], used a fractional step method at  $Re$  varying from 100 to 200 to analyze the flow around multiple cylinders. The numerical simulation approach has been less effective compared to the experimental data, due to the intricacy of the flow across cylinders, [47]. [48], considered a laminar flow regime at  $Re = 100$  for a six-row inline tube bank. A critical spacing range between 3.0 and 3.6 was identified at which the mean drag as well as the RMS (root mean square) lift and drag coefficients for the last three cylinders reached their maximum values. In [49], a standard LES with the Smagorinsky subgrid-scale model was retained to explore the characteristics of the vortices shed from the circular tandem cylinders at  $Re = 2.2 \times 10^4$  and  $L/D$  varying from 2 to 5. They found that the critical spacing was about  $L/D = 3.25$  and the mean drag and fluctuating lift coefficients of each cylinder jumped to higher values for this critical spacing. [50], discussed the flow characteristics across tandem circular cylinders in the range of subcritical ( $Re = 2.4 \times 10^4$ ) and supercritical ( $Re = 3.0 \times 10^6$ ) regimes by numerical simulation at  $L/D$  ranging from 2 to 5 by means of improved delayed DES (IDDES) method. They demonstrated that for both Reynolds numbers, the vortex shedding occurred from both upstream and downstream cylinders as soon as  $L/D \geq 3.5$ . Moreover, the fluctuating lift coefficients of the upstream cylinder were almost independent of  $Re$ , but those of the downstream cylinder dropped as  $Re$  was increased. In [51], Delayed Detached Eddy Simulations (DDES) were used to simulate the flow around tandem circular cylinders at  $L/D = 3.7$  and  $Re = 1.66 \times 10^5$ . Simulations were performed on a (relatively) coarse

grid containing about 31 million grid points, and on a fine grid containing about 133 million grid points. The conclusion drawn was that some of the fine grid DDES results were not significantly different from those obtained with the coarse grid DDES. [52], simulated the flow interference between tandem cylinders based on the hybrid RANS/LES methods with non-linear eddy viscosity formulations at  $Re = 1.66 \times 10^5$  for  $L/D = 1.4, 3, \text{ and } 3.7$ . The presence of a bistable wake between the cylinders and the subsequent drag inversion on the downstream cylinder was noted at  $L/D = 3$ . Additionally, it was observed that the bistable wake resulted in an elevation of the turbulent kinetic energy level within the gap between the cylinders.

The evaluation of the SST-SAS model's performance was conducted in the analysis of the flow around two circular cylinders of identical diameter arranged in tandem at a high subcritical Reynolds number ( $Re = 1.2 \times 10^5$ ) by [13]. Additionally, [53], employed a numerical model that combines Reynolds-Averaged Navier-Stokes (RANS) and Large Eddy Simulation (LES) to simulate the flow around two tandem cylinders at  $Re = 1.66 \times 10^5$  for  $L/D = 3.7$ . In this study, the results obtained with the SST-SAS model were utilized only for comparative purposes. In [13], interference effects for distances  $L/D$  varying from 1.1 to 7 were explored by comparing them with those obtained for the flow around a single isolated cylinder. The results under-predicted the mean drag coefficient for the upstream cylinder, while that for the downstream cylinder provided they were in satisfactory agreement with their experimentally obtained counterparts. A critical spacing value of  $(L/D)_{crit} = 3$  and the flow patterns associated with the bistable flow, [54], were also observed.

### 3.3 Staggered Tube Bundle

The flow through bundles of cylinders has been mostly investigated in the context of heat exchanger design and analysis. This configuration exhibits a vortex shedding behavior quite similar to that observed for the flow past a single cylinder but with the added complexity of strong interactions between the wakes of the tubes. This configuration represents quite a challenging test case for any existing model or newly derived model. Indeed, many researchers have simulated this configuration using a broad range of approaches, from RANS models to Direct Numerical Simulation (DNS). For validation purposes, many of these studies used the experimental data obtained in [55], [56], [57], for the configuration of water flowing through a staggered tube bundle array at  $Re = 18000$ .

[58], examined the turbulent flow through a tube bundle at a Reynolds number of 9300, both experimentally and numerically. They closed the steady RANS equations by using four different turbulence models:  $k-\varepsilon$ ,  $k-\omega$ , SST, and the Reynolds Stress Model (RSM). The Reynolds normal stresses approximated from the  $k-\omega$  and SST models demonstrated a closer agreement with experiments than those obtained from the RSM model. However, these RANS simulations failed to provide reliable predictions for this flow due to the poor estimation of the turbulence kinetic energy behavior. [59], applied RANS and URANS simulations to predict the experiments in [55], [56], [57]. URANS simulations using a Reynolds stress model (RSM) exhibited better agreement with experimental data than the 2-equation model, although some discrepancies persisted, particularly when it came to reproducing the Reynolds normal stress behavior. [60] and [61], investigated the same flow configuration as [59], and reached similar conclusions when comparing the results of RANS and URANS simulations. [62], employed LES and a  $k-\varepsilon$  model to simulate experiments configuration in [55], [56], [57]. They reported well-predicted mean velocity profiles in both cases. However, in the wake region, the  $k-\varepsilon$  model provided a poorer quality of prediction of the Reynolds stresses compared to LES. [63], utilized LES, coarse LES, and RSM-based URANS approaches to model the flow in [55], [56], [57], at a Reynolds number of 9000. They reported that both the LES and RSM-based URANS approach provided satisfactory results compared to experiments, with the former being slightly more consistent with DNS results. A study by [64], employed Partially Filtered Navier–Stokes (PANS) and LES, reporting that both methods predicted the flow with relatively good agreement with experimental data, although PANS simulation was conducted on a much coarser grid than LES. [65], used 3D DNS to predict experiments in [55], [56], [57], at a lower Reynolds number ( $Re = 6000$ ) to limit the computational cost. The results were in good agreement with the experiments. Additionally, [66], performed DNS simulations of the flow through a staggered tube bundle over the range  $1030 \leq Re \leq 5572$ . One of their objectives was to determine the Reynolds number value at which transition occurs at the matrix transition point e.g. the point at which the second frequency peak becomes prominent in the spectral signature of the vortex shedding. They observed that such a transition occurred at  $Re \approx 3000$ , a value similar to that observed for the transition for the single-cylinder flow configuration.

The study by [18], delved into the predictive capabilities of the SST-SAS turbulence model. They simulated the flow configuration in [55], [56], [57]. Their results proved to be quite satisfactory when compared with the experimental data in terms of both mean velocity components and turbulence quantities. The study introduced a quantitative objective scoring criterion, utilizing relevant norms to compare the SST-SAS results with those obtained from other models in the literature. The comparison revealed that the SST-SAS model presented a remarkable consistency in its predictive capability, ranking among the top-performing models in agreement with experimental data. Moreover, in [18], an in-depth analysis of the Reynolds stress tensor's behavior was conducted for unsteady URANS models. The analysis utilized the triple decomposition of the instantaneous velocity field. The findings indicated that, in the case of the SST-SAS model, the contribution of time-resolved motion to the total velocity correlations was significantly higher when compared to other URANS models, reaching levels exceeding 95 %.

## 4 Wall-mounted Cylinder

“The more available experimental data, the better for simulation validation” is the motto behind the choice of building up a new experiment on turbulent flows over a wall-mounted cylinder to create a database that will be subsequently made available in open access. The configuration represents a distinctive case where the cylinder encounters the flow passage from only one side. The experimental and numerical results reported here are restricted to a low Reynolds subcritical flow at  $Re = 2300$  based on the diameter of the cylinder  $D = 0.04 \text{ m}$ , the kinematic viscosity of air  $\nu = 1.53 \times 10^{-5} \text{ m}^2/\text{s}$ , and the bulk velocity  $U_{bulk} = 0.88 \text{ m/s}$ .

### 4.1 Experimental Set-Up and Metrology

The MAVERIC test facility installed on the premises of LMAP (CNRS/Pau University, France) for studying effusion cooling flows, [67], [68], was updated to accommodate a specifically designed test section housing a removable cylinder of the circular cross-section. A side view of the test section fitted with the cylinder is displayed in Figure 3. The rig consists basically of two 2.5 m-long superimposed separate channels of identical rectangular cross-section (width  $W = 400 \text{ mm}$  x height  $H = 120 \text{ mm}$ ) followed by the Plexiglas-made test section. Each channel is fed in air by a dedicated centrifugal fan powered by a 1-KW electrical motor regulated in



rotation by a Siemens Micro-Master MC420 controller. The test section which accommodates the plate supporting the removable cylinder in the upper channel is followed by the exhaust section which evacuates outside the airflow through the lateral wall of the laboratory. A two-component planar particle image velocimetry (PIV) LaVision system combined with computer-controlled translation stages permitted to selection the desired image plane by accurately displacing the Imager Pro X CCD recording camera (1600 pixels  $\times$  1200 pixels, intensity range over 14 bits, 50 mm lens, f-number = 4). The airflow was seeded with Di-Ethyl-Hexyl-Sebacat (DEHS) particles of 1  $\mu\text{m}$  of average diameter. A double-pulse Nd-Yag laser combined with divergent optics produced a divergent laser sheet (wavelength = 532 nm, thickness of the sheet  $\approx$  1 mm) introduced normally in the flow through the top wall of the test section (Figure 3).

All the measurements were made in the mid-plane of the channel. Twelve hundred double-frame recordings featuring a 10-pixel/mm resolution were acquired for three different streamwise positions of the camera to cover a flow region extending from 6  $D$  upstream to 6  $D$  downstream of the cylinder. The number of recordings was chosen to ensure the convergence of the estimator of the average of the two velocity components. The recordings were first pre-processed by i) subtracting the background images obtained by firing the lasers without seeding the flow and ii) normalizing the particle intensity. Then, these pre-processed recordings were successively processed by a multi-pass cross-correlation algorithm (LaVision Davis Software 8.4.0) using interrogation windows of decreasing size from 96 pixels  $\times$  96 pixels down to 32 pixels  $\times$  32 pixels.

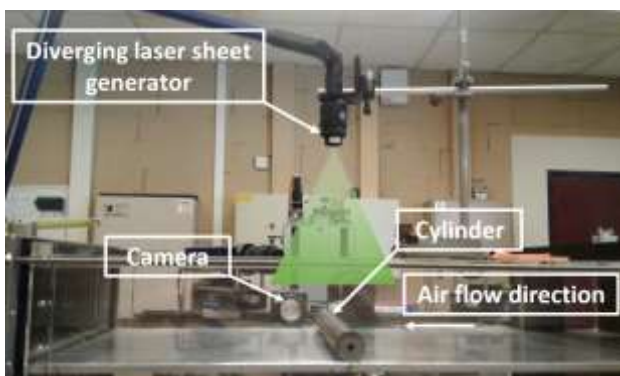


Fig. 3: Wall-mounted cylinder - Side view of the test section of the MAVERIC rig and some components of the PIV system

## 4.2 Numerical Set-Up

The numerical solver used in this research was the commercial CFD code Ansys Fluent 15, in line with [69]. This code employs the finite volume cell-centered method to solve the governing equations describing fluid motion in a segregated manner. Spatial discretization of these equations was performed on three-dimensional structured grids generated with ICEM CFD. Convection terms were discretized using a bounded central differencing scheme, while pressure and turbulent quantities ( $k$  and  $\omega$ ) were evaluated with a second-order scheme. Further, the equations were discretized in time using a bounded second-order implicit scheme. The pressure-velocity coupling was managed using the SIMPLE (Semi-Implicit Method for Pressure-linked Linked Equations) algorithm, [70]. Results from [71], utilizing the SST-SAS turbulence model demonstrated that SIMPLE exhibits acceptable performances in resolving unsteady turbulent flow around a circular cylinder, requiring less computational time compared to the SIMPLEC [72] and PISO [73] approaches.

### 4.2.1 Boundary Condition

Figure 4 depicts a schematic of the computational domain and of the boundary conditions employed. Inlet conditions for this investigation are established using a velocity profile outlined in Eq. (9). The resulting profile is incorporated as an input condition through the User-Defined Function (UDF) provided by the code. At the outlet, a reference zero pressure condition is applied. For the upper and lower limits of the domain, a no-slip wall condition is specified. The same condition of zero velocity on the wall is applied to the surface of the cylinder. Lastly, at the lateral limits (normal to the  $x$ - $y$  plane), periodicity conditions are imposed, considering that we are dealing with a reduced 2D model corresponding to the length of the cylinder.

$$U_{(y)} = \begin{cases} \text{if } y < 0.052 & U_{bulk} \left( \frac{y}{0.06} \right)^{0.2} \\ \text{if } 0.052 \leq y \leq 0.068 & 0.98 U_{bulk} \\ \text{if } y > 0.068 & U_{bulk} \left( \frac{0.12-y}{0.06} \right)^{0.13} \end{cases} \quad (9)$$

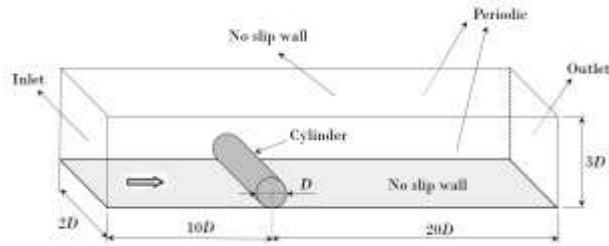


Fig. 4: Flow around a wall-mounted circular cylinder at  $Re = 2300$  - Schematic of the computational domain and boundary conditions used for the simulations. The diameter of the cylinder is  $D = 40\text{ mm}$

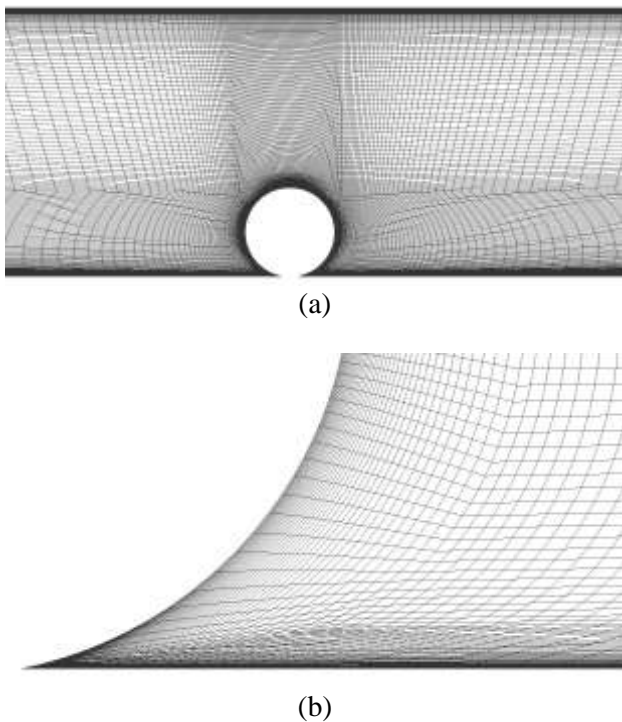


Fig. 5: Flow around a wall-mounted circular cylinder at  $Re = 2300$  - 2D cutting view of the 3D structured mesh: a) Overview of the mesh and b) Detail at the intersection between the supporting wall and the cylinder surface

#### 4.2.2 Mesh

The three-dimensional mesh is generated by extending the two-dimensional mesh (Figure 5) in the  $z$  direction, spanning it over a distance equal to twice the cylinder diameter. Figure 5-(a) provides an overall view of the mesh which featured refinement near the cylinder surface and at the level of the upper and lower limits of the domain. This refinement was crucial for accurately capturing the boundary layer on these surfaces, ensuring that the normal distance to the wall of any wall-adjacent cell satisfied  $y^+ < 1$ . Figure 5-(b) illustrates how the

structured mesh was adapted to reproduce accurately the acute angle formed between the bottom of the cylinder and the supporting wall.

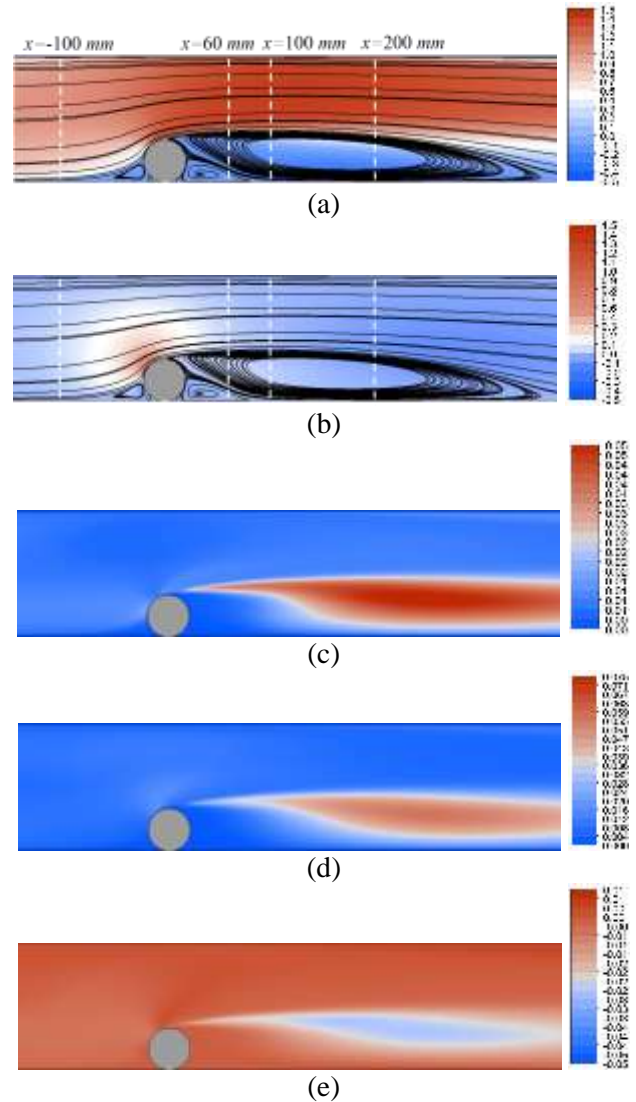


Fig. 6: Flow around a wall-mounted circular cylinder at  $Re = 2300$  - Contours of the velocity field ( $m/s$ ) and average Reynolds stress fields ( $m^2/s^2$ ); (a) streamwise component of the velocity; (b) normal component of the velocity; (c) longitudinal Reynolds stress  $R_{xx}$ ; (d) normal Reynolds stress  $R_{yy}$ ; (e) shear Reynolds stress  $R_{xy}$

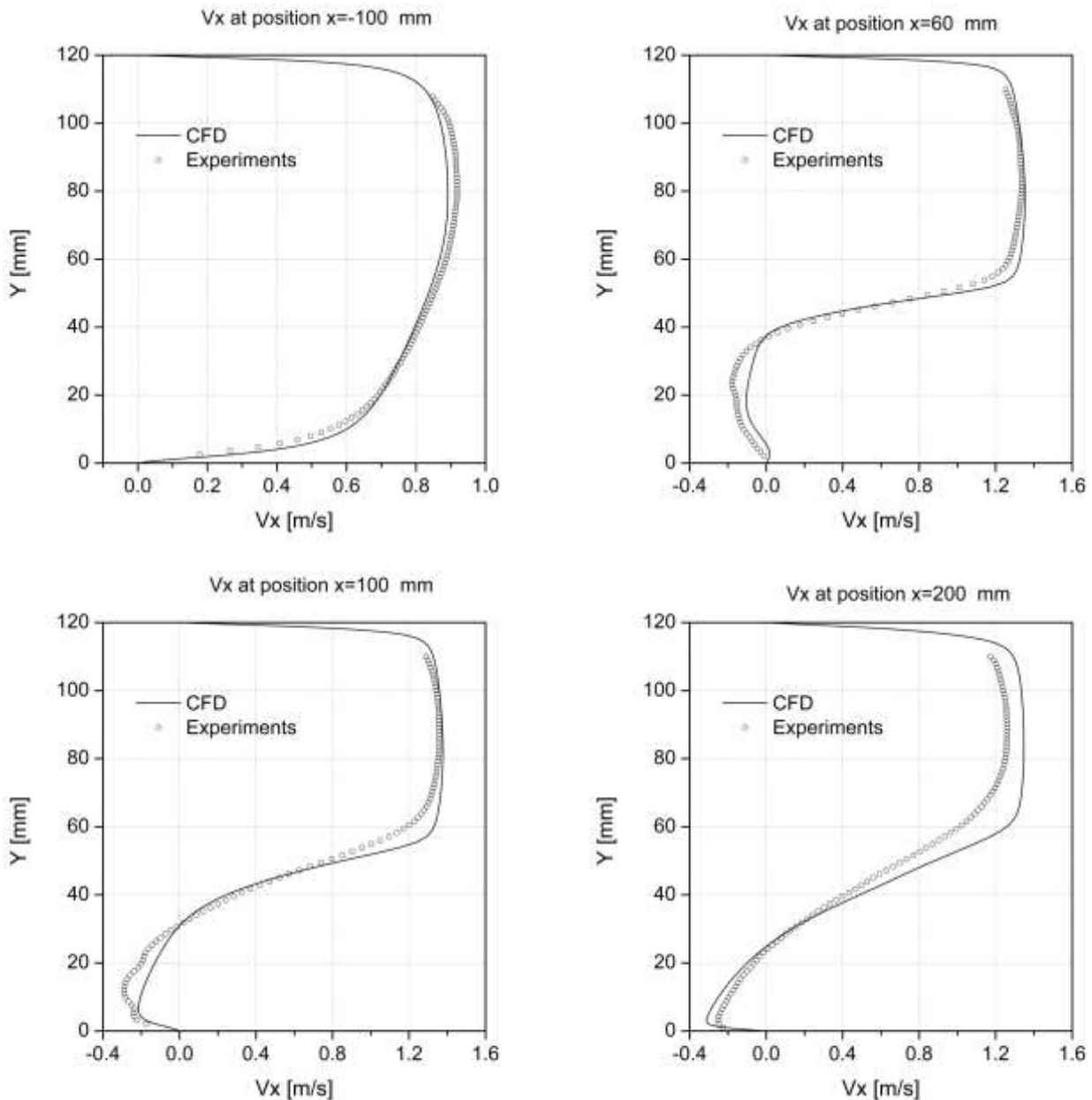


Fig. 7: Flow around a wall-mounted circular cylinder at  $Re = 2300$ . Profiles of the time average of the streamwise velocity component at four vertical cross-sections. Upper left: upstream position at  $x = -100$  mm ( $x/D = -2.5$ ). Upper right: downstream position at  $x = 60$  mm ( $x/D = 1.5$ ). Lower left: downstream position at  $x = 100$  mm ( $x/D = 2.5$ ). Lower right: downstream position at  $x = 200$  mm ( $x/D = 5$ )

### 4.3 Illustration of the Average Flow Field

The simulated flow field is initially illustrated by presenting the time average of the fields of the two velocity components,  $V_x$  (Figure 6-(a)) and  $V_y$  (Figure 6-(b)), along with the fields of three components of the Reynolds stress tensor (Figure 6-(c) to 6-(d)).

In both time averages of the resolved fields of  $V_x$  and  $V_y$ , a small recirculation zone can be observed e.g. where the streamlines approaching the cylinder appear to bifurcate. One part of the flow is directed towards the upper surface of the cylinder,

while the other part is oriented towards the wall, hence delimitating a recirculation zone. The flow bifurcation point and the recirculation zone closely resemble those obtained by PIV for a cylinder in contact with a plane wall at  $Re = 3000$  by [74] (refer to Figure 2 in their study). It is worth stressing that in [74], was visualized the flow only in the region in front of and above the cylinder, making a direct comparison challenging for the recirculation region generated behind the cylinder. Nevertheless, a comparison is feasible for the region behind the cylinder with the PIV data obtained by [75], at  $Re =$

5000. Although the Reynolds number is slightly different, it's apparent that the main recirculation and the recirculation generated just behind the cylinder and the lower limit (Figure 6-(a) and (b)) are highly similar to those obtained for  $Re = 5000$  (Figure 2 in [75]).

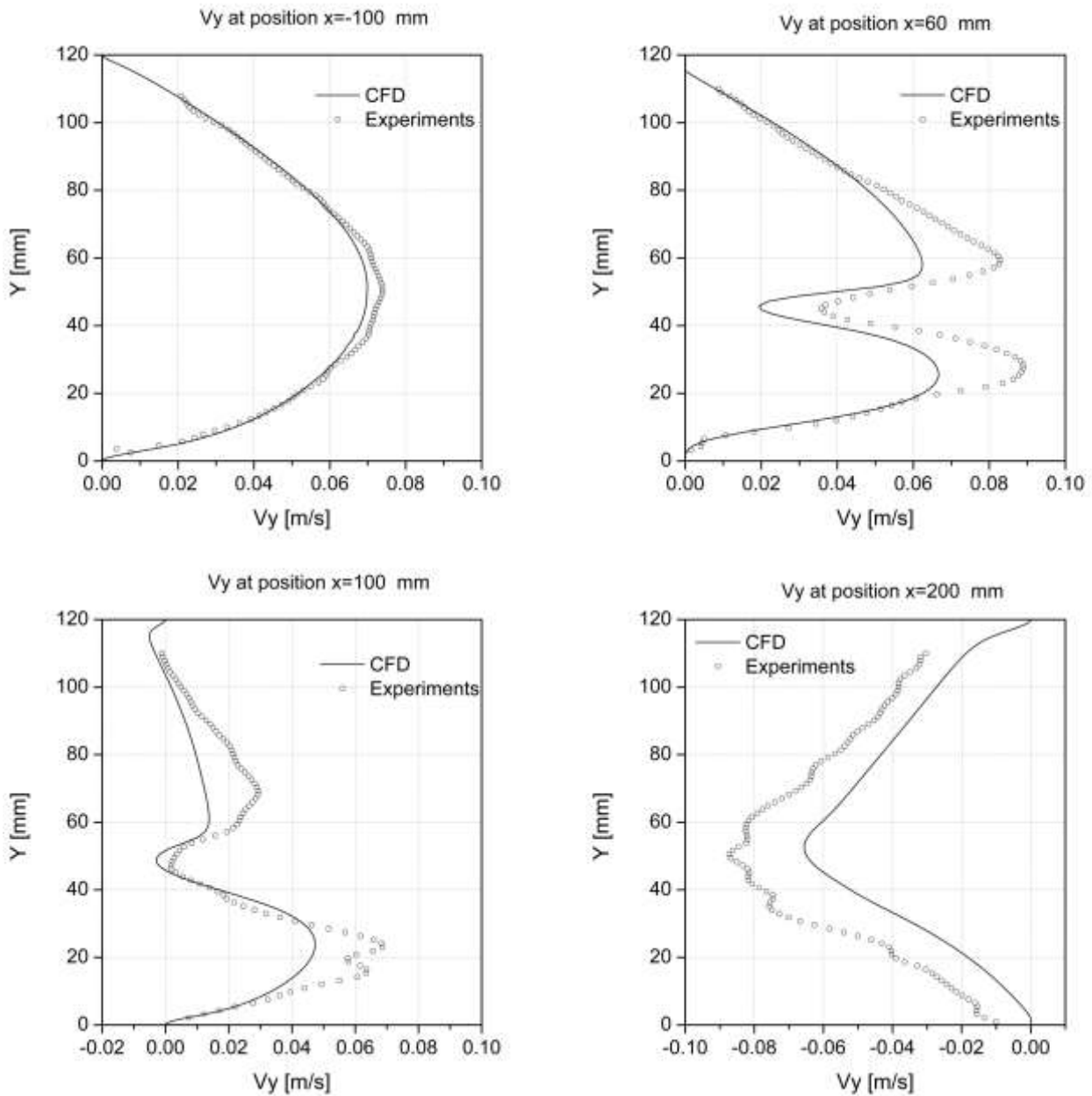


Fig. 8: Flow around a wall-mounted circular cylinder at  $Re = 2300$ . Profiles of the time average of the normal velocity component at four vertical cross-sections. Upper left: upstream position at  $x = -100$  mm ( $x/D = -2.5$ ). Upper right: downstream position at  $x = 60$  mm ( $x/D = 1.5$ ). Lower left: downstream position at  $x = 100$  mm ( $x/D = 2.5$ ). Lower right: downstream position at  $x = 200$  mm ( $x/D = 5$ )

#### 4.4 Preliminary Comparison of PIV vs CFD Results

The normal profiles of the streamwise and the normal components of the velocity and their experimentally obtained counterparts are shown in Figure 7 and Figure 8 at four different abscissas. The corresponding vertical cross-sections are materialized by vertical dashed cutting lines in Figure 6-(a) and (b). The prediction of the velocity component profiles with SST-SAS proved to be quite satisfactory when compared to their experimental counterpart. Indeed, the profiles of the velocity streamwise component ( $V_x$ ) are very well predicted by the SST-SAS calculations for the three positions at  $x = 60, 100, \text{ and } 200 \text{ mm}$  which represent the recirculation zone downstream of the cylinder. Regarding the normal velocity component  $V_y$ , the comparison is qualitatively good but features some significant discrepancies indicating that the predicted and the measured recirculation zones might have slightly different dimensions. The use of the triple decomposition of the instantaneous velocity field, [18], showed that the contribution of the resolved part of the motion to the total Reynolds stress was negligible. In simpler terms, the velocity unsteadiness is dampened, resulting in a fully steady state for the flow. Consequently, for this flow configuration, the  $Q_{SAS}$  term does not play a determinant role as observed in the preceding cases indicating that the standard  $k-\omega$  SST model is recovered in this case.

## 5 Conclusion

This review strongly supports the notion that the SST-SAS model is a highly relevant choice for simulating unsteady flows around bluff bodies. From both a qualitative and quantitative points of view, the predictive capacity of SST-SAS based simulations proved to be quite superior to those provided by standard RANS models and to match at quite an affordable cost those obtained by the most advanced simulation tools such as the family of LES based approaches. However the world of turbulence modeling is far from being frozen as new “competitors” are continuously emerging. This is the case of the so-called hybrid temporal LES (HTLES) advocated by Manceau and his group [76], [77]. In its version based on the SST-SAS model on a modification of the  $k-\omega$  SST model, the HTLES provides quite a sound alternative to the SST-SAS approach. Comparing the performances of both approaches will be one of the topics of our future activity as well as the enrichment and publication of

the PIV database for the configuration of the flow past wall-mounted cylinder(s).

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The authors equally contributed to the present research, at all stages from the formulation of the problem to the final findings and solution.

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### **Conflict of Interest**

The authors have no conflicts of interest to declare.

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