

Modeling of seismoelectric effects in the low frequency regime for field survey applications, American Geophysical Union/Advancing Earth And Space Sciences

Arjeta Heta, Hélène Barucq, Julien Diaz, Christina Morency

▶ To cite this version:

Arjeta Heta, Hélène Barucq, Julien Diaz, Christina Morency. Modeling of seismoelectric effects in the low frequency regime for field survey applications, American Geophysical Union/Advancing Earth And Space Sciences. AGU 2023 - American Geophysical Union / Advancing Earth And Space Sciences, Dec 2023, San Francisco (CA), United States. 2023. hal-04394440

HAL Id: hal-04394440 https://inria.hal.science/hal-04394440v1

Submitted on 15 Jan 2024

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.







Lawrence Livermore National Laboratory

Modeling of seismoelectric effects in the low frequency regime for field survey applications, American Geophysical Union/Advancing Earth And Space Sciences

Arjeta Heta 1,2 , Hélène Barucq 1,2 , Julien Diaz 1,2 , Christina Morency 3 ¹ Inria Bordeaux Sud-Ouest, Pau, France ² Université de Pau et des Pays de l'Adour, Pau, France ³ Lawrence Livermore National Laboratory, Livermore, CA, USA 1 arjeta.heta@inria.fr, 1 helene.barucq@inria.fr, 1 julien.diaz@inria.fr, 3 morency1@llnl.gov



SEE4GEO Introduction

A conductive porous medium excited by a seismic wave is the scene of complex physical phenomena known as seismo-electric effects. Understanding them opens new prospects for imaging geological objects invisible to seismic imaging. Their modeling began with the equations proposed by Pride in the 90s, which are constructed by coupling Maxwell's equations with Biot's wave equations. The coupling terms are written in terms of a frequency-dependent operator, which poses a major difficulty in the time domain, as it is an integral Fourier operator whose discretization is not trivial, especially as it must also consider the co-existence of waves propagating a thousand times faster than seismic waves.

Pride's equations for seismoelectric effects

Pride's equations Pride (1994) and Haartsen and Pride (1994) model SEE by coupling Maxwell's (electromagnetics) and Biot's (elastodynamics) equations. Here, we consider only the seismo-electric coupling.

$$i\omega \rho_{a}\dot{\mathbf{u}}_{s}+i\omega \rho_{f}\dot{\mathbf{w}}=\nabla\cdot\boldsymbol{\tau}+f_{u} \quad \text{Poroelastic} \\ i\omega p=-M\nabla\cdot\dot{\mathbf{w}}-M\alpha:\epsilon(\dot{\mathbf{u}}_{s}) \quad \text{constitutive laws} \\ i\omega\boldsymbol{\tau}+i\omega\alpha p=\mathbf{C}:\epsilon(\dot{\mathbf{u}}_{s}) \\ i\omega\delta_{0}\mathbf{E}=\nabla\times\mathbf{H}-\mathbf{J}+\mathbf{f}_{C} \quad \text{Dynamical} \\ i\omega\mu_{0}\mathbf{H}=-\nabla\times\mathbf{E} \quad \text{equations} \\ i\omega\rho_{f}\dot{\mathbf{u}}_{s}+i\omega\rho_{dyn}(\omega)\dot{\mathbf{w}}=-\nabla\mathbf{p}+i\omega\rho_{dyn}(\omega)\underline{\mathbf{E}}(\omega)\mathbf{E}+f_{\omega} \quad \text{Transport} \\ \mathbf{J}=\sigma\mathbf{E}-\underline{L}(\omega)(\nabla p+i\omega\rho_{f}\dot{\mathbf{u}}_{s}) \quad \text{equations}$$

Pride's equations are solved in time in Morency and Tromp (2008) and Morency (2020):

$$\rho \partial_t^2 \mathbf{u}_s + \rho_f \partial_t^2 \mathbf{w} = \nabla \cdot \mathbf{T} + \mathbf{F}$$

$$\eta k^{-1} \partial_t \mathbf{w} + \frac{\rho_f c}{\phi} \partial_t^2 \mathbf{w} + \rho_f \partial_t^2 \mathbf{u}_s = \nabla \cdot \mathbf{T}_f + \mathbf{F}$$
Biot's
$$\mathbf{T} = (B \nabla \cdot \mathbf{u}_s + C \nabla \cdot \mathbf{w}) \mathbf{I} + 2\mu_{fr} \mathbf{D}_s$$

$$\mathbf{T}_f = -p_f \mathbf{I} = (C \nabla \cdot \mathbf{u}_s + M \nabla \cdot \mathbf{w}) \mathbf{I}$$

$$\epsilon \partial_t^2 \mathbf{E} = \nabla \cdot (\partial \tilde{\mathbf{H}}) - \sigma \partial_t \mathbf{E} - \partial_t \mathbf{j}_s$$

$$\partial_t \tilde{\mathbf{H}} = \tilde{\mu}^{-1} : \nabla \mathbf{E}$$

$$\mathbf{j}_s = \underbrace{Q_v k \eta^{-1}}_{L_0} (\nabla \cdot \mathbf{T}_f - \rho_f \partial_t^2 \mathbf{u}_s + \mathbf{F})$$
Maxwell's
equations

Frequency dependent coupling

Electrokinetic (Maxwell-Biot coupling) coefficient $L(\omega)$:

$$L(\omega) = L_0 \left(1 - i \frac{m \omega}{4 \omega_t} \right)^{-1/2} \quad \text{with} \quad L_0 = \frac{\phi \epsilon_0 \epsilon_r^f \zeta^p}{\alpha_\infty \eta} \underbrace{\left(1 - 2 \frac{d^l}{\lambda} \right)}_{\approx 1}$$

In time domain, Pride's equations are solved with $L(\omega) \simeq L_0$. This is a low-frequency approximation that only applies to field-type simulations. We show that, at frequencies encountered in laboratory experiments (>20kHz), the effect of frequency on coupling is too significant to be neglected. Frequency-dependent coupling is very difficult to account for in time domain as L(t) is a Fourier integral operator global in time and space (inverse Fourier):

$$LE(\vec{x},t) = L_0 \int_{\mathbf{R}} (1 - i\frac{\omega}{\omega_t})^{-1/2} \widehat{E}(\vec{x},\omega) e^{i\omega t} d\omega$$
 (1

Simplified frequency dependent coupling operators introduced in Heta, Barucq, and Diaz (2022) can be used. In polynomial or rational form, the equivalent time domain equations are simple to obtain. For ω/ω_t small enough,

$$L(\omega) \simeq \mathcal{L}_n(\omega) = L_0 \prod_{j=1}^n \left(1 - ic_j^{(n)} \frac{m\omega}{4\omega_t} \right) / \left(1 - ib_j^{(n)} \frac{m\omega}{4\omega_t} \right)$$

where

$$b_j^{(n)} = \cos\left(\frac{j\pi}{2n+1}\right)^2, \quad c_j^{(n)} = \sin\left(\frac{j\pi}{2n+1}\right)^2, \quad a_j^{(n)} = \frac{2c_j^{(n)}}{2n+1}$$

Modeling of the problem

$\overline{\mathbf{u}_s}$	solid displacement
\mathbf{W}	fluid displacement
p	fluid pressure
au	stress tensor
Ε	electric density field
Н	magnetic intensity field
J	electric current density

Table 1 – Unknowns

Table 2 – Porous sub-soil physical parameters ρ_a , ρ_f , ρ_{dyn} averaged, fluid, dynamic densities effective stress tensor exterior forces f_u, f_w, f_C coupling coefficient stiffness tensor $\epsilon(u)$ strain tensor fluid-solid coupling modulus

conductivity

 δ_0 , μ_0

electric factor and permeability

frame shear modulus macroscopic source solid strain deviator bulk density fluid viscosity fluid permeability B,C,M Biot coefficients Tortuosity

Table 3 – Porous sub-soil physical parameters

RESULTS & DISCUSSION

T total stress

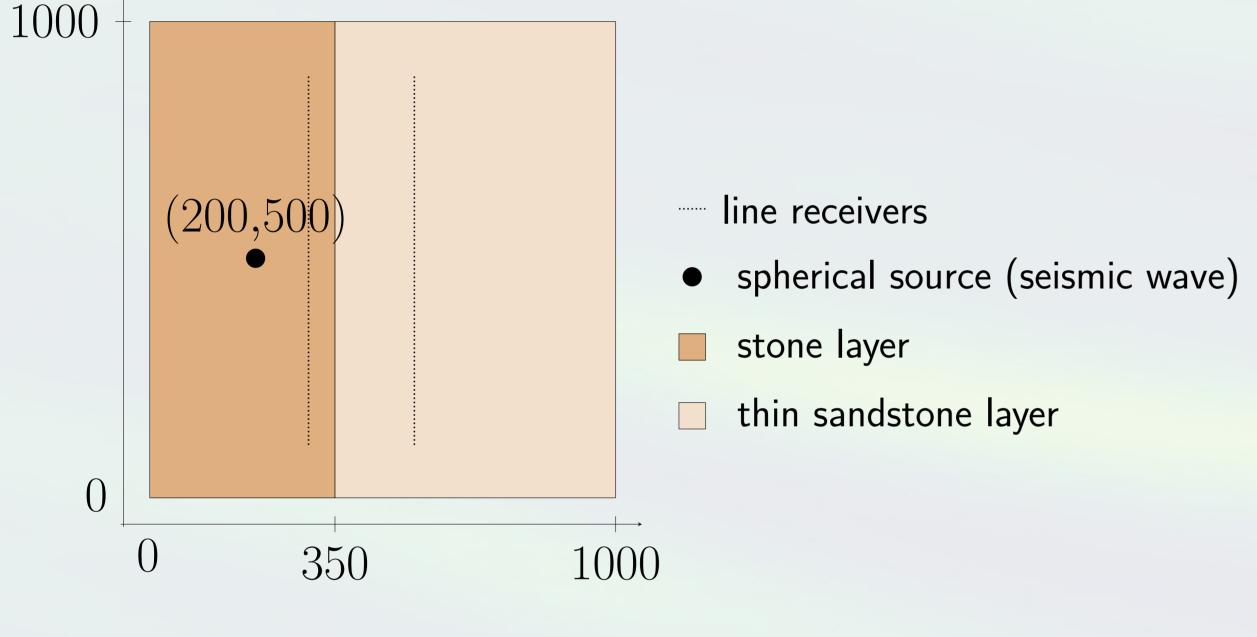
 \mathbf{T}_f fluid stress

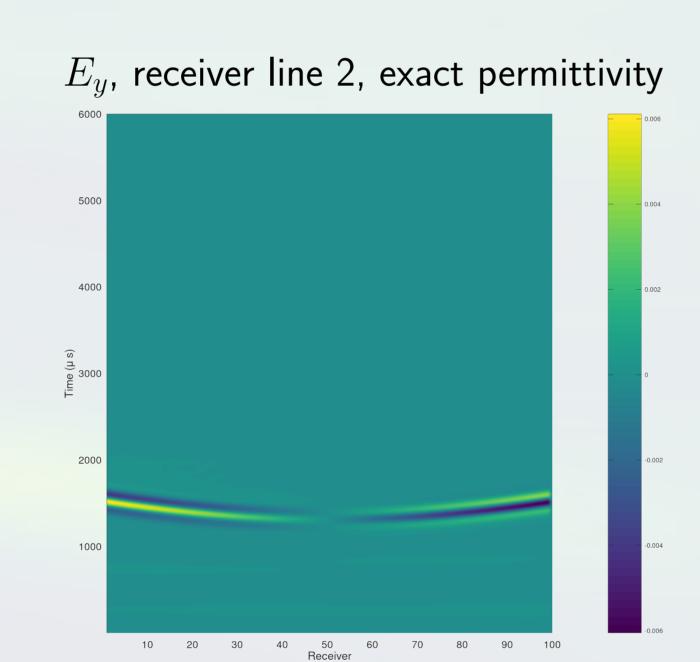
It has been shown in Heta, Barucq, and Diaz (2022) that $L(\omega)\simeq L_0$ is a good approximation of cut-off frequency ω_t . For comparison with the time-domain equations using L_0 , we use $L(\omega) = L_0$. The frequency-domain equations are solved using the Hybridizable Discontinuous Galerkin method with the solver hou10ni(Figure 2).

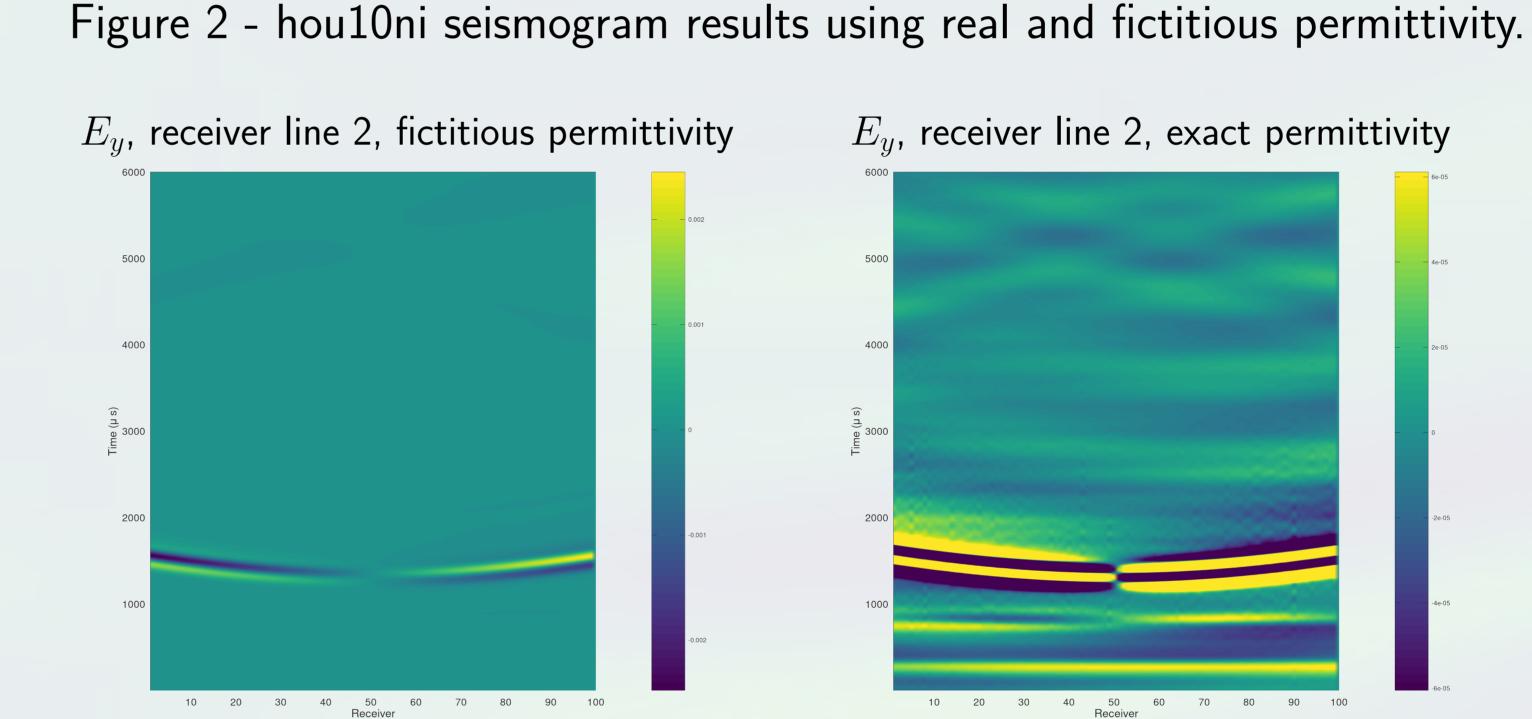
The use of a fictitious permittivity $\epsilon \simeq 7.965 \cdot 10^{-4}$ Fm $^{-1}$ to address the diffusive nature of the EM signal has been introduced with success in e.g. Maaø (2007) and Mittet (2010) to carry out time-domain simulations valid on a field scale. The time-domain equations are solved using the Spectral Element Method with the solver SPECFEM(Figure 3).

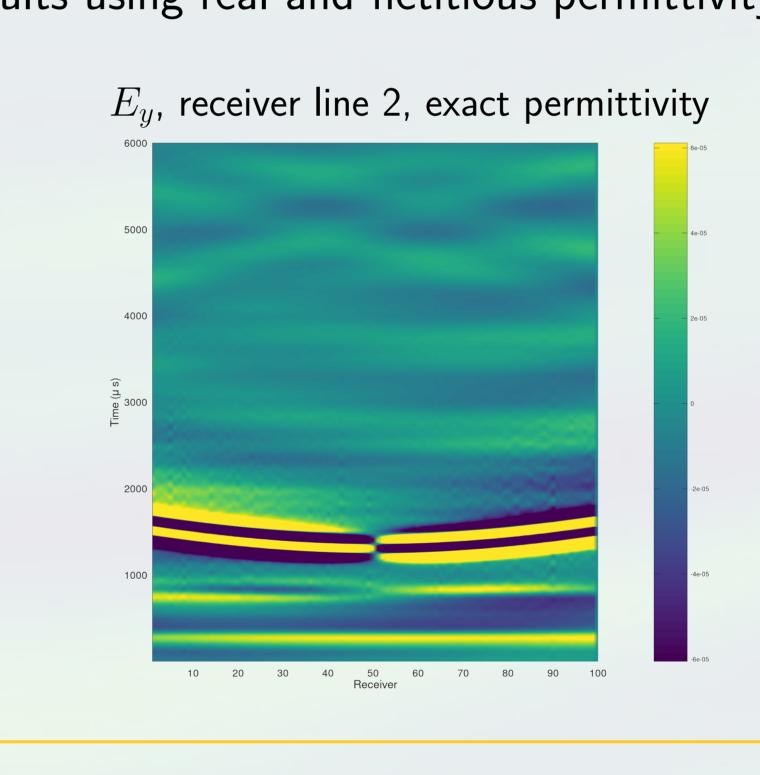
Using a discrete inverse Fourier transform, seismograms are computed from a frequency sweep. These results are compared to the solutions computed directly in time domain.

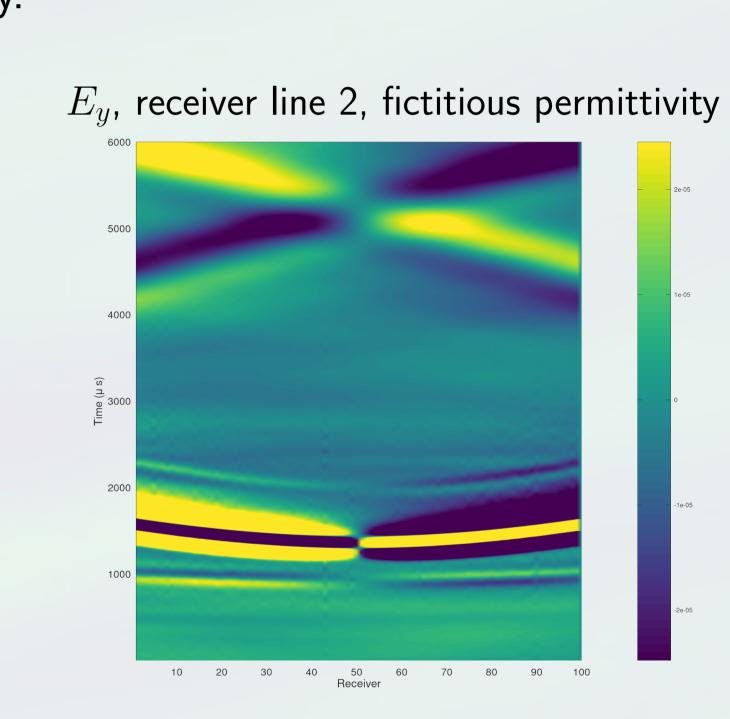
Figure 1 - Simulation domain at the field scale.











Observations

- Results with true and with fictitious permittivity are very similar in frequency domain, consistent with time domain findings.
- SPECFEM was run with 150000 time steps. hou10ni results were computed on fine meshes but for 400 distinct frequencies up to 400Hz.
- In frequency domain, only the source and reflected wave are visible in E_y . In time domain, the converted wave is visible in domain 2 (arrives at $t \simeq 180 \mu s$).
- Despite the higher resolution of the time domain computations, arrival times coincide with the two methods.

Conclusion

A use of a fictious permittivity allows to compute solutions in time but it modifies the behaviour of the converted wave. The comparisons between our solvers, one in time(SPECFEM) and the other one in frequency(Hou10ni), show a quite good consistency regarding the field V and the co-seismic wave. We have a perfect arrival time but the amplitudes do not match.

References

- HAARTSEN; PRIDE. Modeling of coupled electroseismic wave propagation from point sources in layered media. In: SEG Technical Program Expanded Abstracts 1994. [S.I.]: Society of Exploration Geophysicists, 1994. p. 1155–1158.
- HETA, A.; BARUCQ, H.; DIAZ, J. Approximate Coupling Terms in Seismoelectric Theory: from Frequency Domain to Time Domain. In: AGU22-AGU Fall Meeting **2022**. [S.l.: s.n.], 2022.
- MAAØ, F. A. Fast finite-difference time-domain modeling for marine-subsurface electromagnetic problems. Geophysics, Society of Exploration Geophysicists, v. 72, n. 2, a19-a23, 2007. MITTET, R. High-order finite-difference simulations of marine CSEM surveys using a
- correspondence principle for wave and diffusion fields. Geophysics, Society of Exploration Geophysicists, v. 75, n. 1, f33-f50, 2010. MORENCY, C. Electromagnetic wave propagation based upon spectral-element
- methodology in dispersive and attenuating media. Geophysical Journal International, Oxford University Press, v. 220, n. 2, p. 951–966, 2020. MORENCY, C.; TROMP, J. Spectral-element simulations of wave propagation in porous media. Geophysical Journal International, Blackwell Publishing Ltd
- PRIDE. Governing equations for the coupled electromagnetics and acoustics of porous media. Physical Review B, APS, v. 50, n. 21, p. 15678, 1994.

Acknowledgments

Oxford, UK, v. 175, n. 1, p. 301-345, 2008.

This research was funded by the Geothermica european co-fund initiative, project SEE4GEO, including LLNL under Contract DE-AC52-07NA27344, and the E2S UPPA project.

SEE4GEO





2e-05

1e-05

-1e-05

Figure 3 - Seismograms obtained with SPECFEM (time domain) and hou10ni2d+IFFT (frequency domain) using fictitious permittivity and $L(\omega) \simeq L_0$.

