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SEE4GEO

Introduction

Modeling of seismoelectric effects in the low frequency regime for field survey applications, American Geophysical Union/Advancing Earth And Space Sciences

Arjeta Heta^{1,2}, Hélène Barucq^{1,2}, Julien Diaz^{1,2}, Christina Morency³

¹ Inria Bordeaux Sud-Ouest, Pau, France
 ² Université de Pau et des Pays de l'Adour, Pau, France
 ³ Lawrence Livermore National Laboratory, Livermore, CA, USA
 ¹ arjeta.heta@inria.fr, ¹ helene.barucq@inria.fr, ¹ julien.diaz@inria.fr, ³ morency1@llnl.gov







(1)

A conductive porous medium excited by a seismic wave is the scene of complex physical phenomena known as seismo-electric effects. Understanding them opens new prospects for imaging geological objects invisible to seismic imaging. Their modeling began with the equations proposed by Pride in the 90s, which are constructed by coupling Maxwell's equations with Biot's wave equations. The coupling terms are written in terms of a frequency-dependent operator, which poses a major difficulty in the time domain, as it is an integral Fourier operator whose discretization is not trivial, especially as it must also consider the co-existence of waves propagating a thousand times faster than seismic waves.

Pride's equations for seismoelectric effects

Pride's equations Pride (1994) and Haartsen and Pride (1994) model SEE by coupling Maxwell's (electromagnetics) and Biot's (elastodynamics) equations. Here, we consider only the seismo-electric coupling.

$$\begin{split} &i\omega\rho_{a}\dot{\mathbf{u}}_{s} + i\omega\rho_{f}\dot{\mathbf{w}} = \nabla\cdot\tau + f_{u} \\ &i\omega p = -M\nabla\cdot\dot{\mathbf{w}} - M\alpha:\epsilon(\dot{\mathbf{u}}_{s}) \\ &i\omega \tau + i\omega\alpha p = \mathbf{C}:\epsilon(\dot{\mathbf{u}}_{s}) \\ &i\omega\delta_{0}\mathbf{E} = \nabla\times\mathbf{H} - \mathbf{J} + \mathbf{f}_{C} \\ &i\omega\mu_{0}\mathbf{H} = -\nabla\times\mathbf{E} \\ \end{split}$$
 Dynamical equations
$$\begin{split} &i\omega\rho_{f}\dot{\mathbf{u}}_{s} + i\omega\rho_{dyn}(\omega)\dot{\mathbf{w}} = -\nabla\mathbf{p} + \underline{i\omega\rho_{dyn}(\omega)}E + f_{\omega} \\ &\mathbf{J} = \sigma\mathbf{E} - L(\omega)(\nabla p + i\omega\rho_{f}\dot{\mathbf{u}}_{s}) \\ \end{split}$$

Pride's equations are solved in time in Morency and Tromp (2008) and Morency (2020):

 $\begin{array}{l} \rho \partial_t^2 \mathbf{u}_s + \rho_f \partial_t^2 \mathbf{w} = \nabla \cdot \mathbf{T} + \mathbf{F} \\ \eta k^{-1} \partial_t \mathbf{w} + \frac{\rho_f c}{\phi} \partial_t^2 \mathbf{w} + \rho_f \partial_t^2 \mathbf{u}_s = \nabla \cdot \mathbf{T}_f + \mathbf{F} \\ \mathbf{T} = (B \nabla \cdot \mathbf{u}_s + C \nabla \cdot \mathbf{w}) \mathbf{I} + 2\mu_{fr} \mathbf{D}_s \\ \mathbf{T}_f = -p_f \mathbf{I} = (C \nabla \cdot \mathbf{u}_s + M \nabla \cdot \mathbf{w}) \mathbf{I} \\ \epsilon \partial_t^2 \mathbf{E} = \nabla \cdot (\partial \tilde{\mathbf{H}}) - \sigma \partial_t \mathbf{E} - \partial_t \mathbf{j}_s \\ \partial_t \tilde{\mathbf{H}} = \tilde{\mu}^{-1} : \nabla \mathbf{E} \\ \mathbf{j}_s = \underline{Q_v k \eta^{-1}} (\nabla \cdot \mathbf{T}_f - \rho_f \partial_t^2 \mathbf{u}_s + \mathbf{F}) \end{array} \right\}$ Maxwell's equations

Frequency dependent coupling

Electrokinetic (Maxwell-Biot coupling) coefficient $L(\omega)$:

$$\boldsymbol{L}(\boldsymbol{\omega}) = \boldsymbol{L}_0 \left(1 - i\frac{m\,\boldsymbol{\omega}}{4\,\boldsymbol{\omega}_t} \right)^{-1/2} \quad \text{with} \quad \boldsymbol{L}_0 = \frac{\phi\epsilon_0\epsilon_r^f\zeta^p}{\alpha_\infty\eta} \underbrace{\left(1 - 2\frac{d^l}{\lambda} \right)}_{\simeq 1}$$

In time domain, Pride's equations are solved with $L(\omega) \simeq L_0$. This is a low-frequency approximation that only applies to field-type simulations. We show that, at frequencies encountered in laboratory experiments (>20kHz), the effect of frequency on coupling is too significant to be neglected. Frequency-dependent coupling is very difficult to account for in time domain as L(t) is a Fourier integral operator global in time and space (inverse

$\mathbf{c} = \mathbf{c} = $		\dot{L}_0)	Fourier):
Modeling of the problem					$LE(\vec{x} t) - L_{\alpha} \int (1 - i\frac{\omega}{\omega})^{-1/2} \widehat{E}(\vec{x} \omega) e^{i\omega t} d\omega$
Table 1 – Unknowns	Table 2 – Porous sub-soil physical parameters		Table 3 – Porous sub-soil physical parameters		$DL(x,t) = L_0 \int_{\mathbf{R}} (1 t \omega_t) D(x,\omega) t \omega \omega$
$ \mathbf{u}_s $ solid displacement	$\overline{\rho_{a}}, ho_{f}, ho_{dyn} ig $ ave	eraged, fluid, dynamic densities	μ_{fr} frame s	frame shear modulus	Simplified frequency dependent coupling operators introduced in Heta,
w fluid displacement	α effe	ective stress tensor	\mathbf{F}	macroscopic source	Barucq, and Diaz (2022) can be used. In polynomial or rational form, the
p fluid pressure	$f_u, f_w, f_C = ext$	erior forces	\mathbf{D}_{s}	solid strain deviator	equivalent time domain equations are simple to obtain. For ω/ω_t small
au stress tensor	L(ω) coι	upling coefficient	ho	bulk density	enough,
E electric density field	C stif	ffness tensor	η	fluid viscosity	$L(\omega) \sim \mathcal{C}(\omega) - L_0 \prod^n \left(1 - ic^{(n)} \frac{m\omega}{m\omega}\right) / \left(1 - ib^{(n)} \frac{m\omega}{m\omega}\right)$
H magnetic intensity field	$\epsilon(u)$ stra	ain tensor	k	fluid permeability	$L(\omega) = \mathcal{L}_n(\omega) = L_0 \prod_{i=1}^{I} \left(1 - \frac{ic_j}{4\omega_t} \right) / \left(1 - \frac{io_j}{4\omega_t} \right)$
J electric current density	M flui	id-solid coupling modulus	B,C,N	<i>I</i> Biot coefficients	where
T total stress	δ_0 , μ_0 elec	ctric factor and permeability	c	Tortuosity	$(i\pi)^2 \qquad (i\pi)^2 \qquad ($
$ \mathbf{T}_{f} $ fluid stress	σ cor	nductivity			$b_j^{(n)} = \cos\left(\frac{J^n}{2n+1}\right) , c_j^{(n)} = \sin\left(\frac{J^n}{2n+1}\right) , a_j^{(n)} = \frac{2c_j}{2n+1}$

RESULTS & DISCUSSION

It has been shown in Heta, Barucq, and Diaz (2022) that $L(\omega) \simeq L_0$ is a good approximation at low frequencies as a function of cut-off frequency ω_t . For comparison with the time-domain equations using L_0 , we use $L(\omega) = L_0$. The frequency-domain equations are solved using the Hybridizable Discontinuous Galerkin method with the solver hou10ni (Figure 2).

The use of a fictitious permittivity $\epsilon \simeq 7.965 \cdot 10^{-4} \text{Fm}^{-1}$ to address the diffusive nature of the EM signal has been introduced with success in e.g. Maaø (2007) and Mittet (2010) to carry out time-domain simulations valid on a field scale. The time-domain equations are solved using the Spectral Element Method with the solver SPECFEM(Figure 3).

Using a discrete inverse Fourier transform, seismograms are computed from a frequency sweep. These results are compared to the solutions computed directly in time domain.



Observations

- Results with true and with fictitious permittivity are very similar in frequency domain, consistent with time domain findings.
- SPECFEM was run with 150000 time steps. hou10ni results were computed on fine meshes but for 400 distinct frequencies up to 400Hz.
- In frequency domain, only the source and reflected wave are visible in E_y . In time domain, the converted wave is visible in domain 2 (arrives at $t \simeq 180 \mu s$).
- Despite the higher resolution of the time domain computations, arrival times coincide with the two methods.

Conclusion

A use of a fictious permittivity allows to compute solutions in time but it modifies the behaviour of the converted wave. The comparisons between our solvers, one in time(SPECFEM) and the other one in frequency(Hou10ni), show a quite good





consistency regarding the field V and the co-seismic wave. We have a perfect arrival time but the amplitudes do not match.

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V_y , SPECFEM, full line 2





V_y , hou10ni, full line 2



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