

## Interpretable reduced order modeling using neural autoencoders

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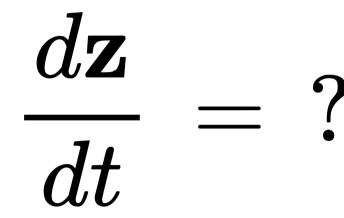
# Interpretable Learning of Effective Dynamics for multiscale systems

*E. Menier, S. Kaltenbach, M. Yagoubi, M. Schoenauer, P. Koumoutsakos* MORTech 2023 – 6th International Workshop on Model Reduction Techniques

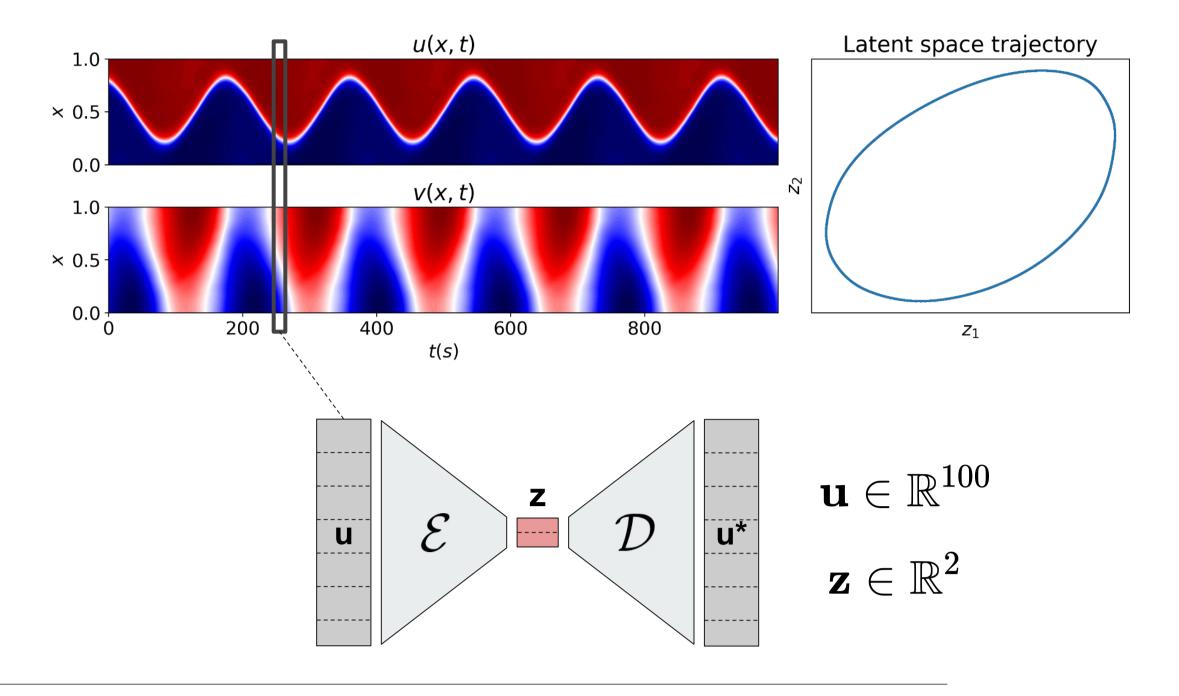
# **Dimensionality Reduction**

Neural AutoEncoders can be used to identify low dimensional representation spaces for dynamical systems. On the left, the 1D Fitz-Hugh Nagomo model is reduced from a representation on a 100 points spatial mesh to two latent coordinates (z1 and z2).

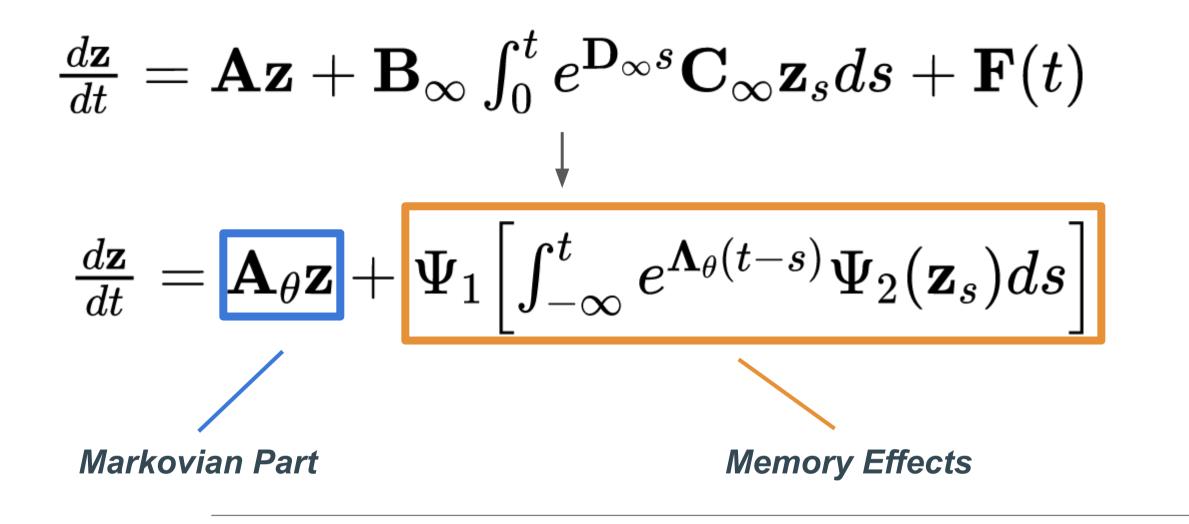
Unfortunately, the dynamics of this low dimensional representation are a-priori unknown :







# **Form of the Dynamics**



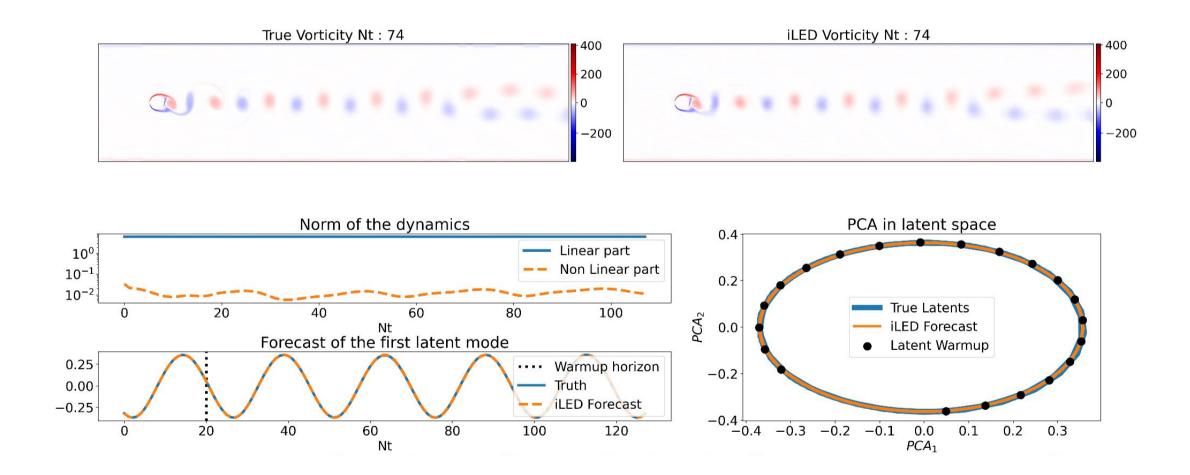
Results from dynamical systems theory, mainly the theory of the Koopman Operator (see [1]) can be used to derive an ansatz for the reduced dynamics.

The proposed form of the dynamics requires the learning of two linear operators (**A** and **A**) and two neural networks ( $\Psi_1$  and  $\Psi_2$ ).

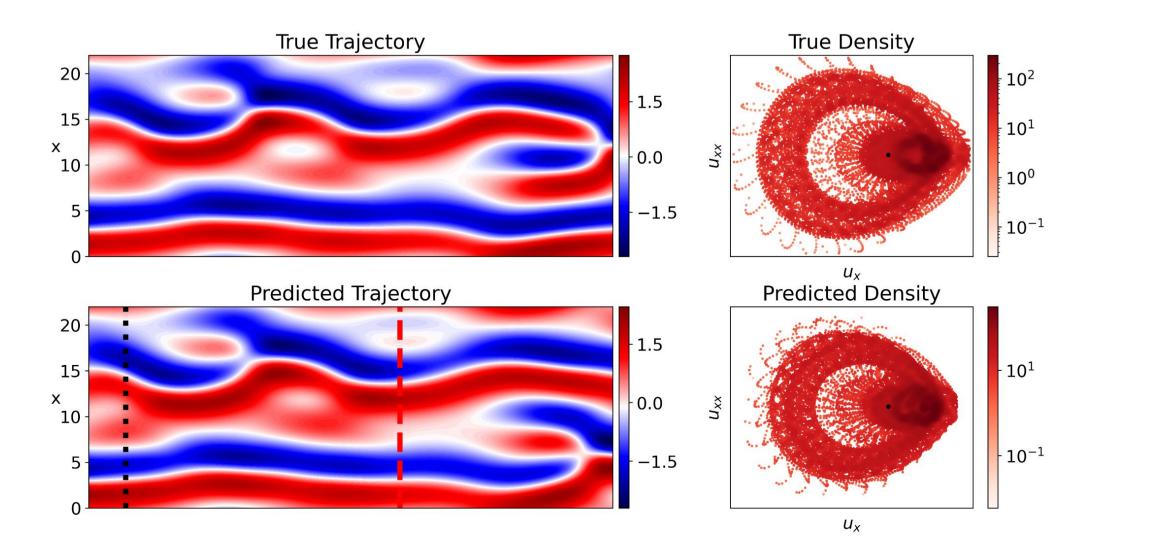
## **Application : Cylinder Flow**

The 2D cylinder flow can also be reduced to a two dimensional representation. After training the proposed dynamical model, a model is obtained, able to forecast the state of the system efficiently and accurately for multiple periods of the system.

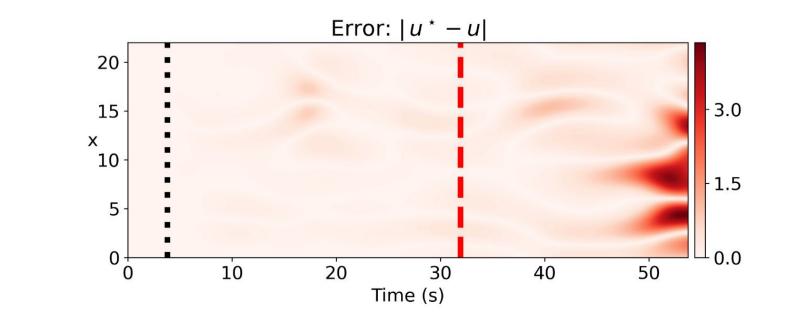
It is interesting to note that the dynamics are almost completely linear, yielding a highly interpretable model.



## **Application : Kuramoto-Sivashinsky**



The method is able to learn chaotic dynamics as well. In these cases, the non-linear memory effects become critical to the model.



[1]: Menier, E., Kaltenbach, S., Yagoubi, M., Schoenauer, M., & Koumoutsakos, P. (2023). Interpretable learning of effective dynamics for multiscale systems. arXiv preprint arXiv:2309.05812



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