

Interpretable reduced order modeling using neural autoencoders

Emmanuel Menier, Sebastian Kaltenbach, Mouadh Yagoubi, Marc Schoenauer, Koumoutsakos Petros

▶ To cite this version:

Emmanuel Menier, Sebastian Kaltenbach, Mouadh Yagoubi, Marc Schoenauer, Koumoutsakos Petros. Interpretable reduced order modeling using neural autoencoders. MORTech 2023 – 6th International Workshop on Model Reduction Techniques, Nov 2023, Gif-sur Yvette, France. hal-04296372

HAL Id: hal-04296372 https://inria.hal.science/hal-04296372

Submitted on 20 Nov 2023 $\,$

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.



Distributed under a Creative Commons Attribution 4.0 International License

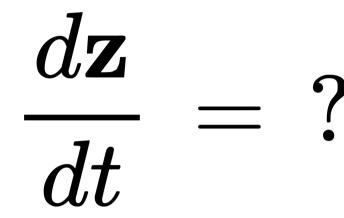
Interpretable Learning of Effective Dynamics for multiscale systems

E. Menier, S. Kaltenbach, M. Yagoubi, M. Schoenauer, P. Koumoutsakos MORTech 2023 – 6th International Workshop on Model Reduction Techniques

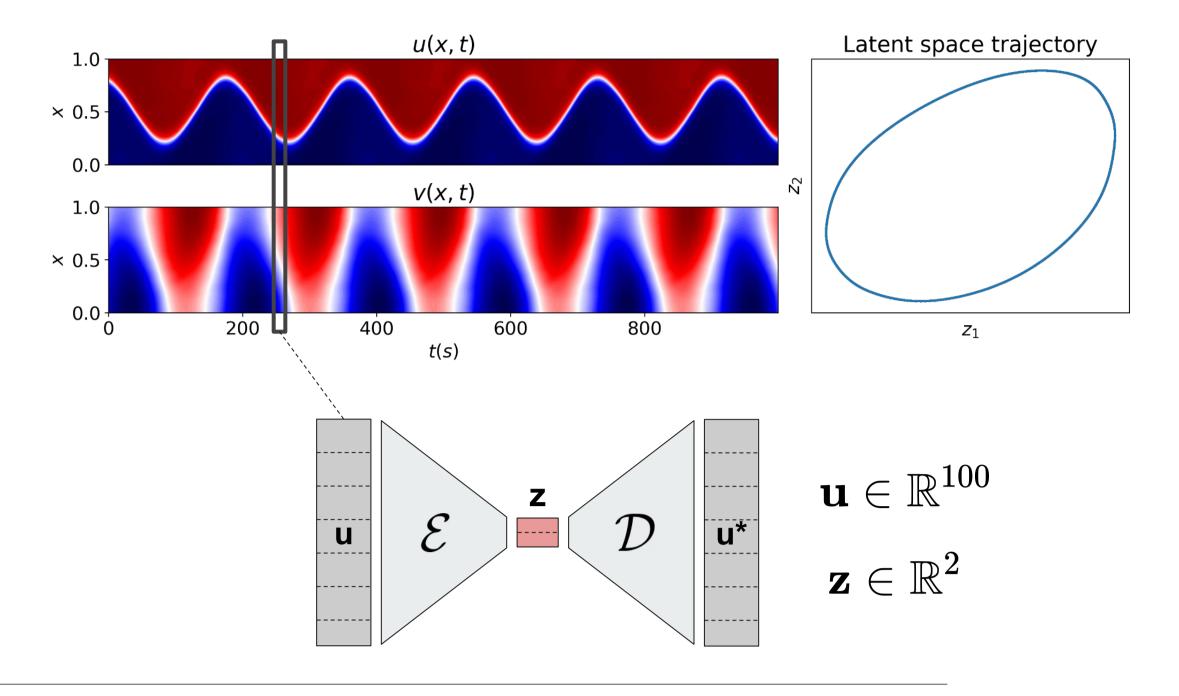
Dimensionality Reduction

Neural AutoEncoders can be used to identify low dimensional representation spaces for dynamical systems. On the left, the 1D Fitz-Hugh Nagomo model is reduced from a representation on a 100 points spatial mesh to two latent coordinates (z1 and z2).

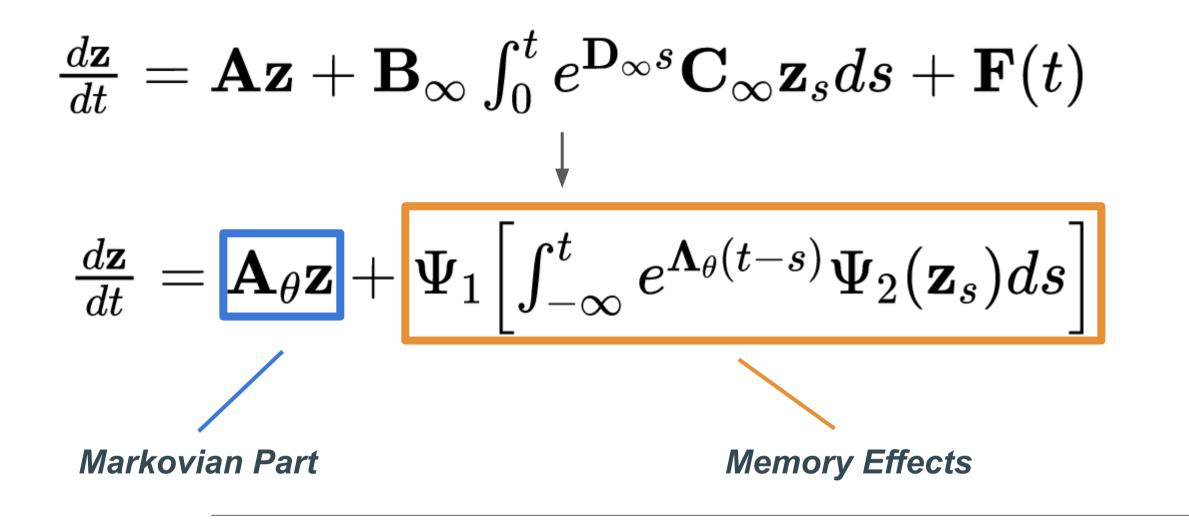
Unfortunately, the dynamics of this low dimensional representation are a-priori unknown :







Form of the Dynamics



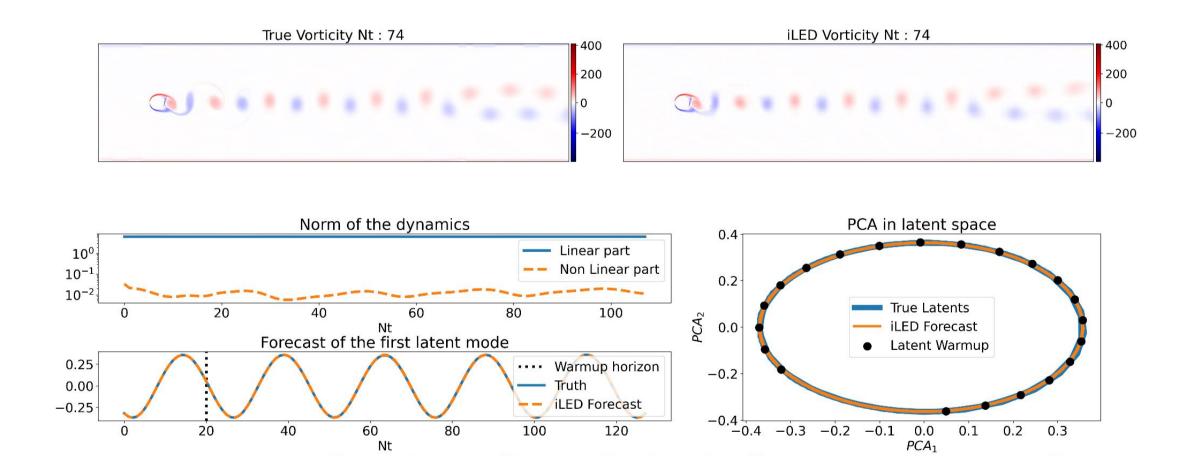
Results from dynamical systems theory, mainly the theory of the Koopman Operator (see [1]) can be used to derive an ansatz for the reduced dynamics.

The proposed form of the dynamics requires the learning of two linear operators (**A** and **A**) and two neural networks (Ψ_1 and Ψ_2).

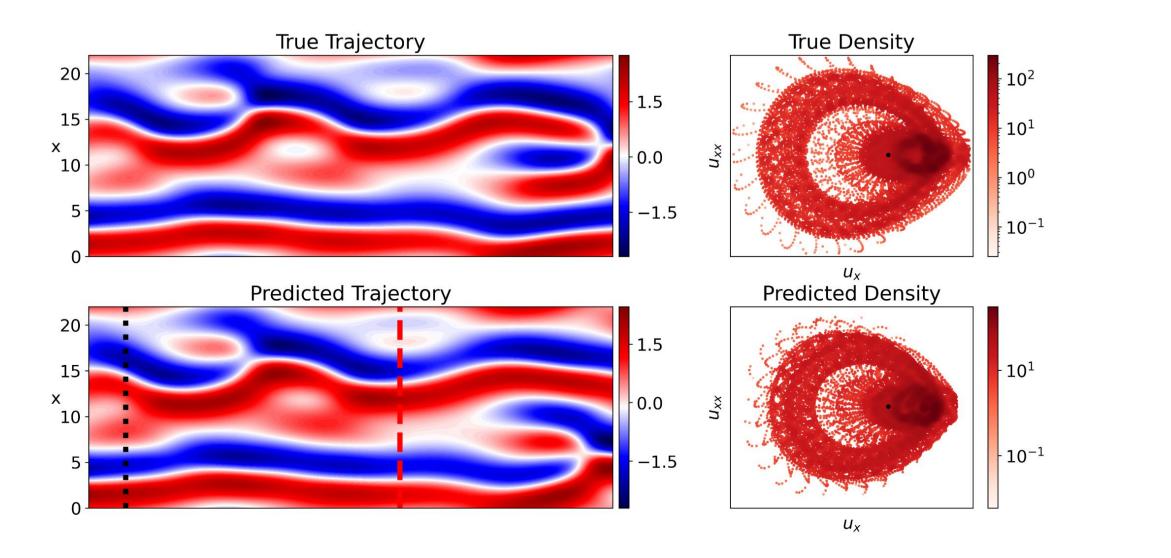
Application : Cylinder Flow

The 2D cylinder flow can also be reduced to a two dimensional representation. After training the proposed dynamical model, a model is obtained, able to forecast the state of the system efficiently and accurately for multiple periods of the system.

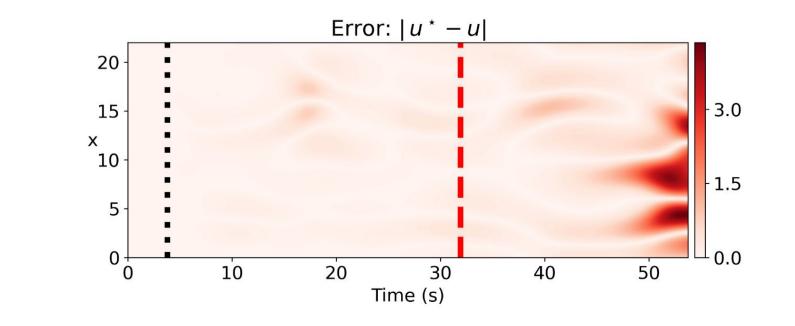
It is interesting to note that the dynamics are almost completely linear, yielding a highly interpretable model.



Application : Kuramoto-Sivashinsky



The method is able to learn chaotic dynamics as well. In these cases, the non-linear memory effects become critical to the model.



[1]: Menier, E., Kaltenbach, S., Yagoubi, M., Schoenauer, M., & Koumoutsakos, P. (2023). Interpretable learning of effective dynamics for multiscale systems. arXiv preprint arXiv:2309.05812



Harvard John A. Paulson School of Engineering and Applied Sciences





