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Differential Meet-In-The-Middle Cryptanalysis

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Abstract. In this paper we introduce the differential meet-in-the-middle framework, a new cryptanalysis technique for symmetric primitives. Our new cryptanalysis method combines techniques from both meet-in-the-middle and differential cryptanalysis. As such, the introduced technique can be seen as a way of extending meet-in-the-middle attacks and their variants but also as a new way to perform the key recovery part in differential attacks. We apply our approach to SKINNY-128-384 in the single-key model and to AES-256 in the related-key model. Our attack on SKINNY-128-384 permits to break 25 out of the 56 rounds of this variant and improves by two rounds the previous best known attacks. For AES-256 we attack 12 rounds by considering two related keys, thus outperforming the previous best related-key attack on AES-256 with only two related keys by 2 rounds.

Keywords: differential cryptanalysis, meet-in-the-middle cryptanalysis, SKINNY, AES

1 Introduction

Since the 1970's and the standarization of the DES block cipher hundreds of different symmetric primitives have been designed to address special needs and industrial requirements or to provide an answer to particular research problems. A fundamental procedure that permits to decide which among those primitives can be trusted and safely deployed is cryptanalysis. The first modern symmetric cryptanalysis techniques were developed in the late 1970's, 1980's and in the beginning of the 1990's. Among these first and most important attacks are, of course meet-in-the-middle [21], differential [8] and linear cryptanalysis [39],

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but also boomerang [46] and rectangle attacks [6], impossible differential [35, 5], higher-order differential [36] or differential-linear attacks [37]. More attacks appeared in succession to new designs, as for example the square attack [17], particularly well-adapted to AES-like constructions or the subspace invariant attacks [38] that worked well against some particular lightweight ciphers. In parallel, some techniques, as the division property [44], permitted to define a new algorithmic framework to generalize older attacks. As the field is well advanced, nowadays, it is more and more rare to come up with entirely new cryptanalysis techniques, while improvements of the known ones are more common.

Among the existing cryptanalysis techniques, differential attacks [8] are among the oldest and the best studied cryptanalysis methods. Their idea is to exploit an input difference that propagates through the cipher to an output difference with a high probability. Through the years, these attacks have been refined and many improvements to different parts of the attack procedure have been introduced: the use of structures to build up the plaintext or ciphertext pairs [9], the use of truncated differentials [36], conditional differentials [34], the technique of probabilistic neutral bits [16] or refinements in the key recovery process, to mention only a few. A first research question in link with our work is the following:

Question 1. Do there exist alternative methods for doing the key recovery step of a differential attack more efficiently?

Another popular – and actually even older – technique that has been useful in many cryptanalysis applications, and the subject of a large number of improvements and further studies is meet-in-the-middle (MITM) cryptanalysis [21]. The idea of basic MITM attacks is to split the cipher into two parts, where each part can be computed with partial knowledge of the key. An attacker can then validate partial key guesses by checking for a match in the middle. Again, many extensions and refinements of the basic attack exist today: the technique of partial matching, where only a part of the middle state is known, guessing some bits of the internal state [24], the all-subkeys approach [31], the splice-and-cut technique [1, 2, 28] and the sieve-in-the-middle (SITM) approach [14] that permits to extend the length of a MITM attack by searching for a match through an extra S-box layer in the middle. Finally, the method of bicliques is a cryptanalysis technique [12] that aims at extending MITM attacks by some rounds. A second research problem of interest to us and that motivated our initial work is:

Question 2. Can we find a new way to extend a MITM attack to more rounds?

In this paper we provide a positive answer to both questions simultaneously by proposing a new cryptanalysis technique that we call the *differential meet-in-the-middle attack*. The idea of this new technique is to use a differential to cover several middle rounds of the cipher while running a meet-in-the-middle attack on its external rounds. In a nutshell, this combination has many potential advantages. In particular, with our new technique, a middle part of the cipher is covered by a differential and thus we have to apply MITM techniques on much less rounds than with all previous MITM-type attacks. Note that Demirci-Selçuk

MITM attacks [19] applied with the differential enumeration technique [23] also combine to some extent truncated differentials and the MITM approach, but in this case the guess is done in parallel on the inner part (with a truncation-based distinguisher) and the external part, trying to match some particular properties of the differential set. Interestingly, our new method can also be interpreted as a differential attack where the key recovery step is done in a different way. Indeed, starting from a given plaintext-ciphertext pair, we guess in parallel the input keys that allow us to compute a matching plaintext ensuring the given input difference of the differential, and the output keys that allow us to compute the ciphertext that ensures the output difference of the differential, and compute the associated plaintext for all these ciphertexts by making calls to the oracle. Next, we try to match the list of plaintexts computed with the guesses of the input key bits and the list of plaintexts computed with the list of output keys by finding a collision. We repeat this for enough plaintexts so that we can expect one of them to satisfy the differential. All collisions found will imply a potential candidate for the associated guess of keys. The matching can usually be done efficiently with list merging algorithms like the ones in [41].

In order to demonstrate the efficiency of our new cryptanalysis technique, we provide two applications. First, we apply the attack in the single-key setting to the block cipher SKINNY and we show how to break 25 out of the 56 rounds of SKINNY-128-384, the 128-bit block variant employing a 384-bit key. Our attack improves by two the number of rounds of the previous best attack against this variant in the single-key model. A summary of the best attacks against SKINNY-128-384 is given in Table 1. Then, we provide an application to AES-256 by breaking 12 rounds of the cipher in the related-key model. Our attack uses only 2 related keys, whereas the best previous attacks with this number of related keys could reach at most 10 rounds. A summary of the best attacks against AES-256 is given in Table 2.

The rest of the paper is organized as follows. Section 2 describes the general framework of our new cryptanalysis technique, compares it to both differential and MITM attacks and provides several improvements. Our attacks against SKINNY-128-384 are described in Section 3 and our application on AES-256 is given in Section 4. Finally, several open problems are discussed in Section 5.

2 The new attack: Differential MITM

We propose in this work a new cryptanalysis technique against symmetric primitives. This new attack aims at combining meet-in-the-middle (MITM) attacks together with differential cryptanalysis, and we will call this new technique differential MITM. The original motivation of our work was to investigate whether there exists a method for reaching more rounds than the sieve-in-the-middle attack [14,15], an extension of classical MITM attacks. However, our technique can also be interpreted as a new key-recovery method to apply in differential

⁵ Note that [30] provides a 26-round integral attack against SKINNY-128-384 but it relies on differences in the tweak.

4 Boura et al.

 $\begin{tabular}{ll} \textbf{Table 1.} Best attacks against SKINNY-128-384 in the single-key (SK) model together with the results presented in this paper. ID stands for impossible differentials, MITM for meet-in-the-middle attacks and DS-MITM for Demirci-Selçuk-type MITM.$

# Rounds	Data	Time	Memory	Type	Ref.
21	2^{123}	$2^{353.6}$	2^{341}	ID	[47]
21	$2^{122.89}$	$2^{347.35}$	2^{336}	ID	[30]
22	2^{96}	$2^{382.46}$	$2^{330.99}$	DS-MITM	[43]
22	$2^{92.22}$	$2^{373.48}$	$2^{147.22}$	ID	[45]
23	2^{104}	2^{376}	2^{8}	MITM	[22]
23	2^{117}	$2^{361.9}$	$2^{118.5}$	Diff-MITM	Section 3.2
24	2^{117}	$2^{361.9}$	2^{183}	Diff-MITM	Section 3.4
24	$2^{122.3}$	$2^{372.5}$	$2^{123.8}$	Diff-MITM	Section 3.5
25	$2^{122.3}$	$2^{372.5}$	$2^{188.3}$	Diff-MITM	Section 3.5

Table 2. Best attacks against AES-256 together with the results presented in this paper. † The parameter s should be such that $0 \le s \le 7.5$.

# Rounds	Data	Time	Memory	# Related-key	Type	Ref.
9	2^{120}	2^{203}	2^{203}	0	MITM	[20]
10	2^{114}	2^{173}	2^{64}	64	Rectangle	[7, 33]
14	-	-	_	4	Boomerang	[11]
14	-	2^{92+s}	_	2^{19-s}	Boomerang	[29] †
14	2q	$q2^{66}$		2q	q-multicollisions	[27]
14	2^{125}	2^{125}	2^{65}	2^{32}	basic RK differential	[27]
12	289	2^{206}	$2^{71.6}$	2	Diff-MITM	Section 4

cryptanalysis, that can be sometimes combined with MITM improvements for reaching more rounds. We will present in this section a high-level description of the new technique. More precisely, we will provide a general framework that describes how to mount a differential MITM attack in a generic and simple way, and we will show how to combine this generic method with two techniques: the parallel treatment of data partitions in order to add one round mostly for free (idea that inherits from MITM attacks, like bicliques, and that cannot be applied to classical differential attacks), as well as a technique to reduce the data complexity.

2.1 General framework

Consider a *n*-bit cipher E decomposed into three sub-ciphers: $E_{out} \circ E_m \circ E_{in}$, as depicted in Figure 1. Let the number of rounds of E_{in} , E_m and E_{out} be r_{in} , r_m and r_{out} respectively. Finally, let Δ_x be the input difference to the middle part E_m , Δ_y the output difference of E_m and suppose that the differential $\Delta_x \to \Delta_y$, covering the r_m middle rounds, has probability 2^{-p} .

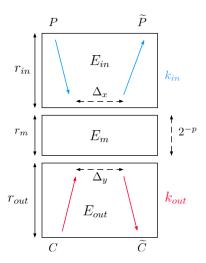


Fig. 1. A high-level description of the Differential MITM technique.

We start our analysis with a first randomly chosen plaintext P and its associated ciphertext C, and we aim at generating a second plaintext-ciphertext pair (\tilde{P}, \tilde{C}) such that together they satisfy the differential on the middle rounds. Our new idea is to generate (\tilde{P}, \tilde{C}) with a meet-in-the-middle approach. For this, candidate plaintexts \tilde{P} are computed from both the plaintext P and the difference Δ_x for each possible value of the associated key k_{in} , while candidate ciphertexts \tilde{C} are computed from C and Δ_y for each possible value of the involved key, k_{out} . The match is then performed on the relation $E(\tilde{P}) = \tilde{C}$ (or $\tilde{P} = E^{-1}(\tilde{C})$). Note

that the roles of the upper and lower part can be interchanged without loss of generality in order to optimize the data and memory complexity, if we consider that the access to both the encryption and the decryption oracles is granted.

Upper part. Given P, the aim is to guess the minimal amount of key information, that we will denote by k_{in} , such that we can compute the associated \widetilde{P} that ensures $E_{in}(P) \oplus E_{in}(\widetilde{P}) = \Delta_x$ if the guess of k_{in} corresponds to the secret key. For each guess i for k_{in} , we obtain a different candidate for \widetilde{P} , that we denote by \widetilde{P}^i , leading to a total of $2^{|k_{in}|}$ such values. From them, we can compute the $2^{|k_{in}|}$ associated ciphertexts $\widehat{C}^i = E(\widetilde{P}^i)$ with calls to the encryption oracle and store them in a hash table H.

Lower part. Similarly, given C, we can guess some key material k_{out} , of bitlength $|k_{out}|$, and compute a new ciphertext \widetilde{C} that satisfies the equation $E_{out}^{-1}(C) \oplus E_{out}^{-1}(\widetilde{C}) = \Delta_y$ if the key guess is correct. We obtain $2^{|k_{out}|}$ values for \widetilde{C}^j , each associated to a guess j for k_{out} .

Number of pairs and match. For the correct key guess, the transition $\Delta_x \to \Delta_y$ will happen with a probability 2^{-p} . Therefore, we will repeat the upper and lower procedures 2^p times with 2^p different messages P_ℓ so that we can expect one pair $(P_\ell, \widetilde{P}^i_\ell)$ to satisfy the differential together with the associated pair $(C_\ell, \widetilde{C}^j_\ell)$. When this is the case, we will find a collision for a certain ℓ between a \widehat{C}^i_ℓ computed in the upper part and stored in H and a \widetilde{C}^j_ℓ computed from the lower part. Each collision (i, j) has an associated key guess $k_{in} = i, k_{out} = j$, that we will consider as a potential candidate. The number of expected collisions for each fixed P_ℓ is $2^{|k_{in}| + |k_{out}| - |k_{in} \cap k_{out}| - n}$.

Algorithm 1 Differential MITM attack

```
while right key not found do
                                                                                        \triangleright 2^p trials expected
    Randomly pick P
    C \leftarrow E(P)
                                                                                                  \triangleright Oracle call
    H \leftarrow \emptyset
                                                                                ▶ hash table initialization
    for each guess i for k_{in} do
                                                                                   ▶ Forward computation
         Compute \widetilde{P}^i from i and P
         \widehat{\widehat{C}}^i \leftarrow E(\widetilde{P}^i) \\ H[\widehat{C}^i] \leftarrow H[\widehat{C}^i] \cup \{i\}
                                                                                                  ▷ Oracle call
    end for
    for each guess j for k_{out} do
                                                                                ▶ Backward computation
         Compute \widetilde{C}^j from j and C
         for each i \in H[\widetilde{C}^j] do
              Complete (i, j) to retrieve the master key
              Try candidates against extra data
         end for
    end for
end while
```

Complexity. The time complexity of this attack can be estimated as

$$\mathcal{T} = 2^p \times (2^{|k_{in}|} + 2^{|k_{out}|}) + 2^{|k_{in}| + |k_{out}| - |k_{in} \cap k_{out}| - n + p},$$

where the first term corresponds to the computations done in E_{in} and E_{out} , and the last one to the number of expected key candidates. With this, we recover $k_{in} \cup k_{out}$, so if we expect fewer key candidates than the whole set $k_{in} \cup k_{out}$, (i.e $|k_{in}| + |k_{out}| - |k_{in} \cap k_{out}| - n + p < |k_{in} \cup k_{out}|$, which holds as long as p < n), we can guess the remaining bits of the master key and test the guess with additional pairs. Thus we recover the whole key with a complexity smaller than the cost of an exhaustive key search, and an additional cost of

$$2^{k-(|k_{in}\cup k_{out}|)} \times \max\{1, 2^{|k_{in}|+|k_{out}|-|k_{in}\cap k_{out}|-n+p}\}$$

to be added to the time complexity \mathcal{T} . In the expected case where $|k_{in}| + |k_{out}| - |k_{in} \cap k_{out}| - n + p \ge 0$, the total time complexity is thus

$$\mathcal{T} = 2^p \times (2^{|k_{in}|} + 2^{|k_{out}|}) + 2^{|k_{in} \cup k_{out}| - n + p} + 2^{k - n + p}.$$

The (naive) data complexity of this first version of the attack can be estimated as

$$\mathcal{D} = \min(2^n, 2^{p + \min(|k_{in}|, |k_{out}|)}).$$

Finally, the naive memory complexity is given by $\mathcal{M} = 2^{\min(|k_{in}|,|k_{out}|)}$, though it can be improved to $2^{\min(|k_{in}|-|k_{in}\cap k_{out}|,k_{out}-|k_{in}\cap k_{out}|)}$ by first guessing the common key material before running the attack.

2.2 Improvement: Parallel partitions for layers with partial subkeys

We will show now that in the case where the round key addition does not affect the whole state but only a part of it (as is for instance the case in Feistel constructions [25], or in the SKINNY [4] and GIFT [3] ciphers), we can extend the attack by one round. As we will show, if the m bits of the state affected by the key addition are such that m < p (where p is the $-\log_2$ of the probability of the differential distinguisher), the time complexity of adding this round will not be affected. However, the exact data complexity of the attack has to be checked case-by-case, as it might depend on the configuration of the differences in the external states. A technique on how to reduce the data complexity will be further discussed in Section 2.3. The memory complexity might be a priori increased.

The main idea here is to consider, in addition to guessing in parallel the key bits intervening in the lower and upper parts, a partial parallel guess of the final states. More precisely, 2^m penultimate and final states (or the initial state, without loss of generality) will be guessed in parallel, without needing to guess the key that allows the transition from the penultimate one to the final. When performing the final match, we will take into account this key transition. Actually, it can be seen as considering 2^m plaintexts P_i and ciphertexts C_j in parallel, without knowing which ones would match together, as this transition is determined by the last round-key.

Since we expect to try on average 2^p plaintexts in order to find one that will satisfy the differential of probability 2^{-p} , we can divide the final state of size 2^n into two parts. The part without the key addition will take 2^{p-m} different values, and the attack will be repeated for each one of those.

On the other hand, the part affected by the key addition will take 2^m possible values for X, the state before the key addition, and for each we can compute the state S_{r-1} in Figure 2 from the output of the differential MITM attack. From this state, we will guess the k_{out} bits, in order to compute the associated state potentially generating the output difference of the middle differential, obtaining $2^{|k_{out}|+m}$ candidates to match. In parallel, the state Y after the key addition will also take all the 2^m possibilities, and with them we decrypt in order to obtain the plaintext, and do the upper key guessing procedure to deduce the good pairs, obtaining $2^{|k_{in}|+m}$ candidates. The number of possible solutions might seem higher by a factor of 2^{2m} , but note that we have to match X and Y, as well as their associated pairs X' and Y', and they must satisfy $X \oplus X' = Y \oplus Y'$. This adds m bit-conditions, or more if this final subkey was already determined by k_{in} and k_{out} , which is usually the case. This implies m additional conditions, and $2^{2m}2^{-m}2^{-m}=1$, so the cost, given by the number of solutions, stays exactly the same as the attack with one round less. We will see how this technique can be applied in practice in Section 3.

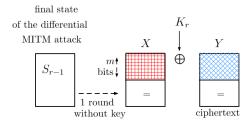


Fig. 2. Partial guess of the final state to add one round for free. S_{r-1} is the final state of the simple differential MITM attack.

2.3 Improvement: Reducing data with imposed conditions

We explain here a way to obtain time-data-memory trade-offs for the original attack. If when choosing the plaintext P, we force x of its bits, that might have been active otherwise, to a certain value, and if we expect the same from the associated plaintext \tilde{P} , the overall probability of the attack will decrease to 2^{-p-x} , as we will have to repeat the procedure until a \tilde{P} that satisfies this constraint is found. More precisely, if \tilde{P} does not fit this condition, the corresponding tuple will not be stored in the hash table since we do not have access to its ciphertext. However by doing so, the data complexity will be reduced by a factor of 2^x as well as the memory complexity. When combining this technique with the

previous one, we can derive the following two inequalities for x:

$$p + x \le n - x$$
 and $2^{p+x}(2^{|k_{in}|} + 2^{|k_{out}|}) < 2^k$.

This type of trade-off applies in particular when all the code book of size 2^n is needed before fixing the x bits, and the data complexity becomes 2^{n-x} .

Data reduction without time increase. As the total number of candidates for the key of the input part (respectively output) will be $2^{|k_{in}|-x}$ (respectively $2^{|k_{out}|-x}$), if we are able to find these candidates with their associated \widetilde{P} (respectively \widetilde{C}) in a complexity given by the number of solutions, the time complexity would become:

$$2^{p+x}(2^{|k_{in}|-x}+2^{|k_{out}|-x})=2^p(2^{|k_{in}|}+2^{|k_{out}|}),$$

which allows us to reduce the data complexity to 2^{n-x} while not increasing the time complexity. The optimal data complexity in this case will be $2^{\frac{n+p}{2}}$, obtained with x equal to $\frac{n-p}{2}$.

This can actually be done in many cases using rebound-like techniques [40]. This is the case for all our attacks summarized in Table 1. An example can be seen in Section 3.

2.4 Discussion and Comparison

As argued before, our new cryptanalysis technique is closely related to two families of techniques: MITM attacks and differential attacks. In this section we will discuss similarities and differences between these families and will try to identify cases where our new technique might be efficient or cases where it permits to reach better results compared to the best known attacks.

Relation to MITM attacks In relation to MITM attacks and its variants, like the sieve-in-the-middle technique, our attack, already if using a differential with probability one, could have, a priori, the potential of reaching more rounds. The starting point of our research was whether it was possible to add even more rounds in the middle of a MITM-like attack and this is how we came up with the new attack. The data complexity of the new attack could be higher than a classical MITM one as now we compute a new \tilde{P} from each guess of the key, and this plaintext can take many different values, besides the 2^p different plaintexts P_ℓ taken as starting points in order to find one that satisfies the differential. On the other hand, despite the fact that the sets of bits k_{in} or k_{out} involved in the parallel computations of the differential MITM attack are not determined in the same way as the key bits involved in MITM attacks, we expect those quantities to be relatively close under similar settings, as this principally depends on the propagation properties of the round function. More precisely, it seems that more aligned [13] the round function is, closer the sets will be.

Therefore, we expect that ciphers where classical MITM attacks work well, can also be interesting targets for differential MITM attacks. This is actually how we found the application shown in Section 3 on SKINNY. Indeed, the best known attack against SKINNY-384-128 previous to ours was a MITM one [22].

Relation to differential attacks Curiously enough, our new attack can also be seen as a new way of performing the key-recovery part associated to a differential distinguisher.

Classical differential attacks. A differential attack starts with a differential distinguisher on r_m rounds of relatively high probability 2^{-p} . One then typically extends the distinguisher by r_{in} rounds to reach the plaintext state and by r_{out} rounds to reach the ciphertext state, with probability 1 as depicted in Figure 3. Structures are then used to build plaintext (or ciphertext) pairs. A structure of size 2^s allows to build 2^{2s-1} pairs (though building all these pairs is rarely needed), but for each structure we need to consider typically an additional probability so that the pairs from the structure satisfy the input difference of the distinguisher. If we are not considering truncated but fixed differentials, as it will be our case, the probability of reaching a fixed difference Δ_x is approximately 2^{-s} . In order to expect that at least one pair will satisfy the distinguisher, we will need to consider 2^{p-s+1} structures, each of size 2^s , and for each structure, 2^{s-1} pairs will reach the input difference Δ_x , leading to a total of $2^{p-s+1+s-1}=2^p$ pairs reaching Δ_{T} . Typically, for determining a priori potential good pairs, one performs some sieving that will allow not to try all the pairs from all the structures. This sieving is done by looking at the activity pattern of the ciphertexts and can be estimated as $2^{-c} = 2^{-n+a}$, where a is the bit-size of the active part in the ciphertext. The key recovery part depends on the particular properties of the round function. Its complexity can be often accurately lower bounded by the number of the partial key candidates in the key-recovery rounds, thanks to early abort and divide-and-conquer techniques.

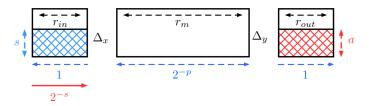


Fig. 3. Framework of a classical differential attack.

The data complexity of such an attack is 2^{p+1} and the time complexity can be estimated as

$$2^{p+1} + 2^{p-s+1}2^{2s-1}2^{-c}C_k \approx 2^{p+s-n+a},\tag{1}$$

where C_k is the average cost of determining the key bits for each candidate pair. This quantity can be lower bounded by the number of partial key candidates in the key-recovery rounds and this number can be much greater than 1 if the key is bigger than the state.

We can see that if s and a are big enough, i.e. $a + s \gg n$, which can happen when several rounds are appended, the complexity of a differential MITM attack for an equivalent number of rounds might be more interesting. Indeed, the influence of the input and output extensions to the complexity are added and not multiplied. In particular, our attack can become much more efficient when the key size of the cipher is bigger than the state size, otherwise 2^p might already be close to the limit.

3 Differential Meet-the-Middle attacks against SKINNY-128-384

We provide in this section our applications to SKINNY-128-384. We start by recalling the specifications of the SKINNY family of ciphers.

3.1 Specifications of SKINNY

The SKINNY family of tweakable block ciphers was designed by Beierle et al. [4]. It is a family of lightweight ciphers following a classical SPN structure but implementing a very compact S-box, a linear layer based on a sparse non-MDS binary matrix and a lightweight key schedule. The block size n can be 64 or 128 bits and for both versions the state is seen as a 4×4 matrix of 4-bit or 8-bit cells. Row 0 is considered the uppermost one and column 0 is taken to be the leftmost one. The numbering of the words inside the state matrix is as follows.

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

SKINNY follows the tweakey framework [32] and XORs a tweakey to the two upmost rows of the state. There exist three main variants for the tweakey size: t = n, t = 2n and t = 3n and the corresponding variant is denoted by SKINNY-n-t. Furthermore, the tweakey to block size ratio is denoted by z = t/n. The tweakey state is viewed also as a set of $z + 4 \times 4$ arrays of cells. For z = 3, which is the variant of interest to us, the three tweakey arrays are denoted by **TK1**, **TK2** and **TK3**.

The round function of SKINNY is depicted on Figure 4, and the number of times this function is iterated depends on both n and t, as shown in Table 3.

One round of SKINNY is composed of five operations applied in the following order: SubCells (SC), AddConstants (AC), AddRoundTweakey (ART), ShiftRows (SR) and MixColumns (MC). We now briefly describe the operations that are of interest to us.

Table 3. Number of rounds for each of the main variants SKINNY-n-t.

Block size n	t = n	t = 2n	t = 3n
64	32	36	40
128	40	48	56

SubCells (SC) This operation applies an S-box to all cells of the state. The table representation of the 8-bit S-box S used in the 128-bit variants is

AddRoundTweakey (ART) We describe this step only for the variants with z = 3. Here, the first and second rows of the 3 tweakey arrays **TK1**, **TK2** and **TK3** are extracted and XORed to the internal state, respecting the bit positions inside the arrays. More formally, if $\mathbf{IS}_{i,j}$ is the cell at the intersection of row i and j of the state, we have that for $(i,j) \in \{0,1\} \times \{0,1,2,3\}$:

$$IS_{i,j} = TK1_{i,j} \oplus TK2_{i,j} \oplus TK3_{i,j}$$
.

ShiftRows (SR) This operation rotates the cells inside a row to the right by a certain offset that depends on the row. More precisely, cells in row i, where $0 \le i < 4$, are rotated by i positions to the right.

MixColumns (MC) This operation updates the state by multiplying each column by a binary matrix M. This matrix, as well as its inverse are as follows.

$$\mathbf{M} = \begin{pmatrix} 1 & 0 & 1 & 1 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 \\ 1 & 0 & 1 & 0 \end{pmatrix}, \quad \mathbf{M}^{-1} = \begin{pmatrix} 0 & 1 & 0 & 0 \\ 0 & 1 & 1 & 1 \\ 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 1 \end{pmatrix}.$$

Next we describe the tweakey schedule of SKINNY-128-384, the variant we analyse in this work.

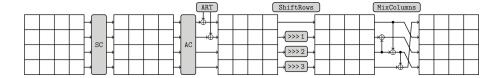


Fig. 4. Round function of SKINNY [4].

Tweakey schedule of SKINNY-128-384 At each round, all tweakey arrays are updated as follows (see also Figure 5). First, the same permutation P_T is applied on the cell positions of the 3 tweakey arrays: for all $0 \le i \le 15$, we have that $\mathbf{TK1}_i \leftarrow \mathbf{TK1}_{PT[i]}$ with

$$P_T = [9, 15, 8, 13, 10, 14, 12, 11, 0, 1, 2, 3, 4, 5, 6, 7],$$

and the same exact permutation is applied to the cells of TK2 and TK3. Finally, the cells of the first two rows of TK2 and TK3 are individually updated by the LFSR:

$$(x_7||x_6||x_5||x_4||x_3||x_2||x_1||x_0) \to (x_0 \oplus x_6||x_7||x_6||x_5||x_4||x_3||x_2||x_1),$$

where x_0 is the LSB in a byte.

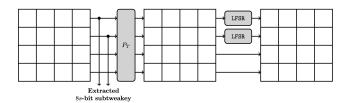


Fig. 5. Tweakey schedule of SKINNY. All tweakey arrays TK1, TK2 and TK3 follow the same transformation with the only exception that no LFSR is applied to TK1. [4]

Property. In most attacks, including ours, it is more efficient to guess round-key bits than key bits. Since the key-schedule of SKINNY is fully linear, guessing enough (e.g. 384 in the $\mathbf{TK3}$ model) independent round-key bits allows to uniquely determine the master key and thus all remaining round-key bits. SKINNY has a unique property that makes the evaluation of the dimension of any set of round-key bytes easy: in the \mathbf{TKx} model, a round-key byte $\mathbf{K_r}[\mathbf{i}]$ always depends on exactly x master key bytes, one from each \mathbf{TK} key and they all have the same index. Furthermore, given x round-key bytes from the 30 first rounds and depending on the same x master key bytes, they are always independent and allow to uniquely determine their x corresponding master key bytes.

We present now 3 attacks against round-reduced variants of SKINNY-128-384 by using our new differential meet-in-the-middle technique. We first describe a simple attack against 23 rounds as well as several improvements and trade-offs. We then explain how this attack can be extended to an attack on 24 rounds without increasing the attack's overall complexity. Finally, we describe a new attack against 25 rounds.

3.2 An attack against 23-round SKINNY-128-384

As explained in Section 2, differential meet-in-the-middle attacks rely on two classical cryptanalysis techniques: differential attacks and meet-in-the-middle attacks. The main idea is to use a meet-in-the-middle attack to generate a pair following a given differential in the middle rounds. Thanks to this procedure, we are able to extend a differential distinguisher by more rounds than with a classical early-abort procedure, as discussed in Section 2.4.

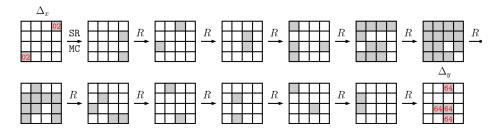


Fig. 6. Truncated differential trail for the attack on 23 rounds.

Differential. The truncated differential used in our attack against 23 rounds of SKINNY-128-384 is depicted in Figure 6. It has 56 active S-boxes, without counting those of the first and the last round. We verified that this truncated differential can be successfully instantiated by using the constrained programming Choco-solver [42], and more precisely the model developed by Delaune et al. to search for the best differential characteristics for the SKINNY family of block ciphers [18]. The best instantiation of this truncated differential has a probability of 2^{-119} and there are in total 2048 instantiations with this same probability. These instantiations can be divided into four groups $(\Delta_x^{(i)}, \Delta_y^{(i)})$, for i=1,2,3,4, each one having 512 trails inside, starting with the same difference $\Delta_x^{(i)}$ and terminating after 13 rounds with the same difference $\Delta_y^{(i)}$. We found as well many more differential trails with the same input/output differences but smaller probabilities: 2560 with probability 2^{-120} , 7168 with probability 2^{-121} , 18432 with probability 2^{-122} and 44800 with probability 2^{-123} . Thus the probability of the differential depicted on Figure 6 is higher than $2^{-105.9}$.

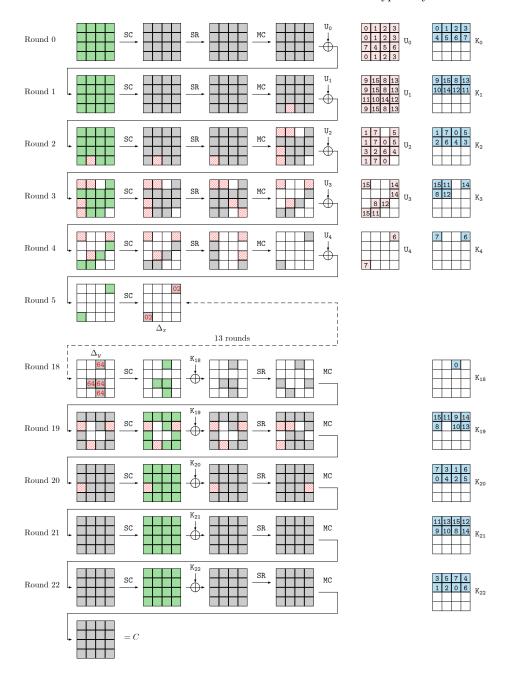


Fig. 7. Core attack against 23 rounds of SKINNY-128/384. Knowledge of blue key bytes allows to compute values of green ones and thus to propagate differences. No difference in both white and red bytes, but the red ones are required to compute green bytes. Indexes in subkey bytes are the indexes of the corresponding master key bytes. The equivalent subkeys U_i are computed as $MC(SR(K_i))$, from the original subkeys K_i .

The attack. We describe now our core attack against 23-round SKINNY-128-384.

- 1. Ask for the encryption of the whole codebook.
- 2. Randomly pick one plaintext/ciphertext pair (P, C).
- 3. For each possible value i of k_{in} compute the tuple (P, P, i) so that the difference on the state after the 6th S-box layer is $[0\ 0\ 0\ 2\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]$ (see Figure 6). Doing so requires to know the values of all the active S-boxes involved in the probability 1 transition $\Delta_x \to \Delta_P$, where Δ_P is the plaintext difference, and k_{in} is the set of subkey bytes needed to compute them from the plaintext.
- 4. Store all these tuples in a hash table. This step requires to guess 31 subkey bytes as depicted in Figure 7.
- 5. Similarly, for each possible value j of k_{out} compute the tuple (C, \widetilde{C}, j) so that the difference on the state before the 19th S-box layer is 0x64 on all active bytes. The set k_{out} involves 32 bytes and thus there are 2^{256} such tuples.
- 6. For each of them check for possible matches on the hash table. The match is performed on both the new ciphertext (i.e. $(\widetilde{P},\widetilde{C})$ must be a valid plaintext/ciphertext pair) as well as on the linear relations between the subkey bytes of the upper and lower guess.
- 7. Each match leads to a (full) key candidate that can be tried against very few additional plaintexts (3 in our case).
- 8. Repeat from Step 2 until the right key is retrieved.

Byte	k_{in}	k_{out}	# equations
0	$K_0[0], K_2[2]$	$K_{18}[2], K_{20}[4], K_{22}[6]$	2
1	$K_0[1], K_2[0]$	$K_{20}[2], K_{22}[4]$	1
2	$K_0[2], K_2[4]$	$K_{20}[6], K_{22}[5]$	1
3	$K_0[3], K_2[7]$	$K_{20}[1], K_{22}[0]$	1
4	$K_0[4], K_2[6]$	$K_{20}[5], K_{22}[3]$	1
5	$K_0[5], K_2[3]$	$K_{20}[7], K_{22}[1]$	1
6	$K_0[6], K_2[5], K_4[3]$	$K_{20}[3], K_{22}[7]$	2
7	$K_0[7], K_2[1], K_4[0]$	$K_{20}[0], K_{22}[2]$	2
8	$K_1[2], K_3[4]$	$K_{19}[4], K_{21}[6]$	1
9	K ₁ [0]	$K_{19}[2], K_{21}[4]$	0
10	K ₁ [4]	$K_{19}[6], K_{21}[5]$	0
11	$K_1[7], K_3[1]$	$K_{19}[1], K_{21}[0]$	1
12	$K_1[6], K_3[5]$	K ₂₁ [3]	0
13	K ₁ [3]	$K_{19}[7], K_{21}[1]$	0
14	$K_1[5], K_3[3]$	K ₁₉ [3], K ₂₁ [7]	1
15	K₁[1], K₃[0]	K ₁₉ [0], K ₂₁ [2]	1

Table 4. Subkey bytes involved in the 23-round core attack.

The data complexity of this attack is 2^{128} since in Step 1 we ask for the encryption of the full codebook. The memory complexity is determined by Step 3

in which 2^{248} words of 128+248=376 bits each are stored. Note that we do not need to store C_1 since it is common to all tuples. Thus the memory complexity is $2^{249.5}$ 128-bit words. The time complexity is 2^{248} for computing the hash table, 2^{256} for performing Step 4, and, as shown in Table 4, $k_{in} \cup k_{out}$ is the full key so that the complexity of Step 6 is $2^{384-128}=2^{256}$. Finally, the attack has to be repeated $2^{105.9}$ times (the probability of the distinguisher) in order to construct one right differential pair. Hence, the overall complexity of our attack is $2^{105.9} \times 2^{256} = 2^{361.9}$.

Decreasing memory complexity. It is possible to decrease the memory complexity of the attack by avoiding the match on the linear relations between both k_{in} and k_{out} . Indeed, since the key-schedule of SKINNY is fully linear, we can first guess the intersection of k_{in} and k_{out} , and only then run the attack. The dimension of the intersection is 248 + 256 - 384 = 120 and thus the memory complexity can be decreased to $2^{249.5-120} = 2^{129.5}$.

Data-time-memory trade-off. To decrease the data complexity of our attack, as described in Section 2.3, it is possible to only ask for the encryption of a portion of the whole codebook, let say 2^{128-x} plaintext/ciphertext pairs. In this case, the probability that we have access to the corresponding ciphertext of \widetilde{P} is 2^{-x} and the attack has to be ran 2^x times to compensate. Overall, the complexity of our 23-round attack is then $\mathcal{D}=2^{128-x}$ plaintext/ciphertext pairs, $\mathcal{M}=2^{129.5-x}$ 128-bit words and $\mathcal{T}=2^{361.9+x}$ encryptions. To expect at least one pair following the differential under the extra constraint on the plaintexts, x cannot be higher than (128-105.9)/2=11.05.

As explained in Section 2.3, in practice, given any pair of ciphertexts, we can enumerate the possible values for both k_{in} and k_{out} with a complexity roughly equivalent to the number of solutions. Such a procedure is described in Section 3.3. Thus, the trade-off does not increase the time complexity and the overall complexity of our attack is $D = 2^{117}$, $T = 2^{361.9}$ and $M = 2^{118.5}$.

3.3 Enumeration Procedure of k_{out} for the 23-round Attack

In this section we describe a procedure to retrieve the possible values of k_{out} in the case where the pair of ciphertexts is given. Its complexity is 2^{128} simple operations, showing that the data/time/memory trade-off described in Section 2.3 can be applied without increasing the time complexity. Since the key is not applied on the full state, the procedure is more complex than a classical rebound but still relies on the fact that, on average, knowing the differences at both the input and output of an Sbox leads to one pair of actual values.

The steps of our enumeration procedure are depicted on Figure 3.3. The main idea is to propagate differences from the ciphertexts to Round 18, get the actual values since differences in this internal state are fully known, and propagate them back to the ciphertexts to obtain the key material we want. Except from Step 1 in which we guess 8 values, all following steps perform one guess each.

Steps 7 and 8 have both a probability of success of 2^{-8} and thus we expect only $2^{13\times8}=2^{104}$ partial solutions at the end of Step 8.

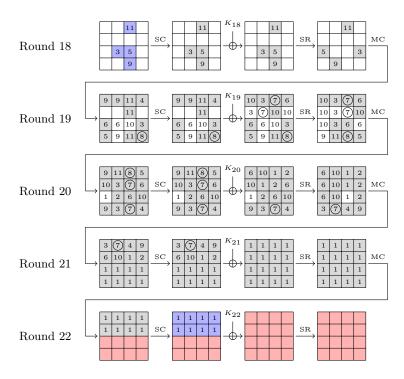


Fig. 8. Enumeration procedure of k_{out} for the 23-round attack. Differences in blue cells and actual values in red cells are known. No difference in white cells.

3.4 Extension to 24 rounds

Our differential meet-in-the-middle attack against 23-round SKINNY can be extended to an attack against 24 rounds without increasing its overall complexity by using the generic improvement presented in Section 2.2. This can be achieved since on one hand the key-schedule is linear (and enough subkey bytes are involved in our attack so that the master key is fully retrieved) and on the other hand the subkey is only applied on half of the state in each round. The scenario of this new attack is quite similar to the original one:

- 1. Ask for the encryption of the whole codebook.
- 2. Pick 2^{64} plaintext/ciphertext pairs (P_{ℓ}, C_{ℓ}) such that $MC^{-1}(C_{\ell})$ is constant on the last two rows as depicted in Figure 9. Here we exploit the fact that the round key is only applied on the first two rows of the internal state.

- 3. As for this original attack, compute all possible tuples $(P_{\ell}, \widetilde{P}_{\ell}^{i}, i)$ for each value i of k_{in} and each P_{ℓ} from the structure defined at the previous step such that the state difference after the 6th S-box layer is 0x02 on both active bytes.
- 4. Store them in a hash table. Note that the tuples are computed for all the 2^{64} plaintexts selected at Step 2 so the memory complexity is $2^{248+64} = 2^{312}$ 504-bit words.
- 5. For each value j of k_{out} and each state $S_{23,\ell}$ coherent with Step 2 (i.e. 2^{64} states, one for each possible value of the subkey K_{23}), compute all possible tuples $(S_{23,\ell}, \widetilde{S}_{23,\ell}^j, j)$ so that the difference on the state before the 19th S-box layer is 0x64 on the four active bytes.
- 6. Check for possible matches on the hash table. The match is now performed on three quantities:
 - the difference between the last states: $C \oplus \widetilde{C} = MC \circ SR(SC(S_{23}) \oplus SC(\widetilde{S}_{23}))$. This is a 64-bit filter because the difference is zero on the two last rows since $MC^{-1}(C)$ is constant on these rows.
 - the filter on the keys (from key schedule equations): a 120-bit filter as for the original attack against 23 rounds (15 equations on 8 bits each, see Table 4).
 - the filter on the keys (from equations describing the last round). Indeed, since $k_{in} \cup k_{out}$ generates the master key, K_{23} can be rewritten as $f(k_{in}) \oplus g(k_{out})$ where f and g are both linear and, because of the linearity of all the operations, the equation $C = \text{MC}(\text{SR}(\text{SC}(S_{23}) \oplus K_{23}))$ can thus be rewritten as $C \oplus \text{MC}(\text{SR}(f(k_{in}))) = \text{MC}(\text{SR}(\text{SC}(S_{23}) \oplus g(k_{out})))$. This represents a 64-bit filter.
- 7. Repeat from Step 2 until the right key is retrieved.

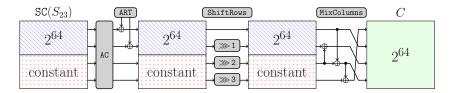


Fig. 9. Last round of the attack against 24 rounds.

The attack has to be repeated enough times so that the structure contains at least one pair following the differential. Since during Step 2 we generate 2^{64} pairs and since the probability of the differential is $2^{-105.9}$, the procedure has to be repeated $2^{41.9}$ times. Thus the data complexity is 2^{128} (i.e. the whole codebook is needed), the memory complexity is around 2^{314} 128-bit words and the time complexity $2^{256+64+41.9} = 2^{361.9}$ encryptions.

Note that previous improvements regarding both the memory and data complexities still apply and thus our attack has complexity: $\mathcal{D} = 2^{128-11} = 2^{117}$

plaintext/ciphertext pairs, $\mathcal{M}=2^{194-11}=2^{183}$ 128-bit words and $\mathcal{T}=2^{361.9}$ encryptions.

3.5 An attack against 25 rounds of SKINNY-128-384

To mount a differential meet-in-the-middle attack against 25 rounds of SKINNY, we used the differential depicted in Figure 10. The best instantiation of this truncated differential has a probability of 2^{-131} . By fixing the difference of the active bytes to 0x32 at the input and to 0x64 at the output, we found several instantiations with a high enough probability: 2048 with probability 2^{-131} , 10240 with 2^{-132} , 28672 with 2^{-133} and finally 73728 trails with probability 2^{-134} . Thus, the probability of the depicted differential is higher than $2^{-116.5}$. This differential is then extended by 4 rounds to the plaintext and 5 rounds to the ciphertext to reach 24 rounds as depicted in Figure 11.

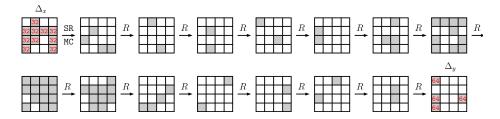


Fig. 10. Truncated differential trail for the attack on 25 rounds.

The key bytes involved in the attack are given in Table 5, leading to a complexity of $\mathcal{D}=2^{128}$ data, $\mathcal{T}=2^{256}\times 2^{116.5}=2^{372.5}$ encryptions and $\mathcal{M}=2^{249.5}$ 128-bit words. Furthermore, the dimension of the intersection between both k_{in} and k_{out} is once again 248+256-384=120, which allows to reduce the memory complexity to $2^{129.5}$ 128-bit words.

As for the 23-round attack described above, this attack can be extended by one round without increasing its overall complexity. As a consequence, and after applying the data/time/memory trade-off presented in Section 2.3, the complexity of our attack against 25 rounds is $\mathcal{D}=2^{128-x}$ plaintext/ciphertext pairs, $\mathcal{M}=2^{194-x}$ 128-bit words and $\mathcal{T}=2^{372.5+x}$ encryptions. In this case, x cannot be higher than (128-116.5)/2=5.75. Furthermore, we can again apply this trade-off without increasing the time complexity and thus the final complexity is $D=2^{122.3}$, $T=2^{372.5}$ and $M=2^{188.3}$.

3.6 Comparison of the attacks on SKINNY-128-384 with differential attacks

One may wonder whether the improved attacks on SKINNY-128-384 and in particular the one reaching 25 rounds, are exclusively due to the quality and the

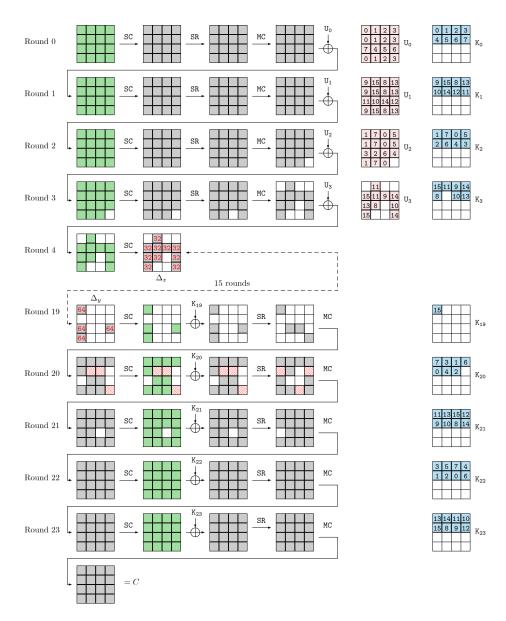


Fig. 11. Core attack against 24 rounds of SKINNY-128-384. Knowledge of blue key bytes allows to compute values of green ones and thus to propagate differences. No difference in both white and red bytes, but the red ones are required to compute green bytes. Indexes in subkey bytes are the indexes of the corresponding master key bytes.

Byte	k_{in}	k_{out}	# equations
0	K ₀ [0], K ₂ [2]	K ₂₀ [4], K ₂₂ [6]	1
1	K ₀ [1], K ₂ [0]	K ₂₀ [2], K ₂₂ [4]	1
2	K ₀ [2], K ₂ [4]	K ₂₀ [6], K ₂₂ [5]	1
3	K ₀ [3], K ₂ [7]	$K_{20}[1], K_{22}[0]$	1
4	$K_0[4], K_2[6]$	$K_{20}[5], K_{22}[3]$	1
5	K ₀ [5], K ₂ [3]	$K_{22}[1], K_{24}[0]$	1
6	$K_0[6], K_2[5]$	$K_{20}[3], K_{22}[7]$	1
7	$K_0[7], K_2[1]$	$K_{20}[0], K_{22}[2]$	1
8	$K_1[2], K_3[4]$	$K_{21}[6], K_{23}[5]$	1
9	$K_1[0], K_3[2]$	$K_{21}[4], K_{23}[6]$	1
10	$K_1[4], K_3[6]$	$K_{21}[5], K_{23}[3]$	1
11	$K_1[7], K_3[1]$	$K_{21}[0], K_{23}[2]$	1
12	K ₁ [6]	$K_{21}[3], K_{23}[7]$	0
13	$K_1[3], K_3[7]$	$K_{21}[1], K_{23}[0]$	1
14	$K_1[5], K_3[3]$	$K_{21}[7], K_{23}[1]$	1
15	K ₁ [1], K ₃ [0]	$K_{19}[0], K_{21}[2], K_{23}[4]$	2

Table 5. Subkey bytes involved in the 24-round core attack.

length of the differential distinguisher used. In this section we show that this is not the case, and that the best classical differential attacks that we could build using the same differential reached strictly less rounds than our attack. We show that even when considering optimal lower bounds for the complexities of classical differential attacks, it is not possible to reach more than 24 rounds for SKINNY-128-384 this way. This shows that differential MITM attacks can reach more rounds than differential ones in certain scenarios.

A lower bound on the complexity of differential attacks can be determined in part by the number of partial key candidates. When the key schedule is linear, as in SKINNY, the partial candidates for the key can be obtained optimally and in parallel for the input and the output, and can then be merged with respect to the common information between both partial keys, given by the key schedule.

In particular, for 24 rounds of SKINNY-128-384 starting from the differential of Figure 10, and considering all the possible combinations for the number of input, r_{in} , and output, r_{out} rounds, the complexity, given by Eq.(1), cannot be smaller than:

$$2^{116+128}(2^{120} + 2^{128} + 2^{120+128-120}) = 2^{373},$$

where the parameters (with respect to Eq.(1)) are p = 116, s = 128, c = 0, and $C_k = (2^{120} + 2^{128} + 2^{120+128-120})$. As the number of pairs needed to find one pair that verifies the input difference and also the differential path is $2^{116+128}$, we need a structure of size 2^{122} . If we solve both parts sequentially, the complexity will exceed exhaustive search, as the most of the external keys are independent of those in the other part. Instead, considering both parts in parallel, we have 64 + 64 + 64 + 56 keybits involved in the input for a condition on 128 bits of recovering the input difference (so 2^{120} key candidates), and 64 + 64 + 64 + 56 + 8

keybits involved in the output part, with 128-bit conditions (so 2^{128} key candidates). The memory need is 2^{128} for the parallel computation. The linear relations between both partial keys are 64+56, given by the even and odd subkeys respectively. So the previous result provides a lower bound on the complexity that such an attack would obtain. If we try to add one extra round and attack 25 rounds, a minimal additional factor of 2^{64} has to be added to one of the parallel computations, as the number of partial solutions will increase by this amount. This would be too expensive and we can therefore conclude that we cannot build classical differential attacks on 25 rounds of SKINNY-128-384 based on this distinguisher.

This extra round can be added in our case due to the different nature of the attack, and its relation to MITM cryptanalysis. Therefore, it is fair to conclude that in this case, differential meet-in-the-middle attacks are more powerful than classical differential attacks, reaching one extra round while having a similar complexity.

4 New attack against 12-round AES-256 in the related-key setting

To show how powerful our new cryptanalysis technique is, we propose an application against AES-256 in the related-key model. It is well known that this version of AES was fully broken by Biryukov and Khovratovich in [11]. However, this attack is a boomerang one and thus requires 4 related keys as well as both encryption and decryption oracles. In our case, we propose an attack in the chosen plaintext setting and requiring only 2 related keys. It is depicted in Figure 14 and uses a differential characteristic similar to the one from [10].

In this section we first give a short description of AES-256, then we explain the key generation process that has to be performed by the adversary and finally we explain the whole attack.

4.1 Description of AES-256

The Advanced Encryption Standard [26] is a Substitution-Permutation Network (SPN) that can be instantiated using three different key sizes: 128, 192, and 256 bits. The 128-bit plaintext initializes the internal state viewed as a 4×4 matrix of bytes, i.e. values in the finite field \mathbb{F}_{256} , which is defined using the irreducible polynomial $x^8 + x^4 + x^3 + x + 1$ over \mathbb{F}_2 . Depending on the version of the AES, N_r rounds are applied to that state and $N_r = 14$ for the 256-bit version. Each of the N_r rounds (see Figure 12) applies four operations to the state matrix (except in the last round where the MixColumns operation is omitted):

- AddRoundKey (AK) adds a 128-bit subkey to the state.
- SubBytes (SB) applies the same 8-bit to 8-bit invertible S-Box S 16 times in parallel on each byte of the state.
- ShiftRows (SR) shifts the *i*-th row left by *i* positions.

- MixColumns (MC) replaces each of the four columns C of the state by $M \times C$ where M is a constant 4×4 maximum distance separable matrix over \mathbb{F}_{256} .

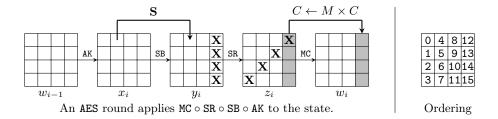


Fig. 12. Description of one AES round and the ordering of bytes in an internal state

After the N_r -th round has been applied, a final subkey is added to the internal state to produce the ciphertext. The key expansion algorithm to produce the $N_r + 1$ subkeys is described in Figure 13. We refer to the original publication [26] for further details.

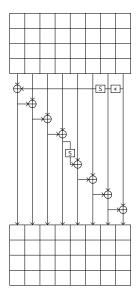


Fig. 13. Key schedule of AES-256

4.2 Generation of the related keys

Because the key schedule of AES involves S-boxes, it is impossible to control the difference of each key byte, otherwise the possible values of some key bytes would be restricted, limiting the choice of the master key for the adversary and thus leading to weak-key attacks.

In our attack, the adversary is free to pick any master key K and we assume that he can then perform the following procedure to generate a related key K'. First, we choose the difference a to any non-zero value and another value b such that the differential transition $b \to a$ through the S-box happens with probability 2^{-6} . In the case of our attack, as depicted in Figure 14, the adversary applies the difference b on the first byte of k_8 and the difference MC((a, 0, 0, 0)) to the first column of k_9 . He finally reconstructs K' from (k'_8, k'_9) .

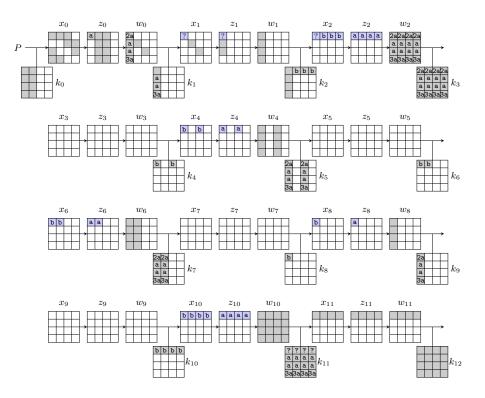


Fig. 14. Differential characteristic used in our 12-round attack. No difference in white cells. Transitions in blue belong to the distinguisher.

4.3 The attack

The distinguisher we use for the attack starts from columns 0 and 3 of state w_0 and columns 1 and 2 of z_1 and stops at state x_{11} . Both transitions $\Delta x_1[0] \rightarrow$

 $\Delta z_1[0]$ and $\Delta x_2[0] \to \Delta z_2[0]$ depend on uncontrollable differences from the key and thus there is a probability of 2^{-2} that the characteristic does not hold. However, if it does, the average probability of the distinguisher is $2^{-(7\times 2+6\times 12)} = 2^{-86}$.

Step 1. The difference on P belongs to a vector space of dimension 11 since the differences on bytes 10, 11, 12 and 15 have to be 0 and $\Delta P[1] = \Delta P[5]$ (because they are both equal to $\Delta k_2[1]$). Thus, we start by asking for the encryption of a structure of 2^{88} messages under the key K and a similar one under the key K'.

Step 2. We then pick a message P and the goal is to generate all the possible \widetilde{P} and to associate to each of them the corresponding key values. First, we guess 9 bytes of k_0 and 2 bytes of k_1 to compute $z_0[0]$ and both $z_1[1]$ and $z_1[2]$. We then guess the difference in the first column of k_2 and propagate backwards the differences and values to obtain \widetilde{P} . Furthermore, guessing the difference of k_2 gives us the values of the last column of k_3 since both the difference at the input and output of the S-box would be known for each byte of this column. As a result, we generate $2^{(9+2+4)\times 8} = 2^{120}$ tuples for

$$(\widetilde{P}, k_0[0, 2, 3, 4, 7, 8, 9, 13, 14], k_1[5, 10], k_3[12, 13, 14, 15]).$$

Step 3. Starting from the same message P as above and taking its corresponding ciphertext C, the goal is now to generate all the possible \widetilde{C} . The procedure is quite straightforward. First, we guess the difference of $k_{11}[0]$ as well as the difference on the first column of k_{12} . This gives us the difference on both k_{11} and k_{12} . Then we guess the first line of k_{12} except the last byte (which is obtained by computing $k_{12}[8] \oplus k_{10}[12]$) and we can compute \widetilde{C} . As a result, we generate $2^{(5+3)\times 8} = 2^{64}$ tuples for

$$(\widetilde{C}, k_{10} \texttt{[12]}, k_{11} \texttt{[12,13,14,15]}, k_{12} \texttt{[0,4,8,12]}).$$

Step 4. We now look at matches between both lists of tuples so that $(\widetilde{P},\widetilde{C})$ is a valid plaintext-ciphertext pair. We expect around $2^{120+64-128}=2^{56}$ matches, each leading to a possible value for $\widetilde{P},\widetilde{C},\ k_0[0,2,3,4,7,8,9,13,14],\ k_1[5,10],\ k_3[12,13,14,15],\ k_{10}[12],\ k_{11}[12,13,14,15],\ k_{12}[0,4,8\ and\ 12].$

Using a simple Gaussian elimination, we found that it is enough to guess 9 extra key bytes to fully reconstruct the master key, which then has to be checked against few additional data.

Complexity. The time complexity of Steps 2 to 4 is $\max(2^{120}, 2^{64}, 2^{72}) = 2^{120}$ and the memory complexity is around 2^{64} tuples of 128 + 64 = 192 bits since only the list built at Step 3 has to be stored. The attack has to be repeated 2^{86} times (the probability of the distinguisher), leading to an overall complexity of 2^{206} . The data complexity is 2^{89} chosen plaintexts, 2^{88} messages for each of both keys.

Note that the probability that the trail holds is 2^{-2} because of the transitions $\Delta x_1[0] \to \Delta z_1[0]$ and $\Delta x_2[0] \to \Delta z_2[0]$. Thus, it might be needed to repeat

the attack several times to retrieve the key, either by asking another key K' computed with another value of (a,b) or by modifying the position of the zero difference on the first column of z_1 (3 possible choices).

5 Conclusion and open problems

We introduced in this work a new cryptanalysis technique, that we called the differential MITM attack. We managed to successfully apply this new technique to SKINNY-128-384 and AES-256 in two different settings. Our attack against SKINNY allowed us to provide the best single-key attack against the analyzed variant by reaching two more rounds than the previously best known attack. Our application on AES-256 permitted to break 2 rounds more than the previously best attack that used two related keys or less.

The introduction of this new technique releases naturally numerous questions and opens many new research directions. First, we would like to further understand the link between the new attack and classical MITM attacks and how these two attacks can be compared. For example, we would like to identify for what kind of primitives the quantity of the involved key material in the differential MITM attack would be typically smaller compared to a classical MITM attack applied to the same cipher in a similar setting. We did some preliminary experiments on different ciphers by mounting both types of attacks in a comparable way and in some cases the amount of key bits to be guessed was smaller for the new attack while in some other cases this same amount was smaller for a classical MITM attack. It would therefore be interesting to be able to predict in an easy way, how this quantity compares for the two attacks. It would also be interesting to understand the details that allow our technique to be more performant than classical differential attacks and the other way round.

As MITM attacks combine particularly well with the technique of bicliques, another natural question is whether differential MITM attacks combine well with bicliques as well. Furthermore, is it possible to find any concrete application where the combination of a differential MITM with bicliques could improve previous MITM or other attacks? Finally, can the technique of bicliques be combined with the method of partitions we proposed in the case of partial subkey additions, and how do they compare?

A last open question is whether instead of combining MITM techniques with differential attacks, one could successfully combine MITM with some other well-known family of cryptanalysis, such as for example linear or differential-linear attacks.

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A Automatic detection of involved keys

We provide here a simple algorithm to search, given a differential, for efficient applications of the new attack. Indeed, in many cases, it is technically very easy to exactly determine which information about the key is required in the forward or backward computation. As often, when it comes to the question of dependency only, the easiest and less error-prone method is to experimentally determine which bits have an actual influence. Assume we are given (the implementation of) a function $F: \mathbb{F}_2^n \to \mathbb{F}_2^m$ and want to determine if the *i*th input bit of x has an influence on the output of F(x), that is if there exist an input x such that

$$F(x) \neq F(x \oplus e_i),$$

where e_i is the vector that has a one exactly at position i.

For this, we could simply take a random input x and compute $F(x) \oplus F(x \oplus e_i)$. If the result is non-zero, we know that the output depends on the ith input bit. After repeating this process a few times and if we always get zero as a result, we conclude that the ith bit does not have an influence on the output. The later decision might of course be wrong (while the former never is). However, for our applications this is (i) very unlikely to happen due to the construction of the round functions and (ii) irrelevant for the attacks as a key bit that influences the output only in one out of many outputs usually does not have to be guessed.

Focusing on our target, given the implementation of the cipher, i.e. in particular the (round-reduced) encryption and decryption procedures along with the key schedule, we can easily process as represented in Algorithm 2.

Algorithm 2 CHECK DEPENDENCIES

Input: An Implementation of the round reduced encryption and decryption E_r , a difference Δ

Output: The set of key bits K required to propagate Δ through E_r^{-1}

```
1: \mathcal{K} \leftarrow \emptyset
 2: for each i from 0 to n-1 do
 3:
         for each t from 1 to tries do
 4:
              x \leftarrow \text{random message}
 5:
              k \leftarrow \text{random key}
 6:
              y_1 \leftarrow E_r(k,x)
                                                                                       ▶ Query Encryption
              z_1 \leftarrow E_r^{-1}(k, y_1 \oplus \Delta)
                                                                                       ▷ Query Decryption
 7:
              y_2 \leftarrow E_r(k \oplus e_i, x)
 8:
                                                                 ▶ Query Encryption with bit flipped
              z_2 \leftarrow E_r^{-1}(k \oplus e_i, y_2 \oplus \Delta)
                                                                 ▶ Query Decryption with bit flipped
9:
              if z_1 \neq z_2 then
10:
11:
                   Include key bit i to K
              end if
12:
13:
         end for
14: end for
15: Return K
```

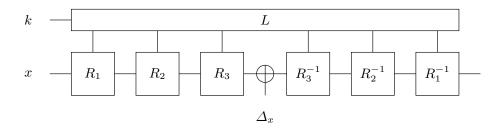
The nice feature of the algorithm is that it works for any cipher structure and without the need to know or implement any internal details. However, on this generality we might miss many possible improvements. As an example, consider the key schedule of SKINNY. Here, every round-tweak-key bit is the sum of three bits of (updated) master tweak-key bits. The algorithm above would (correctly) detect the dependence of the output on those three bits, but obviously guessing the sum of the bits is enough. We can easily adopt the above algorithm to take into account linear (tweak) key-schedules. The main idea is not to flip master key-bits directly, but rather round-key bits.

Let us denote the linear key schedule by $L: \mathbb{F}_2^{\kappa} \to \mathbb{F}_2^{n\dot{r}}$. The *i*th bit of the expanded key can thus be written as $\langle L_i, k \rangle$ where L_i denotes the *i*th row of the matrix corresponding to L. Furthermore we denote by \hat{E}_r the encryption

excluding the key schedule, i.e.

$$E_r(k,x) = \widehat{E}_r(L(k),x).$$

Instead of master key-bits, we now aim at computing the round-key bits that the encryption depends on and collecting the corresponding linear combinations of the master-key.



Algorithm 3 CHECK LINEAR-DEPENDENCIES

Input: An Implementation of the round reduced encryption and decryption \widehat{E}_r , the key-schedule L and a difference Δ

Output: A linear subspace of key bits $\mathcal K$ required to propagate Δ through $\widehat E_r^{-1}$

```
1: \mathcal{K} \leftarrow \{\}
 2: for each i from 0 to n \dots r - 1 do
 3:
          for each t from 1 to tries do
 4:
               x \leftarrow \text{random message}
 5:
               k \leftarrow \text{random key}
                                                                                                \rhd \ {\rm Query} \ {\rm Encryption}
 6:
               y_1 \leftarrow \widehat{E}_r(L(k), x)
 7:
               z_1 \leftarrow \widehat{E}_r^{-1}(L(k), y_1 \oplus \Delta)
                                                                                                \triangleright Query Decryption
               y_2 \leftarrow \widehat{E}_r(L(k) \oplus e_i, x)
 8:
                                                                        ▷ Query Encryption with bit flipped
               z_2 \leftarrow \widehat{E}_r^{-1}(L(k) \oplus e_i, y_2 \oplus \Delta)
                                                                        ▷ Query Decryption with bit flipped
 9:
10:
               if z_1 \neq z_2 then
                     Include L_i to K
11:
                end if
12:
13:
          end for
14: end for
15: Return span(\mathcal{K})
                                                      \triangleright Vector space spanned by the corresponding L_i
```

The vector-space contains the information that is sufficient to guess in order to compute the upper part of the attack. The dimension of $\mathcal K$ corresponds to the amount of information that has to be guessed, its Gauss-Jordan-basis contains information on which master key bits can be guessed equivalently. This algorithm again is easy to adapt given an implementation of a cipher. In practice,

given a differential $\Delta_x \to \Delta_y$, we can apply this algorithm on both (E_{in}, Δ_x) and (E_{out}^{-1}, Δ_y) to respectively get the sets k_{in} and k_{out} required in our new framework.

For SKINNY, Algorithm 3 allows to complete both the differential trails given in Section 3 into attacks against 23 and 24 rounds, that we will finally extend by one additional round at the end to get the currently best known results on SKINNY-128-384.