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The aim of this work is to improve musculoskeletal-based models of the upper-limb Wrench Feasible Set i.e. the set of achievable maximal wrenches at the hand for applications in collaborative robotics and computer aided ergonomics. In particular, a recent method performing wrench capacity evaluation called the Iterative Convex Hull Method is upgraded in order to integrate non dislocation and compression limitation constraints at the glenohumeral joint not taken into account in the available models. Their effects on the amplitude of the force capacities at the hand, glenohumeral joint reaction forces and upper-limb muscles coordination in comparison to the original iterative convex hull method are investigated *in silico*. The results highlight the glenohumeral potential dislocation for the majority of elements of the wrench feasible set with the original Iterative Convex Hull method and the fact that the modifications satisfy correctly stability constraints at the glenohumeral joint. Also, the induced muscles coordination pattern favors the action of stabilizing muscles, in particular the rotator-cuff muscles, and lowers that of known potential destabilizing ones according to the literature.

1. Introduction

One fundamental assumption of human centered robot control is the ability to measure or estimate the physical capacity of humans to continuously adapt the robot assistance level based on the real-time need of its human counterpart (Carmichael and Liu, 2013; Figueredo et al., 2021; Pehlivan et al., 2016). Moreover, within the framework of computer-aided design of workstations, the knowledge of human force capacities enables to evaluate to what extent a task is in adequacy with the capacities of the operators (Figueredo et al., 2021; Perdeaux et al., 2010), to define ergonomic criteria of discomfort (Maurice et al., 2017) and to implement models of muscular fatigue (Ma et al., 2010; Savin et al., 2017, 2021). Different methodologies have been proposed to assess human force capacities. Data based approaches rely on the availability of experimental data (Khalaf and Parnianpour, 2001; Guenzkofer et al., 2012; Lannersten et al., 1993; Hall et al., 2021; Kotte et al., 2018; La Delfa and Potvin, 2017) which are numerous but limited to particular postures. Within the context of model based approaches, several algorithms using musculoskeletal models, predominantly of the upper-limb, are available (Skuric et al., 2022; Valero-Cuevas, 2009; Carmichael and Liu, 2013; Ingram et al., 2016). From posture, muscular forces and muscles moment arms, the set of achievable wrench at the hand called the Wrench Feasible Set (WFS) can be computed under the form of a convex polytope. Its main interest is that it allows an exhaustive evaluation of force capacities whatever the direction of force application or the posture. The base assumption of all these algorithms is that muscular forces are the limiting factor. However, other factors can limit force capacities such as joint stability (Blache et al., 2017a,b; Ingram et al., 2016), safety mechanisms implemented by the central nervous system for preventing joint injuries (Assila et al., 2021; Maurice et al., 2017) or balance constraints (Perdeaux et al., 2010). When considering the upper-limb and the glenohumeral (GH) joint, the stability issue is of paramount importance (Lippitt et al., 1993; Dickerson et al., 2008; Labriola et al., 2005; Blache et al., 2017a; Sinha et al., 1999). Indeed, this joint has the greatest range of motion of all the joints of the human body. This is due to the relative laxity of the shoulder ligaments, but especially to the shallow conformation of the humeral head on the glenoid fossa, which surface is relatively flat. The side effect is that the GH joint is prone to dislocation when the shear component of the GH Joint Reaction Force (JRF) exceeds a certain percentage of its compressive component (Lippitt et al., 1993; Dickerson et al., 2008). To prevent this phenomenon, several muscles including the rotator cuff muscles act to stabilize the GH joint by orienting the JRF toward the middle of the glenoid fossa while pressing the humeral head against it (Lippitt et al., 1993). Therefore, the induced muscle coordination pattern may have a significant effect on strength capacities and, if not accounted for, may lead to a potential overestimation of the WFS. However, to our knowledge, the only works implementing GH non dislocation constraints considered the shoulder torque feasible set only (Ingram et al., 2016) or

61 were used to assess shoulder muscles forces with inverse dynamics and static optimization (Dickerson
62 et al., 2008; Blache et al., 2017b,a) or with EMG assisted optimization (Assila et al., 2020, 2021).

63 To fill this gap and to improve models of WFS computed from musculoskeletal models, the recent
64 iterative convex hull method (ICHM) (Skuric et al., 2022) is upgraded in order to integrate two important
65 limiting factors of force capacities i.e. GH joint non dislocation and limitation of GH JRF compression
66 component. The core of the ICHM consists in finding the vertices of the WFS by solving a linear
67 programming problem. To ensure GH joint non dislocation, additional constraints take the form
68 of inequalities involving the admissible ratio between shear and compressive components of the GH
69 JRF (Lippitt et al., 1993; Dickerson et al., 2008; Blache et al., 2017b; Ingram et al., 2016). Also
70 additional constraints bound the GH JRF compression. In this context, the objective of this work is to
71 test *in silico* the effects on the WFS of the ICHM implementation incorporating the GH constraints.
72 In particular, the following points are verified:

- 73 • P_1 : the decrease of the range of maximal achievable forces,
- 74 • P_2 : the orientation of the GH JRF toward the middle of the glenoid fossa,
- 75 • P_3 : the decrease of the amplitude of the GH JRF compression,
- 76 • P_4 : the modifications of muscle force coordination pattern with an expected increase in the
77 contribution of the rotator cuff (Blache et al., 2017a) and biceps muscles (Labriola et al., 2005)
78 and a decrease in that of the deltoids and pectoralis major muscles (Labriola et al., 2005).

79 They are tested by considering a validated musculoskeletal model of the upper-limb (Saul et al.,
80 2015) in three different postures.

81 2. Methods

82 2.1. Wrench Feasible Set definition

83 Let us consider a serial kinematic chain \mathcal{C} with n rotational degrees of freedom (dofs) representing
84 the upper-limb. Its configuration is specified by the joint angle vector $\mathbf{q} \in \mathbb{R}^n$ and the joint velocity
85 vector $\dot{\mathbf{q}} \in \mathbb{R}^n$. $\boldsymbol{\tau} \in \mathbb{R}^n$ refers to the joint torque vector. The task space is of dimension $m = 3$, the end
86 effector position is defined by $\mathbf{x} \in \mathbb{R}^m$ and the end-effector wrench by $\mathbf{F} \in \mathbb{R}^m$. \mathcal{C} is actuated by d
87 muscles ($d > n$) producing muscular tension force $\mathbf{t} \in \mathbb{R}^d$. The joint torque $\boldsymbol{\tau} \in \mathbb{R}^n$, generated by the
88 muscle force $\mathbf{t} \in \mathbb{R}^d$ at joint configuration $\mathbf{q} \in \mathbb{R}^n$, can be calculated as follows:

$$\boldsymbol{\tau} = -L^T(\mathbf{q})\mathbf{t} \quad (1)$$

89 $L(\mathbf{q})^T \in \mathbb{R}^{n \times d}$ is the transpose of the moment arm matrix, which is defined as the muscle length
 90 Jacobian relating the space of joint and muscle length velocities

$$\dot{\mathbf{l}} = L(\mathbf{q})\dot{\mathbf{q}}, \quad L_{ij} = \frac{\partial l_i}{\partial q_j} \quad (2)$$

91 where $\dot{\mathbf{l}} \in \mathbb{R}^d$ is the muscle lengthening velocity and $\dot{\mathbf{q}} \in \mathbb{R}^n$ the joint angular velocity. The negative
 92 sign in equation (1) makes the force applied in the length shortening direction of the muscle positive.

93 The muscles have a limited force capacity and each component $t_i = 1..d$ of \mathbf{t} is to lie within an
 94 interval $[\underline{t}_i, \bar{t}_i]$. Also, $0 \leq \underline{t}_i < \bar{t}_i$ because a muscle can only pull and not push. The tension t_i developed
 95 by muscle i is defined according to a Hill type model (Saul et al., 2015).

96 A general achievable set of muscle-tendon forces $\mathbf{t} \in [\underline{\mathbf{t}}, \bar{\mathbf{t}}]$ forms a d -dimensional hyper-rectangle
 97 with side lengths equal to the ranges of each of the d muscle forces. Using the moment arm matrix $L(\mathbf{q})$
 98 and equation (1) this hyper-rectangle can be projected into the n -dimensional space of joint torques
 99 $\boldsymbol{\tau}$, forming the convex polytope of achievable joint torques \mathcal{P}_τ

$$\mathcal{P}_\tau = \{ \boldsymbol{\tau} \in \mathbb{R}^n \mid \boldsymbol{\tau} = -L^T(\mathbf{q})\mathbf{t}, \mathbf{t} \in [\underline{\mathbf{t}}, \bar{\mathbf{t}}] \} \quad (3)$$

100 Furthermore, the dual relationship of the m -dimensional Cartesian wrenches \mathbf{F} and the generalised
 101 joint torques $\boldsymbol{\tau}$ is given through the Jacobian transpose matrix $\mathbf{J}^T(\mathbf{q})\mathbf{F} = \boldsymbol{\tau}$ and defines the achievable
 102 Cartesian feasible wrench:

$$\mathcal{P}_F = \{ \mathbf{F} \in \mathbb{R}^m \mid \mathbf{J}^T(\mathbf{q})\mathbf{F} = \boldsymbol{\tau}, \boldsymbol{\tau} \in \mathcal{P}_\tau \} \quad (4)$$

103 Combining (3) and (4) the implicit definition of \mathcal{P}_F is

$$\mathcal{P}_F = \{ \mathbf{F} \in \mathbb{R}^m \mid \mathbf{J}^T(\mathbf{q})\mathbf{F} = -L^T(\mathbf{q})\mathbf{t}, \mathbf{t} \in [\underline{\mathbf{t}}, \bar{\mathbf{t}}] \} \quad (5)$$

104 2.2. Outline of the ICHM algorithm

105 The ICHM is a recent algorithm for the feasibility set analysis of a generic class of linear algebra
 106 problems. It is suited for the determination of the feasible Cartesian WFS \mathcal{P}_F associated to a muscu-
 107 loskeletal model of the human upper limb (5) (Skuric et al., 2022). It is based on two processes. The
 108 first one consists in finding the vertices of \mathcal{P}_F by solving a linear programming (LP) problem for a
 109 chosen set of directions $\mathbf{c} \in \mathbb{R}^m$ in the Cartesian task space. The second one consists in computing the
 110 convex hull of the current vertices in order to define a new directions set \mathbf{c} orthogonal to the current
 111 polytope faces. This process is iterated until the distance between the new vertices and the current
 112 polytope faces are below a predefined threshold. In the case of the WFS \mathcal{P}_F determination, the LP
 113 problem solved during the vertex search for appropriately chosen \mathbf{c} directions is the following:

$$\begin{aligned}
& \max_{\mathbf{t}} \quad -\mathbf{c}^T \mathbf{J}^{T+}(\mathbf{q}) \mathbf{L}^T(\mathbf{q}) \mathbf{t} \\
& \text{s.t.} \quad \mathbf{V}_2^T \mathbf{L}^T(\mathbf{q}) \mathbf{t} = \mathbf{0} \\
& \quad \underline{\mathbf{t}} \leq \mathbf{t} \leq \bar{\mathbf{t}}
\end{aligned} \tag{6}$$

114 $\mathbf{V}_2 \in \mathbb{R}^{n \times (n-r)}$ forms an orthonormal basis of $\mathcal{Ker}(\mathbf{J}(\mathbf{q})) = \mathcal{Im}(\mathbf{J}^T(\mathbf{q}))^\perp$. It is obtained from a
115 singular value decomposition of $\mathbf{J}(\mathbf{q}) = \mathbf{U}\mathbf{\Sigma}\mathbf{V}^T$ where $\mathbf{V} = [\mathbf{V}_1, \mathbf{V}_2]^T$. The null space basis of $\mathbf{J}(\mathbf{q})$ is
116 spanned by the columns of \mathbf{V} corresponding to singular values equal to zero and stored in \mathbf{V}_2 . r is the
117 rank of $\mathbf{J}(\mathbf{q})$ and $\mathbf{J}^{T+}(\mathbf{q})$ is the Moore-Penrose pseudo-inverse of the $\mathbf{J}(\mathbf{q})^T$.

118 The LP problem (6) finds a vertex or face of \mathcal{P}_F furthest to a face of the current polytope which
119 normal is \mathbf{c} by finding the maximum of the projection of a wrench $\mathbf{F} = -\mathbf{J}^{T+}(\mathbf{q}) \mathbf{L}^T(\mathbf{q}) \mathbf{t}$ on the \mathbf{c}
120 direction. The equality constraints $\mathbf{V}_2^T \mathbf{L}^T(\mathbf{q}) \mathbf{t} = \mathbf{0}$ ensure that $\mathbf{L}^T(\mathbf{q}) \mathbf{t} \in \mathcal{Im}(\mathbf{J}^T)$ and therefore that
121 $\mathbf{F} = -\mathbf{J}^{T+}(\mathbf{q}) \mathbf{L}^T(\mathbf{q}) \mathbf{t}$ is an exact solution for the wrench \mathbf{F} in the equation $\mathbf{J}^T(\mathbf{q}) \mathbf{F} = -\mathbf{L}^T(\mathbf{q}) \mathbf{t}$. In
122 other words, the equality constraints guarantee that the wrench \mathbf{F} can be generated by the joint torque
123 $\boldsymbol{\tau} = -\mathbf{L}^T(\mathbf{q}) \mathbf{t}$ such that $\mathbf{F} = \mathbf{J}^{T+}(\mathbf{q}) \boldsymbol{\tau}$. The LP formulation is very flexible and allows to add new
124 constraints relative to the GH non dislocation involving the JRF.

125 2.3. Adding GH joint non dislocation constraints to the vertex search algorithm of the ICHM

126 2.3.1. Formulation in terms of GH Joint Reaction Force

127 Due to the particular conformation of the humerus and the glenoid fossa of the scapula, GH joint
128 dislocation can occur if the JRF exerted by the humerus head on the the glenoid fossa is outside a
129 particular irregular conic region (Figure 1). Its boundaries can be defined by considering the admissible
130 ratio μ_j between the shear and compression components of the JRF which are parallel and orthogonal
131 to the plane of the glenoid fossa (Dickerson et al., 2008; Lippitt et al., 1993), respectively. The interior
132 of the polyhedral conic region is defined by a serie of affine constraints represented by half planes
133 (Figure 2). For a direction j defined by an angle θ_j within the glenoid fossa plane $(\mathbf{y}_{GH}, \mathbf{z}_{GH})$, the
134 constraint is expressed as following:

$$\begin{bmatrix} \mu_j & \cos\theta_j & \sin\theta_j \end{bmatrix}^{GF} \mathbf{F}_{H/S} \leq 0 \tag{7}$$

135 where $^{GF} \mathbf{F}_{H/S}$ is the Joint Reaction Force exerted by the humerus head (H) on the scapula glenoid fossa
136 (S) expressed in the frame of the glenoid fossa (superscript GF). The first component of $^{GF} \mathbf{F}_{H/S} =$
137 $[F_n, F_{t1}, F_{t2}]$ is compression and the other two are shear forces. F_n along \mathbf{x}_{GF} is always negative due
138 to the choice of the glenoid fossa frame (Figure 1).

139 For a set of directions, a linearized version of the cone boundaries is obtained by stacking the
140 constraints (7) in the matrix \mathbf{C}_{DIS} :

$$\mathbf{C}_{DIS} {}^G \mathbf{F}_{H/S} \leq \mathbf{0} \quad (8)$$

141 — please insert Figure 1 around here —

142 — please insert Figure 2 around here —

143 2.3.2. Incorporating muscular and external forces

144 Let consider the static equilibrium of the humerus expressed in the global frame (denoted by the
145 superscript 0). The weight of the segments is neglected.

$${}^0 \mathbf{F}_{S/H} + {}^0 \mathbf{F}_{F/H} + \Sigma {}^0 \mathbf{F}_{M/H} = \mathbf{0} \quad (9)$$

146 ${}^0 \mathbf{F}_{S/H}$ and ${}^0 \mathbf{F}_{F/H}$ represents the forces exerted on the humerus by the scapula and forearm, respec-
147 tively, $\Sigma {}^0 \mathbf{F}_{M/H}$ represents the action of forces (expressed in the global frame) of muscles acting on the
148 humerus and crossing the GH joint. An external force ${}^0 \mathbf{F}_{EXT}$ exerted at the hand is transmitted to
149 the humerus according to the third Newton's law. Then, ${}^0 \mathbf{F}_{F/H} = {}^0 \mathbf{F}_{EXT}$. ${}^0 \mathbf{F}_{H/S}$ the Joint Reaction
150 Force exerted by the humerus on the scapula in the global frame can be expressed as following:

$${}^0 \mathbf{F}_{H/S} = \Sigma {}^0 \mathbf{F}_{M/H} + {}^0 \mathbf{F}_{EXT} \quad (10)$$

151 The contribution of muscular forces to the GH JRF, $\Sigma {}^0 \mathbf{F}_{M/H}$, can be replaced by ${}^0 \mathbf{C}_{JRF}(\mathbf{q})\mathbf{t}$ with
152 ${}^0 \mathbf{C}_{JRF} \in \mathbb{R}^{m \times d}$. Each column of ${}^0 \mathbf{C}_{JRF}(\mathbf{q})$, called the force direction matrix (Ingram et al., 2016),
153 stores the contribution \mathbf{n}_i of a 1N force of muscle i to the GH JRF:

$${}^0 \mathbf{C}_{JRF}(\mathbf{q}) = \begin{bmatrix} \mathbf{n}_1 & \dots & \mathbf{n}_i & \dots & \mathbf{n}_d \end{bmatrix} \quad i = 1..d \quad (11)$$

154 Combining the action of muscles and that of ${}^0 \mathbf{F}_{EXT}$, the GH JRF expression in the global frame
155 is :

$${}^0 \mathbf{F}_{H/S} = {}^0 \mathbf{C}_{JRF}(\mathbf{q})\mathbf{t} + {}^0 \mathbf{F}_{EXT} \quad (12)$$

156 It is considered that ${}^0 \mathbf{F}_{EXT}$ acting at the hand is counterbalanced by one element $\mathbf{F} \in \mathcal{P}_F$. Since
157 the equality constraints in the LP (6) ensure that $\mathbf{L}^T(\mathbf{q})\mathbf{t} \in \mathcal{I}m(\mathbf{J}^T)$; for a certain \mathbf{t} , ${}^0 \mathbf{F}_{EXT}$ can be
158 expressed as:

$${}^0 \mathbf{F}_{EXT} = \mathbf{J}^{T+}(\mathbf{q})\mathbf{L}^T(\mathbf{q})\mathbf{t} \quad (13)$$

159 Then (12) becomes:

$${}^0\mathbf{F}_{H/S} = ({}^0\mathbf{C}_{JRF}(\mathbf{q}) + \mathbf{J}^{T+}(\mathbf{q})\mathbf{L}^T(\mathbf{q}))\mathbf{t} \quad (14)$$

160 Expressed in the frame of the glenoid fossa (14) becomes:

$$\begin{aligned} {}^{GF}\mathbf{F}_{H/S} &= {}^{GF}\mathbf{R}_0 {}^0\mathbf{F}_{H/S} \\ {}^{GF}\mathbf{F}_{H/S} &= {}^{GF}\mathbf{R}_0 ({}^0\mathbf{C}_{JRF}(\mathbf{q}) + \mathbf{J}^{T+}(\mathbf{q})\mathbf{L}^T(\mathbf{q}))\mathbf{t} \end{aligned} \quad (15)$$

161 where ${}^{GF}\mathbf{R}_0$ is the rotation matrix from the glenoid fossa frame to the global frame.

162 2.3.3. Constraints and LP formulation

163 The GH non dislocation constraints are obtained by substituting ${}^{GF}\mathbf{F}_{H/S}$ in (8) by its expression
164 in (15):

$$\begin{aligned} \mathbf{C}_{DIS} {}^{GF}\mathbf{R}_0 ({}^0\mathbf{C}_{JRF}(\mathbf{q}) + \mathbf{J}^{T+}(\mathbf{q})\mathbf{L}^T(\mathbf{q}))\mathbf{t} &\leq \mathbf{0} \\ \mathbf{C}\mathbf{t} &\leq \mathbf{0} \end{aligned} \quad (16)$$

165 In addition, the amplitude of the first component of ${}^{GF}\mathbf{F}_{H/S}$ corresponding to compression is kept
166 under a maximum value by considering the following constraint:

$$\mathbf{D}\mathbf{t} - f_{max} \leq 0 \quad (17)$$

167 where \mathbf{D} is the first row of ${}^{GF}\mathbf{R}_0 ({}^0\mathbf{C}_{JRF}(\mathbf{q}) + \mathbf{J}^{T+}(\mathbf{q})\mathbf{L}^T(\mathbf{q}))$ and f_{max} the maximum allowed
168 compressive force.

169 Finally, the formulation of the LP problem incorporating GH non dislocation constraints and
170 limitation of GH JRF compression is:

$$\begin{aligned} \max_{\mathbf{t}} \quad & -\mathbf{c}^T \mathbf{J}^{T+}(\mathbf{q})\mathbf{L}^T(\mathbf{q})\mathbf{t} \\ \text{s.t.} \quad & \mathbf{V}_2^T \mathbf{L}^T(\mathbf{q})\mathbf{t} = \mathbf{0} \\ & \mathbf{C}\mathbf{t} \leq \mathbf{0} \\ & \mathbf{D}\mathbf{t} - f_{max} \leq 0 \\ & \underline{\mathbf{t}} \leq \mathbf{t} \leq \bar{\mathbf{t}} \end{aligned} \quad (18)$$

171 2.4. Implementation details

172 The seven degrees of freedom and 50 muscles Opensim upper-limb model proposed in (Saul et al.,
173 2015) was used. The Jacobian matrix, muscles moment arm matrix, maximal and minimal muscle

174 forces were obtained with the Matlab Opensim API.

175 Using the `calcReactionOnParentExpressedInGround` method of the Opensim joint object, each
 176 column \mathbf{n}_i of $\mathbf{C}_{JRF}(\mathbf{q})$ was obtained by dividing ${}^0\mathbf{F}_{H/S_i} = t_i\mathbf{n}_i$, the individual contribution of muscle
 177 $i = 1..d$ to the GH JRF, by the value of the muscle tension t_i :

$$\mathbf{n}_i = \frac{{}^0\mathbf{F}_{H/S_i}}{t_i} \quad (19)$$

178 The contribution \mathbf{n}_i to the GH JRF was computed for each muscle by setting its activation a to a
 179 random value in the interval $]0, 1]$, to ensure that $t_i > 0$, and by setting the force of the other muscles
 180 to 0 (both passive and active components). In order to quantify the static GH JRF, the rotational
 181 inertia was set to huge values to prevent joint rotational acceleration and acceleration of the humerus
 182 center of gravity allowing to obtain individual contribution of a single muscle to the GH JRF in a
 183 static condition.

184 Since (8) was expressed in the frame of the glenoid fossa, the rotation matrix from this frame to the
 185 global frame was needed. Three markers were attached to the scapula of the chosen Opensim model
 186 (Figure 3) and the glenoid fossa frame was defined according to the method proposed in (Blache et al.,
 187 2017b):

188 — please insert Figure 3 around here —

$$\begin{aligned} \mathbf{x}_{GF} &= \frac{(\mathbf{gf}_2 - \mathbf{gf}_3) \times (\mathbf{gf}_1 - \mathbf{gf}_3)}{\|(\mathbf{gf}_2 - \mathbf{gf}_3) \times (\mathbf{gf}_1 - \mathbf{gf}_3)\|} \\ \mathbf{y}_{GF} &= \frac{\frac{\mathbf{gf}_1 + \mathbf{gf}_2}{2} - \mathbf{gf}_3}{\|\frac{\mathbf{gf}_1 + \mathbf{gf}_2}{2} - \mathbf{gf}_3\|} \\ \mathbf{z}_{GF} &= \mathbf{x}_{GF} \times \mathbf{y}_{GF} \\ {}^0\mathbf{R}_{GF} &= \begin{bmatrix} \mathbf{x}_{GF} & \mathbf{y}_{GF} & \mathbf{z}_{GF} \end{bmatrix} \\ {}^{GF}\mathbf{R}_0 &= {}^0\mathbf{R}_{GF}^T \end{aligned} \quad (20)$$

189 The \mathbf{x}_{GF} axis corresponded to the direction of the compressive component of the GH JRF which
 190 was always negative because the humeral head was pressing against the glenoid fossa. The \mathbf{y}_{GF} and
 191 \mathbf{z}_{GF} axes corresponded to shear forces because it was assumed that the glenoid fossa was almost flat.

192 The μ_i ratios were defined such that the constraint boundary was an ellipse with a ratio of 0.5 in
 193 the cranial-caudal directions and 0.3 in the anterior-posterior directions (Dickerson et al., 2008; Lippitt
 194 et al., 1993). f_{max} was set to 1500N according to (Assila et al., 2020; Blache et al., 2017a).

195 **3. Results**

196 The WFS was computed using the ICHM algorithm with and without the GH constraints. Three
197 postures with different levels of arm abduction and elbow flexion were considered (Table 1 and Figure
198 4). They were chosen such that a range of GH abduction was covered and also because the third
199 posture corresponded to the so-called "apprehension test" for shoulder luxation testing (McMahon
200 and Lee, 2002; McMahon et al., 2003). The forearm pronation-supination, wrist flexion-extension and
201 radial-ulnar deviation were set to 0°.

202

203 — please insert Table 1 around here —

204

205 — please insert Figure 4 around here —

206

207 — please insert Figure 5 around here —

208

209 — please insert Figure 6 around here —

210

211 The results were divided in three parts. Firstly, the WFS with and without GH non dislocation
212 constraints were compared to verify P_1 . In order to assess the global difference between WFS with
213 and without GH constraints, the following procedure was used. The two WFS were superimposed. A
214 set of rays originating from the center of the WFS with GH constraints was constructed. They were
215 defined by a set of direction $\mathbf{v}(r, \theta, \varphi)$, with $r = 1$, $\theta \in [0, 360^\circ]$ and $\varphi \in [0, 180^\circ]$, which spherical
216 coordinates vary with an increment of 1°. Each ray intersects (Tuszynski, 2018) with both WFS and
217 the "length" (in N) of the segment between the two points of intersection was computed for each
218 ray. The graphical representation consisted of a sphere projected in 2D whose surface was colored
219 according to the "length" of the segments corresponding to the \mathbf{v} direction (Figure 6). In addition,
220 the difference between the minimal and maximal forces for each polytope and the segments "length"
221 for some particular directions in the global reference frame (front, back, up, down, right and left) was
222 also assessed (Table 2).

223 In the second part, the GH JRF corresponding to each vertex of the WFS preventing GH dislocation
224 was obtained from (14) and the constraints satisfaction was checked by computing the ratio between
225 shear and compressive components (P_2). The limit of compression forces was also checked (P_3).

226 In the third part, the coordination of the shoulder muscles was investigated to verify P_4 . A
227 particular attention was paid to the forces of the deltoid and pectoralis major muscles on one side
228 and rotator cuff and biceps muscles on the other side, which were known to have a destabilizing and

229 stabilizing action on the GH joint, respectively (Labriola et al., 2005; Sinha et al., 1999).

230 3.1. Effect of GH joint constraints on the WFS

231 The GH constraints reduced the WFS amplitude. The maximal forces were reduced by 66, 45 and
232 71 N for Posture 1, 2, and 3 respectively. Also, the maximal reduction were noticed when both non
233 dislocation and compression constraints were ON. For posture 1; the main reductions were for front,
234 up and left (55, 28 and 20 N respectively). For posture 2 it was front, left and down (124, 99 and 45
235 N, respectively) and for posture 3 front and down (66 and 24N). The global difference, of the sphere
236 projected in 2D is given in Figure 5.

237

238 — please insert Table 2 around here —

239

240 3.2. GH Constraints satisfaction

241 The ratio of the GH JRF shear forces divided by the compressive component superimposed with
242 the boundary of the GH non dislocation constraints for the three chosen postures are presented in
243 Figure 7. Without the non dislocation constraints, the developed muscular forces conducted to a dis-
244 location of the GH joint for 61%, 55%, and 76% of the vertices of the corresponding WFS for postures
245 1, 2, and 3, respectively (ratios depicted by red circle lying outside of the GH boundaries). When
246 GH constraints were ON, these percentages dropped to 5%, 2%, and 3%. For posture 1, the GH JRF
247 vectors are directed upward (Figure 7.A), anteriorly for postures 2 and in the anterior-inferior direction
248 for posture 3 (Figures 7.B and 7.C). When the GH constraints are active, the ratios between shear
249 and compressive lye inside the constraints boundaries validating P_2 . The JRF depicted in Figure 8
250 confirms the orientation of the dislocating JRF and show the effect of the constraints limiting the
251 amplitude of compressive forces (blue thick arrows in Figure 8).

252

253 — please insert Figure 7 around here —

254

255 — please insert Figure 8 around here —

256

257 — please insert Figure 9 around here —

258

259 — please insert Figure 10 around here —

260

261 3.3. Muscle force coordination

262 The effect of GH constraints on shoulder muscles force coordination was investigated. The pectoralis
263 major, anterior, middle and posterior parts of deltoid were considered for their destabilizing effect and
264 the rotator cuff muscles (subscapularis, infraspinatus, supraspinatus and teres minor) and biceps (for
265 high GH abduction values) for their stabilizing contribution (Labriola et al., 2005; Sinha et al., 1999).
266 Firstly, the maximum compression constraint was relaxed in order to compare the sole effect of the
267 non dislocation constraint i.e. the direction of the GH JRF within the glenoid fossa. For the WFS
268 without GH constraints, the mean and standard deviation of muscular forces was computed separately
269 for the vertices conducting to GH dislocation (red circles in Figure 7) and those not conducting to
270 GH dislocation (green stars in Figure 7). The mean and standard deviation of muscular forces was
271 assessed for all the vertices of the WFS with GH non dislocation constraints. The results are depicted
272 in Figure 9 for the three postures.

273 4. Discussion

274 4.1. Force amplitudes

275 The consideration of GH constraints for avoiding dislocation and too excessive joint load had an
276 effect on the WFS at the hand. A decrease of the maximal forces was noticed particularly in the
277 anterior and mediolateral left directions and depended on the posture.

278 The non dislocation constraints had a moderate effect on the maximal forces at the hand but re-
279 sulted in a modification of muscle coordination with a modulation of tension that ensured GH non
280 dislocation. This illustrates the muscular redundancy implemented in the musculoskeletal model allow-
281 ing a redistribution of muscular forces conducting stabilize the GH joint without affecting significantly
282 the maximal forces. On the other hand, the maximum compression constraint contributed more sub-
283 stantially to the lowering of forces at the hand by a global decrease of all muscle tensions (Figure
284 10).

285 4.2. Muscle coordination

286 Apart from generating joint movements the muscles action is also directed toward the stabilization
287 of the joints. This is especially true for the GH joint. Our results are coherent with those of the
288 literature with a decrease of the force amplitude of the deltoids and pectoralis major in the three
289 postures (Figure 9) with a particular implication of pectoralis muscle exemplified by the effect of its
290 spasms in GH dislocation (Sinha et al., 1999). In our results, it is particularly noticeable for this muscle
291 with a decrease of the mean tension of 216 N, 575N and 746N corresponding to 27%, 54% and 77% when
292 comparing the WFS with GH non dislocation constraints to the WFS vertices conducting to dislocation

293 for posture 1, 2, and 3 respectively. Moreover, in posture 3, corresponding to the apprehension test,
294 it can be seen that without the proposed constraints, the JRF is directed toward the anterior-inferior
295 direction. This observation is consistent with the literature indicating that GH dislocation occurs in
296 this direction when performing forceful apprehension test on cadaveric upper-limbs (McMahon and
297 Lee, 2002; McMahon et al., 2003).

298 4.3. Limitations

299 The present model has several limitations. Firstly, only muscular contribution to joint non dislo-
300 cation was considered but not the static restraints such as capsulolabrum, articular surface geometry
301 and intracapsular pressure. However, it is hypothesized that the non dislocation ratios consider their
302 contribution in some way (Lippitt et al., 1993; Dickerson et al., 2008). Secondly, the WFS is com-
303 puted in an isometric condition neglecting the segments weight and movement dynamics. To relax
304 these hypotheses the equation relating muscle tension \mathbf{t} and \mathbf{F} should be replaced by the following
305 one:

$$J^T(\mathbf{q})\mathbf{F} = -L(\mathbf{q})\mathbf{t} - \boldsymbol{\tau}_b \quad (21)$$

306 where $\boldsymbol{\tau}_b$ is the bias joint torque produced by the gravity and the model dynamics. Results on muscles
307 tension are global and are averaged for all the WFS vertices and therefore their standard deviation
308 is high. It would be valuable to differentiate the results by considering the Cartesian directions.
309 However, the global presentation was chosen for better synthesizing the results. Another limitation is
310 that the results heavily depend on the quality of the musculoskeletal model in terms of muscle force
311 and moment arm matrix. The tested model was generic without any scaling and was used to provide
312 a proof of concept for the proposed method. Finally, an experimental validation is mandatory and will
313 be conducted on the basis of the experiment carried out in (Rezzoug et al., 2021).

314 5. Conclusion

315 The aim of this work was to propose an extension of the ICHM to assess the upper-limb WFS
316 taking into account the limiting factor of GH joint stability. The adaptations of the ICHM were
317 described and implemented. The results confirmed the lowering of the WFS due to the association
318 of GH constraints on the JRF. The non dislocation constraints had an effect on the coordination of
319 muscular forces while compression constraints limited muscle tensions. The change in muscle tension
320 were investigated and in global agreement with the literature, the activity of some muscular groups
321 was lowered or increased. Taking into account biomechanical constraints such as those implemented
322 on the GH joint allow to improve models of musculoskeletal capacities for better simulating human
323 behavior in various application such as collaborative robotics and ergonomics.

324 6. Conflict of Interest Statement

325 The authors declare that they have no known competing financial interests or personal relationships
326 that could have appeared to influence the work reported in this paper.

327 7. Acknowledgements

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Table 1: Glenohumeral and elbow joint angles in degrees for the selected postures. EL: Elevation angle, SE: shoulder elevation, SR: Shoulder rotation, and EF: Elbow flexion.

Posture	EL (°)	SE (°)	SR (°)	EF (°)
Posture 1	10	20	0	70
Posture 2	0	70	-30	90
Posture 3	0	90	-90	90

Table 2: Force difference (N) between the WFS without and with GH constraints according to posture, constraints and directions. disloc : dislocation constraints, comp : compression constraints, min and max: directions of the minimal and maximal force of the WFS without GH constraints, respectively, front, back, up, down, right and left correspond to directions in the global reference frame.

Posture	disloc	comp	min	max	front	back	up	down	right	left
1	ON	OFF	0	0	0	0	0	0	0	4
1	ON	ON	9	66	55	3	28	0	10	20
2	ON	OFF	1	0	22	2	0	13	1	46
2	ON	ON	2	45	124	8	1	45	2	99
3	ON	OFF	0	7	48	0	-2	0	3	-1
3	ON	ON	1	41	66	2	7	24	7	2

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451 finally the blue crosses correspond to vertices of a WFS with GH constraints on. Panels A, B, and C
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460 dislocation constraints status. The GH maximum compression constraints are off. A, B, and C stand
461 for posture 1, 2, and 3, respectively. PCEM: pectoralis major, DELT: sum of anterior, middle and
462 posterior deltoid, ROTCUFF: sum of rotator cuff muscles: supraspinatus, infraspinatus, teres minor,
463 and subscapularis, TMAJ: teres major, LAT: latissimus dorsi, CORB: coracobrachialis, TRlong : long

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466 **Figure 10:** Muscles tension according to posture and GH compression constraints: blue (dark)
467 constraint is off, orange(light) constraint is on. GH non dislocation constraints status is ON for both
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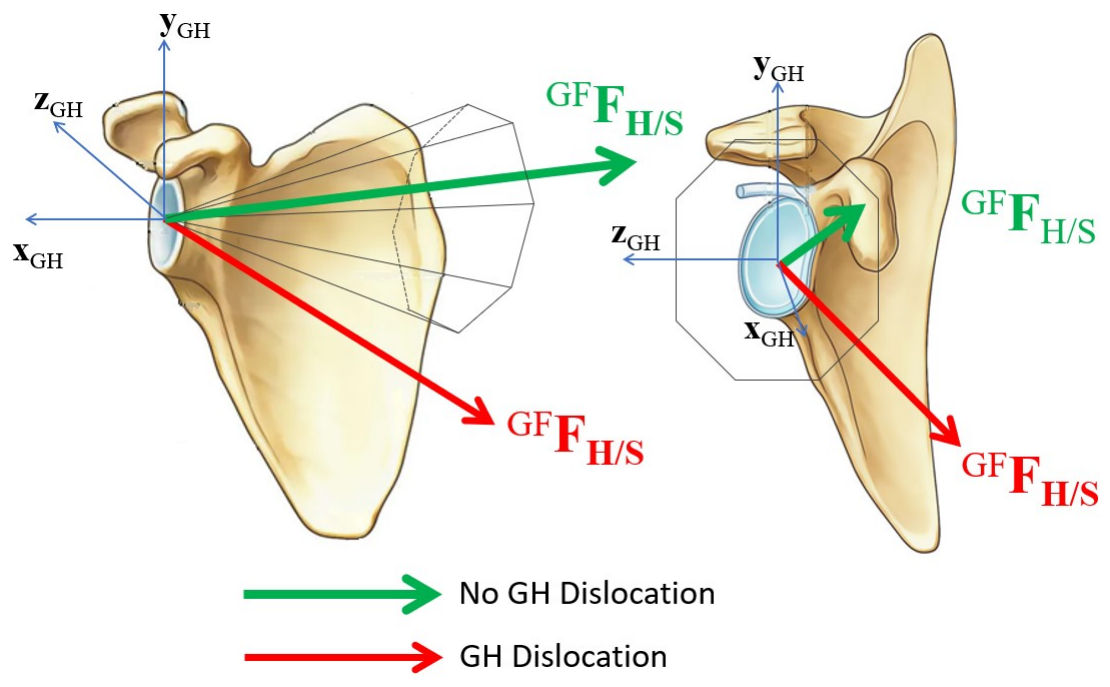


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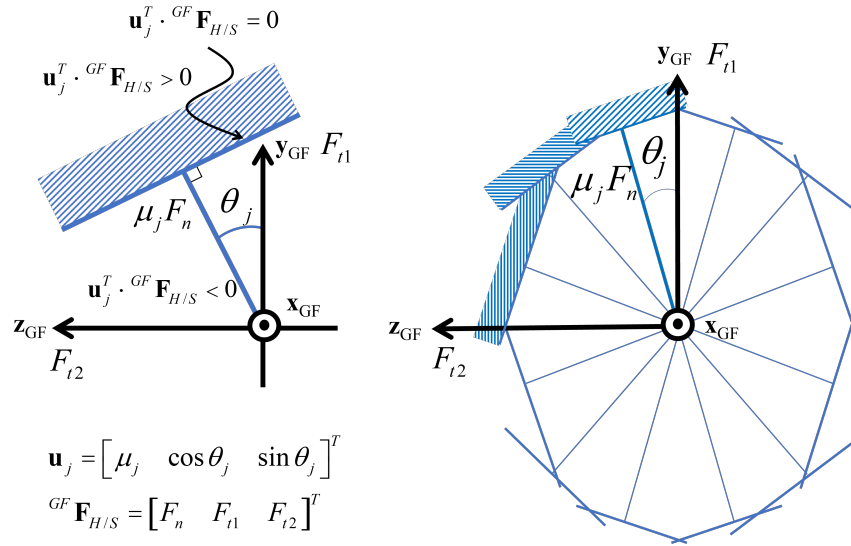


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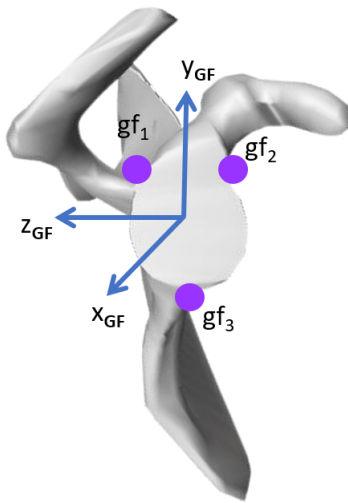


Figure 3: Glenoid fossa reference frame

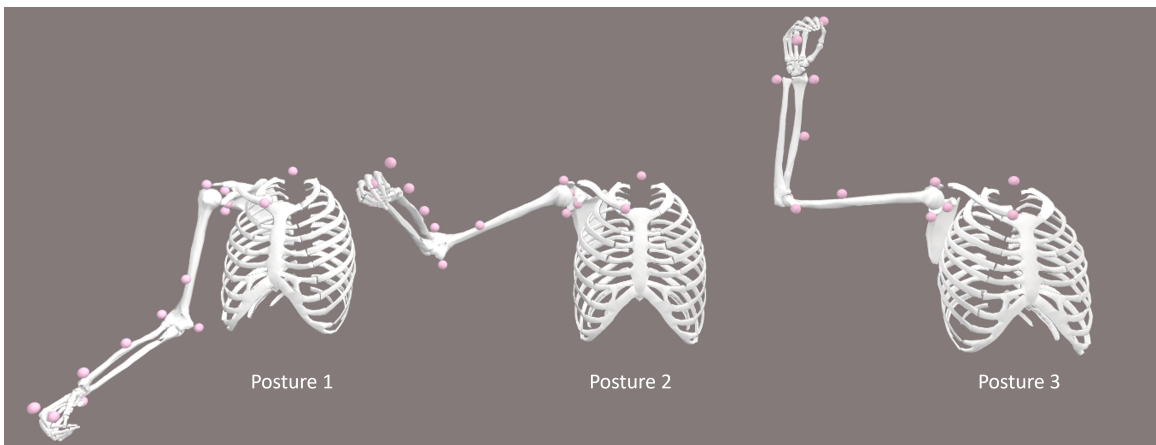


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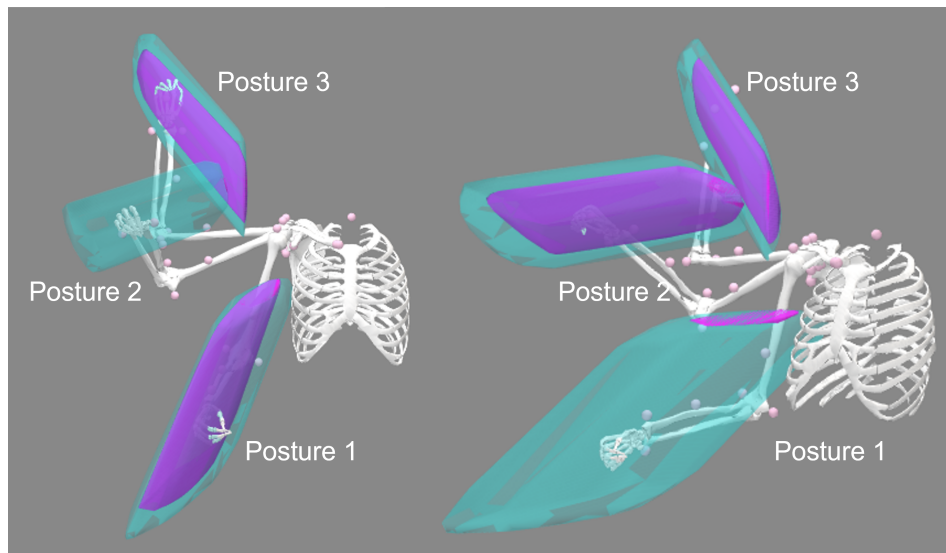


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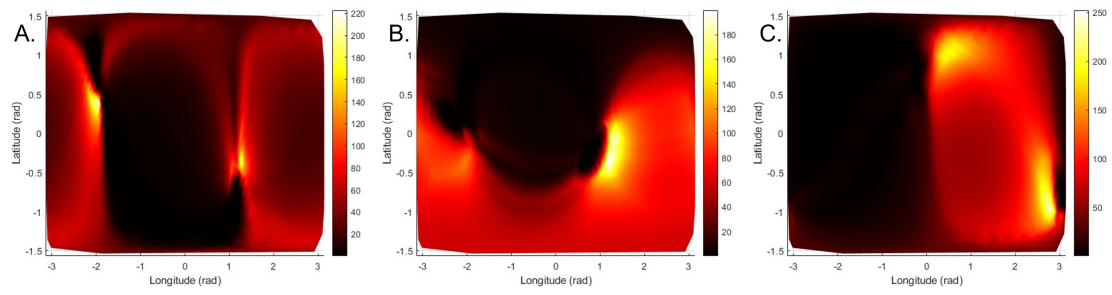


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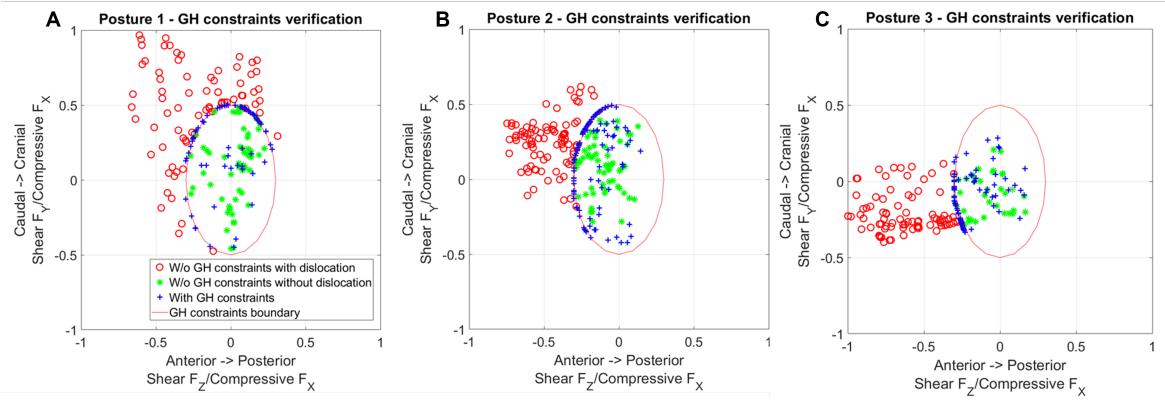


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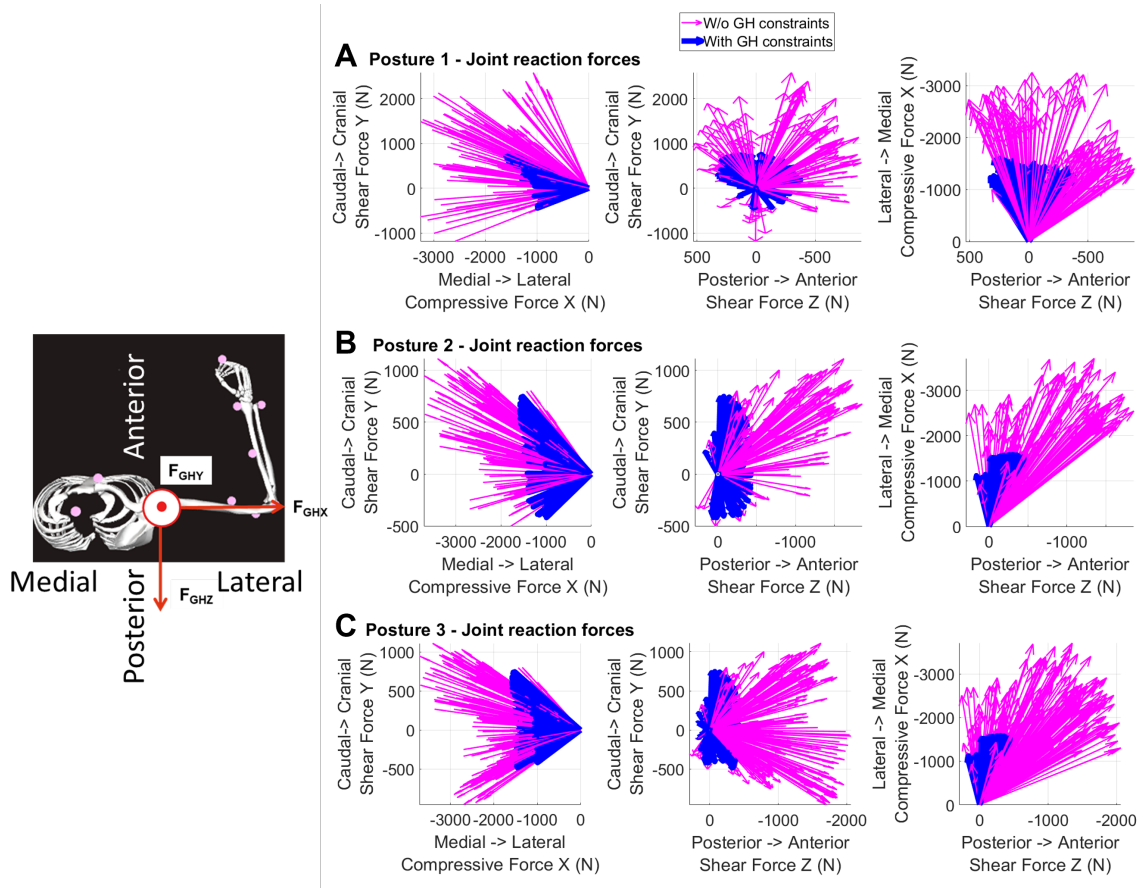


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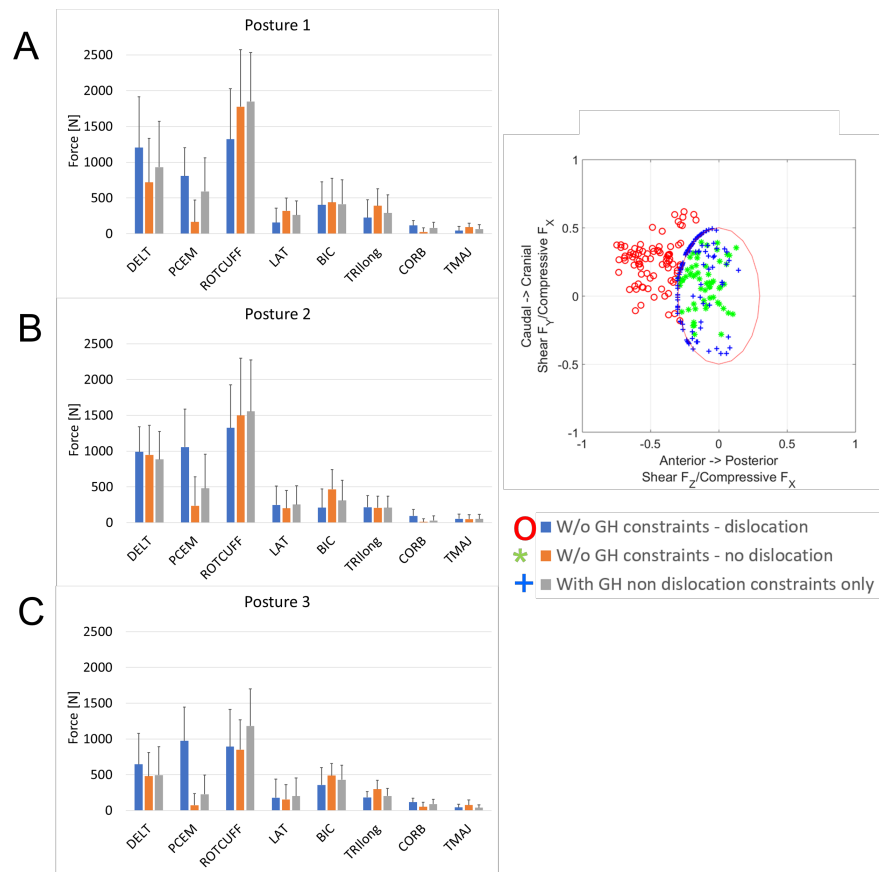


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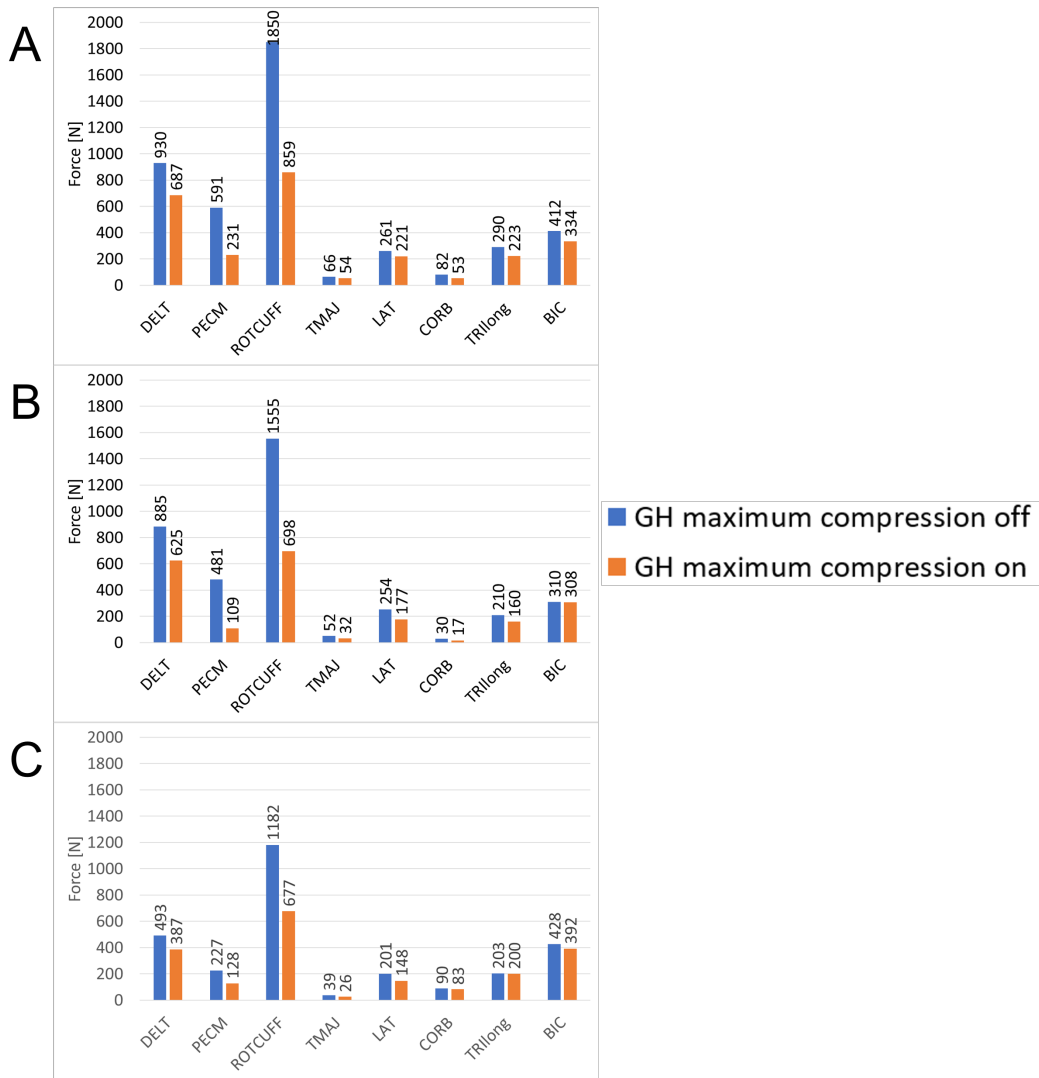


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