

Modelling the dynamics of *Salmonella* infection in the gut at the bacterial and host levels

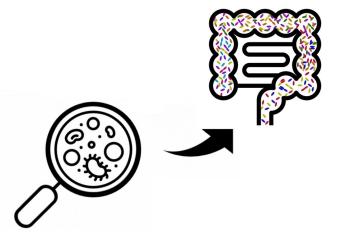
MULLER Coralie UGALDE SALAS Pablo

7th International Symposium on Systems Biology of Microbial Infection

September 21 – 22, 2023

Gut microbiota

- Gut microbiome is a complex community :
 - Thousands of interacting microbial species¹
 - Non-homogeneous spatial distribution²
 - Strong interaction with the host³



• The perturbations that it suffers may alter the stability of the community. e.g. pathogen invasion.

1 Arumugan et al. Nature (2011) 2 Labarthe et al. Journal of theoretical Biology (2019) 3 Levy *et al,* Nature Reviews Immunology (2017)

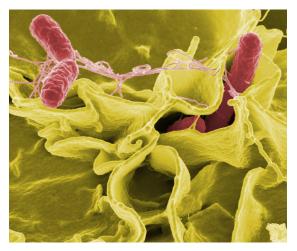
Case Study

- The case of Salmonella enterica Typhimurium infection in a human gut is a medical textbook example of an invader with huge societal costs. (88M € in Australia 2015)¹
- **Case study:** the pathogen turns around the immune system response to its advantage.²
- Experimental studies are costly: **Modelling** to represent mechanistically the situation.



Serve as a proxy for experimental design.³

¹Ford *et al* Journal of Food Protection, 2019. ²Rivera-Chávez and Baumler Annual review of microbiology, 2015 ³Kumar *et al.* Nature Microbiology, 2019



Salmonella Typhimurium (red) invading cultured human cells. Credit: Rocky Mountain Laboratories, NIAID, NIH

Modelling a Salmonella invasion

- The colonization of Salmonella in a healthy gut is a priori not ecologically possible.
- Salmonella thrives in aerobic environments, whereas the human gut is mostly anaerobic.

Rivera-Chávez and Baumler Annual review of microbiology, 2015

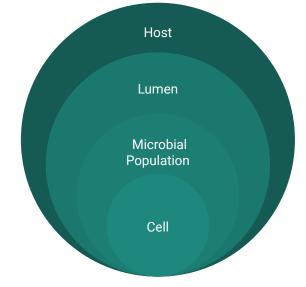
Modelling a Salmonella invasion

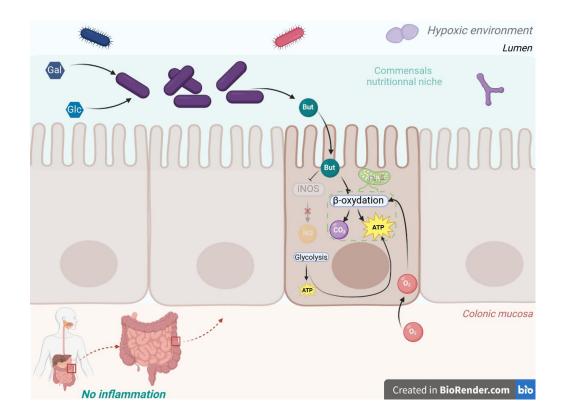
- The colonization of Salmonella in a healthy gut is a priori not ecologically possible.
- Salmonella thrives in aerobic environments, whereas the human gut is mostly anaerobic.
- Modelling:
 - Take into account nutrient variability and metabolic activity of the agents involved.
 - The host immune system response and the passage from an anaerobic to aerobic environment.

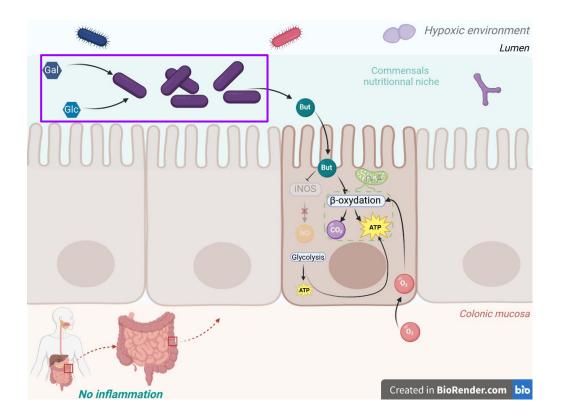
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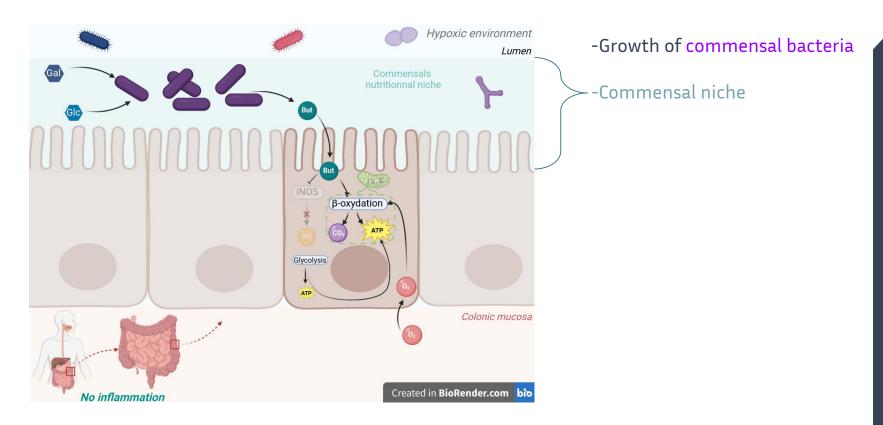
- 1. Model the ecological process taking into account the role of species and host metabolism as well as its immune system response.
- 2. Propose a framework to overcome the difficulty of scale integration.
 - a. Metabolic models
 - b. Dynamic model
 - c. Surrogate model

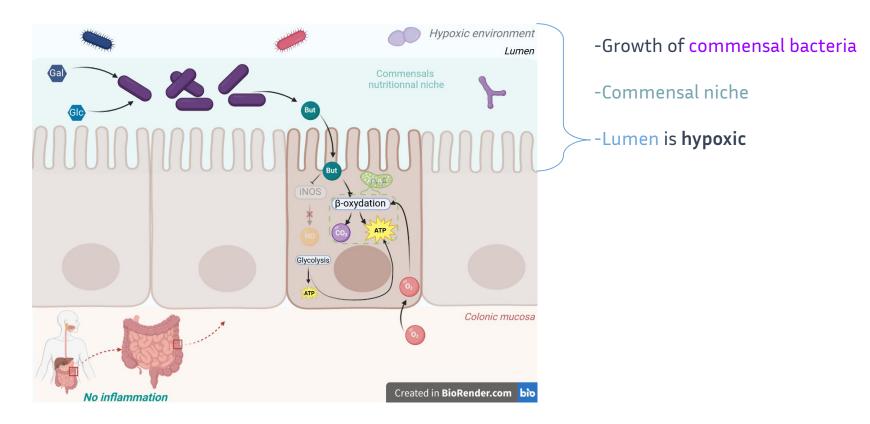


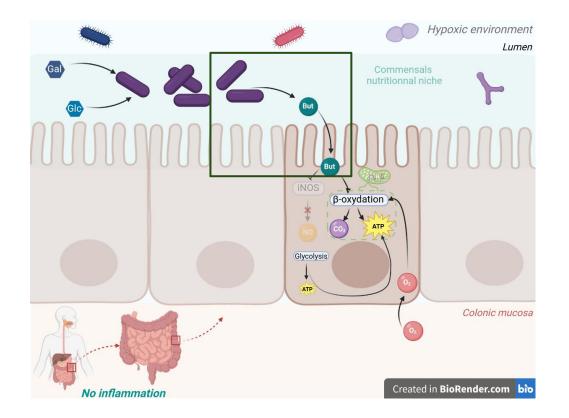




-Growth of commensal bacteria





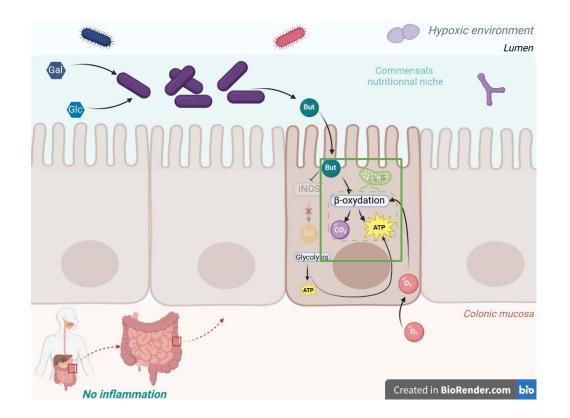


-Growth of commensal bacteria

-Commensal niche

-Lumen is hypoxic

-Butyrate production ensured by commensal bacteria



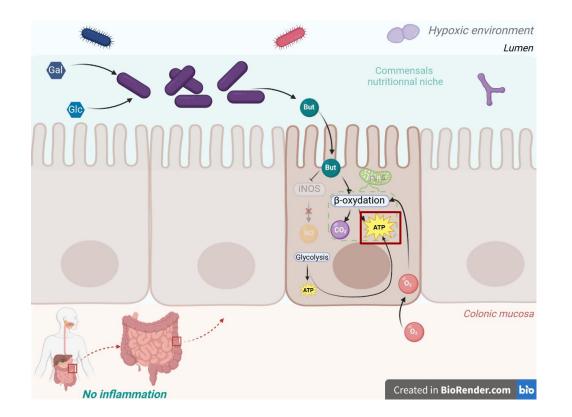
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-Butyrate is **a crucial** precursor for **β**-oxydation, essential for the **Krebs Cycle (TCA)**



-Growth of commensal bacteria

-Commensal niche

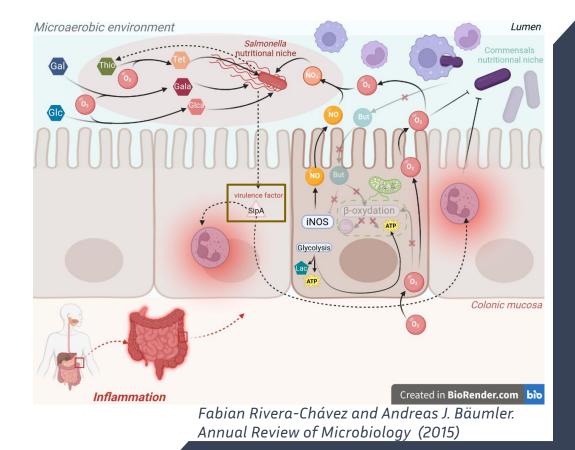
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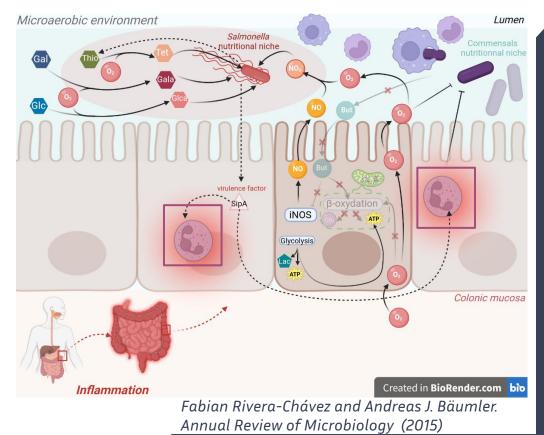
-ATP production via the electron transport chain (ETC)

- Immune system is **triggered** by a **virulence factor** → **Inflammation**



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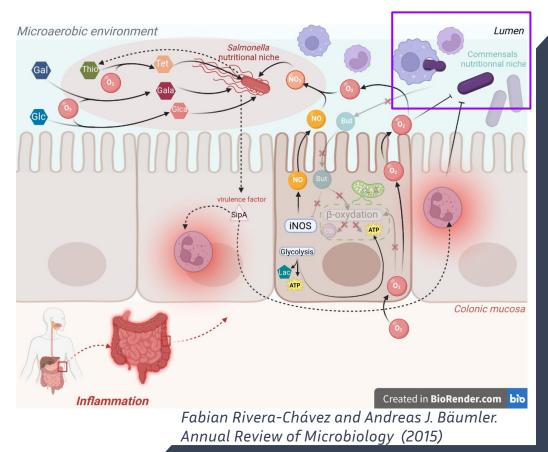
- Infiltration of neutrophils in the lumen



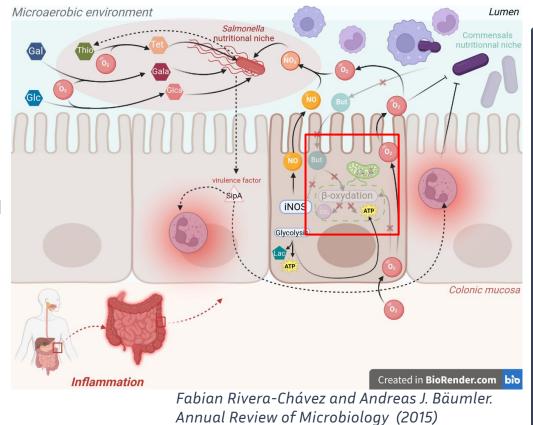
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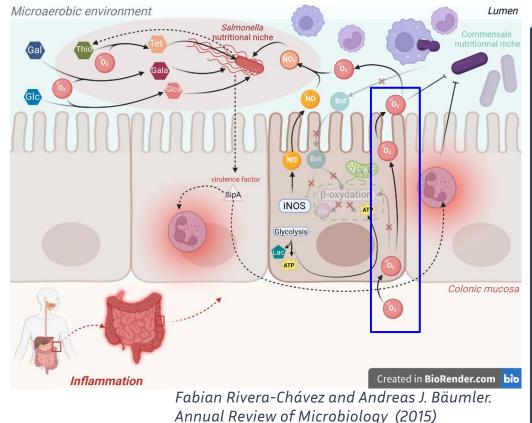
- Decrease of commensal bacteria \implies reduction in butyrate production



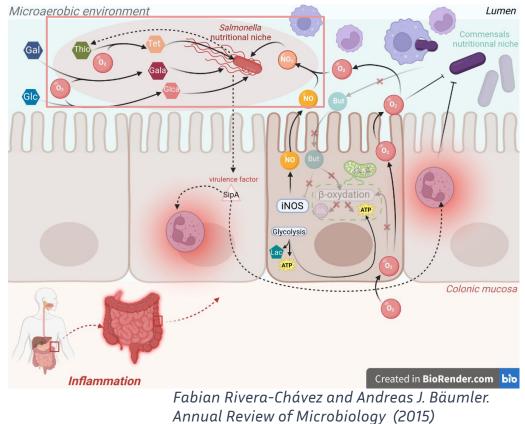
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- TCA cycle and the ETC activity is reduced
 ATP production is reduced



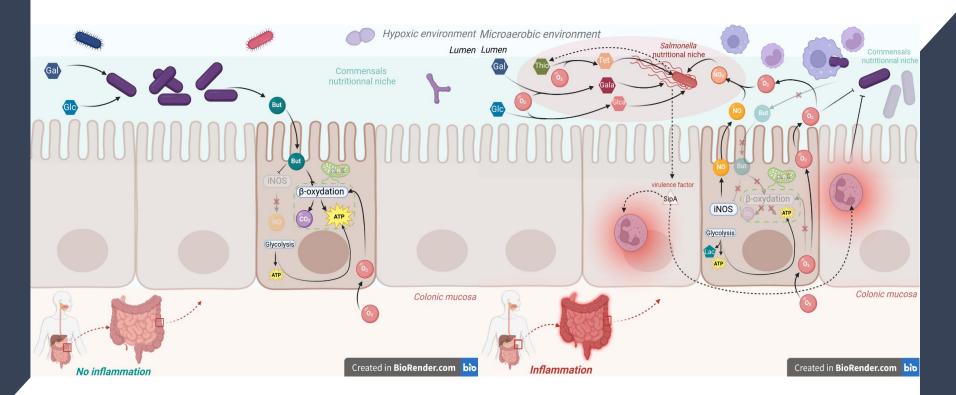
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- Lead to an overflow of O₂ in lumen
 ⇒ Lumen is microaerobic



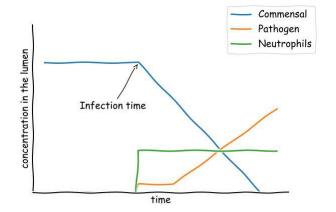
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- Lead to an overflow of O₂ in lumen
 ⇒ Lumen is microaerobic
- **Oxidation** of metabolites **favors** an **oxidative niche** for *Salmonella*



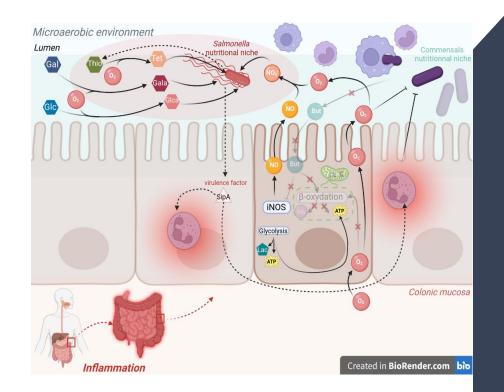
Biological setting: Complete model



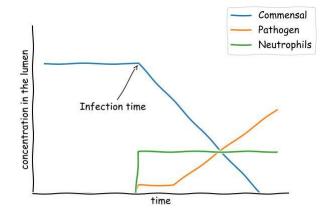
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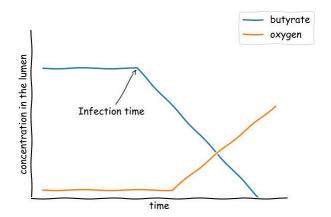
What we expect our model to produce



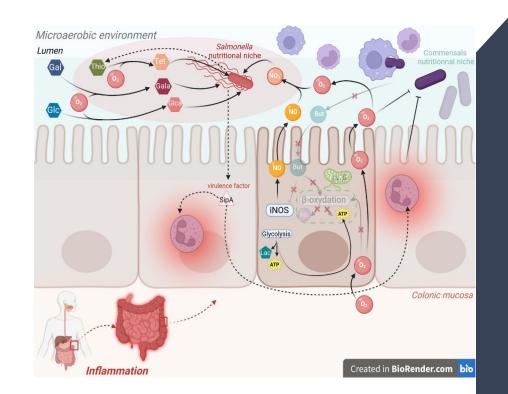
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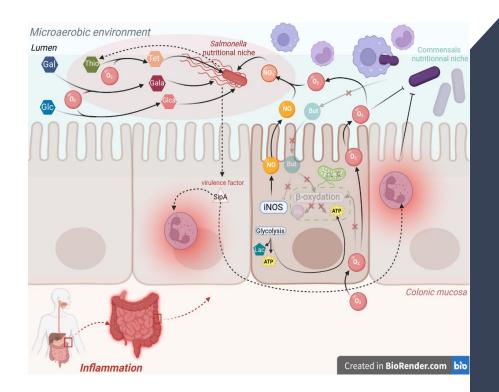
What we expect our model to produce



Modelling choices

• Consider Salmonella **only** in the lumen

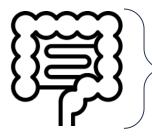
 Use of genome scale metabolic models to represent the metabolism of commensal bacteria, salmonella, and enterocytes







1 Kocabaş K, et al. PLOS ONE. (2022)

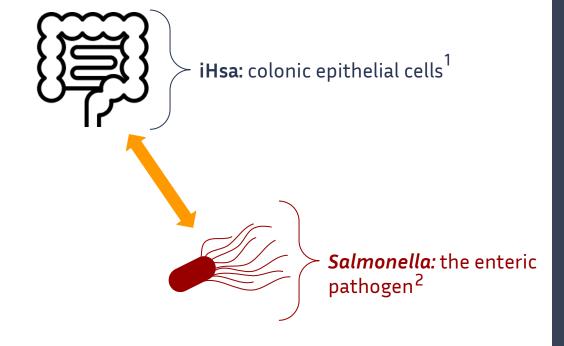


iHsa: colonic epithelial cells¹

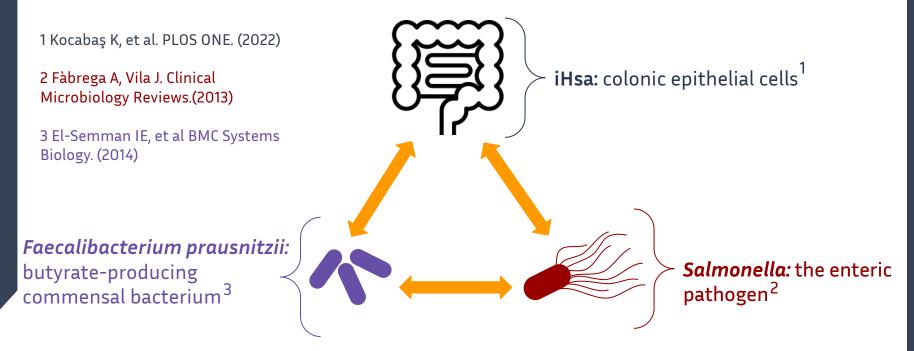


1 Kocabaş K, et al. PLOS ONE. (2022)

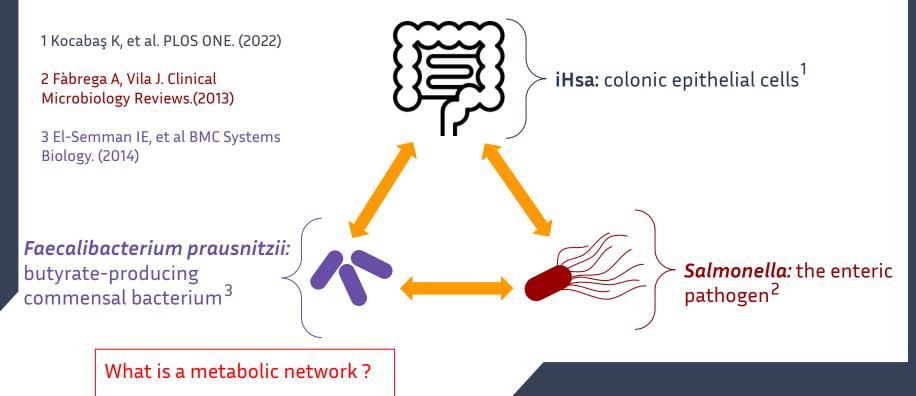
2 Fàbrega A, Vila J. Clinical Microbiology Reviews.(2013)









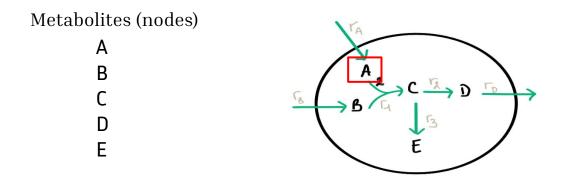




• Set of metabolic and physical processes that determine the physiological and biochemical properties of a cell.

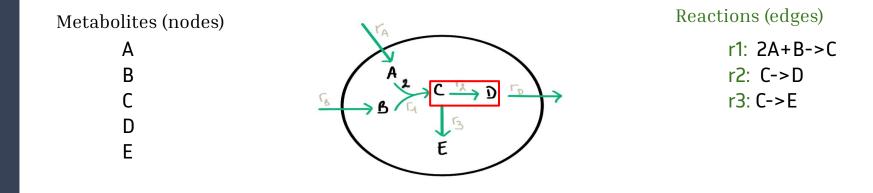


- Set of metabolic and physical processes that determine the physiological and biochemical properties of a cell.
- Can be represent in a graph with **metabolites** as **nodes**



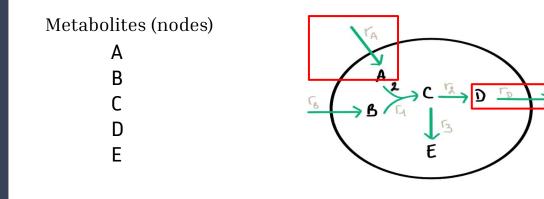
Metabolic networks

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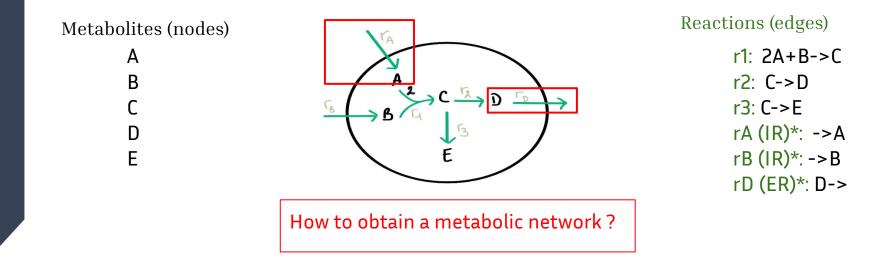
Reactions (edges)

r1: 2A+B->C r2: C->D r3: C->E rA (IR)*: ->A rB (IR)*: ->B rD (ER)*: D->

*IR: Import reaction ER: Export reaction

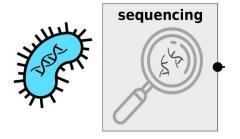
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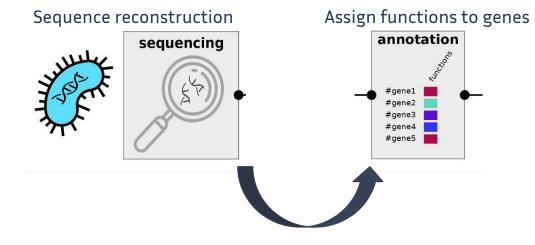


Workflow: metabolic network creation

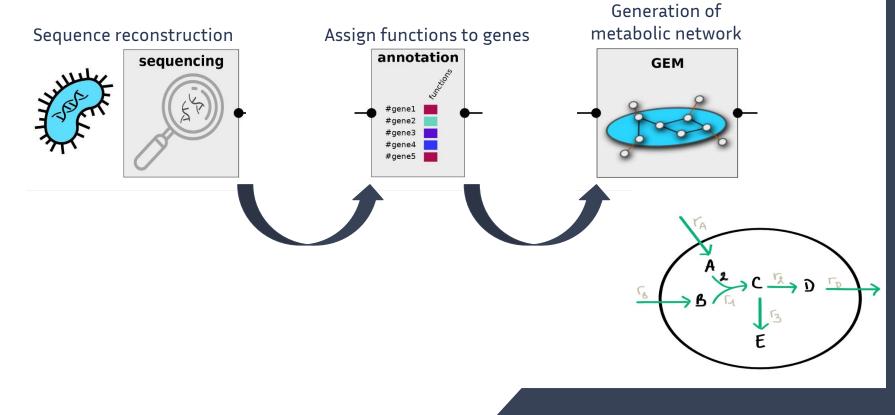
Sequence reconstruction



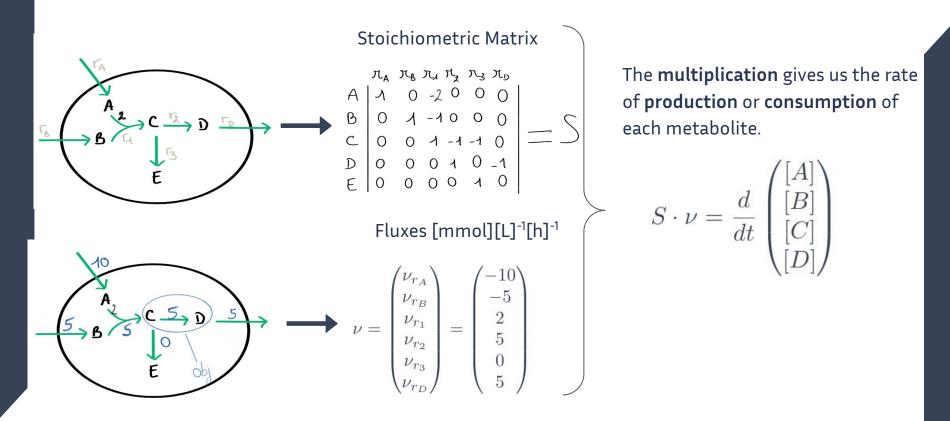
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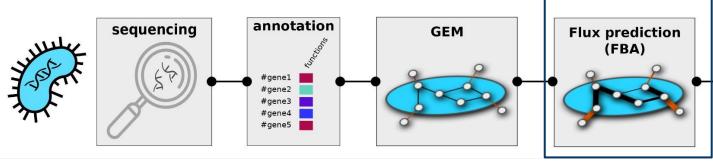
Workflow: metabolic network creation



Metabolic network and fluxes



Workflow: metabolic model and FBA



Predict fluxes (v)

Flux Balance Analysis Hypothesis:

- Quasi-steady state at the interior of cells
- Physical **constraints** of the fluxes.
- -Objective function

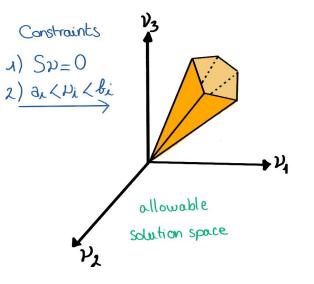
-Exchange reactions constrained by available metabolites

Quasi-steady state : Intracellular metabolites concentration are considered constant

$$S \cdot \nu = \frac{d}{dt} \begin{pmatrix} [A] \\ [B] \\ [C] \\ [D] \end{pmatrix} = 0$$

Constraint: Fluxes are bounded (enzyme capacity)

$$a_i \le \nu_i \le b_i$$

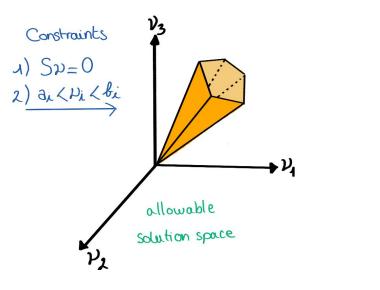


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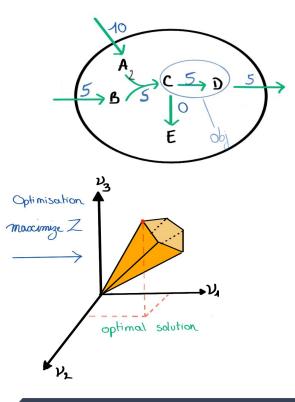
Constraint: Fluxes are bounded (enzyme capacity)

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How to choose one solution among them?

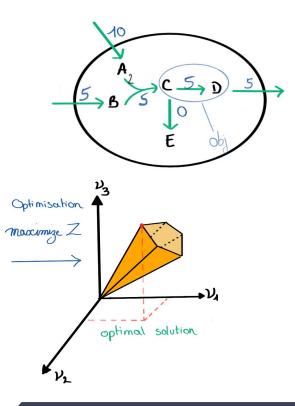
What does the cell search to do?



What does the cell search to do?

Objective function:

-Choose a reaction (or a combination of them) to be maximized.

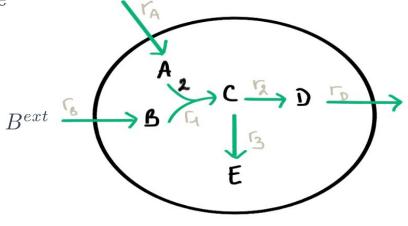


Uptake reactions:

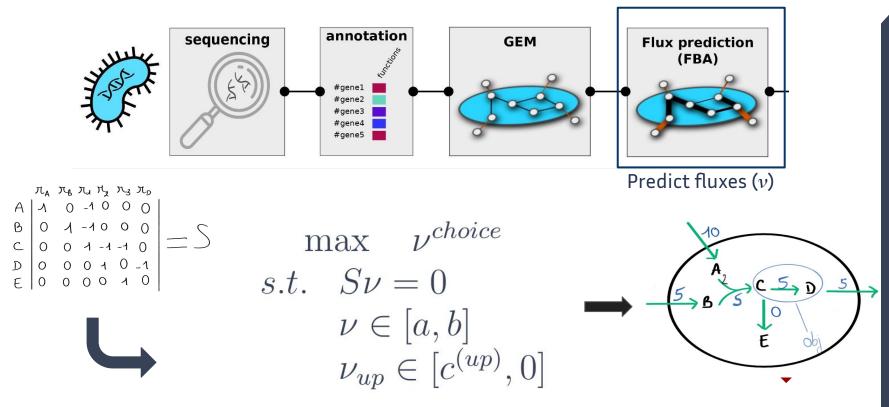
• They bring metabolites into the cell (r_A and r_B)

• Uptake flux is bounded by the metabolite availability

$$c^{up}([B^{ext}]) \le \nu_B^{up} \le 0$$

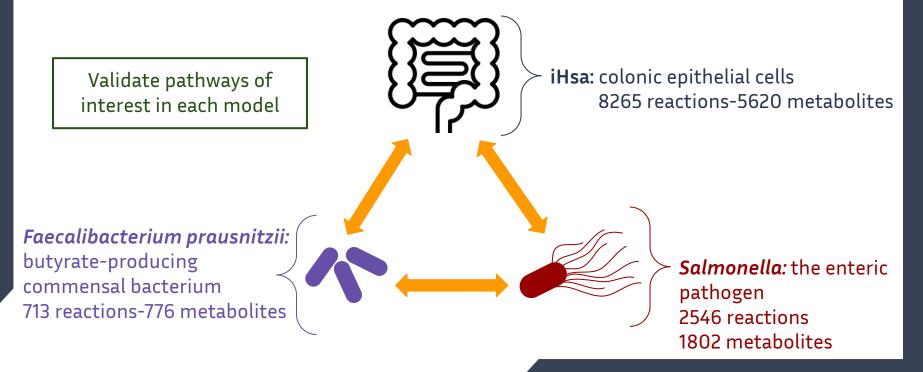


Workflow: metabolic model and FBA



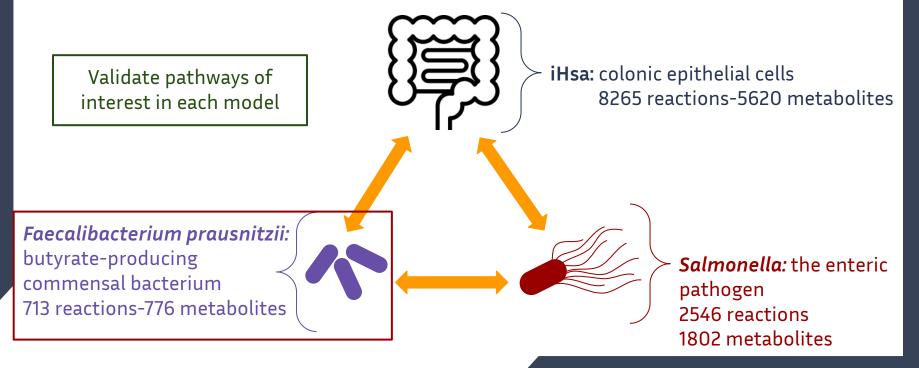
Metabolic model:

• Build a host-microbiota-pathogen system using 3 metabolic networks



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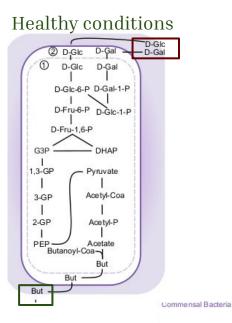


Metabolic model: Fprau



• Objective function: - Biomass

Metabolic model: Fprau



Infection conditions D-GIC Glor D-Gal 02 1 Galt L



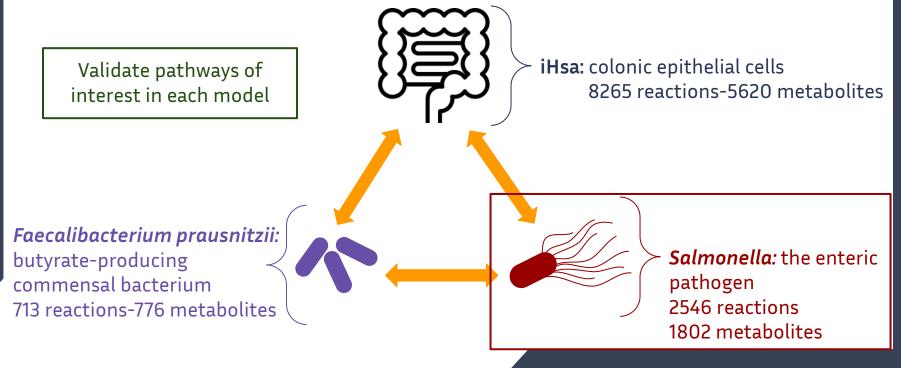
- Objective function: - Biomass
- Uptake metabolites of interest:
 -Glucose/Galactose
- Output metabolites of interest:
 Butyrate

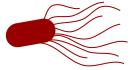
() cytosol
 (2) periplasm
 (3) mitochondria
 (4) intermembrane space
 (5) mitochondrial inner membrane
 (6) matrix

high activity
 medium activity
 low activity

Metabolic model:

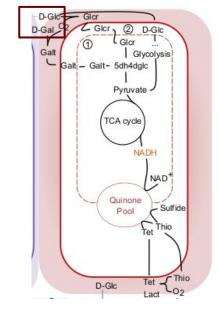
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• Objective function: - Biomass

Infection conditions



Salmonella

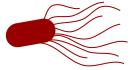
(2)periplasm

③ mitochondria
 ④ intermembrane space
 ⑤ mitochondrial inner membrane

----- medium activity

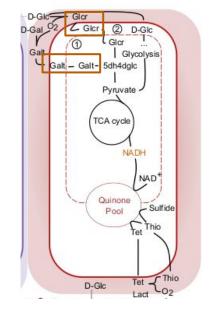
(1) cytosol

6 matrix —— high activity



- Objective function: - Biomass
- Uptake metabolites of interest:
 -Glucose/Galactose

Infection conditions



Salmonella

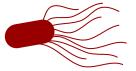
(2)periplasm

3 mitochondria 4 intermembrane space 5 mitochondrial inner membrane

----- medium activity

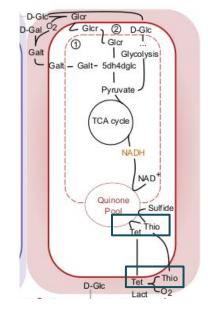
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- Uptake metabolites of interest:
 -Glucose/Galactose
 - -Glucarate/Galactarate

Infection conditions



Salmonella

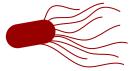
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②periplasm
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(a) intermembrane space
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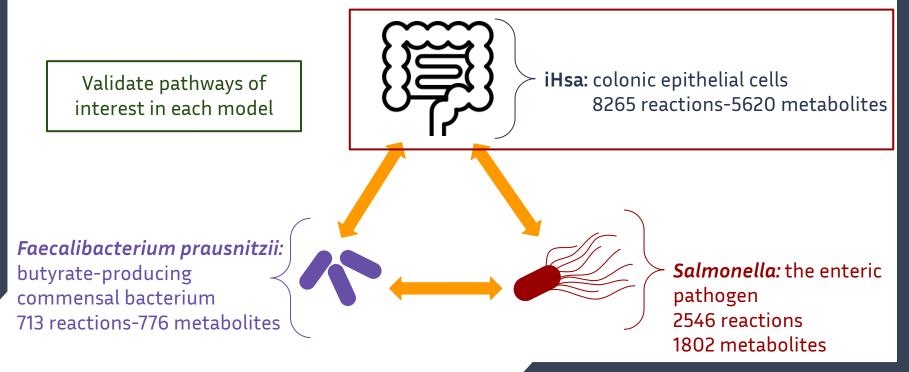
— medium activity



- Objective function: - Biomass
- Uptake metabolites of interest:
 - -Glucose/Galactose
 - -Glucarate/Galactarate
 - -Thiosulfate/Tetrathionate

Metabolic model:

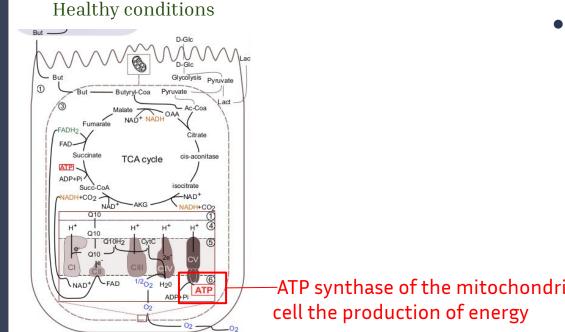
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Objective function:
 Butyrate has no impact on

the biomass production





Objective function: - Butyrate has no impact on the biomass production

- Set up the ATP synthase

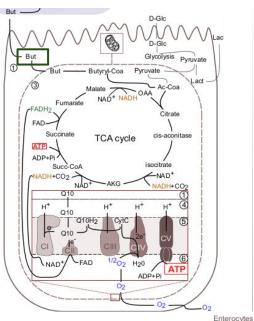
-ATP synthase of the mitochondria,

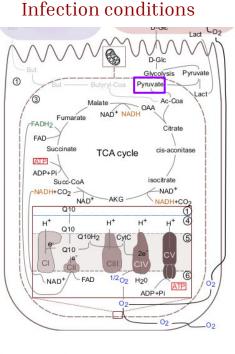
Enterocytes

(1) cytosol Deriplasm ③ mitochondria (a) intermembrane space (5) mitochondrial inner membrane 6 matrix - high activity

— medium activity

Healthy conditions





Cytosol
 Zperiplasm
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 dintermembrane space
 Smitochondrial inner membrane
 6 matrix

high activity medium activity low activity

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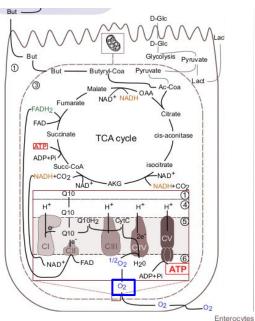
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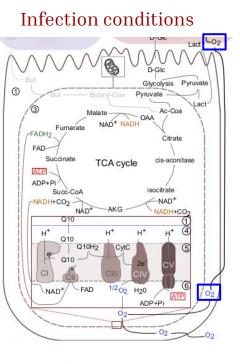
• Uptake/Output metabolites of interest:

-Butyrate (uptake)

-Pyruvate (uptake)

Healthy conditions



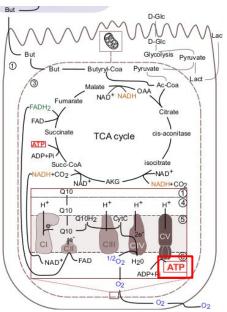


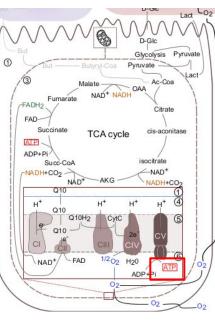
Ocytosol
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medium activity

- I算I
- Objective function: - Butyrate has no impact on the biomass production
 - Set up the ATP synthase
- Uptake/Output metabolites of interest:
 - -Butyrate (uptake)
 - -Pyruvate (uptake)
 - -O2 (uptake in healthy condition and output in infection condition)

Healthy conditions





Enterocytes ① cytosol ② periplasm

- ③mitochondria
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 ⑥ matrix
 - high activity medium activity

Infection conditions

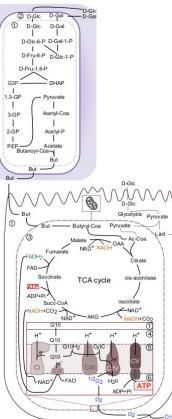
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- Uptake/Output metabolites of interest:
 - -Butyrate (uptake)
 - -Pyruvate (uptake)
 - -O2 (uptake in healthy condition and output in infection condition)
- Production metabolites of interest:

-ATP (stable in healthy conditions and decreased in infection conditions)

Complete model





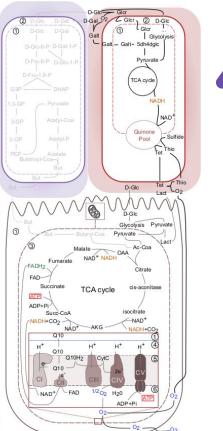




Cytosol
 Operiplasm
 The second s

- high activity

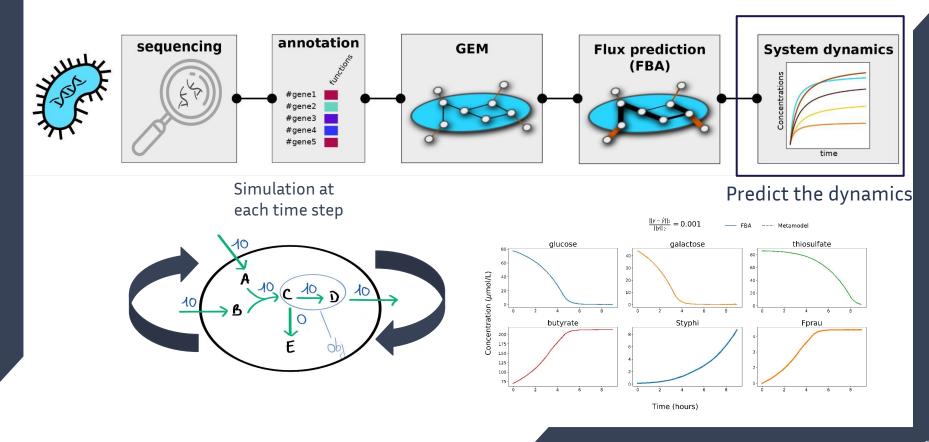
------ medium activity low activity







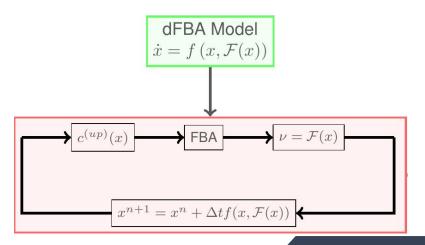
Workflow





Let \mathcal{F} be the function that maps the **constraints** $c^{(up)}$ to the optimal **flux** v^* obtained by **FBA**

$$\mathcal{F}: \quad \mathbb{R}^{N^{up}} \longrightarrow \mathbb{R}^{N_r}$$
$$c^{(up)} \mapsto \nu^*$$

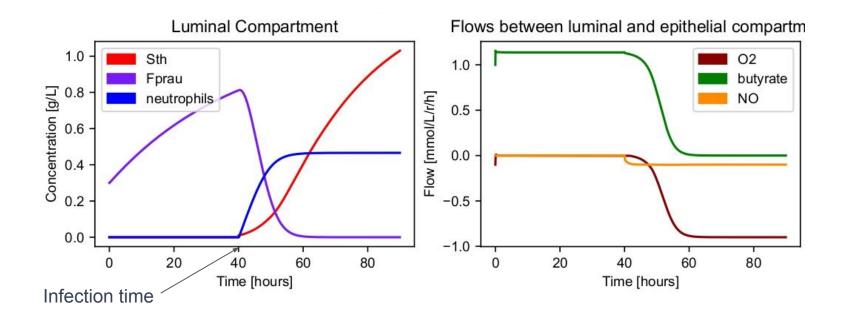




$$\partial_t s = \frac{Q_{in}s_{in} - Q_{out}s}{V} + \text{ biological and chemical reactions} + \text{ exchange to epithelial compartment.}$$

Muñoz-Tamayo *et al,* Journal of Theoretical Biology (2010)

Results



Results: Luminal Compartment

Ratio of reduced to total forms of thiosulfate

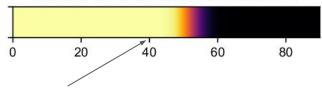
Ratio of reduced to total forms of galactose

Ratio of reduced to total forms of glucose

Ratio of reduced to total forms of nitric_oxide

Ratio of butyrate to maximum level attained

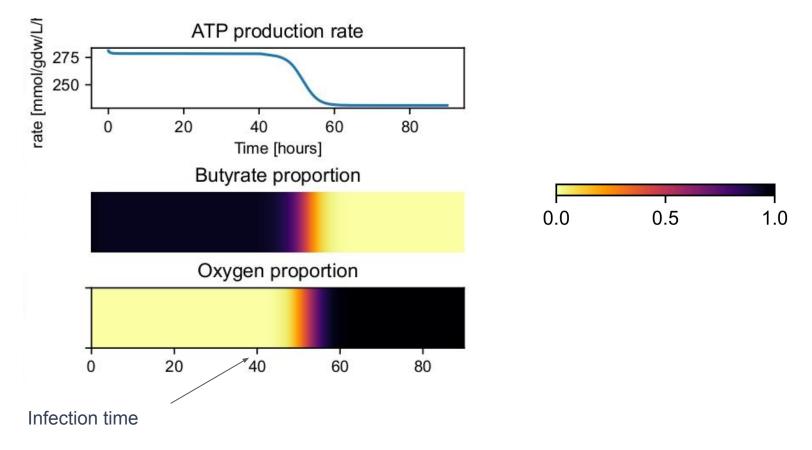
Ratio of O2 to maximum level attained



Infection time

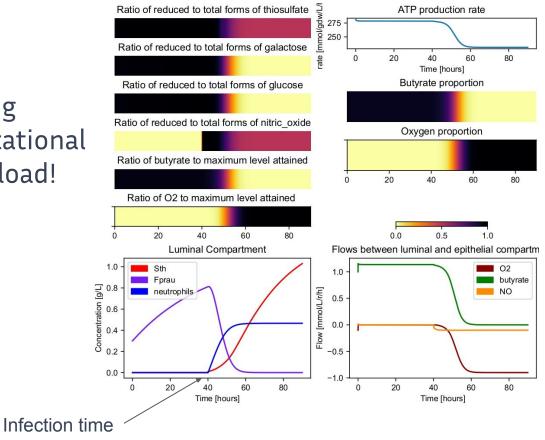
	1	
0.0	0.5	1.0

Results Epithelial Compartment











- A surrogate model consists of **approximating** a function by another one, in order to gain computation time.
- **Statistical Learning:** Methods to reconstruct a function describing an unknown underlying distribution from a set of observations.

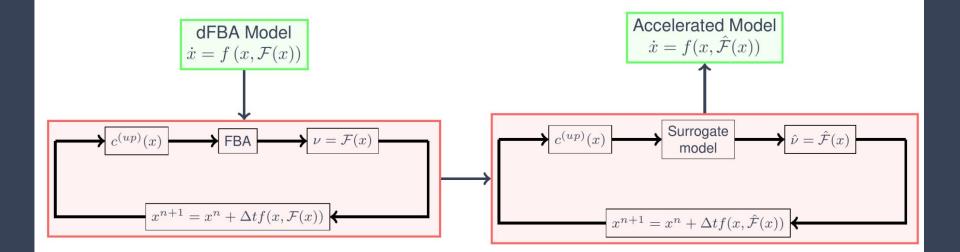


- A surrogate model consists of **approximating** a function by another one, in order to gain computation time.
- **Statistical Learning:** Methods to reconstruct a function describing an unknown underlying distribution from a set of observations.
- But we already know the function! $\mathcal{F}: \mathbb{R}^{N^{up}} \longrightarrow \mathbb{R}^{N_r}$

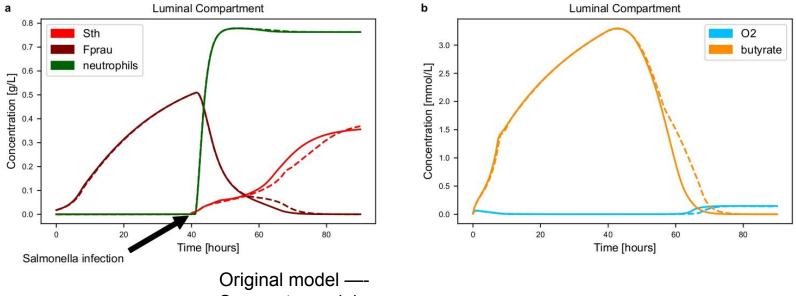
 $c^{(up)} \mapsto \nu^*$

- 1. Generate a database of observations
- 2. Construct a surrogate model
 - 3. Replace the original function

Speeding up the dynamic model

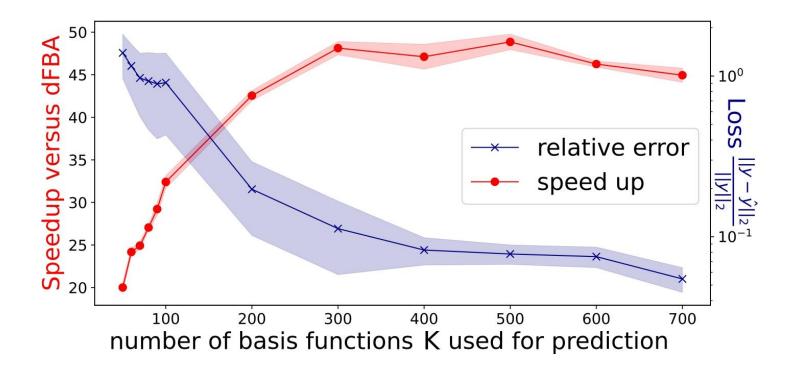


Speeding up the dynamic model



Surrogate model - - - -

Speeding up the dynamic model





• Success at efficiently **capturing** and **predicting** the metabolic roles of **each** partner in the infection at the **cost of limited loss in accuracy**



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- A **mechanistic** and **accurate** metabolic model of a complex system involving a human metabolic network



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Take-Home Message

Our model **paves the way** to a **more systematic** use of metabolic models as descriptors of **microbe-microbe** and **host-microbe** interactions during dysbiosis





• **Optimize** the speed-up and the accuracy \implies **Benchmark** of other metamodel



- Optimize the speed-up and the accuracy ⇒ Benchmark of other metamodel
- Add spatialization to our model



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- Add spatialization to our model
- Model of dysbiosis to model implying *E. coli* to compete with *Salmonella*
- **Generalize** the approach to other ecosystems which functions are **important** for dynamics of the community

Acknowledgement

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CBIO – Centre for Computational Biology

Laboratoire de Mathématiques et Modélisation d'Évry





Clémence Frioux Simon Labarthe Pablo Ugalde-Salas David Sherman Marie-Luce Taupin Rafael Kaempfer Arie Wortsman Sylvie Huet Julien Martinelli Thibault Malou

SLIMMEST project coordinators



UNIVERSITE PARIS-SACLAY



Thank you for your attention !

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