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José Galaz, Maria Kazolea, Antoine Rousseau. Modeling wave breaking by coupling dispersive and hyperbolic water wave models. MOMI 2023 - Le Monde des Mathématiques Industrielles 2023: Smart Environment, Apr 2023, Sophia Antipolis, France. 2023. hal-04189458

HAL Id: hal-04189458 https://inria.hal.science/hal-04189458v1

Submitted on 28 Aug 2023 $\,$

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Modeling wave breaking by coupling dispersive and hyperbolic water wave models

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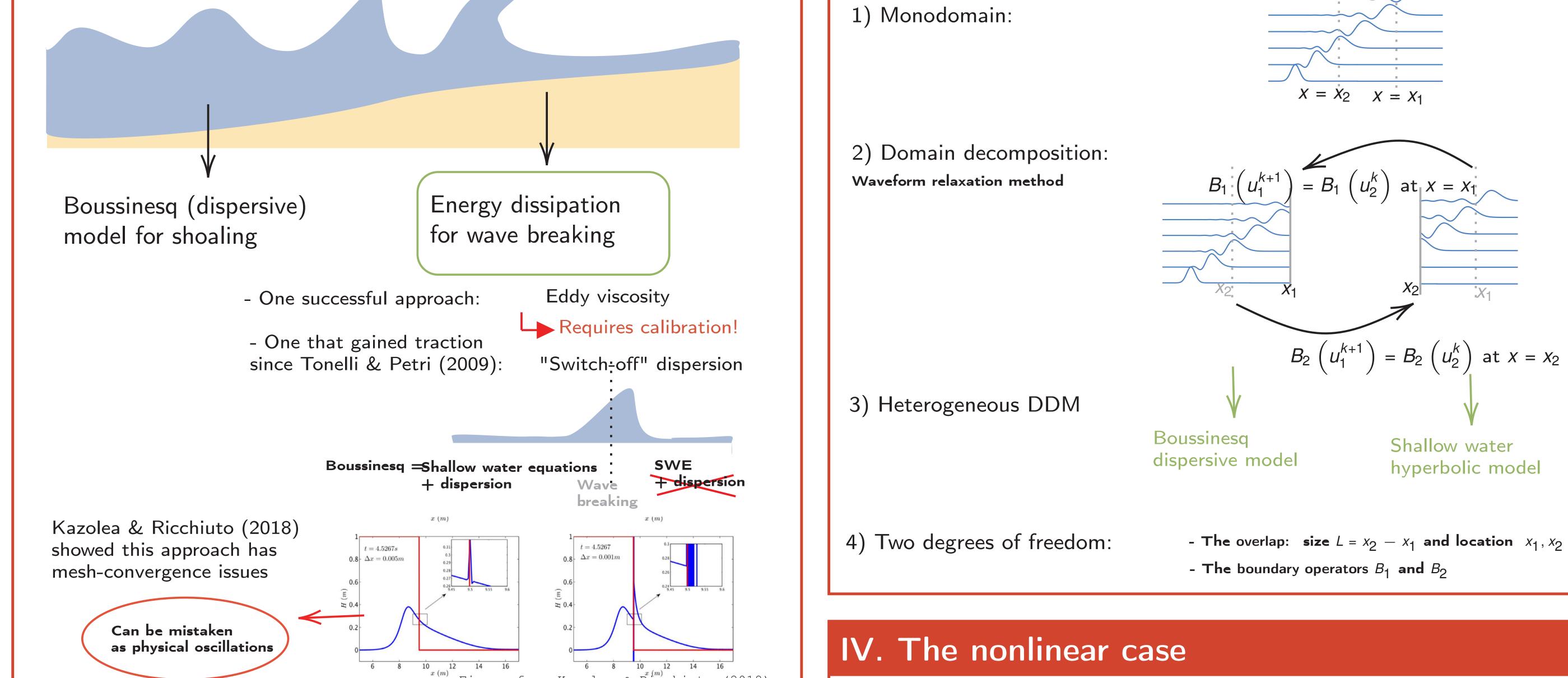
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I. Current coupling techniques can be unstable

In coastal engineering applications, wave breaking is usually handled with two model components:

II. Schwarz-Waveform relaxation method ...

... is a domain decomposition method first presented by Gander & Halpern (2007), that iterates information from two subdomains using **boundary conditions** and **overlapping zones**.

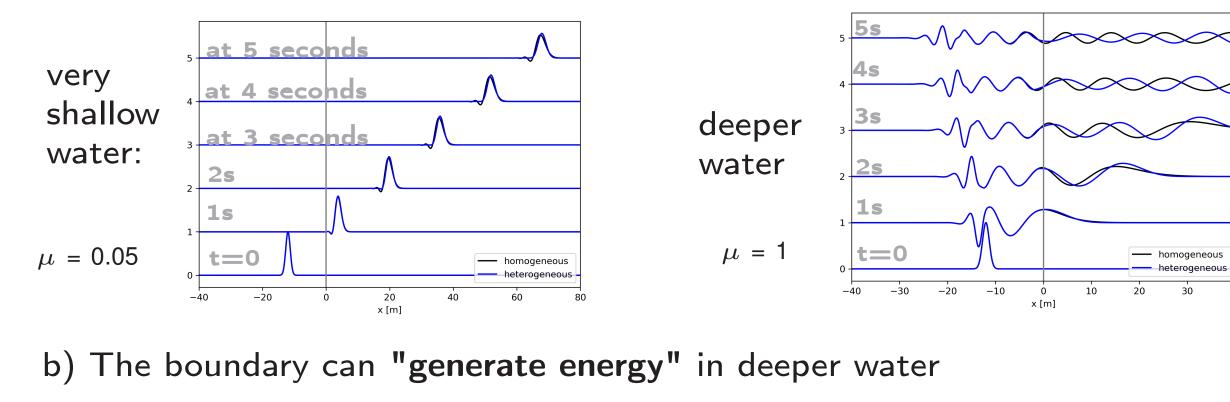




' Figure from Kazolea & Ricchiuto (2018)

III. The linear case

- 1) Without overlap $L = x_1 x_2 = 0$
 - a) The coupling always acts as an **approximate absorbing boundary**: reflections start to appear only in **deeper water**

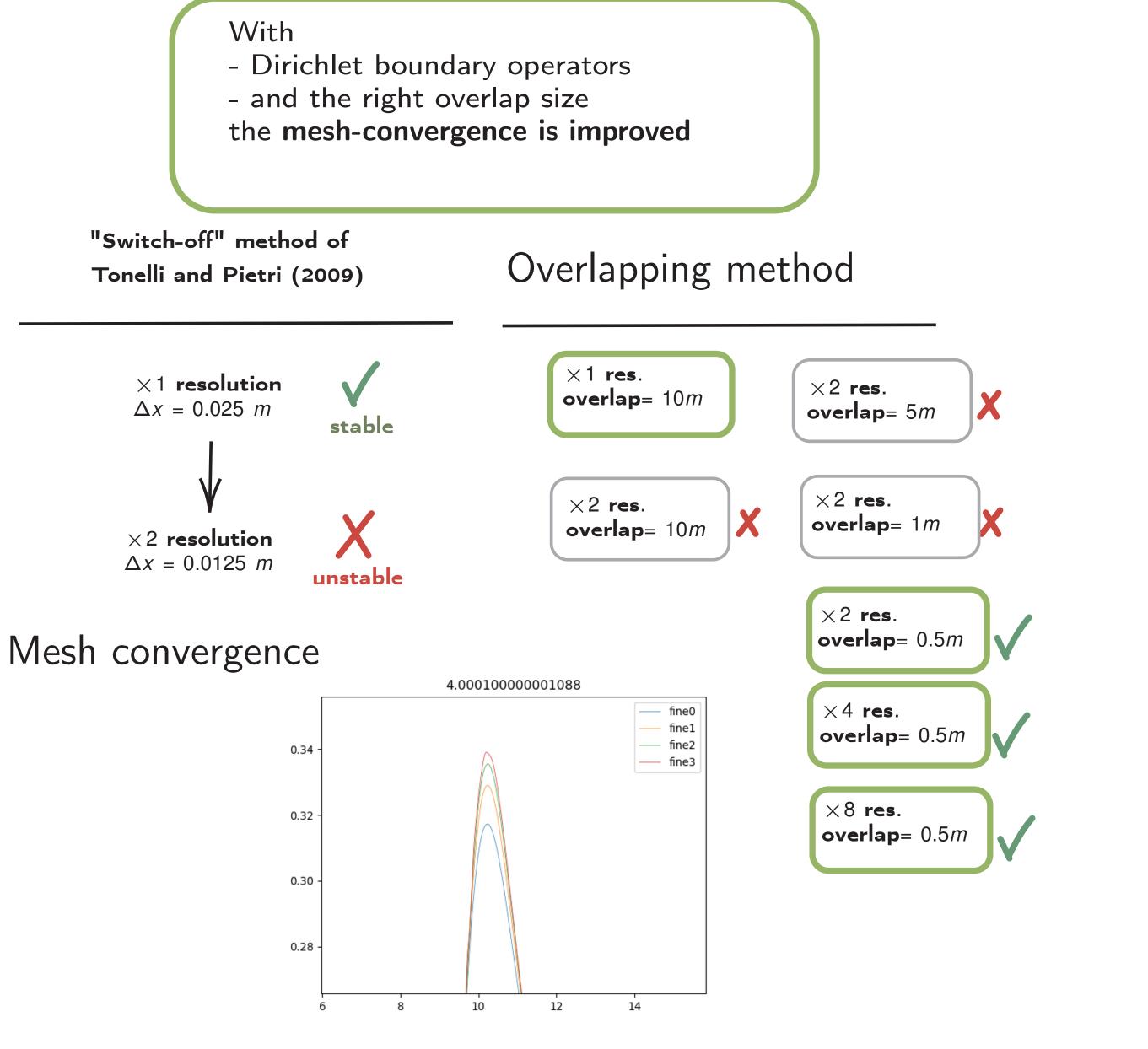


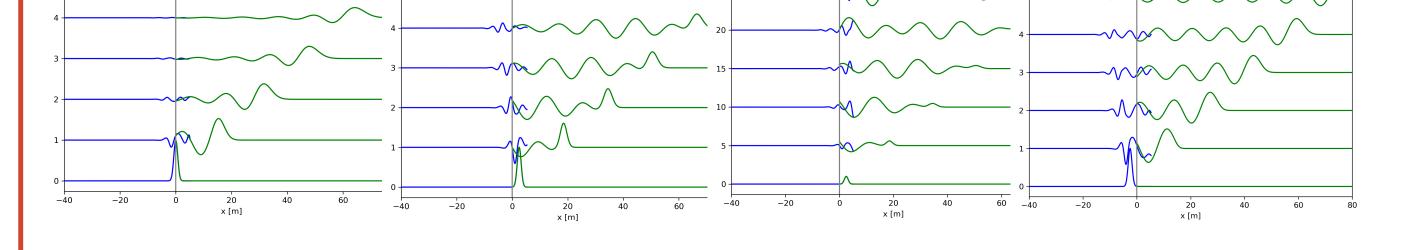
$$E(t) = E(0) + \frac{1}{2\pi} \int_{\mathbb{R}} |\mathcal{L}(U)(\xi)|^2 \left(\frac{c}{2} - \frac{\mu\xi^2}{c}\right) d\xi \qquad \text{sometimes}$$
is positive

2) With overlap $L = x_1 - x_2 > 0$

The choice of the operator changes the wave dynamics			
Dirichlet-Dirichlet	Neumann-Dirichlet	Dirichlet-Neumann	Robin-Robin
5-	25	5	

Nwogu's Boussinesq equations for weakly dispersive - weakly nonlinear waves:





Bibliography

- Kazolea, M., & Ricchiuto, M. (2018). On wave breaking for Boussinesq-type models. Ocean Modelling, 123, 16-39.
- Tonelli, M., & Petti, M. (2009). Hybrid finite volume-finite difference scheme for 2DH improved Boussinesq equations. Coastal Engineering, 56(5-6), 609-620.
- Gander, M. J., & Halpern, L. (2007). Optimized Schwarz waveform relaxation methods for advection reaction diffusion problems. SIAM Journal on Numerical Analysis, 45(2), 666-697.

Next questions:

- What is the "good overlap" for different resolutions, breaking strength, bathymetry slope, etc?
- Do other boundary conditions stabilize the nonlinear model?