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Validity of summary statistics-based mixed-effects group fMRI

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What is the link between meta-analysis and group fMRI?



Methods

GLM for group fMRI



Solving the GLM: OLS vs. FGLS

Y = Xβ + ε, where ε ~ N(0,
$$\tau^2$$
 + σ^2_i)

Assuming $\tau^2 + \sigma_i^2$ constant, **Ordinary Least Squares (OLS)** gives the following group statistic estimate:

$$T = \left(\sum_{i=1}^{N} \frac{Y_i}{\sqrt{N}}\right) \middle/ \widehat{\sigma_C^2}$$

where $\widehat{\sigma_C^2}$ is the usual one-sample variance. Under ${
m H_0}:~T\sim {\cal T}_{N-1}$

Solving the GLM: OLS vs. FGLS

Y = Xβ + ε, where ε ~ N(0,
$$\tau^2$$
 + σ^2_i)

Feasible Generalised Least Squares (FGLS) gives the following group statistic estimate:

$$T = \left(\sum \kappa_i Y_i\right) / \sqrt{\sum_{i=1}^N \kappa_i}$$
 where $\kappa_i = 1/(\hat{\tau}^2 + s_i^2)$

where s_i^2 is the study i's sampling variance. In large samples, under ${
m H_0}$: $T\sim {\cal T}_{N-1}$

Solving the GLM: OLS vs. FGLS

	Statistic	Assumptions	Implementation		
OLS	$T = \left(\sum_{i=1}^{N} \frac{Y_i}{\sqrt{N}}\right) \middle/ \widehat{\sigma_C^2}$	τ^2 + σ^2_{i} constant	SPM 'One-sample t-test' (default)		
			'Mixed effects: Simple OLS'		
			AFNII 3dttest++		
FGLS	$T = \left(\sum \kappa_i Y_i\right) / \sqrt{\sum_{i=1}^N \kappa_i}$	Large samples	SPM 'Mixed-effects analysis'		
			'Mixed effects: FLAME1' (default)		
			AMI 3dMEMA		

Goal: assess the validity of OLS and FGLS under violation of their assumption

Method: Monte Carlo simulations

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And in meta-analyses?



Question: Does this issue also affects group fMRI studies?

Simulations

Between- and within-subject variances in real fMRI data

21 studies investigating pain

Study	# subjects	# outliers	Mean τ^2	Mean σ^2_{in}	Max/Min σ² _{in} ratio	$\underset{\sigma^{2}_{out}}{\text{Mean}}$
01	25	2	354	100	4	282
02	25	1	680	100	5	317
03	20	2	800	100	5	281
04	20	3	886		9	347
05	9	0	1802		3	-
Summary		0-15%	18-170	100	2-9	164-300

Simulation setup

- $N \in \{25, 50\}$ subjects
- $\tau^2 = 1$ and mean(σ^2_{in}) = 1
- Two settings for the within-subject variance:
 - $\max(\sigma_{in}^2) / \min(\sigma_{in}^2) \in \{1, 2, 4, 6, 8, 10\}$
 - 16% of outliers with $\sigma^2_{out} \in \{ 0.25, 0.5, 2, 4 \}$

10⁶ realisations

Results

Varying levels of heteroscedasticity



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In the presence of outliers



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Real data



Conclusions

FGLS can be invalid is small samples, especially in the presence of strong heteroscedasticity or 'low variance' outliers.

RFX remained valid in all studied settings.

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