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# Autovesk: Automatic vectorized code generation from unstructured static kernels using graph transformations

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Leveraging the SIMD capability of modern CPU architectures is mandatory to take full advantage of their increased performance. To exploit this capability, binary executables must be vectorized, either manually by developers or automatically by a tool. For this reason, the compilation research community has developed several strategies for transforming scalar code into a vectorized implementation. However, most existing automatic vectorization techniques in modern compilers are designed for regular codes, leaving irregular applications with non-contiguous data access patterns at a disadvantage. In this paper, we present a new tool, Autovesk, that automatically generates vectorized code from scalar code, specifically targeting irregular data access patterns. We describe how our method transforms a graph of scalar instructions into a vectorized one, using different heuristics to reduce the number or cost of instructions. Finally, we demonstrate the effectiveness of our approach on various computational kernels using Intel AVX-512 and ARM SVE. We compare the speedups of Autovesk vectorized code over GCC, Clang LLVM and Intel automatic vectorization optimizations. We achieve competitive results on linear kernels and up to 11x speedups on irregular kernels.

CCS Concepts: • **Computer systems organization** → **Single instruction, multiple data**; • **Software and its engineering** → **Source code generation**; • **Theory of computation** → **Vector streaming algorithms**.

Additional Key Words and Phrases: Automatic vectorization, code generation, graph transformations

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## 1 INTRODUCTION

Vectorization is a feature of modern CPUs that consists in applying a single instruction to multiple data (SIMD) [12]. It is one of the hardware features that has increased CPU performance despite the stagnation of the clock frequency. To take advantage of this functionality, a binary must explicitly use vector instructions, and this requires that the program be vectorized by the back-end compiler when it issues the machine code, or at runtime [14].

HPC experts tend to vectorize their code manually [6] in assembly or with intrinsic functions<sup>1</sup>. This allows them to fine-tune and control the behavior of their computational kernels. However, it

<sup>1</sup>An intrinsic function is a function that is usually converted into a single instruction by the compiler, allowing some instructions to be used explicitly while remaining at a high level

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also requires significant expertise and can imply re-implementing new kernels for each instruction set architecture (ISA). To mitigate this drawback, several abstraction libraries have been created [5, 11, 13, 19, 21, 31, 36]. They allow writing vectorized code with an abstract vector type that is fixed at compile time depending on the target architecture. This clearly facilitates maintainability, but requires a moderate level of understanding of the vectorization concept. The main limitation of this approach is that the operations supported by the library should be present in all underlying ISAs, or if not, the desired behavior should be implemented with more instructions, leading to the difficulty of having a single kernel implementation that is efficient everywhere. From another research perspective, the compilation community has proposed different strategies for automatically transforming scalar code into a vectorized equivalent. The resulting mechanisms, introduced in modern compilers, work well when the code is regular, i.e., with contiguous data accesses and affine loops. However, when the code to be vectorized is irregular or has complex dependencies between variables, the compilers tend to fail. This strategy allows to have a single clear and portable source code and still obtain good performance thanks to the compiler. This paper presents a new strategy for vectorizing irregular and unstructured computational kernels. Our method aims to complement existing mechanisms by focusing on non-contiguous data access patterns. It allows non-expert programmers to benefit from vectorization and experts to delegate complex vectorization implementations that require many data transformations. In fact, our tool tries to minimize the number of instructions at the cost of complex vector transformations (permutations, extractions, merges, etc.) that are usually tedious to manage with intrinsics or in assembly.

The contribution of our work is the following:

- to provide a new automatic vectorization strategy. Our approach operates on an instruction graph that is transformed to minimize the total number of instructions;
- to decompose the problem into several sub-problems and provide different heuristics to solve them;
- to study the performance of the resulting vectorized kernels against automatic vectorization in modern compilers, namely GCC and icpx Intel, and state-of-the-art techniques in LLVM’s vectorizer;
- to propose a new instruction ordering strategy to reduce register spilling, i.e. transfers between the stack and registers.

The paper is organized as follows. In Section 2 we describe the background of vectorization and automatic vectorization. We discuss related work in Section 3. In Section 4, we present our method. Finally, we evaluate the benefit of our method in Section 5.

## 2 PROBLEM DESCRIPTION

### 2.1 Vectorization

The principle of vectorization, as developed in modern CPUs, can be described as a technique that allows a single instruction to be applied to one or more vectors of native data types. The implementation of this concept in modern CPUs is subject to several constraints. For instance, the size of the vector is fixed and hardware-dependent, although it is possible to pad the vector with arbitrary values to operate on smaller sizes. The vectors are CPU registers, so load and store operations must be used to exchange data with main memory. The set of operations supported by a processing unit to manipulate the vectors is hardware dependent. More specifically, it is tied to the ISA, and each ISA may have operations that are not supported by others. For example, some may allow shuffling of data within the vectors, while others may only support shuffling within half of the vectors. Some may support non-contiguous memory access with gather/scatter operations, while others may not. However, we can safely assume that they all support arithmetic/logic operations,

which are usually applied term by term to two vector operands. In our approach, we consider that vector transformation instructions are available to shuffle the data, extract elements, and merge two vectors into one. When considering performance, it is usually more efficient to load/store contiguous elements into memory and use aligned memory accesses (i.e., the starting address pointer is a multiple of a given value). Predication is a feature supported by some ISAs, such as ARM SVE, which allows operations to be applied only to certain active elements using predicate vectors. Other ISAs, namely x86, can achieve similar functionality but with a different implementation. It generates mask vectors that are used with binary operations to eliminate inactive elements.

## 2.2 Automatic vectorization

Automatic vectorization consists of converting a scalar source code or binary into a vectorized equivalent without explicit guidance from the developers. Source code vectorization is not straightforward because it can be written in a way that complicates the vectorization process. This includes the use of inappropriate data structures and inefficient memory access. It is also not always feasible to generate a vectorized kernel prior to execution because it can be difficult to predict data dependencies. Moreover, even if vectorization can be applied, the result can be inefficient and take longer to execute than the original version. Indeed, if we suppose that we put a single scalar value (or a few of them) inside each vector, it seems straightforward to obtain a naive vectorized program. However, the waste in the vectors and the fact that vectorized operations may have a higher cost (either in latency or throughput) would lead to a poor implementation. Therefore, a good metric for predicting the performance of a vectorized kernel is to count the number of instructions, each of which may have a cost associated with it, and consider the lower the better. In this study, we focus on static kernels, which allow us to know the original number of scalar instructions. Some non-static kernels can be seen as a dynamic iteration of a static kernel, so our method is also useful in this case. We will demonstrate the complexity of the problem by giving an approximation of the amount of computation that is required to obtain an optimal solution.

We consider a direct acyclic graph  $G(V, E)$ , where  $V$  represents the set of vertices corresponding to  $N$  scalar operations in the original source code, and  $E$  represents the edges indicating the dependencies between these operations. The number of possibilities to group the  $N$  scalar operations into subsets of size  $k$  is bounded by

$$\prod_{i=0}^{\lceil N/k \rceil} \frac{(N - i \times k)!}{(N - k \times i - k)!} \quad (1)$$

These scalar operations can be loads, stores or other types of operations. It's important to note that, given the dependencies in the directed acyclic graph (DAG), even operations of the same type but at different depths are considered as different types. Any subset we form must group operations of the same type, and considering this constraint reduces the number of possibilities. However, the proposed bound assumes that  $N$  is divisible by  $k$ , resulting in  $N/k$  subsets where all vectors of size  $k$  are full. If we deviate from this assumption and make the subsets non-full, the problem becomes more complex, leading to an increase in the number of ways to group the scalar operations. Due to this complexity, finding an optimal vector graph by a brute-force approach seems infeasible. Hence, we emphasize the need for heuristic methods to effectively tackle this problem.

## 3 RELATED WORK

Auto-vectorization transforms scalar operations into SIMD operations that can process multiple data elements in parallel, leading to significant performance improvements on modern processors.

There are two main strategies for automatic vectorization in modern compilers: loop vectorization and Superword Level Parallelism (SLP).

Loop vectorization is a technique that leverages parallelism in loop iterations to transform scalar operations into SIMD operations [1, 17, 30]. Multi-dimensional vectorization simultaneously vectorizes multiple loops in a loop nest, providing benefits such as data reuse, register tiling, and improved memory access efficiency [20]. Outer-loop vectorization targets a different level than the innermost loop, which can be beneficial for loops with greater data-level parallelism and locality [9, 23]. However, many computations require more advanced loop transformations to be in a vectorizable form and preferably without dependencies to ensure consistency. One of the challenges of loop vectorization is dealing with non-contiguous access patterns to the operation data. To address this, Nuzman et al. [22] introduced an extension to a classical loop-based vectorizer that handles non-unitary computations and data accesses, particularly data with powers of 2 on CPUs. This extension helps to exploit spatial locality and address interleaved data access, but remains limited to regular strided access patterns. [2] presents a generalized approach to loop vectorization that achieves significant speedups for both power-of-2 and non-power-of-2 interleaving factors.

Loop vectors mostly deal with the data parallelization aspect directly related to the SIMD architecture. As a counterpart, there is the SLP algorithm, originally introduced in [18]. It performs instruction-oriented vectorization. It is often commonly used to convert linear code to vector code, complementing traditional loop-based vectorizers. The SLP algorithm analyzes the input code by scanning the intermediate representation (IR) generated by the compiler looking for instruction groups that can be combined into vectors. It replaces these selected instruction groups with the corresponding vector instructions. Rosen et al. [29] proposed the Bottom-Up SLP algorithm, which is implemented in the well-known GCC and LLVM compilers. The main contribution of the algorithm is its ability to handle sequential code anywhere in the program, not just in loops. It can also vectorize code inside loops if the loop vectorizer fails. Our proposed tool has a similar objective, but is currently limited to working with code that uses C++ templates, as it has not yet been integrated into a compiler at the IR level. While the evaluation focuses on vectorization opportunities within loops, which are generally more common, it still provides valuable insight into the potential of our techniques. The SLP approach has some limitations. First, it operates locally or even atomically on individual SLP graphs which can be limiting in the case of consecutive graphs sharing data. In such cases, vectorization costs may be overestimated, leading to missed opportunities even in simple code. The SLP vectorizer may miss several vectorization opportunities in loops, as shown in the results of our work (Section 5). Rocha et al. [28] presented Vectorization Aware Loop Unrolling (VALU), a new heuristic accompanying the compiler in searching for loop unrolling opportunities to enable automatic vectorization of sequential code. VALU checks whether loop unrolling is cost effective for the SLP vectorizer and identifies the loop unrolling factor that can maximize the use of vector units in the target architecture. In *Autovesk*, we fully unroll the kernels as we create the scalar instruction graph, allowing for more instruction grouping possibilities, i.e., better vectorization of the code. Porpodas et al. [26] presented Look-Ahead SLP (LSLP), an improved vectorization algorithm based on SLP that focuses mainly on commutative operations. It is implemented in the LLVM compiler. The main contributions of LSLP are, first, the ability to extend the SLP graph data structure to form multi-nodes of chains of commutative operations of the same type. Second, it introduces a more powerful operand reordering scheme that makes informed decisions based on instructions deeper in the code. Our method enables chain reduction for improved vectorization efficiency by transforming the scalar instruction graph and grouping and annotating commutative operation nodes. Porpodas et al. [25] go further and present Super-Node SLP (SN-SLP), a new algorithm similar to LSLP with multi-nodes, including both commutative operations and their corresponding inverse elements, for example, addition and its inverse subtraction. SN-SLP leverages the algebraic

properties of these operators to allow additional transformations, increasing the possibilities of vectorization. It is implemented in LLVM. Several works have proposed heuristics to optimize instruction ordering and code regions for vectorization in SLP-based algorithms. Nevertheless, our new approach is competitive and offers additional flexibility by allowing vectorization of kernels with irregular data access patterns through instruction grouping and reordering transformations and heuristics.

Since vectorization can be seen as instruction-level parallelization, the work on automatic parallelization using the polyhedral model can be used [4, 24, 35]. Polyhedral compilers are specifically designed to support calculations in the affine domain, where loop boundaries and subscript expressions can be expressed as integer linear functions of both loop indices and loop constants.

Irregular applications such as graph algorithms, particle simulation codes, and sparse matrix codes that use compact representations [3, 8, 10, 16] are now being considered for acceleration using SIMD capabilities. However, the initial focus of SIMD devices has been on speeding up regular applications such as dense matrix multiplication and image processing. Vectorization becomes particularly challenging when dealing with irregular access patterns. Another challenge is dealing with memory alignment, which has been largely ignored in previous research focusing on properly aligned memory references. Existing vectorization approaches for such irregular applications include inspector/executor and conflict masking. Inspector/executor transformations involve loop and data layout transformations that require a runtime component due to unresolved indirect array accesses. The Sparse Polyhedral Framework (SPF) extends the capabilities of the Polyhedral Framework by incorporating uninterpreted functions to represent non-affine array accesses, non-affine loop boundaries, and inspector-executor transformations [32, 37]. Conflict masking is an approach to resolving data conflicts in SIMD vectors by identifying non-conflicting lanes and writing only to them in each round of execution. A conflict detection instruction (`vpconflict`) has been added to the Intel AVX-512 instruction set to facilitate conflict masking. The vectorization performance of conflict-masking depends on the input distribution. If conflicts arise frequently in the input, conflict-masking will result in low SIMD utilization and thus poor vectorization performance. Jiang and Agrawal [15] propose a code transformation called in-vector reduction that can efficiently vectorize a class of associative irregular applications. Further research aims to support aggressive SIMD vectorization of important loops, even when their bodies contain complex control flow and the entire computation cannot be fully parallelized, such as speculative execution [33, 34]. Beyond this, Chen et al. [7] propose VeGen, an extensible framework that targets non-SIMD vector instructions by introducing a new model of vector concurrency called lane-level concurrency (LLP). This new model goes beyond traditional SLP by allowing instructions to perform multiple non-isomorphic operations, and operations on any output lane can use values from arbitrary input lanes.

## 4 AUTOVESK

### 4.1 Transformation flow

We provide in Figure 1 an overview of the internal organization of our engine<sup>2</sup>. First, the process starts by obtaining a graph of scalar instructions of a given computational kernel (Section 4.2). In the second step, the graph can be transformed to take advantage of reduction when relevant (Section 4.3). In the third step, the instructions are grouped to obtain a meta-graph (Section 4.4). Next, the groups are split to match the desired vector size, denoted by `VEC_SIZE` (Section 4.5). We divide the loads/stores first, then the arithmetic/logical operations. Then the order of the elements in each group is set, and the necessary permutations/extractions are performed (Section 4.6). Finally,

<sup>2</sup><https://gitlab.inria.fr/bramas/autovesk>

the resulting vector operation graph is ready to be translated into a vector instruction list by our backend (Section 4.8).

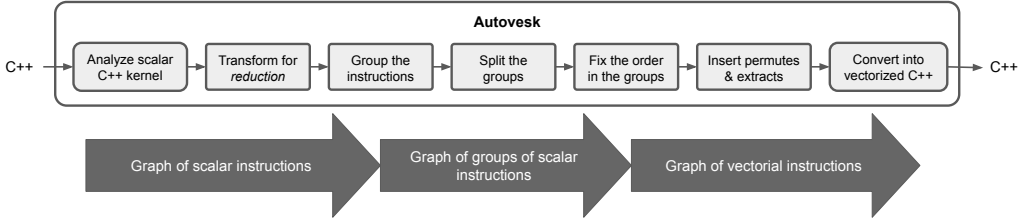


Fig. 1. Overview of the transformation flow in Autovesk. Starting from a C++ code, the tool successively uses a graph of scalar instructions, a graph of groups and a graph of vector instructions.

To illustrate these different mechanisms, we will consider the vectorization of two kernels given in Figure 2 under the names *KA* and *KB*.

```

1 void Kernel_A(const double* inValue1, const double* inValue2, double* outValue, const
2   long size){
3   for(long int idx = 0 ; idx < size ; ++idx){
4     outValue[idx] = inValue1[(idx*2)%size] * inValue2[(idx*2)%size];
5   }
6 }
7 void Kernel_B(const double* inValue1, const double* inValue2, double* outValue, const
8   long size){
9   double x = 0;
10  for(long int idx = 0 ; idx < size ; ++idx){
11    x += inValue1[idx] + inValue2[idx];
12  }
13  outValue[0] = x;
14 }

```

Fig. 2. Two example functions to be vectorized, denoted by *KA* and *KB*. A static version of these functions is obtained by fixing the *size* variable. In this case, the loops can be fully unrolled and vanish.

## 4.2 Scalar graph generation

In our current engine, we generate a direct acyclic graph of scalar instructions using a custom C++ tool based on templates and operator overloading, which builds the graph during the execution of a compiled program. This stage will disappear when Autovesk is ported to an existing compiler, but it allows us to validate the transformation steps. We have four types of scalar nodes that compose our graph:

- set: is the assignment of a variable with a given value, for example the line 7 in Figure 2.
- load: is accessing memory using an address to read a value, for example the lines 3 and 9 in Figure 2.
- operation: is the use of one or more elements as input and the creation of an output. Arithmetic operations belong to this category.
- store: is accessing memory using an address to write a value, for example the lines 3 and 11 in Figure 2.

What we get is a graph, not a tree, because for a given node, the subgraphs of its successors are not necessarily disjoint. For instance, if we have the instructions  $a = x$ ,  $b = a * a$ ,  $c = a + a$ , and  $d = b + c$ , the nodes representing  $b$  and  $c$  will have the same predecessors and successors. In

our representation, the scalar graph describes operations that are applied from loads/sets to stores without having the notion of variables. Therefore, some instructions are invisible, such as copying a variable to a local variable, since they do not affect memory. The graph for  $KA$  and  $KB$  is shown in Figure 3.

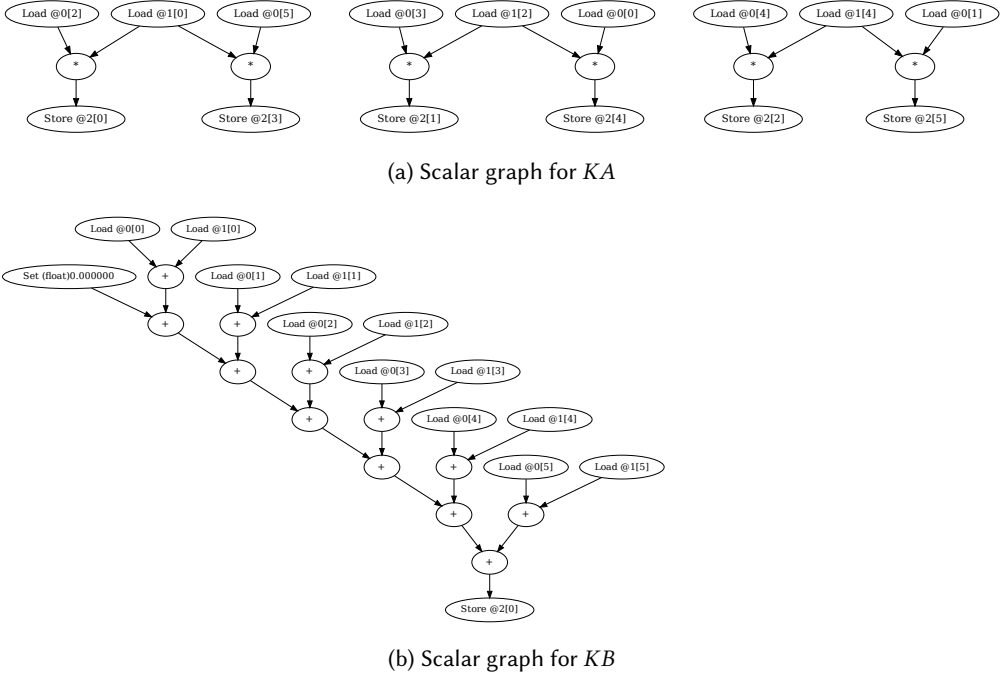


Fig. 3. Graphs of scalar instructions for  $KA$  and  $KB$  for kernel size equals 6. The arrays given in the parameters are numbered from 0 to 2 in order.

At this stage, we can already remove the duplicate nodes. Two nodes are considered equivalent if they perform the same operation and have the same input. If the operation is commutative, we assume that the order of the inputs is irrelevant. Thus, we iterate on the graph from loads/sets to stores, removing the duplicate nodes wherever possible.

### 4.3 Commutative operations and reductions

In vectorization, the reduction pattern consists of changing the order of commutative operations to maintain multiple intermediate results, which are then reduced to one, opening the possibility of more efficient vectorization. In our case, we enable the reduction by transforming the scalar instruction graph and annotating the corresponding nodes to group them (Section 4.4). The transformation consists in finding a path in the graph of similar consecutive commutative operations and splitting this path so that we obtain independent  $VEC\_SIZE$  sub-paths. Therefore, we iterate over all nodes of the graph, and when we find a commutative operation, we evaluate if it is the starting point of a reduction path. Then, we check if the length of the path is enough to hope to benefit from the reduction, i.e. if there are more than  $VEC\_SIZE$  nodes. If this is the case, we split this path into chunks of  $VEC\_SIZE$  and connect them with reduction nodes. We provide the graph for  $KB$  after the reduction transformation in Figure 4. Unlike  $KB$ , there is no opportunity for



reduction in the *KA* example, i.e. there is no chain of commutative operations to be reduced into an output result.

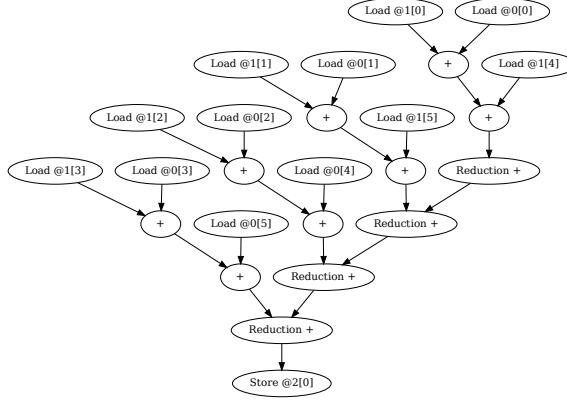


Fig. 4. Graph of scalar instructions for *KB* for kernel size equals 6 and  $VEC\_SIZE = 4$ . We can observe that the operations just before the store node were replaced by reduction nodes which materialize the reduction instruction that will be generated later. We can also see that the sources of these nodes are 4 reduction chains (as much as  $VEC\_SIZE$ ) that happen to be isomorphic so they can be vectorized.

#### 4.4 Instruction grouping

In this step, we generate a meta-graph where the nodes contain lists of scalar operations that could potentially be vectorized together. To perform this transformation, we group nodes of the same type. Thus, we group the loads that refer to the same array, and we do the same with the stores. Then we group the same operations that are at the same distance from the leaves of the graph (i.e., loads and stores). By doing this, we ensure that there are no dependencies between the nodes of a group because we are managing it by construction. At this stage, groups can contain more scalar nodes than the size of the SIMD vector can handle ( $VEC\_SIZE$ ), and the internal order of scalar operations in the list is unspecified. We provide the group for *KA* and *KB* in Figure 5.

#### 4.5 Group divisions

Once we have the meta-graph, we need to decide how to split the groups that contain more than  $VEC\_SIZE$  instructions. We do this in two steps, first on loads/stores, then on operations.

*Loads/stores divisions.* To divide the groups of load operations, we follow three rules. First, we need to load the values in a contiguous order. Second, we want to minimize the number of memory accesses. Finally, there should be no more than one vector that is not fully filled, i.e. all used vectors are filled with  $VEC\_SIZE$  values and at most one vector has less than  $VEC\_SIZE$  values. Suppose we have an array of  $L$  scalar loads, where  $L = k \times VEC\_SIZE + r$ , with  $0 \leq r < VEC\_SIZE$ . If  $L$  is divisible by  $VEC\_SIZE$  without leaving a remainder (i.e.  $r = 0$ ), there is no choice: loads are in order and all vectors will be full. However, if we have  $r > 0$ , we have to decide which vector will not be fully filled, i.e. how to distribute the scalar loads among the vectors with respect to the contiguous order. This decision affects the other stages of vectorization because it determines the initial state of the vectors, which in turn affects the number of transformations required in subsequent stages. This can affect the final quality of the vector implementation.

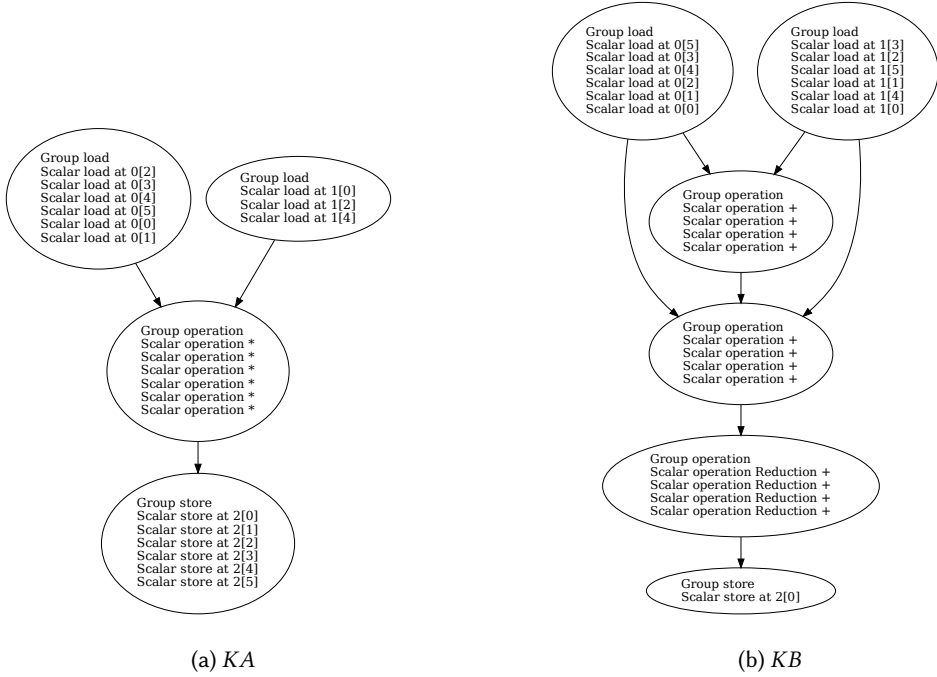


Fig. 5. Graphs of groups for KA and KB for a kernel size equal to 6. An edge between two nodes indicates that at least one instruction from each of the two groups is connected.

Therefore, we tackle this problem by generating all possible combinations that satisfy the three rules above, and picking the combination that leads to the vector graph with fewer nodes. If we consider that the number of vectors needed to load  $L$  values is  $V$  (with  $V = k + 1$  if  $r \neq 0$ , or  $V = k$  otherwise), we have  $V$  possibilities. This is because only one of the  $V$  vectors should be incomplete. If there are  $A$  arrays accessed in the kernel, either by load or store operations, the total number of possibilities is given by  $C = \prod_{i=1}^{i=A} V_i$ , where  $V_i$  is the number of vectors for array  $i$ . Concretely, if we have two arrays as input and one array as output, and load ten vectors from each,  $C$  will be one thousand. The different combinations for the kernels KA and KB are shown in Figure 6.

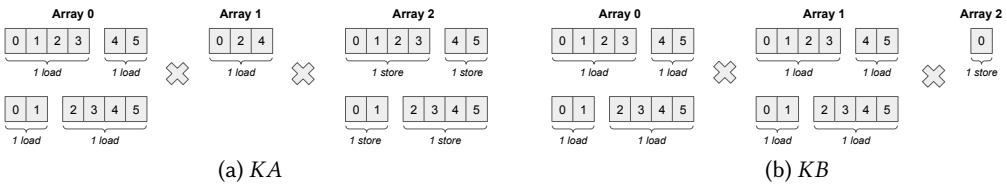


Fig. 6. All the combinations of loads/stores for the two kernels KA and KB considering size equals 6 and  $VEC\_SIZE = 4$ . There are 4 possibilities for KA ( $2 \times 1 \times 2$ ) and KB too ( $2 \times 2 \times 1$ ).

*Operation divisions.* After splitting the load/store groups, we split the operation groups. We iterate through the operation groups from loads to stores. By doing this, we can be sure that the inputs to the operations are already divided (or if the inputs are loads, they are also already fixed).

For each group  $g$  we compute a score-matrix  $d$  of dimension  $|g| \times |g|$ , which aims to express which of the elements of  $g$  should be in the same vector operation, i.e.  $d(i, j)$  describes the expected interest of putting the scalar operations  $i$  and  $j$  in the same vector operation. The calculation of this score is defined in Algorithm 1. The score  $d(i, j)$  increases with the number of common predecessors/successors between  $i$  and  $j$ . If they are two separate nodes, we increment the score by the number of common sources. For each destination group: if it is a *store* group, we increment the score by 1; if it is an *operation*, we increment by 1 in the case of a group of size less than or equal to  $VEC\_SIZE$ , or we increment by the inverse of the size of the destination in the case of a group of size greater than  $VEC\_SIZE$ , so the larger the size of the destination, the less value we bring to this group. We show an example of a score-matrix in Figure 7.

---

**Algorithm 1:** Compute the matrix entry  $d(A, B)$  for elements  $A$  and  $B$  of the same group.

---

```

1 score ← 0;
2 if A ≠ B then
3   | // Increment score by 1 or 2 for same sources
3   | score += (in_same_vector(A.src1,B.src1) + in_same_vector(A.src2,B.src2));
4 else
5   | // For the diagonal, add the number of sources, i.e. 1 or 2
5   | score += (A.src1 != null) + (A.src2 != null);
   | // Increment score if they are used at the same place (destination)
6 for d in Intersection(A.dest,B.dest) do
7   if d is a Store Group then
8     | score += 1;
9   else
10    | // d is an Operation Group
10    | if d.size ≤ VEC_SIZE then
11    | | score += 1;
12    | else
13    | | score += (1 / d.size);

```

---

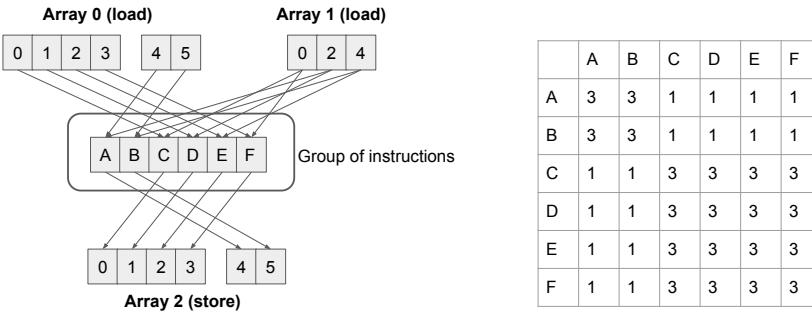


Fig. 7. Example of score matrix  $d$  for  $KA$  to split the scalar instruction group. The groups of loads and stores are already divided, and the Algorithm 1 is used to compute the matrix. The given matrix is found out for this specific configuration of loads/stores and could be different otherwise.

To split the group of operations, we propose two main strategies based on the division of the matrix  $d$ :

- (1) a clustering strategy where we create initial subgroups and then aggregate the elements using the best remaining score so far;
- (2) a partitioning strategy where we split the matrix at the point with the lowest score.

We know that we need  $V = \lceil |g|/VEC\_SIZE \rceil$  vectors. The partitioning strategy is provided in Algorithm 5 in Appendix A. We start with a partition that contains all elements. We find in this partition the two elements with the lowest score in the matrix (line 13) and initiate two new partitions (line 14). Then we aggregate the remaining elements on these two partitions while ensuring that no partition exceeds a given size. This is done either by finding the highest accumulated score among the remaining elements and moving them one by one (line 23) or by placing each element in the partition where it has the heaviest weight, represented by the maximum accumulated sum of its scores relative to all others.

The clustering strategy is provided in Algorithm 6 in Appendix B. We start by finding the two elements  $i$  and  $j$  with the lowest scores in the matrix, i.e. those with the least number of common predecessors and successors, and use them to initiate two subgroups (line 1). Then we find  $V - 2$  more elements, one by one, by selecting the elements with the lowest scores compared to the already fixed elements (line 5). We end up with  $V$  subgroups, each containing one element. Finally, we process the remaining elements. We compute, for each of them, the sum of the scores of the nodes of all subgroups and choose the subgroup with the best score (line 15).

#### 4.6 Fixing the order of vector's elements

At this stage we have subgroups that contain at most  $VEC\_SIZE$  scalar instructions. The order of these instructions is fixed for the loads and stores, but not for the operations. This is the aim of this layer. We have to find the correct positions to make the operations coincide with their predecessors and successors, thus ensuring the coherence of the kernel. Fixing the order will imply the use of permutations, merges, and extractions; therefore, the goal is to find the order of each group to minimize the need for additional instructions. We note that using an *Extract* instruction is costly in terms of execution time for the vectorized code. We also note that if we have to extract a single element using a vector instruction, this is equivalent in terms of execution time to extracting several elements less than or equal to the size of the vector instruction.

In a subgroup, for  $VEC\_SIZE$  scalar operations, we have  $VEC\_SIZE!$  possibilities to order them, leading to the impossibility to compare all of them greedily. That said, in our case an additional layer of constraints is added, which reduces the number of such possibilities. We have the connections between a subgroup of operations and their predecessors and successors, the order of the predecessors is already fixed (the order of a successor is fixed if it is a store). Therefore, taking into account the order of a successor, for example, forces the use of *extract/permute* instructions to retrieve the data required for the operation from other groups and to ensure kernel consistency. To illustrate the effects of a good order of operations, we present the examples in Figure 8.

It is enough that the positions of the operations are changed in the group of instructions that we are forced to add *Extract* instructions to make the vector instructions coincide. A good order prevents this. In Algorithm 2 we address this problem. It begins by identifying dependent sources, where fixing the position according to one source implies an *extract* for the other one. Next, it identifies operations with the same source position, making them dependent as well. The algorithm then sorts the sources based on the number of dependencies. It iterates through the dependent sources, identifying if any element is used by multiple operations, in which case an *extract* is required. It also checks if any operation uses the same source for both operands. For all other cases,

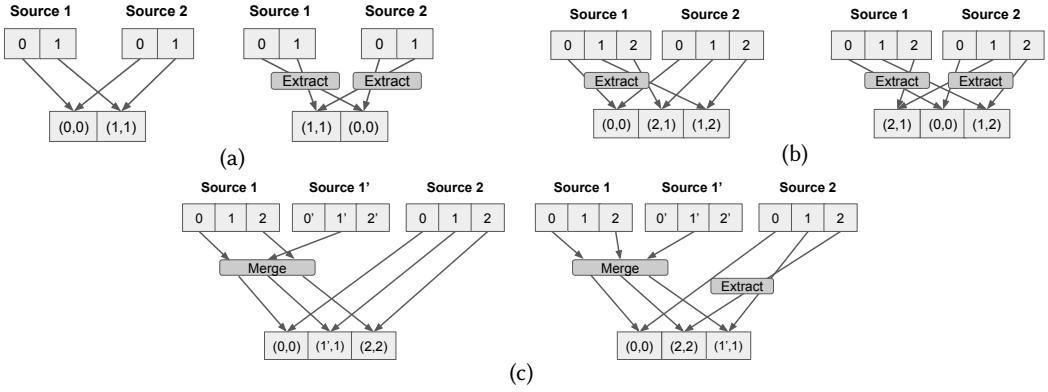


Fig. 8. Three examples with different order of the elements in the output vector. In each example (a, b, c) on the left, we demonstrate the efficiency of a good order of operations that minimizes the need for additional extract instructions compared to the chaotic order on the right. An *Extract* operation is used to select some elements and/or permuting elements. A merge operation is used to select elements from two vectors and store them in a single vector.

the algorithm fixes the position of the operations to avoid an extract. Finally, it places operations that require extractions in free positions, ensuring the most efficient ordering to minimize extractions.

#### 4.7 Prospecting for the best configuration using a greedy strategy

In the previous sections, we introduced various strategies for group partitioning, element ordering, and optimization. However, some of these transformations are exclusive and cannot be used jointly, such as choosing between clustering and partitioning algorithms for operation group splitting. Similarly, only one of the split configurations of the loads/stores can be used. In addition, not all kernels benefit from reduction transformations, adding to the difficulty of predicting the best approach. To meet this challenge, we propose to test all the strategies with a greedy algorithm and select the one that produces the graph with the least number of instructions. We provide the final vector graph we obtain for *KA* and *KB* in Figure 9.

In cases where a kernel is complex, exhaustive testing of all transformation configurations may be impractical and time-consuming. However, users can guide our tool and explicitly configure the transformations. This option allows them to selectively explore the search space and save time. Determining the optimal configuration depends on the user's understanding of the problem and the specific characteristics of the kernel, such as potential reductions, contiguous load accesses, and the need for advanced group partitioning techniques. By considering these factors, users can effectively navigate the transformation options and improve the vectorization process. In summary, the greedy selection algorithm can be useful to further assist in identifying the most efficient transformation configuration.

#### 4.8 Backend

Our backend takes as input the graph of vector instructions and generates a C++ program by converting each instruction into an intrinsic function call. The conversion is straightforward, and no low-level optimization is performed at this stage. However, because we fully unroll and inline the kernels we can potentially obtain a significant code portion which can put pressure on the registers,

**Algorithm 2:** Set the order of operations in a group by minimizing the extracts

---

```

1 dependent_sources ← ∅ ;
  // Sources with different positions are dependent, fixing one implies extract for the other
2 for operation in in_operations_to_reorder do
3   if operation.src1.position ≠ operation.src2.position then
4     dependent_sources[op.src1].insert(operation.src2);
5     dependent_sources[op.src2].insert(operation.src1);
  // Operations with the same source position are dependent, fixing one implies extract for the
  other
6 for src1 in dependent_sources do
7   for src2 in dependent_sources do
8     if src1 and src2 use the same positions for different operations then
9       dependent_sources[src1].insert(src2);
10      dependent_sources[src2].insert(src1);
  // Sort the sources by number of dependencies
11 sort(dependent_sources);
12 unfixed_operations ← in_operations_to_reorder;
13 positions_used ← ∅ ;
14 ordered_operations_positions ← ∅ ;
15 for src in dependent_sources do
16   if there is an element in src used by more than one operation then
17     break ;
18   if there is an operation using src for both operands (sources) then
19     break ;
20   if src.position ∈ positions_used then
21     break ;
  // Fix the position to avoid an extract
22 for op in src.operations do
23   if src == op.src1 then
24     ordered_operations_positions[op].insert(op.src1.position);
25   else if src == op.src2 then
26     ordered_operations_positions[op].insert(op.src2.position);
27   positions_used.add(ordered_operations_positions[op]) ;
28   unfixed_operations.remove(op) ;
  // Put operations that will need an Extract anyway in the vacant positions
29 while unfixed_operations ≠ ∅ do
30   op ← unfixed_operations.pop() ;
31   positions_used.add(op.position) ;
32   ordered_operations_positions[op].insert(op.position) ;

```

---

leading to register spilling. Therefore, to help the compiler that will compile the generated C++, we propose a reordering algorithm that aims to reduce the save/restore of intermediate variables.

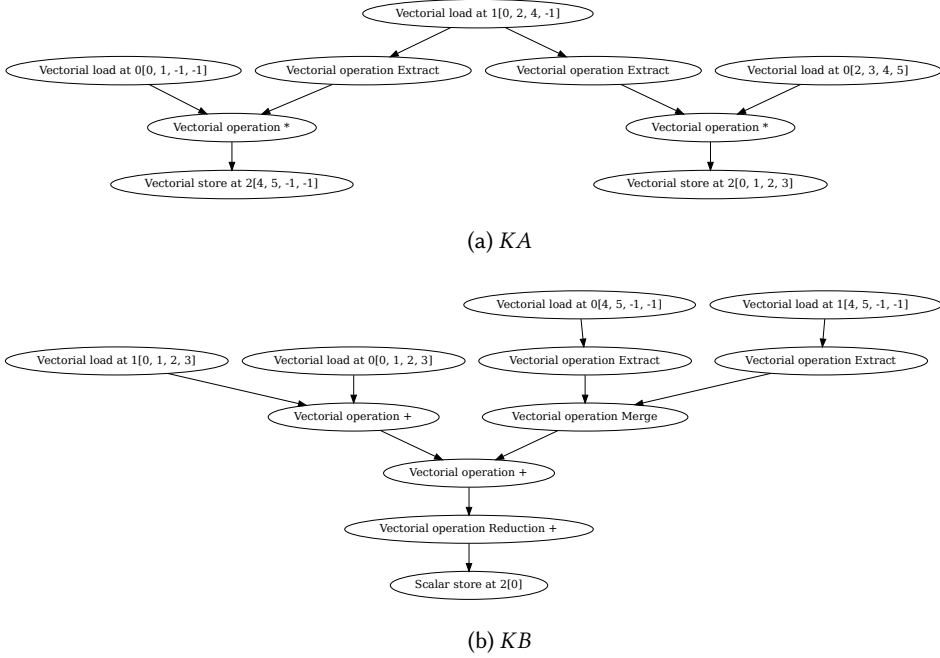


Fig. 9. Graphs of vector instructions for *KA* and *KB* for kernel size equals 6 and  $VEC\_SIZE = 4$ .

To this end, we propose Algorithm 3. It is a two-step algorithm.

---

**Algorithm 3:** Schedule a list of instructions  $l$ .

---

```

1 instructions  $\leftarrow \emptyset$ ;
2 ready_list  $\leftarrow$  roots( $l$ );
3 inverse_depth  $\leftarrow$  distance_from_leaves( $l$ );
4 while ready_list is not empty do
5   costs  $\leftarrow$  compute_costs(ready_list);
6   // Sort the instructions using their costs first and their inverse_depth if tie
7   ready_list  $\leftarrow$  sort(ready_list, costs, inverse_depth);
8   next_i  $\leftarrow$  ready_list.front();
9   instructions.insert(next_i);
10  ready_list.pop_front();
11  ready_list  $\leftarrow$  manage_dependencies(next_i);
12 return instructions;

```

---

In the first step, we find disjoint parts in the instruction list, i.e. parts of the graph that are not connected. Each of these parts is then treated separately in the second step. Our second step is to iterate over the graph as if it were a graph of tasks. We maintain a list of ready tasks (the instructions that can be computed), select the task to be computed next, and then release the dependencies, with the possibility of moving new tasks to the list of ready tasks. This approach

offers several advantages. It has low complexity and does not require managing the correctness of moving instructions before or after the instructions on which they depend (it prevents generating cycles). In addition, the core part lies in the selection of the next task among those in the ready list.

Our strategy is to sort the list based on a register benefit and the depth to the leaves of the graph. We present in the Algorithm 4 the computation of the cost of scheduling an instruction as the next one. The benefit is based on the number of registers that will be released if the instruction is computed. If we consider that there are no unused variables, a load or an operation has a cost of 1 because the result of the instruction has to be stored somewhere. Then, for each instruction, we iterate over its predecessors (input) and see what will be the gain of computing it. For this purpose, we do the sum of the average of the successors of the predecessors. We give an example in Figure 10. We use the longest distance to the leaves to sort the instructions only when the benefit is equal between multiple tasks. Consequently, our algorithm has a local view of the graph and focuses on a minimal local.

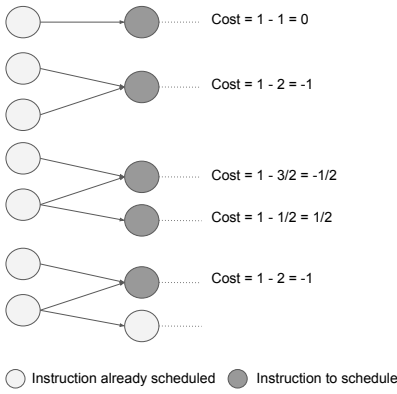


Fig. 10. Example of costs to schedule the instructions.

---

**Algorithm 4:** Compute the cost of scheduling instruction  $i$  next.

---

```

1 cost ← 0;
2 if  $i$  has successors then
   // We need a register to store the
   // result
3   cost += 1;
4 for  $p$  in  $i$ .predecessors do
   // Considered  $p$  is done already
5   for  $sp$  in  $p$ .successors do
6     if  $sp$  is not done then
7       counter += 1;
8   cost -= 1/counter;
9 return cost;
```

---

## 5 PERFORMANCE STUDY

### 5.1 Configurations

We evaluate our tool on two platforms:

- INTEL-AVX512: is an Intel Xeon Skylake Gold 6240 with 2x 18 cores at 2.6GHz and 512-bit AVX, i.e. a vector can contain eight double floating-point values. The node has 192 GB memory and each core has 64KB private L1 cache, 1MB private L2 cache and 1.375MB private L3 cache. The operating system is CentOS Linux release 7.6.1810 (Core). We use the GNU compiler 10.2.0, Clang the LLVM-based compiler 15.0.1 and icpx the Intel compiler 2022.0.0.
- ARM-SVE: is an ARMv8.2 A64FX - Fujitsu with 48 cores at 1.8 GHz and 512-bit SVE, i.e. a vector can contain eight double floating-point values. The node has 32 GB HBM2 memory arranged in four core memory groups (CMGs) with 12 cores and 8GB each, 64KB private L1 cache, and 8MB shared L2 cache per CMG. The operating system is Red Hat 8.3.1-5. We use the GNU compiler 10.3.0 (20210408).

We compile both the scalar (original programs) and the vectorized (output of Autovesk) with the optimization flags `-march=native -mtune=native -O3 -ffast-math`. The executions are pinned to a single core using `taskset`.



## 5.2 Test cases

We use 10 custom computational kernels (Set-CK) and 4 common numerical kernels (Set-NK) to evaluate Autovesk's vectorization performance.

The Set-CK kernels are specifically designed to cover a wide range of patterns. They include kernels with scalar input/output (denoted 1) and those with arrays (denoted  $N$ ). The access patterns to the elements of the arrays vary and can be either contiguous, random or shifted (circular access). These kernels are in the form of for loops on data arrays. They represent a variety of scenarios, including linear contiguous access, irregular access, and circular access. Each of the 10 kernels in the set consists of two inputs and one output. Some of these kernels are expected to be well vectorized by modern compilers. The Set-CK kernels are:

- $(N,N) \rightarrow N$ :  $dest[i] = op(src0[i], src1[i]), \forall i \in [O, N[$ . It is similar to Blas *axpy*.
- $(N,N) \rightarrow 1$ :  $dest+ = op(src0[i], src1[i]), \forall i \in [O, N[$ .  
This kernel includes KB and is similar to a dot product.
- $(N,1) \rightarrow N$ :  $dest[i] = op(src0[i], src1), \forall i \in [O, N[$
- $(N,1) \rightarrow 1$ :  $dest+ = op(src0[i], src1), \forall i \in [O, N[$
- $(r(N),N) \rightarrow N$ :  $dest[i] = op(src0[r(i)], src1[i]), \forall i \in [O, N[$
- $(N,N) \rightarrow r(N)$ :  $dest[r(i)]+ = op(src0[i], src1[i]), \forall i \in [O, N[$
- $(r(N),N) \rightarrow 1$ :  $dest+ = op(src0[r(i)], src1[i]), \forall i \in [O, N[$
- $(r(N),1) \rightarrow N$ :  $dest[i] = op(src0[r(i)], src1), \forall i \in [O, N[$
- $(r(N),1) \rightarrow 1$ :  $dest+ = op(src0[r(i)], src1), \forall i \in [O, N[$
- $(s(N),s(N)) \rightarrow N$ :  $dest[i] = op(src0[s(i)], src1[s(i)], \forall i \in [O, N[$ . This kernel includes KA.

The shift function  $s(x)$  is defined as

$$s(x) = (x + 2) \pmod{N}. \quad (2)$$

The random access function  $r(x)$  is defined as

$$r(x) = (x \text{ XOR } 0x55555555) \pmod{N}. \quad (3)$$

A binary operation  $op$  is either a sum or a multiplication.

We evaluate each kernel from size equal to 4 to 128, and an increasing step equal to 4. An evaluation consists of executing a kernel on 21 distinct arrays 10000 times. Consequently, we use at most  $21 \times 3$  arrays of 128 double floating point values, which takes 63KB, such that the data fits into the L1 cache for both hardware configurations.

The kernels from Set-NK come from real applications:

- *bcucof* (size 4): *bcucof* routine [27] computes a table for bi-cubic interpolation. The bi-cubic algorithm is often used to scale images and videos for display.
- *bcucofx2f*: Two consecutive calls to *bcucof* (size 4) on different data that are vectorized together.
- *weight* (size 7): *weight* routine [27] computes differentiation matrices for pseudo-spectral collocation, which are essential in spectral methods. Spectral methods are a powerful tool widely used for solving partial differential equations (PDEs) due to their high accuracy and efficiency.
- *convolution* (sizes 8 and 16) Discrete convolution is a mathematical operation that combines two discrete functions  $f$  and  $g$  to produce a new function  $f * g$  representing their combined effect. It is commonly used for filtering, smoothing and feature detection in various fields including audio and image processing.

For all the test cases, the data is initialized before calling the kernels, so it is already in the cache before the first execution. When showing the speedup, we obtain it by comparing the scalar version automatically vectorized vs. the version vectorized by Autovesk, both compiled with the same compiler.

### 5.3 Results

*Set-CK.* Our performance study compared the automatically vectorized C++ code generated by Autovesk with the automatic vectorization techniques of scalar kernels produced by the GCC compiler, the Clang LLVM-based compiler, and the Intel icpx compiler. Figure 11 shows the execution times of the 10 kernels with different problem sizes for both the INTEL AVX512 and ARM-SVE configurations. The comparison is made between the vectorized code generated by Autovesk and the automatic vectorization of the GCC compiler on scalar codes. The results show that vectorized kernels provide a noticeable speedup over scalar kernels, as indicated by the speedup shown at some points. In Figure 12, we provide a detailed breakdown of the number and types of graph nodes for the different kernels and problem sizes in our study. There are scalar graph nodes, including loads, stores and operations, and vector graph nodes for the generated vectorized code, including loads, stores, operations and data transformations. Importantly, the data transformation operations exist only for the vectorized kernels, as they apply to vectors. Although the number of resulting binary instructions may differ, it is highly correlated with the number of graph nodes shown. These results provide insight into the complexity of the vectorization process and the types of operations involved in generating efficient vectorized code from scalar code.

From the execution times, we observe that our approach provides a significant speedup for all kernels on both configurations, except for the  $(N, 1) \rightarrow N$  and  $(N, N) \rightarrow N$  kernels. For these kernels, the compiler is able to vectorize and achieve execution times similar to our approach. The kernels  $(N, 1) \rightarrow 1$  and  $(N, N) \rightarrow 1$  are easily vectorized, but require a reduction. We can see from Figures 11a and 11c, that our approach is faster for all sizes on ARM-SVE and after a fairly large size on INTEL-AVX512. When using random access ( $r(N)$ ) or a shift ( $s(N)$ ) our method can provide a significant speedup of 12. The execution times can vary, and we can understand this behavior by looking at Figure 12. For instance, for the kernel  $(r(N), 1) \rightarrow 1$ , execution time Figure 11f and operations Figure 12f, we can see that the data transformation operations vary significantly depending on the size. This is because we do not always use a multiple of 8 (the length of the SIMD vector), which leads to different best instruction graphs. This effect is visible in Figures 12a, 12g and 12c but with less impact on performance. As expected for the kernel  $(N, N) \rightarrow N$ , Figure 12d, there are no data transformation operations. Among the strategies to fix the order of the vector's elements, 76% of the best configurations were obtained by leaving the elements in their original order, which is not surprising due to the types of kernels we tested. Then, 16% were obtained with the partitioning strategy and 8% with the clustering strategy.

Figure 13 shows the speedups achieved by Autovesk compared to the Intel icpx and Clang compilers for the 10 kernels selected in our study. To evaluate the performance, we ran each kernel as we did for the comparison with GCC, i.e., with different problem sizes, but instead of showing all the details, we calculated the average speedup along with the minimum and maximum variation over the automatic vectorization techniques of the compilers. The evaluation showed that the performance of the vectorized kernels using Autovesk is better than the compiler versions for most kernels. For the cases " $(N, N) \rightarrow N$ " and " $(N, 1) \rightarrow N$ " using Intel icpx, see Figure 13b, we obtain similar performance, which we expect since the data accesses are contiguous and linear. However, Clang did not deliver the same performance, see Figure 13a.

The average time to generate vectorized code for all kernels and sizes is 4.12 seconds, with a minimum of 0.001 seconds and a maximum of 179.258 seconds. However, this phase is not fully optimized, so there is room for improvement. We expect that strategies such as a branch and cut technique could improve the efficiency of the process by pruning the research of the best coefficients.

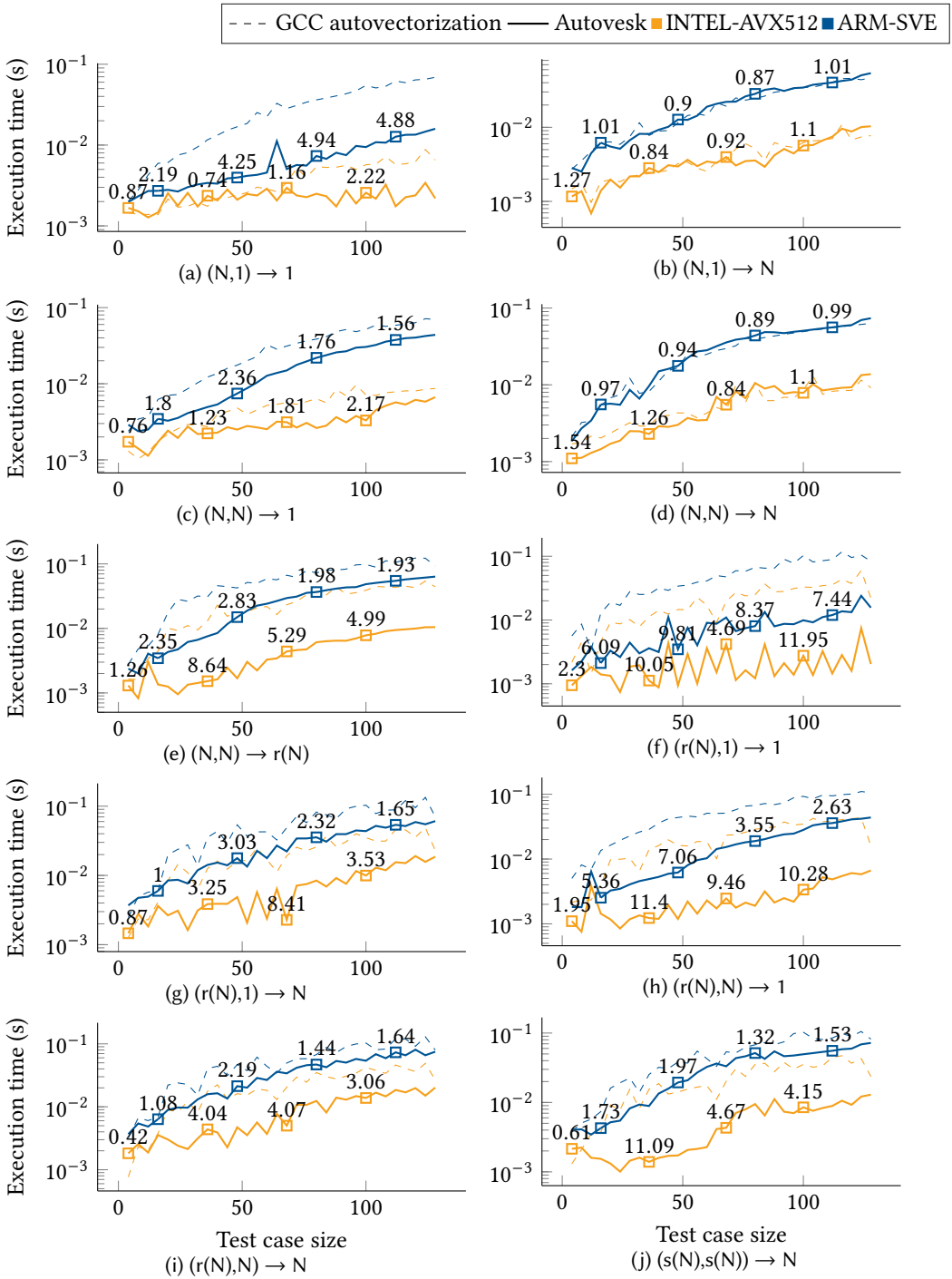


Fig. 11. Execution times for the different kernels and different problem sizes for the INTEL-AVX512 and ARM-SVE configurations. The speedup of the vectorized kernels by Autovesk against the automatic vectorization techniques of GCC compiler on scalar kernels is shown for some points.

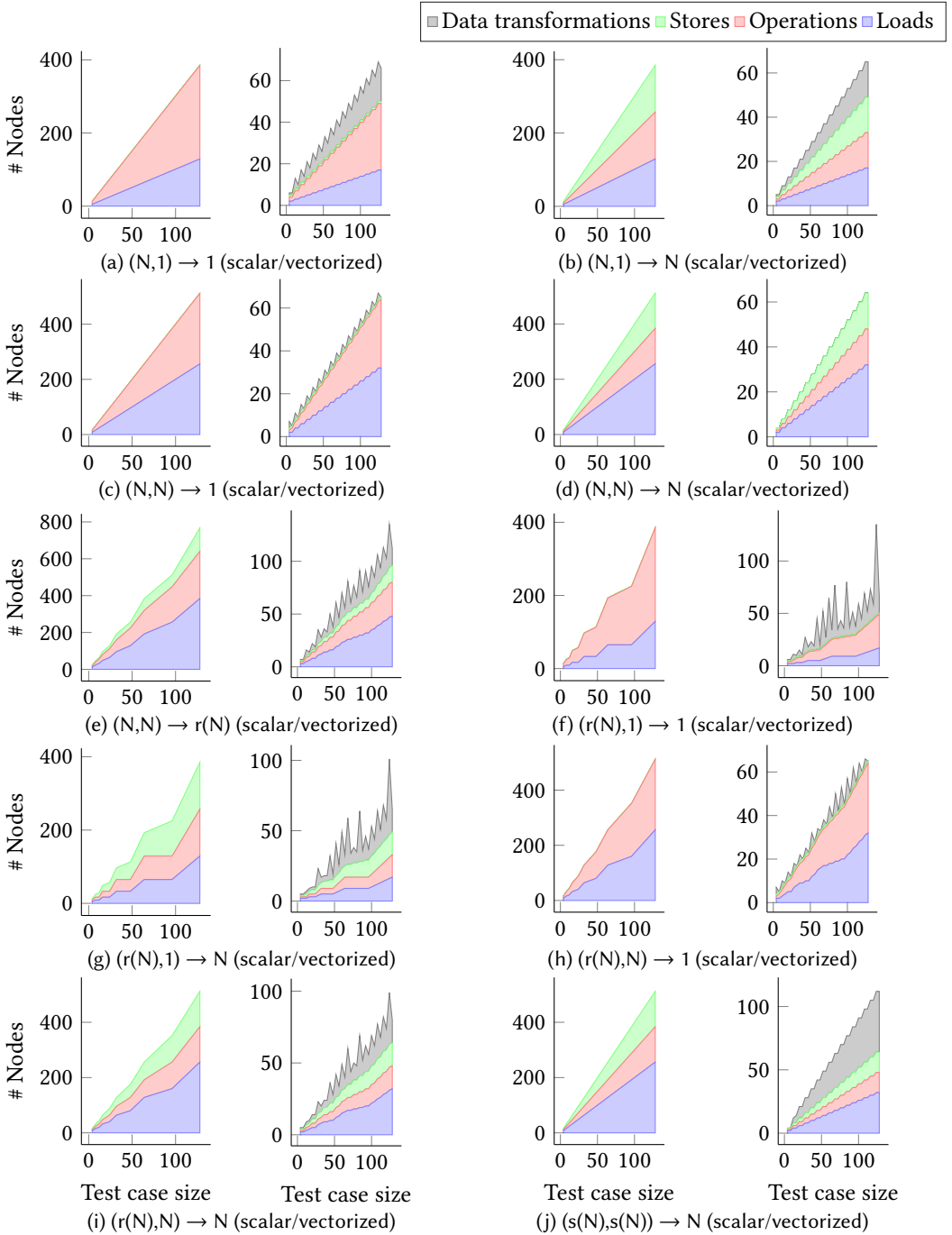


Fig. 12. Number and types of graph nodes for the different kernels and different problem sizes. The data transformation operations only exist for the vectorized kernels because they apply to vectors. The number of resulting binary instructions can differ but will be highly correlated to the numbers shown. A side-by-side comparison between the results of the scalar source code (left side) and the vectorized generated code (right side).

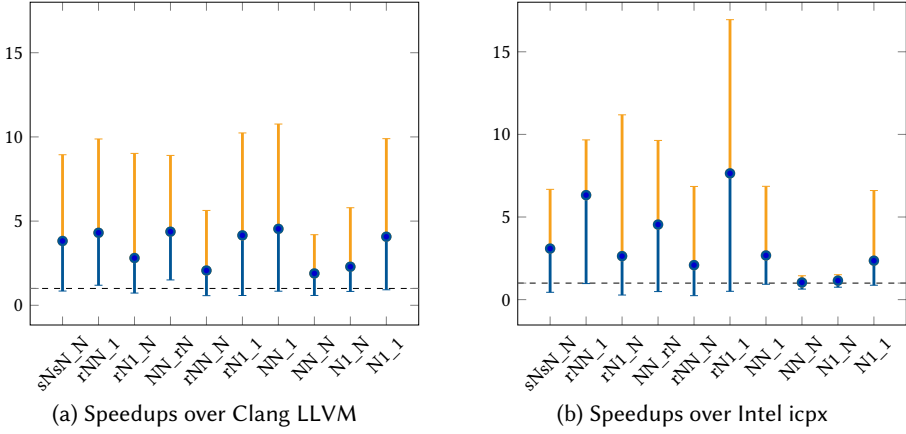


Fig. 13. Comparison of Autovesk’s automatic vectorization speedsups against the Clang LLVM-based and Intel icpx compilers on 10 selected kernels. Each kernel was executed with different problem sizes. The minimum, average, and maximum speedsups over the compilers’ auto-vectorization techniques are shown.

*Set-NK*. Figure 14 provides the results for the numerical kernels.

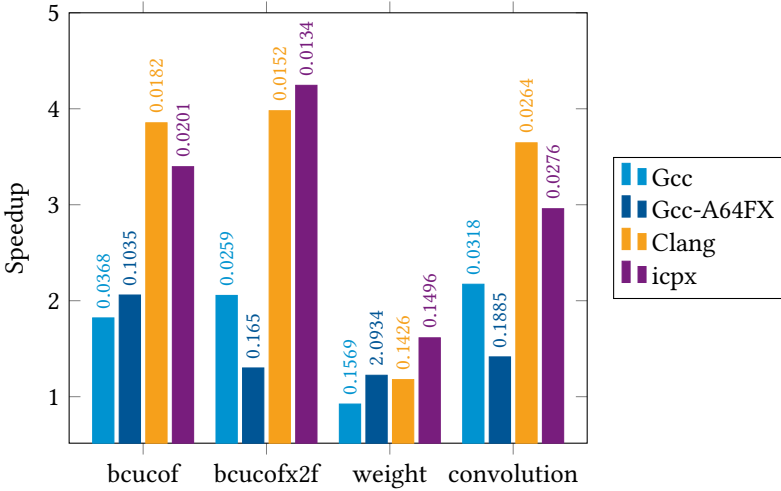


Fig. 14. Comparison of Autovesk’s automatic vectorization speedup against the GNU compiler (GCC) on x86 architecture and A64FX 64-bit ARM architecture, Clang LLVM-based compiler and the Intel (icpx) compiler for 4 different numerical kernels. We provide the execution times of the Autovesk versions above each bar.

Our study highlights the relative advantages of Autovesk over modern compilers in optimizing the numerical computations presented. In particular, Autovesk achieves significant speedsups over Clang and Intel compilers, exceeding the speedsups achieved over GCC. For the "bcucof" kernel, Autovesk runs 1.8 times faster than GCC. It also outperforms Clang LLVM by 3.8 times with an execution time of 0.0182. Vectorizing "bcucof" presents challenges due to non-contiguous index operations within the loop. However, Autovesk overcomes this limitation by efficiently transforming the input arrays into registers with minimal overhead, thereby enabling operation factorization

and facilitating effective vectorization. Autovesk achieves a remarkable 2x speedup over GCC for the "bcucofx2f" kernel. Compared to Intel icpx, Autovesk achieves a significant speedup of 4.2x, reducing the execution time to 0.0134. Autovesk performs well on the "weight" kernel and excels on the "convolution" kernel with speedups of 2.1x over GCC, 3.6x over LLVM, and 2.9x over Intel icpx, reducing the execution time to 0.0276. These consistent and significant performance improvements highlight the effectiveness of Autovesk in optimizing numerical kernels. Further investigation is required to explore its potential in broader application domains.

## 6 STACK/REGISTER EXCHANGE MINIMIZATION

To alleviate the pressure on the registers and minimize stack/register exchange, we proposed a reordering algorithm for the generated C++ code in Section 4.8.

### 6.1 Test cases

To evaluate the effectiveness of our proposed reordering algorithm, we generated random instructions using our test case generator, PredX. This generator creates random instructions that have dependencies between variables. The  $X$  in PredX represents the maximum number of predecessors for a given variable. To generate the test cases, we start with a single variable and link it to previous variables with a jump between 1 and 10, meaning that the first 9 variables could have zero predecessors. A variable with zero predecessors is considered a load and a variable with zero successors is considered a store. We generated AVX512 code, where each variable is an AVX512 vector, and simply added the input. This allowed us to test the performance of our reordering algorithm on randomly generated code of varying complexity. Our test case generator is referred to as PredX, where  $X$  means that a variable is computed using from 1 to  $X$  variables (i.e. in the dependency graph, a variable can have up to  $X$  predecessors).

### 6.2 Results

Using our test case generator PredX, we evaluated the effectiveness of our proposed reordering algorithm by generating random instructions for two different test case configurations: Pred4 and Pred10, while varying the problem sizes. We provide the results in Figure 15, showing the number of stack accesses (push, pop or direct accesses) with and without the reordering algorithm. We can observe that reordering the instructions with our strategy always provides a benefit. More precisely, for Pred4, the compiler can avoid using the stack for all problem sizes, but will spin 68 registers with the original order. For Pred10, the gain is about 15%.

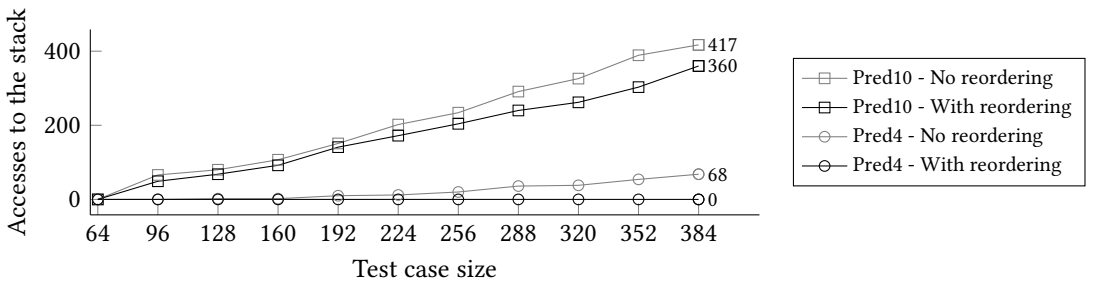


Fig. 15. Number of stack accesses (push, pop or direct accesses) for different test case sizes. PredX refers to a test case where a new variable is constructed with up to  $X$  other variables as input.

## 7 LIMITATIONS AND FUTURE WORKS

Our research has focused on automatically vectorizing unstructured static kernels with irregular data access patterns, but there are several limitations and room for future improvement. One area we intend to address is extending the applicability of Autovesk to cases where non-static loops can be expressed as repetitions of static ones. Indeed, non-static kernels can be divided into those that can be described by the polyhedral model, for which our approach is not beneficial and those that cannot. For the latter, there are non-static kernels that require alternative optimization methods, and those that can be viewed as repetitions of static kernels, where we aim to apply our method. Although our tool automatically generates vectorized code, at this stage, it still requires the user to provide input code in a specific format, since we use C++ templates to extract the graph of instructions. To eliminate user intervention and extend the range of code that can be automatically vectorized, we plan to integrate Autovesk's transformations into an existing compiler. Alignment is not handled in the current implementation of Autovesk. Integrating our techniques into a compiler offers a potential way to address alignment issues in future work. In addition, we can investigate incorporating a cost model for each strategy in the graph transformations. By considering the potential benefits and overheads of vectorization, informed decisions can be made to avoid unnecessary vectorization and focus on cases where it will provide significant performance gains. These directions improve the usability and effectiveness of Autovesk in various applications.

## 8 CONCLUSION

We introduced Autovesk, an automatic vectorization tool designed for complex computational kernels. We presented our strategy that relies on heuristic-based algorithms to avoid paying the price of finding an optimal solution. Our method generates several solutions and returns the one with the least number of operations. To assess the vectorization performance of Autovesk, we performed a comparative evaluation against three leading compilers: GCC, LLVM, and Intel, using a set of proposed kernels, including both custom and real-world numerical kernels. We demonstrate that Autovesk can provide significant speedups on several kernels. It remains competitive even in cases where general-purpose compilers can vectorize. Furthermore, Autovesk includes a procedure to reorder the instructions to reduce register spilling. While Autovesk shows promising results for the automatic vectorization of unstructured static kernels, there is still room for improvement and extension. Our ongoing research will continue to explore these possibilities.

## ACKNOWLEDGMENTS

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## A PARTITIONING STRATEGY

---

**Algorithm 5:** Converting a group into a set of  $V$  subgroups, where each group has at most  $VEC\_SIZE$  elements.

---

```

// Given a list of elements  $e$  and matrix score  $d$ 
// Start with a partition containing all elements
1 wip_partitions.push(new_partition(e));
2 final_partitions  $\leftarrow \emptyset$ ;
3 while |final_partitions|  $\neq V$  do
4    $p \leftarrow$  wip_partitions.pop();
5   if  $|p| \leq VEC\_SIZE$  then
6     final_partitions.insert( $p$ );
7     continue;
// We compute the desired partition sizes
8 vecs_in_p  $\leftarrow (|p| + VEC\_SIZE - 1)/VEC\_SIZE$ ;
9 margin  $\leftarrow$  vecs_in_p  $\times VEC\_SIZE - |p|$ ;
10 size_max_p1  $\leftarrow (|p|/2) \times VEC\_SIZE$ ;
11 size_max_p2  $\leftarrow (|p|/2) \times VEC\_SIZE$ ;
12 size_min_p1  $\leftarrow$  size_max_p1 - margin;
13 size_min_p2  $\leftarrow$  size_max_p2 - margin;
// Find the elements in  $p$  with the lowest
  score
14 ( $i, j$ )  $\leftarrow$  find_min_score( $p, d$ );
15 sub_p1  $\leftarrow i$ ;
16 sub_p2  $\leftarrow j$ ;
17 p.remove( $i, j$ );
18 while  $|p| \neq 0$  do
19   if  $|sub\_p1| == size\_max\_p1$  then
20     sub_p2.insert( $p.pop()$ );
21   else if  $|sub\_p2| == size\_max\_p2$  then
22     sub_p1.insert( $p.pop()$ );
23   else
24     // Find the element  $n$  that has the
25     // highest accumulated score either
26     // with sub_p1 or sub_p2
27     [ $n, score1, score2$ ]  $\leftarrow$  find_highest_score( $p,$ 
28     sub_p1, sub_p2);
29     p.remove( $n$ );
30     if  $score1 \geq score2$  OR ( $score1 == score2$ 
31     AND
32     size_max_p1 -  $|p1| \geq size\_max\_p2 - |p2|$ )
33     then
34       sub_p1.insert( $n$ );
35     else
36       sub_p2.insert( $p.pop()$ );
37   wip_partition.insert(sub_p1, sub_p2);

```

---

## B CLUSTERING STRATEGY

---

**Algorithm 6:** Converting a group into a set of  $V$  subgroups, where each group has at most  $VEC\_SIZE$  elements.

---

```

// Given a list of elements  $e$  and
  matrix score  $d$ 
// We initiate the subgroups
1 subgroups[V]  $\leftarrow \emptyset$ ;
2 ( $i, j$ )  $\leftarrow$  find_min( $d$ );
3  $e \leftarrow$  remove( $e, i, j$ );
4 subgroup[0].add( $i$ );
5 subgroup[1].add( $j$ );
6 for  $v$  from 2 to  $V$  do
7   worst_idx  $\leftarrow 0$ ;
8   worst_score  $\leftarrow +\text{inf}$ ;
9   for  $idx$  in  $e$  do
10    score  $\leftarrow$ 
11     $\sum_{i=0}^v d(\text{subgroup}[i][0], idx)$ ;
12    if  $score < worst\_score$  then
13      score = worst_score;
14      worst_idx =  $idx$ ;
15    $e \leftarrow$  remove( $e, worst\_idx$ );
16   subgroup[ $v$ ].add(worst_idx);
17 while  $e$  is not empty do
18   best_idx  $\leftarrow 0$ ;
19   best_subgroup  $\leftarrow 0$ ;
20   best_score  $\leftarrow -\text{inf}$ ;
21   for  $v$  from 0 to  $V$  do
22     for  $idx$  in  $e$  do
23       score  $\leftarrow$ 
24        $\sum_{i=0}^v d(\text{subgroup}[i][:], idx)$ ;
25       if  $score > best\_score$  then
26         score = best_score;
27         best_idx =  $idx$ ;
28         best_subgroup =  $v$ ;
29    $e \leftarrow$  remove( $e, best\_idx$ );
30   subgroup[best_subgroup].add(best_idx);

```

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