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Decentralized in-order execution of a sequential task-based code for shared-memory architectures

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**Abstract**— The hardware complexity of modern machines makes the design of adequate programming models crucial for jointly ensuring performance, portability, and productivity in high-performance computing (HPC). Sequential task-based programming models paired with advanced runtime systems allow the programmer to write a sequential algorithm independently of the hardware architecture in a productive and portable manner, and let a third-party software layer—the runtime system—deal with the burden of scheduling a correct, parallel execution of that algorithm to ensure performance. Many HPC algorithms have successfully been implemented following this paradigm, as a testimony of its effectiveness.

Developing algorithms that specifically require fine-grained tasks along this model is still considered prohibitive, however, due to per-task management overhead [1], forcing the programmer to resort to a less abstract, and hence more complex “task+X” model. We thus investigate the possibility to offer a tailored execution model, trading dynamic mapping for efficiency by using a decentralized, conservative in-order execution of the task flow, while preserving the benefits of relying on the sequential task-based programming model. We propose a formal specification of the execution model as well as a prototype implementation, which we assess with synthetic workloads. The results show that under the condition of a proper task mapping supplied by the programmer, our proposal enables a cost-effective parallel execution of algorithms with fine-grained tasks expressed in the STF programming model. There are, of runtimes, including OpenMP since revision 4.0 (through the task construct and depend clause inspired from OmpSs), StarPU with the default configuration and PaRSEC through its dynamic task discovery (DTD) mode.

While STF is therefore arguably a popular programming model in HPC, the per-task management overhead incurred by such runtime systems makes it prohibitive in practice to execute fine-grained tasks, as highlighted in a recent study of their performance as a function of task sizes [1]. The study estimates that on current architectures, the minimal duration of individual tasks should be on the order of 100μs for the approach to be profitable. Unfortunately, some important classes of HPC applications actually do involve tasks of small granularity. A typical example is the High Performance Linpack Benchmark [9] (HPL) used for establishing the TOP500 [10] supercomputer ranking. The core of the HPL algorithm is a LU matrix factorization with partial pivoting: while most operations are performed at coarse granularity, the pivoting itself requires fine-grained operations that can not be efficiently executed as tasks with such runtime systems.

Most task-based runtime systems assessed in [1] support the STF programming model while internally using various strategies for their execution model. In this paper, we further formalize the important but often implicit difference between the programming model and execution model. We highlight that most runtime systems supporting the STF programming model on shared-memory machines most often explicitly or implicitly assume a centralized, out-of-order execution model (the scheduling work possibly being decentralized, but the consistency management work remaining centralized). While this execution model may be an excellent choice for dealing with moderate or coarse grain tasks, on the contrary, this paper proposes a new lightweight execution model relying on the principles of decentralized dependency management and in-order execution, to drastically reduce per-task management overhead. We introduce a formal specification of the proposed execution model as well as a prototype implementation (for shared-memory, homogeneous multicore architectures), which we assess with synthetic workloads. The results are promising, showing that under the condition of a proper task mapping supplied by the programmer, our proposal enables a cost-effective parallel execution of algorithms with fine-grained tasks expressed in the STF programming model. There are,
however, two limitations: first the programming model is slightly modified by need to provide a mapping function, and second the absence of dynamic re-ordering leads to less efficient pipelining in the presence of coarse tasks. Even though we compare our model with the established centralized out-of-order paradigm our intent is not to replace the general-purpose runtimes cited earlier, but to demonstrate superior efficiency on some classes of computation involving fine granularity, and eventually enable those general purpose runtimes to delegate relevant computations to an embedded low-overhead runtime, as the one described in this paper.

Our original contributions include the execution model, its formal specification (as well as a specification of the STF programming model that the execution model must satisfy), and an analysis of the performance of a prototype implementation of that model on different synthetic benchmarks.

The paper is organized as follows. Section II presents some background on the STF programming model (section II-A), typical execution models (section II-B) employed in the HPC literature for supporting it on shared-memory machines, and our methodology to assess the efficiency of execution models (section II-C). Section III introduces our proposal for a lightweight execution model implemented in our Run-in-Order (RIO) runtime system prototype, to execute sequential flows of fine-grained tasks. Section IV presents the methodology we have employed to define the formal specification of both the STF model and the proposed execution model. Section V reports on experiments we conducted to assess the proposed approach. Section VI concludes this paper.

II. BACKGROUND

Throughout this paper we make a clear distinction between the **programming model** and the **execution model**. The programming model defines the semantic of a program, it gives guarantees about the behavior of the program but does not specify how it is executed. Defining the precise execution of a program is the role of the execution model. It must conform to the high level semantics described by the programming model but is free to choose the underlying implementation. Decoupling the programming and execution models is important when discussing performance, because even though the programming model imposes constraints on the execution, different implementations can result in very different performance profiles.

A. The Sequential Task Flow programming model

In the STF model the programmer writes its program as a sequence of tasks to be executed, that we call the task flow. A task is a pure function (e.g. without side effects) that can operate on some data objects managed by the runtime system. For each such data object, the task declares an access mode: read-only, write-only or read-write. The STF model gives the sequential consistency guarantee that the result of a valid parallel execution in this model will be the same as the result of a sequential execution of the tasks in the order given by the task flow.

The appeal of STF comes from the implicit management of data dependencies it offers: such dependencies are deduced from the access order in the task flow and the respective data access modes declared by the tasks. Sequential consistency is guaranteed by the runtime by ensuring that each read access happens after all previous write operations and that each write access happens after all previous read and write operations. Dependencies being implicit, writing a STF algorithm is similar to writing the sequential version of that algorithm. As a result, STF applications avoid common pitfalls of concurrent programs such as deadlocks, and data races.

B. The Execution Model

While the programming model describes the semantic of the —STF in our case— programs, the execution details within the boundaries of these semantic constraints are left for the runtime to decide. The simplest possible execution model for STF would be to execute the tasks sequentially in the order given by the task flow. While semantically correct, this execution model would make a poor usage of a parallel computer. More efficient execution models have thus been developed and are gaining momentum as an effective way to write high performance applications for supercomputers.

Multiple runtimes are compliant with the STF programming model: StarPU [3], PaRSEC [4] with Dynamic Tasks Discovery, Quark [11], SuperGlue [5], OmpSs [6] and OpenMP starting with version 4.0 [2] and the introduction of the task construct and depend clause. Within a hardware node, most STF-compliant runtimes use very similar execution models that we describe as **centralized** and **out-of-order** (OoO). We designate them as centralized because they rely on a master-worker model (especially on shared-memory architectures), in which a master thread unrolls the task flow to discover the tasks and dispatch them to a pool of workers (illustrated in Figure 1). In addition, the master thread (through scheduling) and/or the workers (through work stealing) can re-order the...
tasks to minimize idleness as long as sequential consistency is maintained. The execution is thus said to be OoO.

Centralized OoO runtimes are indeed effective. StarPU for instance is consistently achieving performance within a few percent of the best performing (possibly non STF) implementation on the Task Bench runtime survey [1]. OoO runtimes are able to make good scheduling decisions at runtime by taking into account parameters such as data locality, expected task execution time and upcoming tasks, while also dynamically balancing the workload through work stealing techniques. Those features come at the cost of higher per-task overhead, as highlighted by the Task Bench survey, which makes execution of fine-grained tasks intractable.

C. Decomposing runtime efficiency

Figure 2 shows the evolution of the execution time against the dimensions of the sub-matrices, for a matrix multiplication. It uses a state-of-the-art general matrix multiplication kernel for double precision values (DGEMM) from the Intel MKL library, together with StarPU, on a dual socket 12-core Intel Xeon E5-2680 v3 processor [12]. It illustrates the impact of granularity on the execution time: finer grained tasks lead to a longer execution. However, Figure 2 by itself does not explain why the efficiency decreases, which results from a combination of factors. Figure 3 shows the efficiency of the Intel MKL DGEMM routine against the matrix tile sizes when splitting the whole computation into tasks. This experiment makes it clear that the global execution time is not a good measurement of the runtime performance characteristics, since the computation kernel itself looses efficiency with smaller tasks. Matrix multiplication kernels usually exploit hardware caches efficiently on sufficiently large matrices, while dividing the computation into smaller tasks reduces opportunities for cache reuse, which in return degrades the kernel efficiency.

In this paper we investigate the impact of the runtime system on the global computation efficiency, using a methodology inspired by previous works ([13], [8] and [14]) to decompose the global efficiency into a product of efficiencies more easily attributable to specific components and properties of execution models. In the following, we use the notations:

- $t$: execution time of the fastest sequential algorithm;
- $t(g)$: execution time of the sequential algorithm when splitting the problem in tasks of granularity $g$;
- $t_p(g)$: execution time when using a runtime with $p$ threads and tasks of granularity $g$;
- $e$: parallel efficiency [15].

As discussed, the parallel efficiency encapsulates not only the cost of the runtime but also overheads such as the reduced efficiency of tasks’ computation kernels at a given granularity. In our analysis, we thus want to isolate the efficiency of the computation kernel from the efficiency of the runtime itself. To that effect we further refine our notations by introducing the cumulative execution time using a runtime $\tau_p(g) = p \cdot t_p(g)$ and decomposing it into three parts depending on the type of event occurring at a given instant:

- $\tau_{p,t}(g)$: cumulative time spent executing tasks;
- $\tau_{p,i}(g)$: cumulative time spent idle, waiting for a dependence constraint to be resolved, for instance;
- $\tau_{p,r}(g)$: cumulative time spent in the runtime not executing a task nor idle, which corresponds to the management cost of tasks (e.g. memory allocation, scheduling).

The sum of these cumulative times corresponds to the total parallel execution time multiplied by the number of threads: $\tau_p(g) = \tau_{p,t}(g) + \tau_{p,i}(g) + \tau_{p,r}(g)$. This can be viewed as a rectangle of height $p$ and width $t_p$, being covered by events among the above three possible types (processing tasks, idle, internal runtime management).

Using these notations we decompose the parallel efficiency $e$ into a product of four efficiencies: the granularity efficiency $e_g$ representing the efficiency of the computation kernel at a given granularity, the locality efficiency $e_l$ encapsulating the effect of locality in a multi-threaded application, the pipelining efficiency $e_p$ for the ability of the runtime to efficiently pipeline tasks execution, and the runtime efficiency $e_r$ representing the overhead of managing tasks in the runtime. Introducing $t(g)$ the sequential time when operating at
In OoO execution models, tasks can be freely re-ordered as long as sequential consistency holds. A smart OoO scheduler can take advantage of that to yield better computation overlapping and reduce idle time. The gains from OoO scheduling come from the ability to execute ready tasks while other tasks are waiting for a dependency, which can produce efficient execution even if the order of task submissions in the task flow is not optimal. The overhead of OoO execution is due to both the need for good (hence expensive) heuristics and the necessary data structures used to store pending tasks, whose space requirement is linear in the number of tasks.

To handle a high volume of fine-grained tasks, we propose to use an in-order execution model rather than traditional OoO. An in-order execution model removes the need for scheduling heuristics and task storage, drastically reducing the per-task overhead at the cost of a much higher sensitivity to task submission order. The scheduler in OoO models is also responsible for resources allocation, and often aims at maximizing data locality. In our proposed in-order execution model there is no dynamic scheduler; the assignment of tasks to resources must thus be done through other means.

### B. Task mapping

We propose to rely on a static mapping of the tasks to do so. For some classes of computation, including most popular numerical algorithms, there has been extensive research on efficient static scheduling, such as 2d-block cyclic mapping in dense linear algebra [16] or proportional mapping in sparse linear algebra [17], [18], which can be leveraged to write efficient task mapping and discovery order. Static mappings have also been used in a distributed-memory task-based context [7], [19]. Although such mappings have been much more often considered for designing distributed-memory algorithms, nothing prevents one to translate them to the shared-memory case. It is to be noted that in the case the mapping is collected from the application, it also slightly changes the programming model, as an additional information (the mapping) is requested to write the algorithm. However, the automatic computation of static mappings has also been considered [20]. We advocate that, although less convenient than the original STF model relying on dynamic scheduling, the additional constraint of providing (or computing) a task mapping may be viewed as reasonable in HPC where there is already a well established expertise of optimizing mappings in a distributed context. In any case, this is the assumption we assess in this paper.
C. Decentralized task management

Centralized runtimes rely on a master-workers model in which a single thread is responsible for unrolling the task flow and managing dependencies, while delegating task execution to a worker pool. This model makes sense when the task execution time is much greater than the unrolling and management cost, but the master thread can become a bottleneck with smaller tasks. The total execution time \( t_p(g) \) can be modelled, in first approximation, as a function of the time spent in the runtime per task \( t_r \) and the task execution time \( t_s(g) \):

\[
t_{p,\text{centralized}} = \max\left( n\ t_{r,\text{centralized}}, \frac{n\ t_s(g)}{w} \right),
\]

where \( n \) is the number of tasks to execute and \( w \) the number of worker threads. With coarse tasks the application is limited by the speed at which the workers execute the tasks, but at smaller granularity the master thread may become the bottleneck.

We propose to use a decentralized execution model instead: all the threads have symmetric roles, they all unroll the whole task flow, while only executing tasks assigned to them through the mapping function (see section III-B). The model is illustrated in Figure 5. We also present an algorithm for cheap decentralized data synchronization in section III-D. With this model the total execution cost can be modelled as:

\[
t_{p,\text{decentralized}} = n\ t_r + \frac{n\ t_s(g)}{w}
\]

D. Decentralized data synchronization

Without a master thread to coordinate workers, a new protocol is needed to ensure data accesses are properly synchronized and respect the sequential consistency ordering imposed by the STF model. Such a distributed protocol is actually commonly used by task-based runtime systems (including StarPU) on distributed-memory machines \([7], [19]\), where there is typically one master thread per hardware node: each master thread delegates the handling of tasks mapped on the node to the node workers, but the master threads of all the nodes have to coordinate with each other. We adapt this approach into a shared-memory algorithm defining a light-weight protocol for synchronizing data accesses in a decentralized in-order execution model. We present this approach in algorithm \([1]\) which we further introduce in the remaining of this section.

We make the following assumptions:

1. Tasks are numbered in the order in which they appear in the control flow, that number is called the Task ID.
2. All the threads discover the same sequence of tasks, i.e. the tasks have the same ID and dependencies and are delivered in the task flow order for all threads.
3. All the threads have access to a mapping function that deterministically associates a Task ID to a unique thread.
A shared-memory region is managed by a data object, composed of both a thread-local and a shared state. Accesses to the latter must be properly synchronized. To keep pseudocode concise, algorithm 1 supposes there is a single data object. The local state contains two integer values: local.nb_reads_since_write corresponding to the number of read operations encountered by the thread on this shared-memory region (but maybe not yet executed) since the last write, and local.last_registered_write which is the Task ID of the last write operation encountered on this memory region. The shared state also contains two integers: shared.nb_reads_since_write holding the number of reads performed on the shared-memory region since last write, and shared.last_executed_write containing the Task ID of the last write operation performed on the memory region.

Finally we define a set of routines for the data object that manipulates the local and shared states. Each routine exists in two versions: read or write. The appropriate version must be called depending on the access mode requested by the task (lines 4 & 12 in algorithm 1). We replace read or write by op in the following routines (detailed in algorithm 2):

- declare_op: declare an operation in op mode but does not execute it on the current thread. This only requires to modify the local state.
- get_op: return a pointer to the data for use in op mode. This operation might be blocking: it can only return once all dependencies have been resolved, which may require reading the shared state and potentially waiting for other threads.
- terminate_op: declare that an operation in op mode has been executed. This modifies the shared state.

Given these definitions, to synchronize accesses to a shared-memory location through a data object all the threads must iterate over the list of tasks. For each task in which the memory location is involved, the thread calls the mapping function (line 3 in algorithm 1) to get the identifier of the thread responsible for that task. If the thread is assigned to the task it calls get_op (lines 6 & 14) to get access to the memory location, performs the task and then releases the memory location with terminate_op (lines 8 & 16). If the thread is not responsible for the task, it updates its local state by calling the declare_op function (lines 10 & 18).

A read-only operation can be executed if local.last_registered_write is equal to shared.last_executed_write of the data object (algorithm 2 lines 12 & 13), this ensures that all the required writes have been performed on the data. A write operation has to check that local.last_registered_write and shared.last_executed_write are the same and the number of reads since that write in the local and shared nb_reads_since_write variables are equal (algorithm 2, lines 17 to 20). This asserts that all the previous reads and writes have been performed on the data.

A property of algorithm 1 is its low overhead, both in time and space. A data object requires 2 integers in the shared state plus 2 integers per worker for synchronization, independently from the number of tasks. In contrast with centralized execution models, threads progress independently until they block on a dependency. Coupled with very small per-task overhead when the thread is not responsible for executing the task (a single write in private memory per data object for a read operation, two writes in private memory for a write operation), the decentralized model avoids the bottleneck of centralized runtimes’ workers (section III-C) waiting for the master thread to dispatch the tasks.

---

**Algorithm 1: Decentralized Data Synchronization**

1: for all threads do
2:     for all task in TaskFlow do
3:         executor ← mapping(task)
4:     if task has read dependency then
5:         if executor = self then
6:             data ← get_read()  /* data can be used in read mode here */
7:         terminate_read()
8:     else
9:         declare_read()
10:     end if
11: end if
12: if task has write dependency then
13:     if executor = self then
14:         data ← get_write()  /* data can be used in write mode here */
15:     terminate_write(task.id)
16: else
17:     declare_write(task.id)
18: end if
19: end if
20: end for
21: end for
22: end for

---

**Algorithm 2: Decentralized Data Synchronization Routines**

1: function declare_read() do
2:     local.nb_reads_since_write ← local.nb_reads_since_write + 1
3: end function
4: function declare_write(task_id) do
5:     local.nb_reads_since_write ← 0
6:     local.last_registered_write ← task_id
7: end function
8: function get_read() do
9:     wait for local.last_registered_write = shared.last_executed_write
10: end function
11: function get_write() do
12:     wait for local.last_registered_write = shared.last_executed_write
13:     wait for local.nb_reads_since_write = shared.nb_reads_since_write
14: end function
15: function terminate_read() do
16:     shared.nb_reads_since_write ← shared.nb_reads_since_write + 1
17: declare_read()
18: end function
19: function terminate_write(task_id) do
20:     shared.nb_reads_since_write ← 0
21:     shared.last_executed_write ← task_id
22: declare_write(task_id)
23: end function
An extended variant of this algorithm is used for depend-ence management in the centralized, OoO task-based runtime system SuperGlue [5]. It introduces the notion of data versioning [21], where a new version of a piece of data is created upon a write by a task, and lets task dependencies be expressed as references to specific versions of some pieces of data. It enables expressing additional constructs beyond the strict sequential consistency of STF, such as reductions.

E. Task pruning

The main drawback of the decentralized model is that the work of unrolling the task flow is duplicated on all the workers. Scaling the number of tasks with the number of workers increases the overhead, because each worker has to process the tasks of all workers. Figure 7 illustrates this behavior. It reports the total execution time of $2^{15} \approx 32000$ independent tasks per worker consisting in incrementing counters.

In case the runtime overhead becomes intractable because of a high volume of extremely fine-grained tasks, an application-specific solution is to use task pruning. Task pruning for STF has been successful in distributed-memory settings [7].

Fig. 7. Total execution time of $2^{15} \approx 32000$ independent tasks per worker consisting in incrementing counters.

IV. FORMAL SPECIFICATION

In addition to the algorithm described in section III and a concrete implementation of the decentralized in-order execution model, we propose a formal specification of the model in TLA+ [22]. This formalism allows us to precisely (1) distinguish the programming model from the execution model and (2) define the proposed model in terms independent from the proposed implementation. In addition, although model checking is subject to combinatorial explosion and is intrinsically limited to the assessment of very small test cases, it may still provide further confidence on the assessed model (as a complement to the — necessarily non exhaustive — at scale actual experiments we will discuss later on in section V).

The specification consists in two modules: a specification of the STF model and a specification of our Run-In-Order execution model which must comply with this STF specification. For a matter of conciseness, we only present here the methodology we have followed together with the illustration of a particular property, and we report to appendix B of the associated research report [23] for an exhaustive specification.

The STF module describes all the possible executions of a STF program for a given set of workers, data, tasks and task flow. By giving concrete values to these variables, tools such as the TLA+ model checker, TLC [24], can be used to verify that some properties hold for any possible execution. We illustrate it with the termination property. In the STF specification, termination is defined as any state in which the union of active tasks (tasks that a worker is actively executing) and pending tasks (tasks not yet executed or being executed by a worker) is empty.

$\text{Terminated} \triangleq \text{pendingTasks} \cup \text{activeTasks} = \{\}$

The STF specification also defines a data-race freedom property that is satisfied as long as no pair of workers are executing tasks with a dependency on the same data and one of the tasks performing a write to that data. There is no property enforcing the sequential consistency in the STF specification. Instead, it is encoded in the state transition by exclusively allowing states to be reached for which sequential consistency holds. We report to appendix B.1 of the associated research report [23] for an exhaustive specification of the STF model.

The Run-In-Order module describes all possible execution for the in-order execution model presented in this paper. In addition to the workers, data, tasks and task flow variables, an additional mapping variable is used to attribute tasks to workers. The state transition is further restricted to prevent workers from re-ordering their tasks. The only property checked against the Run-In-Order model is that it implements the STF specification, that is the set of executions allowed by the Run-In-Order model is a subset of all possible STF executions. Because the STF model is checked to verify termination and data-race freedom and ensures sequential consistency, checking the Run-In-Order model also ensures those properties. Appendix B.2 of the associated research report [23] gives the full specification of the execution model.

Using the TLC model checker we checked the correctness of the STF and Run-In-Order specifications by emulating a tiled LU matrix factorization using two workers. The results for different sizes using TLC are reported in table I. The exponentially growing number of tasks only allows us to assess...
TABLE I. Number of states found and execution time of TLC to check the STF and Run-In-Order models on the LU factorization algorithm with different matrix sizes (number of row × column blocks).

<table>
<thead>
<tr>
<th>Size</th>
<th>STF Generated States</th>
<th>STF Distinct States</th>
<th>STF Time</th>
<th>Run-In-Order Generated States</th>
<th>Run-In-Order Distinct States</th>
<th>Run-In-Order Time</th>
</tr>
</thead>
<tbody>
<tr>
<td>2 × 2</td>
<td>445</td>
<td>23</td>
<td>1s</td>
<td>2322</td>
<td>11</td>
<td>1s</td>
</tr>
<tr>
<td>3 × 2</td>
<td>54 481</td>
<td>94</td>
<td>11s</td>
<td>1 847 877</td>
<td>29</td>
<td>56s</td>
</tr>
<tr>
<td>3 × 3</td>
<td>542 753 065</td>
<td>655</td>
<td>22h27min</td>
<td>-</td>
<td>-</td>
<td>&gt;-48h</td>
</tr>
</tbody>
</table>

very small test cases. We nonetheless found no errors during model checking and obtained a low state collision probability of at most $1.9 \times 10^{-8}$, giving us some confidence in the correctness of the proposed models.

V. PERFORMANCE EVALUATION

For evaluating the ability of a decentralized in-order runtime to efficiently execute tasks of fine granularity, we have implemented the specifications proposed in section III within our new RIO runtime. We compare it against StarPU, a state-of-the-art runtime whose default execution model within a node is centralized OoO. The experiments have been conducted on a dual socket 12 cores Haswell Intel Xeon E5-2680 v3 [12].

A. Methodology

We consider four test cases to assess our method:

- Experiment 1 (Fig. 8 row 1) uses independent tasks;
- Experiment 2 (Fig. 8 row 2) uses random read and write dependencies (128 data objects with 2 random read and 1 random write dependencies per task);
- Experiment 3 (Fig. 8 row 3) uses the matrix multiplication dependency graph; and
- Experiment 4 (Fig. 8 row 4) uses the dependency graph of a LU factorization without pivoting.

As illustrated above with the matrix multiplication (Figure 3), the efficiency of the considered kernels executed by the tasks may be sensitive to the effects of the granularity and of the locality, which are orthogonal to the issues we focus on in the present study. When operating at low granularity, the dumping of the traces notifying all the events which would allow one to remove such effects in post-processing would have a non-negligible impact on the overall performance. Instead, we chose to substitute each actual task with a synthetic task, common for all the tasks of the four experiments. This common synthetic task consists in incrementing a counter:

```c
volatile uint64_t counter = 0;
for (uint64_t i = 0; i < N; i++)
    counter = i;
```

Using this kernel, we get a granularity efficiency $e_p(g) = 1$ as incrementing a single counter up to $N$ is almost exactly as long as incrementing $n$ counters up to $N/n$. Also, because the only relevant memory location lives on the thread’s stack, the locality efficiency also becomes irrelevant: $e_l(g) = 1$.

With this kernel the experiments become sensitive only to the two remaining efficiencies, $e_p(g)$ and $e_r(g)$, the ones of interest for our study. They depend on the cumulative time spent executing tasks $\tau_{p,t}(g)$, idle $\tau_{p,i}(g)$ and the total cumulative execution time $\tau_p(g)$. Because there is no locality effect, $\tau_{p,t}(g)$ is equal to the execution time for the same sequence of tasks on a single computation unit without runtime, $t(g)$, and the total measured execution time $t_p(g)$ can be used to trivially derive $\tau_p(g)$. As RIO uses mutexes for synchronization, the idle time can be obtained with non-intrusive measurements from the CPU time share, while StarPU offers lightweight built-in online performance monitoring tools for measuring idle time that does not require to dump a trace. Measurements in StarPU are intrusive and do incur a small overhead, but because StarPU has a parallel efficiency close to zero due to the bottleneck effect with fine granularity, that overhead is negligible in our experiments.

All in all, the four experiments we conducted therefore correspond to the actual task graphs of the considered test cases but the tasks themselves are synthetically generated.

B. Results

The results of the four experiments are shown in Figure 8. Centralized OoO and decentralized in-order execution models indeed exhibit very different performance profiles: StarPU demonstrates very good and consistent performance for coarse tasks on all four experiments while RIO is much more sensitive to the dependency graph, especially when no appropriate mapping and task ordering can be given, as with random dependencies (experiment 2).

The runtime overhead of StarPU is almost independent from task sizes and explained by the fact that one of the thread is completely dedicated to task management, capping the maximal theoretical runtime efficiency to $e_p-1$ when running on $p$ threads. When tasks get small, between $10^5$ and $10^6$ instructions for StarPU, the centralized model starts struggling to handle all the tasks: the master thread is not able to produce enough tasks to feed all the workers, who are then forced to enter idle mode leading to the observed drop in pipelining efficiency. Decentralized models do not have this weakness because the workers independently process the task flow. With RIO, we observe that the execution becomes limited either by the pipelining or by the runtime efficiency depending on the task graph. If the number of synchronizations required is low or mainly for read operations (experiments 1 and 3), the time spent by the runtime for processing the task flow is the main source of slowdown, but thanks to the efficient in-order execution, the overhead is still reasonable even for very fine tasks of $10^4$ to $10^2$ operations. When more synchronization are needed (experiments 2 and 4), the time spent waiting for dependencies becomes the main source of total execution time.

VI. CONCLUSION

While most modern STF runtimes rely on centralized OoO execution models when dealing with shared-memory machines, other models are possible. In particular, inefficiency in handling fine-grained tasks was previously considered as a limitation of the STF programming model itself, while we showed it can in fact be attributed to the centralized execution...
Fig. 8. Efficiency decomposition as a function of task sizes for a decentralized in-order runtime (Rio) and a centralized OoO runtime (StarPU) on different task graphs.
model used de facto in current implementations. We have proposed and assessed an alternative decentralized in-order execution model, on top of an enriched (with the additional requirement to provide a static mapping) STF model. This execution model achieves a higher level of performance in the special case of fine-grained tasks, thanks to lower runtime overhead and independent task flow unrolling. By drawing a distinction between the programming and execution models, we demonstrate that the case of small granularity is not an intrinsic limitation of the STF model itself and we hope that the present study might motivate future work combining both execution models (and thus requiring only partial mappings) for enabling efficient and portable implementations of wider classes of algorithms within the STF programming model. We also plan to investigate leveraging OpenMP’s included tasks as a building block for implementing a decentralized-in-order STF execution model within the scope of the standard, to let a broader audience benefit from it.

REFERENCES


