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Rules, Computation and Politics: Scrutinizing Unnoticed Programming Choices in French Housing Benefits

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1 INTRODUCTION

1.1 Technical Specifications and their Consequences

Modern administrative services use computer programs to automate the massive application of certain legal directives. One of the most emblematic example of such an automation lies in the computation of social benefits, distributed in many welfare states by government agencies. The program computes the amount of benefits owed by the government to the individual or household, depending on a long list of inputs characterizing a household and being able to turn him or her into a beneficiary. The algorithm followed by the program is determined by a set of laws and regulations providing the legal basis for the welfare State.

The programs computing social benefits, implemented since the late 1970 in public administrations, are sometimes referred to as *legal expert systems*. They consist in a series of logic rules that effectively define a specification of a particular interpretation of the law, as described by Merigoux [2022]. In a nutshell, the specification is a socio-technical *mediation* that bridges the gap between the intent of the legislator, more or less accurately conveyed by the text of the law, and the limited set of operations a computer is able to execute. In particular, the specification should effectively describe a computation, with determined inputs and outputs, and a series of computation steps between the two. As such, the specification is merely a projection of the law with a narrow application objective that does not capture the full descriptive power of the law, but rather seeks to disambiguate it completely for a specific purpose, usually at price of embedding several interpretations and tacit knowledge into the program.

While less powerful in collective meaning and interpretability than the text of the law, this computer specification has the benefit of increasing file processing efficiency and saving labor costs compared to an army of civil servants using pocket calculators behind their counters. As a second decree of consequence, the centralization of the computation from the hands of the civil servants into a single computer program can help lower the level of “discretionary power” and sometimes imperfect guidelines on law implementation introduced by the human treatment of clerical administrative procedures¹.

Lately, some experts promoted by the OECD suggest there are advantages to using a novel approach in digital government services based on such computer specifications (or in a sense the replacement of the law by these specifications), and called “rules as code” [Mohun and Roberts 2020]. In the case of social benefits in the US, Kennan and Soka [2022] write that the massive

¹According to Lipsky [1980], public policies are made by street-level workers who regularly interact with citizens in the course of their jobs and that develop techniques to manage with rules and agency pronouncements.

and computerized application of benefits law across the US has emphasized the small differences that existed in all the social programs enacted by the States and the federal government. These small differences regarding the definition of the staples of benefits law (income, family status, etc.), already detrimental to confused beneficiaries that sometimes give up benefits applications, are magnified by the computerized treatment of benefits eligibility. With centralization of eligibility screening, programmers of the legal expert systems have to deal with inconsistencies of legislation designed independently across branches of government. The “rules as code” doctrine then consists in promoting a transformation of the standards for writing legal rules, so that they can be directly transposed into a programming language and there is no gap between the legislator’s intention and large-scale application. It is part of what Hildebrandt has labeled “code-driven law” [Hildebrandt 2020].

1.2 Turning the Rules into Code: a Focus on Social Implications

While some authors, with a normative stance, call for an increased use of “rules as code” methodology into the very design and enactment process of legislation to reduce these inconsistencies, we first suggest a comprehensive investigation of the computational complexity of turning legal rules into code. From a computer scientist’s point of view, social benefits eligibility and computation software routinely exhibits buggy behavior, as laid out by Escher and Banovic [2020]. Some of these bugs come from a purely technical failure of the IT system, others are more interesting to us as they stem from the way the computer specification translates the intent of the law. In the latter, the term “bug” is not always appropriate as the unexpected behavior of the program does not always reflect an error, but rather a divergence about how the program *should* behave.

Indeed, although it should stem in all impartiality from the text of the law, the specification conveys the point of view of the program authors (and the administration that they work for), in multiple ways. Firstly, when the law is ambiguous, the administration responsible for writing and operating the computer program has to choose a single way in which the computation will be encoded, due to the rigidity of computers programs portrayed by Diver [2021]. The sources of ambiguity are diverse. Sometimes, the law is purposely ambiguous so as to give some leeway for its interpretation: for instance, alleviating sanctions for an indicted individual acting “in good faith”. It is impossible to formalize what good faith is, as it is a notion heavily dependent on context; we shall not try to define its meaning in a computer program. Other times, the law is simply *inconsistently* drafted and leaves open different and conflicting syntactic or semantic interpretations. In this article, we will not expand on these ambiguities as they have been a staple of computational law studies for more than 60 years [Allen 1956].

Secondly, and this will be the core subject of this article, it is up to the writers of the program to define the *model of reality* that their computer program will act upon. Their work is precisely to “inscribe” this vision of the world in the technical content of the program. This vision of the functioning of technical objects echoes the sociological notion of “script”. Comparing technologies to film, Akrich [1992] suggests that “like a film script, technical objects define a framework of action together with the actors and the space in which they are supposed to act.” The interest of this notion is to underline that the behavior of technical objects, even the most sophisticated ones, does not always match the will of their designers, they have an “agency”. Concretely, a form will ask from the recipient a certain amount of personal information required to assess their eligibility to the benefit, and compute the precise amount to which they are entitled to. Such personal information usually includes the income, family situation, dependent children, etc. Star [1990] has underlined the cost of surveillance that is borne by users when filling out the forms, the impossibility for the administration to guarantee that particular situations are effectively taken into account, and the

inevitable alteration of relationships when a user makes a non-standard request². Other sociologists has shown the personal information provided by the potential beneficiary is the key of their interaction with the State [Alauzen 2019; Weller 1999]: it should be detailed enough to fill the boxes of the administrative forms, but also backed by paperwork and sometimes very thorough investigations in users' homes [Dubois 2021] that constitute the evidence of the reality of the information. For example, a period of the career of the potential beneficiary for which they cannot provide payslips might be rejected for consideration of the pension computation, leading to a lower overall pension. Because the programs determine the script that both users and administrations have to follow, we claim that programs have power in setting the relationship between the state and citizens, and their work around translating law in computation devices is a site of *neglected discretionary power*.

1.3 Case-study : Housing Allowances in France (1945-2022)

To scrutinize unnoticed programming choices in legal computation, we select the application for housing benefits in France. Our choice was informed both by the very broad nature of this benefit (owners, tenants, students, families, etc.) and the fact that it has been in the news several times because of its recent drop and problems with its computation [Zerouala 2021].

Three categories of housing benefits were brought in the French welfare system (hereinafter referred to the contemporary National Family Allowance Fund as CNAF) throughout the second part of the 20th century. The first is the family housing allowance (hereinafter referred to as ALF), which was created in 1948³ in order to compensate for the distortions in the housing sector caused by the Second World War and the increase in rents resulting from the law of September 1st, 1945 written to rebuild housing and the nation. In the early 1970s, a new category of housing benefit was created to assist other vulnerable households which did not meet the eligibility conditions for the ALF, the social housing allowance⁴ (hereinafter referred to as ALS). Finally, the third and last category, to which this article is dedicated, is the personalized housing benefit (hereinafter referred to as APL) created in 1977 by the so-called "Barre" reform⁵ (named after, Raymond Barre, the Minister who initiated it). The computation of the amount of these three allowances is complex and depends, for instance for tenants, on the geographical area in which the accommodation is located, the amount of the rent or the monthly repayments, the size of the family and its resources.

The management of housing allowances and, more generally, family benefits is carried out by the departmental family benefits offices of the CNAF. They are located throughout the country and interact with users daily. These funds were created by the decree of October 4th, 1945, the Article 19 of which stating that: "The management of family benefits is ensured by family benefits offices whose district and headquarters are determined by decree of the Minister of Labor and Social Security, taking into account the territorial districts of the primary social security funds"⁶. Additionally, personal housing assistance and removal grant are financed by the national housing

²"This is not the disenfranchised, which may at some point be 'targeted'; not the residual category not covered in present marketing taxonomies. This is that which is permanently escaping, subverting, but nevertheless in relationship with the standardized. It is not nonconformity, but heterogeneity." [Star 1990]

³"Loi n° 48-1360 du 1^{er} septembre 1948 portant modification et codification de la législation relative aux rapports des bailleurs et locataires ou occupants de locaux d'habitation ou à usage professionnel et instituant des allocations de logement."

⁴"Loi n° 71-582 du 16 juillet 1971 relative à l'allocation de logement."

⁵"Loi n° 77-1 du 3 janvier 1977 relative au maintien des aides publiques à l'investissement malgré l'institution de l'aide personnalisée au logement." This law gave rise to the classic work of Bourdieu [2005] on the market of the individual house.

⁶"Ordonnance du 4 octobre 1945, Article 19 : 'La gestion des prestations familiales est assurée par des caisses d'allocations familiales dont la circonscription et le siège sont fixés par arrêté du ministre du travail et de la sécurité sociale, compte tenu des circonscriptions territoriales des caisses primaires de sécurité sociale.'"

assistance fund⁷, which provides the legal framework and standardizes the procedures. While the CNAF has invested in automation since its creation in 1945, in 1997 it introduced the CRISTAL⁸ information system to handle the increasing complexity of the legislation and regulations for all its benefits, including housing benefits, and compute allowances [Kounowski 2002].

The logic of a generalized aid whose amount depends on the ability to pay the rent followed by the French State for the creation of the APL differs considerably from previous policies in terms of housing allowances [Calcoen and Cornuel 2001]. The APL pursues more of an overall objective of a generalized personal aid, which also conflicts with previous policies of aid to property, aimed more at investment in real estate. Public intervention on these issues increased at the end of the 1980's and beginning of the 1990's in order to extend the scope of this aid to all rental housing, but also in a desire for social equity towards more beneficiaries. If the intent behind housing benefits that transpires from all the policies taken during the 20th century appears to tend more towards social action, the trend has been reversed since the beginning of the 21st century, especially during president Macron's first five-year term (2017-2022). Several reforms have, in fact, resulted in the reduction of the housing benefits. The first of these reforms, introduced by a decree, was materialized by a flat-rate reduction of 5 euros for all recipients of personalized housing benefit⁹. Another reform was introduced by the decree of February 27th, 2018, which provides for a decrease in personalized housing assistance correlating with the reduction in solidarity rent for households that benefit from it¹⁰. The latter was introduced as part of the 2018 finance law and involves a cut in aid paid by the State but borne by social landlords¹¹. Thus, this does not appear to be a reduction in aid for the beneficiaries, but it is nevertheless a source of savings for the welfare state and a change of philosophy, which is transferring the "social burden" to the private sector. Later, in 2019, a new method of computing personal housing benefits was introduced. The updated computation implies that resources are taken into account "in real time", over the last twelve months and no longer over a period of time two years earlier¹². Numerous adjustments were necessary following the adoption of these decrees, but, beyond the succession of technical rules, the political intention that has not escaped observers is a significant reduction in personalized housing benefit [Cour des comptes 2020].

2 DATA AND METHODS : FIXING THE ABSENCE OF AN EXPLOITABLE SOURCE CODE BASE

2.1 Source Code Investigation

To study the unvalued discretionary power that comes into the computation of housing benefits in France, we will dive into the technical intricacies of one of the legal expert systems used by the French administration to power the financial redistributions operated at the national level. Computer systems taking automated administrative decisions are under quite heavy academic scrutiny in two main circumstances: in case of scandals or affairs, or, more recently, when the source code is open. For instance, in France, the introduction of "Parcoursup", a matchmaking algorithm between prospective first-year students and universities launched a collective process of

⁷Articles L811-1 and following of the Construction and Housing Code.

⁸Acronym for "Conception Relationnelle Intégrée du Système de Traitement des Allocations".

⁹"Décret n° 2017-1413 du 28 septembre 2017 relatif aux aides personnelles au logement et au seuil de versement des allocations de logement."

¹⁰"Décret n° 2018-136 du 27 février 2018 relatif à la baisse de l'aide personnalisée au logement dans le cadre du dispositif de réduction de loyer de solidarité."

¹¹"Loi n° 2017-1837 du 30 décembre 2017 de finances pour 2018, Art. 126."

¹²"Décret n° 2019-1574 du 30 décembre 2019 relatif aux ressources prises en compte pour le calcul des aides personnelles au logement."

investigation into the allocation of training courses, in which economics, sociology of education and computational sciences were involved [Becker et al. 2020; Frouillou et al. 2019]. Such critical investigation indeed requires a combination of skills between social sciences, law and computer science.

Apart from these situations in which the public investigates administrative software, the main obstacle for critical investigation has been the access to the source code of these legal expert systems. Since 2016 in France¹³, the source code of legal expert systems involved in automated administration decision making is subject to the same access rights as administrative documents. Nevertheless, the publication of the source code is operated independently by each administration. While a lot of source code has been released on code.gouv.fr [Guerry 2019], for computer scientists the material is not always fit for reuse, exploitation or even investigation. Indeed, the legal expert systems operated by the French administration often use legacy technologies and programming languages like the historic language for business operations in mainframes, COBOL. Some programs are even written in a custom programming language used only by the administration [Merigoux et al. 2021b]. Because they date from times when writing, verification and collaboration practices were not the same as today, these legacy or custom programming languages sometimes lack the infrastructure necessary to actually run programs written with them on modern machines : compilers, interpreters, etc. The published source code also rarely comes with adequate documentation¹⁴ about how to feed the program input, what does the program even compute exactly, or how to interpret the administrative terms inside the names of functions and variables. For resolute computer scientists, the absence of documentation may be compensated by a significant retro-engineering effort, which can also prove impossible to achieve if some key information was withheld by the administration during publication. Hence, even if the source code of the legal expert system is published, it is often unworkable for a critical investigation of the underlying algorithm, for instance to check its faithfulness to the legislation it is supposed to follow.

This situation holds true for the case study of this article, concerning the computation of French housing benefits. Even though they are distributed locally by a network of social benefits agencies, the rules that specify the eligibility and amount are enacted and translated into code for the CNAF's IT system, CRISTAL, at the national level. When we asked for the source code of the housing benefits computation in October 2020, the CNAF replied by physically mailing us a CD-ROM containing a set of COBOL files similar to the ones obtained two years earlier by journalists [Berne 2018]. These COBOL files, lacking any documentation about how to compile or run them, appear to be generated by a [Computer-Aided Software Engineering](#) (CASE) tool, whose high level sources have not been published. In other terms, what the CNAF published is merely the low-level source code, not meant to be read or edited by humans, while the real high-level source edited through a CASE tool is probably still hidden behind the CNAF curtains.

Moreover, we received in November 2021 during subsequent discussion with the CNAF another excerpt from the source of the housing benefits computation. This excerpt was written using Oracle's proprietary [Oracle Intelligent Advisor](#) (OIA) programming language, as it appears that the CNAF had recently undertaken a rewrite of the housing benefits computation algorithm using this

¹³“Loi n° 2016-1321 du 7 octobre 2016 pour une République numérique.”

¹⁴Guidelines for high-quality software artifacts documentation are for example released by the [Association for Computing Machinery](#) [2020].

new technology, as a part of a grand scheme to modernize the CRISTAL system. We asked for the rest of the source code written in OIA but got no answer¹⁵.

2.2 Replication of the Codebase

In the absence of an exploitable source code base, we have developed a working implementation of the housing benefits computation so that we could study it instead of the “official” one. This method of replication is common in critical code studies. We have used the Catala programming language and methodology already empirically tested for the tax code [Huttner and Merigoux 2022; Merigoux et al. 2021a] to translate the housing benefits computation into computer code directly from the text of the law. Concretely, we have spent more than 70 hours doing interdisciplinary *pair-programming* as a lawyer-programmer duo to produce more than 10,000 lines of rules and code, literally constituting a computer program able to compute the eligibility and amount of housing benefits entitled to a household described by a computer form. This form, as well as the computation rules, have been extracted from a corpus of legislative and regulatory provisions constituted after an extensive legal search of everything related to housing benefits on the French legal database (legifrance.gouv.fr). Once the corpus had been constituted, the translation to code was done in the order of the legislative texts, following the hierarchy of rules from high to low. The resulting source code is published under the Apache license on [GitHub](#).

During the process of translation, we have recorded all the instances where we realized that we were making a micro-choice in the textual interpretation of the legal framework that may affect the outcome of the computation or the attitude of the beneficiary. While we cannot claim to have identified all such micro-choices in our case study, as some of them may have fallen outside of our scrutiny, we believe those we singled out are sufficient to support our main statements. We present below three of these micro-choices as detailed case studies: imprecision, simplification and invisibilisation. They were selected because each explicit a kind of unnoticed decision programmers make. The categories chosen empirically represent the majority of micro-choices that we recorded during our work.

2.3 Inquiry in the Administration

In order to verify that the replication of the code is as rigorous as possible (*i.e.* as close as possible to the letter of the law), we carefully looked for CNAF forms (both paper and online) and we contacted the administrations responsible for writing the texts that govern the computation of housing allowances (two interviews, with six people in 2022, and a dozen email exchanges). We explained to them our replication approach and sent them the list of inconsistencies and typos that we had found. The interaction allowed us to understand the ordinary conditions of the production of this type of rules (formal and informal constraints, justifications and incertitudes, negotiating sequences, the intertextual construction of legal rules...), to which we will return in the discussion.

¹⁵The rewriting of this legal expert system, whose new source code is an administrative document, using a proprietary technology (OIA) is problematic in light of article L300-4 of the French code of relationship between the public and the administration: “Every electronic publication done in application of the present book has to be done in an open standard, easily reusable and exploitable by an automated processing system”. We do not know the exact details of the intellectual property (IP) situation of the source code as the CNAF’s contract with Oracle has not yet been released, but there could be a friction between L300-4 and the IP rights of Oracle about the communicability of the source code of the housing benefits computation.

3 MICRO CHOICES EXPLICITATION

3.1 “Should we ask couples for the date of conception?” Imprecision at stake

The first case study chosen to expose the type of choices involved in translating the law into a program concerns the computation of the moving allowance, which depends on the state of the pregnancy of the potential beneficiary. This social benefit is set out in Article D823-20 of the Construction and Housing Code which provides :

*The moving allowance is awarded to persons or households with at least three children born or to be born who move into a new housing entitled to one of the personal housing allowances during a period between the first day of the calendar month following the third month of pregnancy in respect of a child of rank three or more and the last day of the month preceding that in which the child reaches his or her second birthday [...]*¹⁶

This mode of determining the temporality of personal rights is widespread in law, but it does not fit well with computational logic. Indeed, this article is complex for coders in that it makes the eligibility for a social benefit (in this case the moving allowance) dependent on an uncertain event or at least of uncertain timing, namely the birth of a child.

The main issue here is to determine which date has to be taken into account for the start of the pregnancy in order to ascertain when that period of three months effectively starts to be able to compute the allowance. Two options can be envisioned for the computation: the date of the conception of the child or the date considered to be the beginning of the pregnancy. However, the search for this kind of data may be deemed too intrusive or non-relevant from the point of view of the beneficiary completing the form and may lead to non-take up.

Another issue was the computation of periods of time, specifically here, months¹⁷. It is therefore difficult to establish a time frame for the first day of the civil month of the third month of pregnancy with precision. In other words, this article does not really provide a clear starting date for the time period it sets, thus, making it challenging to incorporate into the program the most accurate time and duration assessment method possible.

Beyond these technical considerations, there is also the question of the usefulness of such personal data for the computation of the personalized housing benefit. The search for these elements is intrusive in the private life of the potential beneficiary. It is therefore essential to question the need for such information as the choices made at this stage will have a direct impact on the questions asked in the form and on the user who will proceed with an application.

The question then becomes: what does the administration’s program do? Will the programmer look for the easiest information to code, even if that information turns out to be intrusive and a potential deterrent to claiming a right? Or will she look for alternative solutions to preserve privacy and reduce non take up? Without access to source code, we do not know precisely how CRISTAL

¹⁶“Code de la construction et de l’habitation, Article D823-20 : ‘La prime de déménagement est attribuée aux personnes ou aux ménages ayant à charge au moins trois enfants nés ou à naître et qui s’installent dans un nouveau logement ouvrant droit à l’une des aides personnelles au logement au cours d’une période comprise entre le premier jour du mois civil suivant le troisième mois de grossesse au titre d’un enfant de rang trois ou plus et le dernier jour du mois précédant celui au cours duquel cet enfant atteint son deuxième anniversaire [...]’”

¹⁷The concept of time is complex to implement through a computer language as there are various ways to measure it. Most computers count the number of milliseconds elapsed since Jan. 1st, 1970 for their time computations, but French law implicitly relies on computations using the Gregorian calendar, which themselves can be ambiguous. For instance, what is “Mar. 31st + 1 month”? Is it May 1st or Apr. 30th?

computes the pregnancy condition. Nevertheless, given the official form we have had access¹⁸, we deduce that the program uses medical data named “the presumed date of the beginning of the pregnancy” that doctors declare to plan mandatory medical examinations (such as ultrasounds), preparatory interviews and childbirth and parenthood preparation sessions with midwives. In other words, for information system convenience, the housing allowance computation system asks users to provide medical data filled in another form, for another purpose.

In addition to making these kinds of choices explicit, replication in Catala allowed us to experiment with alternative paths that show that it could be otherwise. Hence, translated in Catala, the article D823-20 is as follows :

```

code_construction_reglementaire.catala_fr
règle condition_période_déménagement sous condition
(selon ménage.date_naissance_troisième_enfant_ou_dernier_si_plus sous forme
  -- MoinsDeTroisEnfants: faux
  -- PlusDeTroisEnfants de date_naissance_ou_grossesse:
    (selon date_naissance_ou_grossesse sous forme
      -- AvantPremierJourMoisCivilTroisièmeMoisDeGrossesse: faux
      -- AprèsPremierJourMoisCivilTroisièmeMoisDeGrossesse: vrai
      -- DernierJourMoisPrécédantDateDeNaissance de date_naissance:
        date_ouverture_droits <=@ date_naissance +@ 2 an))
conséquence rempli

```

We have chosen to leave it up to the user to determine whether his or her request is actually made after the first day of the calendar month of the third month of pregnancy, via the use of an input variable taking values into a predetermined enumeration. Thus, no unnecessary data is collected, the data required to determine eligibility for the removal allowance is verified and the form remains neutral. This solution results from the breakdown of the various possible hypothesis:

- The household has less than 3 children and is therefore not eligible;
- The household has 3 or more children and the last child is already born: the period runs from the child’s birth to the date of the second birthday;
- The household has 3 or more children and the last child is still to be born: it is then up to the user to ensure that the application is made after the first day of the calendar month of the third month of pregnancy.

This decision was taken with a view of protecting the privacy of beneficiaries while ensuring compliance with the law and accuracy of computation. Privacy is protected in French law at several levels: first by law since 1970¹⁹, then by the Constitution since 1999²⁰, but also at the European level by Article 8 of the European Convention for the Protection of Human Rights and Fundamental Freedoms. By translating this law in such a way that there is no need to process such information in order to determine eligibility, the protection of the privacy of the potential recipient is ensured (to the extent of any information necessary and useful for the determination of the eligibility of the recipient).

¹⁸“CERFA 50040#06, Premier examen médical prénatal.”

¹⁹“Loi n°70-643 du 17 juillet 1970.”

²⁰“Conseil Constitutionnel, 23 juillet 1999.”

The decision to simplify the information required in this case as much as possible also had a significant effect on the translation of the text into code. The relevant part of the program was considerably simplified as we removed some of the complex date computations.

The question of how to compute the duration set out in the law indicates that programming choices have consequences for the input forms that users fill out. They are directly involved in their more or less privacy-friendly nature and have heavy implications for the user. First, the most convenient programming choices for developers may breach the privacy of the user that has to supply extensive personal information that is not *per se* required to apply the law. Second, they might create form boxes impossible to fill by users whose situation had not been planned, making the form harder to fill or reducing the interpretation leeway intended by the legislator and consequently reducing the use of rights. And all this, because of a question of precision of the duration of a parameter entitling to a moving grant, while this parameter can itself only be determined with uncertainty.

3.2 “Are there too many labels in the law?” The temptation to simplify categories

The second micro-choice concerns Article R821-3 of the Construction and Housing Code providing:

In the event of legal or de facto separation of the spouses *resulting in the creation of two separate households* and the occupation of two main residences, as determined by the paying agency at the time of entitlement or at the beginning of the payment period, *personal housing assistance may be granted to each spouse*²¹.

In this case, it is not so much of an imprecision of the law but rather a situation that does not appear to be taken into consideration in other articles of law (especially those determining the family situation) or by the administration when creating the forms used by the beneficiaries to apply to these housing benefits. “De facto separation of the spouses” is therefore a category that exists only in this legal device and is apparently confusing with other family situation categories (“single”), which programmers may tend to overlook.

On the [CNAF online form](#) (accessed on June 21st, 2022), there is only one possible choice: “You live as a couple: yes or no”. We therefore deduce that the computer program does not respect the letter of the law – because it is concerned with not multiplying the questions, or because it has forgotten or is not aware of this category. Yet, it is a situation that can arise for a couple. They may occupy two separate housings and are entitled to receive this aid individually, although they might still be legally married and appear as one household. Trickier: if a separated-but-still-legally-married person starts cohabitating with a new partner, then they should file as a couple with the new partner. Accuracy of the form that program makes and couples complete is of utmost importance here since any lack of precision could prevent a potential beneficiary from accessing rights to which they would otherwise be entitled to.

Again, the replication in Catala shows that it could be otherwise. To ensure adequacy with R821-3, the review of existing categories for the “family status” provided in Article L822-1 was required²². This was translated in Catala as follows :

²¹“Code de la construction et de l’habitation, Article R821-3 : ‘En cas de séparation, légale ou de fait, des conjoints entraînant la création de deux foyers distincts et l’occupation de deux résidences principales constatées par l’organisme payeur lors de l’ouverture du droit ou au début de la période de paiement, une aide personnelle au logement peut être accordée à chacun des conjoints.’”

²²Article L822-1 of the Construction and Housing Code : “The provisions of this book relating to the beneficiary, the principal residence or the taking into account of resources *applicable to the spouse are applicable, under the same conditions, to the partner linked by a civil solidarity pact or to the cohabitant.*”

code_construction_legislatif.catala_fr

déclaration énumération SituationFamiliale:

```
-- Célibataire
-- Mariés contenu date # Date du mariage, utilisée par L841-1
-- Pacsés
-- Concubins
-- CélibataireSéparéDeFait # Voir R821-3
-- ConcubinageDontSéparéDeFait # Voir R821-3
```

Instead of creating a whole new category, we assessed the different possible situations which could emerge from a case where the couple is *de facto* separated. We came to the conclusion that each person *de facto* separated could either be single or in another relationship and cohabitating with the person. We then used two pre-existing categories : “single” and “cohabitating partners” to fit this new scenario giving birth to two new variables : “*de facto* separated and single” and “*de facto* separated and cohabitating”. Because they are attached to the same enumeration in Catala, the programming language will force the programmer to review those two new cases every time the family status is used in the code of the program. Here, we use a technical feature of the programming language (here, its type system) to ensure consistent application of a legal subtlety across the codebase.

Revealing the family status of the user is necessary for the housing benefits computation as it allows the administration to determine the exact number of people occupying the accommodation. Being as precise as possible and not to simplify legal categories in form is thus mandatory. Catala allows us to determine all the different hypotheses to have the most representation, so that when the user completes the form, she will not hesitate between categories and have a choice actually consistent with the reality of her situation. Indeed, she might not complete an application for housing benefits because she is not aware that both of them have access to it or giving up because none of the previous categories fit their personal situation which could lead her to believe that she does not have the right to such housing benefits. This reasoning allows for simplified access to housing benefits for this particular case for certain beneficiaries who might otherwise suffer from a lack of information or knowledge in this regard.

3.3 “Does the computation always benefit the user?” On corner cases invisibilization

The third micro choice explicitation we identified with the replication method focuses on the processing of the different housing benefits when dealing with an application made by a potential beneficiary. Article L841-2 of the Construction and Housing code provides:

People who do not benefit from the family housing allowance or the personalized housing allowance can claim the social housing allowance²³.

Although quite understandable at first glance, the phrasing of this article leaves the door open for interpretation.

One may claim that it sets a hierarchy between these different allowances as it prioritizes the APL over the ALF and the ALS. The Ministry of Housing, we questioned on this point, has confirmed to us by email this is the interpretation adopted by CNAF²⁴. According to them: if a household is eligible to the APL, they will benefit from it. If they are not, but eligible to the ALF, then they will

²³“Code de la construction et de l’habitation, Article L841-2 : ‘Les personnes ne bénéficiant pas de l’allocation de logement familiale ou de l’aide personnalisée au logement peuvent prétendre au bénéfice de l’allocation de logement sociale.’”

²⁴Email exchange with DGALN/DHUP/FE4, May 30th, 2022.

benefit from the ALF, and finally, if they are not eligible neither to the APL nor the ALF, they will benefit from the ALS.

A slightly different interpretation may rest on the *de facto* distinction between being eligible for an allowance and benefiting from it, *i.e.* between meeting all the requirements set out to access this aid and effectively receiving it. The legislator's choice to create a rule which relies on the actual payment of the allowance to the beneficiary rather than on eligibility seems to reflect a desire to prevent beneficiaries from accumulating allowances, rather than the establishment of an decree of priority in the treatment of housing allowances.

Questioning the initial interpretation came from the mathematical realization that the computation of these allowances differed, which implies that it may sometimes be more profitable for a household to receive one allowance than another. Yet, if a person is eligible for the APL, they will receive the APL, regardless of whether they are eligible for another benefit that is more advantageous. It then proceeds that the interpretation of the administration might lead to financially hurting those eligible for both ALF/ASL and APL, and for whom the amount of ALF or ALS is higher than the amount of APL. This situation appears to have been overlooked by the administration, as a careful inspection of the computation formulae for the ALS/ALF and the APL leads to observing that in most cases, the amount of APL is indeed higher than the amount of ALS/ALF for the same household. However, these computation formulae have *corner cases*, specific situations where the actual result might deviate from the intended outcome. Corner cases are a notion with which all programmers are familiar, as these are the cases that consume most of their attention and time when they write computer code.

We provide such a corner case for which the ALS/ALF amount is higher than the APL amount, in Appendix A²⁵. This corner case corresponds to a household an elderly couple living in communal housing, one of them working for the minimum wage, the other having no income at all. We do not know how many real households this corner case corresponds to, as we do not have access to the CNAF's database²⁶. Nevertheless, this corner case intuitively sounds realistic ; the difficulty to find such a case in reality will probably come from the relatively low rent that the couple pays (360 € per month), although they live outside of a big agglomeration subject to rent inflation. For this couple, the financial loss of taking the APL instead of the ALS/ALF is about 120 € a year, but would increase with a lower rent due to the nature of the formulae for housing benefit computation.

When completing the online form on the CAF website, there is no mention of a possibility for the beneficiary to choose which benefit they are applying to. The CAF decides for them, and this decision prioritizes the APL, sometimes at the expense of the beneficiaries' access to rights. Indeed, this choice of interpretation, integrated into the CAF's computer system, potentially calls into question the efficiency of the processing of housing benefits. The divergent interpretation of a rule whose initial intention may seem clear, seen from a certain perspective, can have a major impact on beneficiaries' access to benefits. Yet, one of the fundamental principles of social protection that we were reminded directly in the ministries is that the purpose of these measures is always to prioritize the beneficiary, compared to the administration or any other entity. In this case, it seems to us that there is an obvious contradiction.

In order to testify that it could be otherwise, for our replication in Catala, we compute both the amount of ALS/ALF and APL for households that are eligible to both, and attribute the benefit with

²⁵A necessary preliminary explanation on the computation of these allowances is also provided in Appendix A.

²⁶As this database contains a lot of private information about millions of French households, its access by researchers is subject to a heavy procedure under the [Committee for Statistical Secret](#).

the maximum amount. This solution is clearly more complex technically, both in terms of number of lines of code, but also performance-wise. Indeed, this single choice is likely to double the computation time for each household. Re-running a computation with different parameters or tweaks to compare outputs is a practice sometimes called “multiple liquidations” by the administration developers we met.

4 DISCUSSION

If we do not know precisely how CRISTAL computes social benefits, the case studies from the replication presented above highlight a few of the unnoticed programming choices, influenced by the writing of the law, that can significantly affect the effective application of a piece of legislation having a big financial impact on its millions of beneficiaries: imprecision, simplification and invisibilisation. These programming choices have certainly been encountered by CRISTAL’s programmers, but also by many other programmers when writing legal expert systems.

The method of transcribing French housing law line by line also taught us that there were some kind of “mistakes” in the writing of the law. In this last section, we propose to discuss these mistakes in the light of interviews conducted and email exchanges with the agents responsible for writing these legal texts, and ruling the CNAF.

4.1 Unscrewing the Legislator

The two meetings with the agents of the Ministry of Housing and Health and Solidarity immediately confirmed one of the fundamental lessons of ethnomethodology studies in the field of law: there is *no legislator with a synoptic view of the law* [Dupret and Ferrie 2008; Latour 2010]. Even more, in the office responsible for personal housing assistance, there is not even a single document listing all the texts framing the personal right to housing. We put together this document as we were replicating the CRISTAL code and sent it to them²⁷. So how do they manage it? When they have to modify or write housing law texts, the agents “go hunting for legal texts”²⁸ and do not always find the texts they need (especially when the circulars are old and there have been many versions). Moreover, our literal transcription of the law has shown us that a certain number of texts were never published²⁹. The agents of the ministries confirmed to us that the information they contain still arrives in the administrations concerned by means of instruction documents and practical guides. This is not to say that in other places and in other areas of the law this synoptic view does not exist, but it is probably only temporary, partial and extremely difficult to build and maintain. As Latour [2010] has shown, the normal mode of existence of law is intertextuality, not a broad overview and we need to unscrew our modern legal fictions to grasp law in action [Callon et al. 1981].

²⁷“Par ailleurs vous nous avez indiqué avoir listé l’ensemble des textes relatifs aux APL. Nous sommes preneurs de votre listing”, Email exchange with DGALN/DHUP/FE4, May 25th, 2022.

²⁸Interview with DSS/AFPAT/2B, June 8th, 2022.

²⁹This is the case for another benefit, the solidarity benefit for elderly people (“Allocation de Solidarité pour Personnes Agées”, ASPA). The benefit is instituted by article L815-1 of the Social Security Code, and its maximal amount is set by article D815-1 of the same code. D815-1 is a decree that is supposed to be renewed each year, as the maximal amount for ASPA is indexed on the inflation. However, the latest version of D815-1 we could find dates from 2018, and we could not find any decree or order updating the values since then. We do know that the value is effectively updated each year, because we found yearly internal memos of the pensions agency (CNAV) managing the ASPA indicating the inflated values. This is problematic, because article L815-4 of the Social Security Code mandates that the amount of ASPA should be fixed by a decree, and an internal memo does not have the same value as a decree. At this point, we have not sought for comment from the pension agency about this situation, but it is likely that they would quickly write and publish the missing decrees if one were to point this out to them. The ASPA amount is needed for the housing benefits computation through article R823-4 of the Construction and Housing Code.

The absence of this holistic view of the area of law for which they are responsible is not due to organizational failure or malpractice, but is the result of the organization of the work routine. Indeed, the agents who arrive at the office responsible for the regulation of housing subsidies first inherit Excel tables with complex rates, values and formulae. Their task is to update these values annually or quarterly in the table and in the related regulatory texts. They often do not have a university education in law, and may not even be familiar with social protection regulations, the role and history of the welfare state in France. Traditionally, positions in the Ministry of Housing are held by engineers³⁰. Not only are these agents who write the law caught up in an extremely advanced division of social labor and bureaucratic specialization, but the regulatory writing for which they are responsible has a largely *infra-political character*. As Martinais [2010] has argued in relation to the drafting of regulations on environmental risks in the same Ministry, the formatting of regulatory texts is more the responsibility of the “sub-administration”, by delegating the work of writing and designing methods to the departments concerned. The making of law thus tends to be operationalized in a configuration that ensures a great deal of autonomy for subordinate agents in central administrations while opening up margins of maneuver.

Consequently, if lawyers were to read the texts these agents write, they would realize that there is no high concept of “Law”, prompt to hermeneutics, but a rather complex activity, which is carried out most of the time with no reference to the general principles of law, outside a thought of coherence and readability... and even which may seem opaque to lawyers! The reading of the Appendix A about $ALS = K \times (L + C - L0)$ in the Article D842-15 of the Construction and Housing Code should convince them of this.

4.2 The Normal and the Pathological of Regulatory Work

In meeting the agents who write housing law, we confirmed that the ordinary mode of production of legal rules and computer programs is structured by “current events”. Current events are both legal (such as a finance law in which a revision must be included) and political (such as an announcement by the president of the “deconjugalization” of an aid). This news guides the writing process, which then proceeds through multiple layers of rereading by the hierarchy, other administrations concerned, and experts. Due to the technical nature of the texts, in order to save time, the agents make many copies and pastes, changing only the dates or the reference values. However, this practice of reproducing texts does not prevent typos and inconsistencies. During our replication process of the housing benefits computation, we found several errors. Indeed, while French law describes the general principles for housing benefits eligibility and computation, the detailed values and parameters can be found in a separate ordinance³¹. The ordinance contained several typos that affected some parameters of the computation (for instance “2987.27” written instead of “287.27” in article 33), and missed a key listing of parameters for a special case. Overall, three articles (18, 31 and 33) contained at least an error.

When we reported the first of these errors to the ministries concerned, we were quietly told that “There are plenty of errors in the social security code”³². We were not the only ones to have detected them; some had already been pointed out to them by partner administrations, or agents had become aware of them while writing other texts. As in the process of collaborative writing of computer programs, the correction of errors in regulatory texts is part of a normal process. It is integrated into the work cycle and does not alert the agents. The whole legal edifice does not collapse on the basis

³⁰From the [State Civil Engineering Corps](#).

³¹“Arrêté du 27 septembre 2019 relatif au calcul des aides personnelles au logement et de la prime de déménagement.”

³²Interview with DSS/AFPFAT/2B, June 8th, 2022.

of an error in a computation parameter, however big it may be. The error in the publication of a text is not pathological, and it is not due to a lack of professional conscience or understanding of the law of the agents, but once again due to the social processes in which the regulatory texts are inscribed. On the one hand, CRISTAL's programmers do not re-encode directly from the text of the article each time, they just change a rate, a parameter and thus modify the program by small adjustments. Moreover, the thought that the errors are not pathological is confirmed by the complaint letters that the Ministry of Housing sometimes receives from users who dispute the computation of their situations by the CNAF. They manually redo the computations and conclude that "the computation is never a problem, the issue is the resources taken into account at the beginning"³³. In other words, aspects relating to the readability of the form and the quality of the data provided by the users, not to the law governing the computation.

Our methodology does, however, highlight a point of vigilance, since we noticed when reading the CNAF forms that there were simplifications and that not all situations governed by law could be declared (Section 3.2), but also that the interpretations of the law taken into account in the computation might not always benefit the users, thus contradicting the logic of social protection (Section 3.3).

4.3 An Automation Frontier in the Bureaucratic Division of Labor

The exercise of replicating the CRISTAL code for calculating housing benefits opened up a space for dialogue with the administration, which allowed us to learn crucial elements about the division of bureaucratic labor, beyond the normal and the pathological. One of the first things we were told by the head of the office of family and housing benefits at the Ministry of Health and Solidarity is that those who write the law "believe too much in the performativity of the law"³⁴. It means, in this context, that they deem the law is sufficient to bring about an alignment of the information systems, of the practices of the agents at the counters and of the whole bureaucratic process of housing benefits.

In this case, this belief is based on two phenomena. The first phenomenon is a *frontier of automation* in the division of bureaucratic labor, which has to do first with the training of French civil servants. Those who write the law in the ministries are not (or do not consider themselves) able to read the source code of information systems to check whether they respect the letter of the law and have been correctly updated. The few among them who would like to access it in order to conduct impact studies of a regulatory change for example, cannot do so directly. They have to go through many intermediaries (at the Ministry's information systems department, at the CNAF's managers, etc.). We can make the similar assumption that, by virtue of the same specialization of administrative knowledge, it is unlikely that CRISTAL's programmers will refer to the letter of the law as we have done and ultimately verify the program's compliance with positive law. Rather, they would use internal memos summarizing the computational content of positive law written at another level of the administration. Secondly, the procedure for writing standards according to current events described above reinforces the existence of this automation frontier. Indeed, in reaction to current events, they must quickly write a text and therefore ask the CNAF for their technical constraints, which they record in the writing of the rule itself. They therefore often have neither the time nor the technical capacity to carry out counter-expertise and to see the problems of time precision, such as those raised by Section 3.1.

³³Interview with DGALN/DHUP/FE4, May 23th, 2022.

³⁴Interview with DSS/APPFAT/2B, June 8th, 2022.

This social division of labor between the writers of the text, the functional specifications and the source code thus constitutes a *communicative circuit between the writing of the code and the law*. This circuit is undoubtedly code-driven in certain respects, but not exclusively: it is also guided by political choices (the reduction in allocations mentioned in Section 1.3) and by many other constraints linked to the bureaucratic writing process.

5 CONCLUSION: FROM PROGRAMMING CHOICES EXPLICITATION TO RE-SPECIFICATION AND RE-ORIENTATION

The article addressed the issue of unnoticed programming choices within social benefits computation. So far, we want to specify the two contributions that it brings to the contemporary debates. First, it suggests a contribution to the field of law and informatics, calling for a re-specification of the subject of research. Asking “Is law computable?” [Deakin and Markou 2020], scholars have focused on the nature of the law and more precisely to the alteration that computer technologies inflict to the law. Therefore, they have missed the phenomenon of practices, including the ordinary practices of writing, reading and revision of both law and code, in relation to a political, administrative and technological environment. In other words, we bring back here Garfinkel’s [1967] “missing what” problem of the study of objective reality of social facts which would encompass the contents of practices. Filling out the “missing what” seems to us even more indispensable when legal practices deal with technical rules, computation, formulae and invites us not to have a preconceived or normative idea of the “nature” of legal texts and coding activities. In the French housing allowance case, it leads us to discover an automation frontier in the division of administrative work, with, on the one hand, the writing of regulatory texts in the ministries, and, on the other hand, the writing of functional specifications and source code at CNAF. It also invites to pluralize the conception of the law and to fully consider the role of regulatory texts, even in their most technical and boring aspects. With each successive adjustment, such rules fuel the infrastructure for computing and distributing social assistance to millions of beneficiaries — also called the welfare state. However, this is far to mean that the articulation of legal and computational activities and knowledge is smooth and there is nothing like a public issue with digital technology and the law. We have identified, during the process of literal replicating the CRISTAL source code, that the transition to computer program is confronted with a problem of precision of the writing (Section 3.1), that the coders may encounter the temptation to simplify heterogeneous or atypical categories (Section 3.2), and that the corner case reasoning does not match with the current administrative process and has detrimental consequences on users (Section 3.3). In other words, when turning rules into code, “bugs” and indeterminate concepts are not the only problems we see. Moreover, we also identified other potential paths in reforming administrative practices and training agents.

Secondly and lastly, the article also contributes to law and society debates. Until now, most of the authors that have studied law as a practical activity have focused on Parliament activity, lawyers at work and trials. Our case studies suggest a re-orientation of research to open the black box of the mundane writing of law by state agents and to think and deal with computer programs as “living law”.

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A A CORNER CASE IN THE COMPUTATION OF THE FRENCH HOUSING BENEFITS

The computation formulae for the housing benefits are so complex that the government edits each year a [primer about the computation elements](#), that collects the rules scattered in the various regulations and presents them in a concise and logical order.

First and second, we propose a translation of the excerpts of this primer related to the APL and ALS computations in the specific corner case related in Section 3.3 we want to tackle: an elderly couple (within the meaning of 3° of article D842-16), with one individual earning the minimum wage and the other having no income, which brings their resources to 15,000 € per year. They live in communal housing (“logement-foyer”) that meets the criteria for the 1° of D832-25 , in Zone III, and pay a monthly rent of 360 €.

Third and fourth, we highlight how those rules apply by explaining each step of the computation of the APL and ALS on our corner case; The computations for this corner cases have been checked both manually by the authors and automatically by running our Catala program for the housing benefits computation.

In this example, it is preferable for the household to receive the ALF/ALS rather than the APL. Over one year, this represents a difference of about 120 €, a considerable amount for a low-income household. However, since they are eligible to the APL, that is the allowance they will receive from the CNAF, regardless of the real nature of their situation and needs.

A.1 A Primer on the ALS Computation

The computation of social housing allowance (ALS) is determined according to the formula set out in Article D842-15 of the Construction and Housing Code:

$$ALS = K \times (L + C - L0)$$

The application of this formula implies the prior determination of several variables.

The takeover coefficient “K”. Within the framework of the computation of personal housing aid, in the case of communal housing, this computation is based on the formula set out in the 2° paragraph of article D832-25 of the same code which reads as follows:

$$K = 0.90 - \frac{R}{cm \times N}$$

Where:

- “R” represents the resources of the potential beneficiary.
- “cm” is a multiplying coefficient whose value is set out in Article 30 of the decree of September 27th, 2019.
- “N” is the number of units that depends on the number of dependent persons determined according to a scale introduced in d) of 2° of Article D832-25.

K is rounded down to the second decimal.

The rent equivalence “L”. It depends on the family composition according to the figures set out in Article 43 of the decree of September 27th, 2019.

The lump sum for charges “C”. It is defined by Article 30 of the decree of September 27th, 2019.

The minimum rent “L0”. the computation of which is based on the the minimum equivalence “E0” set out in paragraph 2° of Article D832-26. It is necessary to clarify here the different brackets and rates used in the subsequent computations modes. Indeed, two different sets of brackets and rates are possible in the context of residential accommodation. However, the article detailing the ranges does not mention those used in the second computation mode (the one we are interested in here). The [primer about the computation elements](#) of the APL drawn up by the Ministry of Housing in September 2021 nonetheless includes these values, which we have decided to use in our computation. This source does not have full legal value, but it was confirmed to us by an email from the DGLAN/DHUP/FE4 office on May 25th 2022 that these were the correct values.

L0 is determined by the sum of the rates applied to the brackets resulting from the multiplication of the brackets’ limits by the number of portions “N”, then increased by the product of a lump sum defined in paragraph II of article 31 of the decree of September 27th, 2019 and the number of portions “N”, the whole divided by 12. As the wording of this formula is complex, we’ve included here the corresponding Catala code for reference:

```

code_construction_reglementaire.catala_fr
champ d'application CalculAidePersonnaliseeLogementFoyer:
  definition tranches_revenus_d832_26_multipliees egal à
    application pour tranche dans tranches_revenus_d832_26 de
      TrancheRevenu {
        -- haut: (selon tranche.haut sous forme
        -- Infini: Infini
        -- Revenu de tranche_haut:
          Revenu contenu (tranche_haut *€ n_nombre_parts_d832_25))
        -- bas: tranche.bas *€ n_nombre_parts_d832_25
        -- taux: tranche.taux
      }
  definition equivalence_minimale_loyer egal à
    (((somme argent pour tranche dans tranches_revenus_d832_26_multipliees de
      (si ressources_ménage_arrondies <=€ tranche.bas
        alors 0€
        sinon
          (selon tranche.haut sous forme
            -- Revenu de tranche_haut:
              (si ressources_ménage_arrondies >=€ tranche_haut
                alors
                  (tranche_haut -€ tranche.bas) *€ tranche.taux
                sinon
                  ((ressources_ménage_arrondies -€ tranche.bas) *€ tranche.taux))
            -- Infini:
              (ressources_ménage_arrondies -€ tranche.bas) *€ tranche.taux)
          ))) +€
    montant_forfaitaire_d832_26 *€ n_nombre_parts_d832_25) *€ (1,0 /. 12,0)

```

Final steps. A lump sum of 5 € should then be deducted from this result and it should be ensured that the minimal expenditure does not need to be subtracted. Then apply the social contribution tax (CRDS³⁵) rate, round down to the lowest euro and add the CRDS amount again.

A.2 A Primer on the APL Computation

The formula used, in the case of communal housing, is set by article D832-24 of the Construction and Housing Code:

$$\text{APL} = K \times (E - E0)$$

The application of this formula implies the prior determination of several variables.

The takeover coefficient “K”. It is defined in Article D832-24 of the Construction and Housing Code:

$$K = 0.95 - \frac{R - r \times N}{\text{cm} \times N}$$

Where:

- “R” represents the resources of the potential beneficiary.
- “r” is a coefficient set out in Article 30 of the decree of September 27th, 2019.
- “cm” is a multiplying coefficient whose value is set out in Article 30 of the decree of September 27th, 2019.
- “N” is the number of units that depends on the number of dependent persons determined according to a scale introduced in e) of 1° of Article D832-25.

K is rounded down to the second decimal.

The eligible equivalence of rent and rental charges ceiling “E”. It is set by article 27 of the decree of September 27th, 2019.

The computation of the minimum rent and service charge equivalence “E0”. is determined in Article D832-26 : it is the sum of rates applied to the brackets resulting from the multiplication of the ranges, listed in article 31, I) of the decree of September 27th, 2019, by the number of portions “N”, then increased by the product of a lump sum defined in paragraph II of article 31 of the decree of September 27th, 2019 and the number of portions “N”, the whole divided by 12. It is the same formula as in the computation of the ALS presented in Section A.1, but with a different set of brackets and rates.

Final steps. A lump sum of 5 € should then be deducted from this result and it should be ensured that the minimum expenditure does not need to be subtracted. Then apply the CRDS rate, round down to the nearest euro and add the CRDS amount again.

³⁵The contribution for the reimbursement of the social debt (CRDS) is a tax created by decree n° 96-50 of January 24th 1996, relative to the reimbursement of the social debt.

A.3 ALS Computation for Our Corner Case

$$ALS = K \times (L + C - L_0)$$

Where :

- $K = 0.90 - \frac{R}{cm \times N} = 0.90 - \frac{15000}{1.5 \times 21420.91} = 0,43$
- $L = 320.73\text{€}$
- $C = 54.22\text{€}$

For L_0 , it is first necessary to multiply the ranges by the number of portions N , which in this case is 1.5, to obtain the brackets, before applying the rates. This yields :

- 0% between 0€ and $1423.03 \times 1.5 = 2134.54\text{€}$
- 2.40% between 2134,54€ and $2047.61 \times 1.5 = 3071.42\text{€}$
- 20,80% between 3071,42€ and $2629.85 \times 1.5 = 3944.78\text{€}$
- 23,30% between 3944,78€ and $4095.05 \times 1,5 = 6142.58\text{€}$
- 32,80% between 6142,58€ and 15000€.

Hence,

$$L_0 = \frac{3619.29 + 76.32 \times 1,5}{12} = 311.15\text{€}$$

Therefore:

$$ALS = 0.43 \times (320.73 + 54.22 - 311.15) = 27.43\text{€}$$

After applying the lump sums and the CRDS, we obtain :

$$ALS = 22.11\text{€}$$

A.4 APL computation for Our Corner Case

$$APL = K \times (E - E_0)$$

Where :

- $K = 0.95 - \frac{R-r \times N}{cm \times N} = 0.95 - \frac{15000 - 1217.26 \times 1.8}{13393.40 \times 1.8} = 0,41$
- $E = 360\text{€}$ (the rent is below the rent limit in our corner case)

For E_0 , it is first necessary to multiply the tiers by the number of portions N , which in this case is 1.8, to obtain the brackets, before applying the percentages. This gives :

- 4% between 0€ and $1948.10 \times 1.8 = 3056.58\text{€}$
- 10,40% between 3056,58€ and $2678.71 \times 1.8 = 4821.68\text{€}$
- 21,60% between 4821,68€ and $3896.18 \times 1.8 = 7013.12\text{€}$
- 26,40% between 7013,12€ and $5357.44 \times 1.8 = 9643.39\text{€}$

- 32% between 9643,39€ and $6331.29 \times 1.8 = 11396.32\text{€}$
- 48% between 11396,32€ and 15000€

Hence:

$$E_0 = \frac{3735.48 + 45.57 \times 1.8}{12} = 318.13\text{€}$$

Therefore :

$$\text{APL} = 0.41 \times (360 - 318.13) = 17.17\text{€}$$

After applying the lump sums and the CRDS, we obtain :

$$\text{APL} = 12.06\text{€}$$