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Privacy Preserving Image Registration

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Abstract. Image registration is a key task in medical imaging applications, allowing to represent medical images in a common spatial reference frame. Current literature on image registration is generally based on the assumption that images are usually accessible to the researcher, from which the spatial transformation is subsequently estimated. This common assumption may not be met in current practical applications, since the sensitive nature of medical images may ultimately require their analysis under privacy constraints, preventing to share the image content in clear form. In this work, we formulate the problem of image registration under a privacy preserving regime, where images are assumed to be confidential and cannot be disclosed in clear. We derive our privacy preserving image registration framework by extending classical registration paradigms to account for advanced cryptographic tools, such as secure multi-party computation and homomorphic encryption, that enable the execution of operations without leaking the underlying data. To overcome the problem of performance and scalability of cryptographic tools in high dimensions, we first propose to optimize the underlying image registration operations using gradient approximations. We further revisit the use of homomorphic encryption and use a packing method to allow the encryption and multiplication of large matrices more efficiently. We demonstrate our privacy preserving framework in linear and non-linear registration problems, evaluating its accuracy and scalability with respect to standard image registration. Our results show that privacy preserving image registration is feasible and can be adopted in sensitive medical imaging applications.

Keywords: Image Registration · Privacy enhancing technologies · Trustworthiness

1 Introduction

Image Registration is a crucial task in medical imaging applications, allowing to spatially align imaging features between two or multiple scans. Image registration is a key component of state-of-the-art methods for atlas-based segmentation

[8,28], morphological and functional analysis [3,10], multi-modal data integration [15], and longitudinal analysis [4,23].

Overall, typical registration paradigms are based on a given transformation model (e.g. affine or non-linear), a cost function and an associated optimization routine. A large number of image registration approaches have been proposed in the literature over the last decades, covering a variety of assumptions underlying the spatial transformations, similarity metric, image dimensionality and optimization strategy [27].

While image registration is the workhorse of several real-life medical imaging software and services, current registration frameworks are based on the assumption that the image information content is accessible and can be freely manipulated to solve the optimization problem. This basic assumption is currently challenged by regulations and restrictions imposed by law, such as the European General Data Protection Regulation (GDPR) [2], or the US Health Insurance Portability and Accountability Act (HIPAA) [1]. Medical imaging information falls within the realm of personal health data [18] and its sensitive nature may ultimately require the analysis under privacy preserving constraints, for instance by preventing to share the image content in clear form. For this reason, current medical image analysis frameworks based on image-registration may not be compatible with today’s data protection scenarios of several countries.

Advanced cryptographic tools enabling data processing without disclosing it in clear hold great potential in sensitive data analysis problems (e.g., [17]). Examples of such approaches are Secure-Multi-Party-Computation (MPC) [30] and Homomorphic Encryption (HE) [24]. While MPC allows multiple parties to jointly compute a common function over their private inputs and discover no more than the output of this function, HE enables computation on encrypted data without disclosing neither the input data nor the result of the computation.

This work presents a new methodological framework allowing image registration under privacy constraints. To this end, we reformulate the typical image registration problem to integrate cryptographic tools, namely MPC or FHE, thus preserving the privacy of the image data. Due to the well known scalability issues of privacy preserving techniques, we investigate strategies for the practical use of privacy preserving image registration (PPIR) through gradient approximations, array packing and matrix partitioning. In our experiments we evaluate the effectiveness of PPIR in linear and non-linear registration problems. Our results demonstrate the feasibility of PPIR, and pave the way to its application in sensitive medical imaging applications.

2 Problem statement

Given images $I, J : \mathbb{R}^d \mapsto \mathbb{R}$, image registration aims at estimating the parameters \mathbf{p} of a spatial transformation $\mathbf{W}_{\mathbf{p}} \in \mathbb{R}^d \mapsto \mathbb{R}^d$, either linear or non-linear, maximizing the spatial overlap between J and the transformed image $I(\mathbf{W}_{\mathbf{p}})$. For example, a typical cost function to optimize the registration problem is the sum

of squared intensity differences (SSD) evaluated on the set of image coordinates:

$$\text{SSD}(I, J, \mathbf{p}) = \operatorname{argmin}_{\mathbf{p}} \sum_{\mathbf{x}} \left[I(\mathbf{W}_{\mathbf{p}}(\mathbf{x})) - J(\mathbf{x}) \right]^2 \quad (1)$$

Equation (1) can be typically optimized through gradient-based methods, where the parameters \mathbf{p} are iteratively updated until convergence. In particular, under a Gauss-Newton optimization scheme, the parameters update of the spatial transformation can be computed through Equation (2):

$$\Delta \mathbf{p} = H^{-1} \cdot \sum_{\mathbf{x}} S(\mathbf{x}) \cdot (I(\mathbf{W}_{\mathbf{p}}(\mathbf{x})) - J(\mathbf{x})), \quad (2)$$

where $S(\mathbf{x}) = \nabla I(\mathbf{x}) \frac{\partial \mathbf{W}_{\mathbf{p}}(\mathbf{x})}{\partial \mathbf{p}}$ quantifies image and transformation gradients, and $H = \sum_{\mathbf{x}} \left(\nabla I(\mathbf{x}) \frac{\partial \mathbf{W}_{\mathbf{p}}(\mathbf{x})}{\partial \mathbf{p}} \right)^T \left(\nabla I(\mathbf{x}) \frac{\partial \mathbf{W}_{\mathbf{p}}(\mathbf{x})}{\partial \mathbf{p}} \right)$ is the second order term obtained from Equation (1) through linearization [5, 21].

The solution of this problem requires the joint availability of both images I and J , as well as of the gradients of I and of $\mathbf{W}_{\mathbf{p}}$. In a privacy preserving setting, this information may not be available, and the computation of Equation (2) is therefore impossible. We thus consider a scenario with two parties, *party*₁, and *party*₂, whereby *party*₁ owns image I and *party*₂ owns image J . The parties wish to collaboratively optimize the image registration problem without disclosing their respective images to each other. We assume that only *party*₁ has access to the transformation parameters \mathbf{p} , and that is also in charge of computing the update at each optimization step. In particular, to compute the registration update $\Delta \mathbf{p}$ of Equation (2), the only operation requiring the joint availability of information from both parties is the term $R = \sum_{\mathbf{x}} S(\mathbf{x}) \cdot J(\mathbf{x})$, which can be computed as a matrix-vector multiplication on vectorized quantities, $R = S^T \cdot J$.

3 Methods

Before presenting PPIR in Section 3.2, we introduce in Section 3.1 the cryptographic tools underlying the proposed framework.

3.1 Secure Computation

Secure Multi-Party Computation. Introduced by Yao in [30], MPC is a cryptographic tool that allows multiple parties to jointly compute a common function over their private inputs (secrets) and discover no more than the output of this function. Among existing MPC protocols, additive secret sharing consists of first splitting every secret s into additive shares $\langle s \rangle_i$, such that $\sum_{i=1}^n \langle s \rangle_i = s$, where n is the number of collaborating parties. Each party i receives one share $\langle s \rangle_i$, and executes an arithmetic circuit in order to obtain the final output of the function. In this paper, we adopt the two-party computation protocol defined in SPDZ [11], whereby the actual function is mapped into an arithmetic

circuit and all computations are performed within a finite ring with modulus Q . Additions consist of locally adding shares of secrets, while multiplications require interaction between parties. Following [11], SPDZ defines a dedicated MPCMUL operation to compute matrix-vector multiplication within a secure two-party protocol. **Homomorphic Encryption.** Initially introduced by Rivest et al. in [24], HE enables the execution of operations over encrypted data without disclosing neither the input data, nor the result of the computation. Hence, party 1 encrypts the input with her public key and sends this encryption to party 2. Party 2, in turn, evaluates a circuit over this encrypted input and sends the result, which still remains encrypted, back to party 1 which can finally decrypt the result. Among various HE schemes, CKKS [9] supports the execution of all operations over encrypted real values and is considered as a fully homomorphic encryption (FHE). With CKKS, an input vector is mapped to a polynomial and further encrypted with a public key in order to obtain a pair of polynomials $c = (c_0, c_1)$. The original function is further mapped into a set of operations that are supported by CKKS, which are executed over c . The performance and security of CKKS depends on multiple parameters including the degree of the polynomial N , which is usually sufficiently large (e.g. $N = 4096$, or $N = 8192$).

3.2 PPIR: Privacy preserving image registration

In order to ensure the privacy of images I and J against $party_2$ and $party_1$ respectively, we propose to investigate the use of MPC and FHE to develop PPIR. Figure 1 illustrates how these two cryptographic tools are employed to ensure the privacy of the images during registration. As previously mentioned, the only operation that needs to be jointly executed by the parties in a privacy preserving manner is the matrix-vector multiplication: $R = S^T \cdot J$, where S^T is only known to $party_1$, and J to $party_2$.

When MPC is integrated (Figure 1a), $party_1$ secretly shares the matrix S^T to obtain $(\langle S_1 \rangle, \langle S_2 \rangle)$, while $party_2$ secretly shares the image J to obtain $(\langle J_1 \rangle, \langle J_2 \rangle)$. Each party further receives its corresponding share, namely: $party_1$ holds $(\langle S_1 \rangle, \langle J_1 \rangle)$ and $party_2$ holds $(\langle S_2 \rangle, \langle J_2 \rangle)$. Parties further execute a circuit with the MPCMUL operations to compute the 2-party dot product between S^T and J . The parties further synchronize to let $party_1$ to obtain the product, and to finally calculate Δp (see Equation (2)).

When using FHE (Figure 1b), $party_2$ uses a FHE key k to encrypt J and obtain: $\llbracket J \rrbracket \leftarrow \text{ENC}(k, J)$. This encrypted image is sent to $party_1$, who computes the encrypted result $\llbracket R \rrbracket$ of the matrix-vector multiplication. In this framework, only the vector J is encrypted, and therefore $party_1$ executes scalar multiplications and additions in the encrypted domain only (which are less costly than multiplications over two encrypted inputs). The encrypted result $\llbracket R \rrbracket$ is sent back to $party_2$, which can obtain the result through decryption: $R = \text{DEC}(k, \llbracket R \rrbracket)$. Finally, $party_1$ receives R in clear form and can therefore compute Δp .

Thanks to the privacy and security guarantees of these cryptographic tools, during the entire registration procedure the content of the image data S and I is

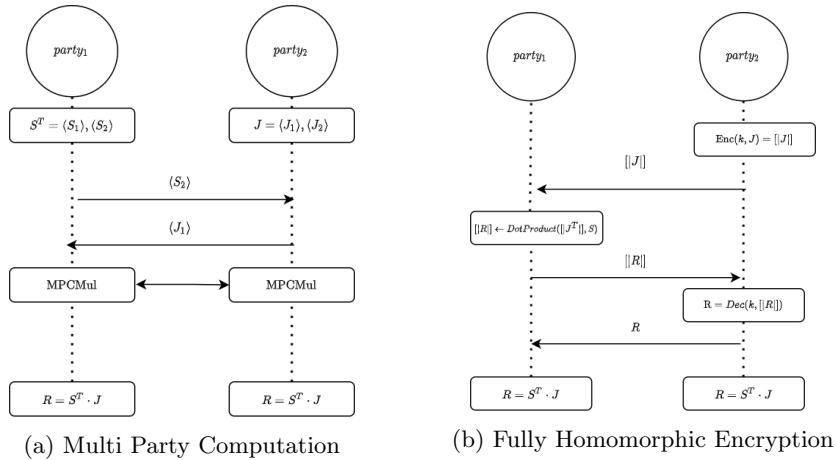


Fig. 1: Proposed framework to compute the matrix-vector multiplication $S^T \cdot J$ relying on MPC and FHE.

never disclosed to the opposite party. Nevertheless, effectively optimizing Equation (1) with MPC or FHE is particularly challenging, due to the computational bottleneck of these techniques when applied to large dimensional objects [7, 14], notably affecting computation time and communication bandwidth between parties. To tackle this issue, in what follows we introduce in the schemes of Figure 1 computational strategies to effectively reduce the dimensionality of the image information through sampling, and to improve the scalability of the algebraic operations when using these cryptographic tools.

Gradient sampling. The update of Equation (2) is computed on the vectorized images, which are large-dimensional arrays representing all the image pixels (or voxels). Since the registration gradient is in general mostly driven by a fraction of the image content, e.g. image boundaries in case of the SSD metric, a reasonable approximation of Equation (2) can be obtained by assessment on relevant image locations only. This idea has been introduced in medical image registration [19, 26, 29], and is here adopted to reduce the dimensionality of the arrays on which encryption is performed. In our works we test two different techniques: (i): Uniformly Random Selection (URS), proposed by [19, 29], in which a random subset of dimension $l \leq s$ of spatial coordinates is sampled at every iteration with uniform probabilities, $Pr(\mathbf{x}) = \frac{1}{s}$; and (ii): Gradient Magnitude Sampling (GMS) [26], consisting in sampling a subset of coordinates with probability proportional to the norm of the image gradient, $Pr(\mathbf{x}) \sim \|\nabla I(\mathbf{x})\|$.

Matrix partitioning in FHE. In addition to gradient sampling, we propose a specific optimization dedicated to PPIR with FHE, in particular when the CKKS algorithm is adopted. CKKS allows packing multiple inputs into a single ciphertext to decrease the number of homomorphic operations. In order to optimize the matrix-vector multiplication, we propose to partition the image

vector J into K sub-arrays of dimension D , and the matrix S^T into K submatrices of dimension $|\mathbf{p}| \times D$. Once all sub-arrays J_i are encrypted, we propose to iteratively apply the (DOTPRODUCT) proposed by [7] between each sub-matrix and corresponding sub-array; these intermediate results are then summed up to obtain the final result, namely: $\llbracket R \rrbracket = \sum_{i=0}^K \text{DOTPRODUCT}(\llbracket J_i^T \rrbracket, S_i) = S^T \cdot \llbracket J \rrbracket$.

4 Experimental Results

We demonstrate and assess PPIR in two examples based on linear and non-linear alignment of respectively positron emission tomography (PET) and anatomical magnetic resonance (MR) images.

Dataset. PET data consists of 18-Fluoro-Deoxy-Glucose (^{18}FDG) whole body Positron Emission Tomography (PET). The images here considered are a frontal view of the maximum intensity projection reconstruction, obtained by 2D projection of the voxels with highest intensity across views (1260×1090 pixels).

MR images are obtained from brain scans of the Alzheimer’s Disease Neuroimaging Initiative [20]. Images underwent a standard processing pipeline to estimate grey matter density maps [3]. The subsequent registration experiments are performed on the extracted mid-coronal slice, of dimension 121×121 pixels.

Implementation. PET image alignment was performed by optimizing the transformation \mathbf{W}_p of Equation (1) with respect to affine registration parameters. The registration of brain grey matter density images was performed by non-linear registration based on a cubic spline model (one control point every five pixels along both dimensions). For both affine and non-linear cases, the registration was performed between two randomly selected patients’ images.

Concerning the PPIR framework with the affine transformation, tests are carried for both MPC and FHE by considering the entire images, and by using gradient approximation techniques (Section 3). The sampling seed for gradient approximation is the same for each test. Due to the smaller dimension of the brain grey matter images, non-linear PPIR with cubic-splines is applied directly to the full data. For MPC we set as prime modulus $Q = 2^{32}$. For FHE, we define the polynomial degree modulus as $N = 4096$, and set the resizing parameter D to optimize the trade-off between runtime and bandwidth. Since D needs to be a divider of the image size, for PET image data we set $D = 128$, while for the grey matter images we set $D = 121$. The PPIR framework is implemented using two state-of-the-art libraries: PySyft [25] supporting SPDZ’s two-party computation, and TenSeal [7] for CKKS. All the experiments are executed on a laptop with an Intel CPU x86-64 architecture (@ 1.90GHz \times 4) using 32GB of RAM. For each registration configuration, the optimization is repeated 10 times, to account for the random generation of the MPC shares and FHE encryption keys.

The quality of PPIR is assessed by comparing the registration results with respect to the ones obtained with standard registration on clear images (CLEAR). The metrics considered are the image intensity difference at the optimum, the overall number of iterations required to converge, and the displacement root mean square difference (RMSE) between CLEAR and PPIR. We also evaluate

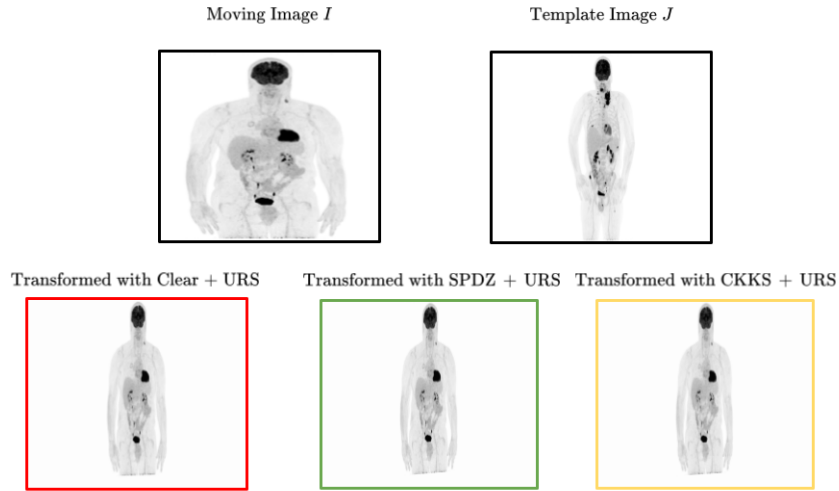


Fig. 2: Qualitative results for affine registration. The red frame is the transformed moving image using CLEAR+URS registration. Green and Yellow frames are the transformed images using respectively MPC+URS and FHE+URS PPIR. The yellow image is the transformed moving using PPIR with CKKS.

the performance of PPIR in terms of average computation (running time) and communication (bandwidth) across iterations.

Results. Table 1 (Registration metrics) shows that affine PPIR through SPDZ leads to negligible differences with respect to CLEAR in terms of number of iterations, intensity and displacement. Registration with CKKS is instead not possible when considering the entire images, due to computational complexity, and is also associated to generally larger approximations when using URS and GMS. Nevertheless, Figure 2 shows that neither MPC nor FHE do decrease the overall quality of the affine registered images. Additional registration results are available in Appendix. Table 1 (Efficiency metrics) shows that SPDZ performed on the full images has highest computation time and communication bandwidth. These figures sensibly improve when using URS or GMS, by factors 10x and 20x for respectively time and bandwidth. Concerning CKKS, we note the uneven time and bandwidth requirements between clients, due to the asymmetry of encryption operations and communication protocol (Figure 1).

Finally, Table 2 reports the metrics for the non-linear registration test. Concerning registration accuracy, we draw similar conclusions to affine case, where SPDZ leads to minimum differences with respect to CLEAR and CKKS seems slightly inferior. Interestingly, SPDZ is associated to sensibly higher execution time and computation bandwidth due to the larger number of parameters of the cubic splines, affecting the size of the matrix S^T .

Table 1: Affine registration test. Registration metrics are reported as mean and standard deviation. Efficiency metrics in terms of average across iterations. RMSE: root mean square error.

Affine Registration metrics				
Solution	Intensity Error (SSD)	Num. Iteration	Displacement RMSE CLEAR vs PPIR (<i>mm</i>)	
CLEAR	4.31 ± 0.0	100 ± 0.0	-	
SPDZ	4.31 ± 0.0	91.8 ± 0.42	5.91 ± 0.14	
CKKS	x	x	x	
CLEAR + URS	4.32 ± 0.0	99.70 ± 4.25	-	
SPDZ + URS	4.31 ± 0.0	103.60 ± 4.67	12.17 ± 13.35	
CKKS (<i>D</i> = 128) + URS	4.48 ± 0.10	100.67 ± 3.32	19.54 ± 8.60	
CLEAR + GMS	4.31 ± 0.0	106 ± 0.0	-	
SPDZ + GMS	4.32 ± 0.0	101.10 ± 5.38	5.39 ± 2.29	
CKKS (<i>D</i> = 128) + GMS	4.36 ± 0.05	99 ± 4.27	13.64 ± 4.20	
Efficiency metrics				
Solution	Time <i>party</i> ₁ (s)	Time <i>party</i> ₂ (s)	Comm. <i>party</i> ₁ (MB)	Comm. <i>party</i> ₂ (MB)
CLEAR	0.0	0.0	-	-
SPDZ	0.73	0.73	14.15	14.15
CKKS	x	x	x	x
CLEAR + URS	0.0	0.0	-	-
SPDZ + URS	0.06	0.06	0.52	0.52
CKKS (<i>D</i> = 128) + URS	0.19	0.0	0.06	0.46f
CLEAR + GMS	0.0	0.0	-	-
SPDZ + GMS	0.07	0.07	0.54	0.54
CKKS (<i>D</i> = 128) + GMS	0.19	0.0	0.06	0.46

Table 2: Non-linear registration test. Registration metrics are reported as mean and standard deviation. Efficiency metrics in terms of average across iterations. RMSE: root mean square error.

Cubic splines Registration metrics				
Solution	Intensity Error (SSD)	Num. Iteration	Displacement RMSE CLEAR vs PPIR (<i>mm</i>)	
CLEAR	6.73 ± 0.0	413 ± 0.0	-	
SPDZ	6.73 ± 0.1	413.70 ± 0.48	1.34 ± 0.08	
CKKS	6.40 ± 0.07	183 ± 17.19	1.15 ± 0.27	
Cubic splines Efficiency metrics				
Solution	Time <i>party</i> ₁ (s)	Time <i>party</i> ₂ (s)	Comm. <i>party</i> ₁ (MB)	Comm. <i>party</i> ₂ (MB)
CLEAR	0.0	0.22 ± 0.02	-	-
SPDZ	0.53	0.53	16.32	20.12
CKKS	0.17	0.17	0.06	0.07

5 Conclusion

This work introduces privacy preserving image registration (PPIR), a novel framework to allow image registration when images are confidential and cannot be disclosed in clear. PPIR is developed with MPC and FHE and implements effective strategies to mitigate their known computational and communication overhead. PPIR is demonstrated and evaluated through a series of quantitative benchmarks in both linear and non-linear image registration problems. Our results highlight the existing trade-off between registration performance and efficiency of the different PPIR schemes.

Future extensions of this work will be devoted to the benchmarking of our framework in more general scenarios, involving 3D medical image data and multimodal registration problem. The application to multimodal data will require the extension of our framework to account for different similarity metrics, such as

Mutual Information or Normalized Cross-Correlation [22, 29]. Moreover, the effectiveness of sampling through URS and GMS motivates the adoption of sparse image registration frameworks, especially for non-linear registration [12, 13]. Another relevant research direction concerns the development of PPIR in deep-learning based approaches [6, 16].

Overall, this study shows that PPIR is feasible and can therefore be adopted in sensitive medical imaging applications.

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