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Correction to "Adaptive Control of Robot Manipulators with Flexible Joints"

B. Brogliato and R. Lozano

I. INTRODUCTION

The above paper¹ contains two flaws that were recently brought to our attention by Hsu [1]. 1) The first mistake concerns the definition of the signal q_{2d} in (6) and (C.20). At time t=0, the term $q_{2d}(0)$ appears on both sides of the equalities in (6) and (C.20). Hence the initial conditions on the state and on the desired trajectory q_{1d} and its

first and second derivatives are constrained. 2) The second mistake is that the regressor matrix Y_4 in (C.18) contains integral terms which are not shown to be bounded. Consequently, the stability analysis in Appendix C [(C.42)–(C.47)], based on some signal chasing, is not complete.

ullet Concerning point 1), it has been shown in [2] that the positive definite function V in (3) can be modified to

$$V = \frac{1}{2}v_1^T D(q_1)v_1 + \frac{1}{2}v_2^T J_m v_2 + \frac{1}{2}(\tilde{q}_1 - \tilde{q}_2)^T K(\tilde{q}_1 - \tilde{q}_2)$$
 (1)

so that q_{2d} is now defined as (see [2, (23)])

$$q_{2d} = q_{1d} + K^{-1}(D(q_1)\ddot{q}_{1r} + C(q_1, \dot{q}_1)\dot{q}_{1r} + g(q_1) - B_1v_1)$$

where $B_1=B_1^T>0$ is a constant feedback gain. This allows us to remove the constraint on the initial conditions and to prove exponential Lyapunov stability of the fixed parameters scheme; see [2]. In the adaptive case, the signal q_{2d} in (C.20) can be modified as well to avoid the initial conditions' constraints problem. Indeed the term $K\int_0^t (v_1-v_2)dt$ in the right-hand side of (C.1) is replaced by $K(\tilde{q}_1-\tilde{q}_2)$. Then w_5 in (C.2), (C.5), and (C.20) is modified to $w_5=-q_{1d}$. This does not affect the definition of the other terms in (C.20) since only w_5 has been modified.

Another possible solution was suggested to us [1], presented here in the nonadaptive case (compare with [3, (3) and (6)])

$$V = \frac{1}{2}v_1^T D(q_1)v_1 + \frac{1}{2}v_2^T J_m v_2 + \frac{1}{2}z^T Kz$$
 (3)

where z and q_{2d} are defined as

$$q_{2d} = q_{1d} - \lambda x + K^{-1}(-v_1 + D(q_1)\ddot{q}_{1r} + C(q_1, \dot{q}_1)\dot{q}_{1r} + g(q_1))$$
(4)

$$\dot{q}_{1r} := \dot{q}_{1d} - \lambda \tilde{q}_1 \tag{5}$$

$$\dot{x} := \tilde{q}_1 - \tilde{q}_2 \tag{6}$$

$$z = \lambda x + (\tilde{q}_1 - \tilde{q}_2) \quad (\dot{z} = v_1 - v_2)$$
 (7)

$$u = -v_2 - J_m[-\ddot{q}_{2d} + \lambda \dot{\tilde{q}}_2] - K[q_{1d} - q_{2d} - \lambda x]. \tag{8}$$

Proof: Consider $V(v_1, v_2, z)$ as given by (3). Differentiating (3) we obtain

$$\dot{V} = v_1^T [D\dot{v_1} + Cv_1 + Kz] + v_2^T [J_m v_2 - Kz]$$
(9)

where we have used property P3 of [3] and the fact that [from (6) and (7)] $\dot{z}=v_1-v_2$. Now, closely following [3, Appendix B]

$$D\dot{v_1} + Cv_1 + Kz = \tag{10}$$

$$-g - K(q_1 - q_2) + D[-\ddot{q}_{1d} + \lambda \dot{q}_1] + C[-\dot{q}_{1d} + \lambda \tilde{q}_1] + Kz =$$

$$-g - K(q_1 - q_2) + D[-\ddot{q}_{1d} + \lambda \dot{q}_1]$$
(11)

$$-g - K(q_1 - q_2) + D(-q_{1d} + \lambda q_1) + C[-\dot{q}_{1d} + \lambda \tilde{q}_1]$$

$$+K[\lambda x + (q_1 - q_2) - (q_{1d} - q_{2d})] =$$
 (12)

$$Kq_{2d} + \{-g - D\ddot{q}_{1r} - C\dot{q}_{1r} - K[\lambda x - q_{1d}]\}.$$
 (13)

The last term within braces is the new w_1 , using the notation of Appendix B of the original paper. From (4), obtained by requiring the expression in (13) to be equal to $-v_1$, we then have

$$\dot{V} = -v_1^T v_1 + v_2^T [J_m \dot{v_2} - K(\lambda x + (\tilde{q}_1 - \tilde{q}_2))]. \tag{14}$$

The last term within brackets is the new w_2 , following our original notation. After some manipulations using the robot motor equations, one gets

$$w_2 = u + J_{m}[-\ddot{q}_{2d} + \lambda \dot{\tilde{q}}_{2}] + K[q_{1d} - q_{2d} - \lambda x].$$
 (15)

Then, as in [3], setting $w_2 = -v_2$, one obtains (8). Consequently, the proposed control law yields (as in [3])

$$\dot{V} = -v_1^T v_1 - v_2^T v_2 \tag{16}$$

which is semi-definite negative as required.

• Concerning point 2): Fundamentally, the flaw comes from the fact that to be able to define signals q_{2d} , \dot{q}_{2d} which are measurable and \ddot{q}_{2d} that does not depend on \ddot{q}_2 (so that the control input in (14) is well defined), we need to filter the first dynamical equation (1) to suitably parameterize Dv_1 in (C.18). In the above paper we filtered (1) with an integrator, hence the possible unboundedness of the regressor Y_4 in (C.18). We now propose to use a first-order filter with transfer function $\frac{1}{s+1}$ instead of the integrator.

Applying the filter to (1) one gets (we drop the arguments for convenience)

$$\frac{1}{s+1} \{ D\ddot{q}_1 + C\dot{q}_1 + g + K(q_1 - q_2) \} = 0.$$
 (17)

Now we have

$$\begin{split} \frac{1}{s+1} \{D\ddot{q}_1\} &= D\dot{q}_1 - D(0)\dot{q}_1(0) - \frac{1}{s+1} \\ &\times \{D\dot{q}_1 - D(0)\dot{q}_1(0)\} - \frac{1}{s+1} \{\dot{D}\dot{q}_1\}. \end{split} \tag{18}$$

Indeed (18) can be obtained by first noting that $D\ddot{q}_1=rac{d}{dt}(D\dot{q}_1)-\dot{D}\dot{q}_1$. Now

$$\frac{1}{s+1} \{ D\ddot{q}_1 \} = \int_0^t e^{-(t-\tau)} D\ddot{q}_1 d\tau. \tag{19}$$

Then using integration by parts one gets

$$\frac{1}{s+1} \{ D\ddot{q}_1 \}
= e^{-t} \left[\left[e^{\tau} \left(D\dot{q}_1 - D(0)\dot{q}_1(0) - \int_0^{\tau} \dot{D}\dot{q}_1 dy \right) \right]_0^t \right.
\left. - \int_0^t e^{\tau} \left(D\dot{q}_1 - D(0)\dot{q}_1(0) - \int_0^{\tau} \dot{D}\dot{q}_1 dy \right) d\tau \right]$$
(20)

which finally yields

$$\frac{1}{s+1} \{ D\ddot{q}_1 \}
= D\dot{q}_1 - D(0)\dot{q}_1(0) - \int_0^t \dot{D}\dot{q}_1 d\tau - \int_0^t e^{-(t-\tau)}
\times \left(D\dot{q}_1 - D(0)\dot{q}_1(0) - \int_0^\tau \dot{D}\dot{q}_1 dy \right) d\tau.$$
(21)

Using the fact that (still integrating by parts)

$$\int_0^t e^{-(t-\tau)} \dot{D} \dot{q}_1 d\tau$$

$$= \int_0^t \dot{D} \dot{q}_1 d\tau - \int_0^t e^{-(t-\tau)} \left(\int_0^\tau \dot{D} \dot{q}_1 dy \right) d\tau \qquad (22)$$

we then get (18) by combining (21) and (22).

Now from (17) and (18) we have

Hom (17) and (18) we have
$$D\dot{q}_1 = D(0)\dot{q}_1(0) + \frac{1}{s+1} \{D\dot{q}_1 - D(0)\dot{q}_1(0)\} + \frac{1}{s+1} \{\dot{D}\dot{q}_1\} - \frac{1}{s+1} \{C\dot{q}_1 + g + Kq_1\} + \frac{1}{s+1} \{Kq_2\}. \tag{23}$$

The terms between brackets can be written as $Y_i(q_1,\dot{q}_1)\theta_i$ for some constant vector θ_i . Hence $\frac{1}{s+1}$ $\{Y_i(q_1,\dot{q}_1)\theta_i\}=\frac{1}{s+1}\{Y_i(q_1,\dot{q}_1)\}\theta_i\triangleq Y_{if}\theta_i$ with $\dot{Y}_{if}+Y_{if}=Y_i(q_1,\dot{q}_1)$. It follows that (C.18) can be written as

$$Dv_1 = Y_{4f}\theta_4 \tag{24}$$

with $\dot{Y}_{4f}+Y_{4f}=Y_4$ for some $Y_4(q_1,\dot{q}_1,q_2)$. Note also that q_{2d},\dot{q}_{2d} in (C.20) can be computed from position and velocities measurements only which is crucial for the algorithm to be implementable. From the new parameterization, it follows that if q_1 , \dot{q}_1 and q_2 are bounded, so is Y_4 . This was not the case when integrators were used.

The stability analysis is much simplified. Note first that the modification of $Y_4\theta_4$ leaves the rest of the analysis and algorithm unchanged. Hence from (C.41), q_1 and \dot{q}_1 are bounded. From (23) it follows that $q_{2f}=\frac{1}{2+1}\{q_2\}$ is bounded. Hence from (C.20) q_{2d} is bounded, and consequently q_2 and \ddot{q}_1 are bounded. Boundedness of \dot{q}_2 follows by differentiating (C.20) which proves that \dot{q}_{2d} is bounded. Hence from (C.41) \dot{q}_2 is bounded. Boundedness of u can be inferred by inspecting (C.27) and (C.32). Consequently \ddot{q}_2 is bounded also.

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