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# Control of Ca<sup>2+</sup> signals by astrocyte nanoscale morphology at tripartite synapses

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- <sup>12</sup> Abstract Astrocytic Ca<sup>2+</sup> signals regulate synaptic activity. Most of those signals are spatially
- restricted to microdomains and occur in fine processes that cannot be resolved by
- diffraction-limited light microscopy, restricting our understanding of their physiology. Those fine
- <sup>15</sup> processes are characterized by an elaborate morphology, forming the so-called spongiform
- domain, which could, similarly to dendritic spines, shapes local Ca<sup>2+</sup> dynamics. Because of the technical limitations to access the small spatial scale involved, the effect of astrocyte morphology
- technical limitations to access the small spatial scale involved, the effect of astrocyte morphology on  $Ca^{2+}$  microdomain activity remains poorly understood. Here, we use computational tools and
- <sup>18</sup> on  $Ca^{2+}$  microdomain activity remains poorly understood. Here, we use computational tools and <sup>19</sup> realistic 3D geometries of fine processes based on recent super-resolution microscopy data to
- realistic 3D geometries of fine processes based on recent super-resolution microscopy data to
   investigate the mechanistic link between astrocytic nanoscale morphology and local Ca<sup>2+</sup> activity.
- $_{20}$  investigate the mechanistic link between astrocytic nanoscale morphology and local Ca<sup>2+</sup> activity.  $_{21}$  Simulations demonstrate that the nano-morphology of astrocytic processes powerfully shapes
- Simulations demonstrate that the nano-morphology of astrocytic processes powerfully shape: the spatio-temporal properties of  $Ca^{2+}$  signals and promotes local  $Ca^{2+}$  activity. The model
- <sup>22</sup> predicts that this effect is attenuated upon astrocytic swelling, hallmark of brain diseases, which
- we confirm experimentally in hypo-osmotic conditions. Upon repeated neurotransmitter release
- events, the model predicts that swelling hinders astrocytic signal propagation. Overall, this study
- highlights the influence of the complex morphology of astrocytes at the nanoscale and its
- <sup>27</sup> remodeling in pathological conditions on neuron-astrocyte communication at tripartite synapses.

## <sup>29</sup> Introduction

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Astrocytes are glial cells of the central nervous system that are essential for brain develop-30 ment and function, playing key roles in e.g ion homeostasis, neurotransmitters uptake and lactate 31 metabolism (see (Verkhratsky and Nedergaard, 2018) for more details). Furthermore, astrocytes 32 can modulate neuronal communication at synapses. In response to the release of neurotransmit-33 ters from neurons.  $Ca^{2+}$  signals are observed in astrocytes, which can trigger the release of neu-34 roactive molecules by the astrocyte, gliotransmitters. The first type of astrocytic  $Ca^{2+}$  signals that 35 has been observed was  $Ca^{2+}$  waves that propagate through gap junctions in astrocyte networks (*Gi*-36 *aume and Venance, 1998*). Ca<sup>2+</sup> waves are also observed within the branches of single astrocytes. 37 sporadically propagating to the soma (Haustein et al., 2014; Bindocci et al., 2017). The recent de-38 velopment of  $Ca^{2+}$  imaging techniques that provide better spatial and temporal resolution has re-39 vealed the existence of spatially-restricted Ca<sup>2+</sup> signals in astrocytes, referred to as microdomains 40

or hotspots (Di Castro et al., 2011: Panatier et al., 2011: Stobart et al., 2018a: Srinivasan et al., 2015: Shigetomi et al., 2013: Sherwood et al., 2017: Otsu et al., 2015: Lind et al., 2013: Bindocci 42 et al., 2017: Agarwal et al., 2017: Arizono et al., 2020). Those local Ca<sup>2+</sup> signals account for as 43 much as 80 % of astrocytic  $Ca^{2+}$  activity and occur in fine astrocytic processes, also referred to as branchlets, which occupy 75 % of the astrocytic volume (*Bindocci et al.*, 2017), referred to as the 45 spongiform domain or gliapil. Given that one astrocyte can contact tens of thousands of synapses simultaneously in the mouse hippocampus (Bushong et al. 2002) and up to two million in the human brain (Oberheim et al., 2006) through these fine processes, local, fast Ca<sup>2+</sup> signals might 48 enable the astrocyte to powerfully yet precisely control the flow of information through synaptic 40 circuits. 50

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Elaborate cellular morphologies lend themselves to the fine compartmentalization of signals. 52 For example, the anatomical design of dendritic spines restricts the spread of  $Ca^{2+}$  to the acti-53 vated synapse, ensuring that there is little cross-talk between different synapses and that the local 54 Ca<sup>2+</sup> concentration can go very high (Santamaria et al., 2011: Tønnesen et al., 2014: Yuste et al., 55 2000: Noguchi et al., 2005: Yasuda, 2017: Holcman and Schuss, 2011). It is thus likely that the 56 complex organization of the reticular structure of astrocytes plays a key role in shaping local  $Ca^{2+}$ 57 microdomains (*Rusakov, 2015*). For example, the complex shape of Bergmann glia has been pro-68 posed to potentially restrict  $Ca^{2+}$  signals to the vicinity of synapses (*Grosche et al., 1999*). Similarly, 59 perisynaptic enlargements called "astrocytic compartments" along major branches of astrocytes 60 also exhibit Ca<sup>2+</sup> signals (*Panatier et al., 2011*). Fine processes of the spongiform domain. however, 61 cannot be resolved by diffraction-limited light microscopy (Rusakov, 2015), so that the contribution 62 of their nanoscale morphology to shaping local  $Ca^{2+}$  signals is poorly understood. Our recent 3D 63 super-resolution Stimulated Emission Depletion (STED) microscopy study (Arizono et al., 2020) re-64 vealed that particular shapes of the complex meshwork of astrocytic processes, reminiscent of 65 dendritic spines, are associated with compartmentalized  $Ca^{2+}$  signals. Furthermore, aberrant  $Ca^{2+}$ 66 signals (Shigetomi et al., 2019) and changes in astrocytic morphology, such as "astrocytic swelling". 67 occur in pathological conditions such as brain injury, including ischemic, traumatic, hemorrhagic 68 and metabolic injuries, stroke and epilepsy (Lafrenave and Simard, 2019). Interestingly, our recent STED study reported that swelling can also occur at the level of fine astrocytic processes (Arizono 70 et al., 2021a). The effect of such a remodeling of astrocytic nano-morphology on the local  $Ca^{2+}$ 71 signals involved in regulating synapses yet remains unclear. Together, there is a great interest 72 in understanding the mechanistic link between the nano-morphology of astrocytic processes and 73 Ca<sup>2+</sup> profiles in health and disease. Changing cell morphology experimentally is not straightforward 74 and can affect cell physiology, notably when the osmolarity of the extracellular space is altered. By 75 contrast, computational approaches can finely tune geometrical properties, resulting in more con-76 trolled investigations than what could be done experimentally. Computational models are thus 77 tools of choice to investigate the isolated impact of morphological parameters on  $Ca^{2+}$  dynamics. 78 Here, we use computational tools to investigate the effect of astrocyte nanoscale morphology 70 on local  $Ca^{2+}$  activity, in healthy and swelling conditions. To account for the stochasticity of molec-80 ular interactions in small volumes such as those of astrocyte processes, we use the stochastic 81 voxel-based model of  $Ca^{2+}$  signals from Denizot et al. (Denizot et al., 2019a). Idealized geome-82 tries of branchlets were designed based on super-resolution microscopy images recently reported 83 in live tissue (Arizono et al., 2020). Branchlets consist in alternations of structures referred to as 84 nodes and shafts. At this spatial scale, swelling resulting from hypo-osmotic conditions results in 85 an increased diameter of shafts, without altering node morphology (see Fig 3 from (Arizono et al., 86 **2021***b*)). To explore how such changes in morphology affect  $Ca^{2+}$  signalling, we performed simula-87 tions in geometrical models of branchlets of varving shaft widths. Our simulation results suggest 88 that astrocyte swelling results in an increased diffusion flux, which decreases  $Ca^{2+}$  peak probabil-89 ity, duration and amplitude in the stimulated and neighboring nodes. To test those predictions, 90 we performed Ca<sup>2+</sup> recordings in organotypic hipppocampal cultures in hypo-osmotic conditions.

- <sup>92</sup> which result in increased shaft width without altering node width. Ca<sup>2+</sup> activity in hypo-osmotic
- <sup>93</sup> conditions was decreased compared to Ca<sup>2+</sup> activity in healthy tissue, in line with our model pre-
- dictions. In case of repeated node stimulation, thin shafts allowed signal propagation even if some
- stimuli were omitted. Thin shafts thus allow for more robust signal propagation within the gliapil,
- <sup>96</sup> which is hindered in swelling conditions.
- 97

Overall, this study sheds light on the influence of the nanoscale morphology of the complex spongiform domain of astrocytes on  $Ca^{2+}$  microdomain activity. Importantly, our results provide evidence that node compartmentalization, resulting from a reduced diffusion efflux from nodes connected to thin shafts, can increase  $Ca^{2+}$  activity locally. Our study indicates that pathological changes in nanoscale astrocyte morphology may substantially affect their  $Ca^{2+}$  activity.

#### 103 Results

#### <sup>104</sup> Geometrical representation of typical astrocyte processes

In order to investigate the effect of astrocyte nanoscale morphology on the spatio-temporal 105 properties of  $Ca^{2+}$  signals, we have designed geometries of typical astrocyte processes, derived 106 from the recent characterization of their ultrastructure at a high spatial resolution (50 nm in x-107 v) in organotypic hippocampal culture as well as in acute slices and *in vivo* (Arizono et al., 2020). 108 Geometries consist of alternations of bulbous structures, nodes, connected to each other with 100 cylindrical structures, referred to as shafts. To reproduce the morphological changes of processes 110 associated with cell swelling reported in hypo-osmotic conditions (Fig 3 in (Arizono et al., 2021b)). 111 geometries with different shaft width  $d_{\text{shaft}}$  and constant node width were designed (Fig 1A). In 112 accordance with node-shaft structures observed experimentally (Arizono et al., 2020), node width 113 was set to 380 nm. To model astrocytic  $Ca^{2+}$  activity with a high spatial resolution while taking into 114 account the randomness of reactions in small volumes, we used the stochastic voxel-based model 115 from Denizot et al. (Denizot et al., 2019a) (see Methods). The reactions included in the model 116 are presented in Fig 1B and in the Methods section. As the majority of  $Ca^{2+}$  signals in astrocytes 117 result from the opening of Inositol 3-Phosphate receptors ( $IP_{2}Rs$ ), located at the membrane of the 118 endoplasmic reticulum (ER) (Srinivasan et al., 2015), signals in the model result from the opening 119 of IP<sub>2</sub>Rs (see Denizot et al. (Denizot et al., 2019a) for discussion on the model's assumptions and 120 limitations). 121



Figure 1. Geometries and kinetic scheme used for simulating  $Ca^{2+}$  dynamics in node/shaft structures of the gliapil. (A) Geometries reproducing node/shaft geometries of the gliapil (*Arizono et al., 2020; Panatier et al., 2014*) were designed. Nodes are approximated as spheres of diameter 380 nm and shafts as 1µm-long cylinders. The geometries designed in this study, referred to as "5 nodes", contain 5 identical nodes and 4 identical shafts. Geometries were characterized by different shaft widths:  $d_{shaft} = d_0 = 380nm$ ,  $d_{shaft} = \frac{d_0}{2}$  and  $d_{shaft} = \frac{d_0}{3}$ . The associated cytosolic volume, plasma and ER membrane areas are presented in Table 1. (*B*) Biochemical processes included in the model.  $Ca^{2+}$  can enter/exit the cytosol from/to the extracellular space or the endoplasmic reticulum (ER), resulting from the activity of  $Ca^{2+}$  channels/pumps.  $Ca^{2+}$  and IP<sub>3</sub> diffuse in the cytosol following Brownian motion. The kinetics of *IP*<sub>3</sub>*R* channels corresponds to the 8-state Markov model from (*Denizot et al., 2019b*), adapted from (*De Young and Keizer, 1992; Bezprozvanny et al., 1991*). When both IP<sub>3</sub> and  $Ca^{2+}$  are bound to IP<sub>3</sub>*R* activating binding sites, the IP<sub>3</sub>*R* is in open state and  $Ca^{2+}$  enters the cytosol.  $Ca^{2+}$  can activate Phospholipase C  $\delta$  (PLC $\delta$ ), which results in the production of IP<sub>3</sub>. For more details, please refer to (*Denizot et al., 2019b*). Neuronal stimulation is simulated as an infusion of IP<sub>3</sub> in the cytosol and the opening of  $Ca^{2+}$  channels at the plasma membrane with an influx rate  $k_{Ca}$  (see Methods).

**Figure 1–Figure supplement 1.** Sensitivity study of the effect of voxel size on Ca<sup>2+</sup> signals. **Figure 1–source data 1.** Characteristics of meshes used to investigate the effect of voxel size on Ca<sup>2+</sup> signals (Table Supplement 1).

#### 122 Thin shafts favor node compartmentalization

In order to test whether the geometries designed in this study are a good approximation of the ultrastructure of the gliapil, we have compared molecular diffusion flux in those geometries with those reported experimentally. To do so, we simulated photobleaching experiments and compared our results to experimental results from Arizono et al. (*Arizono et al., 2020*). The principle of bleaching simulations is presented in the Methods section and in Supplemental Movie 1. Here, we refer to an increased node compartmentalization when the time to recovery after bleaching,  $\tau$ , increases (see Fig 2B).

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Bleaching traces in simulations are both qualitatively (Fig 2B) and quantitatively (Fig 2C) similar to experimental bleaching traces, for shaft width  $d_{\text{shaft}} = d_0$  and  $d_{\text{shaft}} = \frac{d_0}{2}$ . Indeed, no significant difference of  $I_0$  (Fig 2C1),  $I_{inf}$  (Fig 2C2) and  $\tau$  (Fig 2C3) was observed between simulations and experimental traces. Simulations were also performed with  $d_{\text{shaft}} = \frac{d_0}{3}$ . Our simulations successfully reproduce experimental bleaching experiments and suggest that  $\tau$ , and thus node compartmental-

**Table 1.** Characteristics of the geometries of astrocyte branchlets used in this study.  $V_{cyt}$  is the cytosolic volume,  $S_{PM}$  is the area of the plasma membrane and  $S_{ER}$  is the area of the ER membrane. Volumes are expressed in  $nm^3$  and areas in  $nm^2$ . Meshes are available at http://modeldb.yale.edu/266928, access code: lto42@tpk3D?

Geom	$V_{\rm cyt}$ ( $nm^3$ )	$S_{\rm PM}~(nm^2)$	$S_{\rm ER}$ ( $nm^2$ )
"5nodes" $d_{\text{shaft}} = d_0$	$6.20 \times 10^{8}$	$7.73 \times 10^{6}$	$2.19 \times 10^6$
"5nodes" $d_{\text{shaft}} = d_0/2$	$2.63 \times 10^8$	$4.95\times10^{6}$	$1.28\times10^{6}$
"5nodes" $d_{\text{shaft}} = d_0/3$	$1.95 \times 10^8$	$4.10\times10^{6}$	$9.99 \times 10^{5}$
"No ER" $d_{\text{shaft}} = d_0$	$6.73 \times 10^8$	$7.73 \times 10^{6}$	0.00
"No ER" $d_{\text{shaft}} = d_0/2$	$2.83 \times 10^8$	$4.95\times10^{6}$	0.00
"No ER" $d_{\text{shaft}} = d_0/3$	$2.10 \times 10^8$	$4.09\times10^{6}$	0.00
"Node ER" $d_{\text{shaft}} = d_0$	$6.67 \times 10^8$	$7.75\times10^{6}$	$4.17\times10^{5}$
"Node ER" $d_{\text{shaft}} = d_0/2$	$2.74 \times 10^8$	$4.96\times10^{6}$	$4.37 \times 10^5$
"Node ER" $d_{\text{shaft}} = d_0/3$	$2.00 \times 10^8$	$4.11\times10^{6}$	$4.41 \times 10^{5}$
"Cyl ER" $d_{\text{shaft}} = d_0$	$6.27 \times 10^8$	$7.74\times10^{6}$	$2.03 \times 10^6$
"Cyl ER" $d_{\text{shaft}} = d_0/2$	$2.77 \times 10^8$	$4.95\times10^{6}$	$8.78 \times 10^5$
"Cyl ER" $d_{\text{shaft}} = d_0/3$	$2.07 \times 10^{8}$	$4.09 \times 10^{6}$	$5.86 \times 10^{5}$

- ization, increases when shaft width decreases (Fig 2C3). This result is not surprising as a decreased
- shaft width results in a smaller size of the exit point for diffusing molecules from the node. This
- is similar to e.g dendritic spines, which compartmentalization is increased for thinner spine necks
- (Santamaria et al., 2011; Tønnesen et al., 2014). The geometries that we have designed can thus
- be considered as a reasonable approximation of the ultrastructure of the gliapil observed experi-
- 141 mentally in live tissue.



**Figure 2. Simulations confirm that thin shafts favor node compartmentalization.** (*A*) Geometries of different shaft widths  $d_{\text{shaft}}$ ,  $d_{\text{shaft}} = d_0$ ,  $\frac{d_0}{2}$  and  $\frac{d_0}{3}$ , used in the bleaching simulations. Blue color represents the bleached volume, which varied depending on the value of  $d_{\text{shaft}}$  in order to fit experimental values of  $I_0$  and  $I_{inf}$ . (*B*) Representative experimental (top) and simulation (bottom) traces for different shaft width values.  $I_0$ ,  $I_{inf}$  and  $\tau$  were calculated using Eq 1. Note that simulations were also performed for  $d_{\text{shaft}} = \frac{d_0}{3}$ . (C) Quantification of  $I_0$  (C1),  $I_{inf}$  (C2) and  $\tau$  (C3) values in simulations (red) compared to experiments (black). Note that no experimental data was available for  $d_{\text{shaft}} = \frac{d_0}{3}$ . In C1 and C2, n=5×2 and 20×3 for experiments and simulations, respectively. Data are presented as mean  $\pm$  STD. In C3, n=66 and n=20×3 for experiments and simulations, respectively.  $\tau$  is negatively correlated to  $d_{\text{shaft}}$  in experiments (n=66 from 7 slices; Spearman r=-0.72, p<0.001 \*\*\*) and simulations (n=60; Spearman r=-0.89, p<0.001 \*\*\*). Black and red lines represent curve fit of  $\tau$  as a function of  $d_{\text{shaft}}$  of the form  $\tau = a * \frac{1}{d_{\text{shaft}}} + b$  for experiments and simulations, respectively. (D) Schematic summarizing the conclusion of this figure: diffusion flux increases with  $d_{\text{shaft}}$ . In that sense, thin shafts favor node compartmentalization. Data in panels C1 and C2 are represented as mean  $\pm$  STD, n=20 for each geometry.

**Figure 2-video 1.** Movie of a simulated bleaching experiment, with  $d_{\text{shaft}} = \frac{d_0}{2}$ . Fluorescing ZsGreen molecules are in red and bleached, non-fluorescing, ZsGreen are in yellow.

#### <sup>142</sup> Thin shafts enhance Ca<sup>2+</sup> activity in nodes

80% of astrocyte  $Ca^{2+}$  activity occurs in the gliapil (*Bindocci et al., 2017*), which suggests that 143 most neuron-astrocyte communication occurs at fine astrocytic processes. As we observed that 144 a decreased shaft width is associated with a decreased diffusion flux, i.e an increased compart-145 mentalization of nodes, we have tested whether this effect influences Ca<sup>2+</sup> activity upon neuronal 146 stimulation. To do so, we have first analyzed Ca<sup>2+</sup> signals resulting from a single neuronal stimula-147 tion, which was simulated as an infusion of IP<sub>3</sub> and  $Ca^{2+}$  in the stimulated node, node 1 (see Meth-148 ods). Those parameters encompass the IP<sub>3</sub> production by phospholipase C following the activation 149 of  $G_a$ -G-protein-coupled receptors (GPCRs) resulting from the binding of neuronal glutamate, ATP 150 and noradrenaline to  $G_a$  proteins and  $Ca^{2+}$  entry at the plasma membrane through  $Ca^{2+}$  channels, 151 ionotropic receptors or the sodium/calcium exchanger (NCX) functioning in reverse mode (Ahmad-152 pour et al., 2021; Semyanov et al., 2020). Signals were recorded both in the stimulated node, node 153 1, and in the neighboring node, node 2 (Supplemental Movie 1). Representative  $Ca^{2+}$  traces in 154 node 2 for  $d_{\text{shaft}} = d_0$ ,  $\frac{d_0}{2}$  and  $\frac{d_0}{3}$  are displayed in Fig 3A. Our first result is that Ca<sup>2+</sup> peak probability 155

- increases when  $d_{\text{shaft}}$  decreases (Fig 3B1). The time to  $1^{st}$  peak increases with  $d_{\text{shaft}}$  (Fig 3B2). By con-
- trast, peak amplitude (Fig 3B3) and duration (Fig 3B4) increase when  $d_{\text{shaft}}$  decreases. In order to
- $_{158}$  better understand the mechanisms responsible for the increased  $Ca^{2+}$  peak probability, amplitude
- and duration when  $d_{\text{shaft}}$  decreases, we have measured the frequency of  $IP_3R$  opening in nodes
- 1 and 2. The frequency of  $IP_3R$  opening increases when  $d_{\text{shaft}}$  decreases (Fig 3B5). Note that the
- duration of  $IP_3R$  opening and the number of  $IP_3R$ s open per Ca<sup>2+</sup> peak did not vary with  $d_{\text{shaft}}$ . The
- increased  $IP_3R$  opening frequency associated with small values of  $d_{\text{shaft}}$  probably results from the
- increased residency time of molecules in nodes connected to thin shafts (Fig 3C). Indeed, a thin shaft can "trap"  $Ca^{2+}$  and *IP*, longer in the node, thus locally increasing the probability of *IP*, *R*s
- shaft can "trap"  $Ca^{2+}$  and  $IP_3$  longer in the node, thus locally increasing the probability of  $IP_3Rs$ to open, resulting in larger  $Ca^{2+}$  peaks. For more details, the reader can refer to the theoretical
- to open, resulting in larger  $Ca^{2+}$  peaks. For more details, the reader can refer to the theoretical work investigating the narrow escape problem for diffusion in microdomains (*Schuss et al., 2007*).
- Nodes connected to thinner shafts, despite being characterized by a lower diffusion flux (Fig 2).
- could thus consist of signal amplification units, favoring the generation of larger signals, therefore
- increasing Ca<sup>2+</sup> peak probability, amplitude and duration both in the stimulated node and in neigh-
- 171





**Figure 3-video 1.** Movie of a simulation of the neuronal stimulation protocol, with  $d_{\text{shaft}} = \frac{d_0}{2}$ ,  $k_{Ca} = 0 s^{-1}$ .

**Figure 3-Figure supplement 1.** Sensitivity study of the effect of  $d_{shaft}$  on local Ca<sup>2+</sup> signals.

Figure 3-Figure supplement 2. Effect of Ca<sup>2+</sup> influx rate at the plasma membrane on local Ca<sup>2+</sup> signals.
 Figure 3-Figure supplement 3. Sensitivity study of the effect of boundary conditions on local Ca<sup>2+</sup> activity upon single node stimulation.

**Figure 3-Figure supplement 4.** Node/shaft width ratio and node volume control local Ca<sup>2+</sup> activity. **Figure 3-Figure supplement 5.** Thin shafts enhance local spontaneous Ca<sup>2+</sup> activity.

Figure 3-Figure supplement 6. Ca<sup>2+</sup> peak probability, amplitude and duration decrease with ER surface area. Figure 3-Figure supplement 7. Local Ca<sup>2+</sup> activity increases when shaft diameter decreases, for all ER geometries tested.

**Figure 3-Figure supplement 8.** Sensitivity study of the effect of ER morphology on Ca<sup>2+</sup> dynamics. <sup>8</sup> of 24 **Figure 3-Figure supplement 9.** Ca<sup>2+</sup> indicators alter Ca<sup>2+</sup> peak characteristics.

To identify the cause of the increased  $Ca^{2+}$  activity when shaft width decreases (Fig 3), we per-172 formed simulations in which we altered the stimulated node (Supplemental Fig 1D-F).  $Ca^{2+}$  influx at 173 the plasma membrane (Supplemental Fig 2) and boundary conditions (Supplemental Fig 3). Those 174 parameters did not affect the observed effects of  $d_{\text{shaft}}$  on  $\text{Ca}^{2+}$  dynamics. Furthermore, we re-175 peated simulations of Fig 3 with constant cytosolic volume (Supplemental Fig 4) and constant num-176 ber of IP<sub>3</sub>Rs (Supplemental Fig 1A-C), irrespective of the value of  $d_{\text{shaft}}$ . Our results confirm that the 177 relevant parameter responsible for the observed effects of  $d_{shaft}$  on  $Ca^{2+}$  signal characteristics is 178 the node/shaft width ratio or the cytosolic volume rather than  $d_{\text{shaft}}$  itself. Spontaneous Ca<sup>2+</sup> sig-179 nals were affected by shaft width in the same way as neuronal-induced Ca<sup>2+</sup> signals (Supplemental 180 Fig 5) and, in particular, reproduced the increase of the amplitude ratio of spontaneous  $Ca^{2+}$  sig-181 nals between node 2 and node 1 with shaft width observed in hippocampal organotypic cultures 182 (Arizono et al., 2020). Note that ER morphology, in particular ER surface area (Supplemental Fig 6, 183 7 and 8), and  $Ca^{2+}$  buffering by  $Ca^{2+}$  indicators (Supplemental Fig 9), consistent with previous re-184 ports (Denizot et al., 2019a; Bartol et al., 2015; Majewska et al., 2000), can also alter local Ca2+ 185 dynamics. 186 Overall, our results suggest that a decreased shaft width, resulting in a decreased diffusion ef-187

flux from nodes, increases  $Ca^{2+}$  peak probability, amplitude and duration. Conversely, the swelling of fine processes, resulting in an increase of shaft width, attenuates local  $Ca^{2+}$  peak probability, amplitude and duration.

#### <sup>191</sup> Ca<sup>2+</sup> imaging confirms that swelling attenuates local spontaneous Ca<sup>2+</sup> activity

Our recent super-resolution study revealed that the nano-architecture of fine processes is re-192 modeled in hypo-osmotic conditions (Arizono et al., 2021b). At this spatial scale, hypo-osmotic 193 conditions resulted in heterogeneous swelling of processes, where shaft width increased while 194 node width remained unaltered (see Fig 3 in (Arizono et al., 2021b)). Simulation results presented 195 in Fig 3 suggest that processes with increased shaft width  $d_{shaft}$  are associated with decreased  $Ca^{2+}$ 196 peak probability, duration and amplitude. To test whether this effect can be observed in live tis-197 sue, we thus performed experimental measurements of calcium dynamics in fine astrocytic pro-198 cesses under basal and hypo-osmotic conditions. To resolve  $Ca^{2+}$  signals in fine branchlets, we 199 performed experiments using confocal microscopy in organotypic cultures, which provides the best optical access and sample stability in live tissue to date (resolution  $\approx 200$  nm in x-y versus  $\approx$ 201 500 nm for two-photon microscopy). In accordance with our model's predictions,  $Ca^{2+}$  peak ampli-202 tude and duration were lower in hypo-osmotic compared to basal conditions (Fig 4A-D). Note that 203 peak amplitude and duration did not significantly vary when measured repeatedly in basal conditions (Fig 4E-F). Overall, our experimental results confirm that the complex nano-architecture of 205 fine astrocytic processes and its alteration, such as cell swelling, shapes local  $Ca^{2+}$  activity. 206



**Figure 4.**  $Ca^{2+}$  **imaging confirms that swelling attenuates local spontaneous**  $Ca^{2+}$  **activity.** (*A*, *B*) (Top) Confocal images of the astrocytic spongiform domain expressing GCaMP6s at baseline (basal, A) and in hypo-osmotic condition (HOC, B), measured in organotypic hippocampal cultures. (Bottom) Representative traces of spontaneous  $Ca^{2+}$  events from ROIs indicated in A (A1-A3) and B (B1-B3). (*C*, *D*)  $Ca^{2+}$  peak amplitude (C) and duration (D) of spontaneous  $Ca^{2+}$  events are significantly smaller in hypo-osmotic conditions (HOC) compared to basal conditions (Basal). (*E*, *F*) Amplitude (E) and duration (F) of spontaneous  $Ca^{2+}$  events do not significantly vary when measured twice in a row (1, 2) in the absence of HOC. Significance is assigned by \* for  $p \le 0.05$ , \*\* for  $p \le 0.01$ , \*\*\* for  $p \le 0.001$ .

#### 207 Thin shafts favor more robust signal propagation

A single astrocyte branchlet can contact and modulate the activity of multiple synapses, re-208 ferred to as synaptic clusters, which can belong to the same or to different dendrites or even to 209 different neurons (Arizono et al., 2020; Reichenbach et al., 2010; Witcher et al., 2007; Cali et al., 210 2019; Semyanov et al., 2020). The frequency of stimulation of the branchlet can vary depending 211 on the activity of the adjacent synapses. For example, a connection of adjacent astrocytic nodes 212 to co-active synapses would result in a high node stimulation frequency. We have thus tested the 213 influence of the frequency of neuronal stimulation of neighboring nodes on the propagation of 214 Ca<sup>2+</sup> signals in branchlets. To do so, we have performed simulations in which neighboring nodes 215 were repeatedly stimulated after a time period  $\tau_{IP3}$ , that varied from 50 ms to 5s, while Ca<sup>2+</sup> signals 216 were recorded in a remote node, node 5 (Fig 5A). Neuronal stimulation is simulated as an infusion 217 of 50 IP<sub>3</sub> molecules in the stimulated node. Representative  $Ca^{2+}$  traces in node 5 in branchlets with 218

various shaft widths  $d_{\text{shaft}}$  are presented in Fig 5A for  $\tau_{\text{IP3}}$ =250 and 3000 ms. Our first notable result 219 is that the time to  $1^{st}$  peak in node 5 decreases with  $d_{\text{shaft}}$ , whatever the value of  $\tau_{\text{IP3}}$  (Fig 5B1). More 220 specifically, time to 1<sup>st</sup> peak is higher for  $d_{\text{shaft}} = d_0$  compared to both  $d_{\text{shaft}} = \frac{d_0}{2}$  and  $\frac{d_0}{3}$ , while differ-221 ences between  $d_{\text{shaft}} = \frac{d_0}{2}$  and  $\frac{d_0}{3}$  are not as striking. Moreover, the difference between  $d_{\text{shaft}} = d_0$ ,  $\frac{d_0}{2}$ 222 and  $\frac{d_0}{3}$  increases with  $\tau_{IP3}$ . This suggests that geometries with  $d_{shaft} = d_0$  better discriminate slow from 223 fast frequency of node stimulation compared to geometries with thinner shafts. Geometries with 224  $d_{\text{shaft}} = d_0$  are further characterized by a lower Ca<sup>2+</sup> peak probability in node 5 compared to geome-225 tries with  $d_{\text{shaft}} = \frac{d_0}{2}$  and  $\frac{d_0}{2}$  (Fig 5B2). More precisely, Ca<sup>2+</sup> peak probability decreases as  $\tau_{\text{IP3}}$  increases 226 for  $d_{\text{shaft}} = d_0$ , which was observed independently of our boundary conditions (Supplemental Fig 1, 227 see Methods). This suggests that geometries with larger shafts could be associated with decreased 228 signal propagation to remote nodes in case of repeated node stimulation at low frequency ( $\tau_{\rm IP3}$  > 229 2s). 230 231



**Figure 5. Thin shafts are associated with a more robust signal propagation upon repeated neuronal stimuli.** (*A*) (*Top*) Neuronal stimulation protocol: node 1 is stimulated at  $t=t_0=5s$ , node 2 at  $t_0 + \tau_{IP3}$ , node 3 at  $t_0 + 2\tau_{IP3}$  and node 4 at  $t_0 + 3\tau_{IP3}$ ,  $k_{Ca}=0$   $s^{-1}$ . Ca<sup>2+</sup> activity is recorded in node 5. (*Bottom*) Representative Ca<sup>2+</sup> traces in node 5 for shaft width  $d_{shaft} = d_0$  (red),  $\frac{d_0}{2}$  (black) and  $\frac{d_0}{3}$  (blue), with  $\tau_{IP3}=250ms$  (left) and 3000ms (right), expressed as SNR (see Methods). (*B1*) Time to 1<sup>st</sup> peak increases with  $\tau_{IP3}$  for  $d_{shaft} = d_0$  (\*\*\*),  $\frac{d_0}{2}$  (\*\*\*) and  $\frac{d_0}{3}$  (\*\*\*). T-tests revealed that for any value of  $\tau_{IP3}$ , time to 1<sup>st</sup> peak is higher for  $d_{shaft} = d_0$  compared to  $d_{shaft} = \frac{d_0}{2}$  and  $\frac{d_0}{3}$ . Time to 1<sup>st</sup> peak is significantly higher when  $d_{shaft} = \frac{d_0}{2}$  compared to  $d_{shaft} = \frac{d_0}{3}$ , for most values of  $\tau_{IP3}$  (p=0.032 \*, 0.0025 \*\*, 0.034 \*, 0.016 \* and 0.019 \* for  $\tau_{IP3}=250$ , 500, 1000, 4000 and 5000, respectively). (*B2*) Ca<sup>2+</sup> peak probability in node 5 is lower for  $d_{shaft} = d_0$  compared to  $d_{shaft} = \frac{d_0}{2}$  and  $\frac{d_0}{3}$ . Ca<sup>2+</sup> peak probability of failure of node stimulation  $p_{fail}$ , for  $d_{shaft} = d_0$  (C1),  $d_{shaft} = \frac{d_0}{2}$  (C2) and  $d_{shaft} = \frac{d_0}{3}$  (C3), with  $p_{fail} \in [0, 1]$ . (*D*) Schematic summarizing the main conclusion of this figure: decreased shaft width allows signal propagation despite omitted node stimulation, thus favoring more robust signal propagation. Data are represented as mean  $\pm$  STD, n=20 for each value of  $d_{shaft}$  and of  $\tau_{IP3}$ . Lines in panel B are guides for the eyes. The effect of  $d_{shaft}$  on each Ca<sup>2+</sup> signal characteristic was tested using one-way ANOVA. Significance is assigned by \* for  $p \le 0.05$ , \*\* for  $p \le 0.01$ , \*\*\* for  $p \le 0.001$ .

**Figure 5–Figure supplement 1.** Sensitivity study of the effect of boundary conditions on local Ca<sup>2+</sup> activity upon repeated neuronal stimuli.

For  $\tau_{IP3}$ =4s and  $d_{shaft} = \frac{d_0}{2}$ , signals were detected in node 5 11.55 ± 3.89 s after the stimulation of 232 node 1, which means that they occurred before the stimulation of node 4 (t= $t_0$  + 12s for  $\tau_{IP3}$ =4s). 233 This phenomenon was not observed for  $d_{\text{shaft}} = d_0$ , for which time to 1<sup>st</sup> peak when  $\tau_{\text{IP3}} = 4$ s was 23.67 234  $\pm 0.47$  s. This suggests that for  $d_{shaft} = \frac{d_0}{2}$ , contrary to  $d_{shaft} = d_0$ , one node stimulation could be omitted 23 without having any consequence on  $Ca^{2+}$  peak probability in node 5. In order to test this hypothesis, 236 we have performed simulations in which the stimulation of nodes 2, 3 and 4 occurred with a given 237 probability of failure  $p_{\text{fail}}$ . Simulations were performed for  $p_{\text{fail}}=0, 0.05, 0.1, 0.15, 0.25$  and 0.75. Ca<sup>2+</sup> 238 peak probability in node 5, depending on  $p_{fail}$  and on  $\tau_{IP3}$  is presented in Fig 5C, for  $d_{shaft} = d_0$  (Fig 5C1), 239  $d_{\text{shaft}} = \frac{d_0}{2}$  (Fig 5C2) and  $d_{\text{shaft}} = \frac{d_0}{3}$  (Fig 5C3). As expected, Ca<sup>2+</sup> peak probability, despite high values of 240  $p_{\text{fail}}$ , increases when  $d_{\text{shaft}}$  decreases. Thus, thin shafts can favor signal propagation by allowing the 241 omission of a node stimulation. In that sense, geometries displaying thin shafts are characterized 242 by a more robust signal propagation (Fig 5D). 243

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Together, our results suggest that, in the context of repeated node stimulation, thin shafts are 245 associated with an increase of  $Ca^{2+}$  peak probability in more remote nodes, with an earlier sig-246 nal onset, suggesting increased signal propagation. Astrocytic processes with thicker shafts (here 247  $d_{\text{shaft}} = d_0$ , such as observed in hypo-osmotic conditions (*Arizono et al., 2021b*), are associated with 248 lower signal propagation in case of low stimulation frequency (time period > 2s), potentially fa-249 voring the formation of local  $Ca^{2+}$  hotspots. Our results suggest that geometries with thick shafts 250 could impair signal propagation when a branchlet is stimulated at a low frequency. In that sense, 251 astrocyte branchlets with thicker shafts would be better detectors of the surrounding level of neu-252 ronal activity. By contrast, branchlets with thin shafts would be less discriminating and provide 253 more robust signal propagation. 254

#### 255 Discussion

Fine astrocytic processes are responsible for most astrocytic  $Ca^{2+}$  signals (*Bindocci et al.*, 2017) 256 and are preferential sites of neuron-astrocyte communication (Arizono et al., 2020). A better un-257 derstanding of the mechanistic link between their morphology and the spatio-temporal properties 258 of local  $Ca^{2+}$  signals is crucial, yet hard to test experimentally. Here, we perform reaction-diffusion 259 simulations in idealized morphologies of astrocytic processes derived from 3D super-resolution mi-260 croscopy to investigate the effect of astrocyte nanoscale morphology on  $Ca^{2+}$  activity in the gliapil. 261 Our simulation results suggest that the morphology of processes, alternating between large and 262 thinner cellular compartments (Panatier et al., 2014; Arizono et al., 2020; Grosche et al., 1999), in-263 creases  $Ca^{2+}$  peak probability, duration, amplitude and propagation. Conversely, astrocyte swelling 264 attenuates local  $Ca^{2+}$  activity and signal propagation (Fig.6). Our simulation results, in accordance 265 with experimental data, suggest that thin shafts are associated with a decreased diffusion flux, i.e. 266 an increased compartmentalization of nodes. Thus, nodes, similarly to dendritic spines (Santa-267 maria et al., 2011), act as diffusion traps when shaft width is low. Note that, more than the value 268 of shaft width itself, our results emphasize the effect of the ratio between node and shaft diameter 269 on  $Ca^{2+}$  activity. The geometries designed and used in this study emerge as interesting tools to in-270 vestigate the influence of the ultrastructure of fine astrocyte branchlets on the local Ca<sup>2+</sup> dynamics 271 in health and disease. By recording the mechanisms resulting in  $Ca^{2+}$  signals upon neuronal stim-272 ulation in small cellular compartments of the gliapil, which cannot be performed experimentally. 273 our simulation results shed light on the mechanisms by which astrocyte swelling influences the 274 frequency, amplitude and propagation of  $Ca^{2+}$  signals at the nanoscale. 275 276



**Figure 6. Proposed mechanisms that regulate astrocytic**  $Ca^{2+}$  **activity at tripartite synapses.** Our simulation results demonstrate that the nano-morphology of astrocytic processes, consisting in the alternation of nodes and shafts, powerfully shapes the spatio-temporal properties of  $Ca^{2+}$  signals and promotes local  $Ca^{2+}$  activity. Astrocyte swelling, observed in pathological conditions such as brain injury, stroke and epilepsy, results in an increased shaft width without altering node size. Our results suggest that such pathological alterations of the nanoscale morphology of astrocytes result in a decreased local  $Ca^{2+}$  activity, which we confirm experimentally in hypo-osmotic conditions. Upon repeated neuronal stimuli, the we predict that swelling hinders astrocytic signal propagation. Overall, this study highlights the impact of astrocyte nano-morphology on astrocyte activity at tripartite synapses, in health and disease.

Experimental Ca<sup>2+</sup> recordings of astrocyte activity have established that astrocyte processes dis-277 play both highly localized microdomain signals and propagating  $Ca^{2+}$  wayes (*Srinivasan et al., 2015*: 278 Bindocci et al., 2017). Our simulations suggest that the morphology of the cell and of its organelles 279 can strongly influence the formation of these patterns of astrocytic  $Ca^{2+}$  signaling. Notably, thinner 280 shafts allow less discriminating and more robust signal propagation upon repeated stimuli com-281 pared to larger shafts. Thinner shafts indeed allow signal propagation even in the absence of some 282 stimuli or when the time interval between repeated stimuli is large. On the contrary, geometries 283 with thick shafts seem to be more discriminating, potentially favoring the propagation of signals resulting from repeated stimuli from co-active synapses. Cellular morphology thus emerges as 285 a key parameter that regulates the active propagation of  $Ca^{2+}$  signals. The ultrastructure of the 286 spongiform domain of astrocytes is very complex, characterized by abundant branching points. 287 conferring a reticular morphology (Arizono et al., 2020). Those branching points are reportedly 288 sometimes arranged into ring-like structures, although their occurrence and shape are still de-280 bated and could differ depending on the brain region under study (Arizono et al., 2020: Panatier 290 et al., 2014; Kivoshi et al., 2020; Salmon et al., 2021; Arizono and Nägerl, 2021). The effect of this 201 reticular ultrastructure on the propagation of  $Ca^{2+}$  signals remains to be uncovered. Further char-292 acterization of the shape of fine astrocytic processes of the spongiform domain, their variability 203 as well as their connectivity to the neighboring synapses are thus required. Pairing those observa-294 tions with biophysically-detailed models such as the one presented in this study stands to deepen 295 our understanding of the roles of astrocytic and neuronal morphology at tripartite synapses on 296 neuron-astrocyte communication. 297

298

In neurons, both experimental (*Yuste et al., 2000; Noguchi et al., 2005; Tønnesen et al., 2014*)
 and modelling (*Schmidt and Eilers, 2009; Biess et al., 2007; Simon et al., 2014; Bell et al., 2019; Hol- cman and Schuss, 2005, 2011; Santamaria et al., 2011; Cugno et al., 2019*) studies have suggested
 that thin spine necks favor the compartmentalization of Ca<sup>2+</sup> signals within the spine head. This
 compartmentalization of synapses allows neurons to discriminate various inputs and to process

information locally (Wybo et al., 2019: Poirazi and Papoutsi, 2020), increasing the computational 304 power of the neuronal circuits. According to our simulation results, nodes connected to thin shafts 305 could favor the emergence of large signals at the site of neuron-astrocyte communication. Interest-306 ingly, we further propose that those amplified signals in nodes, instead of resulting in  $Ca^{2+}$  hotspots. 307 favor active signal propagation. In response to spike timing-dependent plasticity (STDP) protocols 308 (Argvg et al., 2014) and after long-term potentiation (Tønnesen et al., 2014), the neck of dendritic spines become wider and shorter. Recent in vitro and in vivo studies have reported that the geom-310 etry of the ER in neurons is also highly dynamic (Kucharz et al., 2013), experiencing fast fission and 311 fusion events. Further, the ER is variably distributed in spines, being preferentially present in large 312 spines associated with strong synapses (Holbro et al., 2009). The geometries of dendrites and of 313 their organelles, which influence local signals, are thus highly dynamic. Similarly, fine astrocytic 314 processes encounter morphological rearrangements that are activity-dependent, which notably 316 influence synaptic maturation, efficacy and spine stability (Theodosis et al., 2008; Zhou et al., 2019; 316 Henneberger et al., 2020). Our study sheds light on the influence of rearrangements of the reticular 317 morphology of fine processes on signal computation by astrocytes. Further investigation manipu-318 lating astrocyte morphology in situ as well as in vivo is required to better characterize the variability 319 of astrocyte ultrastructure and the associated integration of  $Ca^{2+}$  signals. 320 321

The morphology of the complex spongiform domain of astrocytes is highly dynamic, subject to activity-dependent as well as pathological remodeling. Our study, providing mechanisms by which an altered astrocyte morphology influences neuron-astrocyte communication at the nanoscale, gives new insights into the involvement of astrocytes in brain function in health and disease.

#### 326 Methods and Materials

#### 327 Stochastic spatially-explicit voxel-based simulations

In order to model astrocyte  $Ca^{2+}$  signals in astrocyte branchlets, we have used the voxel-based 328 "GCaMP" implementation of the Inositol 3-Phosphate (IP<sub>2</sub>) receptor-dependent  $Ca^{2+}$  signaling model 329 from Denizot et al (Denizot et al., 2019a), using the same reaction scheme and parameter values 330 (Fig 1B). Briefly, we model  $Ca^{2+}$  fluxes in and out of the cytosol, mediated by  $Ca^{2+}$  channels and 331 pumps on the endoplasmic reticulum (ER) and on the plasma membrane.  $Ca^{2+}$  signals occur when 332 some IP<sub>2</sub>R channels are in the open state. IP<sub>2</sub> can be synthesized by the  $Ca^{2+}$ -dependent activ-333 ity of phospholipase C  $\delta$  (PLC $\delta$ ) and the removal of IP<sub>2</sub> molecules from the cytosol is expressed 334 as a single decay rate. IP<sub>2</sub>R kinetics is described by a Markov model, derived from De Young & 335 Keizer's model (*De Young and Keizer, 1992*). Fach IP<sub>a</sub>R molecule contains one IP<sub>a</sub> binding site and 336 two  $Ca^{2+}$  binding sites. An IP<sub>2</sub>R is in the open state when in state {110} (first Ca site and IP<sub>2</sub> bound. 337 second Ca site free). Depending on the simulation, other diffusing molecules were added to the 338 model, such as the fluorescent molecule ZsGreen and fluorescent  $Ca^{2+}$  indicators, here 10  $\mu$ M of 339 GCaMP6s GCaMPs are genetically encoded  $Ca^{2+}$  indicators (GECIs) that are derived from the flu-340 orescent protein GFP and the  $Ca^{2+}$  buffer calmodulin (see (*Shigetomi et al., 2016*) for a review on 341 GECIs). For further details on the kinetic scheme and model assumptions, please refer to Denizot et al. 2019 (Denizot et al., 2019a). 343

344

The model was implemented using STEPS (http://steps.sourceforge.net/), a python package per-345 forming exact stochastic simulation of reaction-diffusion systems (*Hepburn et al.*, 2012). More 346 presicely. STEPS uses a spatialized implementation of Gillespie's SSA algorithm (*Gillespie*, 1977: 347 Isaacson and Isaacson, 2009: Smith and Grima, 2018), Simulations in STEPS can be performed in 3/18 complex geometries in 3 spatial dimensions. Space is divided into well-mixed tetrahedral compart-340 ments, referred to as voxels. Reactions between 2 molecules can only occur if they are located 350 within the same voxel. Diffusion events are modeled as a decrease of the number of molecules in 351 the original voxel and an increase in the number of molecules in its neighboring voxel. Boundary 352

conditions, except when specified otherwise, were reflective. In other words, mobile molecules
 could not diffuse away from the geometry, as if they were "bouncing" onto the plasma membrane.
 STEPS enables to compute, in complex 3D geometries, reactions and diffusion in the cytosol as well
 as reactions between cytosolic molecules and molecules located at the plasma or ER membrane.

#### 358 Geometries

Typical astrocyte branchlet geometries were designed from their recent experimental charac-359 terization in live tissue at high spatial resolution (50 nm in x-y) (Arizono et al., 2020). Those geometries consist in alternations of bulbous structures, nodes, connected to each other with cylindrical 361 structures, shafts. Geometries with different shaft widths d<sub>shaft</sub> were designed using Trelis software 362 (https://www.csimsoft.com/trelis, Fig 1A). The geometry of a node was approximated as being a 363 sphere of diameter 380 nm. Shaft geometry consisted in a 1 $\mu$ m long cylinder. Shaft diameter was 364 defined relative to node diameter. For example, shaft diameter was the same as node diameter, i.e 365  $d_{\text{shaft}} = d_0 = 380 \text{ nm}$ . Similarly, shaft diameter was 190 nm and 127 nm for  $d_{\text{shaft}} = \frac{d_0}{2}$  and  $\frac{d_0}{2}$ , respectively. 366 Cones were positioned between spheres and cylinders in order to create a smoother transition be-367 tween nodes and shafts, better approximating the geometry observed experimentally. Cytosolic 368 volume was thus  $V_1$ =0.620  $\mu m^3$ ,  $V_2$ =0.263  $\mu m^3$  and  $V_3$ =0.195  $\mu m^3$ , for  $d_{\text{shaft}} = d_0$ ,  $\frac{d_0}{2}$  and  $\frac{d_0}{3}$ , respectively. 369 A subset of simulations were performed in a geometry with  $V_1$ =0.258  $\mu m^3$ . This geometry is charac-370 terized, similarly to geometries with  $d_{sheft} = d_{0t}$  by a node/shaft width ratio of 1. It contains cylinders 371 of length 750 nm, diameter 285 nm and spheres of diameter 285 nm. As a first approximation, 372 ER geometry was considered to be similar to the geometry of the astrocyte branchlet: node/shaft 373 successions. ER nodes were aligned with cytosolic nodes. As no quantification of the ER volume 374 compared to cellular volume was found for astrocytes in the literature. ER volume was 10% of the 375 total branchlet volume, based on available data in neurons (Spacek and Harris, 1997). The cytoso-376 lic volume, plasma and FR membrane areas of the different "5Nodes" geometries are presented in 377 Table 1. 378

379

A sensitivity study was performed to investigate the effect of voxel size on the kinetics of the molecular interactions modeled. Information on the voxel sizes of the different meshes used is presented in Supplemental Table 1. Results are presented in Supplemental Fig 1. Meshes that contained voxels that were < 50 nm<sup>3</sup> were characterized by aberrant kinetics, resulting in aberrant average numbers of molecules in a given state. Those results thus suggest that to prevent errors due to voxel size, meshes should not display voxel sizes that are< 50 nm<sup>3</sup>. We have thus made sure, while meshing the geometries in which simulations were ran, that no voxels were < 50 nm<sup>3</sup>. Minimum voxel size was 443 nm<sup>3</sup>, 1100 nm<sup>3</sup> and 447 nm<sup>3</sup>, for  $d_{shaft} = d_0$ ,  $\frac{d_0}{2}$  and  $\frac{d_0}{3}$  geometries, respectively.

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In a subset of simulations, ER geometry varied. The shape of the cell was the same as in "5nodes" geometries (Fig 1). ER geometry consisting of node/shaft alternations, described above, is referred to as "Node/shaft ER". "No ER" geometry contains no ER. "Node ER" is characterized by a discontinuous ER geometry, consisting in spheres of diameter 54 nm, located in cellular nodes. "Cyl ER" corresponds to a cylindrical ER, of length  $l_{ER}$ = 6274 nm and a diameter of 108, 54 and 36 nm, for  $d_{shaft} = d_0$ ,  $\frac{d_0}{2}$  and  $\frac{d_0}{3}$ , respectively. The associated cytosolic volume, ER and plasma membrane area are presented in Table 1.

#### <sup>397</sup> Protocol for simulating bleaching experiments

In order to test whether the idealized geometries presented in Fig 1 are a good approximation
 of the spongiform ultrastructure of astrocyte branchlets, we have simulated their fluorescence
 recovery after photobleaching (FRAP) experiments. Briefly, laser pulses are simulated on a node
 (region of interest) while the fluorescence level is being recorded. At bleaching time, the fluores-

<sup>402</sup> cence level in the region of interest decreases to  $I_0$ . Then, because of the diffusion of fluorescent <sup>403</sup> molecules into the region of interest, fluorescence increases until it reaches a new steady state, <sup>404</sup>  $I_{inf}$ . We characterize node compartmentalization by measuring the time  $\tau$  taken by fluorescing <sup>405</sup> molecules to diffuse into the node to reach  $I_{inf}$ . In other words, a high node compartmentalization <sup>406</sup> will be associated with a high value of  $\tau$ . Thus, 3 main parameters characterize bleaching traces: <sup>407</sup>  $I_0$ ,  $\tau$  and  $I_{inf}$ .

408

To mimic bleaching experiments in fine branchlets performed by Arizono et al (Arizono et al., 409 2020). ZsGreen molecules were added to simulation space. After 2 seconds of simulation, providing 410 the basal level of fluorescence, 60% of ZsGreen molecules were bleached. In order to fit  $I_0$  and  $I_{inf}$ 411 that were measured experimentally, and as bleaching time lasted 10 ms in experiments and 1 412 ms in simulations, the bleached volume in simulations was adjusted depending on the geometry 413 (see Fig 2A). Bleaching was simulated as a transition from 7sGreen molecules to 7sGreen-bleached 414 molecules, the latter being considered as non-fluorescing molecules. Screenshots of simulations, 415 illustrating the diffusion of ZsGreen and ZsGreen-bleached molecules, are presented in Fig S2B. 416 The number of ZsGreen molecules in the central node was recorded over simulation time and a fit 417 was performed following equation 1 to determine the values of  $I_{0}$ ,  $I_{inf}$  and  $\tau$ . 418

$$I(t) = I_0 - (I_0 - I_{inf})e^{-t/\tau}$$
<sup>(1)</sup>

, where I(t) is the level of fluorescence measured at time t. The coefficient of diffusion,  $D_{7eGreen}$ , and 410 the concentration. [ZsGreen], of ZsGreen were adjusted to fit experimental data. Indeed, the am-420 plitude of [ZsGreen] fluctuations at steady state is inversely proportional to the number of ZsGreen 421 molecules in the geometry. In other words, fluorescence signals are more noisy when [ZsGreen] 422 is low. Moreover, the autocorrelation of those fluctuations depends on the coefficient of diffusion 423 of ZsGreen,  $D_{ZsGreen}$ . If  $D_{ZsGreen}$  increases, the autocorrelation of Lag, where Lag is the autocorrela-424 tion delay, will decrease faster as Lag increases. Comparing the fluctuations of [ZsGreen] and its 425 autocorrelation in experiments and in simulations thus enabled to find the values of  $D_{ZeGreen}$  and 426 of [ZsGreen] that allowed for the best fit to experimental data. In the simulations presented here, 427  $D_{\text{ZsGreen}}$ =90  $\mu m^2 \cdot s^{-1}$  and [ZsGreen]=25  $\mu$ M. 428

#### 429 Protocols for simulating neuronal stimulation

In order to investigate the propagation of  $Ca^{2+}$  signals from nodes that contact neuronal spines. 430 we have developed 2 different protocols for our simulations, performed in the geometries pre-431 sented in Fig 1. As nodes were the site of Ca<sup>2+</sup> signal initiation (Arizono et al., 2020) and as most 432 spines contacted nodes rather than shafts, we have simulated neuronal stimulation in nodes. To 433 simulate neuronal stimulation,  $IP_3$  and  $Ca^{2+}$  were infused in the cytosol at stimulation time.  $IP_3$ 434 infusion reflects the production of IP<sub>2</sub> by phospholipase C that results from the activation of  $G_2$ -G-435 protein-coupled receptors (GPCRs). Ca<sup>2+</sup> infusion mimics the influx of Ca<sup>2+</sup> in the cytosol through 436  $Ca^{2+}$  channels at the plasma membrane. The rate of this neuronal activity-induced  $Ca^{2+}$  influx,  $k_{Ca}$ . 437 varied within a physiological range of values, from 0 to 1000  $s^{-1}$  (Wu et al., 2018; Brazhe et al., 2018). 438 Signals were recorded both in the stimulated node, Node 1, and in the neighboring node, Node 2. 439

• In the first protocol, 100 IP<sub>2</sub> molecules were infused in Node 1, at  $t=t_0=1s$ , while  $Ca^{2+}$  activity 440 was monitored in Node 1 and in the neighboring node, Node 2 (see e.g Fig 3A). Neuronal 441 activity-induced  $Ca^{2+}$  influx was mediated by generic  $Ca^{2+}$  channels at the plasma membrane. 443 25 of those  $Ca^{2+}$  channels were placed on the plasma membrane of Node 1, corresponding 443 to a similar density to the IP<sub>2</sub>R density on the ER membrane, and were set to an inactive state. 444 At stimulation time  $t=t_0$ ,  $Ca^{2+}$  channels were set to an active state, resulting in an influx of  $Ca^{2+}$ 445 within the cytosol at rate  $k_{Ca}$ . At t= $t_0$  + 1, Ca<sup>2+</sup> channels were set back to their initial inactive 446 state. Simulations were performed in geometries with varying shaft width  $d_{\text{shaft}}$ . 447

- In the second protocol, we have investigated signal propagation in the node/shaft geometry
- depending on shaft width  $d_{\text{shaft}}$  when several nodes were successively stimulated. In "5nodes"
- geometries, 50 IP<sub>3</sub> molecules were infused at  $t_0$ =5s,  $t_0 + \tau_{IP3}$ ,  $t_0 + 2\tau_{IP3}$ ,  $t_0 + 3\tau_{IP3}$  in Nodes 1, 2,
- 3 and 4, respectively. During the whole simulation time,  $Ca^{2+}$  activity was recorded in Node
- 452 5 (see Fig 5). In a subset of simulations, stimulation of Nodes 2, 3 and 4 occurred with a
- 453 probability  $1 p_{fail}$ , with  $p_{fail} \in [0, 1]$ .

### 454 Peak detection and analysis

The same strategy as developed by Denizot et al. (Denizot et al., 2019a) was used for detect-455 ing and analysing  $Ca^{2+}$  signals. Briefly, basal concentration of  $Ca^{2+}$ ,  $[Ca]_{2+}$  was defined based on a 456 histogram of the number of  $Ca^{2+}$  ions in the absence of neuronal stimulation. Peak initiation cor-457 responded to the time when  $[Ca^{2+}]$  was higher than the following threshold:  $[Ca]_{b} + n\sigma_{Ca}$ , where  $\sigma_{Ca}$ is the standard deviation of  $[Ca^{2+}]$  histogram in the absence of neuronal stimulation. The value of 459 n was set by hand depending on signal/noise ratio of the simulation of interest. Peak termination 460 corresponded to the time when  $[Ca^{2+}]$  decreased below the peak threshold. 461 Several parameters were analyzed to characterize  $Ca^{2+}$  signals. Peak amplitude, A. corresponds to 462 the maximum  $[Ca^{2+}]$  measured during the peak duration. It is expressed as signal to noise ratio 463  $SNR = \frac{A - [Ca]_{b}}{[Ca]_{b}}$ . Peak duration corresponds to the time between peak initiation and peak termination. Time to 1<sup>st</sup> peak corresponds to the delay between the beginning of the simulation and 464 465

the first peak detection, measured in the cellular compartment of interest. Peak probability corre-

time in the region of interest.  $Ca^{2+}$  residency time was measured by performing n=300 simulations

for each value of  $d_{\text{shaft}}$ , in which only 1 Ca<sup>2+</sup> ion was added to node 1, without other molecular species. Ca<sup>2+</sup> residency time corresponds to the time taken for the ion to diffuse away from node 1.

#### 472 Organotypic hippocampal slice cultures

Ara All experiments were performed as described in (*Arizono et al., 2020*) and were in accordance with the European Union and CNRS UMR5297 institutional guidelines for the care and use of laboratory animals (Council directive 2010/63/EU). Organotypic hippocampal slices (Gähwiler type) were dissected from 5–7-d-old wild-type mice and cultured 5–8 week in a roller drum at 35°C, as previously described (*Gähwiler, 1981*).

#### 478 Viral infection

AAV9-GFAP-GCaMP6s (*Stobart et al., 2018b*) was injected by brief pressure pulses (40ms; 15
 psi) into the stratum radiatum of 2-3-week old slices from Thy1-YFP-H (JAX:003782) mice 4-6 weeks
 prior to the experiment.

#### 482 Image acquisition

For  $Ca^{2+}$  imaging, we used a custom-built setup based on an inverted microscope body (Leica 483 DMI6000), as previously described in (*Tønnesen et al., 2011*). We used a 1.3 NA glycerol immersion objective equipped with a correction collar to reduce spherical aberrations and thereby allow imag-485 ing deeper inside brain tissue (Urban et al., 2011). The excitation light was provided by a pulsed 186 diode laser (I = 485 nm, PicoOuant, Berlin, Germany). The fluorescence signal was confocally de-487 tected by an avalanche photodiode (APD: SPCM-AORH-14-FC: PerkinElmer). The spatial resolution 188 of the setup was around 175 nm (in x-v) and 450 nm (z). Confocal time-lapse imaging (12.5 x 25 480 um, pixel size 100 nm) was performed at 2Hz for 2.5 min in artificial cerebrospinal fluid containing 490 125 mM NaCl, 2.5 mM KCl, 1.3 mM MgCl<sub>2</sub>, 2 mM CaCl<sub>2</sub>, 26 mM NaHCO<sub>2</sub>, 1.25 mM NaH<sub>2</sub>PO<sub>4</sub>, 20 mM 491 D-glucose, 1 mM Trolox; 300 mOsm; pH 7.4. Perfusion rate was 2 mL/min and the temperature 32 492

- °C. Hypo-osmotic stress (300 mOsm to 200 mOsm) was applied by perfusing ACSF with reduced
- <sup>494</sup> NaCl concentration (119 to 69 mM NaCl).

#### **495** Quantification and statistical analysis

For each parameter set, 20 simulations, with different seeds, were generated. Each parameter describing  $Ca^{2+}$  dynamics was expressed as mean  $\pm$  standard deviation. The effect of  $d_{shaft}$  on each  $Ca^{2+}$  signal characteristic was tested using one-way ANOVA. Comparison between two different conditions was performed using unpaired Student T-test if values followed a Gaussian distribution, Mann-Whitney test otherwise. Significance is assigned by \* for  $p \le 0.05$ , \*\* for  $p \le 0.01$ , \*\*\* for  $p \le 0.001$ .

#### 502 Simulation code

The simulation code, implemented with STEPS 3.5.0, and the meshes are available on ModelDB (*McDougal et al., 2017*) at http://modeldb.yale.edu/266928, access code: lto42@tpk3D?. The original model from Depired et al. (*Depired et al., 2010*) is publicle at http://modeldb.yale.edu/247004

nal model from Denizot et al. (*Denizot et al., 2019a*) is available at http://modeldb.yale.edu/247694.

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**Table 2.** Characteristics of meshes used to investigate the effect of voxel size on  $Ca^{2+}$  signals. Cylinder geometries were generated with various total number of tetrahedra (geometry  $Cyl_i$  with  $i \in [1, 8]$ , see also Fig 1A), resulting in different voxel sizes.  $V_{mean}$  corresponds to the average voxel volume,  $V_{std}$  to its standard deviation,  $V_{max}$  to the maximum voxel volume and  $V_{min}$  to the minimum voxel volume in stude mesh. Volumes are expressed in  $nm^3$ . Diff  $(nm^3)$  corresponds to  $V_{max} - V_{min}$  while Diff (%) is the ratio  $\frac{V_{max} - V_{min}}{V_{max}} * 100$ 

Geom	# tet	$V_{\rm mean}$	$V_{\rm std}$	$V_{\rm max}$	$V_{ m min}$	Diff $(nm^3)$	Diff (%)
$Cyl_1$	372148	84	25	296	15	281	335
$Cyl_2$	274233	115	34	389	20	369	321
$Cyl_3$	125927	249	71	761	33	728	292
$Cyl_4$	40077	782	229	2200	67	2133	273
$Cyl_5$	11523	2700	790	7521	177	7344	272
$Cyl_6$	3103	9900	3200	24000	94	23906	241
$Cyl_7$	1417	21000	11000	62000	241	61759	294
$Cyl_8$	945	32000	28000	145000	241	144759	452

#### 729 Supplemental Movie 1

Movie presenting a simulation of the bleaching protocol, with  $d_{\text{shaft}} = \frac{d_0}{a}$ . Fluorescing ZsGreen 730 molecules are in red and bleached, non-fluorescing, ZsGreen are in yellow. Molecule position 731 was updated every 1 ms. The plot presents the variation of the number of fluorescing ZsGreen 732 molecules with time in the central node. Note that, to facilitate visualization, here [ZsGreen] = 5 733  $\mu$ M. Before the bleaching event, all ZsGreen proteins (red) fluoresce. At bleaching time, fluorescing 734 molecules in the bleached region encounter conformational modifications that prevent them from 735 fluorescing (yellow molecules). Consequently, the fluorescence level drops to  $I_0$ . Because of the 736 diffusion of molecules in the cell, the fluorescence level in the central node then increases until it 737 reaches a new baseline  $I_{inf}$ , after a recovery time  $\tau$ . Fluorescing ZsGreen molecules are in red and 738 bleached, non-fluorescing, ZsGreen are in yellow. 739

#### 740 Supplemental Movie 2

Movie presenting a simulation of the neuronal stimulation protocol, with  $d_{\text{shaft}} = \frac{d_0}{2}$  and  $\text{Ca}^{2+}$  influx rate at the plasma membrane  $k_{Ca} = 0 \text{ s}^{-1}$ . 100 IP<sub>3</sub> molecules are injected in Node 1 at  $t = t_0 = 0.1$ s, while the number of Ca-GCaMP, IP<sub>3</sub> and IP<sub>3</sub>R channels in the open state are monitored in nodes 1 and 2. Molecule position was updated every 0.1 ms. Ca-GCaMP molecules are in yellow, IP<sub>3</sub> in red and IP<sub>3</sub>R in blue. Note that the size of molecules in the movie was increased to facilitate visualization.

Speed was increased 5-fold for visualization purposes.



**Figure 1-Figure supplement 1. Sensitivity study of the effect of voxel size on**  $Ca^{2+}$  **signals.** (*A*) Simulations were performed in a cylinder geometry with various numbers of tetrahedra. 4 examples are presented here, " $Cyl_1$ " (A1), " $Cyl_3$ " (A2), " $Cyl_5$ " (A3) and " $Cyl_8$ " (A4). Please refer to Table 2 for details on the characteristics of each mesh. (B) Study of the average number of IP3R in the ip3\_IP3R state (IP<sub>3</sub> bound to its binding site on IP<sub>3</sub>R, B1) and in the caa\_IP3R state (Ca<sup>2+</sup> bound to the activating site of IP<sub>3</sub>R, B2) depending on the mimimum voxel size of the mesh.



Figure 3-Figure supplement 1. Sensitivity study of the effect of shaft width on local  $Ca^{2+}$  signals upon single node stimulation. (A) Screenshot of a simulation in the "5nodes"  $d_{shaft} = \frac{d_0}{3}$  geometry. In those simulations, IP<sub>3</sub>Rs are only positioned on the ER membrane in nodes (white arrows). The number of IP<sub>3</sub>R channels is 300 for all values of  $d_{shaft}$ . (B) (*Top*) Node 1 was stimulated at  $t=t_0=1s$ , while  $Ca^{2+}$  activity was monitored in nodes 1 and 2. (*Bottom*) Representative  $Ca^{2+}$  traces in node 1 and node 2 for  $d_{shaft}=d_0$  (red),  $\frac{d_0}{2}$  (black) and  $\frac{d_0}{3}$  (blue). (*C*) The frequency of IP<sub>3</sub>R opening increases with  $d_{shaft}$  decreases in nodes 1 (\*\*\*) and 2 (\*\*\*). (*D*) (*Top*) In a second set of simulations, node 3 was stimulated at  $t=t_0=1s$  ( $k_{Ca}=0$   $s^{-1}$ ), while  $Ca^{2+}$  activity was monitored in nodes 3 and 4. (*Bottom*) Representative [Ca-GCaMP] traces in nodes 3 and 4, expressed as SNR (see Methods), for  $d_{shaft}=d_0$  (red),  $\frac{d_0}{2}$  (black) and  $\frac{d_0}{3}$  (blue). (*E1*) The frequency of IP<sub>3</sub>R opening increases when  $d_{shaft}$  decreases in node 3 (\*\*\*) and 4 (\*\*\*). (*E2*)  $Ca^{2+}$  peak probability increases when  $d_{shaft}$  decreases in node 3 (\*\*\*) and 4 (\*\*\*). (*E2*)  $Ca^{2+}$  peak probability increases when  $d_{shaft}$  decreases in node 3 (\*\*\*) and 4 (\*\*\*). (*E3*) Peak amplitude increases when  $d_{shaft}$  decreases in node 3 (\*\*\*) and 4 (\*\*\*). (*E3*) Peak amplitude increases when  $d_{shaft}$  decreases in node 3 (\*\*\*) and 4 (\*\*\*). (*E3*) Peak amplitude increases when  $d_{shaft}$  decreases in node 3 (\*\*\*) and 4 (\*\*\*). (*E3*) Peak amplitude increases when  $d_{shaft}$  decreases in node 3 (\*\*\*) and 4 (\*\*\*). (*E3*) Peak amplitude increases when  $d_{shaft}$  decreases in node 3 (\*\*\*) and 4 (\*\*\*). (*E3*) Peak amplitude increases when  $d_{shaft}$  decreases in node 3 (\*\*\*) and 4 (\*\*\*). (*E3*) Peak amplitude increases when  $d_{shaft}$  decreases in node 3 (\*\*\*) and 4 (\*\*\*). (*E3* Peak amplitude increases when  $d_{shaft}$  decreases in node 3 (\*\*\*)



**Figure 3-Figure supplement 2.** Effect of  $Ca^{2+}$  influx rate at the plasma membrane on local  $Ca^{2+}$  signals. *A*) (*Top*) Neuronal stimulation protocol simulated for each geometry: node 1 was stimulated at  $t=t_0=1$ s, while  $Ca^{2+}$  activity was monitored in node 2. Representative  $Ca^{2+}$  traces for shaft width  $d_{shaft} = d_0$  (red),  $\frac{d_0}{2}$  (black) and  $\frac{d_0}{3}$  (blue), with a  $Ca^{2+}$  influx rate at the plasma membrane  $k_{Ca}=0$  (top), 100 (middle) and 1000  $s^{-1}$  (bottom), expressed as SNR (see Methods). (*B*) Quantification of the effect of  $d_{shaft}$  on  $Ca^{2+}$  signal characteristics for  $k_{Ca}=0$ , 10, 100, 300, 700 and 1000  $s^{-1}$ . Data are represented as mean  $\pm$  STD, n=20 for each set of parameters tested.  $Ca^{2+}$  peak probability increases (\*\*\*, *B1*), Time to 1<sup>st</sup> peak decreases (\*\*\*, *B2*), peak amplitude (\*\*\*, *B3*) and duration (\*\*\*, *B4*) increase when  $d_{shaft}$  decreases, for  $k_{Ca}=0$ , 10, 100, 300, 700 and 1000  $s^{-1}$ .  $Ca^{2+}$  peak characteristics did not statistically vary with  $k_{Ca}$ . The effect of  $k_{Ca}$  on each  $Ca^{2+}$  signal characteristic was tested using one-way ANOVA.



Figure 3-Figure supplement 3. Sensitivity study of the effect of boundary conditions on local Ca<sup>2+</sup> activity upon single node stimulation. (A) Geometries used in the simulations were the "5nodes" geometries (Fig 1A). Boundary conditions were absorbing at the extremity of node 5 (blue), while the remaining boundaries were reflective (green). This mimics the connection of the modeled astrocyte branchlet to the rest of the cell. (B) (Top) Neuronal stimulation protocol simulated for each geometry: node 1 was stimulated at  $t=t_0=1s$  ( $k_{Ca}=0$  s<sup>-1</sup>), while Ca<sup>2+</sup> activity was monitored in nodes 1 and 2. (Bottom) Representative [Ca-GCaMP] traces in nodes 1 and 2, expressed as SNR (see Methods), for  $d_{\text{shaft}} = d_0$  (red),  $\frac{d_0}{2}$  (black) and  $\frac{d_0}{3}$  (blue). (C1) Ca<sup>2+</sup> peak probability increases when  $d_{\text{shaft}}$  decreases in nodes 1 (\*\*\*) and 2 (\*\*\*). (C2) Time to 1<sup>st</sup> peak does not change with d<sub>shaft</sub>, both in node 1 (p-value=0.85) and 2 (p-value=0.90). (C3) Peak amplitude increases when  $d_{\text{shaft}}$  decreases in nodes 1 (p-value=0.0056 \*\*) and 2 (p-value=0.0021 \*\*). (C4) Peak duration increases when d<sub>shaft</sub> decreases in nodes 1 (p-value=0.0051 \*\*) and 2 (p-value=0.014 \*). (C5) The frequency of IP<sub>3</sub>R opening increases when  $d_{\text{shaft}}$  decreases in both nodes 1 and 2 (\*\*\*). Note that there were no  $Ca^{2+}$  peak in simulations with  $d_{shaft}=d_0$ .  $Ca^{2+}$  peak characteristics were not statistically different between node 1 and 2. Data are represented as mean ± STD, n=20 for each geometry. The effect of  $d_{\text{shaft}}$  on each Ca<sup>2+</sup> signal characteristic was tested using one-way ANOVA. Significance is assigned by \* for  $p \le 0.05$ , \*\* for  $p \le 0.01$ , \*\*\* for  $p \le 0.001$ .

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Figure 3-Figure supplement 4. Node/shaft width ratio and node volume control local  $Ca^{2+}$ activity. (A) Screenshots from STEPS visualization toolkit revealing meshes used in this study, that contain 5 identical nodes and 4 identical shafts. (B) (Top) Neuronal stimulation protocol simulated for each geometry: node 1 was stimulated at  $t=t_0=1s$  ( $k_{Ca}=0 s^{-1}$ ), while  $Ca^{2+}$  activity was recorded in node 2. (Bottom) Representative Ca<sup>2+</sup> traces in node 2 in geometries with node/shaft width ratio  $\delta$  =  $\frac{d_0}{d_{shaft}}$ = 1 (red and gray), 2 (black) and 3 (blue), expressed as SNR (see Methods). Red and grey traces correspond to Ca<sup>2+</sup> signals in geometries with  $\delta$ =1 and a volume  $V_1$ =0.620  $\mu m^3$  and  $V_1$ =0.258  $\mu m^3$ , respectively. Black and blue traces were recorded in geometries with  $V_2$ =0.263  $\mu m^3$  and  $V_3$ =0.195  $\mu m^3$ , respectively. (C) Quantification of Ca<sup>2+</sup> signal characteristics depending on node/shaft width ratio  $\delta$  and on process volume. Data are represented as mean  $\pm$  STD, n=20 for each geometry. (C1) Ca<sup>2+</sup> peak probability does not vary with  $\delta$  when  $V_1$ =0.258  $\mu m^3$  (p-value=0.22). (C2) Time to 1<sup>st</sup> peak decreases with  $\delta$  (p-value=0.0018 \*). (C3) Peak amplitude does not vary with  $\delta$  when  $V_1$ =0.258  $\mu m^3$ (p-value=0.16). (C4) Peak duration increases with  $\delta_i$  for both  $V_1$ =0.620  $\mu m^3$  and  $V_1$ =0.258  $\mu m^3$  (\*\*\*). (C5) The frequency of IP<sub>3</sub>R opening increases with  $\delta$ , for both  $V_1$ =0.620  $\mu m^3$  and  $V_1$ =0.258  $\mu m^3$  (\*\*\*). (D) Ca<sup>2+</sup> residency time in nodes increases with  $\delta$ , for both V<sub>1</sub>=0.620  $\mu m^3$  and V<sub>1</sub>=0.258  $\mu m^3$  (\*\*\*, n=300). The effect of node/shaft width ratio on each Ca<sup>2+</sup> signal characteristic was tested using one-way ANOVA. Significance is assigned by \* for  $p \le 0.05$ , \*\* for  $p \le 0.01$ , \*\*\* for  $p \le 0.001$ .



**Figure 3-Figure supplement 5. Thin shafts enhance local spontaneous**  $Ca^{2+}$  **activity.** (*A*) Neuronal stimulation protocol simulated for each geometry. 200  $Ca^{2+}$  ions were infused in Node 1 at time  $t=t_0$ , while  $Ca^{2+}$  activity was recorded in nodes 1 and 2. (*B*) Representative  $Ca^{2+}$  traces in node 1 (top) and node 2 (bottom) for  $d_{shaft}=d_0$  (red),  $\frac{d_0}{2}$  (black) and  $\frac{d_0}{3}$  (blue), expressed as SNR (see Methods). (*C*)  $Ca^{2+}$  peak probability increases when  $d_{shaft}$  decreases in node 2 (\*\*\*). Note that peak probability is 1 in node 1 as the injection of 200  $Ca^{2+}$  ions in node 1 results in a local Ca-GCaMP peak for all seed values tested. (*D1*) Peak amplitude increases when  $d_{shaft}$  decreases in node 1 (\*\*\*) and 2 (\*\*\*). (*D2*) The ratio between peak amplitude in node 2 and in Node 1 increases with shaft width (Spearman r=0.0006, p-value < 0.001 \*\*\*). (*E*) Time to  $1^{st}$  peak in node 2 increases with  $d_{shaft}$  (\*\*\*). Note that time to  $1^{st}$  peak does not vary with  $d_{shaft}$  in node 1 as it occurs quickly after  $Ca^{2+}$  injection, through the binding of the injected  $Ca^{2+}$  ions to GCaMP molecules. (*F*) Peak duration increases when  $d_{shaft}$  decreases in node 1 (\*\*\*) and 2 (\*\*\*). The effect of  $d_{shaft}$  on each  $Ca^{2+}$  signal characteristic was tested using one-way ANOVA. Significance is assigned by \* for  $p \le 0.05$ , \*\* for  $p \le 0.01$ , \*\*\* for  $p \le 0.001$ .



Figure 3-Figure supplement 6.  $Ca^{2+}$  peak probability, amplitude and duration decrease with ER surface area. (A) As the shape and distribution of the ER in fine processes have not been characterized in live tissue so far but are likely highly variable (Aboufares El Alaoui et al., 2021), simulations were performed in meshes with various ER shapes: "No ER", "Node ER" and "Node/shaft ER", in which there was no ER, discontinuous ER in nodes or an ER consisting in node/shaft alternations, respectively. (B) (Top) Neuronal stimulation protocol simulated for each geometry: node 1 was stimulated at  $t=t_0=1s$ , while Ca<sup>2+</sup> activity was monitored in nodes 1 and 2. (*Bottom*) Representative Ca<sup>2+</sup> traces in node 2, in "No ER" (green), "Node ER" (blue) and "Node/shaft ER" (black) geometries  $d_{\text{shaft}} = \frac{d_0}{2}$ , for  $k_{Ca}$ =0, 10, 100, 300, 700 and 1000  $s^{-1}$ , expressed as SNR (see Methods). (C) Quantification of peak characteristics depending on ER geometry and  $k_{Ca}$ . Ca<sup>2+</sup> peak probability (\*\*\*, C1), time to 1<sup>st</sup> peak (\*\*\*, C2), peak amplitude (\*\*\*, C3), duration (\*\*\*, C4) and the frequency of IP<sub>3</sub>R opening (\*\*\*, C5) vary with the ER morphology. Note that Ca<sup>2+</sup> peak characteristics did not vary with  $k_{Ca}$ . (D) Time to 1<sup>st</sup> decreases as ER surface area increases (\*\*\*) while Ca<sup>2+</sup> peak probability (\*\*\*), amplitude (\*\*\*) and duration (\*\*\*) as well as the frequency of  $IP_3R$  opening (\*\*\*) increase as ER surface area increases,  $k_{Ca}$ =0 s<sup>-1</sup>. Data are represented as mean ± STD, n=20 for each geometry. Significance is assigned by \* for  $p \le 0.05$ , \*\* for  $p \le 0.01$ , \*\*\* for  $p \le 0.001$ .



Figure 3-Figure supplement 7. Local Ca<sup>2+</sup> activity increases when shaft diameter decreases, for all ER geometries tested. (A) Screenshots displaying the geometries used to investigate the effect of ER geometry on Ca<sup>2+</sup> dynamics: "No ER", "Node ER", "Node/shaft ER" and "Cyl ER". (B) (Top) Neuronal stimulation protocol simulated for each geometry: node 1 was stimulated at  $t=t_0=1s$  $(k_{Ca}=0 \text{ s}^{-1})$ , while Ca<sup>2+</sup> activity was monitored in node 2. (*Bottom*) Representative Ca<sup>2+</sup> traces in node 2 for  $d_{\text{shaft}} = d_0$  (left),  $\frac{d_0}{2}$  (center) and  $\frac{d_0}{3}$  (right), in "No ER" (green), "Node ER" (blue), "Cyl ER" (red) and "Node/shaft ER" (black) geometries, expressed as SNR (see Methods). (C) Quantification of the effect of  $d_{\text{shaft}}$  on Ca<sup>2+</sup> dynamics. Note that no bar is visible for simulations in "Node ER"  $d_{\text{shaft}}=d_0$ geometries as no peak was detected. Results in "Node/shaft ER" geometries are presented in Fig3 but are added here (black bars) for comparison. (C1) Time to 1<sup>st</sup> peak in node 2 does not vary with d<sub>shaft</sub> in "Node ER" simulations (p-value=0.85) but increases with d<sub>shaft</sub> in "Cyl ER" simulations (p-value= 0.021 \*). (C2) Ca<sup>2+</sup> peak probability in node 2 increases when  $d_{shaft}$  decreases in "Node ER" simulations (\*\*\*) and in "Cyl ER" simulations (p-value=0.01 \*). (C3) Peak amplitude increases when d<sub>shaft</sub> decreases in "Node ER" geometries (p-value=0.027 \*) and in "Cyl ER" (p-value=0.01 \*). (C4) Peak duration increases when  $d_{shaft}$  decreases in "Node ER" simulations (p-value=0.028 \*) and in "Cyl ER" simulations (p-value=0.001 \*\*). Data are represented as mean  $\pm$  STD, n=20, for each geometry. The effect of  $d_{\text{shaft}}$  on each Ca<sup>2+</sup> signal characteristic was tested using one-way ANOVA. Significance is assigned by \* for  $p \le 0.05$ , \*\* for  $p \le 0.01$ , \*\*\* for  $p \le 0.001$ .



Figure 3-Figure supplement 8. Sensitivity study of the effect of ER morphology on  $Ca^{2+}$  dy**namics.** (A) Node  $Ca^{2+}$  residency time is not influenced by ER morphology. (A1) One  $Ca^{2+}$  ion was added in node 1 in geometries with different ER shapes: "No ER" (green), "Node ER" (blue), "Cyl ER" (red) and "Node/shaft ER" (black). (A2) For all ER shapes tested,  $Ca^{2+}$  residency time in nodes increases when  $d_{\text{shaft}}$  decreases. Node  $Ca^{2+}$  residency time does not change depending on ER morphology, suggesting that cellular morphology has a greater influence on compartmentalization than ER morphology in the meshes used in this study. Data are represented as mean  $\leq$  STD, n=300 for each geometry. (B) Sensitivity study of the effect of ER morphology on  $Ca^{2+}$  dynamics with constant number of IP<sub>3</sub>Rs. (B1) Simulations were performed in 'Node ER' (red) and "Node/shaft ER" (black) geometries with IP<sub>3</sub>R channels (white) located in nodes (Top), resulting in a constant number of IP3R channels for both ER shapes. Node 1 was stimulated at t=t0=1s ( $k_{C_0}$ =0 s<sup>-1</sup>), while Ca<sup>2+</sup> activity was monitored in node 2 (bottom). (B2-6) Quantification of Ca2+ signals depending on ER morphology with constant number of IP<sub>3</sub>R in node 2,  $d_{\text{shaft}} = \frac{d_0}{3}$ . Data are represented as mean  $\leq$  STD, n=20 for each geometry. Ca<sup>2+</sup> peak duration (B2), amplitude (B3), probability (B4) and delay (B5) do not vary with ER morphology when IP<sub>3</sub>R channels are located in nodes. (B6) IP<sub>3</sub>R opening frequency does not significantly differ between "Node ER" and "Node/shaft ER" geometries (p-value=0.06). Those results suggest that the decreased  $Ca^{2+}$  activity in branchlets that contain discontinuous ER reported in Fig 4 mainly results from the decreased number of IP<sub>3</sub>R channels associated with the decreased ER surface area of "Node ER" compared to "Node/shaft ER" morphology.



Figure 3-Figure supplement 9.  $Ca^{2+}$  indicators alter  $Ca^{2+}$  peak characteristics. (A) In order to investigate free  $Ca^{2+}$  peak probability, no GCaMP molecules were added to the model. (*Top*) At t= $t_0$ =1s, node 1 was stimulated ( $k_{Ca}$ =0 s<sup>-1</sup>), while Ca<sup>2+</sup> concentration was monitored in node 1. The geometry used for  $d_{\text{shaft}} = d_0$  corresponds to the geometry presented in Fig 1A. (*Middle*) Representative Ca-GCaMP traces in node 1, in simulations containing GCaMP molecules in geometries with shaft width  $d_{\text{shaft}} = d_0$  (light red),  $\frac{d_0}{2}$  (grey) and  $\frac{d_0}{3}$  (light blue). (*Bottom*) Representative free Ca<sup>2+</sup> traces in node 1, in the absence of GCaMP molecules, in geometries with shaft width  $d_{\text{shaft}} = d_0$  (red),  $\frac{d_0}{2}$ (black) and  $\frac{d_0}{2}$  (blue). The amplitude of Ca-GCaMP and free  $Ca^{2+}$  signals is expressed as SNR (see Methods). (B) Characteristics of free  $Ca^{2+}$  signals depending on  $d_{shaft}$ . Ca-GCaMP signals measured in simulations from Fig 3 are presented for comparison. (B1) Free  $Ca^{2+}$  peak probability does not vary with  $d_{shaft}$  (p-value=0.22). Ca-GCaMP peak probability is lower than free Ca<sup>2+</sup> peak probability for  $d_{\text{shaft}} = d_0$  (\*\*\*). (B2) Time to 1<sup>st</sup> free Ca<sup>2+</sup> peak increases with  $d_{\text{shaft}}$  (\*\*\*). Time to 1<sup>st</sup> Ca-GCaMP peak is higher than time to  $1^{st}$  free Ca<sup>2+</sup> peak, for any value of  $d_{shaft}$  (\*\*\*). (B3) Free Ca<sup>2+</sup> peak amplitude increases when  $d_{\text{shaft}}$  decreases (\*\*\*). Ca-GCaMP peak amplitude is lower than free Ca<sup>2+</sup> peak amplitude, for any value of  $d_{\text{shaft}}$  (\*\*\*). (B4) Free Ca<sup>2+</sup> peak duration increases when  $d_{\text{shaft}}$  decreases (\*\*\*). Ca-GCaMP peak duration is higher than free  $Ca^{2+}$  peak duration, for any value of  $d_{shaft}$  (\*\*\*). (B5) The frequency of IP<sub>3</sub>R opening increases when  $d_{\text{shaft}}$  decreases (\*\*\*). (C) Schematic summarizing the main result from this figure: increased Ca<sup>2+</sup> buffering is associated with decreased Ca<sup>2+</sup> peak probability and amplitude. Data are represented as mean  $\pm$  STD, n=20 for each geometry. The effect of d<sub>shaft</sub> on each free Ca<sup>2+</sup> signal characteristic was tested using one-way ANOVA. Significance is assigned by \* for  $p \le 0.05$ , \*\* for  $p \le 0.01$ , \*\*\* for  $p \le 0.001$ .



Figure 5-Figure supplement 1. Sensitivity study of the effect of boundary conditions on local Ca<sup>2+</sup> activity upon repeated neuronal stimuli. (A) Simulations were performed in the "5nodes" geometries (Fig1). Boundary conditions were absorbing at the extremity of node 5 (blue) while the remaining boundaries were characterized by reflective boundary conditions (green). Those boundary conditions mimic the connection of the modeled astrocyte branchlet to the rest of the cell. (B) (Top) node 1 was stimulated at t= $t_0$ =5s, node 2 at  $t_0 + \tau_{IP3}$ , node 3 at  $t_0 + 2\tau_{IP3}$  and node 4 at  $t_0 + 3\tau_{1P3}$ ,  $k_{Ca} = 0 s^{-1}$ , while Ca<sup>2+</sup> activity was monitored in node 5. (*Bottom*) Representative Ca<sup>2+</sup> traces for  $d_{\text{shaft}} = d_0$  (red),  $\frac{d_0}{2}$  (black) and  $\frac{d_0}{3}$  (blue), with  $\tau_{\text{IP3}} = 250$ ms (left) and 3000ms (right), expressed as SNR (see Methods). (C) (Left) Time to 1<sup>st</sup> peak in node 5 increases with  $\tau_{IP3}$  for  $d_{shaft} = d_0$  (\*\*\*),  $d_{shaft} = \frac{d_0}{2}$  (\*\*\*) and  $d_{\text{shaft}} = \frac{d_0}{3}$  (\*\*\*). Time to 1<sup>st</sup> peak is higher for  $d_{\text{shaft}} = d_0$  compared to  $d_{\text{shaft}} = \frac{d_0}{2}$  and  $d_{\text{shaft}} = \frac{d_0}{3}$ . (*Right*) Ca<sup>2+</sup> peak probability in node 5 is lower for  $d_{\text{shaft}} = d_0$  compared to  $d_{\text{shaft}} = \frac{d_0}{2}$  and  $d_{\text{shaft}} = \frac{d_0}{3}$  and decreases as  $\tau_{\text{IP3}}$  increases for  $d_{\text{shaft}} = d_0$  (\*\*\*) and  $d_{\text{shaft}} = \frac{d_0}{2}$  (\*\*\*) but not  $d_{\text{shaft}} = \frac{d_0}{3}$  (p-value=0.054). Note that Ca<sup>2+</sup> peak probability was lower and time to 1st peak higher compared to simulations with reflective boundary conditions. Data are represented as mean  $\pm$  STD, n=20 for each value of  $d_{shaft}$  and of  $\tau_{IP3}$ . Lines are guides for the eyes. The effect of  $d_{\text{shaft}}$  on each Ca<sup>2+</sup> signal characteristic was tested using one-way ANOVA. Significance is assigned by \* for  $p \le 0.05$ , \*\* for  $p \le 0.01$ , \*\*\* for  $p \le 0.001$ .