

## Analysis of Ocean-Atmosphere Coupling from the Point of View of Domain Decomposition Methods

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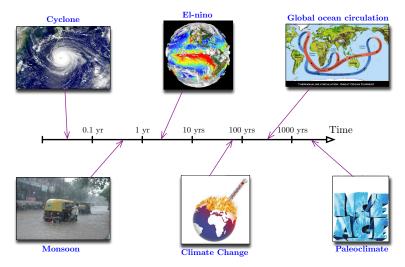
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# Analysis of Ocean-Atmosphere Coupling from the Point of View of Domain Decomposition Methods

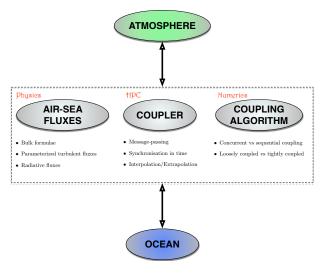
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#### Context Atmospheric and Oceanic Coupled Models (AOCMs)



#### Context

Atmospheric and Oceanic Coupled Models (AOCMs)



#### Content

- 1. Interface conditions and turbulent boundary fluxes
- 2. Algorithmic considerations and shortcomings of existing approaches
- 3. Schwarz algorithms for OA coupling: analysis of the iterative process
- 4. Application of Schwarz iterations in a climate model

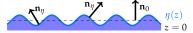
## Interface conditions and turbulent boundary fluxes

F. Lemarié - OA coupling formulation and algorithms

## Nature of interface conditions

The ocean and the atmosphere are two open systems exchanging both energy and matter through their common interface.

 $\mathbf{n}_0$  unit normal to the interface



· Net mass flux:

$$\mathcal{J}^{\text{mass}} = \mathcal{E} - \mathcal{P}_r - \mathcal{P}_s$$

Internal energy (enthalpy) flux:

$$h^{(sw)}\mathcal{J}^{ ext{mass}} + \mathbf{J}_{H}^{ ext{oce}} \cdot \mathbf{n}_{0} = \mathbf{J}_{H}^{ ext{atm}} \cdot \mathbf{n}_{0} + h^{(wv)}\mathcal{E} - h^{(liq)}\mathcal{P}_{r} - h^{(ice)}\mathcal{P}_{s}$$

Blue terms represent energy associated to phase changes.  $J_{H}^{atm} = J_{sen}^{atm} + J_{rad}^{atm}$  denotes the sum of sensible and radiative heat fluxes.

• Mechanical energy flux: continuity of stresses at the free boundary Normal stress:  $-p^{oce} + \sigma_{33}^{oce} = -p^{atm} + \sigma_{33}^{atm}$ Tangential stress:  $\sigma_{i3}^{atm} = \sigma_{i3}^{oce} = \tau_i^{atm}$ , (i = 1, 2)

Main concern: necessity to conserve energy and mass at the air-sea interface

#### Coupled problem (without phase changes)

$$\begin{array}{rcl} \partial_{t}\mathbf{v}^{\text{oce}} + 2\boldsymbol{\Omega} \times \mathbf{u}^{\text{oce}} + \nabla \cdot (\mathbf{u}^{\text{oce}} \otimes \mathbf{v}^{\text{oce}}) = -\frac{1}{\rho_{0}} \nabla p^{\text{oce}} - \frac{\rho^{\text{oce}}}{\rho_{0}} \mathbf{g} + \nabla \cdot \boldsymbol{\sigma}^{\text{oce}} \\ \mathbf{u}^{\text{oce}} &= (u^{\text{oce}}, v^{\text{oce}}, w^{\text{oce}}) & \nabla \cdot \mathbf{u}^{\text{oce}} = 0 \\ \mathbf{v}^{\text{oce}} &= (u^{\text{oce}}, v^{\text{oce}}, 0) & \rho_{0} c_{p}^{\text{oce}} \frac{D\theta^{\text{oce}}}{Dt} = -\nabla \cdot \mathbf{J}_{H}^{\text{oce}} = -\nabla \cdot (\mathbf{J}_{T}^{\text{oce}} + \mathbf{J}_{\text{rad}}^{\text{oce}}) \\ \rho^{\text{oce}} = \rho(\theta^{\text{oce}}, p_{0}(z)) \end{array}$$

$$\begin{split} \rho^{\mathrm{atm}} \left( \partial_t \mathbf{u}^{\mathrm{atm}} + 2\mathbf{\Omega} \times \mathbf{u}^{\mathrm{atm}} + \nabla \cdot \left( \mathbf{u}^{\mathrm{atm}} \otimes \mathbf{u}^{\mathrm{atm}} \right) \right) &= -\nabla p^{\mathrm{atm}} - \rho^{\mathrm{atm}} \mathbf{g} + \rho^{\mathrm{atm}} \nabla \cdot \boldsymbol{\sigma}^{\mathrm{atm}} \\ \partial_t \rho^{\mathrm{atm}} + \nabla \cdot \left( \rho^{\mathrm{atm}} \mathbf{u}^{\mathrm{atm}} \right) &= 0 \\ \rho^{\mathrm{atm}} c_p^{\mathrm{atm}} \frac{D\theta^{\mathrm{atm}}}{Dt} &= -\nabla \cdot \mathbf{J}_H^{\mathrm{atm}} = \left( \mathbf{J}_T^{\mathrm{atm}} + \mathbf{J}_{\mathrm{rad}}^{\mathrm{atm}} \right) \\ p^{\mathrm{atm}} = g(\rho^{\mathrm{atm}}, \theta^{\mathrm{atm}}) \end{split}$$

Interface conditions

$$\begin{array}{lll} p^{\mathrm{oce}}|_{z=\eta} &=& p^{\mathrm{atm}} \\ \mathbf{J}_{H}^{\mathrm{oce}} \cdot \mathbf{n}_{0} &=& \mathbf{J}_{H}^{\mathrm{atm}} \cdot \mathbf{n}_{0} &=& \mathcal{J}_{\mathrm{Sen}} + \mathcal{J}_{\mathrm{LW}} + \mathcal{J}_{\mathrm{SW}} \\ \rho^{\mathrm{oce}}(\boldsymbol{\sigma}^{\mathrm{oce}} \mathbf{n}_{0}) &=& \rho^{\mathrm{atm}}(\boldsymbol{\sigma}^{\mathrm{atm}} \mathbf{n}_{0}) &=& (\boldsymbol{\tau}^{a}, 0)^{T} \end{array}$$

F. Lemarié – OA coupling formulation and algorithms

### Computation of the boundary fluxes $au^a$ and $\mathcal{J}_{ ext{sen}}$

The boundary fluxes are the result of processes in turbulent boundary layers

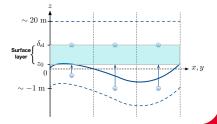
 $\Rightarrow$  they need be parameterized in terms of resolved (Reynolds-averaged) quantities of the model

 $\Rightarrow$  Semi-empirical Monin-Obukhov similarity theory is the basis to derive turbulent quantities from the mean variables available from the models

 $\rightarrow$  Generalization of the classical law of the wall to stratified conditions

The MO theory provides functional relationships to compute fundamental turbulent parameters  $u_{\star}$  and  $\theta_{\star}$  from quantities at the first model level

$$\|oldsymbol{ au}^a\|=
ho^{ ext{atm}}{oldsymbol{u}_\star}^2,\qquad \mathcal{J}_{ ext{sen}}=-
ho^{ ext{atm}}c_p^{ ext{atm}}{oldsymbol{u}_\star}{oldsymbol{ heta}_\star}$$



## MO theory: standard wall law + stability corrections

$$\mathbf{u}^{\text{atm}}(z) = \mathbf{u}^{\text{oce}}(z_0) - \frac{u_{\star}}{\kappa} \left[ \ln\left(\frac{z}{z_0}\right) - \psi_m\left(\frac{z}{L_{\text{Ob}}}\right) + \psi_m\left(\frac{z_0}{L_{\text{Ob}}}\right) \right] e^{i\theta_{\tau}} \theta^{\text{atm}}(z) = \theta^{\text{oce}}(z_0) - \frac{\theta_{\star}}{\kappa} \left[ \ln\left(\frac{z}{z_0}\right) - \psi_s\left(\frac{z}{L_{\text{Ob}}}\right) + \psi_s\left(\frac{z_0}{L_{\text{Ob}}}\right) \right]$$

#### ▶ Usual form :

$$\boldsymbol{\tau}^{a} = \rho^{\operatorname{atm}} C_{D} \| \mathbf{u}^{\operatorname{atm}}(z_{\operatorname{atm}}^{1}) - \mathbf{u}^{\operatorname{oce}}(z_{\operatorname{oce}}^{1}) \| (\mathbf{u}^{\operatorname{atm}}(z_{\operatorname{atm}}^{1}) - \mathbf{u}^{\operatorname{oce}}(z_{\operatorname{oce}}^{1}))$$
$$\mathcal{J}_{\operatorname{sen}} = \rho^{\operatorname{atm}} c_{p}^{\operatorname{atm}} C_{H} \| \mathbf{u}^{\operatorname{atm}}(z_{\operatorname{atm}}^{1}) - \mathbf{u}^{\operatorname{oce}}(z_{\operatorname{oce}}^{1}) \| (\theta^{\operatorname{atm}}(z_{\operatorname{atm}}^{1}) - \theta^{\operatorname{oce}}(z_{\operatorname{oce}}^{1}))$$

#### **General comments**

- Even under ideal conditions, the theory has an accuracy of only about 10–20% [Foken, 2006]
- Bill Large (2006) "Surface fluxes for practitioners of global ocean data assimilation"
  - For hourly fluxes on a spatial scale of 10 km, there is at least a factor of 2 uncertainty due to transfer coefficient variability on these scales
  - Long-term averaging is required before the uncertainty in bulk fluxes is minimized

 $\Rightarrow$  Internal time-scale  $\varDelta t_{\rm MO}$  to keep uncertainty on turbulent flux estimates at a "reasonable level"



## Algorithmic considerations and shortcomings of existing approaches

## Various alternatives

- Concurrent coupling vs sequential coupling (aka parallel vs multiplicative)
- Global-in-time vs local-in-time
- Intergrid transfer operator in time

#### Some criteria to choose an appropriate coupling algorithm

- · Practical aspects
  - Computational efficiency (time to solution & scalability)
  - Minimal modification to existing codes
- Numerical & physical aspects
  - Numerical stability and consistency
  - Conservation properties

(in a weak or strong sense  $\sim$  local-in-time vs global-in-time )

- Consistent with underlying assumptions of physical parameterizations (e.g.  $\varDelta t_{MO},\,\varDelta t_{rad},\,\text{PBL}$  scheme, ...)
- Vertical physics is handled implicitly in time

## Standard partitioned time-stepping methods in CMs

#### 4 variants:

- Global-in-time concurrent coupling (e.g. IPSL-CM6, CNRM-CM)
- Global-in-time "atmosphere first" sequential coupling (e.g. ECMWF)
- Global-in-time "atmosphere first" concurrent coupling (e.g. RPN)
- Local-in-time (used exclusively in regional coupled models so far)

Illustration on a simplified 1D coupling problem

Momentum exchange between two vertical columns

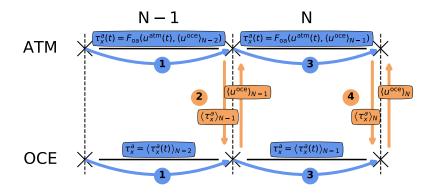
$$\begin{aligned} \partial_t u^{\text{atm}} &= -\partial_z \sigma_{xz}^{\text{atm}} = \partial_z \left( K_z^a \partial_z u^{\text{atm}} \right), & \text{ in } (0, h_{\text{atm}}) \times (0, T) \\ \partial_t u^{\text{oce}} &= -\partial_z \sigma_{xz}^{\text{oce}} = \partial_z \left( K_z^o \partial_z u^{\text{oce}} \right), & \text{ in } (-h_{\text{oce}}, 0) \times (0, T) \end{aligned}$$

+ appropriate initial and external B.C.

**Global-in-time concurrent coupling**  $(0,T) = \bigcup_{N=0}^{K} \mathcal{T}_{N}, \mathcal{T}_{N} = (t_{N}, t_{N-1})$ 

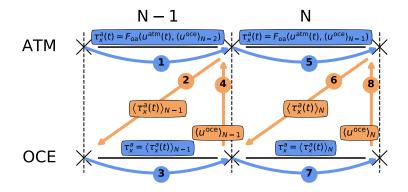
• 
$$\tau_x^a = F_{oa}(u^{atm}(z_a^1), u^{oce}(z_o^1))$$

- Boundary fluxes are computed within the atmospheric component
- $\triangleright \text{ Flux conservation: } \left( \sum_{N=1}^{K} \langle \tau_x^a(t) \rangle_N \right)^{\text{oce}} = \left( \langle \tau_x^a(t) \rangle_{0,...,K-1} \right)^{\text{atm}}$



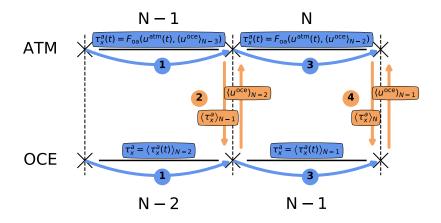
## Global-in-time "atmosphere first" sequential coupling

- $\tau_x^a = F_{\text{oa}}(u^{\text{atm}}(z_a^1), u^{\text{oce}}(z_o^1))$
- · Boundary fluxes are computed within the atmospheric component
- · Flux conservation is re-synchronized in time



## Global-in-time "atmosphere first" concurrent coupling

- $\tau_x^a = F_{\text{oa}}(u^{\text{atm}}(z_a^1), u^{\text{oce}}(z_o^1))$
- Boundary fluxes are computed within the atmospheric component



#### Global-in-time approach (sequential or concurrent)

- + Both models forced by the exact same mean flux on a given time window (except a one-window lag in the concurrent coupling)
- + Models communicate only once per time window
- Consistent with the underlying assumptions of some physical parameterizations (decouples the dynamical and physical time steps)
- Shifted retroaction  $\rightarrow$  loosely coupled solution
- Sequential coupling suppresses a level of parallelism and generally increases time to solution
- In the oceanic component: discontinuity in forcing fields between two successive time windows
- Existing global-in-time approaches = one single iteration of a global-in-time Schwarz algorithm

Local-in-time approach ( $\Delta t_{\rm oce} = \Delta t_{\rm atm}$ ) ATM model

$$\begin{cases} u_{\text{atm}}^{n+1} &= u_{\text{atm}}^n + \Delta t_{\text{atm}} \partial_z \left( K_z^a \partial_z u_{\text{atm}}^{n+1} \right) \\ K_z^a \partial_z u_{\text{atm}}^{n+1}(z=0) &= C_D \| u_{\text{atm}}^n(z_a^1) - u_{\text{oce}}^n(z_o^1) \| (u_{\text{atm}}^{n+a}(z_a^1) - u_{\text{oce}}^n(z_o^1)) \end{cases}$$

OCE model

$$\begin{pmatrix} u_{\rm occ}^{n+1} &= u_{\rm o}^{n} + \Delta t_{\rm occ} \partial_{z} \left( K_{z}^{\rm o} \partial_{z} u_{\rm occ}^{n+1} \right) \\ \rho_{\rm o} K_{z}^{\rm o} \partial_{z} u_{\rm o}^{n+1} (z=0) &= \rho_{\rm a} K_{z}^{\rm a} \partial_{z} u_{\rm atm}^{n+1} (z=0) \end{cases}$$

- a = 1: implicit flux coupling (sequential)
- a = 0: explicit flux coupling (conditionally stable, e.g. [Zhang et al., 2020])

#### Local-in-time approach

- lagged coupling  $\rightarrow$  loosely coupled partitioned scheme
- Relevance of instantaneous air-sea fluxes ? (large uncertainties)
- Very frequent exchanges/remapping of interface data between models
- + Ability to represent processes related to diurnal cycle

• Existing local-in-time approaches = one single iteration of a local-in-time Schwarz algorithm

## How to achieve a tighter coupling: Schwarz algorithms

• [Keyes et al. (2013)]: "Using an approach that ignores strong couplings between components gives a false sense of completion"

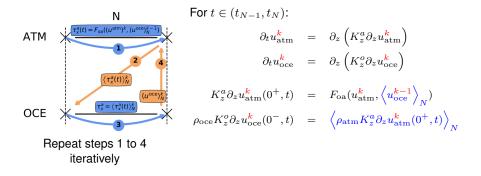
If the iterations actually fail to converge, using only one iteration won't reveal this fact but in this case numerical results would be questionable

$$\left\{ \begin{array}{rcl} \partial_t u_1^k - \nabla \cdot (\nu_1 \nabla u_1^k) &=& f_1, \qquad x \in \Omega_1 \\ \partial_t u_2^k - \nabla \cdot (\nu_2 \nabla u_2^k) &=& f_2, \qquad x \in \Omega_2 \\ & u_1^k &=& u_2^{k-1}, \qquad x \in \Gamma \\ & \nu_2 \nabla u_2^k &=& \nu_1 \nabla u_1^k, \quad x \in \Gamma \end{array} \right.$$

Convergence rate :  $R = \sqrt{\nu_2/\nu_1}$ 

- BUT: tight coupling between components require smoothness
- *Easy way to try it* : Schwarz algorithms (global-in-time for multiphysics problems; only require "perfect" restartibility of numerical models)

# Global-in-time domain decomposition based on Schwarz method



Does it converge ? If yes, what's the impact on the physics ?



#### Schwarz algorithms for OA coupling: analysis of the iterative process

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## A convenient framework: Schwarz methods

- Huge gap to fill between the theory and practical applications in the analysis of the iterative process
- The convergence analysis usually done at a continuous level for linear problems with constant coefficients and no averaging of boundary data

#### In the OA coupling case:

- · Non-linear transmission conditions defined in a semi-discrete sense
- Turbulent viscosities and diffusivities vary greatly in time and space
- · Boundary data are averaged in time

- ▷ The convergence properties depend on the whole viscosity profile  $\nu(z)$ . Strong influence of the turbulent zone [Thery et al. (2021)]
- Impact of boundary averaging for linear problems: solution has the correct average [Thery (2020)]

#### Semi-discrete coupled Ekman problem

$$\begin{aligned} \partial_{t} (\mathbf{u}_{m}^{\mathrm{atm}})^{k} + f \mathbf{e}_{\mathbf{z}} \times (\mathbf{u}_{m}^{\mathrm{atm}})^{k} &= \frac{\nu_{m+1/2}^{a}}{h_{m}} \left( \frac{\mathbf{u}_{m+1}^{\mathrm{atm}} - \mathbf{u}_{m}^{\mathrm{atm}}}{h_{m+1/2}} \right)^{k} - \frac{\nu_{m-1/2}^{a}}{h_{m}} \left( \frac{\mathbf{u}_{m}^{\mathrm{atm}} - \mathbf{u}_{m-1}^{\mathrm{atm}}}{h_{m-1/2}} \right)^{k} \\ \partial_{t} (\mathbf{u}_{m}^{\mathrm{oce}})^{k} + f \mathbf{e}_{\mathbf{z}} \times (\mathbf{u}_{m}^{\mathrm{oce}})^{k} &= \frac{\nu_{m+1/2}^{o}}{h_{m}} \left( \frac{\mathbf{u}_{m+1}^{\mathrm{oce}} - \mathbf{u}_{m}^{\mathrm{oce}}}{h_{m+1/2}} \right)^{k} - \frac{\nu_{m-1/2}^{o}}{h_{m}} \left( \frac{\mathbf{u}_{m}^{\mathrm{oce}} - \mathbf{u}_{m-1}^{\mathrm{oce}}}{h_{m-1/2}} \right)^{k} \\ \left( \nu_{1/2}^{a} \frac{\mathbf{u}_{1}^{\mathrm{atm}} - \mathbf{u}_{0}^{\mathrm{atm}}}{h_{1/2}} \right)^{k} &= C_{D} \| (\mathbf{u}_{1}^{\mathrm{atm}})^{k-1} - (\mathbf{u}_{N}^{\mathrm{oce}})^{k-1} \| \left( (\mathbf{u}_{1}^{\mathrm{atm}})^{k-1+\theta} - (\mathbf{u}_{N}^{\mathrm{oce}})^{k-1} \right) \\ \left( \nu_{N+1/2}^{o} \frac{\mathbf{u}_{N+1}^{\mathrm{oce}} - \mathbf{u}_{N}^{\mathrm{oce}}}{h_{N+1/2}} \right)^{k} &= \frac{\rho^{\mathrm{atm}}}{\rho^{\mathrm{oce}}} \left( \nu_{1/2}^{a} \frac{\mathbf{u}_{1}^{\mathrm{atm}} - \mathbf{u}_{0}^{\mathrm{atm}}}{h_{1/2}} \right)^{k} \end{aligned}$$
with  $(\mathbf{u}_{1}^{\mathrm{atm}})^{k-1+\theta} = \theta (\mathbf{u}_{1}^{\mathrm{atm}})^{k} + (1-\theta) (\mathbf{u}_{1}^{\mathrm{atm}})^{k-1}. \end{aligned}$ 

Asymptotic convergence rate independent from iterates  $\left(\varepsilon = \frac{\rho^{\text{atm}}}{\rho^{\text{oce}}}\right)$ 

$$\lim_{(\omega+f)\to 0}\xi = \frac{1}{\theta} \left| \frac{3}{2} - \theta + \frac{3}{2}\varepsilon \sqrt{\frac{\nu_a}{\nu_o}} \right|, \qquad \lim_{(\omega+f)\to\infty}\xi = 0$$

• Optimization for low frequencies:  $\theta^{\text{opt}} = 3/2$ 

#### Semi-discrete coupled Ekman problem

Asymptotic convergence rate independent from iterates  $\left(\varepsilon = \frac{\rho^{\text{atm}}}{\rho^{\text{oce}}}\right)$ 

$$\lim_{(\omega+f)\to 0} \xi = \frac{1}{\theta} \left| \frac{3}{2} - \theta + \frac{3}{2} \varepsilon \sqrt{\frac{\nu_a}{\nu_o}} \right|, \qquad \lim_{(\omega+f)\to\infty} \xi = 0$$

- Optimization for low frequencies:  $\theta^{\text{opt}} = 3/2$
- Assuming  $C_D \| (\mathbf{u}_1^{\text{atm}})^{k-1} (\mathbf{u}_N^{\text{oce}})^{k-1} \| = \text{cst}$  would give  $\theta^{\text{opt}} = 1$

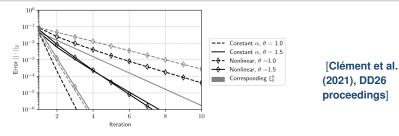


Fig. 2 Evolution of the  $L^2$  norm of the errors. Black lines represent the observed convergence; grey lines are the estimated convergence with slopes  $\xi_0$  for linear cases and  $\xi_0^q$  for quadratic cases.



Application of Schwarz iterations in a climate model

F. Lemarié - OA coupling formulation and algorithms

## Application of Schwarz iterations in a realistic CM

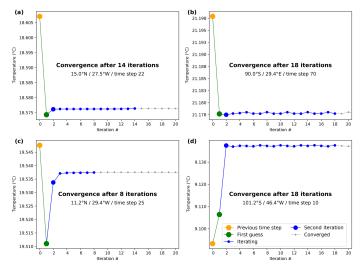
Marti O., S. Nguyen, P. Braconnot, S. Valcke, F. Lemarié, and E. Blayo, 2021: A Schwarz iterative method to evaluate ocean-atmosphere coupling schemes. Implementation and diagnostics in *IPSL-CM6-SW-VLR*, Geosci. Model Dev.

#### **Experiments:**

- State of the art model: ocean, atmosphere, sea-ice, land (used for CMIP6)
- Atm. component:  $3.75^{\circ} \times 1.875^{\circ}$  (39 vertical levels)
- Oce. component:  $2^{\circ} \times 2^{\circ}$  (31 vertical levels)
- 3 numerical coupling methods:
  - Global-in-time concurrent (parallel)
  - Global-in-time "atmosphere first" sequential
  - Global-in-time Schwarz (50 iterations with  $\theta = 1$ )
- 5 day experiments
- Time windows: 1 hour or 4 hours

### **Behavior during iterations**

Sea surface temperature evolution with respect to the iterations at 4 different locations

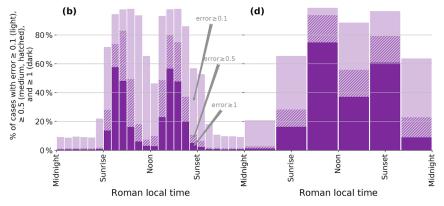


(a,b) 4 hour time window; (c,d) 1 hour time window

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## Diagnosing the error ${\mathcal E}$ of lagged coupling

For a given time window  $(t_{N-1}, t_N)$ ,  $\mathcal{E} = \frac{\text{SST}^{\text{cvg}}(t_N) - \text{SST}^{\text{par}}(t_N)}{\text{SST}^{\text{cvg}}(t_N) - \text{SST}^{\text{cvg}}(t_{N-1})}$ 

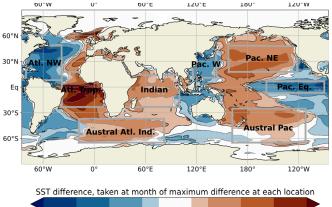


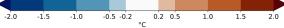
 $\Rightarrow$  large differences after sunrise and before sunset, when the external forcing (insolation at the top of the atmosphere) has the fastest pace of change

## Application of Schwarz iterations in a realistic CM

Results from 1 year ensemble simulations (20 ensembles)

Monthly average of the ensemble mean sea surface temperature (SST) difference between Schwarz vs concurrent (parallel) coupling





#### Summary

- Present ocean-atmosphere coupling methods correspond to loosely coupled partitioned scheme
- Schwarz domain decomposition methods due to their inherent simplicity
  provide a convenient framework for evaluating existing methods
- The convergence/divergence of the iterative Schwarz method can be used as an indicator for the degree of *compatibility* of models and particularly their physical parameterizations
- As soon as the MO theory remains the standard for air-sea fluxes estimate, some form of averaging in the boundary data is needed

#### **Future work**

- ▷ The iterative process is not viable for production runs. How to get the best possible estimate of the converged solution with only 1 or 2 iterations ?
- Need for more systematic benchmarking of coupled models under simplified settings (!)

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