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Diffusion MRI-Based Cytoarchitecture Measurements in Brain Gray Matter using Likelihood-Free Inference

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Synopsis

We propose a new method to solve the inverse problem of relating the diffusion MRI signal with cytoarchitectural characteristics in brain gray matter. Specifically, our method has quantitative sensitivity to soma density and volume. Our solution is twofold. First, we propose a new forward model that relates summary statistics of the dMRI signal with tissue parameters, relying on six b-shells only. We then apply a likelihood-free inference based algorithm to invert the proposed model, which not only estimates the tissue parameters that best describe the acquired diffusion signal, but also a full posterior distribution over the parameter space.

Introduction

Effective characterisation of the brain grey matter cytoarchitecture with quantitative sensitivity to soma density and volume remains an unsolved challenge in diffusion MRI (dMRI). Current methods require demanding acquisitions and stabilise parameter fitting by enforcing constraints. Yet, these still encounter large indetermination areas in the solution space making the results unstable¹. We propose a new forward model requiring only six relatively sparse b-shells and that avoids indeterminacies.

Methods

Modeling Brain Gray Matter with a 3-compartment Model. We model grey matter tissue as three-compartmental², moving away from the Standard Model designed for white matter. The acquired signal is considered as resulting from a convex mixture of signals arising from somas, neurites, and extra-cellular space (ECS), under a no-exchanges assumption². Our direction-averaged grey matter signal model is then:

$$\frac{\bar{S}(q)}{S(0)} = f_n \bar{S}_{\text{neurites}}(q, D_a) + f_s \bar{S}_{\text{somas}}(q, D_s, r_s) + f_{\text{ECS}} \bar{S}_{\text{ECS}}(q, D_e), \text{ with } q(b) = \frac{1}{2\pi} \sqrt{\frac{b}{\tau}}$$

f_n , f_s and f_{ECS} represent neurites, somas and ECS signal fractions respectively ($f_n + f_s + f_{\text{ECS}} = 1$); D_a axial diffusivity inside neurites; D_s and D_e somas and extra-cellular diffusivities; and r_s the average soma radius. Neurites are modeled as 0-radius impermeable cylinders³:

$$\bar{S}_{\text{neurites}}(q) \simeq \frac{1}{4\sqrt{\pi\tau D_a}} \cdot q^{-1}$$

Somas are modeled as spheres and follow the GPD approximation⁴:

$$-\log \bar{S}_{\text{somas}}(q) = C(r_s, D_s) \cdot q^2 = q^2 \frac{2}{D_s \delta^2} \sum_{m=1}^{\infty} \frac{\alpha_m^{-4}}{\alpha_m^2 r_s^2 - 2} \cdot \left(2\delta - \frac{2 + e^{-\alpha_m^2 D_s (\Delta - \delta)} - e^{-\alpha_m^2 D_s \delta} - e^{-\alpha_m^2 D_s \Delta} + e^{-\alpha_m^2 D_s (\Delta + \delta)}}{\alpha_m^2 D_s} \right)$$

We exploit this relation to extract a parameter $C_s = C(r_s, D_s)[m^2]$ which, at fixed diffusivity D_s is modulated by the soma radius. The ECS is approximated as isotropic Gaussian diffusion:

$$-\log(\bar{S}_{\text{ECS}}(q)) = (2\pi q)^2 \tau D_e$$

An Invertible 3-compartment Model: dMRI Summary Statistics. Solving the inverse problem directly from Eq.1 leads to indeterminacies and bad parameter estimations. We therefore introduce rotationally invariant summary statistics to relate the dMRI signal to tissue parameters.

First, we compute a q-bounded RTOP, a direct measure of the restrictions of the diffusing fluid molecule motion⁵:

$$\text{RTOP}(q) = 4\pi \int_0^q \frac{\bar{S}(\eta)}{S(0)} \eta^2 d\eta$$

For q large enough, $\text{RTOP}(q)$ on our 3-compartment model (Eq.1) becomes:

$$\text{RTOP}(q) = \underbrace{f_s \left(\frac{\pi}{C_s} \right)^{3/2} + \frac{f_{\text{ECS}}}{8(\pi\tau D_e)^{3/2}}}_{a_{\text{fit}}} + \underbrace{\frac{f_n}{2} \cdot \sqrt{\frac{\pi}{\tau D_a}}}_{b_{\text{fit}}} \cdot q^2$$

Three different q-values are needed to estimate a_{fit} and b_{fit} .

Secondly, we extended LEMONADE¹, based on a moment decomposition for small q-values, to our 3-compartment model and extract four rotational invariant scalar indices that quantify grey matter microstructure:

$$\begin{cases} M^{(2),0} = f_n D_a + 3f_s \frac{C_s}{(2\pi)^2 \tau} + 3f_{\text{ECS}} D_e \\ M^{(2),2} = f_n D_a p_2 \\ M^{(4),0} = f_n D_a^2 + 5f_s \left(\frac{C_s}{(2\pi)^2 \tau} \right)^2 + 5f_{\text{ECS}} D_e^2 \\ M^{(4),2} = f_n D_a^2 p_2 \end{cases}$$

where p_2 is a scalar measure of neurite orientation dispersion¹. A minimum of three q-values with $b(q) \approx 3\text{ms}/\mu\text{m}^2$ are required.

We assume D_e nearly-constant per subject acquisition and estimate it as the mean diffusivity in the subject's ventricles⁶. Combining equations 6 and 7 and adding the $f_n + f_s + f_{\text{ECS}} = 1$ constraint, we obtain a system of 7 equations and 6 unknowns.

Solving the inverse problem via likelihood free inference. We invert our model using a Bayesian approach based on likelihood-free inference (LFI)⁷. Our algorithm produces an approximation of the full posterior distribution $p(\theta | x_0)$ over the parameter space for a given observation x_0 . This can be used to determine which parameter vector $\theta=(D_a, C_s, p_2, f_s, f_n, f_{\text{ECS}})$ is the most likely to have produced x_0 and the corresponding confidence intervals. Moreover, it describes in which regions of the parameter space the model presents indeterminacies. Our LFI procedure follows the setup from⁸ and approximates the posterior distribution using normalizing flows (a special class of deep neural networks) trained over a set of repeated simulations from the forward model.

Results and Discussion

Simulations. We validated the proposed method using LFI on neuron simulations from neuromorpho.org using dmipy⁹. We present on Fig.2 results for $\theta=(1.7, 905, 0.5, 0.5, 0.3, 0.2)$, which corresponds to spheres with a $35\mu\text{m}$ diameter and $2.3\mu\text{m}^2/\text{ms}$ diffusivity. Two acquisition setups have been considered, both with $\delta/\Delta = 12.9/21.8\text{ms}$ and 128 b-shells with uniformly distributed directions. Setup \mathcal{A} corresponds to an "ideal" case with 10 b-values between 0 and $10\text{ms}/\mu\text{m}^2$. Setup \mathcal{B} reproduces the more challenging setup from the HCP MGH dataset¹⁰, with only 5 b-values: 0, 1, 3, 5, and $10\text{ms}/\mu\text{m}^2$. We interpolated an extra point at $0.1\text{ms}/\mu\text{m}^2$ using MAPL¹¹ to improve moment estimation on the Spiked LEMONADE step. On Fig.3, we estimate the soma radius and diffusivity separately. LFI is unable to determine among all possible solutions which one is the ground truth, but using the parameter C_s instead of r_s and D_s enables to avoid model indeterminacy. A low standard deviation is also observed for signals generated in grey matter tissue conditions, where a soma predominance is expected (Fig.4).

Experiments. We applied the proposed method to the HCP MGH Adult Diffusion dataset¹⁰, whose acquisition is similar to setup \mathcal{B} . D_e was estimated as the mean diffusivity in the ventricles. Fig.5 presents the mean estimations across subjects, where overlay colormaps are masked showing only areas where parameters are stable, i.e. when their value was larger than 2 times the LFI-obtained standard deviation of the fitted posterior. Our figure assesses qualitatively the results on soma size by comparing with nissl-stained histological studies^{12,13,14}. This qualitative comparison shows good agreement between different cortical areas and our parameter C_s which, under nearly-constant intra-soma diffusion D_s , is modulated by soma size.

Conclusion

We presented a methodology based on Bayesian inference with modern tools from neural networks to estimate the tissue parameters and their full posterior distribution out of grey matter dMRI signals. This rich description provides many useful tools, such as assessing the quality of the parameter estimation or characterizing regions in the parameter space where it is harder to invert the model. Moreover, our proposal alleviates limitations from current methods by not requiring physiologically unrealistic constraints on the parameters and avoiding indeterminacies when estimating them.

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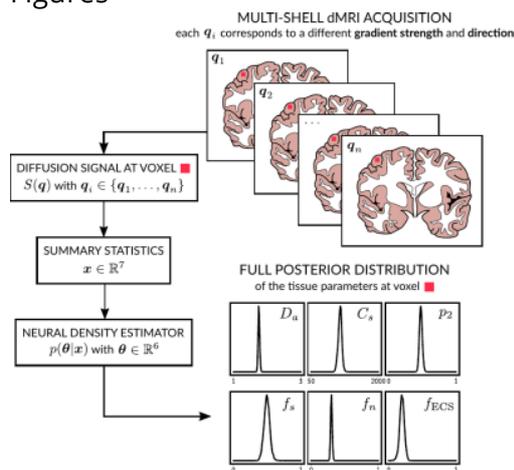
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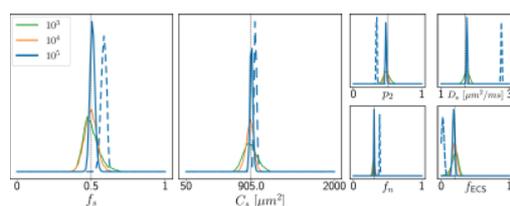
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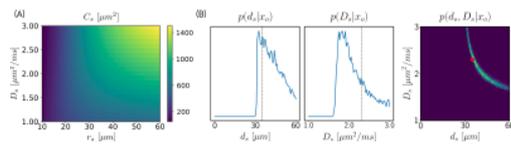
Figures



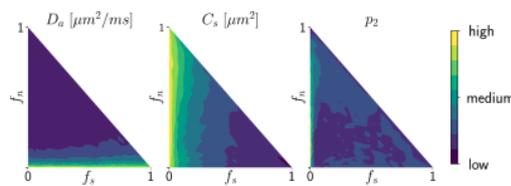
Visual abstract. On the top right we illustrate a multi-shell dMRI acquisition. Based on the proposed 3-compartment model, we then extract summary statistics from it. Applying a neural density estimator we can both estimate the tissue parameters and their full posterior distribution.



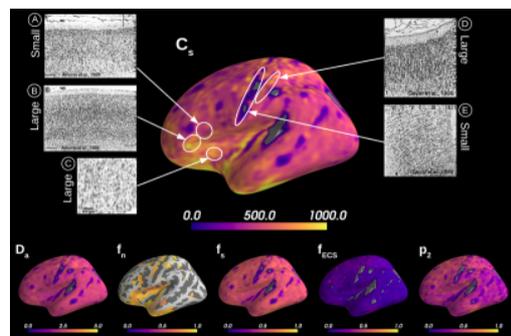
Histograms of 10^4 samples of the approximate posterior distribution with observed dMRI signals generated under two acquisition setups, \mathcal{A} and \mathcal{B} . Vertical black dashed lines represent ground truth values of θ_0 which generated the observed signals. Different colors show how the posterior distribution gets sharper as the number N of simulations in the training dataset increases. Solid curves indicate results for setup \mathcal{A} , which are very close to the true values, and dashed curves for setup \mathcal{B} , which present a bias.



(A) C_s dependence on soma radius r_s and diffusivity D_s . We see that there are several values of (r_s, D_s) that yield the same C_s . (B) Histograms of 10^4 samples from the marginal and joint posterior distributions of $d_s = 2r_s$ and D_s . The ridge in the joint distribution indicates that there are several possible values for the pair (d_s, D_s) with high probability, which are those yielding the same C_s . Estimating C_s directly bypasses this indeterminacy.



Logarithm of the standard deviations for the marginal posterior distribution of D_a , C_s , and p_2 with different choices of ground truth parameters (varying f_s and f_n). We see that when the signal fraction of somas decreases ($f_s \rightarrow 0$) the standard deviation of the C_s estimation increases; and when less neurites are present ($f_n \rightarrow 0$) the standard deviation of p_2 and D_a increases. A low standard deviation is also observed for signals generated in grey matter tissue conditions, where a soma predominance is expected.



Microstructural measurements averaged over 31 HCP MGH subjects. We deemed stable measurements with a z-score larger than 2, where the standard deviation on the posterior estimates was estimated through our LFI fitting approach. In comparing with Nissl-stained cytoarchitectural studies we can qualitatively evaluate our parameter C_s : Broadmann area 44 (A) has smaller soma size in average than area 45 (B)¹³; large von Economo neurons predominate the superior anterior insula (C)¹²; precentral gyrus (E) shows very small somas while post-central (D) larger ones¹⁴.