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## Competitive effects in bacterial mRNA decay

Thibault A. Etienne<sup>a,b</sup>, Muriel Cocaign-Bousquet<sup>a</sup>, Delphine Ropers<sup>b,\*</sup>

<sup>a</sup> TBI, Université de Toulouse, CNRS, INRA, INSA, Toulouse, France <sup>b</sup> Univ. Grenoble Alpes, Inria, 38000 Grenoble, France

#### Abstract

In living organisms, the same enzyme catalyses the degradation of thousands of different mRNAs, but the possible influence of competing substrates has been largely ignored so far. We develop a simple mechanistic model of the coupled degradation of all cell mRNAs using the total quasi-steady-state approximation of the Michaelis-Menten framework. Numerical simulations of the model using carefully chosen parameters and analyses of rate sensitivity coefficients show how substrate competition alters mRNA decay. The model predictions reproduce and explain a number of experimental observations on mRNA decay following transcription arrest, such as delays before the onset of degradation, the occurrence of variable degradation profiles with increased non linearities and the negative correlation between mRNA halflife and concentration. The competition acts at different levels, through the initial concentration of cell mRNAs and by modifying the enzyme affinity for its targets. The consequence is a global slow down of mRNA decay due to enzyme titration and the amplification of its apparent affinity. Competition happens to stabilize weakly affine mRNAs and to destabilize the most affine ones. We believe that this mechanistic model is an interesting alternative to the exponential models commonly used for the determination of mRNA half-lives. It allows analysing regulatory mechanisms of mRNA degradation and its predictions are directly comparable to experimental data.

#### *Keywords:*

Michaelis-Menten kinetics, Quasi-steady-state assumption, Substrate competition, mRNA turnover, Regulation of gene expression

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<sup>\*</sup>Corresponding author

#### 1 1. Introduction

Intracellular levels of bacterial mRNAs result from a balance between 2 transcription and degradation. It has long been believed that mRNA decay 3 plays a minor role in the regulation of bacterial gene expression, most likely 4 because bacterial transcription has been early shown the target of so many 5 regulations. mRNA degradation has gained renewed attention when studies 6 have evidenced tight modulations of mRNA half-life by environmental con-7 ditions, through the action of small RNAs and RNA-binding proteins (see 8 e.g. Bobrovskyy et al., 2015; Mohanty and Kushner, 2016). Short mRNA 9 half-lives allow both a rapid remodelling of gene expression when cells un-10 dergo environmental perturbations and a recycling of the ribonucleotide pool 11 (Carpousis, 2007). In addition, a complicated multi-protein machinery called 12 degradosome is responsible for both mRNA instability and RNA processing 13 (see Marcaida et al., 2006; Lykke-Andersen et al., 2009, for reviews). 14

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Experimental approaches for analysing mRNA decay are based on tran-16 scriptional arrest by antibiotics addition (e.g. rifampicin). The kinetics of 17 mRNA degradation is monitored by measuring mRNA levels along time. 18 With the advent of high-throughput technologies, this is nowadays achieved 19 at the whole cell level using microarrays or RNA sequencing. Fitting the 20 degradation profiles to an exponential model provides half-life values for cell 21 mRNAs. They typically vary between 3 and 8 minutes in the model bac-22 terium *Escherichia coli*, much shorter than the duration of the cell cycle 23 (Bernstein et al., 2004; Chen et al., 2015; Esquerré et al., 2013). By com-24 parison, ribosomal and transfer RNAs are stable and function over several 25 generations. In some extreme cases in the stationary phase, half-lives as high 26 as 50-100 minutes are measured in E. coli (Dressaire et al., 2018) and up to 27 90 minutes in the budding yeast (Wang et al., 2002). 28

29

These exponential models of mRNA decay fall short of providing mech-30 anistic interpretations to the degradation kinetics. They are based on the 31 assumption that mRNA decay follows a first-order reaction, that is, the reac-32 tion rate depends linearly on the mRNA concentration (Bernstein et al., 2002; 33 Chen et al., 2015). They do not explicitly include regulations of mRNA de-34 cay, as this would require complexifying both the model and the procedure of 35 parameter estimation. Notably, one largely ignored regulatory mechanism is 36 the possible implication of substrate competition, while experimental studies 37

point at its possible involvement (Esquerré et al., 2015; Nouaille et al., 2017).
 <sup>39</sup>

Substrate competition is encountered in many biochemical processes, 40 from signal transduction to gene expression or transport in living organ-41 isms (e.g., Cookson et al., 2011; De Vos et al., 2011; Kiel and Serrano, 2012). 42 It occurs when several substrates compete for binding to the same active site 43 of an enzyme, which possibly leads to complex dynamical behaviours. For 44 instance, the substrates of the MAP kinases (MAPK), which regulate vari-45 ous cell fate decisions (proliferation, differentiation, and apoptosis), compete 46 for binding to MAPK in early *Drosophila* embryos (Kim et al., 2010, 2011; 47 Legewie et al., 2007). Their local concentration and their relative binding 48 affinities for the MAPK is predicted to control both MAPK activity and the 40 choice of substrate. This enables the same MAPK pathway to operate in 50 different modes and elicit distinct cell type responses. 51

52

In the case of mRNA degradation, the same machinery is responsible for 53 the fate of messenger RNAs. In E. coli for instance, the main degradation 54 pathway is the internal cleavage of mRNAs by RNase E, an enzyme also in-55 volved in RNA processing (Clarke et al., 2014). In the alternative, so-called 56 5'-end-dependent, pathway, mRNA cleavage by RNase E occurs after the 57 prior recognition and removal of two of the three phosphate groups at the 5' 58 end of the transcript by the pyrophosphohydrolase RppH. The fragments of 59 mRNAs are then rapidly degraded by exoribonucleases. RNase E is abun-60 dant in E. coli cells (Mackie, 2013; Valgepea et al., 2013), at least in excess 61 with respect to individual substrates, but the total substrate concentration 62 largely exceeds that of the enzyme. As a consequence, pools of RNAse E are 63 limited in cells. It is thus expected that differences of substrate affinities and 64 concentrations play a determinant role in the degradation kinetics of mR-65 NAs. Experimental observations seem to agree with this hypothesis, at least 66 for mRNA initial concentrations, for which a strong negative correlation was 67 found with the mRNA lifetime (Esquerré et al., 2015; Nouaille et al., 2017). 68 69

In this manuscript, we study the possible role of substrate competition on mRNA degradation kinetics. We need for this a mechanistic modelling of mRNA degradation describing the binding of RNase E to competing substrates and the subsequent titration of the enzyme. The model should make a trade-off between complexity and biological realism, and have physiologically interpretable parameters. In addition model predictions should be directly comparable to experimental data. Common models of mRNA degradation kinetics do not meet this requirement. We thus developed a mechanistic model
of mRNA decay in this study and analysed the effect of mRNA competition
on the degradation kinetics.

In what follows, we briefly survey mRNA degradation (Section 2). We 80 show in Section 3 how to assimilate mRNA degradation by the degrado-81 some to a macro-reaction catalysed by the limiting enzyme RNase E. The 82 kinetics of the reaction is described by means of a Michaelis-Menten equa-83 tion. To take into account the fact that RNase E is in limited concentration 84 with respect to all mRNA concentrations, we used the tQSSA form of the 85 Michaelis-Menten equation for describing the degradation kinetics. By ex-86 tending previous works by Pedersen et al. (2007) and Tang and Riley (2013), 87 we developed an approximated version of the tQSSA form which includes 88 competition between all cell mRNAs. We used this approximation in Sec-80 tion 4 to study the contribution of competition to mRNA decay by means 90 of numerical simulations, based on carefully chosen parameter values and 91 distributions. Our results show that the introduction of competition leads 92 to variability, delays and increased non linearities in the degradation curves, 93 similarly to experimental observations. Such diversity and non linearities are 94 difficult if not impossible to reproduce in the absence of competition. By 95 means of rate response coefficients in Section 5 and 6, we show how competi-96 tion globally affects degradation by slowing it down and how it differentially 97 affects the fate of mRNAs. We discuss these results in Section 7. 98

# <sup>99</sup> 2. A short survey of mRNA degradation: mechanism, monitoring <sup>100</sup> and kinetic modelling

#### 101 2.1. The mechanism of mRNA degradation and its regulation

In many bacteria, RNase E (EC 3.1.26.12) is a central player of mRNA 102 degradation and RNA processing. It initiates the processing of small RNAs 103 and of a majority of pre-tRNAs, participates to the maturation of riboso-104 mal RNAs in addition to degrading mRNAs. The tetrameric enzyme forms 105 a multi-protein complex called the RNA degradosome, together with the 106 RNA helicase B (RhlB), the glycolytic enzyme enolase (Eno), and the phos-107 phorolytic exonuclease polynucleotide phosphorylase (PNPase) (Carpousis, 108 2007). It is mostly anchored to the cytoplasmic inner membrane, where it 100 forms highly mobile foci diffusing all over the membrane (Strahl et al., 2015). 110

These foci disappear upon inhibition of transcription and the subsequent dis-appearance of mRNAs.

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mRNA degradation results from the combined action of endo- and exo-114 ribonucleases (Fig. 1). As an endoribonuclease, RNase E catalyses the first 115 internal cleavage, followed by a rapid degradation of the RNA fragments by 116 exoribonucleases. This initial cleavage is considered to be the limiting step in 117 mRNA degradation (Kushner, 2002). RNase E has also an indirect effect on 118 mRNA decay, through the processing of small regulatory RNAs that regulate 119 the stability of their target mRNAs (Chao et al., 2017). This is for instance 120 the case of CsrB and C, which control the activity of the post-transcriptional 121 regulator CsrA. Their stabilization or destabilization alters the half-life of 122 many CsrA-regulated genes (Suzuki et al., 2006). 123

124

The gene coding RNase E is essential, presumably due to its role in RNA 125 processing. Knocking down RNase E activity in vivo or decreasing its cel-126 lular level result in a slowdown in the turnover of bulk mRNAs (Bernstein 127 et al., 2004; Sousa et al., 2001; Stead et al., 2010). Microarray analyses have 128 shown RNase E to initiate the decay of 60% of E. coli mRNAs (Bernstein 129 et al., 2004; Stead et al., 2010). Recently RNA-seq experiments have mapped 130 thousands of RNase E cleavage sites in both E. coli and Salmonella tran-131 scriptomes (Chao et al., 2017; Clarke et al., 2014). Other endoribonucleases 132 have been identified, such as RNase III and the paralog of RNase E in E. coli, 133 RNase G, but they have a much more limited set of substrates (Carpousis, 134 2007; Kushner, 2002). 135

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RNase E prefers binding to single-stranded RNA regions that are typically 137 A-U rich, with a strong preference for U at position +2 with respect to the 138 scissile phosphate (Chao et al., 2017; Clarke et al., 2014; Huang et al., 1998; 139 McDowall et al., 1994, 1995). Two determinants of substrate recognition 140 are the 5'-monophosphate termini – known to activate degradation through 141 a higher enzyme affinity (Kime et al., 2010; Mackie, 1998) – and the pres-142 ence of a stem-loop upstream of the cleavage site in most mRNAs cleaved by 143 RNase E (Del Campo et al., 2015). The current model proposes two modes of 144 substrate recognition, which do not need to be mutually exclusive (Bandyra 145 et al., 2018). In the 5'-sensing mode, RNase E binds to the 5' monophos-146 phate and the first bases of the 5' termini, causing an appropriate alignment 147 at the active site of the single-stranded region containing the cleavage site. 148



Figure 1: RNA degradation in Prokaryotes. Endoribonucleolytic cleavage by RNase E generates fragments that are further converted to nucleotides by oligoribonucleases. RNase E binds to a A-U rich sequence of the messenger RNA, often downstream of a stem loop. The binding can be strengthened or weakened by regulatory proteins or RNAs.  $k^+$  and  $k^-$  are the rate constants for the association and dissociation of RNase E to the mRNA, respectively.  $k_{cat}$  is the catalytic constant of the degradation reaction.

In this case, degradation by RNase E requires a preliminary processing by RppH of the 5'-triphosphate termini to 5'-monophosphate (Celesnik et al., 2007; Deana et al., 2008; Garrey and Mackie, 2011). In the 5' bypass mode, which seems to be the most frequent one (Clarke et al., 2014; Richards et al., 2012), the direct binding of RNase E to a structured region of the mRNA allows to align the single-strand region at the active site independently of the nature of the 5' end (Bandyra et al., 2018). 156

The binding of RNase E to individual bacterial mRNAs is also regulated 157 by trans-acting factors (Fig. 1) (Richards and Belasco, 2019). The base pair-158 ing of a small RNA with a mRNA can lead for instance to translational 159 activation or repression in response to stresses. The later case is often asso-160 ciated to an increased destabilization of the messenger RNA. In many cases 161 the process involves the protein chaperone Hfq, which facilitates the base 162 pairing between the sRNA and the mRNA (see for review Santiago-Frangos 163 and Woodson, 2018). Ribosomes bound to the ribosome-binding site protect 164 mRNAs from degradation by RNase E (for review, Deana and Belasco, 2005). 165 Changes in the level and activity of RNase E also modulates the degradation 166 rate. An auto-regulation mechanism has been shown sensing the intracellular 167 level of RNase E (Jain and Belasco, 1995a). However, under normal circum-168 stances there appears to be excess RNase E in the cell, because enzyme levels 160 have to be significantly reduced to see any phenotypic effect (Jain and Be-170 lasco, 1995b). The regulatory proteins RraA and RraB were also shown to 171 repress RNase E activity in vivo when over-expressed (Lee et al., 2003), but 172 their physiological role remains to be determined. 173

#### 174 2.2. Monitoring mRNA degradation kinetics

Current experimental methods monitor mRNA decay in Prokaryotes and 175 Eukaryotes through three different approaches: general inhibition of tran-176 scription by drugs (e.g. rifampycin) or mutation, transcriptional control 177 by regulatable promoters and pulse-chase labelling (Lugowski et al., 2018). 178 Transcription is inhibited in the two first cases, either that of all cellular 179 genes or of a single gene, following which the mRNA level starts to decay. 180 Pulse-chase labelling relies on the cell incorporation of labelled nucleotides 181 into newly synthesized RNAs. The addition of natural nucleotides wash out 182 the labelled nucleotides. mRNA decay is then monitored by following the 183 decline of labelled mRNAs. 184

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Transcription inhibition is often used in Prokaryotes (see Bernstein et al., 2002; Esquerré et al., 2014; Dressaire et al., 2018; Hundt et al., 2007, for a few examples), coupled nowadays to high throughput technologies for the quantification over time of residual mRNA concentrations. Large scale data obtained with micro-arrays are by far the most abundant in the literature (for review Laguerre et al., 2018). At the time of transcription inhibition and

in the following minutes, the culture is sampled, mRNAs are extracted, pu-192 rified, and used as matrix for the synthesis of complementary cDNAs. The 193 latter are then quantified by hybridization to DNA chips. As an illustra-194 tion, mRNA degradation profiles obtained in *E. coli* with this approach are 195 shown in Appendix A.1. Alternatively, qRT-PCR approaches allow obtain-196 ing medium scale data through the amplification of selected cDNAs. RNA 197 sequencing approaches starts also being used (Chen et al., 2015; Laguerre 198 et al., 2018; Moffitt et al., 2016; Potts et al., 2017). They consist in the 199 depletion of ribosomal RNAs and the retro-transcription of mRNAs into cD-200 NAs, before the latter are sequenced. 201

202

Depending on the method chosen for the quantification of residual mR-203 NAs, different types of data normalization can be applied (Laguerre et al., 204 2018). The objective is to compensate for technical variations between sam-205 ples at different time points. The mRNA levels can be further multiplied 206 by RNA extraction yields to obtain mRNA concentrations in arbitrary units 207 per gram dry weight. Mathematical models are subsequently used to esti-208 mate mRNA half-lives from these normalized data, as we shall see in the 209 following section. Other modelling efforts include mRNA degradation beside 210 other processes, some models being used to analyse regulatory mechanisms 211 of mRNA degradation kinetics. 212

#### 213 2.3. Kinetic modelling of mRNA degradation in literature

Various mathematical models of mRNA degradation kinetics have been proposed in the literature, the most common and simplest one being the exponential model. This mathematical description simplifies the mechanism of mRNA degradation to a first-order reaction modelled by the following linear ordinary differential equation (ODE):

$$\frac{d}{dt}m_i(t) = -k_{deg_i}m_i(t), \quad m_i(0) = m_{i0}$$
(1)

219

where  $m_i(t)$  is the concentration at time t of the messenger RNA of gene i.  $k_{deg}$  is the degradation constant, from which mRNA half-life can be determined:  $t_{1/2} = log(2)/k_{deg}$ . This model is valid once transcription has been stopped at time 0, which means that the transcription rate does no longer counterbalance the degradation rate of mRNAs.

225

This mathematical modelling implies that the degradation kinetics depends linearly on the initial concentration of mRNA i, according to the following analytical solution of the ODE system:

$$m_i(t) = m_{i0} \times e^{(-k_{deg_i} \times t)} \,. \tag{2}$$

229

The exponential model in Eq. 2 is commonly used to estimate mRNA half-life 230 by linear regression on a semilog plot of the concentration levels (for review, La-231 guerre et al 2018). The approach has been used for decades to estimate individual 232 mRNA half-lives. It has been extended more recently to genome-wide data (e.g. 233 Bernstein et al., 2002, 2004; Esquerré et al., 2014; Potts et al., 2017). Other related 234 models are now emerging. They extend the exponential model with a delay before 235 the onset of the decay (Chen et al., 2015; Dar and Sorek, 2018; Moffitt et al., 236 2016) and a residual mRNA concentration at the end of the degradation process 237 (Moffitt et al., 2016). The delay is generally attributed to the time required by 238 RNA polymerase to complete transcription initiated prior to the drug addition. 239 240

First-order models provide valuable information on reaction rates through the 241 determination of mRNA half-lives. However, they fell short of describing the 242 biological mechanisms at work. In the literature, mechanistic models including 243 mRNA degradation are generally broader in scope. With a relative simple de-244 scription of the degradation mechanism, they relate several cellular processes such 245 as the synthesis and degradation of mRNAs and proteins, the DNA replication and 246 the cell growth... (e.g. Tadmor and Tlusty, 2008; Thomas et al., 2018; Weiße et al., 247 2015). In (Thomas et al., 2018) for instance, mRNA degradation is identified as 248 one source of growth heterogeneity at slow grow rates, when ribosomes are in too 249 low numbers to protect mRNA from degradation by endonucleases. This leads to 250 variations in biomass production and division times. Some modelling efforts are 251 more focused on the mechanism of mRNA degradation and its regulation, such as 252 the 5' binding and sliding of endonucleases on mRNAs and the mRNA protection 253 by ribosomes in bacteria (Carrier and Keasling, 1997; Deneke et al., 2013), or else 254 the modes of action of miRNAs on protein translation and mRNA degradation in 255 Eukaryotes (Morozova et al., 2012). For instance, Carrier and Keasling (1997) and 256 Deneke et al. (2013) have developed models of this type using a stochastic frame-257 work. However, the simulation of these models comes with a computational cost. 258 which makes it inappropriate to analyse the coupled degradation of all cell mRNAs. 259 260

Knowing that large scale data are mostly available for mRNA degradation nowadays, these mechanistic modelling studies tell us that a compromise has to be reached in terms of model complexity and biological realism. The ideal model

should i) be realistic from a biological point of view and useful to analyse regu-264 latory mechanisms of mRNA degradation including competition; ii) alleviate the 265 computational cost of numerical simulations; iii) include parameters that can be 266 interpreted from a biological point of view; and iv) predict degradation kinetics 267 that can be directly confronted to experimental data. We develop in the follow-268 ing section a kinetic model of the coupled degradation of all cell mRNAs, which 269 meets these constraints as much as possible. We justify how we simplified the 270 complexity of mRNA degradation to a macro-reaction catalysed by the limiting 271 enzyme RNase E. We modelled this reaction and its regulations with the total 272 quasi-steady-state approximation of the Michaelis-Menten equation. We incor-273 porate substrate competition among the regulatory mechanisms. This required 274 extending earlier modelling works on substrate competition to the case when mul-275 tiple substrates compete for the same enzyme and when individual substrates are 276 in excess of enzyme, but not the total substrate concentration. 277

#### 278 3. Model development

#### 279 3.1. Simplified description of mRNA degradation

As explained in Section 2.3, developing a model that can be confronted to 280 experimental data constrains the level of description and the nature of the mecha-281 nisms to consider. We described in Section 2.2 how high throughput approaches are 282 used to quantify residual mRNA concentrations after transcriptional arrest. These 283 approaches quantify full length mRNAs through a good coverage of mRNA se-284 quences. For instance, qRT-PCR and microarray experiments make use of oligonu-285 cleotides distributed along mRNAs (see Esquerré et al., 2014; Nouaille et al., 2017, 286 for example), and read counts for each gene are determined in RNAseq experi-287 ments. In other words, messenger RNAs that have been cut once or several times 288 by endo- and exo-nucleases are not tractable in these experiments. Especially 289 since the rapidity of degradation by exonucleases makes it unlikely that partially 290 degraded mRNAs could be confused with full length mRNAs. According to Fig. 1, 291 this implies that our model does not need to describe reaction steps posterior to 292 the initial cleavage by the endoribonuclease. In most cases, the endoribonuclease 293 is RNase E and we will refer to that enzyme hereafter, although in some cases 294 other endoribonucleases like RNase G are known to specifically degrade some tar-295 get mRNAs. Our model remains valid for these alternative enzymes as well. 296 297

Experiments monitor the disappearance of full length mRNAs following the binding of RNase E to these mRNAs and their internal cleavage. As summarized in Section 2.1, this is the limiting step in mRNA degradation. The initial cleavage by RNase E is followed by the complete degradation of mRNAs into ribonucleotides,

which implies that the reaction is irreversible and we do not expect end-product inhibition. So essentially, the simplest mechanistic description of mRNA degradation would simplify the reaction steps in Fig. 1 to the binding of free RNase E to a given mRNA i and its subsequent cleavage according to the general biochemical equation:

$$\begin{array}{l} \text{RNase } \mathbf{E} + \mathbf{mRNA_i} \underset{k_i^-}{\overset{k_i^+}{\leftarrow}} \text{RNase } \mathbf{E} : \mathbf{mRNA_i} \overset{k_{cat}}{\rightarrow} \text{RNase } \mathbf{E} + \varnothing \,. \end{array}$$

298

The rate constants  $k_i^+$  and  $k_i^-$  denote respectively the rate of association or 299 dissociation of  $mRNA_i$  with the enzyme. Sequence and structure specificities may 300 affect the rate at which RNase E binds to or unbinds from mRNAs.  $k_{cat}$  is the 301 catalytic constant of the reaction. The nature of the 5' extremity of some mRNAs 302 is known to affect this constant when the 5' sensing mode is the mechanism of sub-303 strate recognition. In this case, RNase E can bind to mRNAs with 5' triphosphate 304 termini but do not cleave them due to steric hindrance (Mackie, 1998; Callaghan 305 et al., 2005). These mRNAs need a pre-processing by RppH to convert the 5<sup>3</sup> 306 triphosphate into a 5' monophosphate termini. The conversion of the 5' end by 307 RppH seems to concern only a small fraction of each transcript (Luciano et al., 308 2017; Richards et al., 2012), but the fact has not been established for all cell mR-309 NAs. Given that the direct entry mechanism is the most frequently used and that 310 it functions independently of the 5' end, we will thus consider for simplicity that 311 the catalytic constant is the same for all mRNAs. According to this view, the 312 recognition of the 5' end is expected to act on the enzyme affinity only, in agree-313 ment with Kime et al. (2010). 314

315

The binding of RNase E to its target mRNA can be modulated, for instance 316 by small RNAs, regulatory factors such as the proteins Hfq and CsrA, trans-317 lating ribosomes or else, as we shall see later, by competition between mRNAs. 318 In the following section, we will show how to model the biochemical equation 319 and its regulation. This equation is reminiscent of enzymatic reactions driven 320 by Michaelis-Menten kinetics. However, we will see that the classical Michaelis-321 Menten expression based on the standard quasi-steady-state approximation does 322 not always hold for this particular system along the degradation kinetics and for 323 all mRNAs. 324

#### 325 3.2. Kinetic modelling using quasi-steady-state approximations

Measurements of residual mRNA concentrations are performed experimentally on populations of sampled cells. We will thus use a deterministic modelling framework to describe the degradation kinetics. The model will predict averaged intracellular mRNA concentrations over the population of cells that can be related
 directly to experimental data.

In biochemistry, Michaelis-Menten-Henri kinetics is classically used to model enzymatic reactions (for review, Cornish-Bowden, 2013). The expression is derived from mass-action law and additional simplifying hypotheses introduced by Briggs and Haldane (1925), based on a standard quasi-steady-state approximation (sQSSA). It relates the reaction rate to the substrate concentration. This gives the following formula with our system:

$$v_i = -\frac{d}{dt}m_i(t) = \frac{Vm \times m_i(t)}{Km_i + m_i(t)},\tag{3}$$

where  $m_i(t)$  is the total concentration of mRNA *i*, assumed to be equal to the free substrate concentration:  $m_i(t) \simeq m_{i,free}(t)$ .  $Vm = k_{cat} E_0$  is the maximum velocity achieved by the system at saturating concentration of mRNA *i* and  $E_0$  is the total enzyme concentration. The value of the Michaelis constant  $Km_i = (k_{cat} + k_i^-)/k_i^+$  is defined as the substrate concentration at half maximum velocity. Kinetic parameters and concentrations are in standard units: molar units for Km values and intracellular concentrations, and min<sup>-1</sup> for the  $k_{cat}$ .

The sQSSA form of Michaelis-Menten kinetics in Eq. 3 reduces not only the 345 model complexity but also allows relating model predictions with experimental 346 observations. This canonical equation is commonly used in biochemical models, 347 without regard to the validity of the underlying assumptions. Under the sQSSA, 348 however, the substrate concentration must be greater than the enzyme concentra-349 tion and the following relation should hold in our conditions:  $Km_i + m_i^T \gg E_0$ , where  $m_i^T$  is the total concentration of mRNA *i* corresponding to the concen-350 351 trations of the free form of mRNA i, its form complexed to RNase E and the 352 degradation product. This condition is verified in most *in vitro* enzymatic assays, 353 where the enzyme concentration is chosen much lower than the substrate concen-354 tration. 355

356

However, the sQSSA condition can break down in *in vivo* conditions (e.g. Albe 357 et al., 1990; Sols and Marco, 1970). Intra-cellular enzyme concentrations are usu-358 ally higher or at least of the same magnitude as their substrates. Consequently, a 359 significant fraction of substrates can be bound as complexes (Bennett et al., 2009). 360 What happens to mRNA degradation? The difficulty to verify sQSSA validity lies 361 in the fact that  $Km_i$  values are unknown. Available values in the literature were 362 obtained in *in vitro* assays using synthetic RNAs and resulted in variable values 363 whose validity in *in vivo* conditions is questionable (Jeske et al., 2018; Jiang and 364 Belasco, 2004; Kim et al., 2004; Kime et al., 2008, 2010). We expect that Km 365

values in vivo vary between mRNAs due to sequence and structure specificities. 366 Regulations by small RNAs or RNA-binding proteins may affect as well the affinity 367 of the enzyme for its substrates. Quantitative data are available for the concen-368 trations of RNase E and mRNAs though. For example, Valgepea et al. (2013) 369 have quantified these concentrations in E. coli cultures growing at various rates 370 in steady state. It appears that the median mRNA concentration at  $0.48h^{-1}$  (0.5 371 nM) is way smaller than the concentration of the tetrameric form of RNase E (411 372 nM). This enzyme excess with respect to individual mRNAs is no longer observed 373 at the mRNA population level, since the total concentration of mRNAs is much 374 larger (5927 nM). 375

376

An alternative to sQSSA is the total quasi-steady-state approximation (tQSSA) 377 (Borghans et al., 1996; Tzafriri, 2003). It replaces the concentration of free sub-378 strate with its total concentration. Unmistakably, the total substrate cannot be 379 depleted by the formation of a complex with the enzyme. As a consequence of 380 this simple modification, tQSSA is valid for almost any substrate and enzyme con-381 centrations. Its domain of validity is also larger than a third approximation, the 382 reverse quasi-steady state approximation (rQSSA), which assumes that the sub-383 strate concentration is in quasi-steady-state with respect to that of the enzyme-384 substrate complex (Schnell and Maini, 2000; Segel and Slemrod, 1989; Tzafriri and 385 Edelman, 2004). The rQSSA is valid for high enzyme concentrations and would 386 be appropriate to describe the degradation of individual mRNAs but not for a 387 population of mRNAs. For these reasons of larger domain of validity, we will thus 388 use the total QSSA of the Michaelis-Menten equation. Moreover, this in line with 389 the experimental procedure, which most likely quantifies the total pool of mRNAs 390 due to their deproteination following cell lysis. In the next section, we describe 391 the modelling of the degradation of individual mRNAs using total QSSA. We will 392 extend further the model in Section 3.4 with mRNA competition. 393

#### <sup>394</sup> 3.3. Kinetic modelling of the enzymatic degradation of individual mRNAs

We start here with the simplest case of mRNA degradation, where mRNAs are isolated and do not compete for binding to RNase E. This allows us to develop a simple model for the degradation of isolated mRNAs, which we will refer to as 'isolated system' in the rest of the article. We denote  $m_{i,free}(t)$  the free concentration of mRNA *i*.  $c_i(t)$  is the concentration of complex *RNase*  $E: mRNA_i$ . We have the following mass conservation relation for the total concentration of mRNA *i*:

$$m_i(t) = m_{i,free}(t) + c_i(t).$$

$$\tag{4}$$

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Employing the total substrate concentration instead of the free concentration results in the so-called single reaction tQSSA (Borghans et al., 1996; Tzafriri, 2003). This equation is virtually valid for any substrate and enzyme concentrations:

$$\frac{d}{dt}m_{i}(t) = -k_{cat} \times \frac{E_{0} + Km_{i} + m_{i}(t)}{2} - \frac{\sqrt{(E_{0} + Km_{i} + m_{i}(t))^{2} - 4 \times E_{0} \times m_{i}(t)}}{2}, \quad m_{i}(0) = m_{i0}.$$
(5)

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From the somewhat complex expression in (5), Tzafriri (2003) developed an approximation called first order tQSSA. It resembles the sQSSA form of Michaelis-Menten kinetics:

$$\frac{d}{dt}m_i(t) = -\frac{kcat \times E_0 \times m_i(t)}{Km_i + E_0 + m_i(t)} \tag{6}$$

411

The equation (6) is valid if either of the following criteria is satisfied. Let  $K_i$ to be the individual constant of Van Slyke defined by  $K_i = k_{cat}/k_i^+$ :

$$E_0 + Km_i \gg m_{i0}$$
 and  $K_i \ll Km_i$  or: (7)

$$E_0 \gg m_{i0} \quad \text{and} \quad E_0 \gg K m_i \approx K_i$$

$$\tag{8}$$

414

As for the sQSSA form of the Michaelis-Menten, model parameters are ex-415 pressed in the same international standard units. Note that the comparison of 416 model predictions generated by these models with experimental data may require 417 preliminary conversions or normalizations. Indeed, some experimental protocols 418 used for mRNA quantification generate data in arbitrary units. For instance, mi-419 croarrays quantifying residual mRNAs generate concentrations in arbitrary units 420 per gram dry weight (see Esquerré et al., 2013, for instance), and Ct values for 421 qRT-PCR data (e.g. Nouaille et al., 2017). 422

#### <sup>423</sup> 3.4. Model extension with competition between mRNAs

The tQSSA derived in the previous section is well adapted for the description of the degradation of isolated mRNAs. However, the reality is that cells include a large number of mRNAs that share the same degradation enzyme, not to mention the small RNAs, pre-tRNAs and pre-rRNAs that are also processed by RNase E. Can these multiple substrates titrate the enzyme?

To the best of our knowledge, there is no direct experimental evidence for com-429 petition, through measurements of the intracellular concentration of free or bound 430 RNase E for instance. However, several studies support indirectly this hypothesis. 431 E. coli cells transcribe mRNAs from about 4000 genes, resulting in a much higher 432 intracellular mRNA concentration with respect to the enzyme (Section 3.1). Their 433 capacity to titrate RNase E depends on the enzyme kinetic properties. An efficient 434 enzyme would process the excess of mRNA without being significantly titrated. 435 However, available data for RNase E suggest that the enzyme is far from being 436 a kinetically perfect enzyme (see Table B.1 for details). The rate of turnover of 437 the mRNA-RNase E complex is rather small (11  $min^{-1}$  on average), while the 438 low Km value  $(0.4\mu M)$  indicates a rapid binding of mRNAs to the enzyme. This 439 suggests that the enzyme cannot process the excess of mRNA efficiently and that 440 significant enzyme titration can be expected. A similar regulatory mechanism has 441 been proposed for another ribonuclease with a much smaller set of substrates in 442 E. coli, RNase P. This enzyme is involved in the maturation of the 5' end of eighty 443 tRNA precursors (Yandek et al., 2013). 444

Among the multiple RNase E substrates, those at higher concentration have generally a better chance to bind to the poorly available enzyme and be degraded. This has been experimentally observed by means of reporter genes in *E. coli* (Nouaille et al., 2017). Increasing the concentration of given mRNAs reduced their stability, which is an indirect evidence supporting the existence of competition in RNase E-mediated degradation.

Along these lines, mRNAs would thus compete for binding to the active site of RNase E (Fig. 2), with the consequence that the rate of formation and the concentration of the complex between a mRNA i and RNase E might influence other mRNAs j. We thus extend the model in Section 3.3 to include competition between mRNAs. We will refer to this system as 'competitive' in the rest of the paper.

457

The competition between mRNAs requires to track the free enzyme concentration. This was done in (Pedersen et al., 2007), in which the authors studied the case of two competing substrates. Tang and Riley (2013) extended this work to + mRNA<sub>1</sub>  $\xrightarrow{k_1^+}$  RNase E : mRNA<sub>1</sub>  $\xrightarrow{k_{cat}} \varnothing_1$  + + mRNA<sub>2</sub>  $\xrightarrow{k_2^+}$  RNase E : mRNA<sub>2</sub>  $\xrightarrow{k_{cat}} \varnothing_2$  +

RNase E

RNase E

+ mRNA<sub>3</sub> 
$$\xrightarrow{k_3^+}$$
 RNase E : mRNA<sub>3</sub>  $\xrightarrow{k_{cat}} \varnothing_3$  +  
:  
+ mRNA<sub>n</sub>  $\xrightarrow{k_n^+}$  RNase E : mRNA<sub>n</sub>  $\xrightarrow{k_{cat}} \varnothing_n$  +

Figure 2: mRNA degradation by RNase E in conditions of limiting enzyme concentration.  $\emptyset_i$  denotes the degradation product of mRNA *i*.

complex systems with n substrates, m enzymes and different types of inhibitory mechanisms. The authors also studied the special case of a system with n substrates and one enzyme (Eq. 20 in Tang and Riley (2013)). We applied this derivation to the case of n mRNAs competing for binding to RNase E. Using mass-action law, we wrote the following ODE system, with  $i = 1, \dots, n$  mRNAs (see Appendix C for details):

$$\frac{d}{dt}m_{i}(t) = -k_{cat} \times c_{i}(t), \quad m_{i}(0) = m_{i0}$$

$$\frac{d}{dt}c_{i}(t) = k_{i}^{+} \times \left[ (E_{0} - \sum_{j=1}^{n} c_{j}(t)) \times (m_{i}(t) - c_{i}(t)) - Km_{i} \times c_{i}(t) \right], \quad c_{i}(0) = 0.$$
(9)

467

In their respective works, Pedersen et al. (2007) and Tang and Riley (2013) ap-468 plied approximations to the mass-action law system. They used the quasi-steady-469 state approximation  $\frac{dc_i(t)}{dt} \sim 0$  and either the total two Padé approximation (Ped-470 ersen et al., 2007) or perturbation theory (Tang and Riley, 2013) to eventually 471 obtain similar expressions. The application of the global approximation in (Tang 472 and Riley, 2013) to our system of competition allowed us to obtain a simplified 473 formula, much easier to interpret, which can be related to other Michaelis-Menten 474 expressions (see Appendix C for details): 475

$$\frac{d}{dt}m_i(t) = -\frac{k_{cat} \times E_0 \times m_i(t)}{Km_i \times \left(1 + \sum_{j \neq i} \frac{m_j(t)}{Km_j}\right) + E_0 + m_i(t)}$$
(10)

476

477 with  $j = 1 \cdots n$ .

478

The expression differs from the model of the isolated system in Eq. 6 with the introduction of a competition term  $(1 + \sum_{j \neq i} (m_j(t)/Km_j))$  multiplied to the Km value, similarly to competitive inhibition systems. We will refer to the resulting constant

$$Km_i^{app}(t) = Km_i \times \left(1 + \sum_{j \neq i} \frac{m_j(t)}{Km_j}\right)$$

as "apparent Km" in the rest of the article. The competition term increases the
value of the apparent Km value, indicative of a reduced RNase E affinity for its
target mRNAs in competitive systems compared to isolated systems.

482

Tang and Riley (2013) studied the range of enzyme and substrate concentrations for which their approximation is valid. Pedersen et al. (2007) give also these criteria of validity, as well as the range of Km values for the system with two competing substrates. We could easily extend these criteria to the case of a system with multiple competing substrates. With  $K = \frac{k_{cat}}{\min\{k_{1,i}\}}$ , any of the following conditions imply the validity of the approximation:

$$E_0 \ll Km_i^{app}(0) + m_{i0} \quad \text{and} \quad K \lessapprox Km_i^{app}(0) + m_{i0}$$
$$Km_i \gg \sum_{i=1}^n m_{i0} \quad \text{and} \quad K \ll Km_i^{app}(0)$$
$$Km_i \gg \sum_{i=1}^n m_{i0} \quad \text{and} \quad E_0 \gg K \gtrless Km_i^{app}(0)$$
$$E_0 \gg Km_i^{app}(0) + m_{i0} \quad \text{and} \quad E_0 \gg K$$

489

Using numerical simulations of *in vivo* reactions, Pedersen et al. (2007) showed that their approximation is valid for a large range of parameter values. It fits <sup>492</sup> correctly the original mass-action law model. In (Tang and Riley, 2013), the gen-<sup>493</sup> eralisation of the approximation to multiple substrates and/or enzymes prove to <sup>494</sup> outperform the Michaelis-Menten expression. We will use in what follows this <sup>495</sup> approximated version to investigate competitive effects in mRNA degradation ki-<sup>496</sup> netics.

# 497 4. Numerical simulation of mRNA degradation kinetics in isolated 498 and competitive systems

At this stage, we have developed two alternative models of mRNA degrada-499 tion kinetics in bacteria. Both rely on approximations of tQSSA forms of the 500 Michaelis-Menten expression with extended criteria of validity compared to the 501 classical sQSSA form. One model describes the reaction kinetics in situations 502 where mRNAs are isolated and degraded independently of other mRNAs (Eq. 6). 503 The second model includes the effect of competition between substrates, where 504 the formation of complexes between RNase E and mRNAs possibly affects the 505 formation of other complexes (Eq. 10). Whether this is a true phenomenon in the 506 control of mRNA turnover or not has not been established. Two recent studies 507 suggest that this might be the case, since mRNAs with higher concentrations are 508 destabilized in the bacteria E. coli and Lactococcus lactis (Esquerré et al., 2015; 509 Nouaille et al., 2017). It has been proposed that higher mRNA concentrations 510 increase the probability that RNase E encounters its substrates in these two bac-511 terial strains. 512

513

Although our two models are relatively simple at first glance, the introduction 514 of competition between mRNAs couples the ordinary differential equations. This 515 makes the system behaviour difficult to understand intuitively, in particular when 516 studying degradation of all cell mRNAs. We will rather rely on numerical simula-517 tions for our purpose. This requires setting parameters to reasonable physiological 518 values in order to predict degradation kinetics. Since literature data on the subject 519 are generally scarce, we will use data obtained in the bacterium E. coli for which 520 more knowledge and quantitative information are available. However, the model 521 structure is sufficiently general and the mechanisms considered, well conserved 522 among bacteria, for the model to be valid in other biological backgrounds. 523

#### 524 4.1. Model parameters and initial conditions

<sup>525</sup> Our objective with the models is to generate progress curves comparable to <sup>526</sup> those obtained experimentally. The experimental curves vary a lot, from expo-<sup>527</sup> nential to more linear shapes (see Appendix A.1 as an example). Their fitting by <sup>528</sup> an exponential function allows determining mRNA half-lives ranging from one up to a dozen of minutes. This variability in mRNA stability reflects the diversity of mRNA sequence and structure determinants that modulate the enzyme affinity for its targets. It also results from regulatory mechanisms, such as regulations by small RNAs or mRNA protection by ribosomes to name but a few, which also impact the binding of RNase E to mRNAs. According to our modelling hypotheses described in Section 3.1, this results in an expected large variability of Km values because the  $k_{cat}$  value is held constant between mRNAs.

To account for this variability, we constructed a parameter distribution for 536 Km values based on diverse biological information. First, we chose a log-normal 537 distribution to guarantee positive Km values (Fig. 3):  $Km_i \sim \log \mathcal{N}(\mu_{Km}, \sigma_{Km}^2)$ , 538 where the mean  $\mu_{Km}$  is set to the empirical median value of 13 different Km values 539 estimated from experimental data (Jeske et al., 2018; Jiang and Belasco, 2004; Kim 540 et al., 2004; Kime et al., 2008, 2010) (see also Table B.1 for some values). The 541 dispersion of these data did not reflect the expected variability of Km values in 542 vivo. We thus chose the standard deviation  $\sigma_{Km}$  such that it mirrors the variability 543 of mRNA concentrations measured experimentally:  $\sigma_{Km} = \sigma_{m0}$ , similarly to what 544 is found generally for many enzymes and their substrates (e.g. Bennett et al., 2009). 545 The chosen  $k_{cat}$  and  $Km_i$  values result in a mean catalytic efficiency constant of 546  $6 \cdot 10^5 \text{ s}^{-1} \text{M}^{-1}$ , in the average of values determined experimentally for RNase E 547 (Table B.1). The mRNA concentrations at time 0, together with the RNase E 548 concentration, correspond to transcriptomics and proteomics data in (Valgepea 549 et al., 2013), which we discussed in Section 3.2. The mRNA concentrations form 550 a log-normal distribution illustrated on a logarithmic scale in Panel (a) of Fig. 3. 551 The corresponding distribution for Km values is shown in Panel (b). On the 552 logarithmic scale, the distribution is normal, while it is characterized by a longer 553 tail towards higher Km values on a linear scale. It reflects the proportion of 554 mRNAs potentially affected by specific regulations antagonizing RNase E (less 555 than 10% with the chosen variance). As well, an even smaller fraction of mRNAs 556 have low Km values, reflecting possible regulatory mechanisms activating mRNA 557 decay. This is altogether a reasonable assumption, given the similar fraction of 558 mRNAs shown or predicted to be regulated at the degradation level (Keseler et al., 559 2017; Wright et al., 2014). The distribution of initial mRNA concentrations is also 560 characterized by a longer tail, where few mRNAs have high concentrations. Most 561 of them are present at low intracellular levels. For the catalytic constant, we used 562 the mean value estimated from experimental data obtained with various mRNAs 563 (Jeske et al., 2018). Overall, the distributions and parameter values set verify the 564 criteria of validity for the tQSSA described in Sections 3.3 and 3.4. Remember 565 that in these data, the individual mRNA concentrations are well below the RNase 566 E concentration, while the total mRNA concentration is in large excess (Fig. 3). 567



Figure 3: Log-normal distributions of initial concentrations (a) and Km values (b). The x-axes are on a logarithmic scale. The red and green lines denote the total concentrations of RNase E and mRNA, respectively.

# 4.2. Competition between mRNAs slows down the degradation kinetics and increases the variability of progress curves

With the parameter values and concentrations described above, we simulated 570 the kinetic models of the isolated and competitive systems. The transcriptomics 571 data used for the initial conditions includes information for 4312 mRNAs. We thus 572 ran as many simulations. We took every time a Km value from the log-normal 573 distribution as well as the fixed catalytic constant and enzyme concentration. The 574 same values of parameters and initial conditions were used to simulate the models 575 with and without competition. All simulations were performed with the function 576 ode15s of Matlab (Mathworks). 577

Remember that the simulated models are approximated forms of the tQSSA. 578 valid under the criteria described in Sections 3.3 and 3.4. We could not exclude 579 that some combinations of parameters and initial concentrations may violate these 580 criteria. Beforehand we thus compared the predictions generated by the various 581 tQSSA models to make sure that approximations of poorest quality did not impact 582 significantly the degradation profiles (see Appendix D.1). However, the strong re-583 semblance of the model predictions prompted us to use the approximated versions 584 in the rest of the study. 585

586

Fig. 4 describes the simulation results obtained with the approximated tQSSA models. Predicted mRNA concentrations are shown for the competitive system in Panel (a) and the isolated system in Panel (b) (see Fig. D.2 for a log scale representation of these results). The curves differ by the initial mRNA concentration and



Figure 4: Numerical simulation of mRNA degradation kinetics in isolated and competitive systems. Predicted profiles for the competitive (a) and isolated (b) systems. The profiles are normalized to their respective initial concentrations for the competitive (c) and isolated (d) systems. Predicted free RNase E concentrations for (e) the competitive system  $(E_{free} = E_0 - \sum_{i=1}^{n} c_i(t))$  and (f) the isolated one  $(E_{i,free} = E_0 - c_i(t))$ . 4312 curves are displayed in this case, due to the lack of coupling between mRNAs. The colour bars on the right side represent the normalized gradient of Km values, on a scale from zero (the minimal Km value) to one (maximal value).

the Km value. However, the variability of the mRNA concentrations is such that 591 it hides the effect of differences of RNase E affinity, represented by curves from red 592 (high Km values) to blue (low Km). These differences are more visible in Panels 593 (c) and (d), where the same curves normalized to the initial mRNA concentrations 594 are shown. They differ by their Km value only. A striking difference between the 595 isolated and competitive systems is the rapidity of the decay in the absence of com-596 petition. After two minutes, all mRNAs are at least half degraded in the isolated 597 system (Panel (d)), whereas it takes almost five minutes to the competitive system 598 to reach the same state (Panel (c)). This slower rate of degradation is consistent 599 with measurements of mRNA half-lives in *E. coli* cells (Bernstein et al., 2002; Es-600 querré et al., 2014). For instance in Esquerré et al. (2014), mRNAs have median 601 half-lives ranging from 2.9 to 4.2 minutes in *E. coli* cells at various doubling rates. 602 This general slowdown of mRNA degradation results from the reduced RNase E 603 affinity in a competitive system compared to an isolated one (Section 3.4). This 604 can be easily seen in Fig. E.1, where the distribution at time 0 of the apparent 605 Km values (including the competition term) is shifted to a higher median value 606 compared to the distribution of Km values. 607

608

The competitive effects result in more variable and more non-linear degradation 609 profiles. Hence, the competition affects how degradation is launched. It starts im-610 mediately in isolated systems while it is delayed in competitive ones (Fig. 4(a,b)). 611 This delay is slightly more pronounced with the approximated tQSSA, but still 612 present in the absence of approximation (see Fig. D.1 for comparison). It is there-613 fore a feature of competing mRNAs. The occurrence of delays in mRNA degrada-614 tion kinetics is a known phenomenon. The primary reason is the common use of 615 rifampicin as a drug to block the initiation of transcription (e.g. Chen et al., 2015). 616 Elongating RNA polymerase is insensitive to the drug and pursues transcription. 617 During a transient time, the transcription rate counterbalances the degradation 618 rate. It is thus expected that longer transcripts have longer delays before mRNA 619 levels start decreasing (Chen et al., 2015; Esquerré et al., 2015; Moffitt et al., 2016). 620 Are there other determinants to the delay before degradation? 621

622

In our study we have not modelled the delay explicitly, as least not the time 623 required for the completion of transcription. The predicted delay results from the 624 titration of RNase E by competing mRNAs. As shown in Panel (e), the intracellu-625 lar pool of free RNase E is strongly depleted in the first minutes of the degradation 626 kinetics in the competitive system. While the enzyme level is indeed much higher 627 than those of individual mRNAs, the total mRNA concentration is bigger and the 628 formation of complexes between the enzyme and the mRNAs limits the enzyme 629 availability. This implies that sole mRNAs at high initial concentration or with 630

low Km values are more likely to be degraded by this small enzymatic pool. The
intracellular pool of RNase E raises to higher levels when mRNAs are degraded to
a large extent. At this time of the degradation kinetics, RNase E is in excess and
all mRNAs can be degraded. This is what happens during the whole kinetics for
mRNAs in the isolated system, since the enzyme concentration is never limiting
(Panel (f)). The mRNAs can all bind to RNase E and be degraded soon afterwards.

Another striking difference is the variability of the degradation profiles driven 638 by competing mRNAs (compare Panels (a) and (b) or (c) and (d)). Even though 639 we set the variance of the Km distribution to quite a large value, it is clearly 640 not enough to produce a large diversity of curves in the isolated system. With 641 the same parameters and initial concentrations, the introduction of the compe-642 tition term gives rise to curves with variable shapes. This is especially true for 643 the curves in dark blue in Panel (d), characterized by low Km values. Addition 644 of the competition term spread them out, as can be seen in Panel (c). Cyan to 645 red curves, characterized by a high Km, are not scattered but simply shifted. The 646 corresponding mRNAs seem merely to be stabilized. 647

648

<sup>649</sup> Where do these variability and increased non linearity come from? As can be <sup>650</sup> seen in Panels (a) and (b) for both isolated and competitive systems, many mRNAs <sup>651</sup> have a low initial concentration. Many of them have also higher Km values, as <sup>652</sup> shown in Panels (c) and (d) (lines coloured from cyan to red). In these conditions, <sup>653</sup> the mRNA concentration becomes negligible with respect to the Km and/or the <sup>654</sup> RNase concentration:  $m_{i0} \ll Km_i + E_0$ . Therefore, the kinetics in Eq. 6 can be <sup>655</sup> approximated by the following system for isolated mRNAs:

$$\frac{d}{dt}m_i(t) \approx \frac{k_{cat} \times E_0}{Km_i + E_0} \times m_i(t) \,. \tag{11}$$

<sup>656</sup> For mRNAs in competition, it becomes possible to approximate the degrada-<sup>657</sup> tion kinetics in Eq. 10 by:

$$\frac{d}{dt}m_i(t) \approx \frac{k_{cat} \times E_0}{Km_i \left(1 + \sum_{j \neq i} \frac{m_j(t)}{Km_j}\right) + E_0} \times m_i(t) \,. \tag{12}$$

In both expressions, the degradation rate varies linearly with the mRNA concentration. Note as a side comment that the solution of these ODEs is an exponential function comparable to the classical exponential model used to determine mRNA half-life (see Eq. 2). It is thus appropriate to fit the degradation profiles of these particular mRNAs (higher Km and/or lower initial concentration) with an exponential model. The decrease of enzyme affinity resulting from the increased apparent Km value in the competitive system (Fig. E.1(a)) globally shifts the curves to the right compared to the isolated system (look for instance at the cyan to red curves in Panel (c) versus (d)). All mRNAs with higher Km and/or lower initial concentrations will react in the same manner. While they tend to be stable in the isolated system, competition stabilizes them even more.

669

The situation is different for mRNAs characterized by higher initial concentra-670 tions and/or lower Km values. In these conditions, the approximation in Eqs. 11 671 and 12 does not hold any more. RNase E is closer to saturation at the beginning 672 of the degradation kinetics (see Fig. 4), the substrates start to compete and their 673 degradation rates depend on each other. The degradation rate is no longer linear 674 in the mRNA concentration and the non linearity is amplified by the multiplication 675 of the Km value with the competitive term. We thus expect that these mRNAs re-676 act differently to the competition. This is visible in Fig. E.1(b), where normalized 677 values of the Km and apparent Km for each mRNA are compared. We observe the 678 global rescaling of the apparent Km values at time 0 in the competitive system. 679 However, for a non negligible part of the mRNAs, the trend of the rescaling is 680 different. mRNAs with higher Km values in the isolated system can have lower 681 apparent Km values in the competitive system. It is only later in the kinetics, 682 when mRNAs are degraded in large parts, that the curves for the isolated and 683 competitive systems are more alike. In these conditions, the mRNA concentration 684 becomes negligible. The degradation kinetics become again linear in the mRNA 685 concentration and can be approximated by the simplified expressions in Eqs. 11 686 and 12. 687

688

In summary, competition between mRNAs acts globally on mRNA decay by decreasing RNase E affinity for its substrates and by retarding the onset of degradation. It also acts on each mRNA individually. To better understand how the own characteristics of mRNAs in terms of enzyme affinity and initial concentrations lead to variable responses to competition, we determined rate sensitivity coefficients for the two models, as we shall see in the following section.

# 5. Determination of rate sensitivity coefficients disentangles the effect of substrate concentration and enzyme affinity in compet itive systems

In our models, mRNAs start to decay following the transcription arrest at time zero. The initial velocity of the degradation reaction depends on the saturation

of RNase E. Any change in the initial concentrations of mRNAs and the enzyme 700 affinity is expected to affect the degree of saturation. This is exactly what bac-701 teria experience in nature. They constantly adjust their growth rate to changing 702 environmental conditions. This involves a wide reorganization of gene expression, 703 which includes, among others, changes in mRNA abundance and half-life resulting 704 notably from post-transcriptional regulations (see Bernstein et al., 2004; Esquerré 705 et al., 2014, for instance). The latter affect the enzyme affinity for its substrates in 706 our modelling framework. The consequence is that mRNA stabilities should react 707 differently to these changes according to our simulation results in Section 4.2. 708

The determination of scaled rate sensitivity coefficients allow assessing how 710 changes of initial concentrations and RNase E affinity impact the degradation 711 rates. For each model, we derived such a coefficient for the initial velocity, by 712 determining the scaled change of the initial degradation rate of each mRNA i713 upon a variation of mRNA concentrations at time 0 or of Km value. These coef-714 ficients are the equivalent of the elasticities and control coefficients determined at 715 steady state in Metabolic Control Analysis (Heinrich and Schuster, 1996; Ingalls 716 and Sauro, 2003). Their analytical expressions are shown in Table 1. 717

718

709

We first examined how changing the initial concentration  $(m_{i0})$  or Km value 719  $(Km_i)$  of a messenger RNA i affects the initial velocity  $(v_i)$  of its degradation 720 reaction. The sign of the analytical expressions of the response coefficients in 721 Table 1 shows that the direction of the change is the same in both isolated and 722 competitive systems: increasing the initial concentration destabilizes the mRNA 723  $(R_{m_i}^{v_i} \geq 0)$ , while increasing the Km value (and thus decreasing the enzyme affin-724 ity) stabilizes it  $(R_{Km_i}^{v_i} \leq 0)$ . However, the amplitude of the change may differ 725 between both systems. We quantified it, by evaluating the analytical expressions 726 of the response coefficients for the various pairs of mRNA concentration and Km 727 used for the numerical simulations in Section 4.2. The linear interpolations of the 728 coefficients are reported as contour plots in Fig. 5. We also displayed as points the 729 pairs of concentration and Km value used to generate the degradation profiles in 730 Section 4.2. 731

732

The response coefficients with respect to the change in mRNA concentrations are close to unity for both models (see Panels (a) and (b)). This means that increasing the initial concentration by 10 % results in a similar  $\sim 10\%$  increase in the rate of degradation and conversely, a decrease in the time at which mRNAs are half degraded. The coefficients tend to be even higher for the competitive system. The initial velocity of mRNA degradation is thus essentially determined by the initial messenger concentration and this effect is reinforced in competitive systems. This

Model	Coefficients
Isolated system (Eq. 6)	Effect of changes of $m_{i0}$ and $Km_i$ on $v_i$ : $R_{m_i}^{v_i} = \frac{\partial v_i}{\partial m_{i0}} \frac{m_{i0}}{v_i} = \frac{Km_i + E_0}{Km_i + E_0 + m_{i0}}$ $R_{Km_i}^{v_i} = \frac{\partial v_i}{\partial Km_i} \frac{Km_i}{v_i} = \frac{-Km_i}{Km_i + E_0 + m_{i0}}$
	Effect of changes of $m_{j0}$ and $Km_j$ on $v_i$ : $R_{m_j}^{v_i} = \frac{\partial v_i}{\partial m_{j0}} \frac{m_{j0}}{v_i} = 0$ $R_{Km_i}^{v_i} = \frac{\partial v_i}{\partial Km_i} \frac{Km_j}{v_i} = 0$
Competitive system (Eq. 10)	Effect of changes of $m_{i0}$ and $Km_i$ on $v_i$ : $R_{m_i}^{v_i} = \frac{\partial v_i}{\partial m_{i0}} \frac{m_{i0}}{v_i} = \frac{Km_i \times \left(1 + \sum_{j \neq i} \frac{m_{j0}}{Km_j}\right) + E_0}{Km_i \times \left(1 + \sum_{j \neq i} \frac{m_{j0}}{Km_j}\right) + E_0 + m_{i0}}$ $R_{Km_i}^{v_i} = \frac{\partial v_i}{\partial Km_i} \frac{Km_i}{v_i} = \frac{-Km_i \times \left(1 + \sum_{j \neq i} \frac{m_{j0}}{Km_j}\right)}{Km_i \times \left(1 + \sum_{j \neq i} \frac{m_{j0}}{Km_j}\right) + E_0 + m_{i0}}$
	Effect of changes of $m_{j0}$ and $Km_j$ on $v_i$ : $R_{m_j}^{v_i} = \frac{\partial v_i}{\partial m_{j0}} \frac{m_{j0}}{v_i} = \frac{-m_{j0} \times \frac{Km_i}{Km_j}}{Km_i \times \left(1 + \sum_{j \neq i} \frac{m_{j0}}{Km_j}\right) + E_0 + m_{i0}}$ $R_{Km_j}^{v_i} = \frac{\partial v_i}{\partial Km_j} \frac{Km_j}{v_i} = -R_{m_j}^{v_i}$

Table 1: Scaled rate sensitivity coefficients of the initial velocity  $v_i$  with respect to changes in initial mRNA concentrations and Km values.

agrees well with experimental observations, where mRNA concentration has been 740 found negatively correlated with mRNA half time in E. coli and L. lactis bacteria 741 (Esquerré et al., 2015; Nouaille et al., 2017). To reach this conclusion, the authors 742 of these studies analysed large data sets previously obtained in these bacteria grow-743 ing in environmental conditions leading to changes in mRNA concentrations and 744 half-lives. Increasing specifically the concentrations of four mRNAs by means of 745 inducible promoters elicited again the same negative relationship between mRNA 746 concentration and stability (Nouaille et al., 2017). Similarly to our observations, 747 the correlation is more pronounced at low to middle mRNA concentrations, but 748 less at high mRNA concentration ( $R_{m_i}^{v_i}$  coefficients are a bit smaller). 749

750

We then studied how the isolated and competitive systems react to changes in 751 enzyme affinity. The corresponding response coefficients are shown in Panels (c) 752 and (d) of Fig. 5. For the pairs of initial concentration and Km value used for the 753 numerical simulations in Fig. 4, changing the Km value by 10% leads, on average, 754 to a 3% decrease of the initial velocity in the isolated system  $(R_{Km_i}^{v_i} \sim -0.3)$  and to a 9% decrease in the competitive system  $(R_{Km_i}^{v_i} \sim -0.9)$ . This effect does not 755 756 depend on the initial mRNA concentration. It is stronger at higher Km, but the 757 range of Km values for which the system response is highly negative is much larger 758 in the competitive system than in the isolated one. It encompasses the majority of 759 the pairs of initial concentration and Km value used in the numerical simulations. 760 761

It is interesting to realize that initial concentrations impact the degradation 762 kinetics at two different levels in competitive systems. First of all, as described 763 above, they strongly influence mRNA stability due to the strong, positive response 764 of the degradation rate to changes of concentration. Secondly, they have an an-765 tagonistic effect on the degradation rate in the competitive system, due to the 766 strong negative response to Km changes. This response to Km changes is low in 767 the isolated system, which implies that the enzyme affinity hardly compensates for 768 the effect of the initial concentration  $(R_{Km_i}^{v_i} \sim -0.3 \text{ and } R_{m_i}^{v_i} \sim 1 \text{ on average for}$ 769 the pairs of Km and initial concentration used in the numerical simulations). The 770 degradation kinetics of an isolated system is thus almost exclusively driven by the 771 initial mRNA concentration. Now, in the competitive system, the response coeffi-772 cients are of opposite sign and similar amplitude  $(R_{Km_i}^{v_i} \sim -0.9 \text{ and } R_{m_i}^{v_i} \sim 1 \text{ on}$ 773 average). The combination of these two antagonistic effects explain the non linear-774 ities observed in the predicted degradation curves in Fig. 4(a,c), in particular the 775 occurrence of delayed degradation when mRNAs compete between them. Indeed, 776 as long as the total mRNA concentration is high at the beginning of the kinetics, 777 it augments the apparent Km value to sufficiently high values to compensate for 778 the effect of the initial mRNA concentrations. RNase E is totally saturated and 770

the initial velocity is almost null. It is only when the total mRNA concentration decreases significantly that the weight of the competitive term in Eq. 10 fades away. RNase E is no longer saturated and the competitive system resembles the isolated one, with less sensitivity to changes of enzyme affinity.

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With these analyses, we were able to disentangle the contribution of Km and 785 mRNA concentration to the degradation kinetics in competitive systems. One 786 question remains open though. Since the degradation kinetics of all mRNAs are 787 coupled due to the competition, are they impacted by the cell composition in 788 mRNAs? The competition term in Eq. 10 includes the affinity of cell mRNAs j789 different from the mRNA i of interest, as well as their concentration. Given that 790 there are 4312 different mRNAs in our biological system, the intuition would say 791 that the change of concentration or Km of a single mRNA should not affect the 792 degradation kinetics of another one. But how true is it? We further study this 793 question in the following section. 794

#### <sup>795</sup> 6. Effect of coupling on mRNA degradation kinetics

We analysed a new set of rate sensitivity coefficients to analyse how the changes 796 of concentration or Km value of another mRNA i affect the degradation kinetics of 797 a given mRNA *i*. The analytical expressions for these new coefficients are shown in 798 Table 1. The isolated system is characterized by the absence of coupling between 799 mRNAs. Consequently, the response coefficient to changes of Km value or initial 800 concentration of mRNA j is zero  $(R_{m_j}^{v_i} = R_{Km_j}^{v_i} = 0)$ . In the competitive system, 801 the analytical expression depends on the concentration of the other mRNA j and 802 the relative affinities of mRNAs j and i. The sign of the response coefficients  $R_{m_{s}}^{v_{i}}$ 803 and  $R_{Km_i}^{v_i}$  is opposed to the previous coefficients  $R_{m_i}^{v_i}$  and  $R_{Km_i}^{v_i}$ . It shows that in-804 creasing the initial concentration of mRNA j stabilizes mRNA i  $(R_{m_i}^{v_i} \leq 0)$ , while 805 increasing the Km value of mRNA j (and thus decreasing the enzyme affinity) 806 destabilizes it  $(R_{Km_i}^{v_i} \ge 0)$ . As previously, this is a matter of enzyme titration. If 807 a given mRNA j titrates more RNase E due to a high initial concentration or low 808 Km value, less RNase E will be available for mRNA i, which is stabilized. 809 810

We evaluated the response coefficients by determining how a change of 10% of the initial concentration or Km of each of the 4312 mRNAs j affects the initial velocity of each of the 4311 other mRNAs i and j itself. The results are shown as heatmaps in Fig. F.1. In most cases, the mRNA j marginally affects the other mRNAs (response coefficients close to zero, see the yellow area in Panel (b) for  $R_{m_j}^{v_i}$  and the dark blue area in Panel (c) for  $R_{Km_j}^{v_i}$ ). However, when it does impact the initial velocity, it does so for all mRNAs i (see horizontal lines coloured from



Figure 5: Scaled rate sensitivity coefficients for the initial velocity of mRNA *i* degradation. The points correspond to the pairs of initial concentration and Km used in the numerical simulations in Fig. 4. For each pair, the contour plots display by means of linear interpolation the corresponding response coefficients with respect to (a) the initial concentrations  $(R_{m_i}^{v_i})$  or (c) the Km  $(R_{Km_i}^{v_i})$ , in a competitive system or in the isolated system ((b) and (d), respectively). Colour bars indicate the value of the elasticities. Panels (e) and (f) display the median response coefficients to changes of mRNA *j* concentration  $(R_{m_j}^{v_i})$  or Km  $(R_{Km_i}^{v_i})$ , respectively. The x- and y-axes are on a logarithmic scale.

orange to blue in Panel (b) of Fig. F.1, and from yellow to cyan in Panel (c)). 818 To facilitate the analysis of the response coefficients, we thus took the median 819 response coefficients of all mRNAs i to a change of either the Km value or the 820 initial concentration of a given mRNA j (Fig. F.1). They express how changing 821 the characteristics of mRNA i impacts the average mRNA i. The resulting co-822 efficients are shown in Panels (e) and (f) of Fig. 5. Each point (corresponding 823 to a pair of initial concentration and Km value from the numerical simulations in 824 Fig. 4) represents a given mRNA j. The response coefficients are way smaller than 825 their counterparts  $R_{m_i}^{v_i}$  and  $R_{Km_i}^{v_i}$  in Panels (a) and (c), because they only concern 826 the effect of an external mRNA j on the degradation of the average mRNA i. 827 But interestingly, they are not negligible. The competitive effect is the strongest 828 when the mRNA j has a high concentration or a low Km value. Increasing its 829 concentration by 10% in this case reduces by 0.2% the initial velocity of mRNA 830 *i* degradation  $(R_{m_i}^{v_i} \sim -0.02;$  Panel (e)). The effect is exactly the opposite when 831 increasing the Km by 10%. This stimulates the initial degradation rate of the av-832 erage mRNA i by 0.2% ( $R_{Km_i}^{v_i} \sim 0.02$ ; Panel (f)) and reduces the time at which it 833 is half degraded. Hence, a highly competitive mRNA, which titrates more RNase 834 E due to a high initial concentration or a low Km value, can affect the degradation 835 rate of all cell mRNAs, with an average reduction of 0.2% of the velocity. 836 837

The competing effects that mRNAs exert on each other appear limited at first 838 glance. However, these effects do exist whenever a single competing mRNA is 839 considered and could be even stronger if several competing mRNAs are subject to 840 changes. Indeed mRNA abundances and half-lives are known to massively adjust 841 to environmental conditions (see Bernstein et al., 2004; Schneider et al., 1999, for 842 instance). More precisely, modifications of the total mRNA concentration and the 843 relative abundance of individual mRNAs have been observed. Changes in enzyme 844 affinity are also expected for mRNAs specifically regulated by small RNAs and 845 other post-transcriptional regulations. All these combined changes should affect 846 the decay of all cell mRNAs according to our computed response coefficients. The 847 global increase of the total mRNA concentration globally decrease the enzyme 848 affinity, leading to a global but non uniform decrease of the individual degradation 849 rates, since they are sensitive to various degrees to changes of Km values as we 850 have seen in Panel (c). Among these mRNAs, those with the lowest Km values 851  $(Km_i < Km_j)$  and/or the highest initial concentrations  $(m_{i0} > m_j)$  are less 852 sensitive to changes in the competing mRNA pool, because they are saturated by 853 RNase E (Panels (a) and (c)). They behave similarly to mRNAs in an isolated 854 system. However, the vast majority of cell mRNAs has a low concentration (see 855 Fig. 3(a)) and most likely also a relatively weak affinity (Fig. 3(b)), such that they 856 are not saturated by RNase E. Consequently, it is well possible that a majority of 857

cell mRNAs can be significantly affected by changes in competing mRNA pools, in particular if the latter are highly concentrated and/or affine for RNase E (panels (e) and (f)).

#### 861 7. Discussion

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We have developed in this study a mechanistic model of the coupled degrada-863 tion of all cell mRNAs. The model represents a compromise in terms of complexity 864 and biological realism. Its predictions can be compared directly to degradation 865 profiles obtained experimentally. We hence assimilated the degradation mecha-866 nism by the degradosome machinery to a macro-reaction catalysed by RNase E. 867 Literature data motivated the use of the tQSSA form of the Michaelis-Menten 868 equation for describing the degradation kinetics. We further approximated the 869 tQSSA model by extending previous work by Pedersen et al. (2007) and Tang 870 and Riley (2013). The resulting simplified model allows analysing the effect of 871 regulatory mechanisms on mRNA decay, which are difficult to test experimentally. 872 The possible implication of mRNA competition is one of them. While there is no 873 direct experimental proof for significant titration of RNase E, a body of evidences 874 - on its limited concentration relative that of mRNAs and its mean catalytic effi-875 ciency – suggest that competition between mRNAs could well impact the mRNA 876 degradation kinetics (Section 3.4). We analysed the contribution of competition to 877 mRNA decay by means of numerical simulations and rate sensitivity coefficients, 878 based on carefully chosen parameter values and distributions. To the best of our 879 knowledge, this is the first study focusing on the role of competition in mRNA 880 turnover. A similar study was conducted on the maturation of transfer RNAs by 881 RNase P in conditions of limiting substrates (Yandek et al., 2013), but the number 882 of alternative substrates was low compared to our system. In addition the authors 883 of the study opted for the classical sQSSA form of the Michaelis-Menten frame-884 work, which would not be suitable in our case, given its limits of validity. 885 886

Our results provide a plausible explanation to the observed delays and variable 887 degradation profiles in experimental studies. Under the effect of competition, the 888 profiles vary from seemingly exponential to more linear profiles. Such diversity is 889 difficult to reproduce in the absence of competition, while it is observed exper-890 imentally (e.g., see Fig. A.1). The explanation lies in the titration of RNase E 891 at the beginning of the kinetics and as long as the total mRNA concentration re-892 mains sufficiently high, which delays the onset of degradation. During this period 893 of time, mRNAs compete between them. The consequence is that the degradation 894 rate varies along time, from zero during the delay to maximal when free RNase E 895

is available, and back to zero towards the end of the kinetics. Such variation is
visible in experimental data (e.g., see Fig. A.1).

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The lag effect caused by mRNA competition is a striking result. Residual tran-899 scription is generally associated with delayed degradation, in particular for long 900 genes or genes towards the 3' end of operons (Chen et al., 2015). Could mRNA 901 competition be an additional mechanism? In the absence of direct evidence of 902 this phenomenon, through measurements of the free or bound concentration of 903 RNase E for instance, we cannot answer formally the question. However, an anal-904 vsis of available dynamical transcriptomics data in E. coli indicates that residual 905 transcription alone does not suffice to explain the duration of the delay before 906 degradation kicks in (see Appendix G for details). We estimated the delay before 907 degradation for 3140 mRNAs of this data set (Esquerré et al., 2014), as well as 908 the time needed to transcribe each of them. In the absence of information on the 900 position of RNA polymerase at the time of rifampicin addition, determining the 910 time needed for transcribing an entire mRNA gives an upper bound to the residual 911 transcription time. Among the 2454 mRNAs that are not immediately degraded 912 after rifampicin addition, 51% of them have a delay before degradation larger than 913 the time needed for transcription. The delay is even twice larger for 21% of them 914 (Fig. G.2). While this quick analysis clearly underestimates the number of mRNAs 915 for which the transcription elongation takes a shorter time than the delay before 916 degradation, it indicates that residual transcription is not the sole determinant 917 for the delay in the data set studied. Competition between mRNAs could well be 918 another one. 919

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The competition explains also the negative correlation observed between mRNA 921 half-life and concentration (Esquerré et al., 2015; Nouaille et al., 2017). Our model 922 has the advantage that it provides a mechanistic interpretation to the correlation, 923 through the coupling of the degradation kinetics of each mRNA. This results from 924 the fact that the competition acts at two different levels. First of all, the degra-925 dation rate and thus the time at which the mRNA is half degraded is extremely 926 sensitive to mRNA concentration (Fig. 5(a)). This explains why the correlation 927 is the highest in the experimental data, in particular for mRNAs with low to in-928 termediate concentrations (Nouaille et al., 2017). At higher mRNA levels, the 929 degradation rate becomes less sensitive to the concentrations while it can be still 930 strongly sensitive to the Km values (Fig. 5(a,b)). This is where the correlation 931 between half-life and concentration is smaller: the mRNA half-lives no longer vary 932 with high mRNA concentrations. 933

934

<sup>935</sup> Our simulation results and the response coefficients show that mRNA compe-

tition amplifies the effect of the Km value in the degradation kinetics. mRNAs 936 that have intermediate to low affinities compete for binding to RNase E. The less 937 affine mRNAs will have less chance to be degraded: the competition term in their 938 apparent Km value in Eq. 10 increases due to the presence of competing mRNAs 939 with higher affinities (the ratio  $\sum_{j \neq i} \frac{m_j(t)}{Km_i}$  takes higher values). This results in a higher apparent Km reflecting a stabilisation of these mRNAs (Fig. E.1(b)). 940 941 Hence, the more stable mRNAs are stabilized by competition. On the contrary, 942 the most affine mRNAs are saturated by RNase E, in both isolated and competi-943 tive systems. They are among the less sensitive to the competition and can bind to 944 the low enzyme levels. The ratio  $\sum_{j \neq i} \frac{m_j(t)}{Km_i}$  in the competition term is among the smallest throughout the population of mRNAs, because the competing mRNAs 945 946 have higher affinities. These mRNAs will have the smallest apparent Km values 947 among the population of mRNAs (Fig. E.1(b)). The consequence is that these 948 unstable mRNAs in the isolated system are destabilized by competing mRNAs in 949 the competitive system. 950

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By affecting differently the mRNAs, the competition brings about a diversity of 952 effects that is responsible for the larger variability of degradation profiles in a com-953 petitive system with respect to an isolated one. Surprisingly, a single mRNA can 954 affect the degradation profiles of the other cell mRNAs, provided it is sufficiently 955 concentrated or affine for RNase E. All these observations are interesting because 956 it implies that cells can efficiently control the stability of their entire population 957 of mRNAs through the sole use of a competitive mechanism and a limiting en-958 zyme concentration. This suggests that mRNA competition allows cells to adjust 959 degradation to transcription. Similar coupling effects are observed in Eukaryotes 960 and Prokaryotes like E. coli. Buffering mechanisms against changes in mRNA sta-961 bility or transcription ensure that intracellular levels of mRNAs are maintained 962 for instance, although the molecular mechanisms have not been fully elucidated 963 (Dori-Bachash et al. 2011, 2012; Esquerré et al. 2014; Sun et al. 2012; Shalem 964 et al. 2011; see Hartenian and Glaunsinger 2019 for review). In our simulation 965 results, the positive coupling between transcription and degradation results from 966 the higher probability that mRNAs with increased concentration will be degraded. 967 However, we also observe a counter-acting effect that negatively correlates tran-968 scription and degradation rates. The increase of mRNA concentration through 969 transcription increases RNase E apparent affinity and slows down degradation, 970 although the amplitude of the effect varies between mRNAs. 971

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The occurrence of non linearities resulting from enzyme titration is a well studied phenomenon in biochemistry. It has been observed in many biological systems, ranging from the MAP kinases to transcription and translation (e.g. Buchler

and Cross, 2009; De Vos et al., 2011; Huang and Ferrell, 1996; Mehra and Hatz-976 imanikatis, 2006). Quite often, this results in ultrasensitive responses. We have 977 not really observed such phenomenon in our simulation study. The response coef-978 ficients that we determined from the pairs of Km value and initial concentrations 979 used for the numerical simulations are generally between -1 and 1. Sole responses 980 above one in absolute value reflect an ultrasensitive behaviour. Values slightly be-981 low -1 were sometimes obtained in specific conditions, when the Km value of more 982 affine mRNAs i was varied. This does not mean than no ultra-sensitivity occurs 983 in mRNA degradation since the amplitude of the response coefficients strongly 984 depends on the chosen parametrization. 985

986

While we were able to retrieve quite precise values for the enzyme concentra-987 tion, the mRNA concentrations and the catalytic constant in the literature, this 988 prove to be more difficult for the Km value. Available data for the enzyme affinity 989 were obtained with a limited number of substrates in (often) in vitro assays. While 990 this gave a possible average affinity of RNase E for its substrates, it did not reflect 991 the variety of cell mRNAs. The latter were expected having different affinities, 992 depending on their structural and sequence determinants, as well as their possi-993 ble regulations by small RNAs and other regulatory proteins. This is the reason 994 why we chose a distribution of Km as large as the distribution of measured initial 995 concentrations to take into account as much as possible these different situations. 996 This said, using different Km distributions would only tune the amplitude of the 997 competition effect. Indeed there will be always an antagonism between the con-998 tributions of initial concentrations and enzyme affinities to the competition effect. 999 Depending on their relative distributions, one may become prevailing. In our sim-1000 ulations, the choice of distributions with similar variances lead to contributions of 1001 initial concentrations and Km of similar strength in many cases. 1002

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Estimating the Km value from experimental data, and possibly also the cat-1004 alytic constant, could help refine our analysis on the role of mRNA competition 1005 in mRNA decay. This is beyond the scope of this study and will be done else-1006 where (T.A. Etienne, L. Girbal, M. Cocaign-Bousquet, D. Ropers, in prepara-1007 tion). Using a total quasi-steady-state approximation rather than the classical 1008 quasi-steady-state approximation is known to improve the estimation of parame-1009 ter values by introducing the enzyme concentration in the equation (Choi et al., 1010 2017). In addition to helping with the identifiability problems related to the use 1011 of Michaelis-Menten kinetics, estimating the parameter values of such competition 1012 model allows to determine the true value of the Km and not an apparent constant 1013 that includes a competition term. 1014

1015

The model developed is sufficiently general to be applied to other organisms 1016 and regulatory mechanisms of mRNA degradation. For instance, the apparent Km 1017 value in our equations may be extended to include regulations by small RNAs or 1018 the competition by stable RNAs, which are also known to be matured by RNase 1019 E. The fact that RNase E is active both in the cytoplasm and bound to the 1020 membrane as part of the degradosome allows to interpret the Km in a different 1021 manner. It also reflects the diffusion of substrates to the membrane and allows 1022 to study the effect of substrate localization in the degradation kinetics (Tang and 1023 Riley, 2013; Tzafriri et al., 2002). Overall, we believe that our mechanistic model 1024 of mRNA degradation and its regulation by competition and other mechanisms is 1025 an interesting alternative to the classically used exponential models. 1026

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#### <sup>1035</sup> Appendix A. Example of observed degradation kinetics

We illustrate the type of degradation profiles obtained experimentally with data obtained for mRNAs in *E. coli* cells growing at 0.4 h<sup>-1</sup> in continuous cultures. We display in Fig. A.1 21 degradation profiles out of the 4254 profiles obtained in (Esquerré et al., 2014).



Figure A.1: Experimental monitoring of mRNA decay in *E. coli* cells growing in continuous culture at  $0.4 \text{ h}^{-1}$ . For readability, only 21 out of the 4254 generated profiles are displayed, both on linear (a) and semi-logarithmic (b) scales. At time 0 of the experiment, rifampicin was added to the culture and residual mRNA concentrations were quantified by DNA micro-arrays. Data were taken from (Esquerré et al., 2013). After delays of various duration, most mRNAs have a degradation kinetics resembling an exponential decay (blue curves), while other mRNAs can be slowly decaying, like the murein lipoprotein mRNA *lpp* (black curve).

#### <sup>1040</sup> Appendix B. Kinetic parameters of RNase E

Table B.1: Catalytic efficiency of RNase E. Kinetic parameters  $\mathbf{k}_{cat}$  and Km were estimated from the same assays.

Ref.	Experimental	Substrates	$\mathbf{k}_{cat} \; (\mathrm{s}^{-1})$	Km (M)	$k_{cat}/Km$
	conditions				$(M^{-1}.s^{-1})$
(1)	pH 7.5, 25°C, recom- binant N-terminal do- main	5' hydroxylated fluoro- genic oligonucleotide	0.015	$3.3 \cdot 10^{-7}$	45455
(1)	pH 7.5, 25°C, recombinant N-terminal domain	5' monophospho- rylated fluorogenic oligonucleotide	0.014	$2.3 \cdot 10^{-7}$	60870
(2)	рН 7.5, 30°С	AAUUU-containing RNA oligonucleotide	0.192	$7.3 \cdot 10^{-7}$	263,014
(2)	рН 7.5, 30°С	CAUUU-containing RNA oligonucleotide	0.150	$4.6 \cdot 10^{-7}$	326,087
(2)	pH 7.5, 30°C	GAUUU-containing RNA oligonucleotide	0.765	$1.2 \cdot 10^{-6}$	616,935
(2)	pH 7.5, 30°C	GUUUU-containing RNA oligonucleotide	0.121	$3.7 \cdot 10^{-7}$	327,027
(2)	pH 7.5, 30°C	UAUUU-containing RNA oligonucleotide	0.209	$8.1 \cdot 10^{-7}$	258,025
(2)	рН 7.5, 30°С	UUUUU-containing RNA oligonucleotide	0.023	$3.2 \cdot 10^{-6}$	71,875
		Mean	$0.186 \ (11.2 \ \mathrm{min}^{-1})$	$5.6 \cdot 10^{-7}$	246,161
		Median	$0.136 \ (8.1 \ \mathrm{min}^{-1})$	$4.1 \cdot 10^{-7}$	260,519
		Standard deviation	0.247	$3.4 \cdot 10^{-7}$	191,168

References: (1) - Jiang and Belasco (2004); (2) -Kim et al. (2004)

#### <sup>1041</sup> Appendix C. Development of the tQSSA model with competition

We first describe below the development of the mass-action law model in Equation 9 and its subsequent approximations into tQSSA and first-order tQSSA models.

1045 With  $i = 1 \cdots, n$ , we can write the following mass-action law system:

$$\frac{dm_i(t)}{dt} = -k_i^+ \times E_{free}(t) \times m_{i,free}(t) + k_i^- \times c_i(t)$$

$$\frac{dE_{i,free}(t)}{dt} = \sum_i^n (-k_i^+ \times E_{free}(t) \times m_{i,free}(t) + (k_i^- + k_{cat}) \times c_i(t))$$

$$\frac{dc_i(t)}{dt} = k_i^+ \times [E_{free}(t) \times m_{i,free}(t)] - (k_i^- + k_{cat}) \times c_i(t) \quad (C.1)$$

$$\frac{dP_i(t)}{dt} = k_{cat} \times c_i(t),$$

with  $i = 1 \cdots , n$  and initial conditions at t = 0:  $m_{i,free}(0), E_{free}(0), c_i(0), P_i(0)$ .

1048 Using the conservation laws

$$\frac{dE_{i,free}(t)}{dt} + \sum_{i}^{n} \frac{dc_{i}(t)}{dt} = 0 \Rightarrow E_{free}(t) + \sum_{i}^{n} c_{i}(t) = E_{0}$$
$$\frac{dm_{i,free}(t)}{dt} + \frac{dc_{i}(t)}{dt} + \frac{dP_{i}(t)}{dt} = 0 \Rightarrow m_{i,free}(t) + c_{i}(t) + [P]_{i}(t) = m_{i,free}(t)$$

1049

we can reduce the previous system:  

$$dm_{i,free}(t) = \sum_{k=1}^{n} c_k(t) \times c_{k}$$

$$\frac{dc_{i}(t)}{dt} = -k_{i}^{+} \times (E_{0} - \sum_{i} c_{i}(t)) \times m_{i,free} + k_{i}^{-} \times c_{i}(t)$$
(C.2)  
$$\frac{dc_{i}(t)}{dt} = k_{i}^{+} \times (E_{0} - \sum_{i}^{n} c_{i}(t)) \times m_{i,free}(t)) - (k_{i}^{-} + k_{cat}) \times c_{i}(t))$$

We apply the total quasi-steady-state approximation  $m_i(t) = m_{i,free}(t) + c_i(t)$ and obtain:

$$\frac{dm_i(t)}{dt} = \frac{dm_{i,free}(t)}{dt} + \frac{dc_i(t)}{dt} = k_{cat} \times c_i(t)$$
(C.3)
$$\frac{dc_i(t)}{dt} = k_i^+ \times \left[ (E_0 - \sum_i^n c_i(t)) \times (m_i(t) - c_i(t)) - Km_i \times c_i(t) \right],$$

with  $Km_i$  the Michaelis constant:

$$Km_i = \frac{k_{cat} + k_i^-}{k_i^+} \tag{C.4}$$

1052

We apply the quasi-steady-state assumption :  $\frac{dc_i(t)}{dt} \sim 0$  and obtain:

$$(E_0 - \sum_{i}^{n} c_i(t)) \times (m_i(t) - c_i(t)) = Km_i \times c_i(t)$$
(C.5)

and

$$c_i(t) = \frac{(E_0 - \sum_i^n c_i(t)) \times (m_i(t) - c_i(t))}{Km_i}$$
(C.6)

Two alternative methods have been proposed in the literature to solve the non-linear system (C.6) for  $c_i$ . Tang and Riley (2013, 2017) use perturbation theory applied to sQSSA to derive an approximated solution for the tQSSA system. Pedersen et al. (2007) develop their approximation for a competing system with two substrates by means of the total two Padé approximation. Applied to our system, these approaches allow obtaining the following formulation for the approximated concentration of complex  $c_i$ :

$$\frac{d}{dt}c_i(t) = \frac{E_0 \times m_i(t)}{Km_i \times \left(1 + \sum_{j \neq i} \frac{m_j(t)}{Km_j}\right) + E_0 + m_i(t)}$$
(C.7)

1060 with  $j = 1 \cdots, n$ .

#### 1061 Appendix D. Numerical simulations

#### <sup>1062</sup> Appendix D.1. Numerical simulations will full system

To exclude the fact that poor combinations of mRNA concentrations and Km values may violate the validity of the tQSSA approximation described in Section 3.4, we simulated the full system in Eqs. 5 and 9 and compared the simulation results with the profiles obtained with the approximated tQSSA in Fig. 4. Simulation results are shown in Fig. D.1.



Figure D.1: Numerical simulation of mRNA degradation kinetics in isolated and competitive systems using Eqs. 5 and 9. Predicted profiles for the competitive (a) and isolated (b) systems. The profiles are normalized to their respective initial concentrations for the competitive (c) and isolated (d) systems. Predicted free RNase E concentrations for (e) the competitive system and (f) the isolated one. 4312 curves are displayed in this case, due to the lack of coupling between mRNAs. The colour bars on the right side represent the normalized gradient of Km values, on a scale from zero (the minimal Km value) to one (maximal value). Note that the total concentration of RNase E, but not the free concentration, is a variable in Eqs. 5 and 9. We thus calculated a posteriori the concentration of free RNase E from the total RNase E and complex concentrations. Since the model at time zero is not at steady state, we could not determine a steady-state value for the initial complex concentration, which would have given a more realistic value for the initial concentration of free RNase E. Instead, we used the same initial condition for the complex concentration as in the work of (Pedersen et al., 2007), with ci(0) = 0. This effect is transitory only, since the free RNase E concentration predicted with Eq. 9 becomes quickly similar to that obtained with the approximated tQSSA model in Fig. 4(a).



Figure D.2: Semi-logarithmic representation of simulation results shown in Figs. 4(a,b) (Panels (a) and (b)) and D.1(a,b) (Panels (c) and (d)). The predicted profiles for the competitive (a) and isolated (b) systems were obtained with the approximated tQSSA models (Eqs. 9 and 5, respectively). The predicted profiles obtained with the original models (Eqs. 10 and 6) are shown in Panels (c) and (d) respectively.



Figure E.1: Changes in enzyme affinity upon competition. (a) Log-normal distributions of Km (red) and apparent Km (blue) values. The x-axes are on a logarithmic scale. The red and green lines denote the total concentrations of RNase E and mRNA, respectively. (b) Parallel coordinate plot of  $Km_i$  (red) and  $Km_i^{app}$  values (blue) normalized to the Km value. Axes are on a logarithmic scale.

<sup>1068</sup> Appendix D.2. Log-scale representation of simulation results

#### <sup>1069</sup> Appendix E. Changes of enzyme affinity upon competition

Competition rescale the enzyme affinity through the multiplication of the Km
value with a term of competition. The amplitude of the changes is illustrated in
Fig. E.1.

#### <sup>1073</sup> Appendix F. Heatmaps of rate sensitivity coefficients

In this section, we assess the effect of changing the initial concentration or Km value of a competing mRNA j on the initial velocity of the degradation of a given mRNA i. To that aim, we determine rate sensitivity coefficients for the effect of each of the 4312 mRNAs j on the degradation kinetics of each of the 4312 mRNAs i (they include the mRNA j itself). We obtain a square matrix of 4312×4312 coefficients, represented as heatmap in Fig. F.1.

#### <sup>1080</sup> Appendix G. Contribution of transcription elongation to the delay <sup>1081</sup> before degradation

Elongation of transcription is known to delay degradation, but to which extent? 1082 We used a set of dynamic transcriptomics data from Esquerré et al. (2014) to 1083 answer the question. In this study, mRNA half-lives were determined in continuous 1084 cultures of *E. coli* cells growing at four different rates. We chose one condition 1085  $(0.4 h^{-1})$  and spline fitted the logarithm of the 4254 degradation profiles using 1086 the smooth.spline function of the R package stat. Further analysis was possible 1087 only for 3868 mRNAs, for which the spline fit was satisfactory and information 1088 on the gene length and promoter localization was available. For each of these 1089 3868 profiles, we determined the delay before degradation by simply finding the 1090 time point at which the sign of the first derivative of the spline function changes, 1091 from positive or null to negative due to the decrease of mRNA concentration. We 1092 observed the same phenomena as Chen et al. (2015) in their study: the size of 1093 mRNAs and their position towards the end of an operon increases the duration of 1094 the delay. This is illustrated in Figure G.1 in the case of the operon nuo. Genes 1095 at the beginning of the operon *nuo* have shorter delays before start of degradation 1096 than genes near the 3' end (Panel (b)). The same trend is observed when plotting 1097 the distance from the 5' end of the operon to the 3' end of each gene (Panel 1098 (c)). However, this is not a general rule. For instance, we noticed that many 1099 monocistronic mRNAs of low to medium size have also a delay. 1100

We then assessed the contribution of residual transcription to the total duration of the delay before degradation. In principle, this would require to know the



Figure F.1: Scaled rate sensitivity coefficients for the initial velocity of mRNA i degradation. (a) Schematic drawing of the coupling between the degradation of mRNA i and the other cell mRNAs j. We determined, for each of the 4312 E. coli mRNAs i, the effect of a 10% change in (b) the initial concentration and (c) the Km value of mRNA j on the initial degradation rate of each of the 4312 mRNAs i. Colour bars indicate the value of the response coefficients.



Figure G.1: The distance from the 5' end of the operon *nuo* scales proportionally to the duration of the delay before start of RNA degradation. (a) Organization of the *nuo* operon. Numbers indicate genome position in base. (b) RNA concentration over time of exponential phase MG1655 cells growing at  $0.4 h^{-1}$  on a semilogarithmic scale. Vertical lines indicate the duration of the delay. (c) Delay before degradation increases with the distance of the gene transcript to the 5' end of the operon.

position of RNA polymerase when rifampicin inhibits the holoenzyme. Such data 1103 is not available, which makes it impossible to determine the residual transcription 1104 time precisely. However, we can set an upper limit to this time, by determining the 1105 time needed to transcribe entire mRNAs. If this transcription time is smaller than 1106 the delay before degradation, this means than residual transcription cannot be the 1107 sole determinant of the delay. Results are more difficult to interpret when the 1108 maximal transcription time is larger than the delay before degradation. They can 1109 reflect co-transcriptional degradation as in (Chen et al., 2015) for instance, but also 1110 include false negative: mRNAs with low residual transcription time, but total gene 1111 transcription time larger than the delay, should be counted as mRNAs for which 1112 residual transcription is not the sole determinant of the delay. To determine the 1113 time needed for transcription, we multiplied the elongation rate of transcription 1114 determined at the genome scale by Chen and co-authors (25 nts/s on average), 1115 with the length of each mRNA. When a gene is located within an operon, we used 1116 the promoter operon to determine a maximal size for that mRNA. We focused on 1117 the 2454 out of 3868 mRNAs with a delay before the onset of degradation (the 1118 remaining 1414 are immediately degraded). As shown in Fig. G.2, 1255 out of 1119 2454 mRNAs have a delay before degradation larger than the maximal theoretical 1120 time needed for transcription (points in blue). 512 of them have a delay before 1121 degradation twice as large as the transcription time. Overall these results show 1122 that, for a vast majority of genes, transcription alone does not explain the whole 1123 duration of the delay with the transcription rate considered. This does not prove 1124 the role of competition experimentally, but does not exclude that this phenomenon 1125 could play a role in the retardation of degradation. Note we cannot rule out that 1126 heterogeneity in the polymerisation rate in transcription or in degradation may 1127 affect the estimated transcription times and delays before degradation. However, 1128 our analysis is based on population data for which information on heterogeneity 1129 is not available. 1130



Figure G.2: Role of residual transcription in the retardation of degradation. On log scales and for each mRNA with a non negligible delay, the duration of transcription is plotted versus the delay before degradation. mRNAs with a delay higher than the time needed for transcription are displayed in blue and red, otherwise.

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