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# Indetermination-free cytoarchitecture measurements in brain gray matter via an inverse diffusion MRI signal separation method

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## 1 Introduction

### 3 compartment model

7 parameters to estimate:

- Compartment signal fractions:  $f_n$ ,  $f_s$  and  $f_{ecs}$
- Diffusivities:  $D_a$  and  $D_{ecs}$
- An exiting new parameter modulated by soma radius:  $C_s(r_s, D_s)$
- ODF anisotropy invariant:  $p_2$

$$\frac{S(q)}{S(0)} = f_n S_{neurites}(q) + f_s S_{soma}(q) + f_{ecs} S_{ecs}(q)$$

Hypothesis:

- No exchange between the 3 compartments<sup>3</sup>
- $f_t + f_s + f_{ecs} = 1$

### Intra-cellular space

Neurites	Soma
0-radius tubes <sup>1</sup>	Spheres with fixed radius <sup>2</sup>

$$S_{neurites}(q) = \frac{1}{4\sqrt{\pi}D_a} q^{-1} \quad -\log S_{soma}(q) = C_s(r_s, D_s) q^2$$

### Extra-cellular space

Ellipsoid	
$-\log S_{ecs}(q) = (2\pi q)^2 \tau D_e$	

## 2 Methods

① Estimate  $D_{ecs}$  from CSF (free diffusing fluid)

② Spiked LEMONADE

- Low b-value approximation ( $b \leq 3 \text{ ms } \mu\text{m}^{-2}$ )
- Based on cumulant decomposition of the dMRI signal<sup>4</sup>

$$\begin{cases} M^{(2),0} = f_n D_a + 3 \frac{f_s C_s}{(2\pi)^2 \tau} + 3 f_{ecs} D_e \\ M^{(2),2} = f_n D_a p_2 \\ M^{(4),0} = f_n D_a^2 + 5 f_s \left(\frac{C_s}{(2\pi)^2 \tau}\right)^2 + 5 f_{ecs} D_e^2 \\ M^{(4),2} = f_n D_a^2 p_2 \end{cases}$$

③ RTOP:<sup>5</sup>  $RTOP(q_{max}) = \frac{1}{(2\pi)^3} \int_0^{q_{max}} S(q) dq$

- High b-value approximation ( $b \geq 3 \text{ ms } \mu\text{m}^{-2}$ )
- Least square regression

$$RTOP(q_{max}) = a_{fit} + b_{fit} q_{max}^2$$

$$\begin{cases} a_{fit} = \frac{f_s \sqrt{\pi}}{(2\pi)^3 4 C_s^{3/2}} + \frac{f_{ecs}}{32 \pi^{5/2} (2\pi \sqrt{D_e} \tau)^3} \\ b_{fit} = \frac{f_n}{4(2\pi)^4} \sqrt{\frac{\pi}{D_a \tau}} \end{cases}$$

④ Solve the non-indetermination system of 7 equations and 6 unknowns using LBFGS

## 3 Results



Fig. 1. (a)  $C_s$  is modulated by the sphere diameter. (b) RTOP of the soma signal depends on the sphere diameter. (c) Relative error of  $C_s$  estimation. The bigger the soma, the lower b-values for a better relative error.

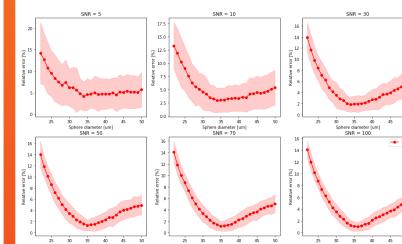
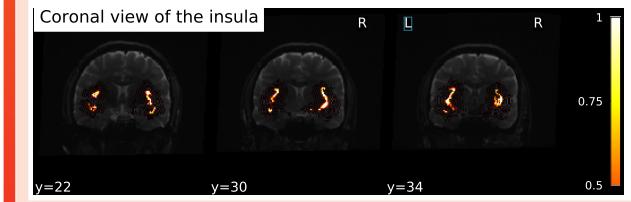


Fig. 2. Evolution of the relative error of  $C_s$  with respect to soma radius for varying SNR. Estimation is better for big soma and is robust towards noise.

Fig. 3.  $C_s$  in the insula. An increasing soma size change can be observed from inferior to superior, agreeing with literature<sup>6</sup>.

Coronal view of the insula



### HCP MGH database

$$\begin{aligned} 6/\Delta &= 12.9 / 21.8 \text{ ms} \\ b &= 0, 1, 3, 5, 10 \text{ ms } \mu\text{m}^{-2} \end{aligned}$$

## 4 Discussion and Conclusion

- $C_s$ : an exiting new parameter modulated by soma radius
- Low requirements: only 5 b-values needed, comprising 3 b-values superior or equal to  $3 \text{ ms } \mu\text{m}^{-2}$
- Unicity of the solution, unlike NODDI or SANDI<sup>3</sup>, making fitted parameters reliably interpretable
- Robust to noise
- No training on simulations required as in SANDI<sup>3</sup>

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