



Indetermination-free cytoarchitecture measurements in brain gray matter via an inverse diffusion MRI signal separation method

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Objective:

- Quantify grey matter cytoarchitecture using diffusion MRI
- Estimate tissue parameters with no indetermination: a unique solution is returned and there is no need to choose between several mathematical and biological possible solutions.

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1 Introduction

3 compartment model

- 7 parameters to estimate:
- Compartment signal fractions: f_n, f_s and f_{ecs}
 - Diffusivities: D_a and D_{ecs}
 - An exiting **new parameter modulated by soma radius**: $C_s(r_s, D_s)$
 - ODF anisotropy invariant: p_2

$$\frac{S(q)}{S(0)} = f_n S_{neurites}(q) + f_s S_{soma}(q) + f_{ecs} S_{ecs}(q)$$

Hypothesis:

- No exchange between the 3 compartments³
- $f_t + f_s + f_{ecs} = 1$

Intra-cellular space

Neurites	Soma
0-radius tubes ¹	Spheres with fixed radius ²
$S_{neurites}(q) = \frac{1}{4\sqrt{\pi}\tau D_a} q^{-1}$	$-\log S_{soma}(q) = C_s(r_s, D_s) q^2$

Extra-cellular space

Ellipsoid
$-\log S_{ecs}(q) = (2\pi q)^2 \tau D_e$

2 Methods

① Estimate D_{ecs} from CSF (free diffusing fluid)

② Spiked LEMONADE

- Low b-value approximation ($b \leq 3 \text{ ms } \mu\text{m}^{-2}$)
- Based on cumulant decomposition of the dMRI signal⁴

$$\begin{cases} M^{(2),0} = f_n D_a + 3 \frac{f_s C_s}{(2\pi)^2 \tau} + 3 f_{ecs} D_e \\ M^{(2),2} = f_n D_a p_2 \\ M^{(4),0} = f_n D_a^2 + 5 f_s \left(\frac{C_s}{(2\pi)^2 \tau} \right)^2 + 5 f_{ecs} D_e^2 \\ M^{(4),2} = f_n D_a^2 p_2 \end{cases}$$

③ RTOP: ⁵ $RTOP(q_{max}) = \frac{1}{(2\pi)^3} \int_0^{q_{max}} S(q) dq$

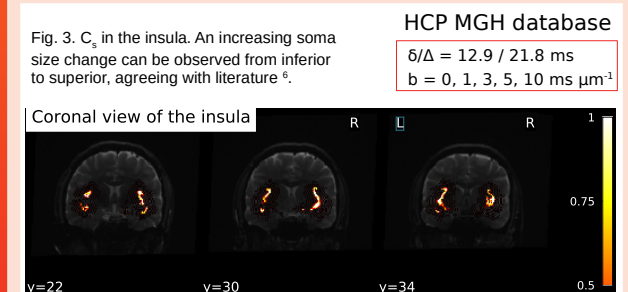
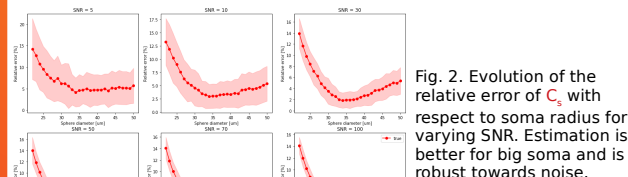
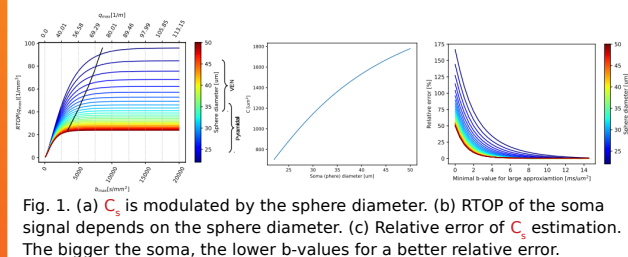
- High b-value approximation ($b \geq 3 \text{ ms } \mu\text{m}^{-2}$)
- Least square regression

$$RTOP(q_{max}) = a_{fit} + b_{fit} q_{max}^2$$

$$\begin{cases} a_{fit} = \frac{f_s \sqrt{\pi}}{(2\pi)^3 4 C_s^{3/2}} + \frac{f_{ecs}}{32 \pi^{5/2} (2\pi \sqrt{D_e} \tau)^3} \\ b_{fit} = \frac{f_n}{4 (2\pi)^4 \sqrt{\frac{\pi}{D_a} \tau}} \end{cases}$$

④ Solve the non-indetermination system of 7 equations and 6 unknowns using LBFGS

3 Results



4 Discussion and Conclusion

- C_s : an exiting new parameter modulated by soma radius
- Low requirements: only 5 b-values needed, comprising 3 b-values superior or equal to $3 \text{ ms } \mu\text{m}^{-2}$
- Unicity of the solution, unlike NODDI or SANDI³, making fitted parameters reliably interpretable
- Robust to noise
- No training on simulations required as in SANDI³

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