

Bruno Cessac, Selma Souihel

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### In collaboration with:

Matteo Di Volo Alain Destexhe

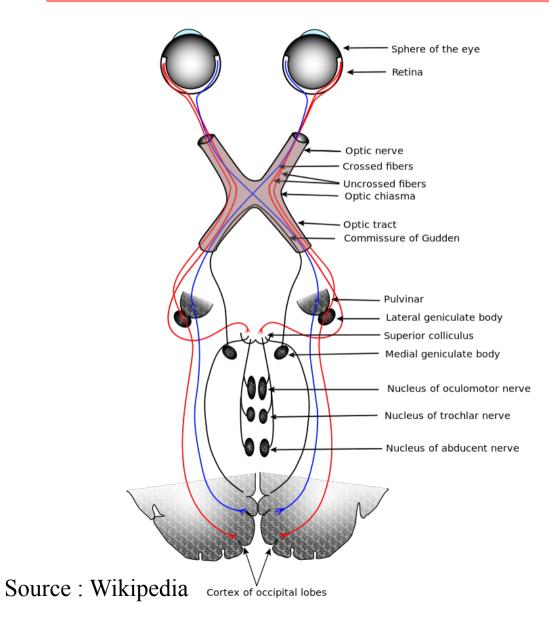


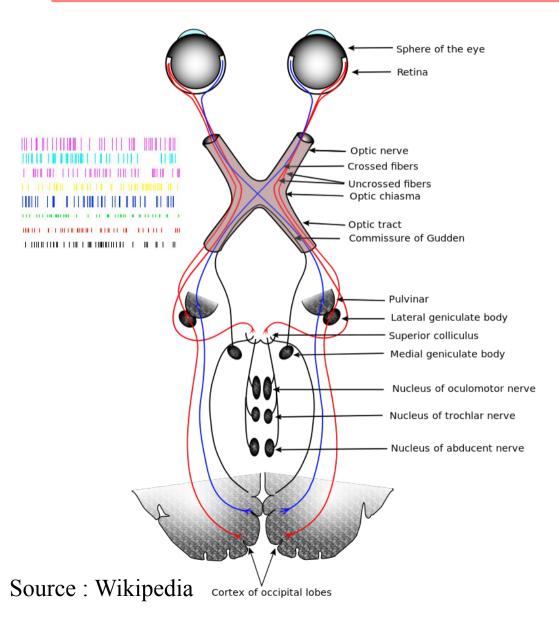
Frédéric Chavane Sandrine Chemla

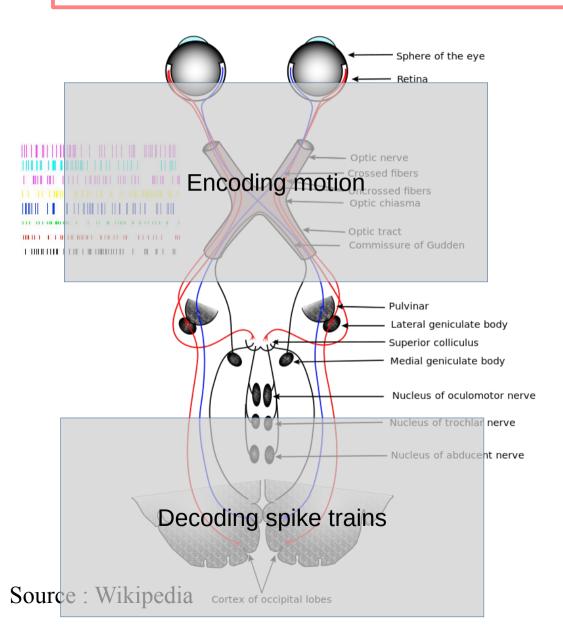


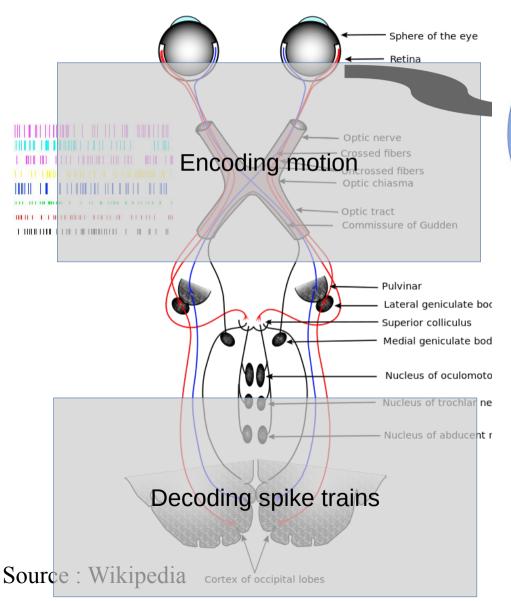
Olivier Marre

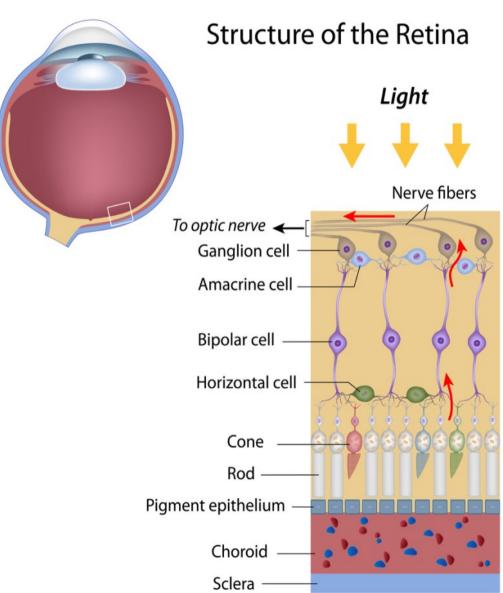


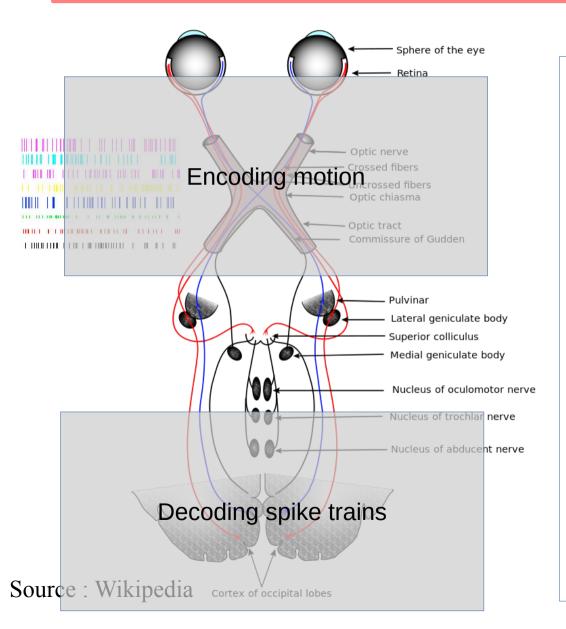




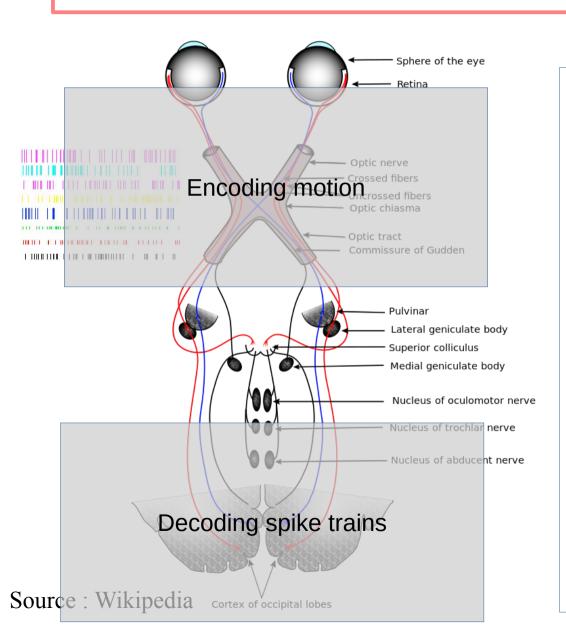




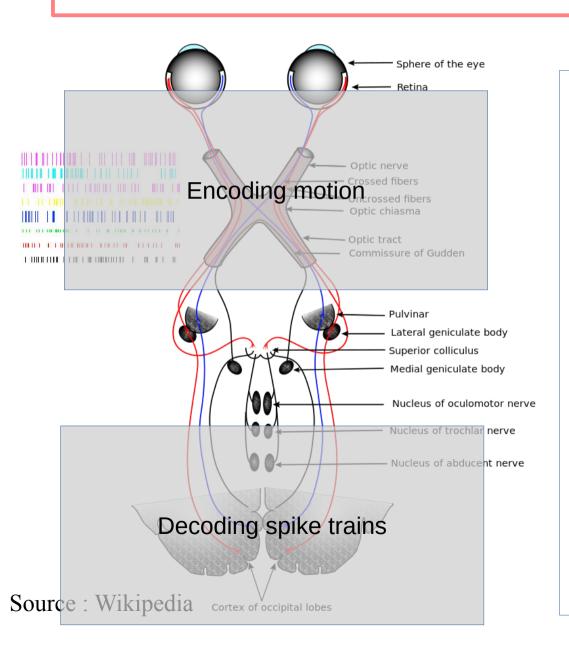




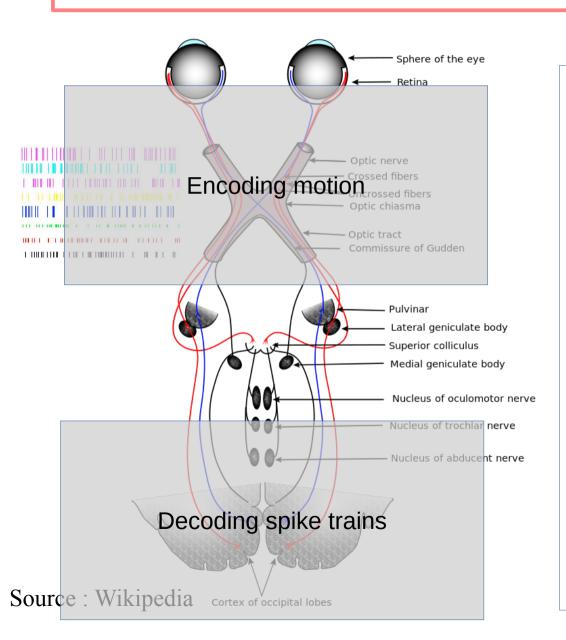
 High transduction rate: 1 photon can trigger a membrane voltage variation of ~1 mV



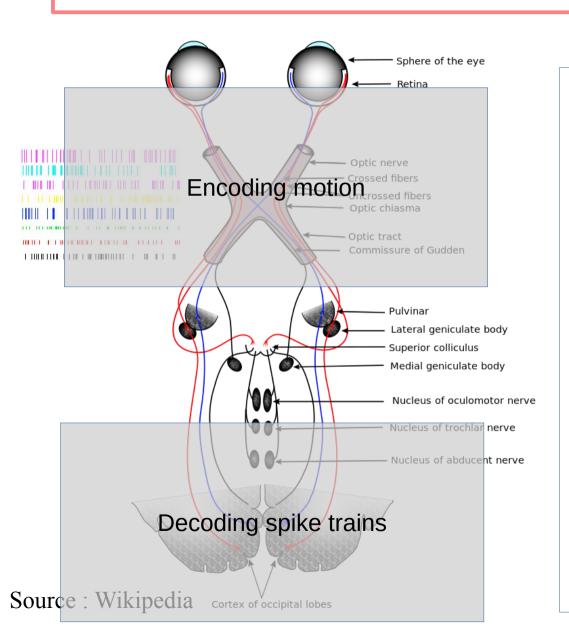
- High transduction rate: 1 photon can trigger a membrane voltage variation of ~1 mV
- · Able to detect approaching motion



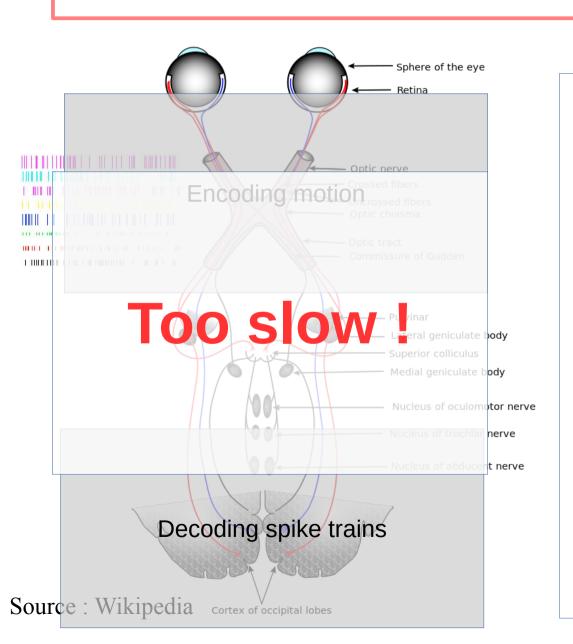
- High transduction rate: 1 photon can trigger a membrane voltage variation of ~1 mV
- Able to detect approaching motion
- · Able to detect differential motion



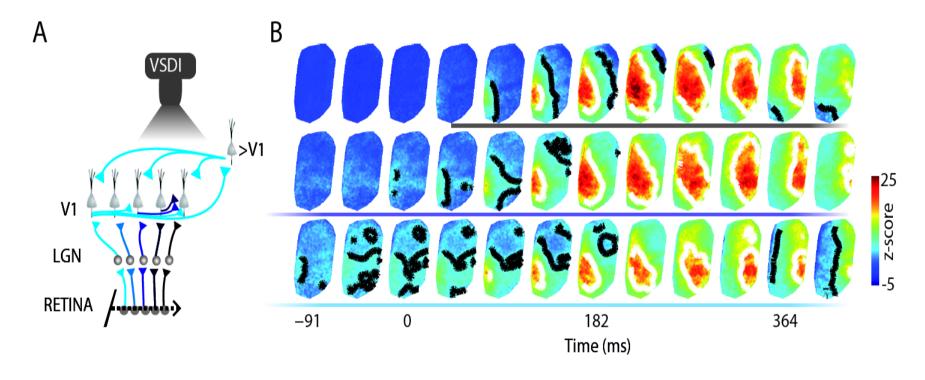
- High transduction rate : 1 photon can trigger a membrane voltage variation of ~1 mV
- · Able to detect approaching motion
- · Able to detect differential motion
- Sensitive to « surprise » in a visual scene



- High transduction rate: 1 photon can trigger a membrane voltage variation of ~1 mV
- Able to detect approaching motion
- · Able to detect differential motion
- Sensitive to « surprise » in a visual scene
- Able to perform motion anticipation

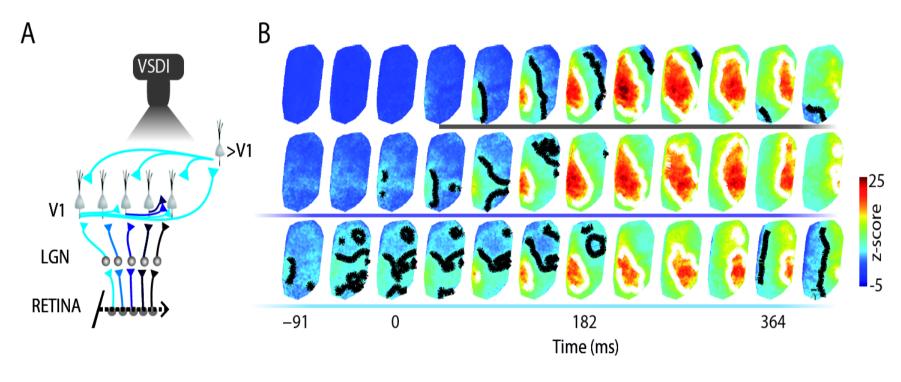


- High transduction rate: 1 photon can trigger a membrane voltage variation of ~1 mV
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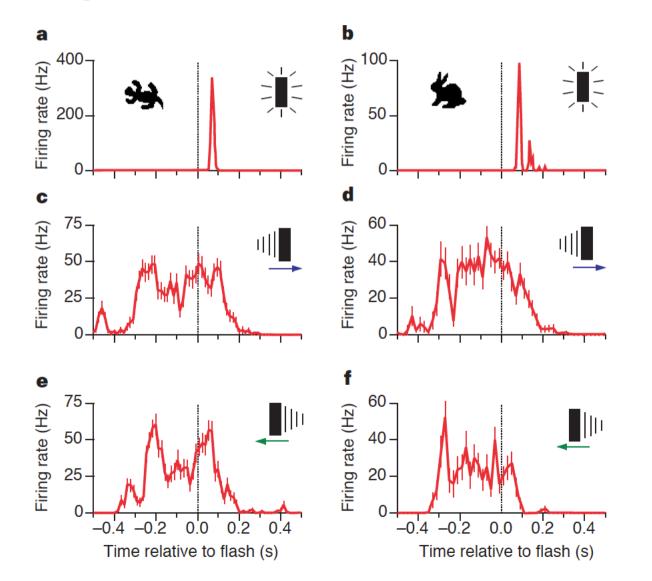
Source: Benvenutti et al. 2015

Anticipation is carried out by the primary visual cortex (V1) through an activation wave



Source: Benvenutti et al. 2015

### Anticipation also takes place in the retina

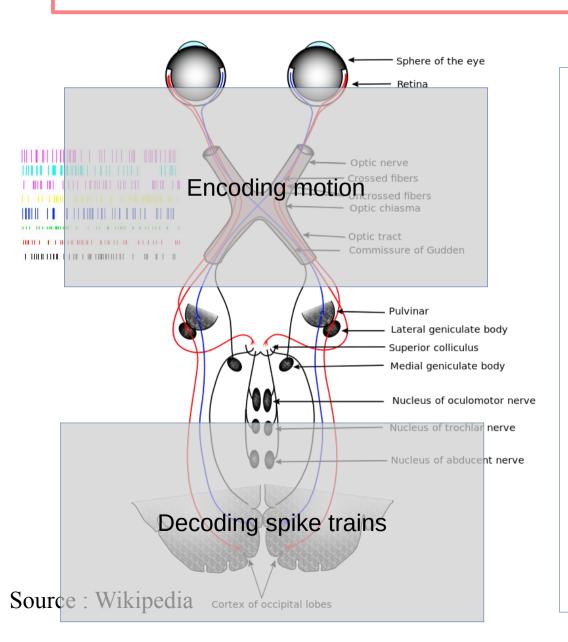


Source: Berry et al. 1999



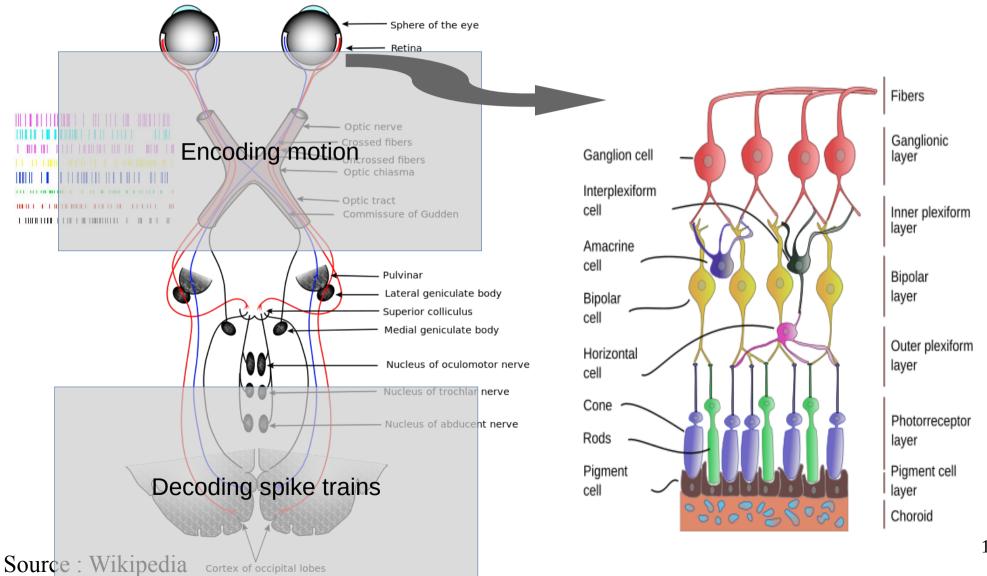
# Trajectory

What are the respective mechanisms underlying retinal and cortical anticipation?

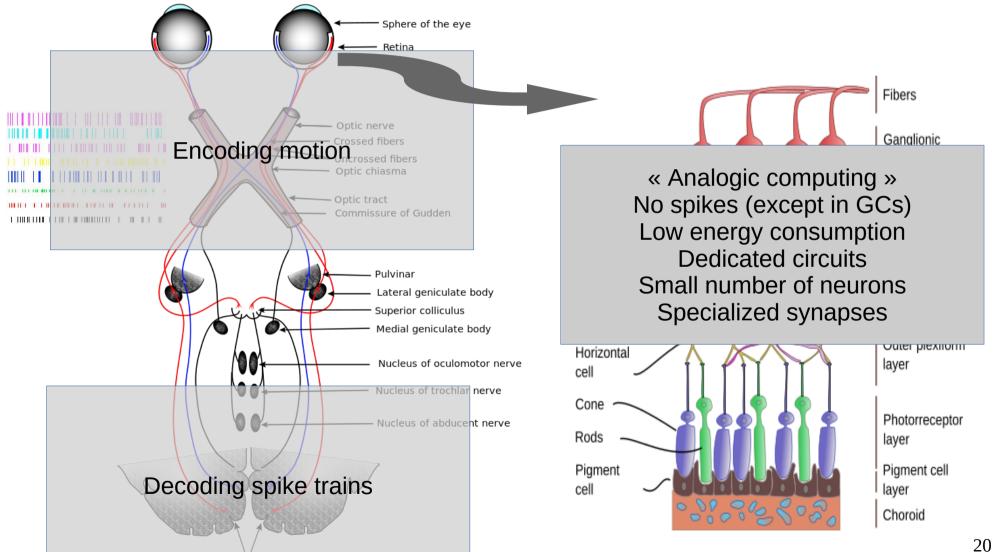


### The retina is NOT a camera

- High transduction rate: 1 photon can trigger a membrane voltage variation of ~1 mV
- Able to detect approaching motion
- · Able to detect differential motion
- Sensitive to « surprise » in a visual scene
- · Able to perform motion anticipation

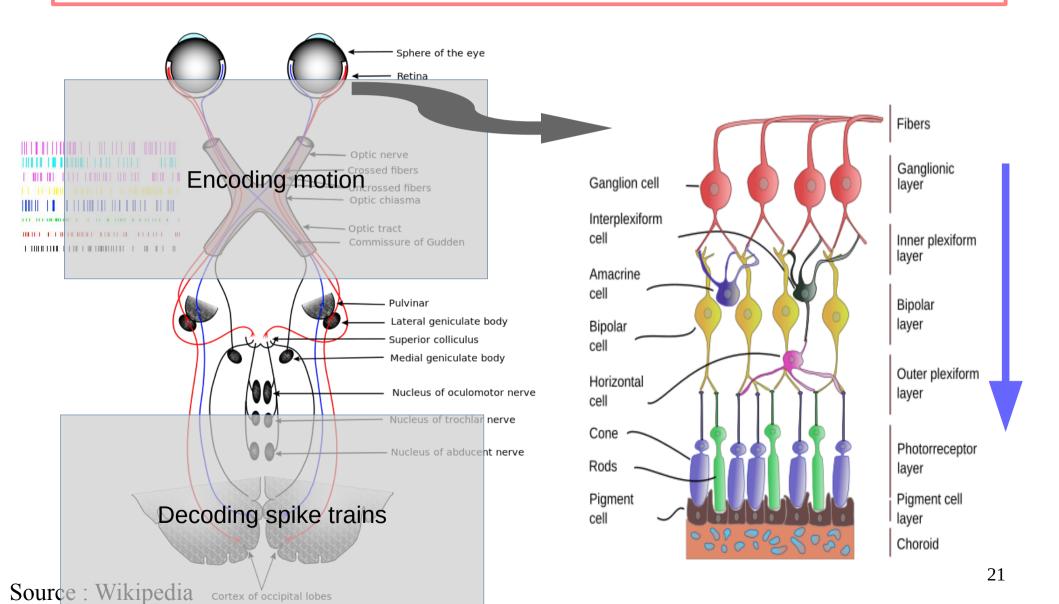


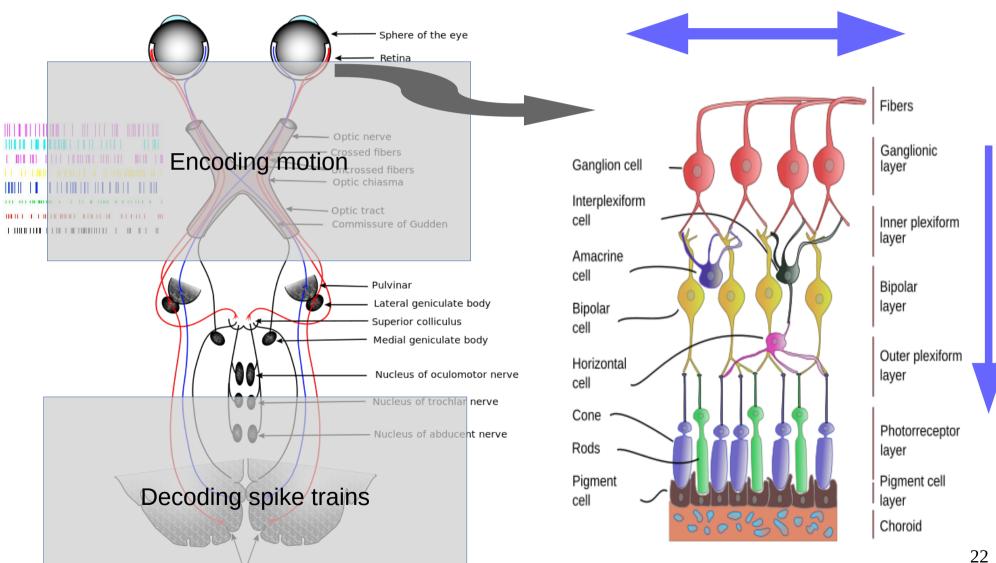
Cortex of occipital lobes



Source: Wikipedia

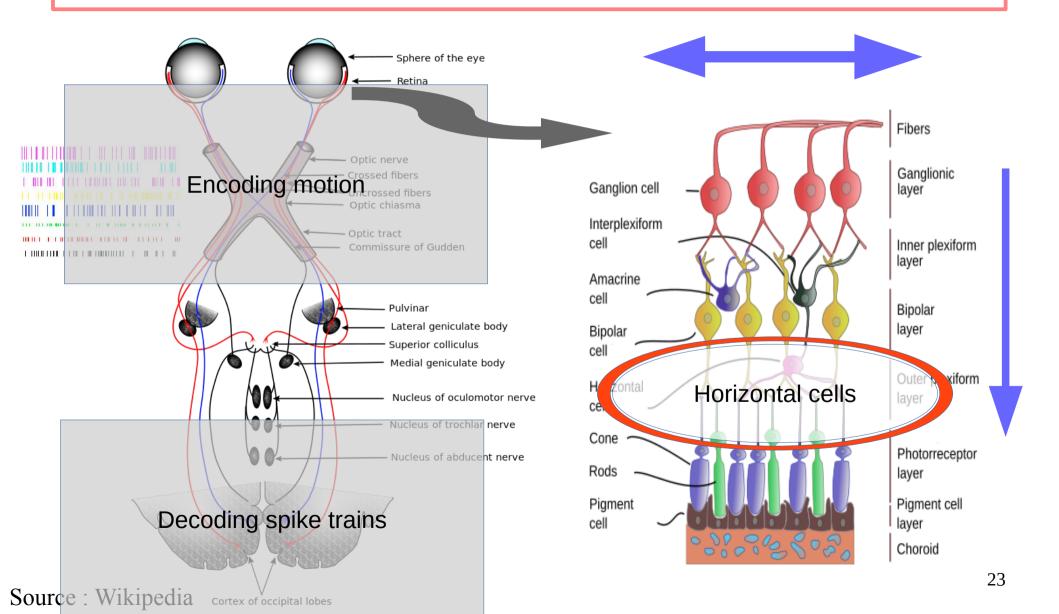
Cortex of occipital lobes

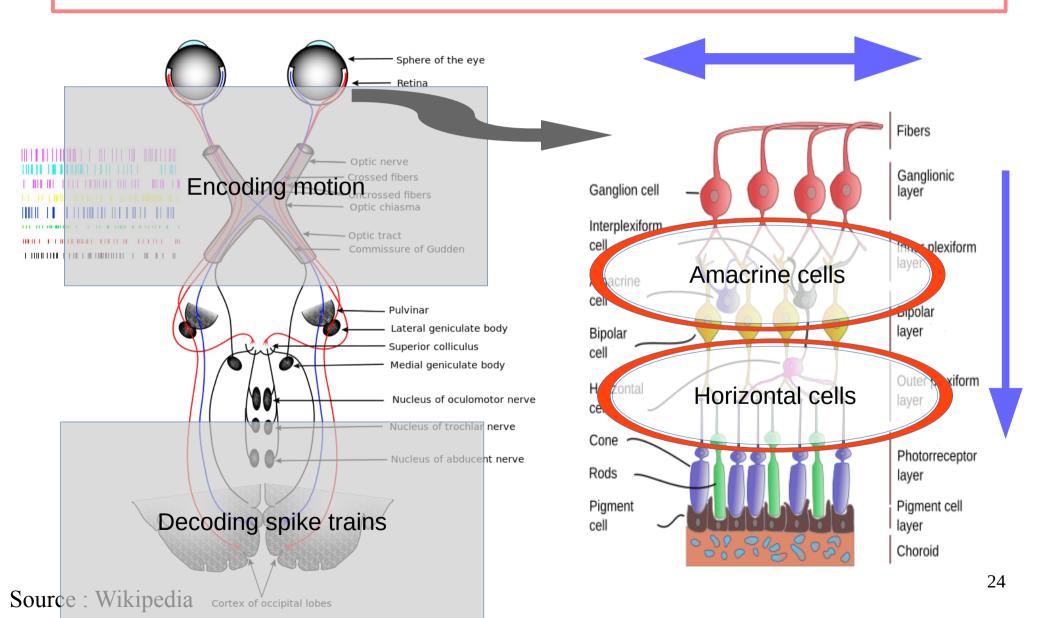


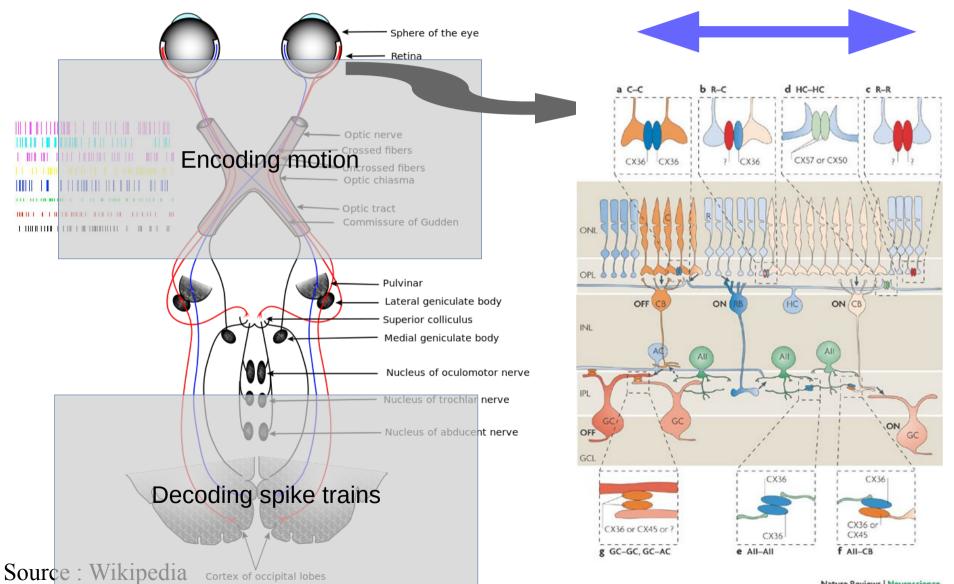


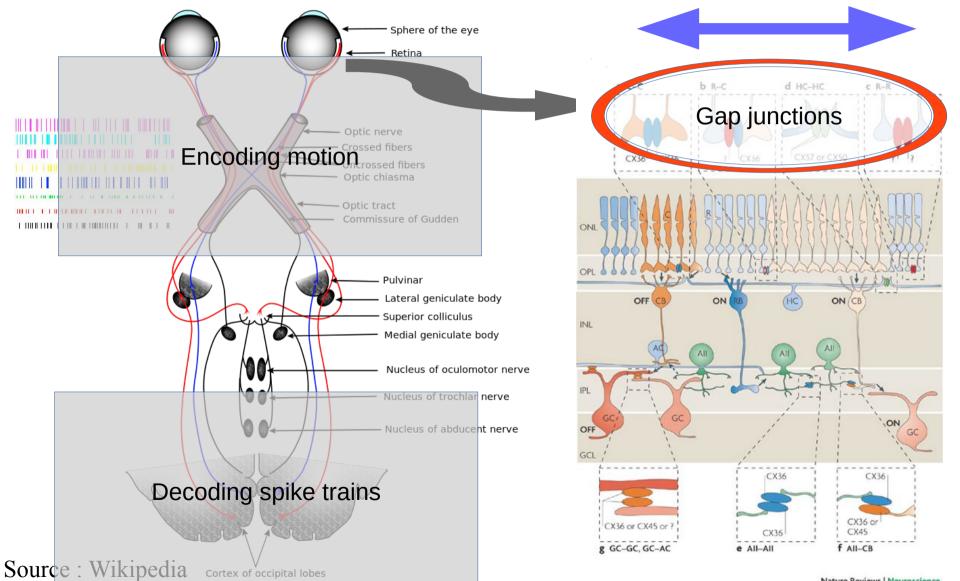
Source: Wikipedia

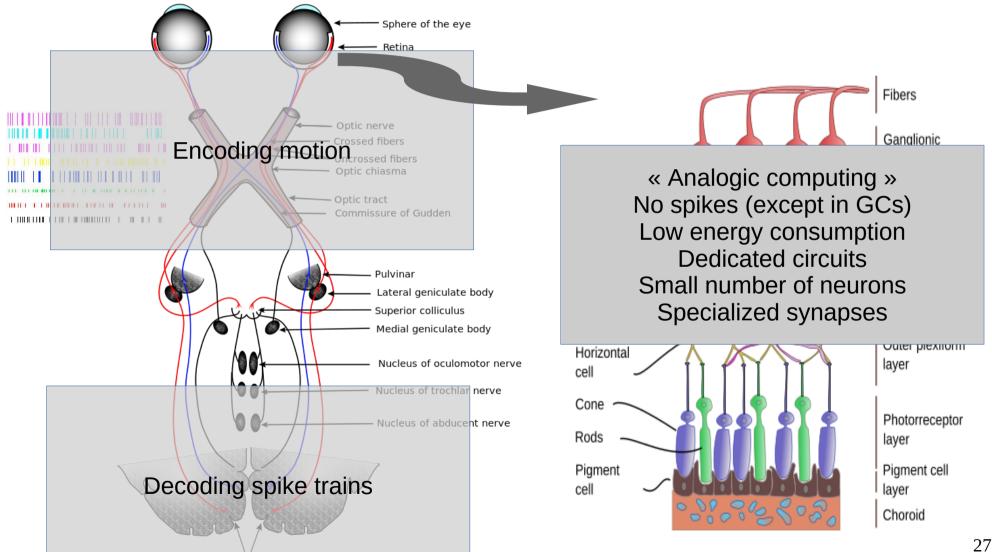
Cortex of occipital lobes







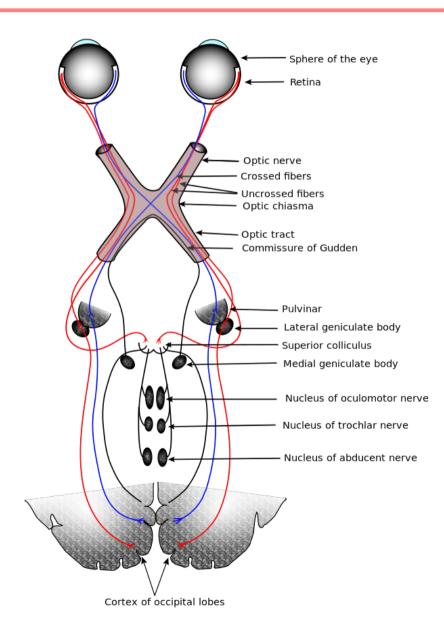


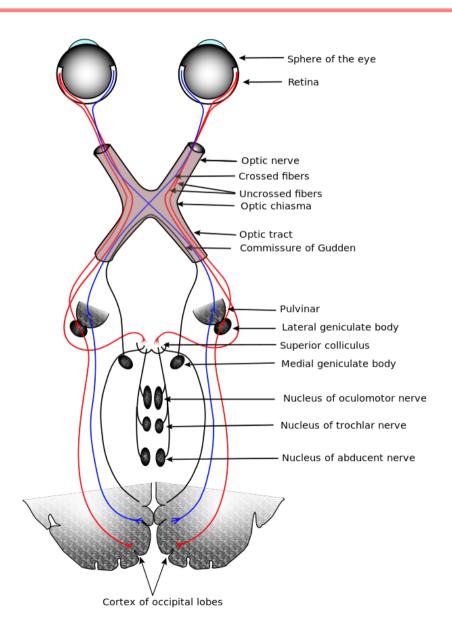


Source: Wikipedia

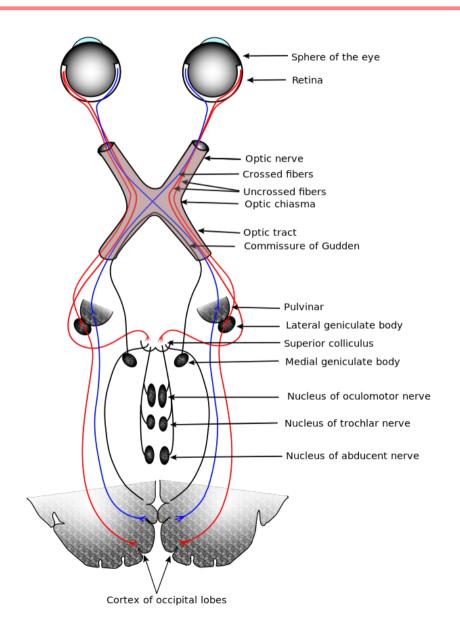
Cortex of occipital lobes

Which generic computational paradigms are at work in the retina?



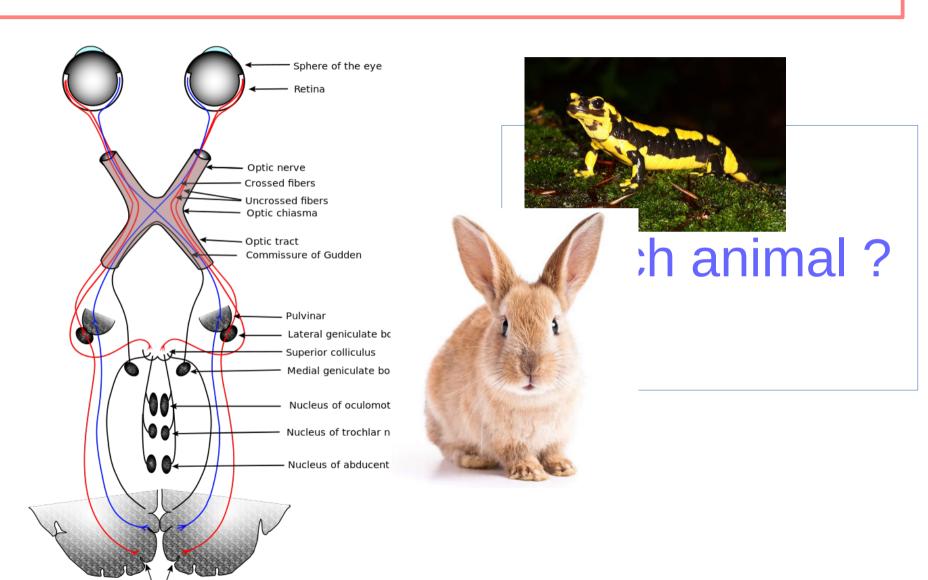


Which animal?

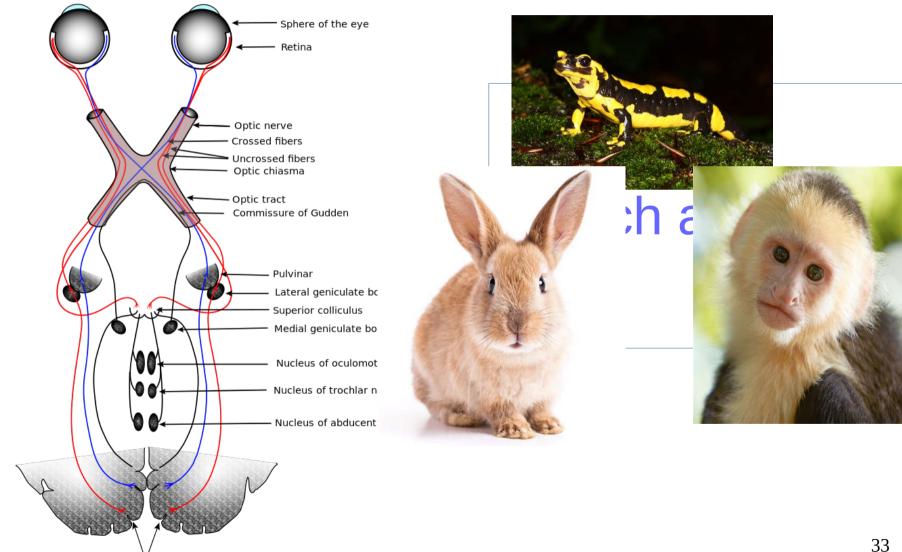




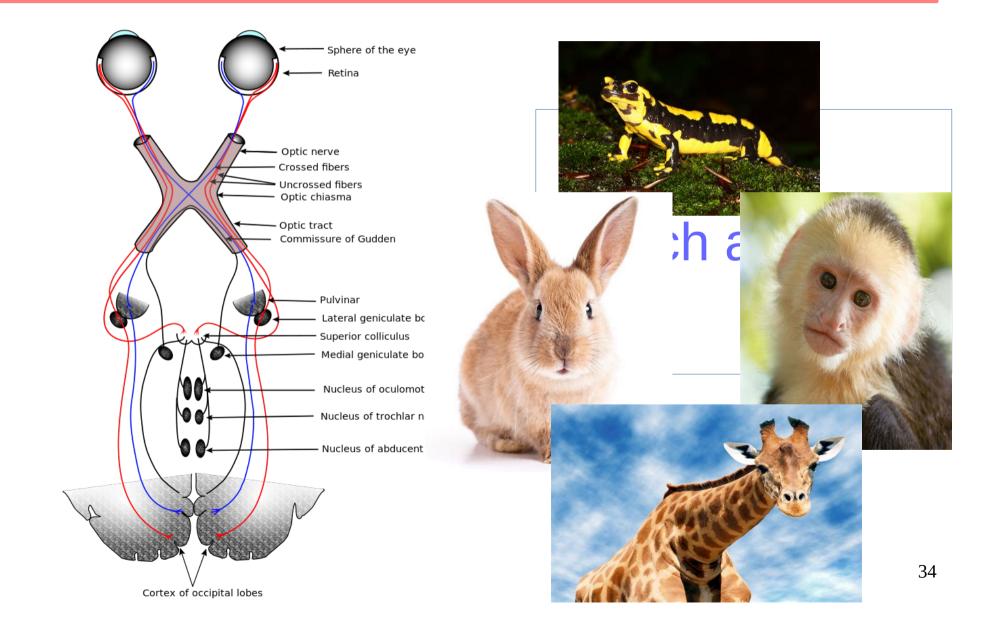
Which animal?

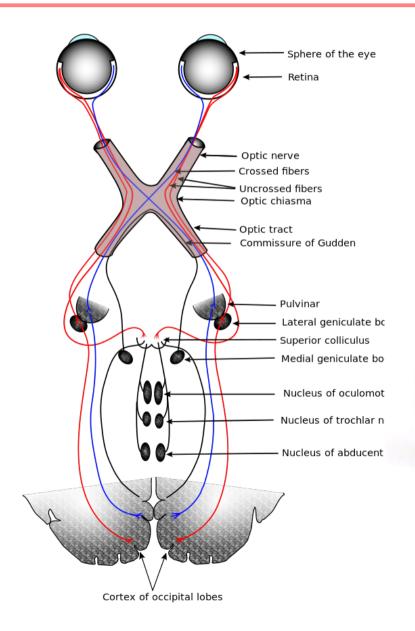


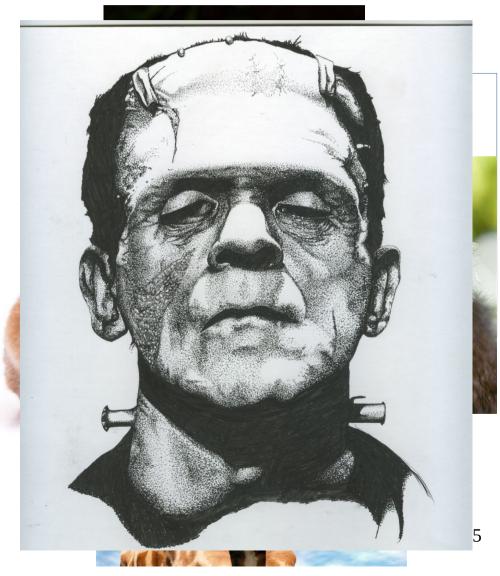
Cortex of occipital lobes



Cortex of occipital lobes







### Visual Anticipation

Developping a retino-cortical model of anticipation so as to

understand / propose

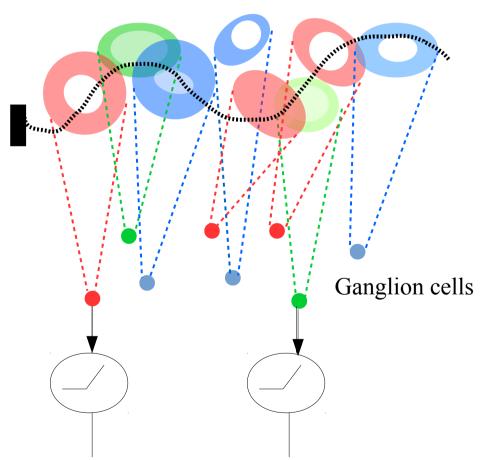
possible generic mechanisms for anticipation in the retina and in the cortex.

### Anticipation in the retina

### The Hubel-Wiesel view of vision

Nobel prize 1981

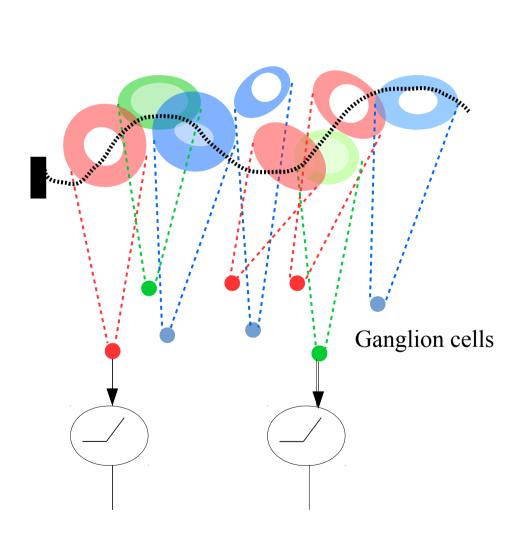
Ganglion cells response is the convolution of the stimulus with a spatio-temporal receptive field followed by a non linearity

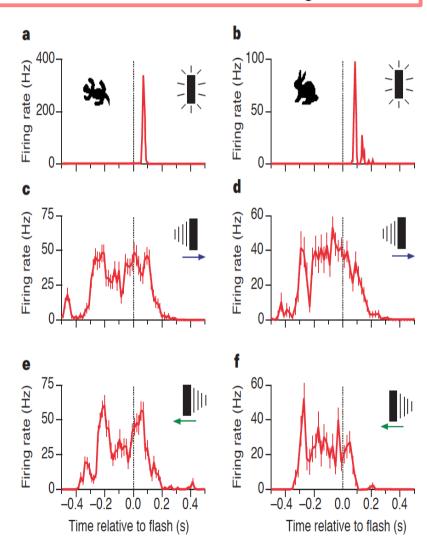


Ganglion cells are independent encoders

### The Hubel-Wiesel view of vision

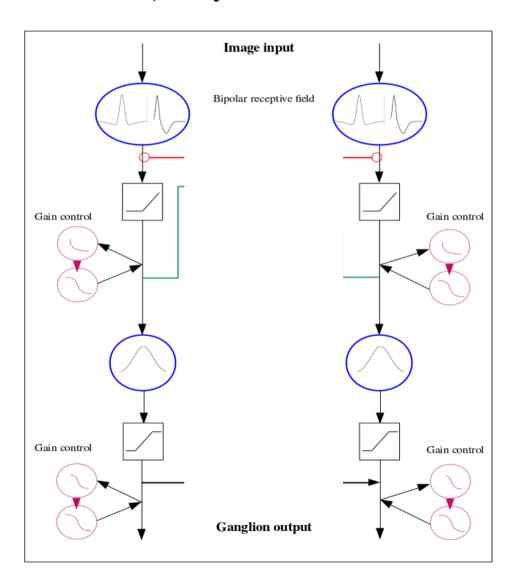
Nobel prize 1981



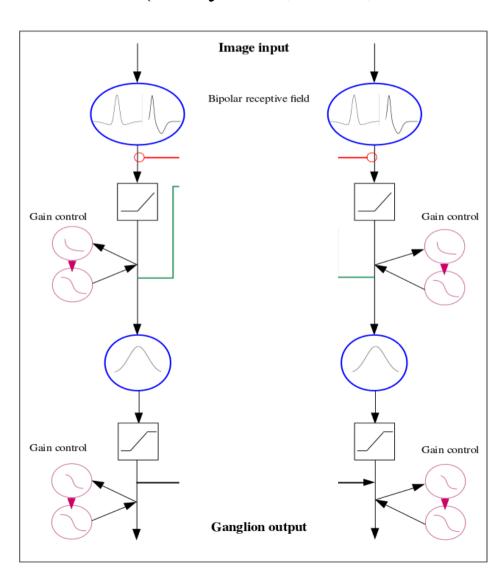


Source: Berry et al. 1999

Gain control (Berry et al, 1999, Chen et al. 2013)



Gain control (Berry et al, 1999, Chen et al. 2013)



• Bipolar voltage:

$$V_{B_i}(t) = V_{i_{drive}}(t)$$
.

Non-linear function :

$$\mathcal{N}_B(V_{B_i}) = \begin{cases} 0, & \text{if } V_{B_i} \leq \theta_B; \\ V_{B_i} - \theta_B, & \text{else.} \end{cases}$$

• Activation function:

$$\frac{dA_{B_i}}{dt} = -\frac{A_{B_i}}{\tau_a} + h \mathcal{N}(V_{B_i}(t)).$$

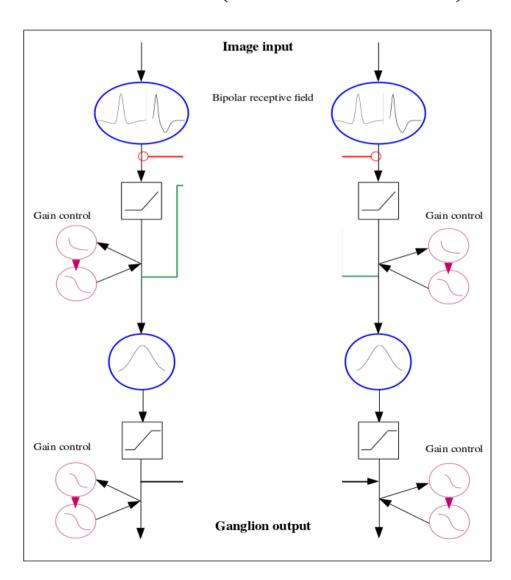
Gain Control function :

$$\mathcal{G}_B(A) = \begin{cases} 0, & \text{if } A \leq 0; \\ \frac{1}{1+A^6}, & \text{else.} \end{cases}$$

Output :

$$R_{B_i} = \mathcal{N}_B (V_{B_i}) \mathcal{G}_B (A_{B_i}).$$

#### Gain control (Chen et al. 2013)



Ganglion voltage

$$V_{G_k} = \sum_{i} W_{G_k}^{B_i} R_{B_i}$$

Non-linear function :

$$\mathcal{N}_{G_F}\left(V\right) = \left\{ \begin{array}{ll} 0, & \text{if} \quad V \leq 0; \\ \alpha_{G_F}(V - \theta_{G_F}), & \text{if} \quad \theta_{G_F} \leq V \leq N_{G_F}^{max}/\alpha_{G_F} + \theta_{G_F} \\ N_{G_F}^{max}, & \text{else.} \end{array} \right.$$

• Activation function :

$$\frac{dA_{G_{F_{k_F}}}}{dt} = -\frac{A_{G_{F_{k_F}}}}{\tau_{G_F}} + h_{G_F} \mathcal{N}_{G_F} \left( V_{G_{F_{k_F}}} \right)$$

Gain Control function :

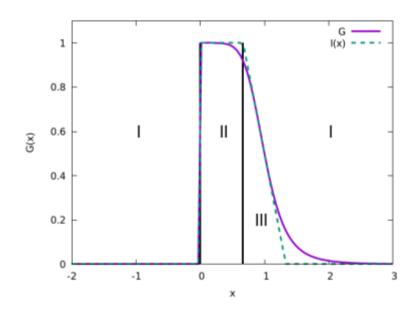
$$G_{G_F}(A) = \begin{cases} 0, & \text{if } A \leq 0; \\ \frac{1}{1+A}, & \text{else.} \end{cases}$$

• Output:

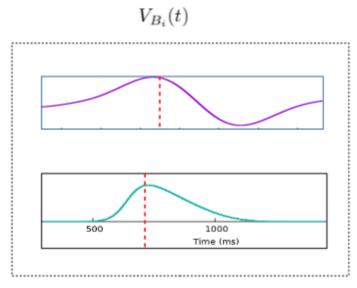
$$R_{G_{F_{k_F}}}\left(V_{G_{F_{k_F}}}, A_{G_{F_{k_F}}}\right) = \mathcal{N}_{G_F}(V_{G_{F_{k_F}}}) \mathcal{G}_{G_F}(A_{G_{F_{k_F}}}).$$

#### 1) Gain control

How does it work?

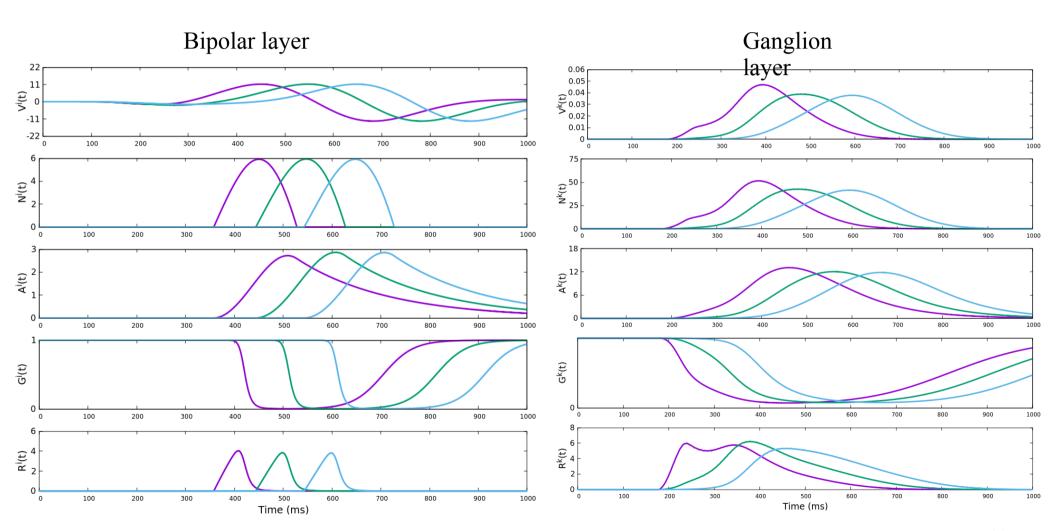


$$\mathcal{G}_B(A) = \begin{cases} 0, & \text{if } A \le 0; \\ \frac{1}{1+A^6}, & \text{else.} \end{cases}$$



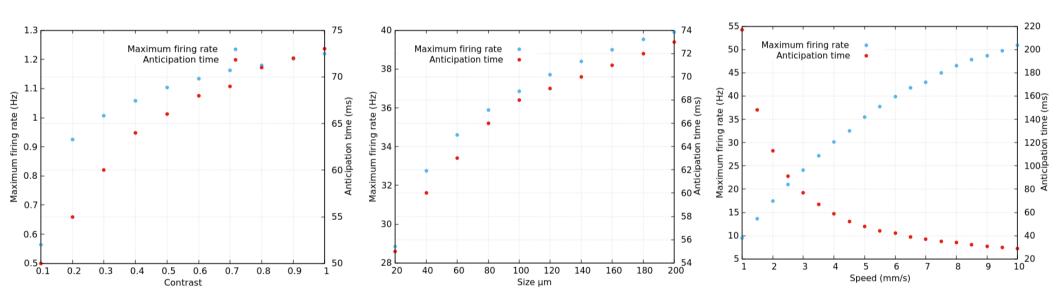
$$R_{B_i} = \mathcal{N}_B(V_{B_i}) \mathcal{G}_B(A_{B_i}).$$

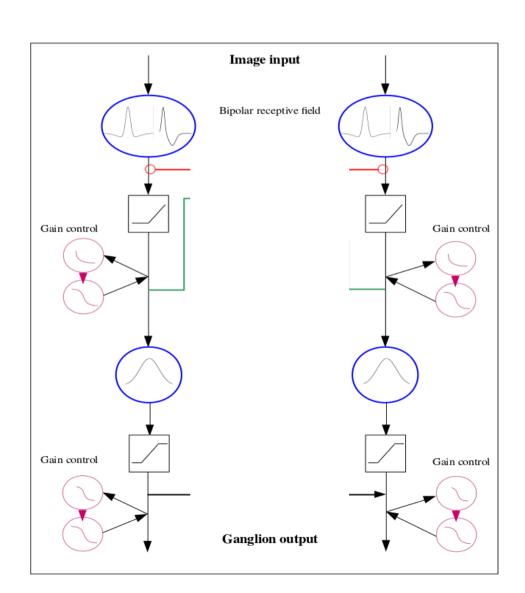
## 1D results: smooth motion anticipation with gain control



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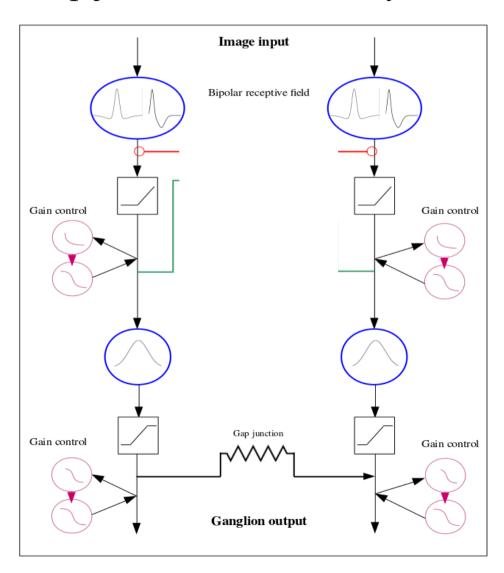
Anticipation variability with stimulus parameters





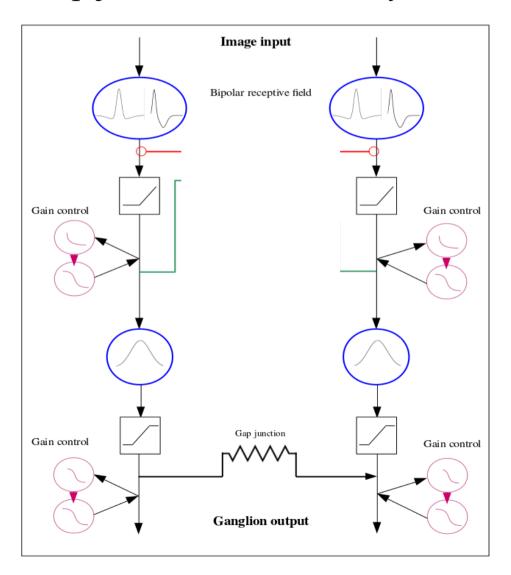
Ganglion cells are independent encoders

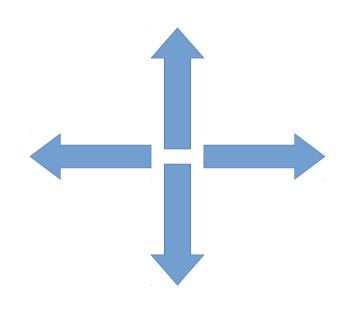
#### Gap junctions connectivity



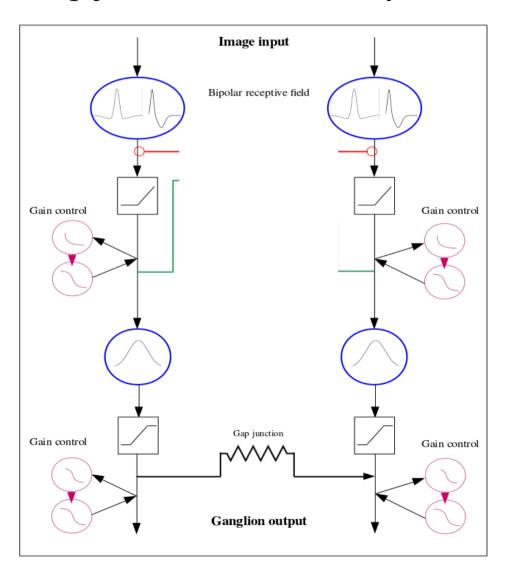
Ganglion cells are **not** independent encoders

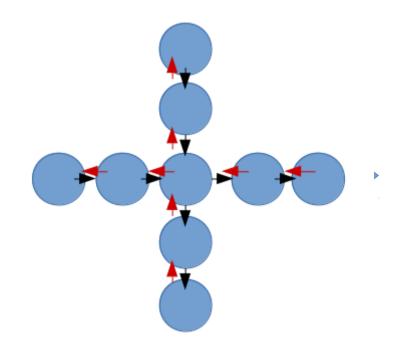
### Gap junctions connectivity



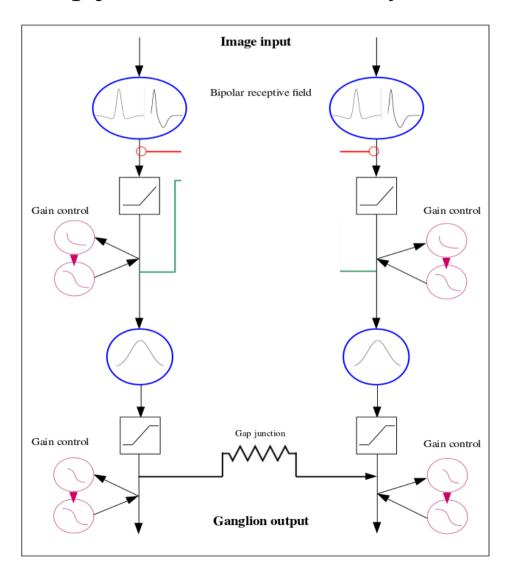


### Gap junctions connectivity

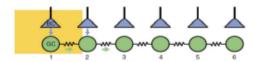




#### Gap junctions connectivity

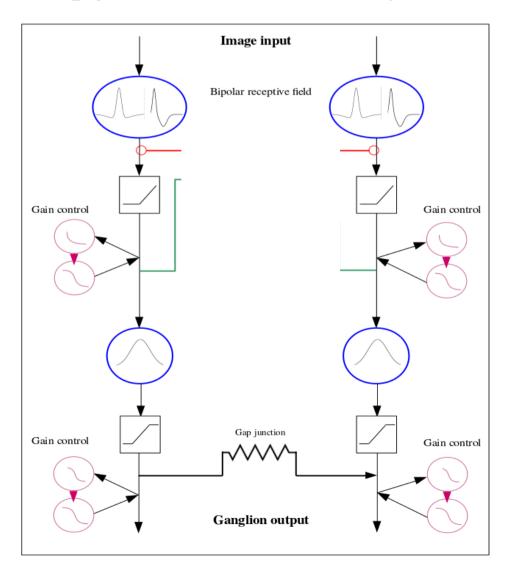


- A class of direction selective RGCs are connected through gap junctions
- Their activity comprises the activity pooled from bipolar cells and the activity coming from the downstream RGCs, in the direction of motion



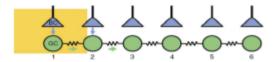
$$R_{G_{D\,k_D}} = V_{G_{D\,k_D}} + \beta\,R_{G_{D\,k_D-1}}$$

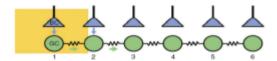
### Gap junctions connectivity

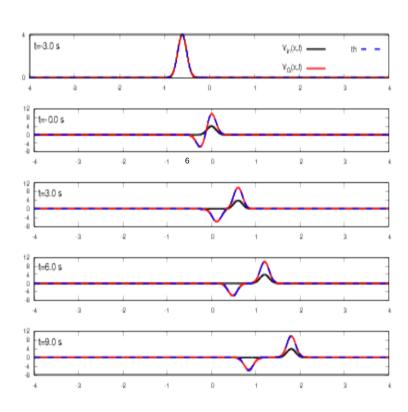


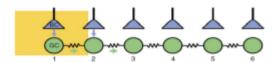
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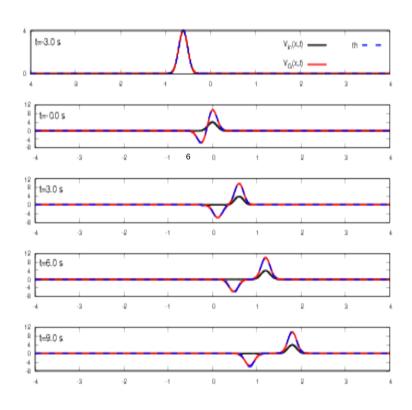
Diffusive wave of activity ahead of the motion  $R_{G_{Dk_D}} = V_{G_{Dk_D}} + \beta R_{G_{Dk_D-1}}$ 

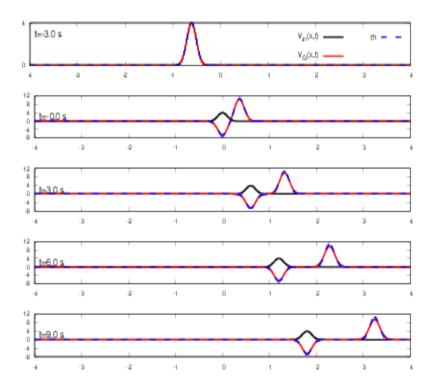




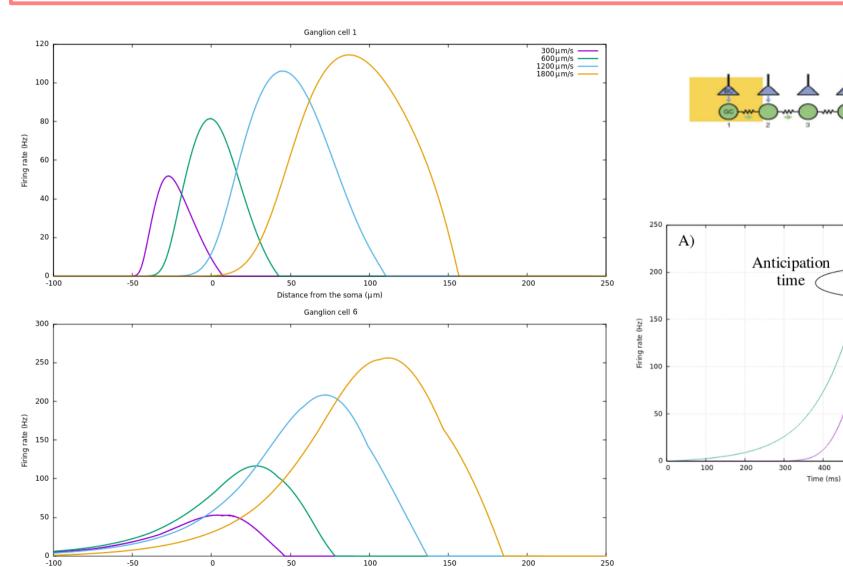








High gap junction conductance

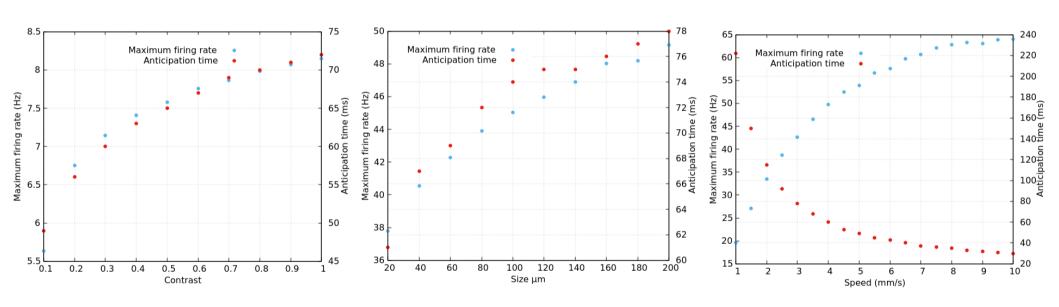


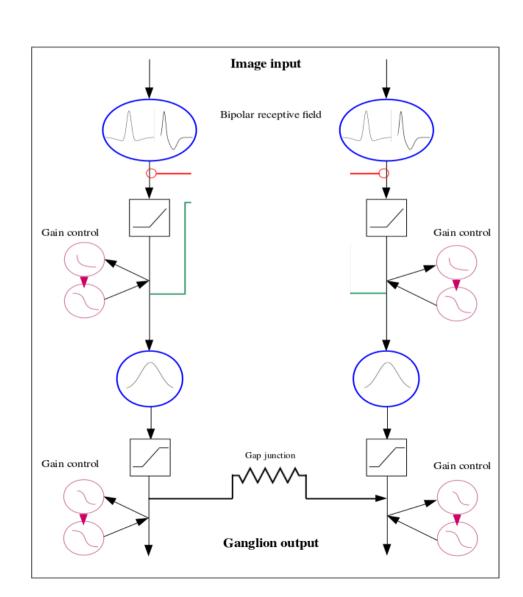
Distance from the soma (µm)

Linear response Response with gap junction

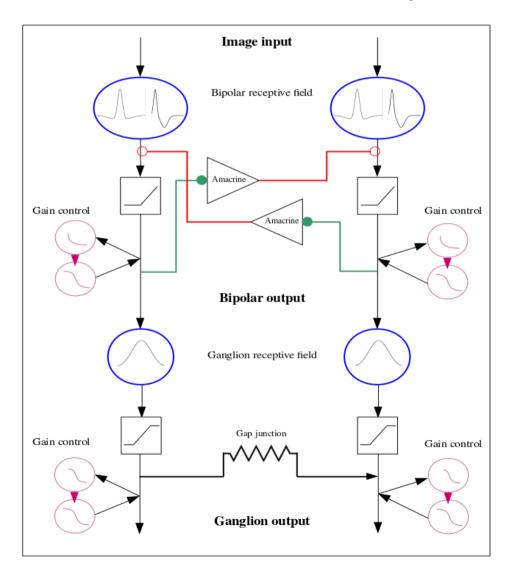
500

Anticipation variability with stimulus parameters





### Amacrine cells connectivity



Ganglion cells are **not** independent encoders

### Amacrine cells connectivity



Amacrine cells connectivity



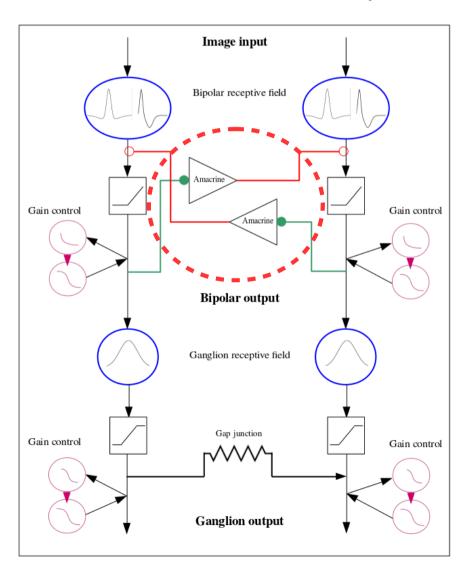
#### Amacrine cells connectivity

• A class of RGCs are selective to differential motion

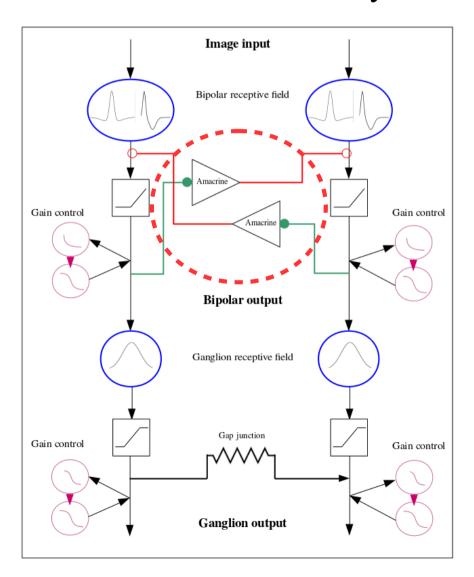


• The circuitry involves amacrine cells connectivity upstream of ganglion cells

### Amacrine cells connectivity



#### Amacrine cells connectivity



• Bipolar voltage:

$$\frac{dV_{B_i}}{dt} = -\frac{1}{\tau_B} V_{B_i} + \sum_{j=1}^{N_A} W_{B_i}^{A_j} V_{A_j} + F_{B_i}(t).$$

External drive :

$$F_{B_i}(t) = \left[ K_i \stackrel{S,t}{*} \left( \frac{S}{\tau_B} + \frac{dS}{dt} \right) \right] (t)$$

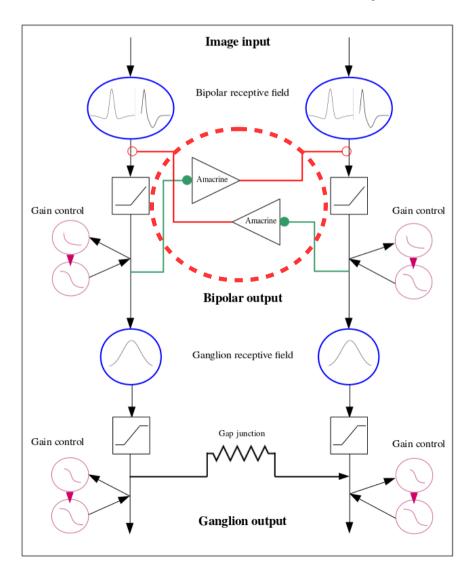
· Amacrine voltage:

$$\frac{dV_{A_j}}{dt} = -\frac{1}{\tau_A} V_{A_j}(t) + \sum_{i=1}^{N_A} W_{A_j}^{B_i} R_{B_i}(t).$$

• Coupled dynamics :

$$\begin{cases} \frac{dV_{B_i}}{dt} &= -\frac{1}{\tau_B} V_{B_i} + \sum_{j=1}^{N_A} W_{B_i}^{A_j} V_{A_j} + F_{B_i}(t) \\ \frac{dA_{B_i}}{dt} &= -\frac{A_{B_i}}{\tau_a} + h \mathcal{N}(V_{B_i}(t)), \\ \frac{dV_{A_j}}{dt} &= -\frac{1}{\tau_A} V_{A_j}(t) + \sum_{i=1}^{N_A} W_{A_j}^{B_i} R_{B_i}(t). \end{cases}$$

#### Amacrine cells connectivity



• Bipolar voltage:

$$\frac{dV_{B_i}}{dt} = -\frac{1}{\tau_B} V_{B_i} + \sum_{j=1}^{N_A} W_{B_i}^{A_j} V_{A_j} + F_{B_i}(t).$$

External drive :

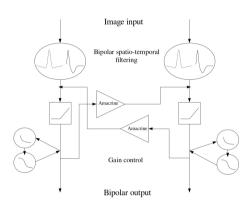
$$F_{B_i}(t) = \left[ K_i * \left( \frac{\mathcal{S}}{\tau_B} + \frac{d\mathcal{S}}{dt} \right) \right](t)$$

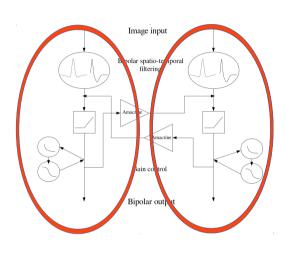
• Amacrine voltage:

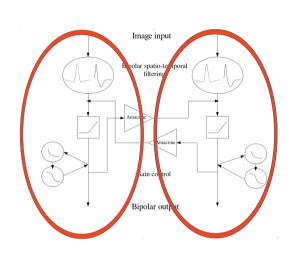
 $\begin{array}{c} \text{Diffusive}_1 \text{wave of activity} \\ \frac{1}{dt} \text{ ahead of the bar} W_{A_j}^{B_i} R_{B_i}(t). \end{array}$ 

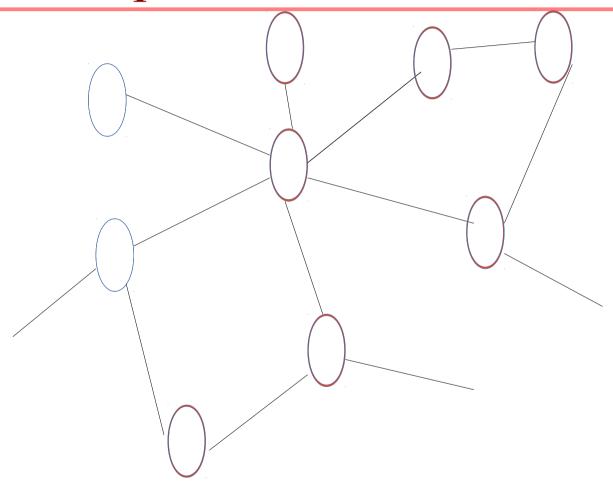
• Coupled dynamics:

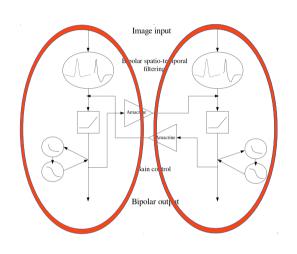
$$\begin{cases} \frac{dV_{B_i}}{dt} &= -\frac{1}{\tau_B} V_{B_i} + \sum_{j=1}^{N_A} W_{B_i}^{A_j} V_{A_j} + F_{B_i}(t) \\ \frac{dA_{B_i}}{dt} &= -\frac{A_{B_i}}{\tau_a} + h \mathcal{N}(V_{B_i}(t)), \\ \frac{dV_{A_j}}{dt} &= -\frac{1}{\tau_A} V_{A_j}(t) + \sum_{i=1}^{N_A} W_{A_j}^{B_i} R_{B_i}(t). \end{cases}$$

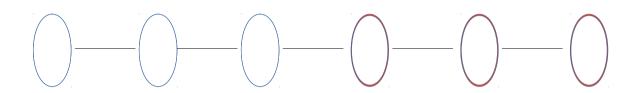


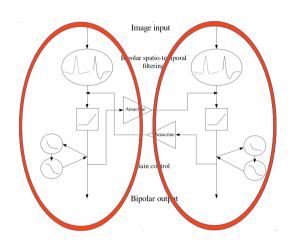


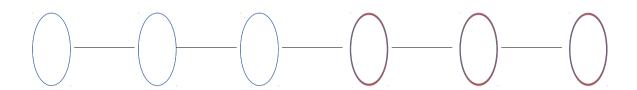




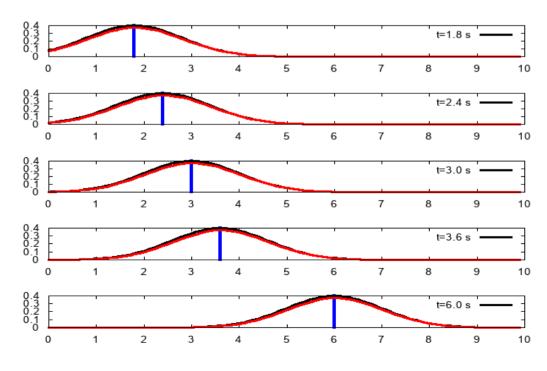


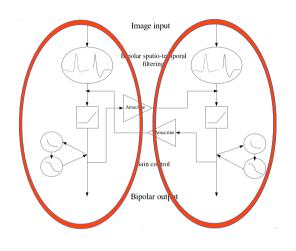


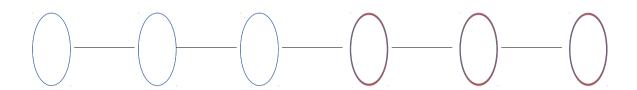




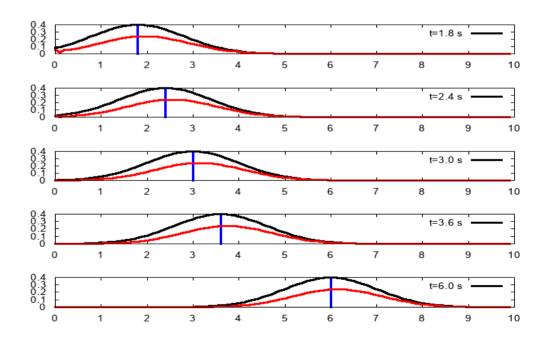
Spatial profiles w=1

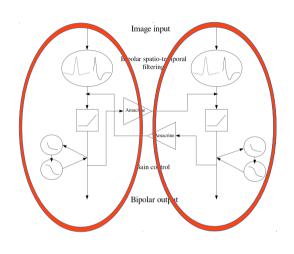


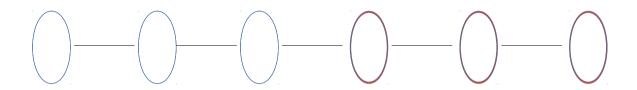




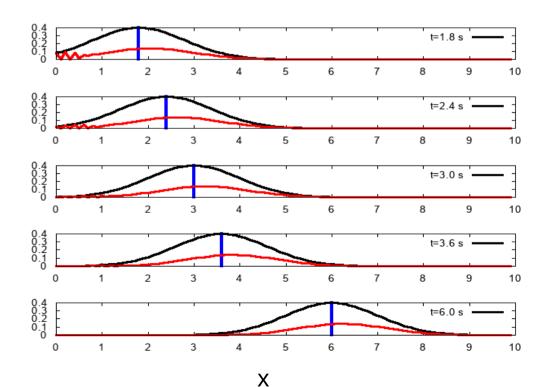
Spatial profiles w=3



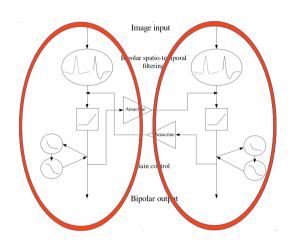


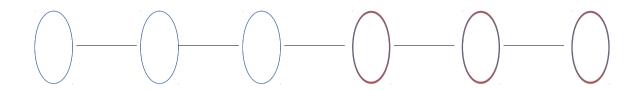


Spatial profiles w=5

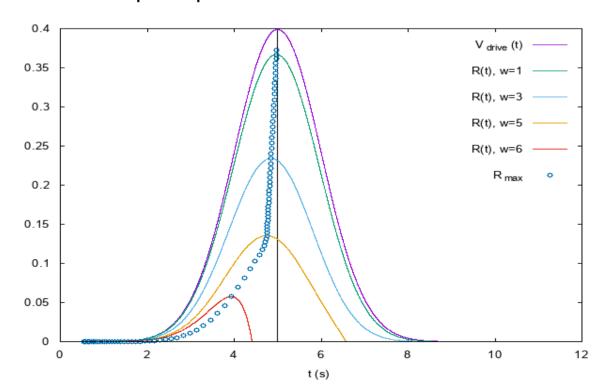


# Building a 2D retina model for motion anticipation

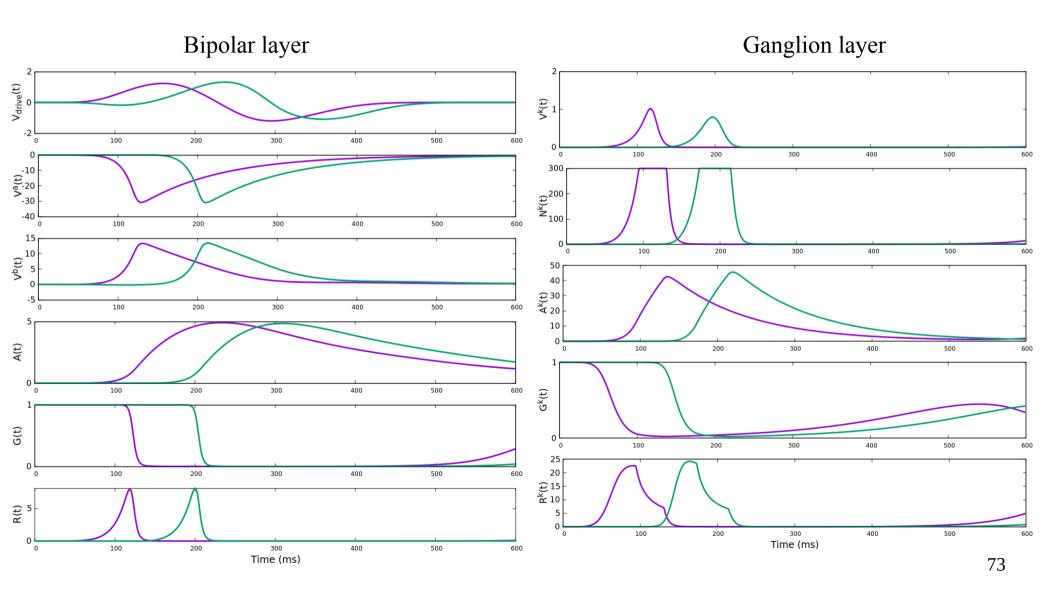




#### Temporal profile of the middle cell

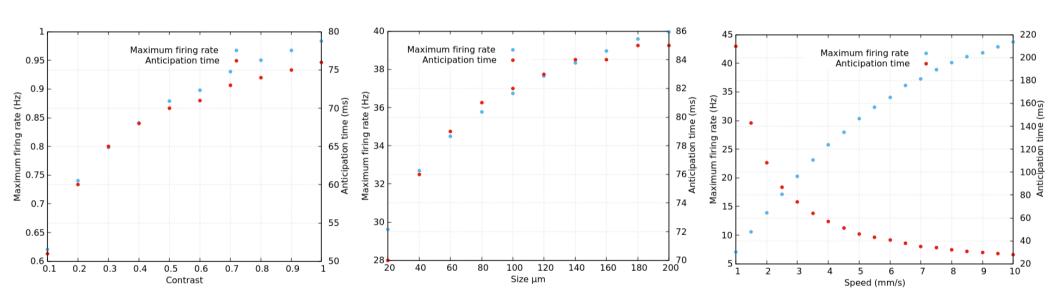


# 1D results: smooth motion anticipation with amacrine connectivity

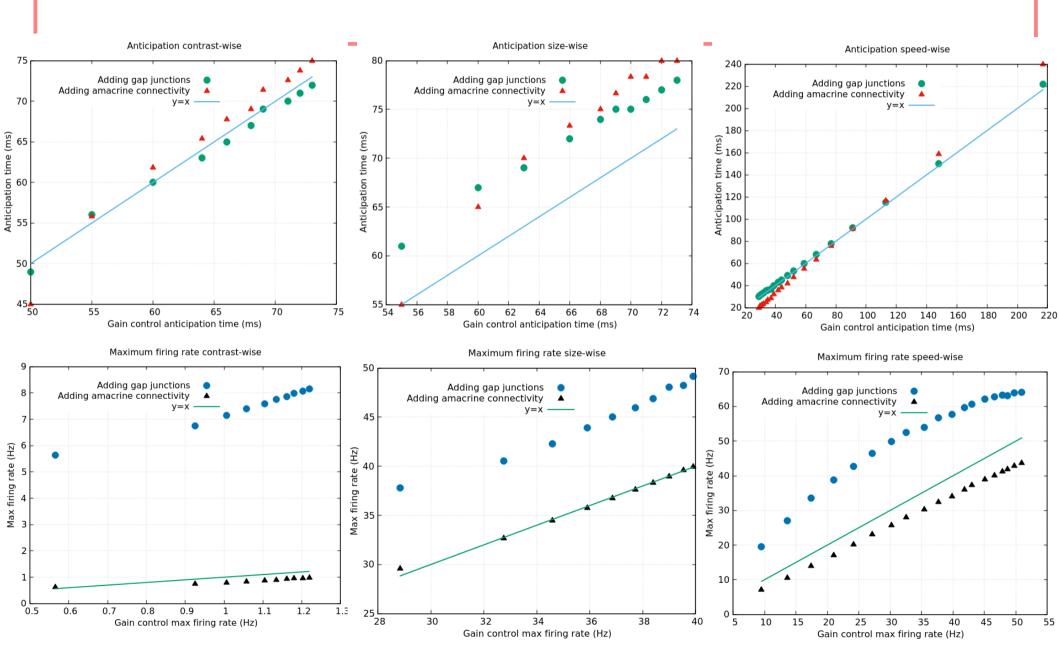


# 1D results: smooth motion anticipation with amacrine connectivity

Anticipation variability with stimulus parameters

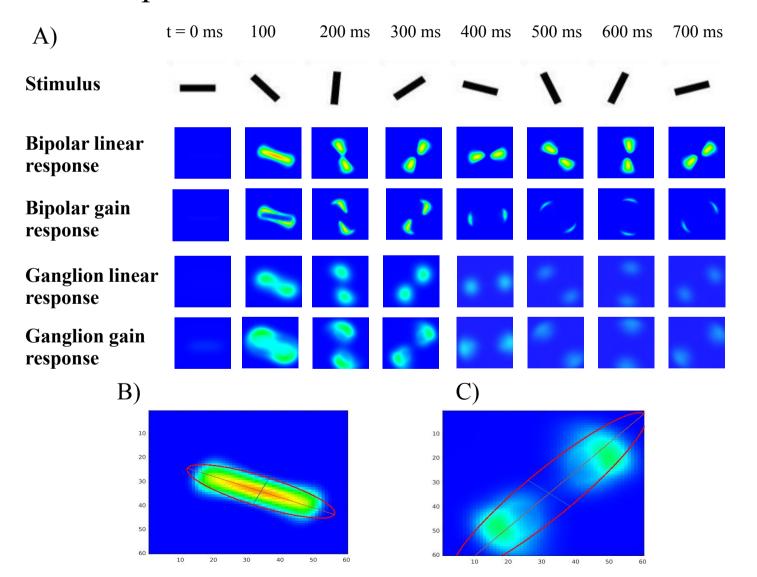


### Comparing the performance of the three layers



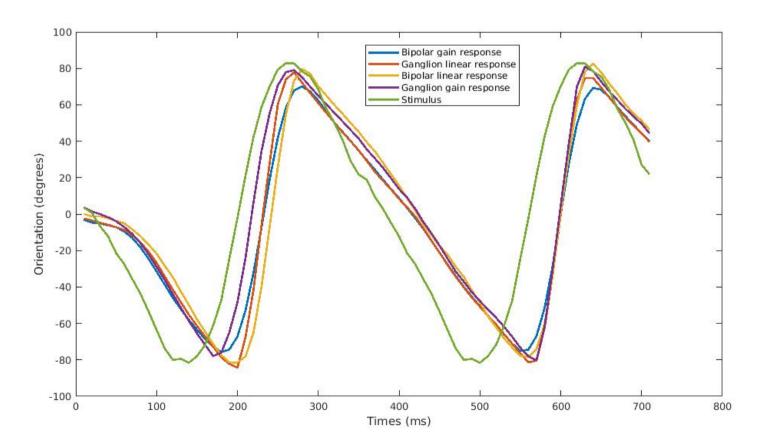
### Suggesting new experiments: 2D results

#### 1) Angular anticipation



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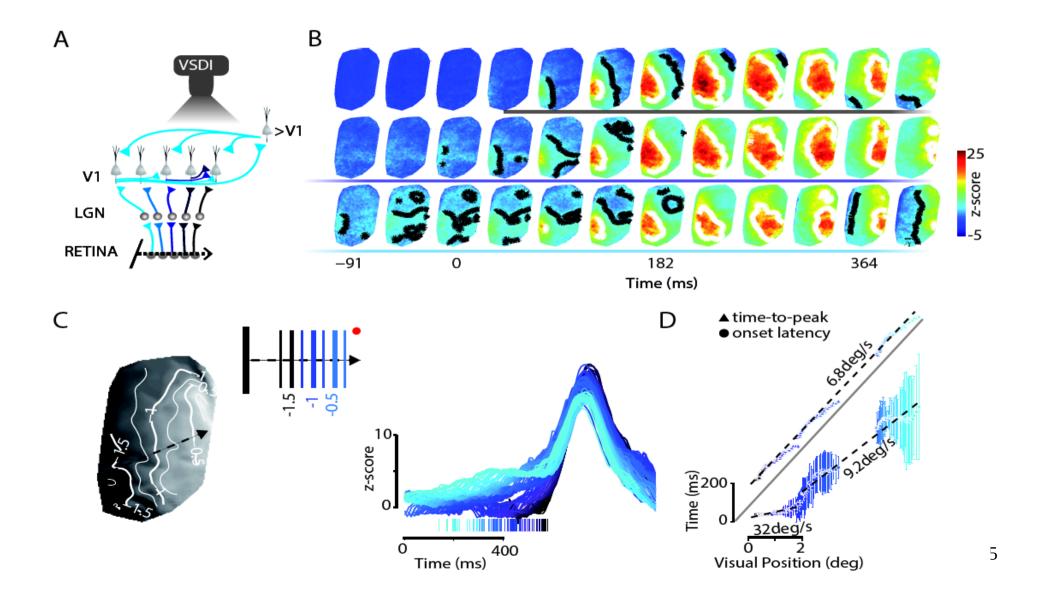
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- Here we propose that lateral connectivity also plays a role in motion anticipation where a wave of activity propagates ahead of the motion.
- Useful paradigms for:
  - 1) Computer vision?
  - 2) Retinal prostheses?

### Anticipation in V1

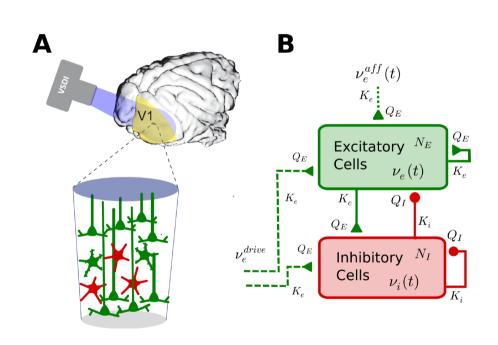
### Anticipation in V1

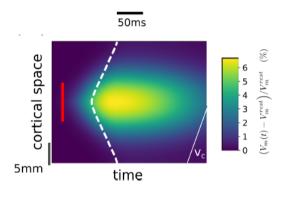


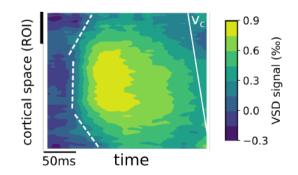
### A mean field model to reproduce VSDI

recordings

Zerlaut et al 2016 Chemla et al 2018







Chemla et al 2018

Master equation for first and second moments local population dynamics (El Boustani and Destexhe, 2009) read:

$$\begin{cases} T \frac{\partial \nu_{\mu}}{\partial t} = (\mathcal{F}_{\mu} - \nu_{\mu}) + \frac{1}{2} c_{\lambda \eta} \frac{\partial^{2} \mathcal{F}_{\mu}}{\partial \nu_{\lambda} \partial \nu_{\eta}} \\ T \frac{\partial c_{\lambda \eta}}{\partial t} = A_{\lambda \eta} + (\mathcal{F}_{\lambda} - \nu_{\lambda}) (\mathcal{F}_{\eta} - \nu_{\eta}) + \\ c_{\lambda \mu} \frac{\partial \mathcal{F}_{\mu}}{\partial \nu_{\lambda}} + c_{\mu \eta} \frac{\partial \mathcal{F}_{\mu}}{\partial \nu_{\eta}} - 2c_{\lambda \eta} \end{cases} \longrightarrow T \frac{\partial \nu_{\mu}}{\partial t} = \mathcal{F}_{\mu} - \nu_{\mu}$$

$$A_{\lambda\eta} = \begin{cases} \frac{\mathcal{F}_{\lambda} (1/T - \mathcal{F}_{\lambda})}{N_{\lambda}} & \text{if } \lambda = \eta \\ 0 & \text{otherwise} \end{cases}$$

# A mean field model to reproduce VSDI recordings Zerlaut et al 2016 Chemla et al 2018

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Chemla et al 2018

Single neuron model (The adaptative exponential integrate and fire model Brette and Gerstner, 2005)

$$\begin{cases} C_m \frac{dV}{dt} = g_L (E_L - V) + I_{syn}(V, t) + k_a e^{\frac{V - V_{thre}}{k_a}} - I_w \\ \tau_w \frac{dI_w}{dt} = -I_w + a \cdot (V - E_L) + \sum_{t_s \in \{t_{spike}\}} b \, \delta(t - t_s) \end{cases}$$

The conductance-based exponential synapse

$$I_{syn}(V,t) = \sum_{s \in \{e,i\}} \sum_{t_s \in \{t_s\}} Q_s \left(E_s - V\right) e^{-\frac{t - t_s}{\tau_s}} \, \mathcal{H}(t - t_s)$$

Semi analytical transfer function:

$$\nu_{out} = \mathcal{F}(\nu_e, \nu_i) = \frac{1}{2 \tau_V} \cdot Erfc(\frac{V_{thre}^{eff} - \mu_V}{\sqrt{2} \sigma_V}) \quad \text{with} \quad V_{thre}^{eff}(\mu_V, \sigma_V, \tau_V^N) = P_0 + \sum_{x \in \{\mu_V, \sigma_V, \tau_V^N\}} P_x \cdot \left(\frac{x - x^0}{\delta x^0}\right) + P_{\mu_G} \log(\frac{\mu_G}{g_L}) \\ + \sum_{x, y \in \{\mu_V, \sigma_V, \tau_V^N\}^2} P_{xy} \cdot \left(\frac{x - x^0}{\delta x^0}\right) \left(\frac{y - y^0}{\delta y^0}\right)$$

Chemla et al 2018

The mean, standard deviation and auto-correlation time of the excitatory and inhibitory conductance read:

$$\mu_{Ge}(\nu_{e},\nu_{i}) = \nu_{e} K_{e} \tau_{e} Q_{e}$$

$$\sigma_{Ge}(\nu_{e},\nu_{i}) = \sqrt{\frac{\nu_{e} K_{e} \tau_{e}}{2}} Q_{e}$$

$$\mu_{Gi}(\nu_{e},\nu_{i}) = \nu_{i} K_{i} \tau_{i} Q_{i}$$

$$\sigma_{Gi}(\nu_{e},\nu_{i}) = \sqrt{\frac{\nu_{i} K_{i} \tau_{i}}{2}} Q_{i}$$

$$\mu_{V}(\nu_{e},\nu_{i}) = \frac{\mu_{Ge} E_{e} + \mu_{Gi} E_{i} + g_{L} E_{L}}{\mu_{G}}$$

$$\sigma_{V}(\nu_{e},\nu_{i}) = \sqrt{\sum_{s} K_{s} \nu_{s} \frac{(U_{s} \cdot \tau_{s})^{2}}{2 \left(\tau_{m}^{\text{eff}} + \tau_{s}\right)}}$$

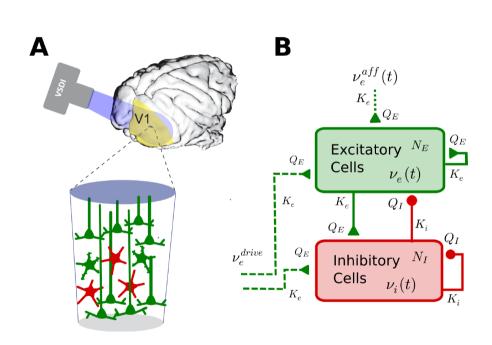
$$\tau_{V}(\nu_{e},\nu_{i}) = \left(\frac{\sum_{s} \left(K_{s} \nu_{s} \left(U_{s} \cdot \tau_{s}\right)^{2}\right)}{\sum_{s} \left(K_{s} \nu_{s} \left(U_{s} \cdot \tau_{s}\right)^{2}/\left(\tau_{m}^{\text{eff}} + \tau_{s}\right)\right)}\right)$$

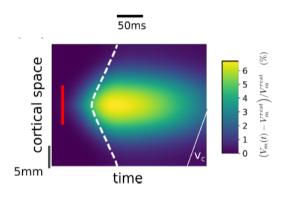
Finally, the transfer function reads:

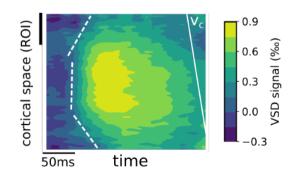
$$\nu_{out} = \mathcal{F}(\nu_e, \nu_i) = \frac{1}{2 \, \tau_V} \cdot Erfc(\frac{V_{thre}^{eff} - \mu_V}{\sqrt{2} \, \sigma_V})$$

recordings

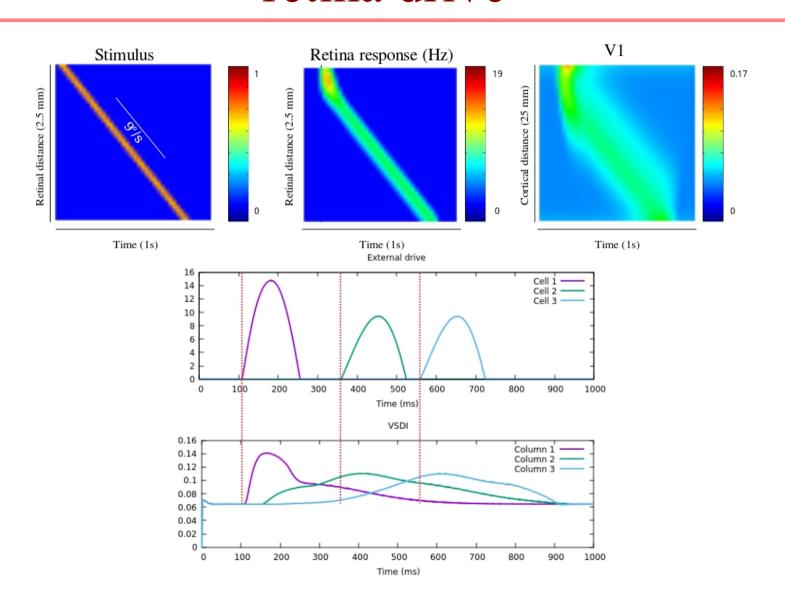
Zerlaut et al 2016
Chemla et al 2018



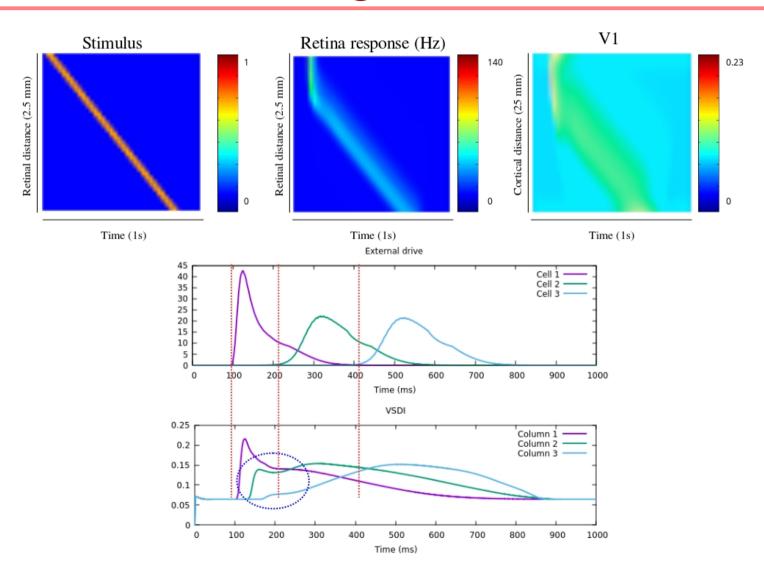




## Response of the cortical model to a LN retina drive



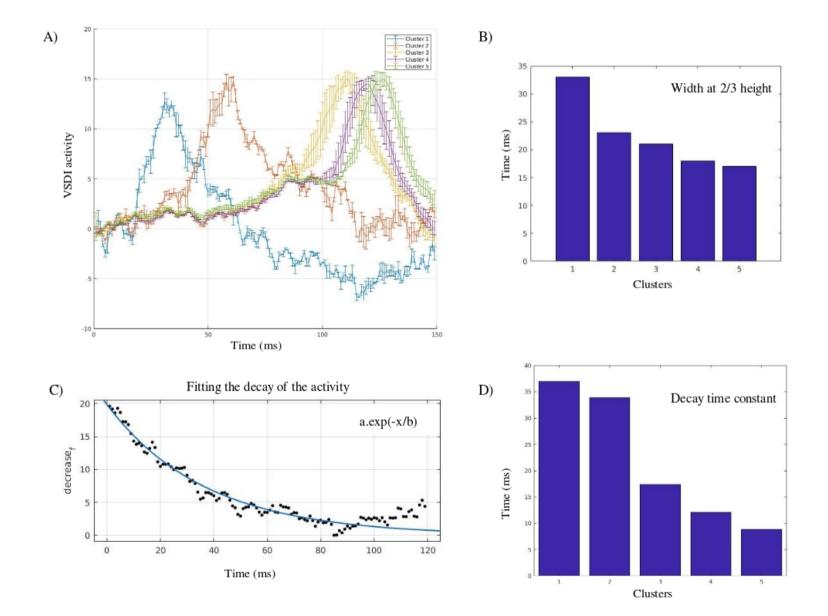
# Response of the cortical model to a retina drive with gain control



### Anticipation in the cortex: VSDI data

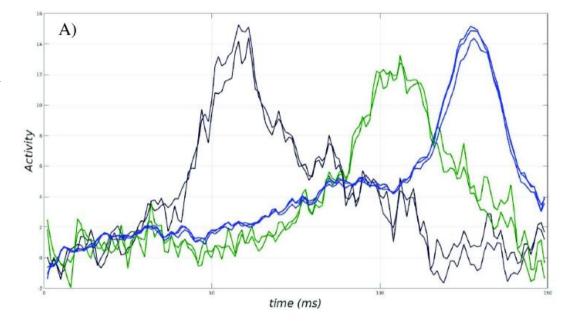
analysis

(Data courtesy of F. Chavane et S. Chemla)

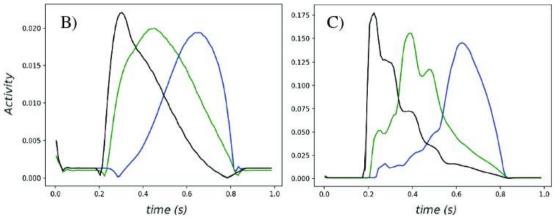


# Comparing simulation results to VSDI recordings

Cortex experimental recordings



Simulation results Response to an LN model of the retina



Simulation results Response to a gain control model of the retina

- We developed a 2D retina with three ganglion cell layers, implementing gain control and connectivity.
- We use the output of our model as an input to a mean field model of V1, and were able to reproduce anticipation as observed in VSDI

- How to improve object identification
  - 1) exploring the model's parameters and
    - 2) using connectivity?
- Is our model able to anticipate more complex trajectories, with accelerations for instance?
- How to calibrate connectivity using biology?
- How does anticipation affect higher order correlations?
- Would it be possible to design psycho-physical tests clearly showing the role of the retina in visual anticipation?

Thank you for your attention!