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Is Acyclic Directed Graph Partitioning Effective for Locality-Aware Scheduling?

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Abstract. We investigate efficient execution of computations, modeled as Directed Acyclic Graphs (DAGs), on a single processor with a two-level memory hierarchy, where there is a limited fast memory and a larger slower memory. Our goal is to minimize execution time by minimizing redundant data movement between fast and slow memory. We utilize a DAG partitioner that finds localized, acyclic parts of the whole computation that can fit into fast memory, and minimizes the edge cut among the parts. We propose a new scheduler that executes each part one-by-one, obeying the dependency among parts, aiming at reducing redundant data movement needed by cut-edges. Extensive experimental evaluation shows that the proposed DAG-based scheduler significantly reduces redundant data movement.

1 Introduction

In today’s computers, the cost of data movement through the memory hierarchy is dominant relative to the cost of arithmetic operations, and it is expected that the gap will continue to increase [6,12]. Hence, a significant portion of research efforts focuses on optimizing the data locality [1,5].

Sparse computations are used by many scientific applications but they are notorious for their poor performance due to their irregular memory accesses and hence poor data locality in the cache. One of widely used such kernels is Sparse Matrix-Vector Multiplication (SpMV), which is the main computation kernel for various applications (e.g., spectral clustering [9], dimensionality reduction [13], PageRank algorithm [10], etc.). Similarly, Sparse Matrix-Matrix Multiplication (SpMM), which is one of the main operations in many Linear Algebraic problems, suffers from similar cache under-utilization caused by unoptimized locality decisions. In this work, we aim to optimize repeated execution of such kernels, whose dependency structure can be expressed as a DAG.

We investigate efficient execution of sparse and irregular computations, modeled as Directed Acyclic Graphs (DAGs) on a single processor, with a two-level memory hierarchy. There are limited number of fast memory locations, and an unlimited number of slow memory locations. In order to compute a task, the processor must load all of the input data that the task needs, and it will also
need some scratch memory for the task and its output. Because of the limited fast memory, some computed values may need to be temporarily stored in slow memory and reloaded later.

Utilizing graph and hypergraph partitioning for effective use of cache has been studied by others before (e.g., [1,14]). However, to the best of our knowledge, our work is the first one that utilizes a multilevel acyclic DAG partitioning. Acyclic partitioning allows us to develop a new scheduler, which will load each part only once, and execute parts non-preemptively. Since the parts are computed to fit into fast memory, and they are acyclic, once all “incoming” edges of the part are loaded, all the tasks in that part can be executed non-preemptively, and without any need to bring additional data. Earlier studies that use undirected partitioning, cannot guarantee such execution model.

The rest of the paper is organized as follows. In Section 2, we present the computational model. Section 3 describes the proposed DAG-partitioning based scheduling algorithms. Experimental evaluation of the proposed methods is displayed in Section 4. We end with a brief conclusion and future work in Section 5.

2 Model

We consider a directed acyclic graph (DAG) $G = (V, E)$, where the vertices in set $V = \{v_1, \ldots, v_n\}$ represent computational tasks, and the dependency among them, hence the communication of data between tasks, is captured by graph edges in set $E$. Given $v_i \in V$, $\text{pred}_i = \{v_j \mid (v_j, v_i) \in E\}$ is the set of predecessors of task $v_i$ in the graph, and $\text{succ}_i = \{v_j \mid (v_i, v_j) \in E\}$ is the set of successors of task $v_i$.

Vertices and edges have weights representing the size of the (scratch) memory required for task $v_i \in V$, $w_i$, and size of the data that is communicated to its successors. Here, we assume $v_i$ produces a data of size $\text{out}_i$ that will be communicated to all of its successors, hence weight of each edge $(v_i, v_j) \in E$ will be $\text{out}_i$. An entry task $v_i \in V$ is a task with no predecessors (i.e., $\text{pred}_i = \emptyset$), and such a task is a virtual task generating the initial data, hence $w_i = 0$. All other tasks (with $\text{pred}_i \neq \emptyset$) cannot start until all predecessors have completed, and the data from each predecessor has been generated. For simplicity in the presentation, we will use $w_i = 0$ and $\text{out}_i = 1$. Hence, total input size of task $v_i$ is $\text{in}_i = |\text{pred}_i|$, and $\text{in}_i = 0$ if task $v_i$ is an entry task.

We will assume the size of fast memory is $C$, and slow memory is large enough to hold whole data and computation. In order to compute task $v_i \in V$, the processor must access $\text{in}_i + w_i + \text{out}_i$ fast memory locations. Because of the limited fast memory, some computed values may need to be temporarily stored in slow memory and reloaded later.

Consider the example in Figure 1. Task $v_1$ is the entry task and therefore just requires one cache location to generate its output data ($\text{out}_1 = 1$). The data corresponding to $\text{out}_1$ remains in cache while there is no need to evict it, while $\text{in}_1$ and $w_1$ will no longer be needed and can be evicted (but for an entry task, these are equal to 0). Consider that $v_2$ is executed next: it will need two cache
locations \((in_2 = out_2 = 1)\). Then \(v_3\) is executed. We want to keep \(out_1\) in cache, if possible, since it will be reused later by \(v_5\) and \(v_7\). Hence, 3 memory locations are required. Similarly, when executing \(v_4\), 4 memory locations are required \((out_2\) should also remain in cache). However, if the cache is too small, say \(C = 3\), one will need to evict a data from the cache, hence resulting in a cache miss.

Given a traversal of the DAG, the livesize (live set size) is defined as the minimum cache size required for the execution so that there are no cache misses. In the example, with the traversal \(v_1 \rightarrow v_2 \rightarrow v_3 \rightarrow v_4 \rightarrow v_5 \rightarrow v_6 \rightarrow v_7\), it would be 4. For another traversal however, the livesize may be smaller, and hence the order of traversal may greatly influence the number of cache misses. Consider the execution \(v_1 \rightarrow v_7 \rightarrow v_2 \rightarrow v_5 \rightarrow v_6 \rightarrow v_3 \rightarrow v_4\): the livesize never exceeds 3 in this case, and this is the minimum cache size to execute this DAG, since task \(v_6\) requires 3 cache locations to be executed.

**Parts, cuts, traversals, and livesize.** We generalize and formalize the definition of the livesize introduced above. Consider an acyclic \(k\)-way partition \(P = \{V_1, \ldots, V_k\}\) of the DAG \(G = (V, E)\): the set of vertices \(V\) is divided into \(k\) disjoint subsets, or parts. There is a path between \(V_i\) and \(V_j\) \((V_i \sim V_j)\) if and only if there is a path in \(G\) between a vertex \(v_i \in V_i\) and a vertex \(v_j \in V_j\). The acyclic condition means that given any two parts \(V_i\) and \(V_j\), we cannot have \(V_i \sim V_j\) and \(V_j \sim V_i\). In the example of Figure 1, an example of acyclic partition is \(V_1 = \{v_1, v_2, v_3, v_4\}\) and \(V_2 = \{v_5, v_6, v_7\}\).

Given a partition \(P\) of the DAG, an edge is called a cut edge if its endpoints are in different parts. Let \(E_{\text{cut}}(P)\) be the set of cut edges for this partition. The edge cut of a partition is defined as the sum of the costs of the cut edges, and can be formalized as follows: 

\[
\text{EdgeCut}(P) = \sum_{(v_i, v_j) \in E_{\text{cut}}(P)} \text{out}_i,
\]

hence it is equal to \(|E_{\text{cut}}(P)|\) with unit weights.

Let \(V_i \subseteq V\) be a part of the DAG \((1 \leq i \leq k)\). A traversal of the part \(V_i\), denoted by \(\tau(V_i)\), is an ordered list of the vertices that respect precedence constraints within the part: if there is an edge \((v, v') \in E\), then \(v\) must appear before \(v'\) in the traversal. In the example, there is only a single possible traversal for \(V_1\): \(\tau(V_1) = [v_1, v_2, v_3, v_4]\), while there are three possibilities for \(V_2\): \([v_5, v_6, v_7]\), \([v_5, v_7, v_6]\), and \([v_7, v_5, v_6]\).

Given a part \(V_i\) and a traversal of this part \(\tau(V_i)\), we can now define the livesize of the traversal as the maximum memory usage required to execute the whole part. We define \(L(\tau(V_i))\) as the livesize computed such that inputs and outputs (of part \(V_i\)) are evicted from the cache if they are no longer required inside the part. Algorithm 1 details how the livesets are computed.

![Figure 1: DAG example.](image-url)
Cache eviction algorithm. If the livesize is greater than the cache size $C$, during execution, some data must be transferred from the cache back into slow memory. The data that will be evicted may affect the number of cache misses. Given a traversal, the optimal strategy consists in evicting the data whose next use will occur farthest in the future during execution. This strategy is called optimal replacement algorithm (OPT, clairvoyant replacement algorithm, Belady’s optimal page replacement algorithm) [2].

Hence, if a data needs to be evicted, the OPT algorithm looks at the upcoming schedule and orders the data in the cache by their next use times in ascending order. If a data is not used by any other task, it is assigned infinite value. The last data in this ordered list (the data not used or with farthest upcoming use) is then evicted from the cache. After scheduling a task, the next upcoming use of data generated by its immediate predecessors are updated.

Optimization problems. The goal is to minimize the number of loads and stores among all possible valid schedules. Formally, the MinCacheMiss problem is the following: Given a DAG $G$, a cache of size $C$, find a topological order of $G$ that minimizes the number of cache misses when using the OPT strategy.

However, finding the optimal traversal to minimize the livesize is already an NP-complete problem [11], even though it is polynomial on trees [8]. Therefore, MinCacheMiss is NP-complete (consider a problem instance where the whole DAG could be executed without any cache miss if the livesize was minimum).

Instead of looking for a global traversal of the whole graph, we propose to partition the DAG in an acyclic way. The key is, then, to have all the parts executable without cache misses, hence the only cache misses can be incurred by data on the cut between parts. Therefore, we aim at minimizing the edge cut of the partition.

Algorithm 1: Computing the livesize of a part

Data: Directed graph $G = (V, E)$, part $V_\ell \subseteq V$, traversal $\tau(V_\ell)$

Result: Livesize $L(\tau(V_\ell))$

1. $L(\tau(V_\ell)) \leftarrow 0$; current $\leftarrow 0$; $V'_\ell \leftarrow V_\ell$;

2. foreach $v_i$ in $\tau(V_\ell)$ order do

3. $V'_\ell \leftarrow V'_\ell \setminus \{v_i\}$;

4. current $\leftarrow$ current $+$ $w_i$ + $out_i$; /* Add current task to liveset */

5. $L(\tau(V_\ell)) \leftarrow \max\{L(\tau(V_i)), \text{current}\}$; /* Update $L$ if needed */

6. if $\text{succ}_i = \emptyset$ or $\forall v_j \in \text{succ}_i$, $v_j \notin V_\ell$ then

7. current $\leftarrow$ current $-$ $out_i$; /* No need to keep output in cache */

8. for $v_j \in \text{pred}_i$ do

9. if $V'_\ell \cap \text{succ}_j = \emptyset$ /* No successors of $v_j$ after $v_i$ in $\tau(V_\ell)$ */

10. then

11. current $\leftarrow$ current $-$ $w_i$; /* Task is done, no need scratch space */
3 DAG-partitioning Assisted Locality-Aware Scheduling

We propose novel DAG-partitioning-based cache optimization heuristics that can be applied on top of classical ordering approaches to improve cache locality, using a modified version of a recent directed acyclic graph partitioner [7].

Three classical approaches are considered for the traversal of the whole DAG, and they return a total order on the tasks. The traversal must respect precedence constraints, and hence a task \( v_i \in V \) is said to be ready when all its predecessors have already been executed: all predecessors must appear in the traversal before \( v_i \).

- **Natural Ordering (nat)** treats the node id’s as the priority of the node, where the lower id has a higher priority, hence the traversal is \( v_1 \rightarrow v_2 \rightarrow \cdots \rightarrow v_n \), except if node id’s do not follow precedence constraints (schedule ready task of highest priority first).
- **DFS Traversal Ordering (dfs)** follows a depth-first traversal strategy among the ready tasks.
- **BFS Traversal Ordering (bfs)** follows a breadth-first traversal strategy among the ready tasks.

When applied to the whole DAG, these three traversal algorithms are baseline algorithms, and they will serve as a basis for comparison in terms of cache miss. Also, these traversals can be applied to a part of the DAG in the DAG-partitioned approach, and also they can be extended to parts themselves: part \( V_i \) is ready if, for all \( v_i \in V_i \), if \((v_j, v_i) \in E \) and \( v_j \notin V_i \), then \( v_j \) has already been scheduled.

Furthermore, the part id is the minimum of ids of the nodes in the part. Then, considering parts as macro tasks, the same traversals can be used.

The modified acyclic DAG partitioner takes a DAG with vertex and edge weights (in this work, unit weights assumed), and a maximum livesize \( L_m \) for each part as input. Its output is a partition of the vertices of \( G \) into \( K \) nonempty pairwise disjoint and collectively exhaustive parts satisfying three conditions: (i) the livesize of the parts are smaller than \( L_m \); (ii) the edge cut is minimized; (iii) the partition is acyclic; in other words, the inter-part edges between the vertices from different parts should preserve an acyclic dependency structure among the parts. The partitioner does not take the number of parts as input, but takes a maximum livesize. That is, the partitioner continues recursive bisection until the livesize of the part at hand is less than \( L_m \), meaning that it can be loaded and completely run in the cache of size \( L_m \) without any extra load operations.

Hence, the DAGP approach (with DAG partitioner) uses multilevel recursive bisection approach, matching (coarsening) methods, and refinement methods that are specialized to create acyclic partitions. The refinement methods are modified versions of Fiduccia-Mattheyses’ move-based refinement algorithm. The partitioning algorithm starts by computing the livesize of the graph. If computed livesize is less than \( L_m \), then it stops and leaves everything in the same part. Otherwise, the graph is partitioned into two subgraphs with the edge cut minimization goal. The same procedure is repeated for the two subgraphs until each part has a livesize smaller than \( L_m \). The partitioner also duplicates the
boundary nodes of predecessor parts to successor parts, so as to account for the input data (caching) requirement of the tasks from predecessor parts.

Given $K$ parts $V_1, \ldots, V_K$ forming a partition of the DAG, we consider three variants of $\text{dagP}$ ($\text{dagP-nat}$, $\text{dagP-dfs}$, and $\text{dagP-bfs}$), building upon the traversals described above. Due to page limits, we always use the same algorithm for parts and for tasks within parts, but any combination would be possible (e.g., order parts with $\text{nat}$, and then tasks within parts with $\text{dfs}$).

## 4 Experimental Evaluation

Experiments were conducted on a computer equipped with dual 2.1 GHz Xeon E5-2683 processors and 512 GB memory. We have performed an extensive evaluation of the proposed heuristics on DAG instances obtained from the matrices available in the SuiteSparse Matrix Collection (formerly known as the University of Florida Sparse Matrix Collection) [3]. From this collection, we picked 15 matrices satisfying the following properties: listed as binary, square, and has at least 100000 rows and at most $2^{26}$ nonzeros. All edges have unit costs, and all vertices have unit weights. For each such matrix, we took the strict upper triangular part as the associated DAG instance whenever this part has more nonzeros than the lower triangular part; otherwise, we took the lower triangular part. The graphs and their characteristics are listed in Table 1. We execute each graph with the natural, DFS, and BFS traversal, and report the corresponding livesize (computed with Algorithm 1).

Note that when reporting the cache miss counts, we do not include compulsory (cold, first reference) misses, the misses that occur at the first reference to a memory block, as these misses cannot be avoided.

| Graph         | $|V|$   | $|E|$   | $\max_{\text{in.deg}}$ | $\max_{\text{out.deg}}$ | $L_{\text{nat}}$ | $L_{\text{dfs}}$ | $L_{\text{bfs}}$ |
|---------------|-------|--------|------------------------|------------------------|----------------|----------------|----------------|
| 144           | 144,649 | 1,074,393 | 21                     | 22                     | 74,689          | 31,293          | 29,333         |
| 598a          | 110,971 | 741,934  | 18                     | 22                     | 81,801          | 41,304          | 26,250         |
| caidaRouterLev. | 192,244 | 609,066  | 321                    | 1040                   | 56,197          | 34,007          | 35,935         |
| coAuthorsCites. | 227,320 | 814,134  | 95                     | 1367                   | 34,587          | 26,308          | 27,415         |
| delaunay-n17  | 131,072 | 393,176  | 12                     | 14                     | 32,752          | 39,839          | 52,882         |
| email-EuAll    | 265,214 | 305,539  | 7,630                  | 478                    | 196,072         | 177,720         | 205,826        |
| fe-ocean       | 143,437 | 409,593  | 4                      | 4                      | 8,322           | 7,099           | 3,716          |
| ford2          | 100,196 | 222,246  | 29                     | 27                     | 26,153          | 4,468           | 25,001         |
| halfb          | 224,617 | 6,081,602 | 89                    | 119                    | 66,973          | 25,371          | 38,743         |
| luxembourg-osm | 114,599 | 119,666  | 4                      | 5                      | 4,686           | 2,768           | 6,544          |
| rgg-n-2-17-s0  | 131,072 | 728,753  | 18                     | 19                     | 759             | 1,484           | 1,544          |
| usroads        | 129,164 | 165,435  | 4                      | 5                      | 297             | 8,024           | 9,789          |
| vsp-finan512.  | 139,752 | 552,020  | 119                    | 666                    | 25,830          | 24,714          | 38,647         |
| vsp-mod2-pgp2.  | 101,364 | 389,368  | 949                    | 1726                   | 41,191          | 36,902          | 36,672         |
| wave           | 156,317 | 1,059,331 | 41                    | 38                     | 13,988          | 22,546          | 19,875         |

Table 1: Graph instances from [3] and their livesizes.
We start by comparing the average performance of the three baseline traversal algorithms on varying cache sizes. Figure 2 shows the geometric mean of cache miss counts, normalized by the number of nodes, with cache size ranging from 512 to 10240 words. In smaller cache sizes, the natural ordering of the nodes provides the best results on average. As the cache size increases, DFS traversal surpasses the others and becomes the best option starting at 3072.

**Effect of Cache Size on Reported Relative Cache Miss.** Figure 3 shows the improvement of our algorithms over their respective baselines, averaged over 50 runs. The left figure shows the relative cache miss on a cache $C = 512$ and the right one on $C = 10240$, with $L_m = C$ (i.e., the partitioner stops when the livesize of each part fits in cache). A relative cache miss of 1 means that we get the same number of cache misses as without partitioning; the proposed solution is better than the baseline for a value lower than 1 (0 means that we reduced the cache misses to 0), and it is worsened in a few cases (i.e., values greater than 1).

One important takeaway from this figure is that as the cache increases, the input graph’s livesize may become less than the cache size (e.g., `fe-ocean`, `luxembourg-osm`, `rgg-n-2-17-s0`, and `usroads` graphs have smaller livesize than the cache size), meaning that there is no cache miss even without partitioning. Thus, the partitioning phase does not need to divide the graph at all and just returns the initial graph.

Finally, the variance from one run to another is relatively low, demonstrating the stability of the algorithm, hence we perform the average over only 10 runs in the remaining experiments.

**Effect of $L_m$ and $C$ on Cache Miss Improvement and Edge Cut.** Figure 4 shows the normalized cache misses when the execution strategy of the graph is `nat`, `dfs`, and `bfs` traversal respectively. We compare the number of cache misses when traversing the input graph with the three partitioning based-heuristics. We use five different values for the $L_m$ parameter of the algorithms: $L_m = \{2C, C, 0.5C, 0.25C, 0.125C\}$ (i.e., from twice the size of cache to down to one eighth of the cache size), and compare the results. Each bar in the chart shows the respective relative cache miss of partitioning-assisted ordering compared to the baseline. Throughout all the bars in all the charts, we can see

![Figure 2: Geometric mean of cache misses using nat, dfs, and bfs traversals.](image-url)
\[ L_m \leq C \] gives better results. This is expected since the partitioning phase is trying to decrease the livesize, which in turn, decreases the upper bound of cache misses, since the whole part can be executed without cache misses if \( L_m \leq C \). Otherwise, for each part, we might still have cache misses.

There are two reasons why the partitioning result is not an exact cache miss count but an upper bound. First, the edge cut counts the edges more than once when a node \( u \) from part \( V_i \) is predecessor for multiple nodes in \( V_j \). In cache, however, after node \( u \) is loaded for one of its successors in \( V_j \), ideally, it is not removed before its other successors are also scheduled (\( L_m \leq C \) guarantees all the nodes in part \( V_j \) can be computed without needing to remove node \( u \) from cache). The second reason is that right after a part is completely scheduled, the partitioner does not take into account the fact that the last tasks (nodes) scheduled from the previous part are still in the cache.

On average, continuing the partitioning after \( L_m = C \) usually improves the performance. However, the improvement as \( L_m \) decreases and the increase in the complexity/runtime of the partitioning is a tradeoff decision.

Comparing the plots of the natural ordering, dfs traversal, and bfs traversal, one can argue that the improvement over dfs ordering is not as high as natural, or bfs ordering. This can be explained by relating to the Figure 2, which shows the average cache miss counts for the baseline algorithms. It is obvious that,
on average, dfs traversal gives much better results compared to the other two. Thus, 
\textit{dagP-DFS} variation has less room to improve over this baseline.

Another general trend is that as the cache size increases, the performance
improvements slightly decrease. This can also be explained by the phenomenon
shown in Figure 3. That is, as the cache size increases, some of the graphs do not
have any cache misses, therefore, the partitioning, cannot improve over zero cache
misses (relative cache miss is equal to 1), decreasing the overall performance
improvement of the heuristics.

When we look at the values in the figure, we see that average relative cache
miss for \( L_m = 0.5 \times C \), is in the range \( 10x \) to \( 100x \) better than the baseline. In
addition, relative cache miss of \textit{dagP-BFS} goes lower than \( 3 \cdot 10^{-3} = 0.003 \) for \( C = 6144 \) and \( L_m = 0.25C \), which is nearly \( 400x \) better than the baseline.

**Overall Comparison of Heuristics.** Figure 5 (left) shows the performance
profile for the three baseline algorithms and heuristics applied versions. A per-
formance profile shows ratio of the instances in which an algorithm obtains a
cache miss count on an instance that is no larger than \( \theta \) times the best cache
miss count found by any algorithm for that instance [4].

Here, we compare the heuristics using \( L_m = 0.5 \times C \), since it constantly
provides better results than \( L_m = C \) and increase in the partitioning overhead
is minimal. We can see that \textit{dagP-DFS} gives the best ordering approximately
75\% of the time; and 90\% of the time, it gives cache misses no worse than
1.5 times the best heuristic. We can also see that all three proposed heuristics
perform better over their respective baselines. Also, all three heuristics perform
better than any of the baselines.

Finally, the runtime averages, including all graphs in the dataset for the
given parameter configurations, are depicted in Figure 5 (right). The black error
bars show the minimum and maximum run times for that bar. It is clear that
for smaller \( L_m \) values, the partitioner needs to do more work, but partitioner
is fast and does not take more than 10 seconds in most common cases (i.e.,
\( L_m = 0.5 \times C \)).

![Figure 5](image_url)

**Figure 5:** (Left) Performance profile comparing baselines and heuristics with
\( L_m = 0.5 \times C \). (Right) Average runtime of all graphs for \textit{dagP-DFS} partitioning.
5 Conclusion and Future Work

As the cost of data movement through the memory hierarchy dominates the cost of computational operations in today’s computer systems, data locality is a significant research focus. Although there have been many approaches to improve data locality of applications, to the best of our knowledge, there is no work that employs a DAG-partitioning assisted approach. Building upon such a partitioner, we design locality-aware scheduling strategies, and evaluate the proposed algorithms extensively on a graph dataset from various areas and applications, demonstrating that we can significantly reduce the number of cache misses. As the next step, it would be interesting to study the effect of a customized DAG-partitioner specifically for cache optimization purposes, and also to design traversal algorithms to optimize cache misses. It would also be interesting to use a better fitting hypergraph representation for the model.

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