

Bruno Cessac, Selma Souihel, Matteo Di Volo, Frédéric Chavane, Alain Destexhe, Sandrine Chemla, Olivier Marre

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Bruno Cessac, Selma Souihel
Biovision







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In collaboration with:

Matteo Di Volo Alain Destexhe

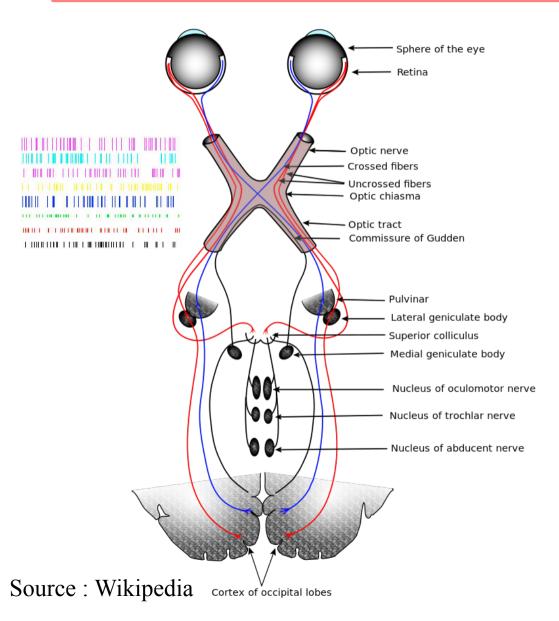


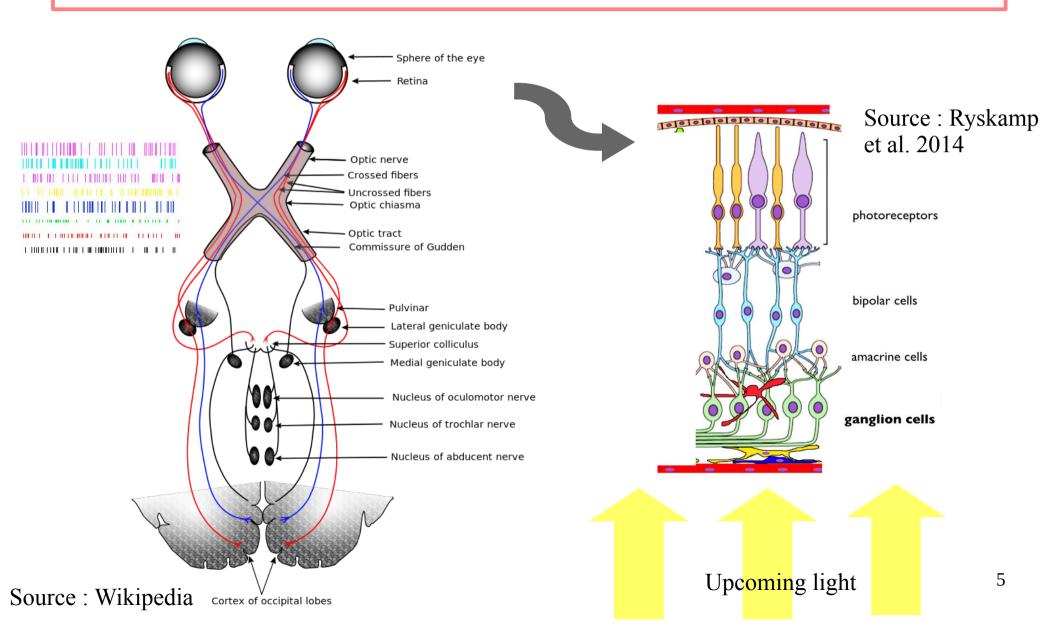
Frédéric Chavane Sandrine Chemla

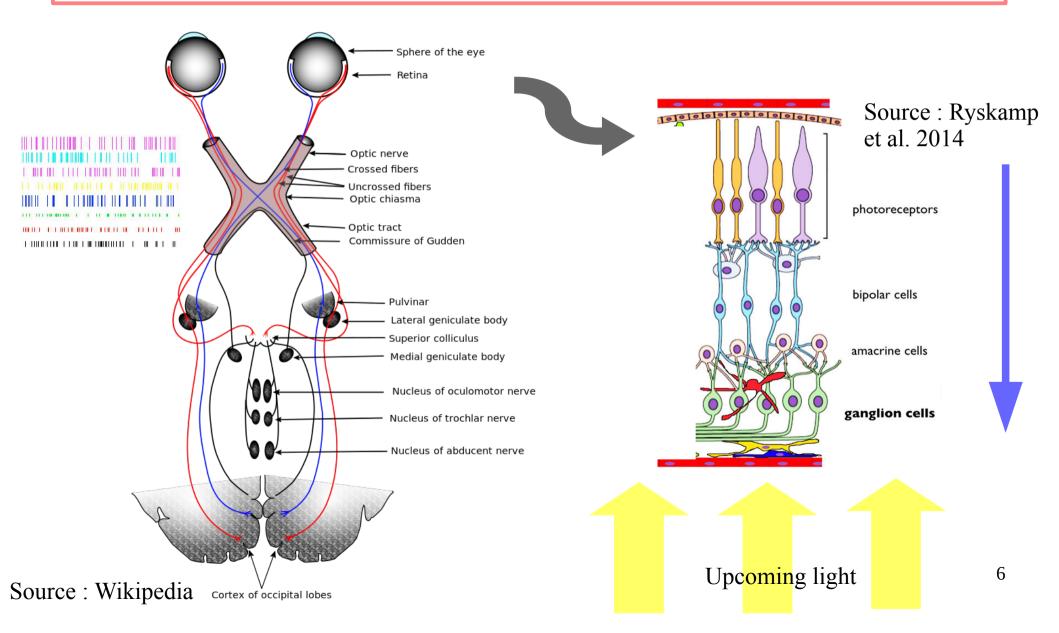


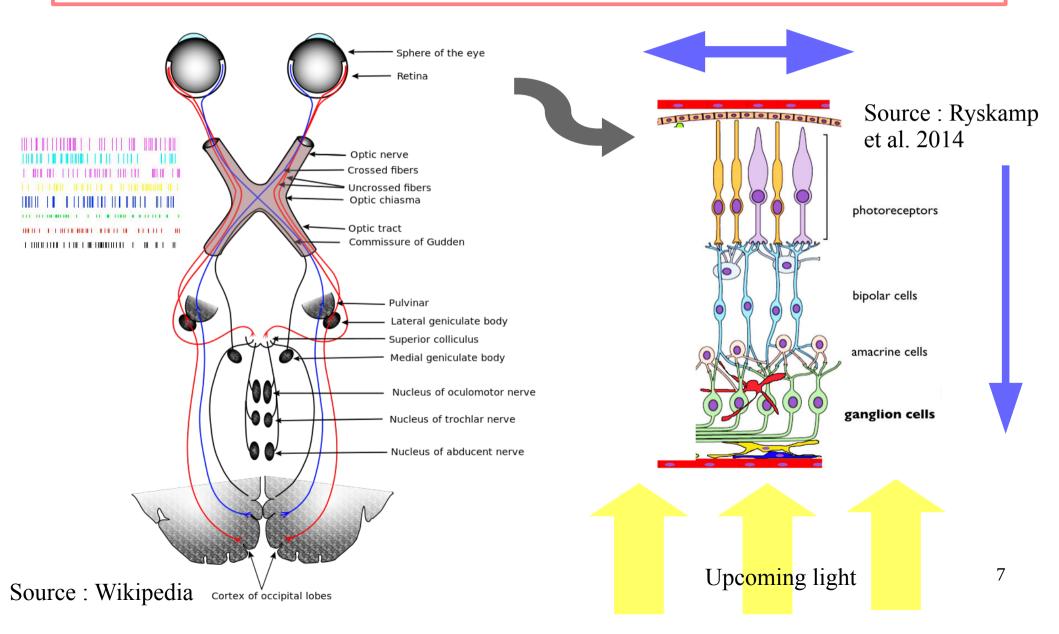
Olivier Marre

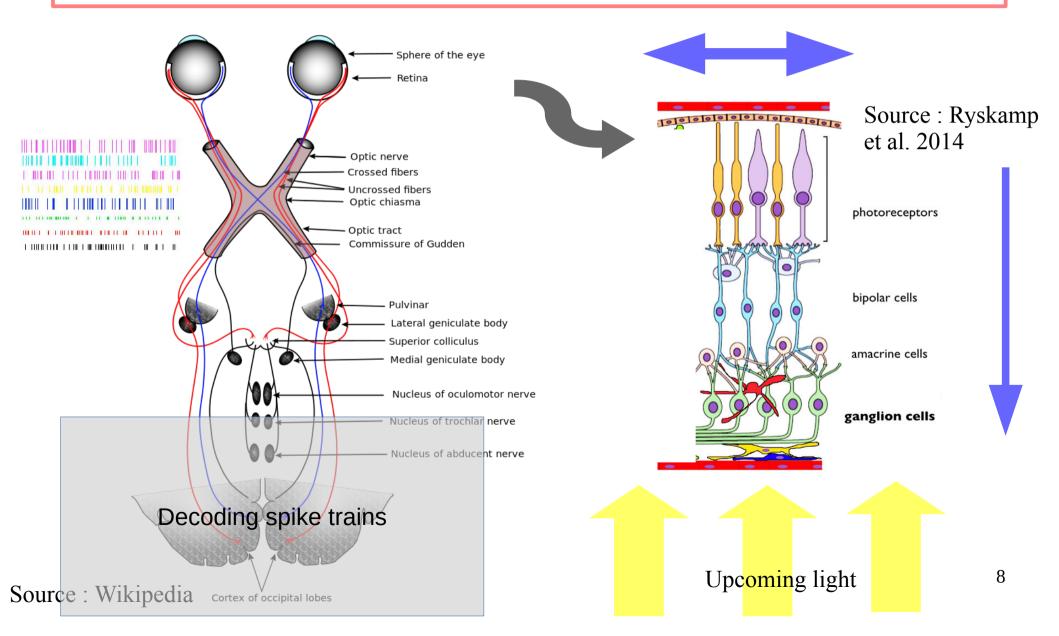


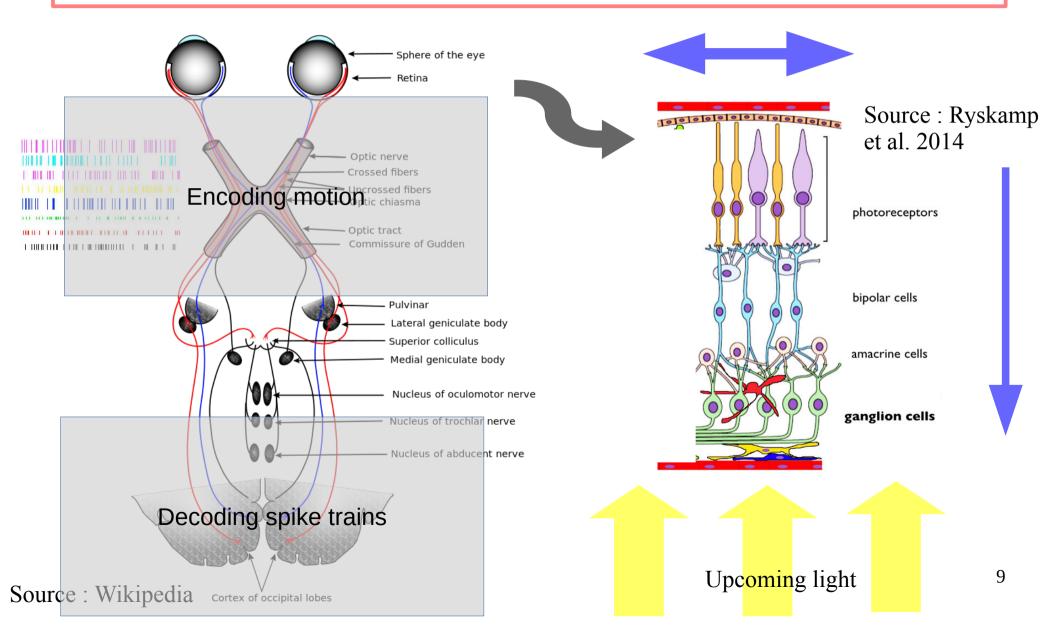


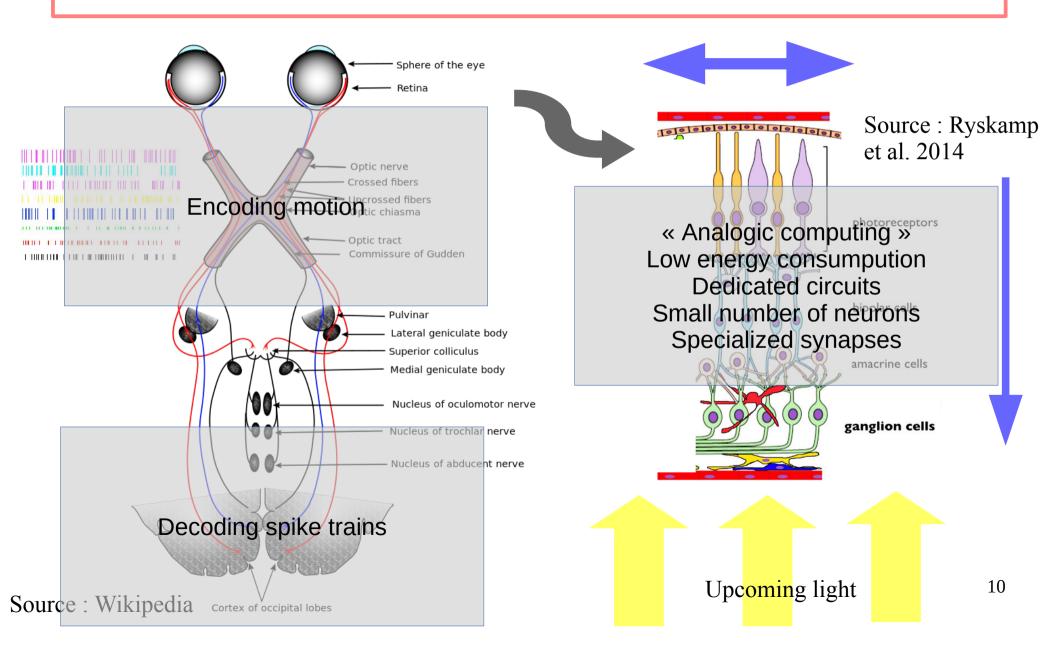


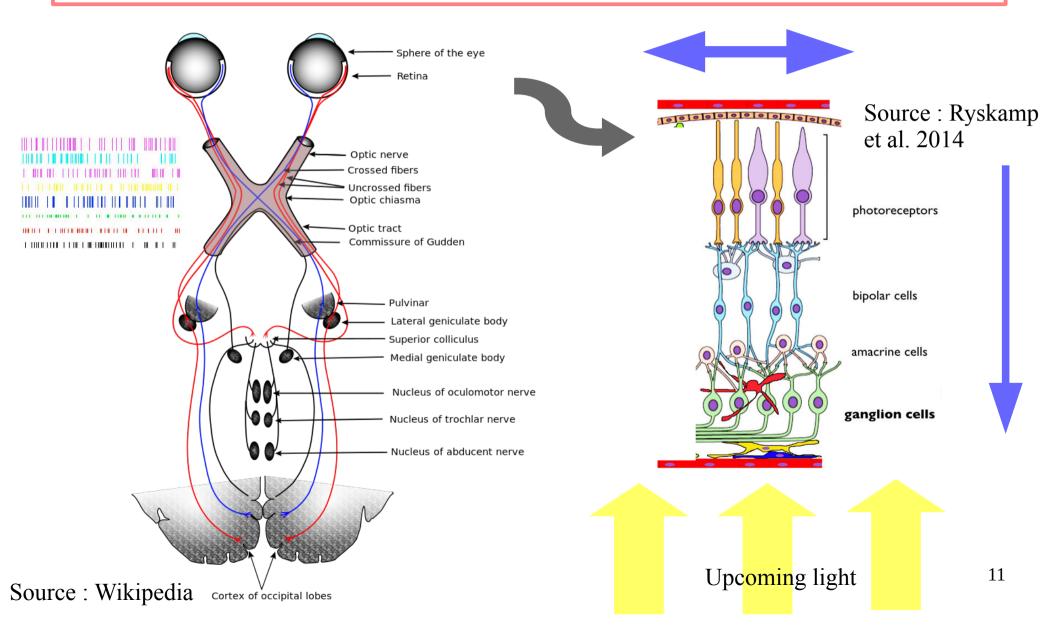


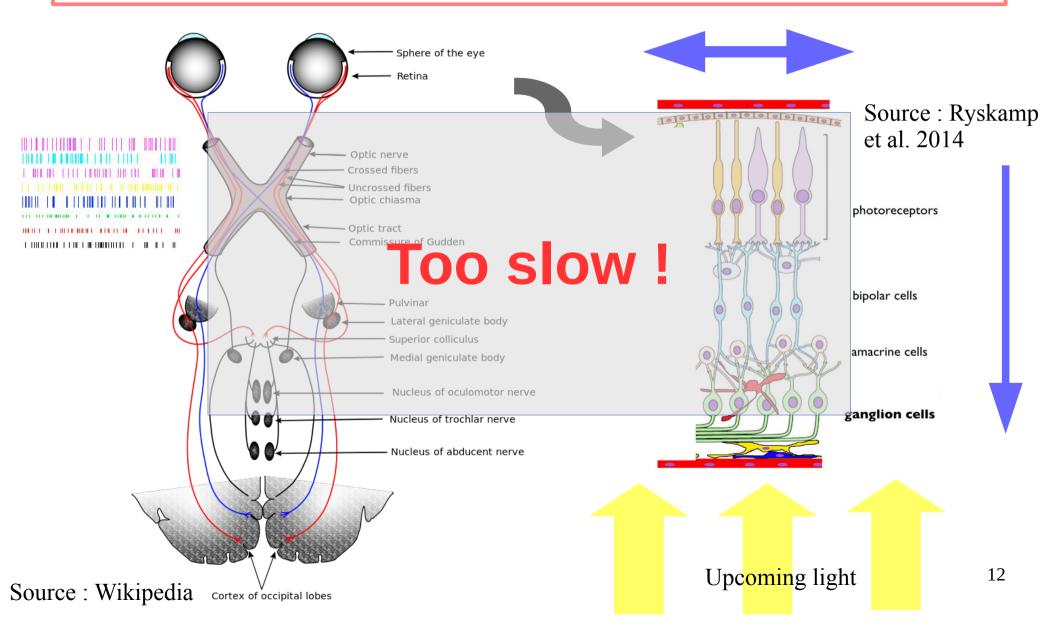


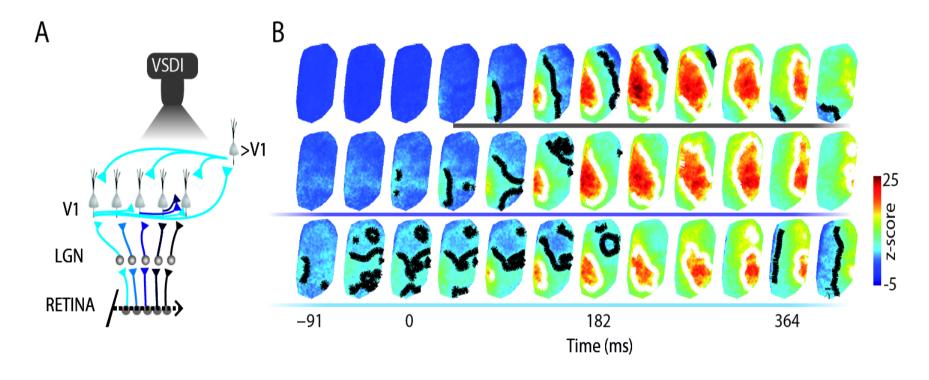






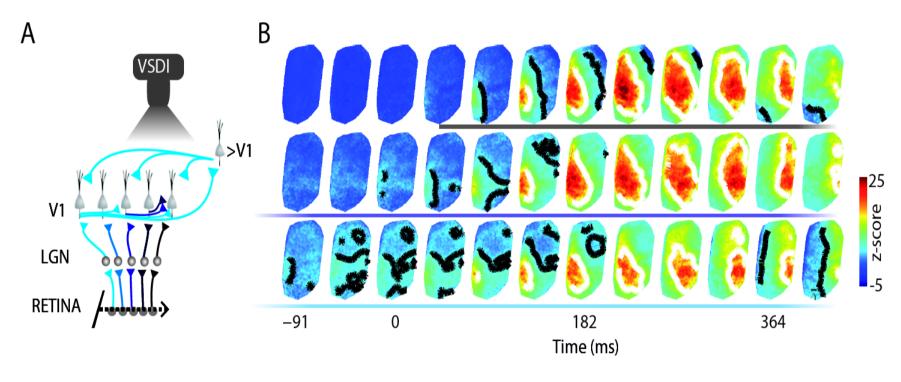






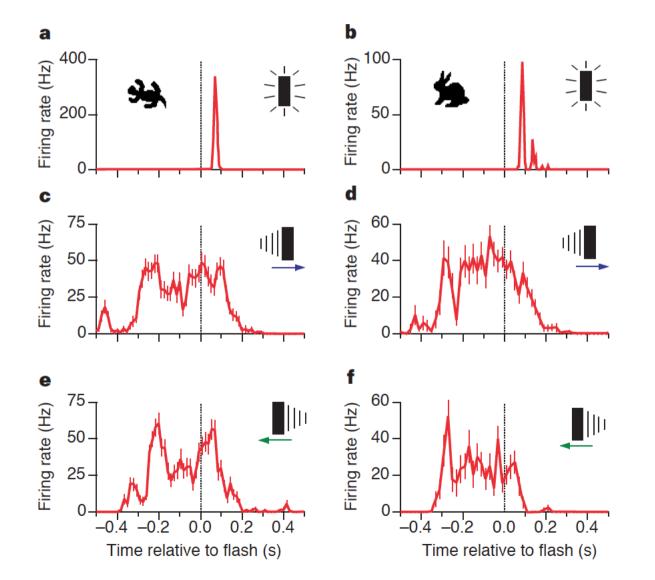
Source: Benvenutti et al. 2015

Anticipation is carried out by the primary visual cortex (V1) through an activation wave



Source: Benvenutti et al. 2015

#### Anticipation also takes place in the retina



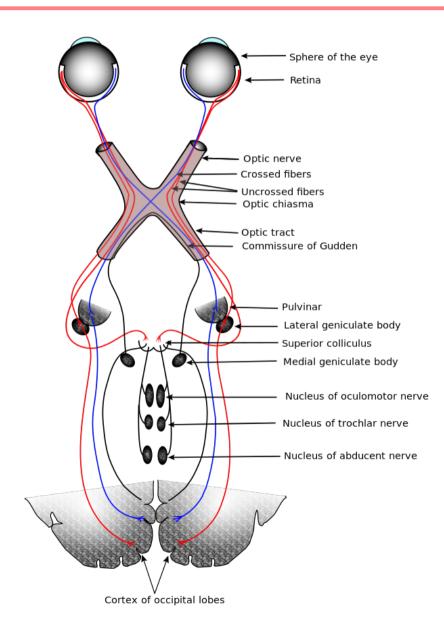
Source: Berry et al. 1999

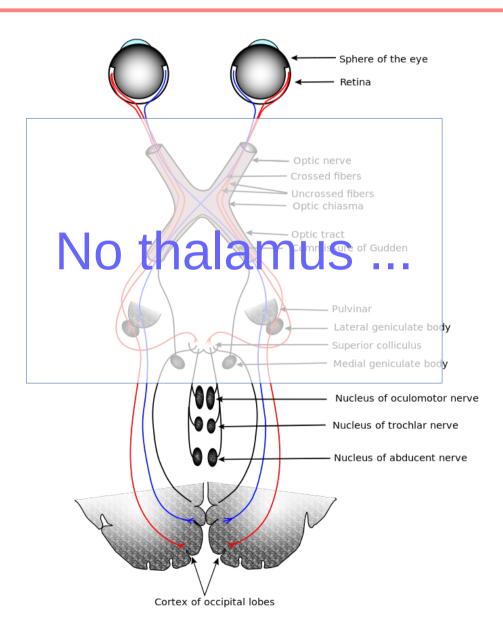


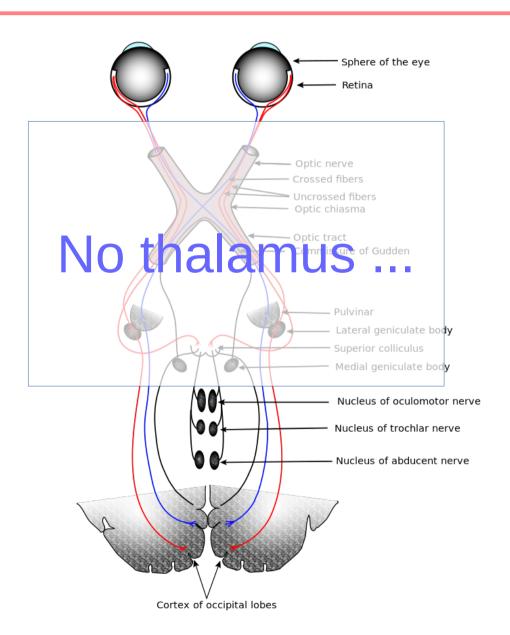
### **Trajectory**

#### What are the respective:

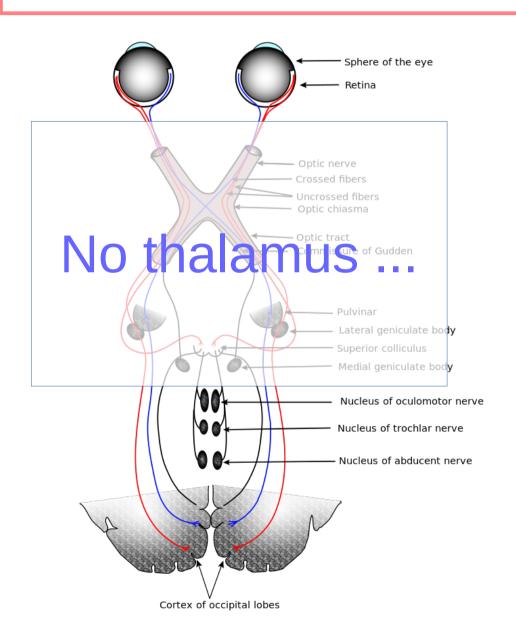
- >Mechanisms underlying retinal and cortical anticipation?
- ➤ Role of each part?





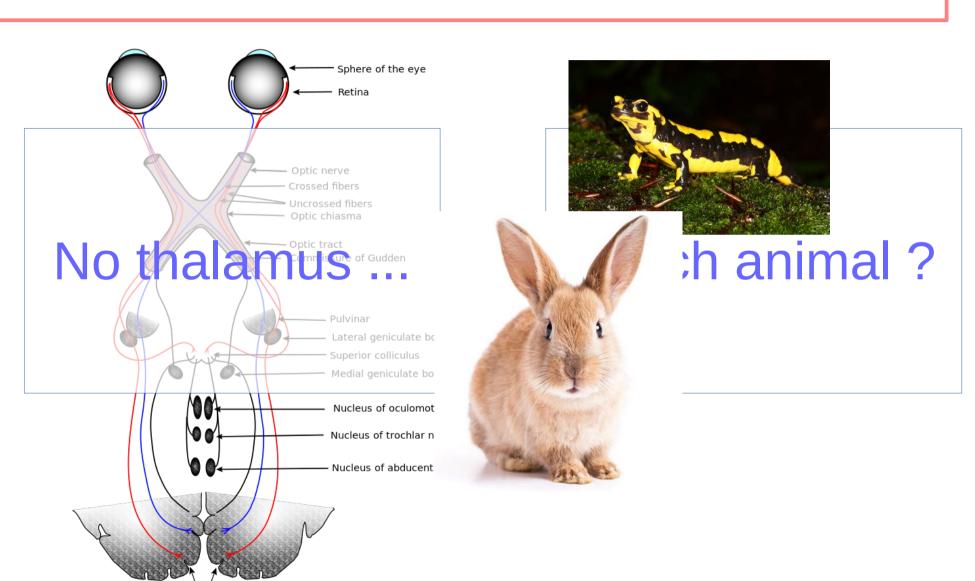


Which animal?

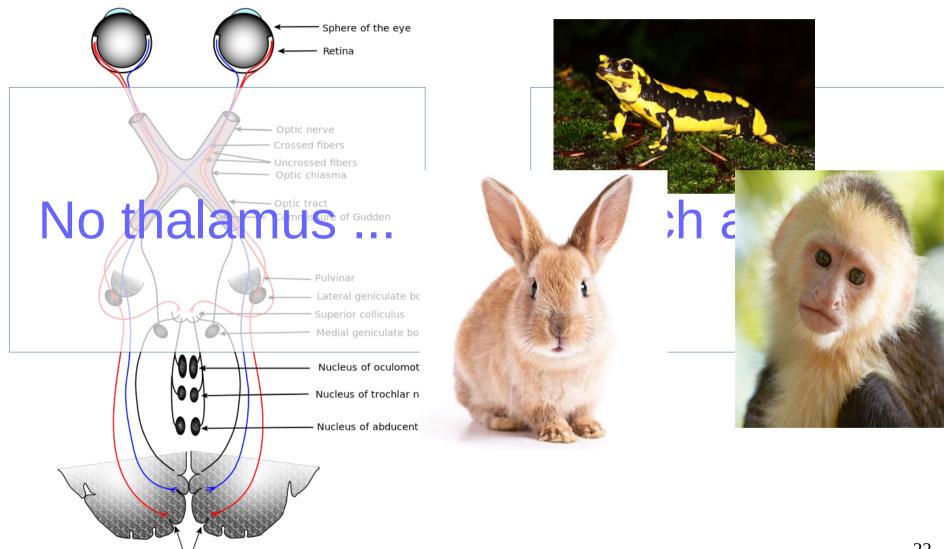




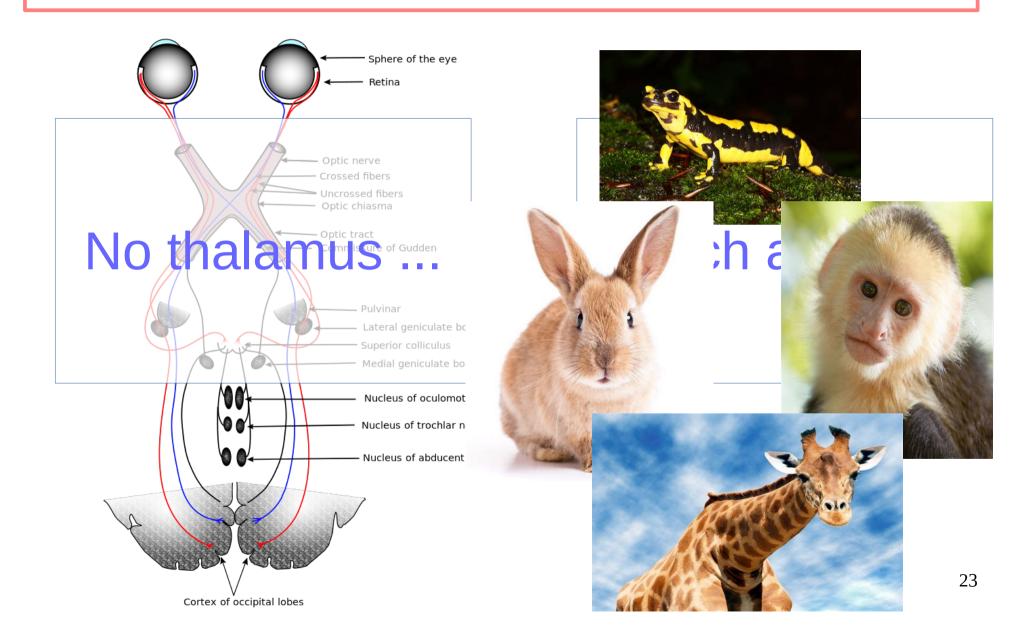
Which animal?

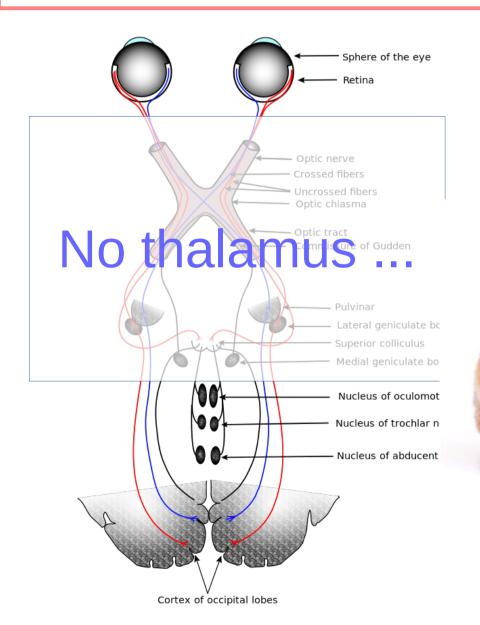


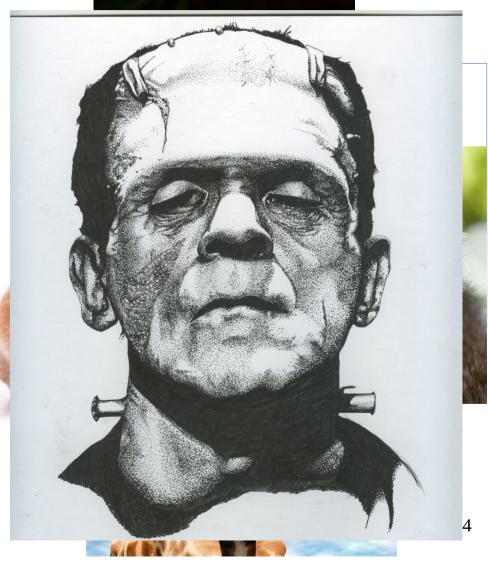
Cortex of occipital lobes



Cortex of occipital lobes







Developping a retino-cortical model of anticipation so as to

understand / propose

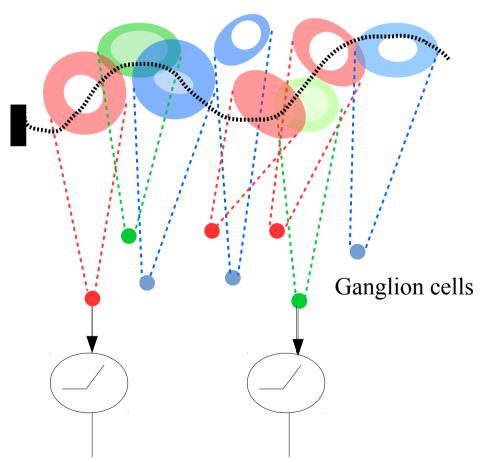
possible mechanisms for anticipation in the retina and in the cortex.

### Anticipation in the retina

#### The Hubel-Wiesel view of vision

Nobel prize 1981

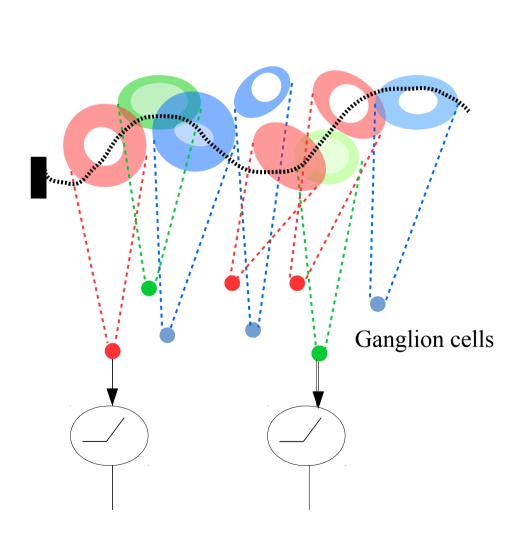
Ganglion cells response is the convolution of the stimulus with a spatio-temporal receptive field followed by a non linearity

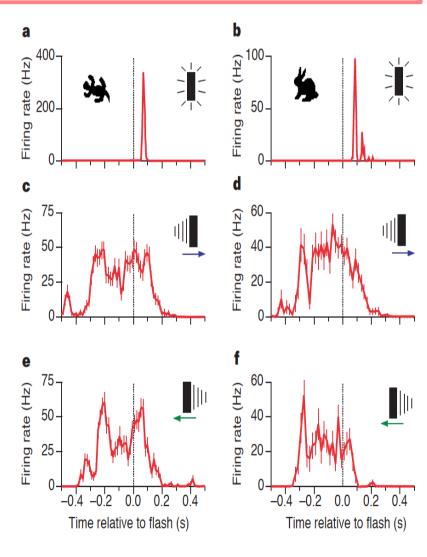


Ganglion cells are independent encoders

#### The Hubel-Wiesel view of vision

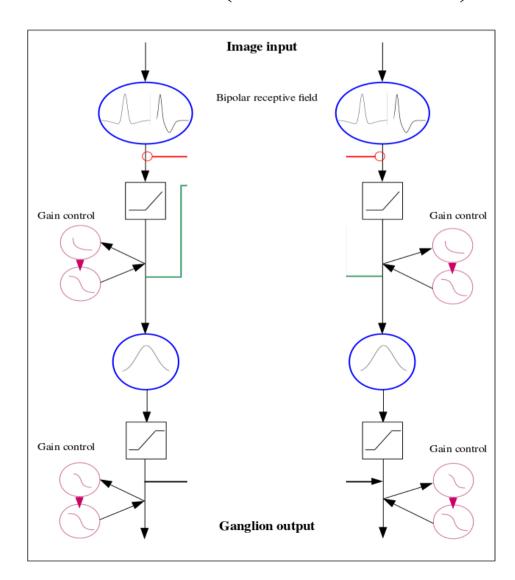
Nobel prize 1981





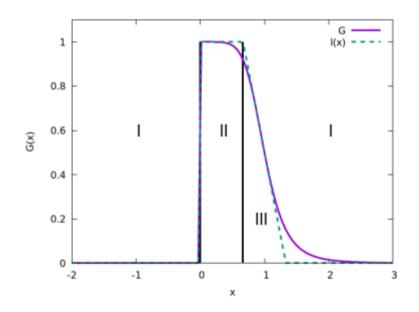
Source: Berry et al. 1999

#### Gain control (Chen et al. 2013)

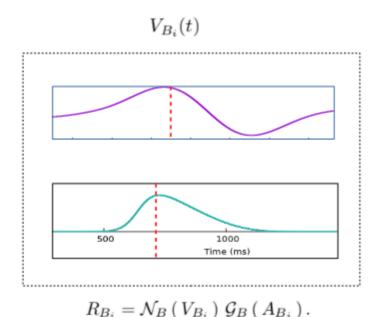


#### 1) Gain control

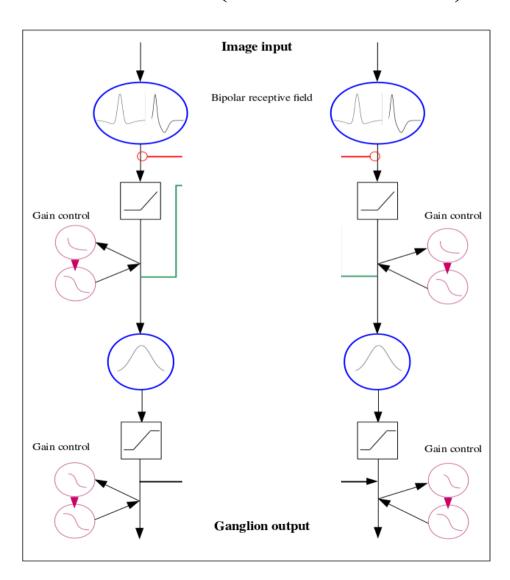
How does it work?



$$\mathcal{G}_B(A) = \begin{cases} 0, & \text{if } A \le 0; \\ \frac{1}{1+A^6}, & \text{else.} \end{cases}$$



#### Gain control (Chen et al. 2013)



• Bipolar voltage:

$$V_{B_i}(t) = V_{i_{drive}}(t)$$
.

• Non-linear function:

$$\mathcal{N}_B(V_{B_i}) = \begin{cases} 0, & \text{if } V_{B_i} \leq \theta_B; \\ V_{B_i} - \theta_B, & \text{else.} \end{cases}$$

• Activation function:

$$\frac{dA_{B_i}}{dt} = -\frac{A_{B_i}}{\tau_a} + h \mathcal{N}(V_{B_i}(t)).$$

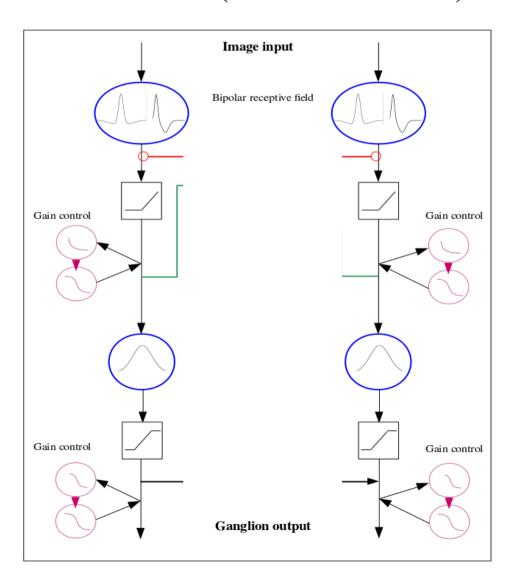
• Gain Control function:

$$\mathcal{G}_B(A) = \begin{cases} 0, & \text{if } A \le 0; \\ \frac{1}{1+A^6}, & \text{else.} \end{cases}$$

Output :

$$R_{B_i} = \mathcal{N}_B(V_{B_i}) \mathcal{G}_B(A_{B_i}).$$

#### Gain control (Chen et al. 2013)



Ganglion voltage

$$V_{G_k} = \sum_{i} W_{G_k}^{B_i} R_{B_i}$$

Non-linear function :

$$\mathcal{N}_{G_F}\left(V\right) = \left\{ \begin{array}{ll} 0, & \text{if} \quad V \leq 0; \\ \alpha_{G_F}(V - \theta_{G_F}), & \text{if} \quad \theta_{G_F} \leq V \leq N_{G_F}^{max}/\alpha_{G_F} + \theta_{G_F} \\ N_{G_F}^{max}, & \text{else.} \end{array} \right.$$

• Activation function :

$$\frac{dA_{G_{F_{k_F}}}}{dt} = -\frac{A_{G_{F_{k_F}}}}{\tau_{G_F}} + h_{G_F} \mathcal{N}_{G_F} \left( V_{G_{F_{k_F}}} \right)$$

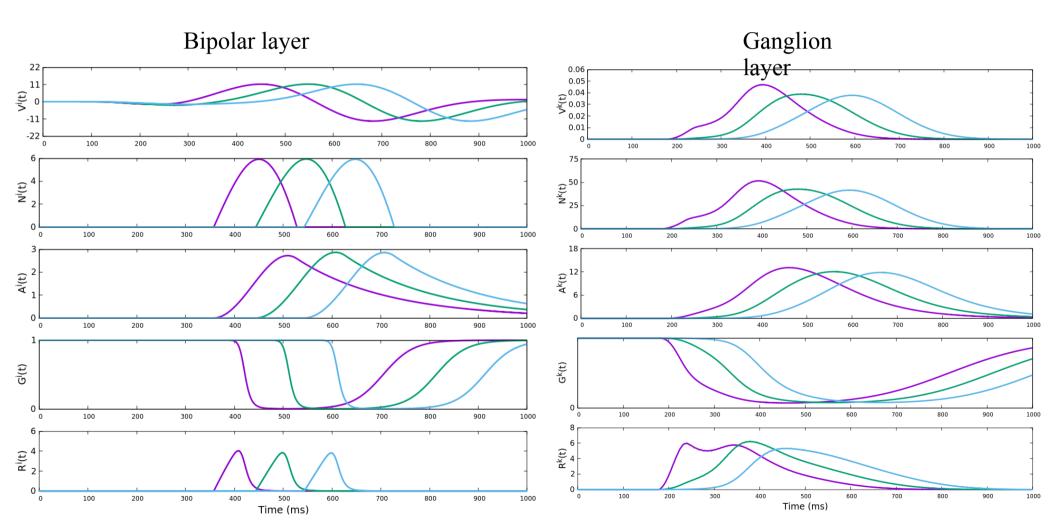
Gain Control function :

$$\mathcal{G}_{G_F}(A) = \begin{cases} 0, & \text{if } A \leq 0; \\ \frac{1}{1+A}, & \text{else.} \end{cases}$$

• Output:

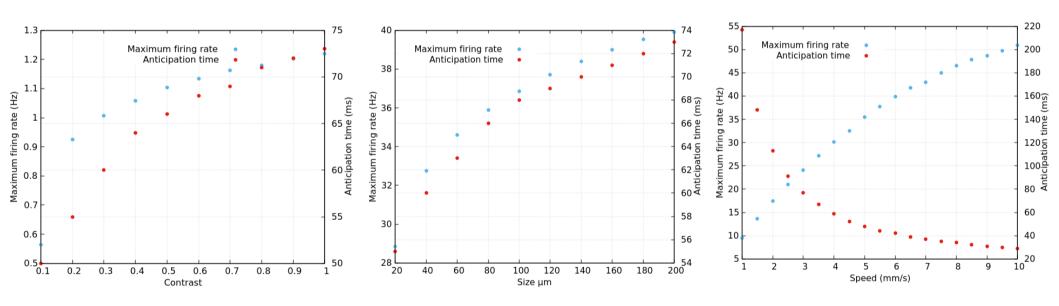
$$R_{G_{F_{k_F}}}\left(V_{G_{F_{k_F}}}, A_{G_{F_{k_F}}}\right) = \mathcal{N}_{G_F}(V_{G_{F_{k_F}}}) \mathcal{G}_{G_F}(A_{G_{F_{k_F}}}).$$

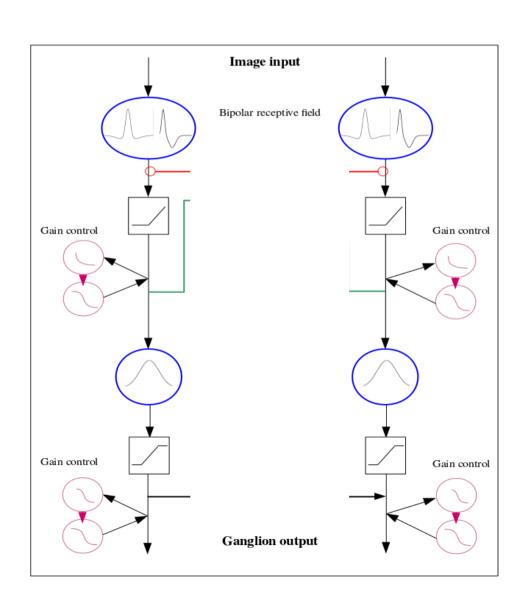
## 1D results: smooth motion anticipation with gain control



## 1D results: smooth motion anticipation with gain control

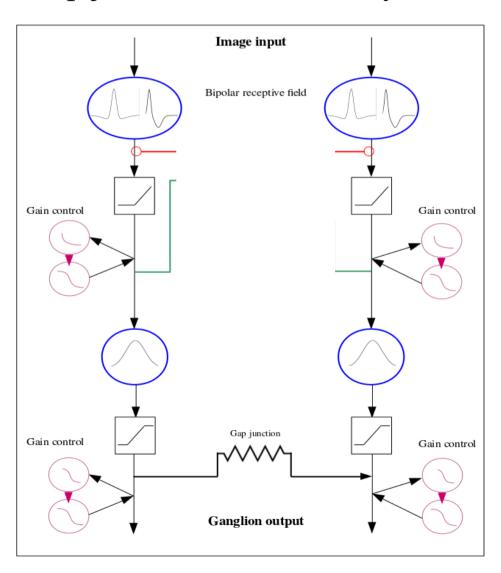
Anticipation variability with stimulus parameters





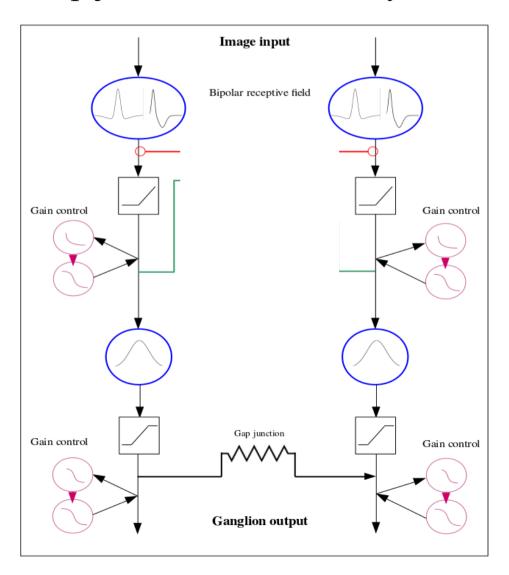
Ganglion cells are independent encoders

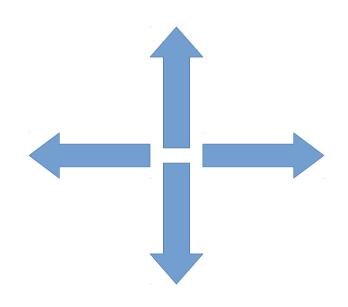
#### Gap junctions connectivity



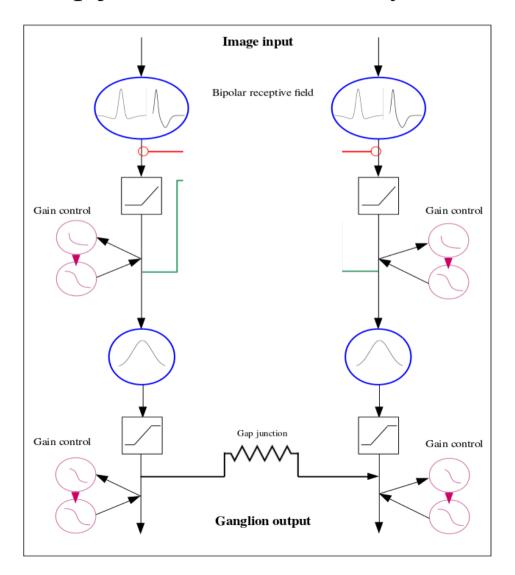
Ganglion cells are **not** independent encoders

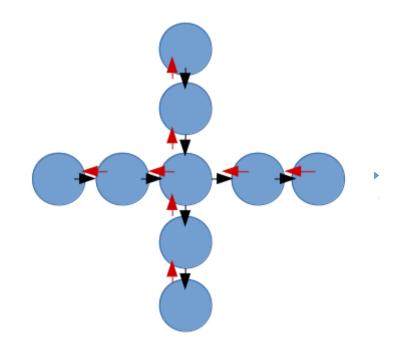
#### Gap junctions connectivity



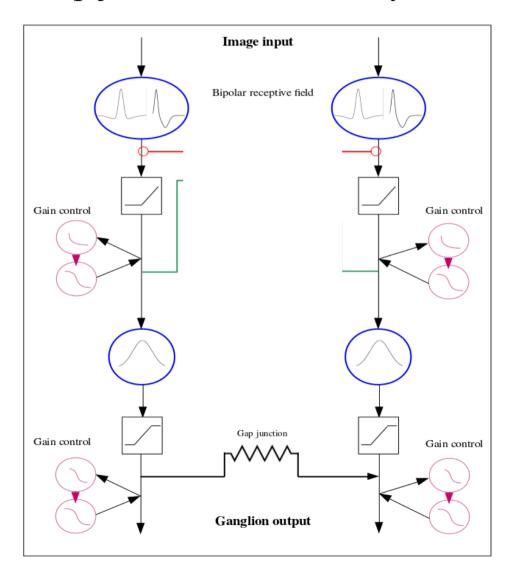


#### Gap junctions connectivity

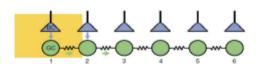




#### Gap junctions connectivity

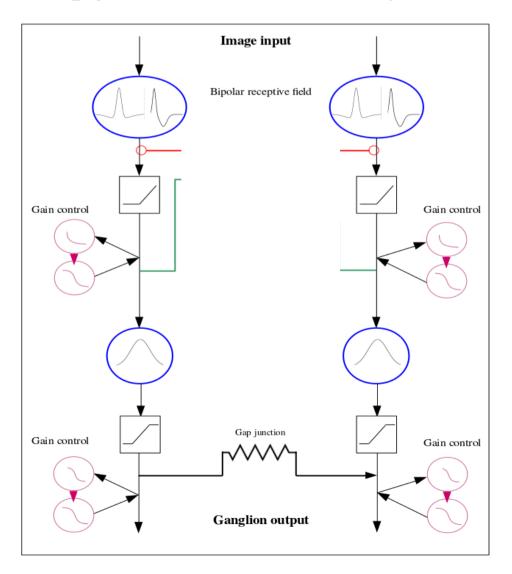


- A class of direction selective RGCs are connected through gap junctions
- Their activity comprises the activity pooled from bipolar cells and the activity coming from the downstream RGCs, in the direction of motion



$$R_{G_{D k_D}} = V_{G_{D k_D}} + \beta R_{G_{D k_D-1}}$$

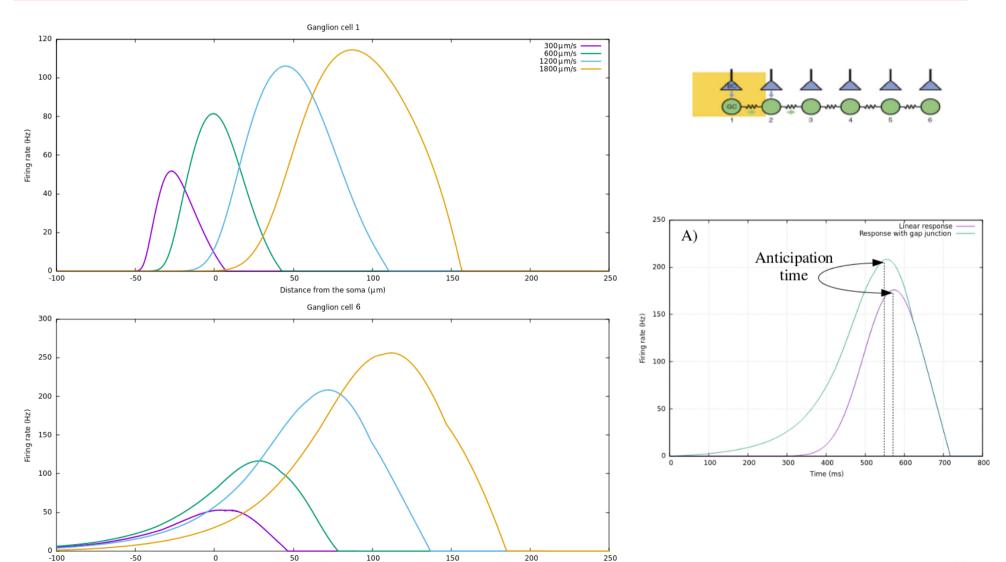
#### Gap junctions connectivity



- A class of direction selective RGCs are connected through gap junctions
- Their activity comprises the activity pooled from bipolar cells and the activity coming from the downstream RGCs, in the direction of motion

Diffusive wave of activity ahead of the motion  $R_{G_{Dk_D}} = V_{G_{Dk_D}} + \beta R_{G_{Dk_D-1}}$ 

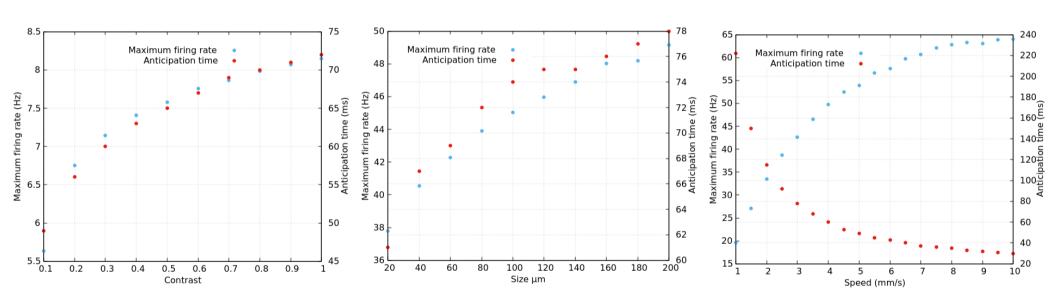
# 1D results: smooth motion anticipation with gap junctions

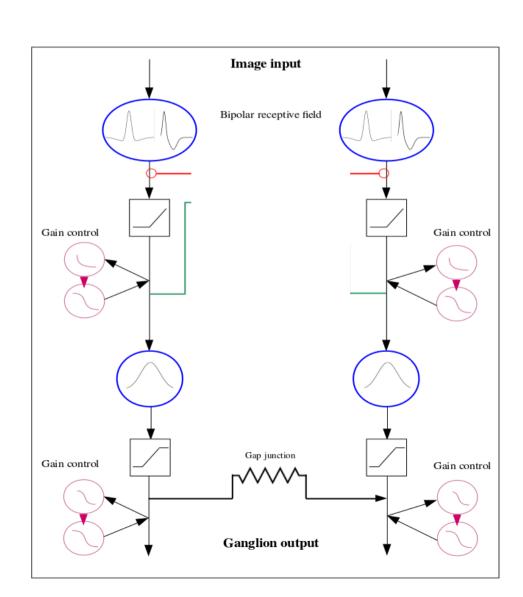


Distance from the soma (µm)

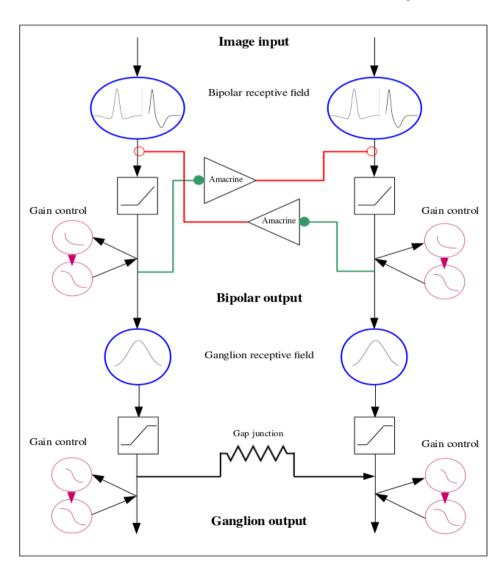
# 1D results: smooth motion anticipation with gap junctions

Anticipation variability with stimulus parameters





#### Amacrine cells connectivity



Ganglion cells are **not** independent encoders

#### Amacrine cells connectivity

• A class of RGCs are selective to differential motion



#### Amacrine cells connectivity

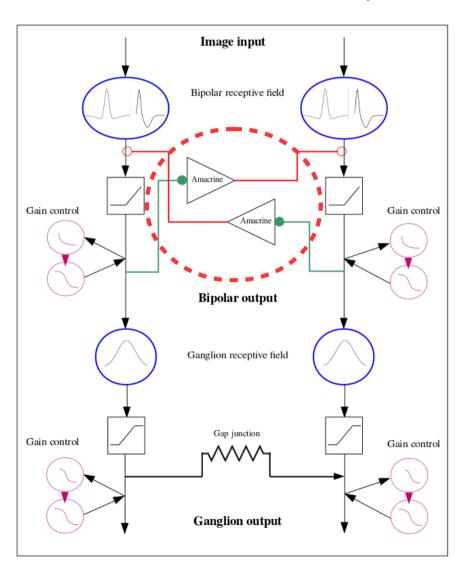
• A class of RGCs are selective to differential motion



• The circuitry involves amacrine cells connectivity upstream of ganglion cells

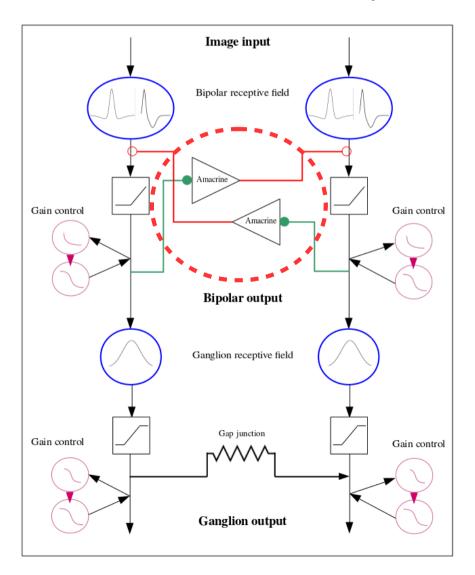
### Connectivity pathways

#### Amacrine cells connectivity



### Connectivity pathways

#### Amacrine cells connectivity



• Bipolar voltage:

$$\frac{dV_{B_i}}{dt} = -\frac{1}{\tau_B} V_{B_i} + \sum_{j=1}^{N_A} W_{B_i}^{A_j} V_{A_j} + F_{B_i}(t).$$

• External drive:

$$F_{B_i}(t) = \left[ K_i \stackrel{S,t}{*} \left( \frac{S}{\tau_B} + \frac{dS}{dt} \right) \right] (t)$$

• Amacrine voltage:

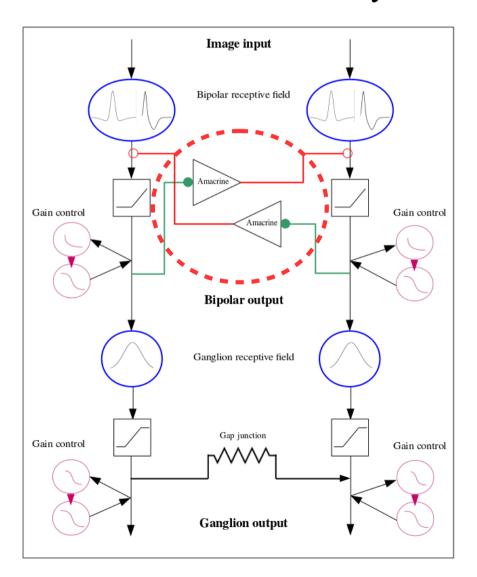
$$\frac{dV_{A_j}}{dt} = -\frac{1}{\tau_A} V_{A_j}(t) + \sum_{i=1}^{N_A} W_{A_j}^{B_i} R_{B_i}(t).$$

Coupled dynamics :

$$\begin{cases} \frac{dV_{B_i}}{dt} &= -\frac{1}{\tau_B} V_{B_i} + \sum_{j=1}^{N_A} W_{B_i}^{A_j} V_{A_j} + F_{B_i}(t) \\ \frac{dA_{B_i}}{dt} &= -\frac{A_{B_i}}{\tau_a} + h \mathcal{N}(V_{B_i}(t)), \\ \frac{dV_{A_j}}{dt} &= -\frac{1}{\tau_A} V_{A_j}(t) + \sum_{i=1}^{N_A} W_{A_j}^{B_i} R_{B_i}(t). \end{cases}$$

### Connectivity pathways

#### Amacrine cells connectivity



• Bipolar voltage:

$$\frac{dV_{B_i}}{dt} = -\frac{1}{\tau_B} V_{B_i} + \sum_{j=1}^{N_A} W_{B_i}^{A_j} V_{A_j} + F_{B_i}(t).$$

• External drive:

$$F_{B_i}(t) = \left[ K_i * \left( \frac{\mathcal{S}}{\tau_B} + \frac{d\mathcal{S}}{dt} \right) \right](t)$$

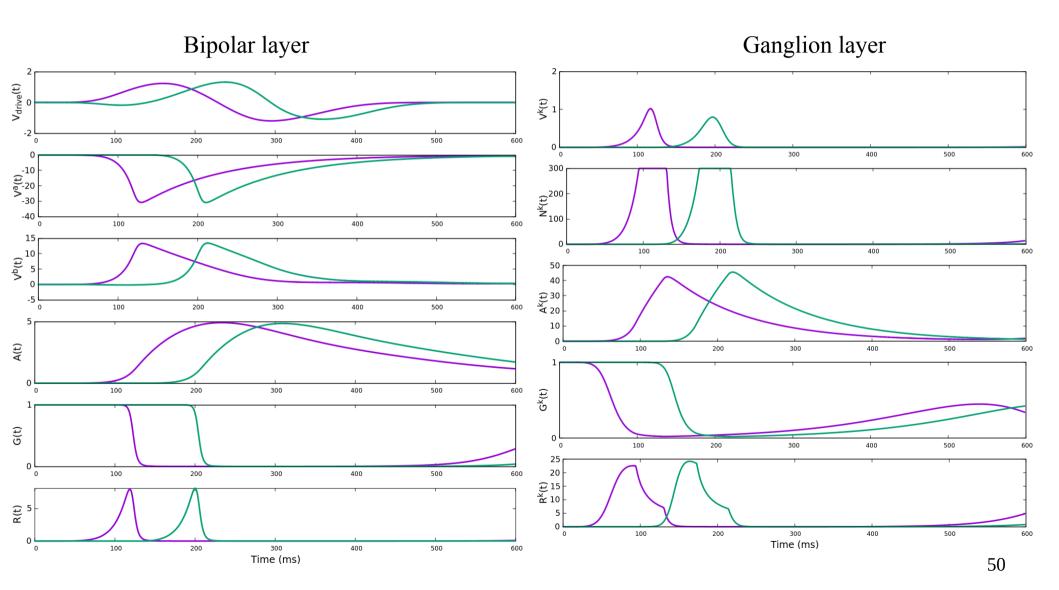
· Amacrine voltage:

Anti-diffusive wave of activity  $\frac{1}{dt}$  ahead of the bar  $W_{A_j}^{B_i}R_{B_i}(t)$ .

Coupled dynamics :

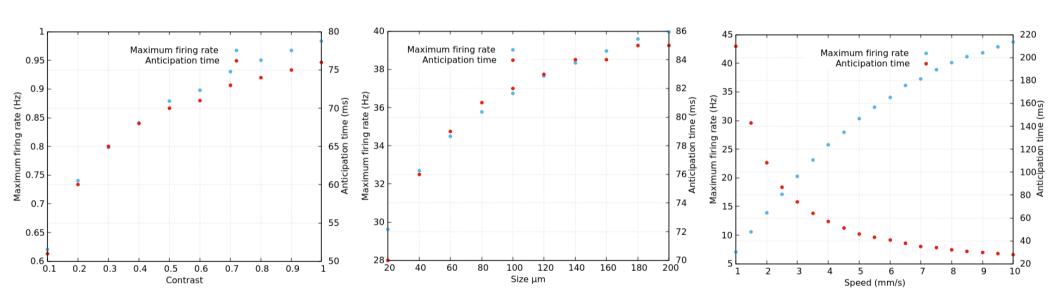
$$\begin{cases} \frac{dV_{B_{i}}}{dt} &= -\frac{1}{\tau_{B}} V_{B_{i}} + \sum_{j=1}^{N_{A}} W_{B_{i}}^{A_{j}} V_{A_{j}} + F_{B_{i}}(t) \\ \frac{dA_{B_{i}}}{dt} &= -\frac{A_{B_{i}}}{\tau_{a}} + h \mathcal{N}(V_{B_{i}}(t)), \\ \frac{dV_{A_{j}}}{dt} &= -\frac{1}{\tau_{A}} V_{A_{j}}(t) + \sum_{i=1}^{N_{A}} W_{A_{j}}^{B_{i}} R_{B_{i}}(t). \end{cases}$$

## 1D results: smooth motion anticipation with amacrine connectivity

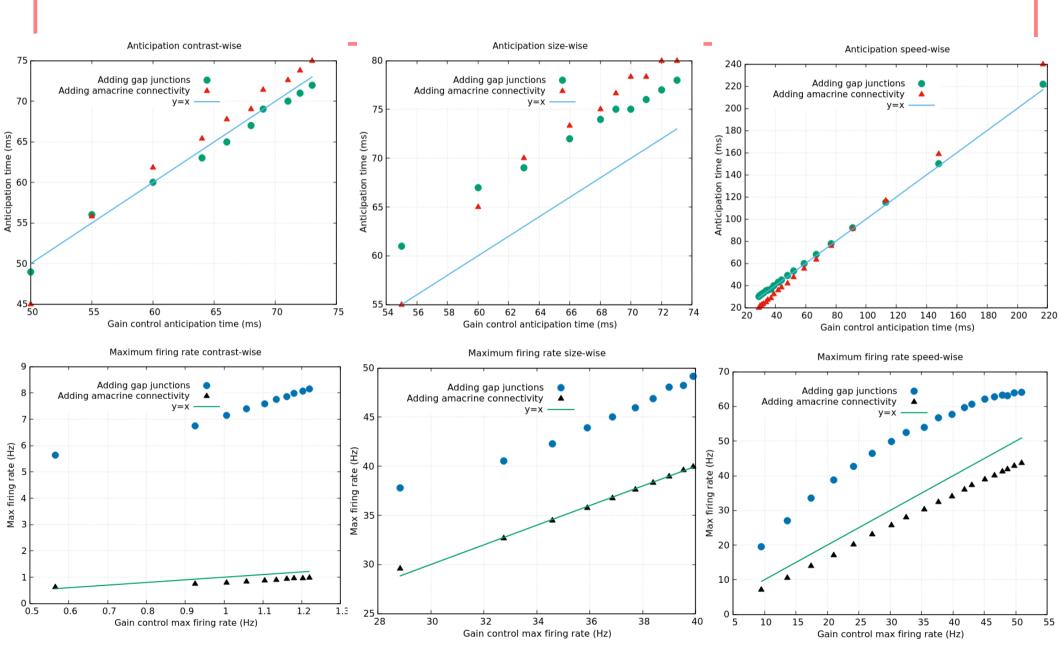


## 1D results: smooth motion anticipation with amacrine connectivity

Anticipation variability with stimulus parameters

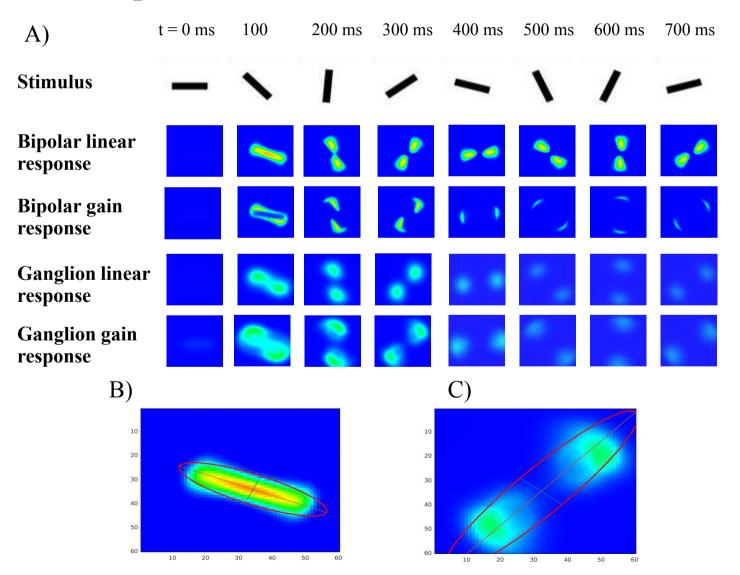


### Comparing the performance of the three layers



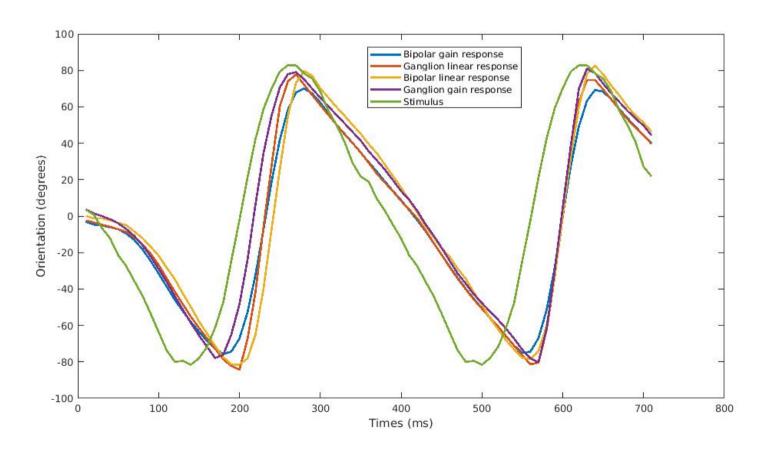
### Suggesting new experiments: 2D results

#### 1) Angular anticipation



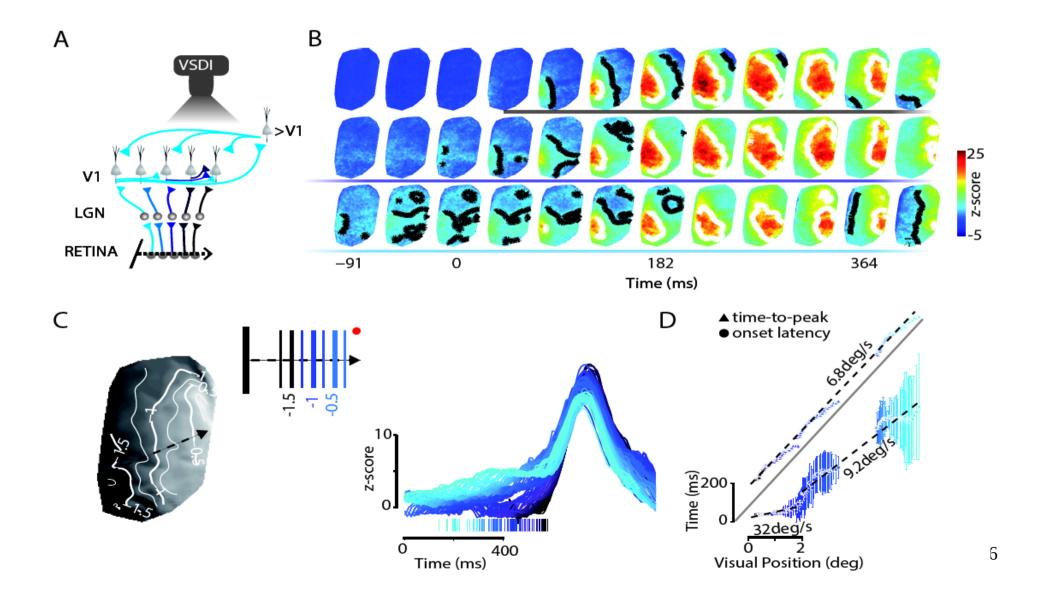
### Suggesting new experiments: 2D results

#### 1) Angular anticipation



## Anticipation in V1

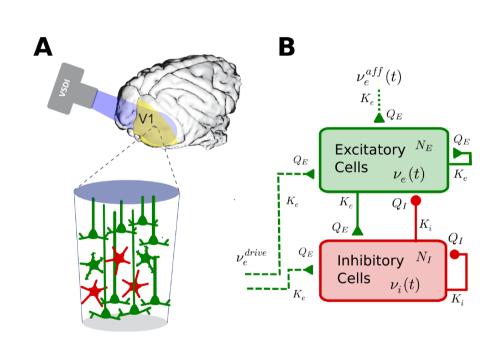
### Anticipation in V1

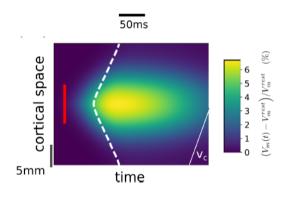


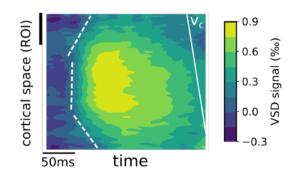
## A mean field model to reproduce VSDI

recordings

Zerlaut et al 2016
Chemla et al 2018







#### A mean field model to reproduce VSDI recordings Zerlaut et al 2016

Chemla et al 2018

Master equation for first and second moments local population dynamics (El Boustani and Destexhe, 2009) read:

$$\begin{cases} T \frac{\partial \nu_{\mu}}{\partial t} = (\mathcal{F}_{\mu} - \nu_{\mu}) + \frac{1}{2} c_{\lambda \eta} \frac{\partial^{2} \mathcal{F}_{\mu}}{\partial \nu_{\lambda} \partial \nu_{\eta}} \\ T \frac{\partial c_{\lambda \eta}}{\partial t} = A_{\lambda \eta} + (\mathcal{F}_{\lambda} - \nu_{\lambda}) (\mathcal{F}_{\eta} - \nu_{\eta}) + \\ c_{\lambda \mu} \frac{\partial \mathcal{F}_{\mu}}{\partial \nu_{\lambda}} + c_{\mu \eta} \frac{\partial \mathcal{F}_{\mu}}{\partial \nu_{\eta}} - 2c_{\lambda \eta} \end{cases} \longrightarrow T \frac{\partial \nu_{\mu}}{\partial t} = \mathcal{F}_{\mu} - \nu_{\mu}$$

$$A_{\lambda\eta} = \begin{cases} \frac{\mathcal{F}_{\lambda} (1/T - \mathcal{F}_{\lambda})}{N_{\lambda}} & \text{if } \lambda = \eta \\ 0 & \text{otherwise} \end{cases}$$

## A mean field model to reproduce VSDI recordings Zerlaut et al 2016 Chemla et al 2018

Master equation for first and second moments local population dynamics (El Boustani and Destexhe, 2009) read :

$$\begin{cases} T \frac{\partial \nu_{\mu}}{\partial t} = (\mathcal{F}_{\mu} - \nu_{\mu}) + \frac{1}{2} c_{\lambda \eta} \frac{\partial^{2} \mathcal{F}_{\mu}}{\partial \nu_{\lambda} \partial \nu_{\eta}} \\ \mathbf{Affords}^{-}_{\mathbf{C}\lambda\eta} \mathbf{T}^{-}_{\mathbf{C}\lambda\eta} \mathbf{S}^{+}_{\mathbf{C}\mu\eta} \frac{\partial^{2} \mathcal{F}_{\mu}}{\partial \nu_{\eta}} - 2c_{\lambda\eta} \\ c_{\lambda\mu} \frac{\partial \mathcal{F}_{\mu}}{\partial \nu_{\lambda}} + c_{\mu\eta} \frac{\partial \mathcal{F}_{\mu}}{\partial \nu_{\eta}} - 2c_{\lambda\eta} \end{cases}$$

$$A_{\lambda\eta} = \begin{cases} \frac{\mathcal{F}_{\lambda} (1/T - \mathcal{F}_{\lambda})}{N_{\lambda}} & \text{if } \lambda = \eta \\ 0 & \text{otherwise} \end{cases}$$

#### A mean field model to reproduce VSDI recordings Zerlaut et al 2016

Chemla et al 2018

Single neuron model (The adaptative exponential integrate and fire model Brette and Gerstner, 2005)

$$\begin{cases} C_m \frac{dV}{dt} = g_L (E_L - V) + I_{syn}(V, t) + k_a e^{\frac{V - V_{thre}}{k_a}} - I_w \\ \tau_w \frac{dI_w}{dt} = -I_w + a \cdot (V - E_L) + \sum_{t_s \in \{t_{spike}\}} b \, \delta(t - t_s) \end{cases}$$

The conductance-based exponential synapse

$$I_{syn}(V,t) = \sum_{s \in \{e,i\}} \sum_{t_s \in \{t_s\}} Q_s \left(E_s - V\right) e^{-\frac{t - t_s}{\tau_s}} \, \mathcal{H}(t - t_s)$$

Semi analytical transfer function:

$$\nu_{out} = \mathcal{F}(\nu_e, \nu_i) = \frac{1}{2 \tau_V} \cdot Erfc(\frac{V_{thre}^{eff} - \mu_V}{\sqrt{2} \sigma_V}) \quad \text{with} \quad V_{thre}^{eff}(\mu_V, \sigma_V, \tau_V^N) = P_0 + \sum_{x \in \{\mu_V, \sigma_V, \tau_V^N\}} P_x \cdot \left(\frac{x - x^0}{\delta x^0}\right) + P_{\mu_G} \log(\frac{\mu_G}{g_L}) \\ + \sum_{x, y \in \{\mu_V, \sigma_V, \tau_V^N\}^2} P_{xy} \cdot \left(\frac{x - x^0}{\delta x^0}\right) \left(\frac{y - y^0}{\delta y^0}\right)$$

#### A mean field model to reproduce VSDI recordings Zerlaut et al 2016

Chemla et al 2018

The mean, standard deviation and auto-correlation time of the excitatory and inhibitory conductance read:

$$\mu_{Ge}(\nu_{e},\nu_{i}) = \nu_{e} K_{e} \tau_{e} Q_{e}$$

$$\sigma_{Ge}(\nu_{e},\nu_{i}) = \sqrt{\frac{\nu_{e} K_{e} \tau_{e}}{2}} Q_{e}$$

$$\mu_{Gi}(\nu_{e},\nu_{i}) = \nu_{i} K_{i} \tau_{i} Q_{i}$$

$$\sigma_{Gi}(\nu_{e},\nu_{i}) = \sqrt{\frac{\nu_{i} K_{i} \tau_{i}}{2}} Q_{i}$$

$$\mu_{V}(\nu_{e},\nu_{i}) = \frac{\mu_{Ge} E_{e} + \mu_{Gi} E_{i} + g_{L} E_{L}}{\mu_{G}}$$

$$\sigma_{V}(\nu_{e},\nu_{i}) = \sqrt{\sum_{s} K_{s} \nu_{s} \frac{(U_{s} \cdot \tau_{s})^{2}}{2 \left(\tau_{m}^{\text{eff}} + \tau_{s}\right)}}$$

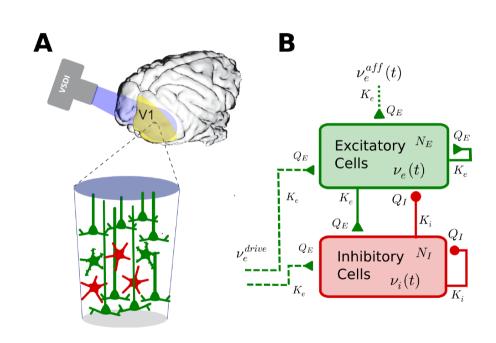
$$\tau_{V}(\nu_{e},\nu_{i}) = \left(\frac{\sum_{s} \left(K_{s} \nu_{s} \left(U_{s} \cdot \tau_{s}\right)^{2}\right)}{\sum_{s} \left(K_{s} \nu_{s} \left(U_{s} \cdot \tau_{s}\right)^{2}/\left(\tau_{m}^{\text{eff}} + \tau_{s}\right)\right)}\right)$$

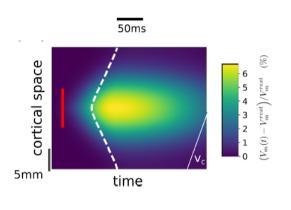
Finally, the transfer function reads:

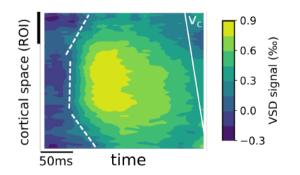
$$\nu_{out} = \mathcal{F}(\nu_e, \nu_i) = \frac{1}{2 \tau_V} \cdot Erfc(\frac{V_{thre}^{eff} - \mu_V}{\sqrt{2} \sigma_V})$$

### A mean field model to reproduce VSDI recordings

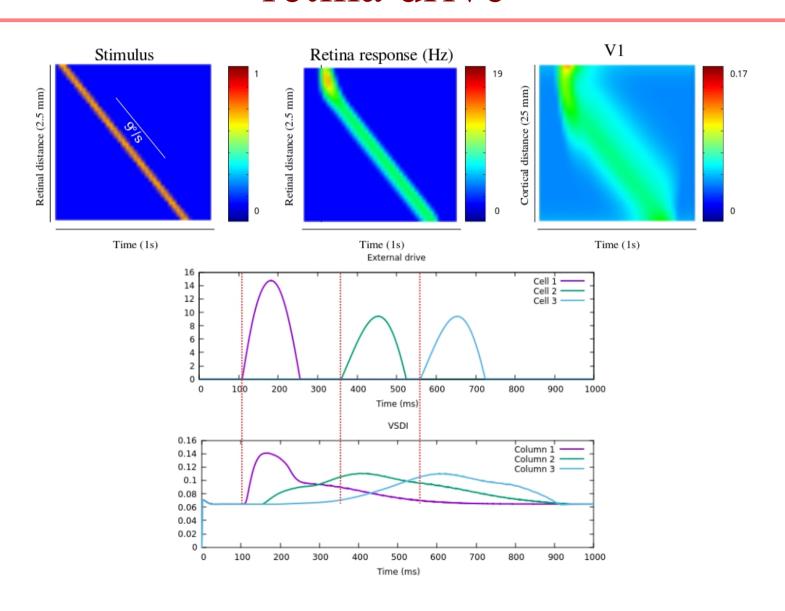
Zerlaut et al 2016 Chemla et al 2018



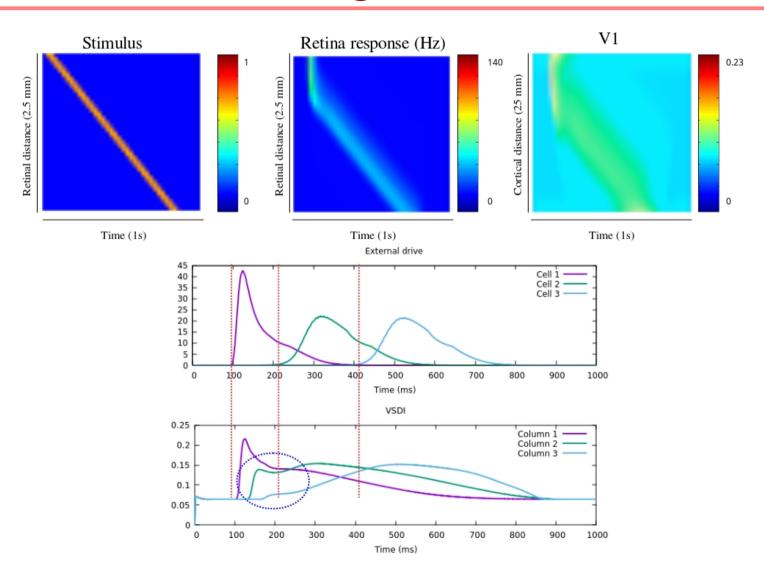




## Response of the cortical model to a LN retina drive



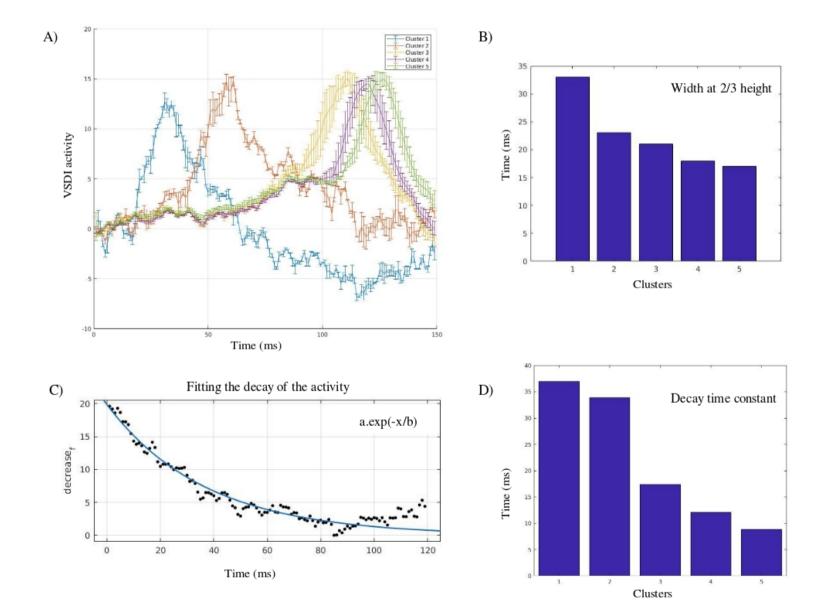
## Response of the cortical model to a retina drive with gain control



## Anticipation in the cortex: VSDI data

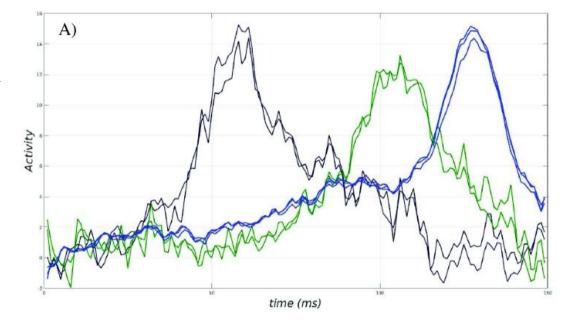
analysis

(Data courtesy of F. Chavane et S. Chemla)

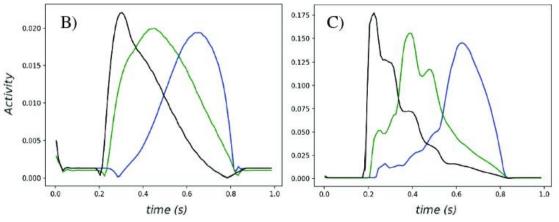


## Comparing simulation results to VSDI recordings

Cortex experimental recordings



Simulation results Response to an LN model of the retina



Simulation results Response to a gain control model of the retina

### Conclusions

- We developed a 2D retina with three ganglion cell layers, implementing gain control and connectivity.
- We use the output of our model as an input to a mean field model of V1, and were able to reproduce anticipation as observed in VSDI

### Conclusions

- How to improve object identification
  - 1) exploring the model's parameters and
    - 2) using connectivity?
- Is our model able to anticipate more complex trajectories, with accelerations for instance?
- How to calibrate connectivity using biology?
- How does anticipation affect higher order correlations?
- Would it be possible to design psycho-physical tests clearly showing the role of the retina in visual anticipation?

Thank you for your attention!