With the advent of NUMA (Non Uniform Memory Access) architectures, optimizing applications execution time is known to be a extremely difficult endeavor. Not only does it require carefully writing the application such that the threads efficiently use the available resources (e.g., cores, caches and memory) but, even if the code is highly optimized, launch time optimizations and decisions may have a great impact on performance.

In this paper, we focus on this second aspect of the problem. We assume that a multithreaded application is already statically optimized, and we look at the factors impacting its execution time that can be set at launch time. The two main factors targeted here are the thread placement policy (which thread is mapped on which core) and the memory allocation policy (where memory pages are allocated). Indeed, data locality and memory contention are affected by these policies and can have a huge impact in several levels of the memory hierarchy and thus on application performance.

The goal of this paper is to provide a methodology and models to answer two questions: (1) Is an application sensitive to the placement of its threads and data on a given NUMA architecture? and (2) What is the best placement and allocation policy for this application on that architecture?

To achieve this goal, we follow several lines of study. First, to capture applications characteristics, we use two methods that allow capturing different kinds of metrics and have a different cost: instrumenting the application binary (costly and characterizing applications regardless of the underlying hardware) or relying on hardware counters (cheap and embedding hardware specific responses). Second, we study several metamodels used in machine learning to model the impact of placement on applications. Third, we target many different applications and benchmarks that embrace a large spectrum of use cases. Fourth, we use testbeds spanning different Intel processor generations. We study predictions on a given architecture and predictions across multiple architectures.

The two main results of this article are the following:

- On multiple Intel platforms, we show that one can build a model that can decide whether a new application is sensitive to locality and can reach an accuracy close to 80%.
- For applications that are sensitive to locality, one also can build models making good placement decisions (with respect to the studied placement strategies) and can achieve speedups that are close to the optimal.

Moreover, the following additional results have been obtained while conducting this study:

- One can build a model on a processor family and obtain good predictions on another processor family.
• Although hardware counters are fast for collecting metrics, they cannot precisely capture the algorithmic characteristics of applications. Nevertheless, they provide sufficient information to make decisions about placement.

The remainder of the paper is organized as follows. In Section 2, we describe the context and the state of the art. The methodology is presented in Section 3. The experimental testbed is described in Section 4. In Section 5, we present and study the results. Concluding remarks are given in Section 6.

2 CONTEXT

2.1 Objectives and Assumptions

This study considers the placement of threads and data of a multithreaded application running in a modern NUMA platform. As illustrated in Figure 1, such platforms are composed of several multicore processors. Each core has access to some private caches while a last-level cache (LLC) is shared among all cores on the same processor. The processors are connected through a high-performance interconnect (e.g., Intel Quick Path Interconnect). The memory is shared among all processors, and cache coherence is ensured by the hardware. A processor together with its local part of the memory is called a NUMA node. Local accesses to data, namely, inside a node, is fast, whereas accesses to a remote node, whether the data is in a remote cache or in a remote memory, is slower.

Several phenomena can impact the performance of multithreaded applications on such platforms. When deciding on the placement of threads and data, two main points need to be considered: locality and contention. Locality refers to the fact that for a thread to perform well, the data it accesses should be as close as possible. The best case is when the data is in some cache that the thread can directly access. The worst case is usually when the data is in another NUMA node. Contention refers to the fact that if too many threads use some shared resources at the same time, performance degradation is to be expected. The LLC, the interconnect links, and the memory controllers are examples of resources that can suffer from contention. Another difficulty comes from the fact that threads of a multithreaded application collaborate to run a computation, and hence use shared memory to synchronize and communicate. The challenge is then to optimize locality by taking into account accesses of threads to private and shared variables while avoiding contention on shared hardware resources.

In this study we consider the case where a single multithreaded application runs on a NUMA platform. The application uses all available cores. Our study is limited to cases where simultaneous multithreading (SMT) is disabled in order to focus on the locality and contention issues that occur at the level of the LLC and below (enabling SMT would raise additional questions, e.g., related to the contention on the computing resources inside one core).

In this context, deciding on the appropriate threads placement and data allocation policy is a complicated problem that we aim to solve. Since placement decision algorithms can be expensive [14], we are also concerned with the application’s need for such an optimization. We seek solutions to these two issues for unseen applications and/or unseen platforms. Such properties are important because they imply that obtained solutions could work for users with different machines and undisclosed applications and would be resilient to modifications in applications. Therefore, our overall goal is to build models that—after a single run of an application for a given set of inputs\(^1\) on a single machine (the minimum effort required to collect metrics) for a target (eventually different) platform—are able to decide (i) whether the application’s performance is sensitive to placement and (ii) if yes, what the best placement policy is for this application.

Our study focuses on compute-intensive applications [1, 2, 12]. We make a few assumptions about the characteristics of applications to which our proposed technique is applied; these assumptions are common to many compute-intensive applications. First, our study focuses on applications that follow the fork-join execution model; that is, threads are not dynamically created as a consequence of some events. Hence the same number of threads is created in all the runs of an application. Furthermore, we assume that threads can be uniquely identified by using IDs assigned based on their creation order, as is the case, for instance, in OpenMP applications. The other major assumption is that for a given set of inputs, the thread with the same ID in two runs of the application execute similar computations. This implies that our approach cannot work with, for example, task programming paradigms out of the box.

We study only static policies: the placement of threads and the policy for memory allocation are decided before launching the application and remain for the application’s whole lifespan. To make our problem tractable, we limit our study to two placement policies for threads and to two for data. For threads, the choice is between (i) having the threads with consecutive IDs placed on the same processor (called Compact hereafter), which favors neighbors sharing, and (ii) having the threads assigned to processors in round-robin (Scatter), mitigating neighbors contention. These two policies are supported by most OpenMP runtime libraries. For data, the choice is between the two standard allocation policies: (i) memory is allocated on the node of the first thread that touches the corresponding page (Firsttouch) targeting data locality and (ii) memory is allocated in round robin on nodes (Interleave), mitigating contention in memory controllers.

The approach we follow is to collect a set of metrics during the run of applications. These metrics are collected by using transparent

\(^1\) In the following, the run of an application is always studied for a given set of inputs.
techniques for the applications, based either on hardware counters or on information obtained through binary code instrumentation. These metrics, together with the preferred placement strategy in a given platform, are then used to train classification algorithms to try to answer the questions raised above.

2.2 Related Work

Placement of threads and data in NUMA platforms has been studied extensively. Locality and resource contention issues are identified as the two main problems to tackle [20, 24, 33].

Our work follows an offline profiling approach to obtain information about interactions between threads and about memory accesses. Some previous works have also used this approach. Diener et al. [19] propose a solution based on binary code instrumentation to obtain information about the interactions among threads. Other works try to collect information about memory accesses using the monitoring capabilities of modern processors [25, 26]. In this paper, we consider metrics coming from information obtained both through binary instrumentation and from hardware counters.

Several works also tried to do online profiling, that is, to collect information during the execution and to adapt thread or memory page mapping based on this information [9, 13, 15, 18, 22]. To the best of our knowledge, only a few of them also tackle the issue of characterizing the need for placement optimization [13]. Some rely on the hardware-monitoring features of processors to make placement decisions [9, 15, 22]. Online profiling has the advantage of being able to adapt to changes in the behavior of the application during the execution. On the other hand, offline profiling allows collecting more extensive and precise information about memory accesses and threads interactions and thus can lead to better placement decisions for applications that have a similar behavior during the whole execution [20].

Most works on thread and/or data placement focus solely on optimizing locality [20]. However, both locality and contention should be taken into account to obtain a solution that can select a good placement for a large variety of applications [15, 17]. A few solutions try to deal with locality and contention only through thread placement. However, they focus mostly on cases where the number of threads is less than the number of cores [22] or where multiple applications are executed simultaneously on the platform [5, 29]. Recent studies show that the best results are achieved when both data and thread placement are considered [9, 15, 19]. This finding is confirmed in our study (see Figure 2). We observe that all the combinations of thread placement (Compact or Scatter) and data placement (First-touch or Interleave) policies are at least once the best strategy for an application.

In existing works, different metrics have been used to make placement decisions: there is no general agreement on the best metrics to use. Among the metrics that can be collected by using hardware counters, cache miss rate, mostly at the LLC level, is often considered as a good indicator of contention [5, 9, 32]. However, other studies show that using this metric can lead to wrong placement decisions [16]. Simple performance metrics such as MIPS (million instructions per second) have also been considered [22]. At the level of memory accesses and NUMA nodes, metrics such as memory read ratio, local access ratio, or memory-controller load imbalance have also been studied [15]. More advanced metrics can be obtained with high accuracy by using binary instrumentation. Such approaches allow collecting information about memory access patterns [32] and about interactions among threads [13, 19]. Such interactions include the volume of data exchanged between threads, the frequency of the exchanges, or the locality of the exchanges. As highlighted in previous studies, these interactions should be tracked at the level of cache lines [13, 19]. Our study considers a representative set of all these metrics (see Section 3) derived from both hardware counters and binary instrumentation. When tracing interactions among threads based on memory accesses, we implemented mechanisms at the granularity of cache lines.

Some works have studied the use of statistical models to predict the performance of multithreaded applications. Castro et al. [10] proposed a machine learning approach to make thread placement decisions in the context of software transactional memory. The work that is the closest to ours is that of Wang et al. [31]. They have proposed solutions based on artificial neural networks and support vector machines (SVMs), using a few simple metrics as inputs such as the number of L1 misses to predict the optimal number of threads and the best scheduling policy for these threads for a new application on a given platform. Their results are encouraging because they are able to make good predictions on average and their solution works on multiple platforms. In this study, we adopt a similar approach, but we tackle a different problem: we do not consider the scalability issue, and we emphasize decisions regarding both threads and data placement. Furthermore, we characterize the need for applying placement policies that may be expensive to compute and apply online. Our study also considers a much larger set of metrics and compares the use of binary instrumentation and hardware counters.

3 METHODOLOGY

Our approach to predict the sensitivity of applications to placement and to identify the best placement policies for threads and data can be summarized as follows. We collect a large set of data to capture the main characteristics of applications through a single run with a default placement policy. This data is obtained via transparent mechanisms at the granularity of cache lines. Our approach to obtain information about the interactions among threads based on memory accesses, we represent a set of all these metrics (see Section 3) derived from hardware counters.

In this section starts with definitions, then details collected metrics about the execution of applications. Finally, the classification algorithms; the preprocessing transformations; and the method for training, evaluating, and validating models is presented.

3.1 Definitions

As described previously, this study focuses on two placement policies for threads (Compact and Scatter) and for memory pages (First-touch and Interleave). We name placement policy or placement strategy, the combination of a thread placement policy and a data allocation policy. Hence, there are four possible placement strategies. We define compact-firsttouch as the default strategy.

We define speedup as the ratio of the application execution time when run with a specific policy over its execution time with the
We select abstract counters defined by PAPI, which are supposed to be equivalent across tested architectures. They capture information about the total number of cycles used by the application, about cache misses at all levels of the cache hierarchy, and about accesses to the NUMA nodes. In order to have a meaningful comparison of these numbers between applications, the models described in this paper follow a classic pipeline of sampling, transformations, learning, and model selection. Obtained models are evaluated based on their ability to generalize their predictions to new applications, new platforms, or even both at the same time.

A communication between threads $i$ and $j$ is defined as the first read from $j$ after $i$ writes to a common cache line. The sum over all cache lines of these events is called the communication amount between these threads. Similarly, the amount of sharing between pairs of threads is defined as the sum over cache lines of individual cache line sharing, where sharing amount is defined as the intersection of the number of accesses for each thread of the pair to a common cache line. Interthread communications and sharing matrices have been used in prior works [19] to derive metrics of interest toward a solution to the threads and data-mapping problems.

For such matrices, heterogeneity, average of normalized values, and balance aim at characterizing the impact of threads mapping.

Heterogeneity represents the proportion of interthreads exchanges over accesses to private data. Balance is defined as the average matrix value over the maximum matrix value; it is high if all the matrix values are close to each other and small if one thread is communicating/sharing more than the others. Neighbors sharing/communication fraction is defined as the sum of adjacent thread pairs communications over the sum of matrix values; it quantifies whether communications are focused mainly on direct neighbors.

The need for balance at the scale of NUMA nodes is measured by the cluster deviation of matrices. It is defined as the standard deviation across NUMA domains (i.e., groups of consecutive thread IDs inside the same NUMA node) of the sum of values inside the corresponding domain. It is small when memory accesses are well balanced across thread groups, whereas high values may indicate that an interleave allocation policy would be a good choice.

When moving data from one thread to another in an occurring communication event, we count the number of hops in the machine topology (cores + caches + memories) as provided by hwloc [8], to walk from source core to destination core. The average number of hops per communication/sharing can then characterize locality among threads with default thread placement.

### 3.2 Characterization Metrics of Applications

A total of 29 metrics are computed per application, based on data collected while running each application with the default placement policy. This set of metrics, described below, is used as input to the models built in our study. For each application a call to a custom library is wrapped around a region of interest to collect hardware counter values by using the PAPI library [28] or to start instrumenting applications binary with the Pin tool [23].

Hardware counters and approaches based on binary instrumentation offer different trade-offs. Collecting hardware counters is a cheap operation compared to binary instrumentation as the former induces negligible side effects on execution compared to a 100X slowdown and heavy memory overhead for the latter. However, these two techniques enable to get different information about applications. With hardware counters, obtained information is less about the application algorithm than about the hardware response to the application execution. Through binary instrumentation, one can extract more precise information about the application algorithm (interactions between threads, memory access patterns), but the collected data is mostly agnostic to the platform on which the application executes.

#### 3.2.1 Hardware counters

For each application, we collect the value of several hardware counters at the end of the execution using PAPI. We select abstract counters defined by PAPI, which are supposed to be equivalent across tested architectures. They capture information about the total number of cycles used by the application, about executed instructions, about cache misses at all levels of the cache hierarchy, about accesses to the NUMA nodes. In order to have a meaningful comparison of these numbers between applications that may have a very different execution duration, metrics derived from these counters are expressed relatively to the total number of cycles or of data accesses. The metrics are summarized in Table 1.

<table>
<thead>
<tr>
<th>Hardware Counter</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>L0_INSTANT</td>
<td>Load instructions per cycle.</td>
</tr>
<tr>
<td>L1_MISS_REL</td>
<td>Data cache misses in the first level cache per memory (load or store) instruction.</td>
</tr>
<tr>
<td>L2_MISS_REL</td>
<td>Same as L1_MISS_REL for level 2 cache.</td>
</tr>
<tr>
<td>L3_MISS_REL</td>
<td>Same as L1_MISS_REL for level 3 cache.</td>
</tr>
<tr>
<td>NODE_MISS_REL</td>
<td>Remote memory accesses per memory (load or store) instruction.</td>
</tr>
</tbody>
</table>

#### 3.2.2 Binary Instrumentation

Runtime instrumentation of applications memory accesses is performed with the Pin framework. Accessible memory addresses are recorded at cache line granularity to maintain a representation of the memory state (e.g., ID of the threads that have accessed the cache line, last thread that modified the cache line, etc.). Such mechanisms enable to compute several statistics on applications execution, including per-thread memory footprint, inter-thread communications, etc. Metrics derived from these statistics are listed in Table 2. For those that are not straightforward, we provide a detailed explanation below.

A communication between threads $i$ and $j$ is defined as the first read from $j$ after $i$ writes to a common cache line. The sum over all cache lines of these events is called the communication amount between these threads. Similarly, the amount of sharing between pairs of threads is defined as the sum over cache lines of individual cache line sharing, where sharing amount is defined as the intersection of the number of accesses for each thread of the pair to a common cache line. Interthread communications and sharing matrices have been used in prior works [19] to derive metrics of interest toward a solution to the threads and data-mapping problems.

For such matrices, heterogeneity, average of normalized values, and balance aim at characterizing the impact of threads mapping.

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#### 3.3 Modeling Methodology

Models described in this paper follow a classic pipeline of sampling, transformations, learning, and model selection. Obtained models are evaluated based on their ability to generalize their predictions to new applications, new platforms, or even both at the same time.

Generalization to new applications employs a one-versus-all training scheme to train models. It consists of removing two applications from the applications set, training the model on all applications but the two removed (i.e. the training set), and then performing a prediction on the first removed application (i.e., the test set) and the second removed application (i.e., the validation set). This training process is repeated for all applications pairs, and the models average performance on predictions for all applications is reported.

---

The complete implementation of the modeling methodology with the dataset described in Section 4 has been published on Code Ocean platform [27] for reproducibility.
Splitting the dataset in this way is necessary in order to perform validation after the model selection stage. Indeed, chances are that choosing a model among thousands based on a few tens of predictions may draw a lucky one or an overfitting one. Using a validation set aims at reducing this risk. More precisely, the model selection methodology is the following. The 1% top performers on the test set are selected, and then the best performer on the validation set among remaining models is elected as the final model. This selection decreases the risk of presenting overfitting models.

When modeling for generalization to new machines, models are trained with all applications on a single platform. Each model is then used for predictions on another platform (the test set), and again on another one (the validation set). In the third scenario (a new application on a new machine), we combine both training schemes; that is, we remove two applications from the training set, use the training set on a single machine, and then predict the two unused applications each on a different unseen machine.

The modeling process includes several preprocessing stages on collected data. These steps are designed to fit more complicated models and perhaps obtain a better quality on the predictions. When needed, they are calibrated on the training set, then applied with the same settings on the test and validation sets. For instance, when normalizing data, the center and amplitude of the dataset are computed on the test set; then normalization of other sets utilizes the same center and amplitude. These steps are the normalization of inputs, (optional) singular value decomposition [21], and (optional) polynomial transformation [3] of inputs, up to degree 2.

Metrics for a preprocessed application are given as input to the classification algorithm by the label, that is, sensitivity to placement or preferred placement policy. We use the classifiers as black boxes: we use the default classification functions without tuning their hyperparameters. Classification building blocks used are the following: random forest [6] from the R package randomForest, logistic regression [4] from the native R glm function, SVMs [11] from the R package kernlab, and artificial neural networks with one hidden layer of four neurons from the R package nnet.

Data and Thread Placement in NUMA Architectures: A Statistical Learning Approach

Table 2: Metrics obtained through binary instrumentation.

<table>
<thead>
<tr>
<th>Metric</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>sharing/communications_CC</td>
<td>Average normalized amount of sharing/communications per thread</td>
</tr>
<tr>
<td>sharing/communications_CB</td>
<td>Sharing/communication matrix balance</td>
</tr>
<tr>
<td>sharing/communications_CH</td>
<td>Sharing/communication matrix heterogeneity</td>
</tr>
<tr>
<td>sharing/communications_NB</td>
<td>Neighbors sharing/communication fraction</td>
</tr>
<tr>
<td>sharing/communications_clusterSD</td>
<td>Inter NUMA cluster sharing/communications deviation</td>
</tr>
<tr>
<td>avg_sharing_degree</td>
<td>Average number of topology hops per sharing/communication</td>
</tr>
<tr>
<td>sd_sharing_degree</td>
<td>Average number of threads sharing a cache line</td>
</tr>
<tr>
<td>avg_write_ratio</td>
<td>Deviation of number of threads sharing a cacheline</td>
</tr>
<tr>
<td>sd_write_ratio</td>
<td>Average writes over memory access per cache line</td>
</tr>
<tr>
<td>avg_shared_write_ratio</td>
<td>Deviation of writes over memory access per cache line</td>
</tr>
<tr>
<td>sd_shared_write_ratio</td>
<td>Same as avg_write_ratio per shared cache line</td>
</tr>
<tr>
<td>avg_write_ratio</td>
<td>Same as sd_write_ratio per shared cache line</td>
</tr>
<tr>
<td>sd_write_degree</td>
<td>Average number of threads writing a cache line</td>
</tr>
<tr>
<td>avg_shared_write_ratio</td>
<td>Deviation of number of threads writing a cache line</td>
</tr>
<tr>
<td>sd_write_degree</td>
<td>Number of cache lines accessed</td>
</tr>
<tr>
<td>footprint</td>
<td>Deviation of number of cache lines accessed</td>
</tr>
</tbody>
</table>

5 Cluster-on-Die for Haswell and Broadwell, Sub-NUMA-Cluster for Skylake.
Table 3: The set of applications and their parameters.

<table>
<thead>
<tr>
<th>Applications</th>
<th>run parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td>bodytrack, canneal, freqmine, swapoptions</td>
<td>input native</td>
</tr>
<tr>
<td>fir, del_dot_vec_2d, energy_calc_alt, vo13d, couple, pressureCalc_alt, pic_2d</td>
<td>N/A</td>
</tr>
<tr>
<td>MILCmk</td>
<td>b 4 -s 100 -i 40 -r 100</td>
</tr>
<tr>
<td>HACCmk</td>
<td>count=200</td>
</tr>
<tr>
<td>lu, cg, ep, mg, sp, bt, ft, sp</td>
<td>class A, B</td>
</tr>
</tbody>
</table>

With a mesh network, both with potential implications on locality and contention.

This section focuses on model performance and on the practicability of placement sensitivity detection and placement policy selection. For each of these, we describe the performance of models along all of placement sensitivity detection and placement policy selection.

Table 7 shows the wrong predictions of new applications made by the best models per machine. Considering the misclassified applications, the table presents the average maximum distance between the speedup achievable with an application and the boundaries set by our definition of placement sensitivity. The results show that our wrong predictions would have only little impact in practice because the misclassified applications are not very sensitive to placement.

Figure 4 presents the performance of models on the test and validation sets, when predicting a new application on a new platform. Each column describes a result with training from a source machine and predicting for a different one. Violin plots in the first line exhibit models performance distribution on test set. Models of individual violins vary in the preprocessing performed, the learning algorithm used, and the set of input parameters. A violin plot is drawn per set of input parameters: hardware counters, instrumentation metrics, or both. In the second line, the outcome of model selection is presented with the best model performance on the validation set (i.e., different machines and applications from those for training and testing).

From Figure 4, we also see that the model performance on the validation set consistently reaches more than 75% accuracy, this time with both a new application and a new machine. Once again, the accuracy difference between using hardware counters or others is not significant. The accuracy distribution on the test set (first row) shows that only few models reach the highest performance. Model validation (second row) reaches similar accuracy as the results for the proposed dimensions: generalization abilities to new applications and machines, with hardware counter versus instrumentation metrics.

5.1 Sensitivity to Data and Threads Placement

Following the proposed methodology, a set of models was trained to detect whether an application is placement sensitive. For this objective, the metric of importance is accuracy, that is, the average number of good predictions among all applications. Figure 3 shows model accuracy on the validation set when predicting application sensitivity to data and threads placement. On the diagonal, models have been trained with runs on a single machine, and predictions are made on unseen applications on the same machine. The performance baseline, represented by a horizontal dashed line, is the accuracy obtained when always predicting that applications are sensitive. Outside of the diagonal, models have been trained with all applications on a system (rows) to predict the same applications on another one (columns). In these cases, the baseline, represented by a horizontal dashed line, is the accuracy obtained when predicting the same output as on the original machine.

Analysis of Figure 3 leads to several conclusions about modeling sensitivity to placement for new applications or new platforms. First, in every scenario, sensitivity to placement can be predicted with around 80% accuracy. Models always improve compared with the baseline even in the case of cross-platform predictions. We also note that using hardware counters provides results similar to those when using binary instrumentation metrics. Thus, a very low overhead application profiling, our models can fulfill the goal of predicting placement sensitivity with good accuracy both for new applications and for new architectures.

Figure 2 represents speedups for the best and worst execution time of each application on the Skylake machine when trying the four placement strategies. A 100% speedup corresponds to the performance with the default placement policy. If the best or worst performance exceeds the 10% threshold materialized with a dashed line, the application is tagged as placement sensitive. On this machine, a majority of applications prefers the default policy. However, placement-sensitive applications can perform significantly better or worse with alternative placement policies.

After running all applications with all placement policies, we are able to tag them as sensitive or not according to our definition (see Section 3.1). Table 5 presents statistics about applications sensitivity to placement with respect to the platform. On the diagonal, the percentage of applications that are placement sensitive on a given platform is reported. Out of the diagonal, the percentage of applications that remain in the same class when changing the platform is provided. From this table, one can see that there is no easy assumption for predicting the sensitivity either of new applications or of known applications on new machines. On average, a good balance exists between sensitive and insensitive applications. This observation motivates the need to identify placement-sensitive applications, in order to avoid useless placement computation. Also, up to 33% of them may change their status from one machine to another, showing that predictions from one machine to another is not straightforward.

Considering the subset of placement-sensitive applications, Table 6 presents the average achieved speedup when using one machine’s preferred policies to run on another machine. The diagonal shows the average of top achievable speedup on each specific machine as a comparison point. Using conservative choices across machines is usually a good choice compared with using the default policy (i.e., speedup > 1). Nevertheless, our results (see Section 5) show that it is possible to improve from this strategy.

5 MODELS PERFORMANCE AND REAL WORLD PRACTICABILITY

This section focuses on model performance and on the practicability of placement sensitivity detection and placement policy selection. For each of these, we describe the performance of models along all.
Table 4: Experimentation platforms.

<table>
<thead>
<tr>
<th>Microarchitecture</th>
<th>Model</th>
<th>Sockets × Cores</th>
<th>NUMA Nodes</th>
<th>Shared L3</th>
<th>Private L2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Haswell</td>
<td>Xeon E5-2680 v3</td>
<td>2 × 12 (2.5GHz)</td>
<td>4 × 32GB</td>
<td>4 × 15MB</td>
<td>24 × 256kB</td>
</tr>
<tr>
<td>Broadwell</td>
<td>Xeon E5-2650L v4</td>
<td>2 × 14 (1.7GHz)</td>
<td>4 × 16GB</td>
<td>4 × 18MB</td>
<td>28 × 256kB</td>
</tr>
<tr>
<td>Skylake</td>
<td>Xeon Gold 6140</td>
<td>2 × 18 (2.3GHz)</td>
<td>4 × 24GB</td>
<td>2 × 25MB</td>
<td>36 × 1024kB</td>
</tr>
</tbody>
</table>

![Figure 2: Application speedups with best- and worst-placement policies and placement sensitivity on the Skylake platform. Policies are noted [thread policy, data policy], with C for Compact, S for Scatter, F for Firsttouch, and I for Interleave.](image)

Table 5: Prediction accuracy of a basic prediction mechanism for sensitivity to placement. On the diagonal, maximum achievable accuracy ratio when predicting a constant output on a given machine. Out of the diagonal, accuracy ratio when assuming that all applications remain in the same class when changing the machine.

<table>
<thead>
<tr>
<th></th>
<th>Haswell</th>
<th>Broadwell</th>
<th>Skylake</th>
</tr>
</thead>
<tbody>
<tr>
<td>Haswell</td>
<td>0.59</td>
<td>0.74</td>
<td>0.67</td>
</tr>
<tr>
<td>Broadwell</td>
<td>-</td>
<td>0.41</td>
<td>0.85</td>
</tr>
<tr>
<td>Skylake</td>
<td>-</td>
<td>-</td>
<td>0.48</td>
</tr>
</tbody>
</table>

Table 6: Average speedup for placement-sensitive applications when applying the per-application best policy of machine A (rows) on machine B (columns). Obtained with the test set, which suggests that models are not overfitting.

<table>
<thead>
<tr>
<th></th>
<th>Haswell</th>
<th>Broadwell</th>
<th>Skylake</th>
</tr>
</thead>
<tbody>
<tr>
<td>Haswell</td>
<td>1.16</td>
<td>1.03</td>
<td>1.06</td>
</tr>
<tr>
<td>Broadwell</td>
<td>1.06</td>
<td>1.06</td>
<td>1.08</td>
</tr>
<tr>
<td>Skylake</td>
<td>1.10</td>
<td>1.04</td>
<td>1.12</td>
</tr>
</tbody>
</table>

Table 7: Average distance to the classification boundary of misclassified applications when predicting new applications only. Average distance to the classification boundary is reported per machine and type of model inputs (counters, instrumentation, all).

<table>
<thead>
<tr>
<th></th>
<th>Machine</th>
<th>Counters</th>
<th>Instrumentation</th>
<th>All</th>
</tr>
</thead>
<tbody>
<tr>
<td>Haswell</td>
<td>0.04</td>
<td>0.06</td>
<td>0.06</td>
<td>0.04</td>
</tr>
<tr>
<td>Broadwell</td>
<td>0.05</td>
<td>0.07</td>
<td>0.04</td>
<td>0.04</td>
</tr>
<tr>
<td>Skylake</td>
<td>0.05</td>
<td>0.07</td>
<td>0.02</td>
<td>0.02</td>
</tr>
</tbody>
</table>

Overall, detecting sensitivity to thread and data placement with the set of proposed parameters is not trivial. However, we achieved it with at least 75% accuracy, a significant improvement over basic strategies, and with errors on the least-sensitive applications. We also found that using hardware counters can provide performance similar to that with specific binary instrumentation. Thus, the most practical models, namely, those with low overhead application profiling, are satisfactory enough compared with more complex application characteristics. Moreover, these models are robust to new users out of the training context, namely, those with different applications and/or different processors with a close architecture.
First, model comparisons show that good results are achieved by mostly on applications that are barely sensitive to placement. In this case, the performance is only slightly improved compared with that of the baseline, which means that the 1% top models on the test set are all overfitting for this particular case.

Figure 6 shows that the overall efficiency remains valid in the case of generalization to both new applications and new machines at the same time. The distributions of model performance on test sets is presented in the first row. The second row shows the best model performance on the validation set after the model selection stage. These performances are to be compared with the upper and lower bound of achievable performance represented as top and bottom horizontal dashed lines, when always predicting respectively the best and worst placement policies for each application. The performance is also to be compared with the baseline where applications are run with the default placement policy. In columns, models are organized by training-to-prediction machine pairs. Model performances are presented considering three set of metrics for training: metrics based on hardware counters, metrics based on binary instrumentation, or both.

In Figure 6, predictions on the validation set reach near-optimal speedup for every machine. The results highlight the generality and practicability of the models. Indeed, we get very good speedups even when both the application and the machine are unknown, and with a low overhead profiling (i.e., hardware counters). There is a little discrepancy with hardware counters models in the couple Haswell, Skylake, which might be attributed to the greater difference between these two systems compared with other couples. The validation set performance is consistent with the performance achieved on the test set and shows that selected models are not likely to be overfitting.

6 CONCLUSION

At the scale of multisocket shared-memory NUMA platforms, thread and data placement matters for performance. However, finding an optimal strategy even with post mortem analysis is far from trivial. The difficulty arises from the numerous interactions and trade-offs in the whole memory hierarchy. Although some of these issues have been tackled in previous studies, improving placement decisions while considering several architectures and several sources of applications characterization had yet to be done.

In this paper we present a thorough modeling methodology with two main goals: (i) assessing the ability for metamodels to predict whether an application will at all be impacted by the placement of its threads and data and, in such a case, (ii) finding the best placement policy. We successfully realized both goals. We were able to train models that can predict the sensitivity of applications with an accuracy of more than 80%, wrong prediction occurring mostly on applications that are barely sensitive to placement. In all cases, we were also able to select a good placement policy and achieve almost optimal performance among the studied policies.

Our results show that the obtained models can be easily used in practice and are general enough to be used in many use cases. First, model comparisons show that good results are achieved by solely using hardware counters to collect metrics. Hence, models

![Figure 3: Accuracy on validation set, when predicting application sensitivity to data and threads placement.](image)

Out of the diagonal, models predict already seen applications but on a new machine (baseline: same answer on training platform and on prediction platform).

### 5.2 Preferred Policy Classification

Similarly to placement sensitivity detection, models are trained with the objective of choosing the preferred placement policy for sensitive applications. For this objective, we do not look at model accuracy but rather at prediction impact on application execution time. We consider that mistakes may be acceptable when they have little impact. The performance of models is therefore presented as the geometric mean of applications speedup using predicted policies; that is, it embeds a lower penalty if wrong choices have small impact on the execution time.

The performance of models when generalizing to new applications or to new platforms is shown in Figure 5. Similarly to Figure 3, results are organized in rows expressing the platform on which models were trained and columns on which the validation was done. On the diagonal, models were trained to predict new applications on a single platform; out of the diagonal, models were trained to predict the same applications on a different platform. In the first scenario, the application set is restricted to applications sensitive to threads and data and placement on a single machine. The upper bound represented as a top dashed line corresponds to average achieved speedup when always predicting best placement policies, and the baseline represented as the bottom dashed line corresponds to always picking the default placement policy. Out of the diagonal, the application set is restricted to applications that are sensitive to placement on at least one machine. In this case, the baseline is the achieved speedup when adopting a conservative policy selection.

Figure 5 exhibits very good model performance. Whether on a new application or a new platform, model predictions always outperform the baseline and consistently reach near-optimal placement policy choice. Moreover, this is true for all categories of input parameters except when using hardware counters to predict for new application on the Haswell machine. In this case, the performance is only slightly improved compared with that of the baseline, which means that the 1% top models on the test set are all overfitting for this particular case.
In the future, we would like to extend the applicability of the approach by adding more policies or by building models for different parallelism paradigms, for example, task-based programming. Our results also show that although hardware counters and binary instrumentation capture very different metrics, models based on each of these sources of data achieve similar performance. Furthermore, in many cases only a small number of parameter sets are needed for making good predictions. The question of understanding what are the best metrics to use to take placement decision should be investigated. Extending the study to dramatically different architectures such as AMD Zen or Intel Knights Landing is also of a great interest in order to increase the generality of the results.

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**REFERENCES**


Figure 6: Speedup obtained when predicting new application preferred execution policy on new machines. Results are detailed per training-to-prediction machine pairs and kind of input metrics. The first row displays all models distribution on the test set, while the second row displays the best model performance for each group on the validation set.