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Constructing Metrics for Evaluating Multi-Relational Association Rules in the Semantic Web from Metrics for Scoring Association Rules

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Abstract—We propose a method to construct asymmetric metrics for evaluating the quality of multi-relational association rules coded in the form of SWRL rules. These metrics are derived from metrics for scoring association rules. We use each constructed metric as a fitness function for evolutionary inductive programming employed to discover hidden knowledge patterns (represented in SWRL) from assertional data of ontological knowledge bases. This new knowledge can be integrated easily within the ontology to enrich it. In addition, we also carry out a search for the best metric to score candidate multi-relational association rules in the evolutionary approach by experiment. We performed experiments on three publicly available ontologies validating the performances of our approach and comparing them with the main state-of-the-art systems.

Keywords—Evolutionary Algorithms; Description Logics; Pattern Discovery

I. INTRODUCTION

The Semantic Web [1] (SW) has undergone a steady and continuous development toward its primary objective, which is to associate meaning with the data and to exploit the data through intelligent processing techniques. We refer to assertional and intensional definitions provided by ontologies as an *ontological knowledge base*. Currently, we can use data mining techniques to exploit and extract hidden knowledge patterns from ontological knowledge bases (KBs), even in incomplete and noisy ontologies. These knowledge patterns are used to enrich an ontology at both terminological (TBox) and assertional (ABox) level. Level-wise generate-and-test methods related to these data mining techniques were proposed in the inductive logic programming (ILP) [2], [3] and a recent approach that exploits the resoning capabilities of the SW, like [4]. In addition, EDMAR [5], an evolutionary inductive programming approach, was recently proposed to discover hidden knowledge patterns in the form of multi-relational association rules (ARs) coded in SWRL [6].

In this paper, we construct a method to change metrics for scoring ARs into metrics for evaluating SWRL rules, with the aim to increase the number of metrics to assess the SWRL rules. New metrics will be used as fitness function in EDMAR and applied to three publicly available ontological KBs.

Basics and definitions are provided in Section II and III. Section IV describes how to convert metrics and defines some typical metrics. The EDMAR algorithm is shown in Section V. Section VI reports on experiments to find out the best metric. Section VII concludes.

II. BASICS

We refer to ontological KBs in Description Logics (DLs) [7], which are a family of formal knowledge representation languages and are the theoretical foundation of OWL¹ (the standard representation language in the Semantic Web). A DL KB $\mathcal{K} = \langle \mathcal{T}, \mathcal{A} \rangle$ consisting of a TBox \mathcal{T} containing the terminological axioms and an ABox \mathcal{A} containing the assertional axioms. It should be recalled that DLs adopt the *open-world assumption* (OWA - a statement may be true irrespective of whether or not it is known to be true). For more details concerning DLs see [7]. In the following, we address the general definition of relational AR with respect to a given ontological KB.

Definition 1 (Relational Association Rule). Given a populated ontological KB $\mathcal{K} = (\mathcal{T}, \mathcal{A})$, a *relational association rule r* for \mathcal{K} is a Horn-like clause of the form: $body \rightarrow head$, where (a) body is a generalization of a set of assertions in \mathcal{K} co-occurring together; (b) head is a consequent that is induced from \mathcal{K} and body.

Definition 2 (Problem Definition). Given $\mathcal{K} = (\mathcal{T}, \mathcal{A})$, a minimum "frequency threshold", θ_f , and a minimum "fitness threshold", θ_{fit} , we desire to discover as many frequent and fit hidden patterns (w.r.t θ_f and θ_{fit}) as possible, in the form of relational ARs, that may induce new assertions for \mathcal{K} .

Intuitively, a frequent hidden pattern is a generalization of a set of concept/role assertions co-occurring reasonably often (w.r.t. a fixed frequency threshold) together, showing an underlying form of correlation that is exploited for obtaining new assertions.

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¹https://www.w3.org/OWL/.

The rules to be discovered (following Def. 2), will be represented in the Semantic Web Rule Language (SWRL) [6], which extends the set of OWL axioms with Horn-like rules.²

Definition 3 (SWRL Rule). Given a KB \mathcal{K} , a SWRL rule is an implication between an antecedent (body) and a consequent (head) of the form: $B_1 \wedge B_2 \wedge \ldots B_n \rightarrow H_1 \wedge \cdots \wedge H_m$, where $B_1 \wedge \cdots \wedge B_n$ is the rule body and $H_1 \wedge \cdots \wedge H_m$ is the rule head. Each $B_1, \ldots, B_n, H_1, \ldots, H_m$ is called an *atom*.

An *atom* is a unary or binary predicate of the form C(s), $R(s_1, s_2)$, where the predicate symbol C is a concept name in \mathcal{K} , R is a role name in \mathcal{K} , s, s_1, s_2 are *terms*. A *term* is either a variable (denoted by x, y, z) or a constant (denoted by a, b, c) standing for an individual name or data value.

The discovered rules can be generally called *multi-relational* rules since multiple binary predicates $R(s_1, s_2)$ with different role names of \mathcal{K} could appear in a rule. The intended meaning of a rule is: whenever the conditions in the antecedent hold, the conditions in the consequent must also hold. A rule having more than one atom in the head can be equivalently transformed, due to the *safety condition* (see Def. 4), into multiple rules, each one having the same body and a single atom in the head. Therefore, we will consider, w.l.o.g., only SWRL rules (hereafter just "rules") with one atom in the head.

III. LANGUAGE BIAS

From Def. 3, we realize that we might generate a multitude of SWRL rules with respect to a given ontological KB. In order to avoid generating trivial rules (e.g., $Male(x) \rightarrow Man(x)$), redundant rules (e.g., fatherOf $(y, x) \rightarrow Male(y)$) or meaningless rules (e.g., fatherOf $(y, x) \rightarrow parentOf(u, v)$), we fix the language bias.

A language bias is a set of constraints giving a tight specification of the patterns worth considering, thus allowing to reduce the search space. Following [5], we are interested in rules having only atomic concepts and/or role names of \mathcal{K} as predicate symbols, and individual names as constants. Only connected [8] and non-redundant [9] rules satisfying the safety condition [6] are considered.

Given an atom A, let T(A) denote the set of all the terms occurring in A and let $V(A) \subseteq T(A)$ denote the set of all the variables occurring in A e.g. $V(C(x)) = \{x\}$ and $V(R(x, y)) = \{x, y\}$. Such notation may be extended to rules straightforwardly.

Definition 4 (Safety Condition). Given a KB \mathcal{K} and a rule $r = B_1 \wedge B_2 \wedge \ldots B_n \rightarrow H$, r satisfies the *safety condition* if all variables appearing in the rule head also appear in the rule body; formally if: $V(H) \subseteq \bigcup_{i=1}^n V(B_i)$,

Definition 5 (Connected Rule). Given a KB \mathcal{K} and a rule $r = B_1 \wedge B_2 \wedge \ldots B_n \rightarrow H$, r is *connected* if and only if every atom in r is transitively connected to every other atom in r.

Two atoms B_i and B_j in r, with $i \neq j$, are *connected* if they share at least a variable or a constant i.e. if $T(B_i) \cap T(B_j) \neq \emptyset$. Two atoms B_1 and B_k in r are transitively connected if there exist in r, atoms B_2, \ldots, B_{k-1} , with $k \leq n$, such that, for all $i, j \in \{1, \ldots, k\}$ with $i \neq j$, $T(B_i) \cap T(B_j) \neq \emptyset$.

Definition 6 (Closed Rule). Given a KB \mathcal{K} and a rule $r = B_1 \wedge B_2 \wedge \ldots B_n \rightarrow H$, r is closed if and only if every variable in r is closed.

Each variable $v_j \in \bigcup_{i=1}^n V(B_i), j \in \{1, \ldots, k\}$, with $k \leq n$, is closed if it appears at least twice in r.

Definition 7 (Redundant Rule). Given a KB \mathcal{K} and a rule $r = B_1 \wedge B_2 \wedge \ldots B_n \to H$, r is a redundant rule if at least one atom in r is entailed by another atom in r with respect to \mathcal{K} , i.e., if, $\exists i \in \{0, 1, \ldots, n\}, \exists j \in \{0, 1, \ldots, n\}$, with $B_0 = H$, results: $B_j \models_{\mathcal{K}} B_i, i \neq j$

IV. METRICS FOR RULE EVALUATION

We notice that the generated rules satisfying the language bias in Section III are definitely not trivial, redundant and meaningless. However, the language bias might not guarantee the quality of generated rules. Therefore, we use metrics that are a data-driven approach for assessing the quality of rules. For each metric, a threshold is used to filter low-quality rules.

So far, only a few metrics introduced in [8] and [5] are used to evaluate the quality of SWRL rules. In this paper we propose a solution that is using metrics employed for evaluating the quality of ARs to assess the quality of SWRL rules. With this solution, we might increase the number of metrics to assess the SWRL rules and in addition also support other studies related to the evaluation of SWRL rules.

A. Computing Metrics for Association Rules

All metrics used to evaluate ARs are computed based on the frequency counts tabulated in Table I.

TABLE I.	A CONTINGENCY TABLE FOR THE ASSOCIATION RULE
	$X \to Y$

	Y	\overline{Y}	
X	f_{11}	f_{10}	f_{1+}
\overline{X}	f_{01}	f_{00}	f_{0+}
	f_{+1}	f_{+0}	N

Table I includes two itemsets X, Y, where X is called antecedent and Y is called consequent; \overline{X} (resp. \overline{Y}) stands for an itemset that does not contain items in the itemset X (Y) for a transaction; f_{11} is the number of times transactions contain items in both X and Y; f_{1+} counts the number of transactions that contain items in X; f_{+1} counts the number of transactions. From the four values of f_{11} , f_{1+} , f_{+1} and N, we can calculate the remaining values in the contingency table. For example, f_{10} is the number of transactions that contain items in X but not in Y and $f_{10} = f_{1+} - f_{11}$.

B. Computing Metrics for SWRL Rules

In order to build metrics for assessing SWRL rules derived from metrics for evaluating ARs, we also need to build a contingency table based on frequency counts. However, instead

²The result is a KB with an enriched expressive power. More complex relationships than subsumption can be expressed.

TABLE II. A CONTINGENCY TABLE FOR THE SWRL RULE $B \rightarrow H$

	Н	\overline{H}	
B	$E_H(r)$	f_{10}	$M_H(r)$
\overline{B}	f_{01}	f_{00}	f_{0+}
	$\Sigma_H(r)$	f_{+0}	N

of counting the number of transactions, we count the number of bindings of variables to individuals in the KB.

The entries in Table II are used to aid in the construction of the metrics for assessing SWRL rules. As in Table I, we only need to obtain the four values $E_H(r)$, $M_H(r)$, $\Sigma_H(r)$ and N, the remaining values being easy to compute based on these values.

Definition 8 (Binding). A binding is a mapping from a set of variables to a set of named individuals that occur in at least one assertion in the ABox.

Given a rule $r = B_1 \land \ldots \land B_n \to H$, let us denote:

- $\Sigma_H(r)$ the set of distinct bindings of the variables occurring in the head of r, formally: $\Sigma_H(r) = \{binding V(H)\}$
- *E_H(r)* the set of distinct bindings of the variables occurring in the head of *r* provided the body and the head of *r* are satisfied, formally: *E_H(r)* = { binding *f* of *V*(*H*) | there is a binding *f*' of *V*(*B*₁ ∧ · · · ∧ *B_n*) that extends *f*, such that *f'*(*B*₁ ∧ · · · ∧ *B_n* ∧ *H*) is satisfied}. Since the rules satisfy the safety condition, *V*(*H*) ⊆ *V*(*B*₁ ∧ · · · ∧ *B_n*)
- M_H(r) the set of distinct bindings of the variables occurring in the head of r also appearing as binding for the variables occurring in the body of r (since the rules satisfy the safety condition), formally:
 M_H(r) = { binding f of V(H) | there is a binding f' of V(B₁ ∧ · · · ∧ B_n) that extends f, such that f'(B₁ ∧
- Σ_i total number of individuals inside a KB.

 $\cdots \wedge B_n$) is satisfied}.

• The rule head of r might be either a concept atom or a role atom. Therefore, N is a number defined as follows:

follows: $N = \begin{cases} \Sigma_i, & \text{if } H \text{ is a concept atom;} \\ P_{\Sigma_i}^2 = \Sigma_i(\Sigma_i - 1), & \text{if } H \text{ is a role atom;} \end{cases}$ This, implicitly, assumes a role cannot be reflexive.

There are two kinds of metrics: symmetric and asymmetric metrics. In our work, we focus only on introducing asymmetric metrics that are suitable for assessing rules coded in SWRL, because SWRL rules have the general form $B \rightarrow H$ and values of an asymmetric metric for $B \rightarrow H$ and $H \rightarrow B$ may not be the same. We do not use symmetric metrics because these are only appropriate for evaluating itemsets of the form $B \wedge H$, which is equivalent to $H \wedge B$, without any distinction between antecedent and consequent.

Following [8], we redefine a few basic definitions of asymmetric metrics through the entries of Table II for use in the experiments (Sec. VI). These definitions are modified from

the classical ones (as given e.g. in [10]) to ensure they fit the case of SWRL rules.

Definition 9 (Rule Support). Given a rule $r = B_1 \land \ldots \land B_n \rightarrow H$, its support is the number of distinct bindings of the variables in the head, provided the body and the head of r are satisfied jointly, formally:

$$\operatorname{supp}(r) = |E_H(r)|. \tag{1}$$

Definition 10 (Head Coverage for a Rule). Given the rule $r = B_1 \land \ldots \land B_n \rightarrow H$, its head coverage is the ration between the rule support and the distinct variable bindings from the head of the rule

headCoverage
$$(r) = \frac{|E_H(r)|}{|\Sigma_H(r)|}.$$
 (2)

Definition 11 (Rule Confidence). Given a rule $r = B_1 \land \ldots \land B_n \rightarrow H$, its confidence is defined as the ratio of the number of the rule support and the number of bindings in the rule body:

$$conf(r) = \frac{|E_H(r)|}{|M_H(r)|}.$$
(3)

Definition 12 (Rule PCA-Confidence). Given the rule $r = B_1 \land \ldots \land B_n \rightarrow H$, its PCA (Partial Completeness Assumption) confidence is defined as follows:

$$pcaconf(r) = \begin{cases} \frac{|E_H(r)|}{|M_H(r)|}, & \text{if } H \text{ is a concept atom;} \\ \frac{|E_H(r)|}{|P_H(r)|}, & \text{if } H \text{ is a role atom,} \end{cases}$$
(4)

where $P_H(r)$ is the set of distinct bindings of the variables occurring in the head of r provided that the body and the head of r are satisfied. In particular, this applies when a role atom is in the head of the considered rule. Formally: $P_H(r) =$ $\{binding V(H) \mid \exists binding V(B_1 \land \cdots \land B_n) \cup v_{rng}(H') :$ $B_1 \land \cdots \land B_n \land H'\}$, where

- *H* and *H'* are role atoms with the same predicate symbol *R*;
- $V(H) \subseteq V(B_1 \land \dots \land B_n)$ since rules are connected and closed
- $v_{dom}(H) = v_{dom}(H')$ and $v_{rng}(H) \neq v_{rng}(H')$; with v_{dom} and v_{rng} standing for the domain and range variables respectively of the predicate symbol R

•
$$v_{rng}(H') \notin V(B_1 \wedge \cdots \wedge B_n).$$

Definition 13 (Certainty Factor for a Rule). Given a rule $r = B_1 \land \ldots \land B_n \rightarrow H$, its Certainty Factor [11] represents uncertainty in the rule and is defined as follows:

$$\operatorname{cf}(r) = \begin{cases} \frac{\operatorname{conf}(r) - \frac{|\Sigma_H(r)|}{N}}{1 - \frac{|\Sigma_H(r)|}{N}}, & \text{if } \operatorname{conf}(r) > \frac{|\Sigma_H(r)|}{N} ;\\ \frac{\operatorname{conf}(r) - \frac{|\Sigma_H(r)|}{N}}{\frac{|\Sigma_H(r)|}{N}}, & \text{if } \operatorname{conf}(r) < \frac{|\Sigma_H(r)|}{N} ;\\ 0, & \text{if } \operatorname{conf}(r) = \frac{|\Sigma_H(r)|}{N} . \end{cases}$$
(5)

Definition 14 (Added Value for a Rule). Given a rule $r = B_1 \land \ldots \land B_n \rightarrow H$, Added Value [12] for the rule r is defined as:

$$\operatorname{av}(r) = \operatorname{conf}(r) - \frac{|\Sigma_H(r)|}{N} \tag{6}$$

This metric is more meaningful when the amount of evidence is large, for it relies on probabilities.

C. Metrics for Evaluating Rule Precision

Definition 15 (Rule Precision). Given the rule $r = B_1 \land \ldots \land B_n \rightarrow H$, its *precision* is the ratio of the number of correct predictions made by r and the total number of correct and incorrect predictions (predictions logically contradicting \mathcal{K}), leaving out the predictions with unknown truth value.

This metric expresses the ability of a rule to perform correct predictions, but it is not able to take into account the induced knowledge, that is the *unknown* predictions. For this reason, the metrics proposed in [13] are also considered (for the evaluation in Sect. VI):

- *match rate*: number of predicted assertions in agreement with facts in the complete ontology, out of all predictions;
- *commission error rate*: number of predicted assertions contradicting facts in the full ontology, out of all predictions;
- *induction rate*: number of predicted assertions that are not known in the complete ontology, out of all predictions.

V. THE EDMAR ALGORITHM

Here, we use the EDMAR (Evolutionary Discovery of Multi-relational Association Rules) algorithm represented in [5]. All the proposed metrics in this paper are in turn used as fitness function in EDMAR algorithm.

VI. EXPERIMENTS AND RESULTS

We carry out a comparison of the best asymmetric metrics [14] with a combination of them. The comparative criteria are based on the number of discovered rules, the number of unknown facts and the number of correct predictions. This comparison is created with the desire to figure out a new metric that is better than the metrics in [14]. The idea of this solution is that the metric combined by the best metrics might obtain discovered rules which satisfies at least one of the best metrics but may not satisfy the remaining metrics.

The EDMAR algorithm is applied to the same publicly available ontologies used in [15]: Financial,³ describing the banking domain; Biological Pathways Exchange (BioPAX),⁴ describing biological pathway data; and New Testament Names Ontology (NTNMerged),⁵ describing named entities in the New Testament. Details in Table V.

In order to assess the ability of the discovered rules to predict new assertional knowledge for a considered ontological KB, for each ontology in Table V, we construct three stratified samples by randomly removing respectively 20%, 30%, 40% of the concept assertions and eliminating role assertions or assertional axioms that involve the removed concept assertions, while the full ontology has been used as a testbed.

We carried out 30 runs of the EDMAR algorithm (cf. Sect. V) for each stratified sample and for each choice of fitness function using the following parameter setting:

n	=	5,000;	$p_{\rm mut}$	=	5%;
MAX_GENERATIONS	=	200;	$ heta_{ m mut}$	=	0.2;
MAX_RULE_LENGTH	=	10;	au	=	$\frac{1}{5}$
$ heta_{ m fit}$	=	0	θ_{f}	=	Ĭ.

Our experiments aimed at comparing the results obtained by the EDMAR algorithm using the five best asymmetric metrics evaluated by [14] (*HeadCoverage*, *Confidence*, *PCA-Confidence*, *Certainty Factor*, *Added Value*) and the metric *Combination*_{metrics}(r) which is a combination of these five metrics (*Combination*_{metrics}(r) = *HeadCoverage*(r) + *Confidence*(r) + *PCA-Confidence*(r) + *Certainty Factor*(r) + *Added Value*(r)). These six metrics are used as fitness function in EDMAR algorithm and the comparison is based on the three following criteria:

- 1) The number of the rules discovered by the EA.
- 2) The *induction rate*: if it is positive, this means assertions are predicted that could not be inferred from the stratified version. The higher the induction rate, the more novel predictions (unknown facts) are induced for the KB.
- The number of correct predictions = number of predictions × precision, where the number of predictions is the number of predicted assertions and precision is defined in Def. 15.

In order to compare the metrics according to these criteria, we applied the rules discovered from the stratified samples to the full ontology versions and collected all predictions, that is the head atoms of the instantiated rules. All predictions already contained in the stratified ontology versions have been discarded while the remaining predicted facts have been considered. A prediction is regarded as *correct* if it is contained/entailed by the full ontology version and as *incorrect* if it is inconsistent with the full ontology version. Results in Table IV have been averaged over 30 different runs with the above parameter setting and have been measured in terms of *precision* (Def. 15), *match rate*, *commission error rate*, and *induction rate* (Sect. IV-C).

Table III shows a comparison of the metrics according to the first criterion. The second and third criteria are used to compare the predictive power of the discovered rules and are shown in Table IV. From the observations in Tables III and IV, we might draw a few remarks:

- The EDMAR algorithm confirms its ability to discover accurate rules (*precision* = match rate + commission rate + induction rate = 1) and no contradicting knowledge is predicted (commission error rate = 0) on all versions of all considered ontologies.
- The combined metric (CM) allows EDMAR to discover the largest number of rules (Tab. III) along with the largest number of correct predictions (Tab. IV) in NTNMerged that is the ontology containing the largest number of individuals (see Table V). In addition, this metric comes up with rules that induce a large number of previously unknown facts (induction rate > 0).

We may see that the fitness function $Combination_{metrics}(r)$ of EDMAR outperforms each

³http://www.cs.put.poznan.pl/alawrynowicz/financial.owl.

⁴http://www.biopax.org/release/biopax-level2.owl.

⁵http://www.semanticbible.com/ntn/ntn-view.html.

TABLE III. COMPARISON OF THE METRICS BY THE NUMBER OF DISCOVERED RULES.

HEADCOVERAGE (H), CONFIDENCE (C), PCA-CONFIDENCE (P), CERTAINTY FACTOR(CF), ADDED VALUE(AV) AND COMBINATION OF FIVE METRICS (CM)

Ont	ç	Total	Total number of discovered rules by metric \pm stdev				
Ont.	5.	Н	С	Р	CF	А	CM
	%	26	25	25	25	26	25
al	20	± 4	± 4	± 3	± 3	± 3	± 4
nci	%(25	25	25	26	24	26
ina	30	± 3	± 4	± 4	± 3	± 4	± 5
Ľ.	9%	23	23	22	23	21	22
	4	± 3	± 3	± 4	± 4	± 3	± 4
	%	129	122	130	118	119	119
×	50	± 13	± 12	± 10	± 9	± 9	± 8
3iopa:	%	128	130	130	117	110	117
	30	± 9	± 13	± 9	± 8	± 9	± 8
	%(129	136	133	124	122	126
	40	± 11	± 11	± 8	± 9	± 7	± 7
-	%	1,157	1,345	1,418	671	656	2,118
50	50	± 168	± 423	± 492	\pm 36	\pm 34	\pm 1,082
Aer	%(1,052	947	1,017	743	728	1,719
2	3(± 353	± 238	± 370	\pm 45	± 48	\pm 840
L F	%(1,088	1,223	1,295	687	664	1,527
	40	± 181	± 177	± 357	± 38	± 34	± 497

of the five best metrics and is the best choice as an optimization criterion (i.e., fitness function) for EDMAR.

In addition, we also notice that the rate of removing concept assertions, does not affect the number of discovered rules from ontological knowledge bases (Tab. III).

We also compared the experimental performance of the EDMAR algorithm using $Combination_{metrics}(r)$ with the two level-wise generate-and-test algorithms RARD [4] and AMIE [8], which are closest to it in purpose. Table VI reports the number of rules discovered by each system given each knowledge base sample. We did not compare the second and third criteria because the maximum length of a rule in EDMAR is different from RARD and AMIE. We may remark the following:

- The metric *Combination_{metrics}(r)* discovers more rules than RARD from NTNMerged, but fewer from the Financial and Biopax KBs. One reason is that EDMAR does not generate *open* rules as RARD; in addition, the maximum length of a rule in EDMAR is 10 atoms while in RARD is 3 atoms. Another reason is that the number of individuals in Financial and Biopax is less than that of NTNMerged.
- The metric $Combination_{metrics}(r)$ is superior to AMIE because it discovers more rules than AMIE from all three KBs, although the rules discovered by AMIE can be inconsistent with KBs and the maximum length of a rule in AMIE is 3 atoms.

VII. CONCLUSIONS

We have shown a method to convert metrics for scoring ARs into metrics for assessing SWRL rules. In addition, we figured out the best metric to score candidate multi-relational association rules in the evolutionary approach by comparison experiment.

Future work might focus on developing other metrics suited for scenarios based on the OWA.

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	Ont	Samp.	Match	Com.	Ind.	Total #	
	Ont.		Rate	Rate	Rate	Predictions	
		20%	0.855	0	0.145	47,232	
	[a]	20 %	± 0.033		± 0.033	\pm 36,777	
nci	30%	0.864	0	0.136	25,456		
	ina	30%	± 0.044		± 0.044	\pm 34,174	
	Ē	400%	0.861	0	0.139	23,207	
		40%	± 0.044		± 0.044	\pm 30,133	
		2007	0.567	0	0.433	84,035	
	×	20%	± 0.031		± 0.031	$\pm 15,018$	
п	A	200%	0.591	0	0.409	85,499	
п	[ii	30%	± 0.03		± 0.03	$\pm 11,660$	
		400%	0.58	0	0.42	90,856	
		40%	± 0.027		± 0.027	$\pm 14,048$	
		200%	0.572	0	0.428	2,311,624	
	6 6	20%	± 0.026		± 0.026	\pm 287,858	
	Ier	2007	0.564	0	0.436	2,314,346	
	ź	50%	± 0.039		± 0.039	\pm 458,522	
	F	4007	0.621	0	0.379	2,345,588	
	-	40%	± 0.027		± 0.027	\pm 357,565	
		2007	0.848	0	0.152	43,151	
	ਿਤ	20%	± 0.045		± 0.045	$\pm 44,254$	
	JCi	200	0.860	0	0.140	27,589	
	nai	30%	± 0.038		± 0.038	$\pm 41,184$	
	E	10.07	0.858	0	0.142	33,795	
		40%	± 0.051		± 0.051	± 41.880	
		2007	0.574	0	0.426	79,454	
	~	20%	± 0.036		± 0.036	± 14.019	
	A	200	0.584	0	0.416	88,879	
С	ioF	30%	± 0.027		± 0.027	± 12.890	
	<u>م</u>	m 4007	0.582	0	0.418	96,884	
	40%	40%	± 0.023		± 0.023	$\pm 13,782$	
	_	2007	0.618	0	0.382	1,437,868	
	Sec	20%	± 0.042		± 0.042	$\pm 253,206$	
	ler	200	0.581	0	0.419	1,164,306	
	È	30%	± 0.036		± 0.036	\pm 167,173	
	E	10.07	0.670	0	0.330	1,557,516	
	2	40%	± 0.030		± 0.030	\pm 280.666	
			0.859	0	0.141	41.350	
	12	20%	± 0.055		± 0.055	± 46.196	
	lci,	l lici		0.850	0	0.150	32.812
	nar	30%	± 0.055		± 0.055	± 41.501	
	Ē	10.00	0.859	0	0.141	29,762	
		40%	± 0.043		± 0.043	± 35.582	
			0.571	0	0.429	89,486	
	_	20%	+ 0.028		+ 0.028	+ 11.303	
_	A)		0.584	0	0.416	92.392	
BioP d	30%	+ 0.023		+ 0.023	+ 13.878		
		0.587	0	0.413	91 849		
	40%	+ 0.027		+ 0.027	+ 11.960		
	-	0.609	0	0.391	2 130 947		
	ed	20%	+ 0.046		+ 0.046	+ 380.546	
	erg		0.588	0	0.412	1.409.235	
	μ Μ	30%	+0.043		+ 0.043	+ 286439	
		F	0.670	0	0 330	1.727 343	
	z	40%	+0.042		+0.042	+ 262.891	
	1	1	1 - 0.0.2		0.0.2		

 TABLE IV.
 AVG (± ST.DEV.) PERFORMANCE ON EACH ONTOLOGY OF HEADCOVERAGE (H), CONFIDENCE (C), PCA-CONFIDENCE (P), CERTAINTY

 FACTOR(CF), ADDED VALUE(AV) AND COMBINATION OF FIVE METRICS (CM)

 precision = match rate + commission rate + induction rate

	Ont	Samp.	Match	Com.	Ind.	Total #
	Ont.		Rate	Rate	Rate	Predictions
		2007-	0.877	0	0.123	31,656
	al	20%	± 0.038		± 0.038	\pm 45,045
	nci	200%	0.852	0	0.148	48,568
	ina	30%	± 0.057		± 0.057	\pm 45,051
	Щ	40%	0.857	0	0.143	31,068
		40 /0	± 0.039		± 0.039	\pm 36,044
		20%	0.556	0	0.444	80,361
	×	20 10	± 0.026		± 0.026	\pm 8,700
CE	PA	30%	0.581	0	0.419	78,933
CI	Sio	50%	± 0.023		± 0.023	$\pm 11,147$
	щ	40%	0.564	0	0.436	84,476
		40 /0	± 0.035		± 0.035	\pm 12,647
	p	20%	0.565	0	0.435	1,039,112
	66	20 /0	± 0.01		± 0.01	\pm 179,322
	Aeı	30%	0.535	0	0.465	1,424,334
	ź	30%	± 0.014		± 0.014	\pm 180,205
	Ę	40%	0.557	0	0.443	2,110,928
		40 /0	± 0.018		± 0.018	\pm 423,539
		200%	0.859	0	0.141	33,358
	al	20%	± 0.041		± 0.041	\pm 31,445
	nci	2007-	0.858	0	0.142	29,866
	ina	50%	± 0.041		± 0.041	\pm 31,123
	Ē	400	0.859	0	0.141	29,870
		40%	± 0.041		± 0.041	\pm 44,276
		20%	0.549	0	0.451	83,666
	×		± 0.032		± 0.032	$\pm 11,663$
	E.		0.578	0	0.422	78,059
A Ioi	loi	50%	± 0.029		± 0.029	$\pm 9,368$
	щ	400%	0.579	0	0.421	84,483
		40%	± 0.02		± 0.02	$\pm 10,376$
	ъ	2007-	0.563	0	0.437	966,840
	ee ee	20%	± 0.012		± 0.012	\pm 204,430
	Ieı	30%	0.541	0	0.459	1,324,518
	ź	30%	± 0.014		± 0.014	\pm 282,410
	Ę	400%	0.566	0	0.434	1,632,633
		40 /0	± 0.014		± 0.014	\pm 218,033
		2007-	0.861	0	0.139	37,766
	al	20%	± 0.046		± 0.046	\pm 44,986
	nci	200%	0.876	0	0.124	28,245
	ina	30%	± 0.043		± 0.043	\pm 33,875
	Ē	400	0.855	0	0.145	38,415
		40%	± 0.053		± 0.053	\pm 42,710
		200%	0.555	0	0.445	82,398
	×	20%	± 0.024		± 0.024	$\pm 11,717$
CM	BA	200	0.576	0	0.424	83,524
CIVI	[o]	50%	± 0.028		± 0.028	$\pm 13,986$
-	щ	400	0.576	0	0.424	90,496
		40%	± 0.026		± 0.026	\pm 12,094
	-	200	0.664	0	0.336	3,254,323
	ee ee	20%	± 0.06		± 0.06	\pm 751,324
	Aer	200%	0.628	0	0.372	3,043,882
	ź	50%	± 0.061		± 0.061	$\pm 627,598$
	Ę	40.07	0.672	0	0.328	3,404,974
	~	40%	± 0.055		± 0.055	\pm 491,617

TABLE V. KEY FACTS ABOUT THE ONTOLOGICAL KBS USED.

Ont.	# Con.	# Rol.	# Indiv.	# Declared	# Decl.+Derived
				Assertions	Assertions
Finan	59	16	1000	3359	3814
Bio	40	33	323	904	1671
NTM	47	27	695	4161	6863

TABLE VI. COMPARISON OF THE NUMBER OF DISCOVERED RULES.

Ontology	Samp	# The total number of rules discovered					
Ontology	Samp.	CM	RARD	AMIE			
	20%	25 ± 4	177	2			
Financial	30%	26 ± 5	181	2			
	40%	22 ± 4	180	2			
	20%	119 ± 8	298	8			
Biopax	30%	117 ± 8	283	8			
	40%	126 ± 7	272	0			
NTNMerged	20%	$2,118 \pm 1,082$	243	1,129			
	30%	$1,719 \pm 840$	225	1,022			
	40%	$1,527 \pm 497$	239	1,063			