

Mathematical Modeling and Prediction of Clinical Metastasis

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Mathematical Modeling and Prediction of Clinical Metastasis

S. Benzekry

BIRS - CMO workshop Oaxaca, Mexico

November 27, 2018

Metastasis (μετά = beyond, στάσιζ = place)

Metastases are the main cause of death (>90%) from solid cancers Lambert and Weinberg, Cell, 2017





Breast

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- 94% of cases are local or regional at diagnosis but 30% will relapse Pollard, N Eng J Med, 2016
- Estimate the amount of residual distant disease at diagnosis in order to personalize the adjuvant (chemo)-therapy
- Avoid unnecessary, heavy toxicities
- Lung
 - 57% of cases are metastatic
 - Decide whether to use whole brain radiation therapy or just (stereotactic) surgery
 - · Avoid cognitive impairment of the patient



Institut Bergonié, Bordeaux

Some biological questions of interest to mathematical modeling

Minimal model of metastatic dissemination and colonization able to reproduce the **systemic** dynamics of a solid cancer disease

- Investigate the relevance of several processes:
 - (early VS late event Klein, Nat Rev Cancer, 2009)
 - (metastases of metastases Gundem et al., Nature, 2015)
 - (dormancy Chambers and Groom, Nat Rev Cancer, 2002)
 - tumor-tumor interactions

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- (cancer-immune interactions)
- differential effect of therapy Ebos et al. (Kerbel), Cancer Cell, 2009
- ((pre-)metastatic niche Peinado et al. (Lyden), Nature, 2005)
- systemic inhibition of angiogenesis O'Reilly et al. (Folkman), Cell, 1990s
- (self-seeding Norton, Nat Med, 2001)

Metastasis: a forgotten major player in modeling

- The majority of mathematical modeling efforts in oncology are focused on (primary) tumor growth
- Existing models are based on a statistical, biologically agnostic, prediction of survival



Metastasis: a forgotten major player in modeling

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Prediction

Outline

1. Modeling the dynamics of **metastatic burden** in clinically relevant ortho-surgical animal systems

2. Clinical applications

3. Tumor-tumor interactions

1. Modeling the dynamics of metastatic burden in clinically relevant ortho-surgical animal systems

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Experimental data and questions



Data

- Clinically relevant ortho-surgical animal models
 of metastasis
- Longitudinal measurements of primary tumor size and total metastatic burden
- n > 400 animals

Questions

- Minimal model of metastatic development.
 Dissemination law? Differences between mets and primary tumor growth?
- Quantify the inter-subject variability of metastatic development
- What is the impact of the primary tumor size at surgery on metastatic development and survival?





Dr Ebos' lab, Roswell Park Cancer Institute

Metastatic burden (cells)





Statistical procedure: nonlinear mixed effects modeling

Usual fitting methods consider each time series independently

 When only sparse data are available from subjects in the same population, one can fit parameters distribution all-in-once

$$y_i^j = M(t_i^j, \theta^j) + \varepsilon_i^j$$

$$\theta^1, \ldots, \theta^N \sim \mathcal{LN}(\theta_\mu, \theta_\omega), \quad \theta_\mu \in \mathbb{R}^p, \ \theta_\omega \in \mathbb{R}^{p \times p}$$



Lavielle, CRC press, 2014

Reduces the number of parameters from pxN to p+p2

The model fits at the individual and population levels

Metastatic burden (cells

104

60 70







Fit

Primary tumor size (cells)



Nonlinear mixed-effects statistical model for inter-animal variability

$$\theta^i = \theta_{pop} + \eta_i, \quad \eta_i \sim \mathcal{N}(0, \omega^2)$$

 \Rightarrow model with same growth for PT and mets was the most parsimonious

 \Rightarrow good practical identifiability (all rse < 30%)

 \Rightarrow parameter μ is a critical coefficient of interanimal variability of metastatic potential (CV = 176%)

Benzekry et al. (Ebos), Cancer Res, 2016

Differential effects of anti-angiogenic therapies between primary tumor and metastases



Cancer Cell Report

Accelerated Metastasis after Short-Term Treatment with a Potent Inhibitor of Tumor Angiogenesis

John M.L. Ebos,^{1,2} Christina R. Lee,¹ William Cruz-Munoz,¹ Georg A. Bjarnason,³ James G. Christensen,⁴ and Robert S. Kerbel^{1,2,*}



John M L Ebos^{1,*}, Michalis Mastri¹, Christina R Lee², Amanda Tracz¹, John M Hudson², Kristopher Attwood³, William R Cruz-Munoz², Christopher Jedeszko², Peter Burns^{2,4} & Robert S Kerbel^{2,4}

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Testing hypotheses for Sunitinib effect



A validated model of metastatic growth with neoadjuvant Sunitinib therapy



Survival model: *µ* as a covariate



Nicolo et al. (Ebos, Benzekry), 2018, in preparation

Trying to predict *µ* from biomarkers using machine learning



2.5

Biological measurements on multiple biomarkers

Nicolo et al. (Ebos, Benzekry), 2018, in preparation

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Impact of treatment breaks



2. Clinical application



Metastatic relapse probability in a breast cancer clinical dataset

Diameter of PT (cm)	Prop. of relapse (Data)	Prop. of relapse (Model)
$1 \le D \le 2.5$	27.1	27.3
$2.5 < D \le 3.5$	42.0	43.1
$3.5 < D \le 4.5$	56.7	56.6
$4.5 < D \le 5.5$	66.5	65.6
$5.5 < D \le 6.5$	72.8	74.0
$6.5 < D \le 7.5$	83.8	80.1
$7.5 < D \le 8.5$	81.3	84.5

- 20 year follow-up of 2648 patients *Koscielny et al., Br J Cancer, 1984*
- Assumptions
 - (lognormal) distribution of µ for interindividual variability
 - Doubling time from median values of the literature (7 months) *Coumans et al., BMC Cancer 2013*
 - Maximal reachable size = 10¹² cells ≃ 1 kg
 Klein, Nat Rev Cancer, 2009
- Probability of developing a met = probability of having one at diagnosis

$$\mathbb{P}(\mathsf{Mets}) = \mathbb{P}\left(\mu \int_0^{\tau_1} V_{\rho}(t) > 1\right)$$

Benzekry et al. (Ebos), Cancer Res, 2016



Diagnosis personalization



Breast cancer patient with primary tumor of 4.32 cm

Data of a NSCLC patient with brain mets



Lung CT

Brain CT scan





Different biological scenarii



The model with dormancy could describe best the data



Objective function

Model	Patient 1	Patient 2
Base	5.51	2.53
Secondary	5.43	2.3
Delay	5.23	1.53
Dormancy	4.93	1.71
Diff. growth	4.95	1.79

Dormancy estimated to 133 days $\pm 4.2\%$



Bilous et al. (Benzekry), biorXiv, 2018



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Primary tumor (lung) Metastases (brain)

Bilous et al. (Benzekry), biorXiv, 2018







3. Tumor-tumor interactions: a dynamical study of

concomitant resistance



Concomitant tumor resistance

- Inhibition of secondary growth by a primary mass
- Critical clinical implications in terms of **post-surgery metastatic acceleration**



O'Reilly et al. (Folkman), Cell, 1994



Questions and experiment

Questions

- Quantitatively distinguish between qualitatively valid theories of tumortumor interactions
- Establish and validate a minimal model able to simulate tumor-tumor interactions

Experiment

- Injection s.c. of two tumors of 10⁶ LLC cells in C57/BL6 mice
- Two groups
 - Control: only one tumor
 - Group S: **simultaneous** injection of cells in two different sites

A mouse with two tumors



One tumor has normal growth and the other is suppressed

Individual growth kinetics

Small/Large in two-tumor bearing animals VS artificially paired small/large controls



Benzekry et al. (Hahnfeldt), Cancer Res, 2017

Two-tumors models

• Requirements:

- Symmetry: same parameters for tumor 1 and tumor 2
- Should resume to **single tumor growth** in the absence of the other tumor
- Main assumption for the difference between the two tumors: difference in **the initial take** ($V_{0,1}$ = 1, $V_{0,2}$ = 0.75)
- Difference in the growth kinetics should not result from difference in V_0
- Model selection (rejection) criteria: goodness-of-fit + parameter identifiability

Competition

$$\begin{cases} \frac{dV_1}{dt} = aV_1 \ln\left(\frac{K}{V_1 + V_2}\right), & V_1(t=0) = V_{0,1} \\ \frac{dV_2}{dt} = aV_2 \ln\left(\frac{K}{V_1 + V_2}\right), & V_2(t=0) = V_{0,2} \end{cases}$$

Angiogenesis inhibition

$$\begin{cases} \frac{dV_1}{dt} = aV_1 \ln\left(\frac{K_1}{V_1}\right), & V_1(t=0) = V_{0,1} \\ \frac{dK_1}{dt} = bV_1 - dV_1^{\frac{2}{3}}K_1 - eV_2 \mathbf{1}_{K_1 > K_0}, & K_1(t=0) = K_0 \\ \frac{dV_2}{dt} = aV_2 \ln\left(\frac{K_2}{V_2}\right), & V_2(t=0) = V_{0,2} \\ \frac{dK_2}{dt} = bV_2 - dV_2^{\frac{2}{3}}K_2 - eV_1 \mathbf{1}_{K_2 > K_0}, & K_2(t=0) = K_0 \end{cases}$$

Proliferation inhibition

$$\begin{cases} \frac{dP_1}{dt} = \alpha P_1 - (\beta P_1 + \gamma (P_1 + P_2)) \mathbf{1}_{P_1 > 0}, & P_1(t = 0) = V_{0,1} \\ \frac{dQ_1}{dt} = \beta P_1 + \gamma (P_1 + P_2), & Q_1(t = 0) = 0 \\ \frac{dP_2}{dt} = \alpha P_2 - (\beta P_2 + \gamma (P_1 + P_2)) \mathbf{1}_{P_2 > 0}, & P_2(t = 0) = V_{0,2} \\ \frac{dQ_2}{dt} = \beta P_2 + \gamma (P_1 + P_2), & Q_2(t = 0) = 0 \end{cases}$$

Benzekry et al. (Hahnfeldt), Cancer Res, 2017

The competition model did not fit



Benzekry et al. (Hahnfeldt), Cancer Res, 2017

The « inhibition of proliferation » model fitted best



Conclusion

- A general modeling framework for modeling metastases
- Statistical nonliner **mixed-effects modeling** very useful for parameter estimations
- Simplified model (growth + dissemination) able to describe available clinically relevant preclinical data of dynamics of total metastatic burden
- Same growth for primary tumor and mets in breast animal model
- A patient-specific key parameter µ is critical in the quantification of patient-specific metastatic aggressiveness
- Could be clinically useful for guiding **adjuvant therapy** (chemotherapy/WBRT)
- Application to clinical data of number and size of brain mets suggested dormancy in NSCLC
- Quantitative exploration of classical theories for metastatic colonization and tumortumor interactions

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Clinic

Brain metastasis from lung tumors

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Bergonié Institute, Bordeaux, FR



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Thank you for your attention!