

Machine learning with Random Neural Networks Gerardo Rubino

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Machine learning with Random Neural Networks

G. Rubino

INRIA Rennes, France

September 2018

G. Rubino (INRIA Rennes, France)

RNN & comp. nets.

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Outline

- $1 \mathsf{RNNs}$
- 2 Queuing origins
- 3 Extension in the Reservoir Computing class
- 4 About deep architectures
- 5 Conclusions and current projects
- 6 Some references

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September 2018 2 / 34

Abstract

- At the DIONYSOS team we have been using ML tools for more than 10 years, for specific networking problems:
 - the PSQA (Pseudo-Subjective Quality Assessment) project, mapping QoS + channel metrics into quantified QoE assessments,
 - time series predictions (for a PSQA 2.0 generation).
- Our main learning problems belong to the Supervised Learning area. we are starting to explore deep architectures.
- In the presentation, I will focus only on the used tool, the Random Neural Network.

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1 — RNNs

Outline

$1 - \mathsf{RNNs}$

- 2 Queuing origins
- 3 Extension in the Reservoir Computing class
- 4 About deep architectures
- 5 Conclusions and current projects
- 6 Some references

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September 2018 4 / 34

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1 - RNNs
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Classic artificial neurons

• A "classic artificial neuron" can be seen as a parametric real function of a real variable:



- We consider *b* as a parameter of the function implemented by the neuron (called *activation* function.
- There are many different activation functions used in practice: $z = \tanh(u b)$, $z = 1(u \ge b)$, ReLU...

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$1 - \mathsf{RNNs}$

Random Neurons

 A Random Neuron is a parametric positive real function of two real positive variables (we also say "ports") called "positive" and "negative" ports.



- We see the number r > 0 as a parameter (the *rate* of the neuron).
- There are several variants of this model. In the main and original one, we must use the function $z = \min(u/(r+v), 1)$.
- Inventor: E. Gelenbe, Imperial College, in the late 80s.
- Observe that there is nothing random here.

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A Random Neural Network (RNN) is a set of interconnected RNs. The connections are weighted by nonnegative reals.



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September 2018 7 / 34

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Jonctions at input ports are additive:



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September 2018 8 / 34

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 $1 - \mathsf{RNNs}$

Possible restriction

• Because of the queuing origin of the RNN tool, in order to respect the strict meaning of the model we must have

for each neuron *i*,
$$\sum_{j} (w_{i,j}^+ + w_{i,j}^-) = r_i$$
.

- This is a constraint to be respected in order to keep the queueing interpretation (and thus, to access all the theory and algorithms associated with).
- The same reason explains the use of $z = \min(u/(r+v), 1)$ instead of z = u/(r+v) (more on this below).

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$1 - \mathsf{RNNs}$

Why using RNNs in our PSQA project?

Because of the favorable comparison with standard software (at the time, several years ago). An example: with the same data and with the same cost (more precisely, the same number of weights), RNN on the left, Matlab on the right (an old version of its ToolBox on ML).



Outline

 $1 - \mathsf{RNNs}$

2 — Queuing origins

3 — Extension in the Reservoir Computing class

4 — About deep architectures

5 — Conclusions and current projects

6 — Some references

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September 2018 11 / 34

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Origin of the model

Refresher:



Consider the M/M/1 model, with arrival rate λ and service rate μ . The queue is stable iff $\lambda < \mu$; in that case, the steady state distribution $(\pi_n)_{n\geq 0}$ is given by $\pi_n = (1-\rho)\rho^n$, $n \in \mathbb{N}$, where the number $\rho = \lambda/\mu = 1 - \pi_0$ is the utilization factor, or load, of the system.

- $\rho = \Pr($ system busy at infinity); if $\lambda \ge \mu$, then we have that $\Pr($ there exists $t < \infty$ such that after t, system is always busy) = 1.
- See then that the load of the queue at infinity, ρ , satisfies

$$ho = \min \{ rac{\lambda}{\mu}, \ 1 \}.$$

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A basic G-queue: positive (standard) customers arrive with rate λ^+ ; negative ones arrive with rate λ^- ; both arrival processes are Poisson; the service rate is μ . Add usual independence conditions. To understand the semantics, see the graph below.



The Markov graph associated with the basic G-queue depicted above.

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The dynamics

In words,

- positive customers behave as ordinary ones;
- negative customers are actually signals: when a negative unit arrives at the queue, if there is some positive customer there, it removes it from the system (both "disappear"), and if the queue is empty, nothing happens;
- only positive customers can be observed; for negative ones, only their action can;
- "G-queue" and "Random Neuron" are two names for the same mathematical object;
- there are two different vocabularies, depending on the context: "G-queue" ≡ "Random Neuron"; "backlog of the queue" ≡ "potential of the neuron"; "busy queue" ≡ "active or excited neuron"; etc.

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From G-queues to G-networks



A tandem: first queue is an M/M/1; when leaving the first node, with probability p customers go to a second queue as positive ones, and with probability 1 - p as negative signals; service rate at queue i is μ_i , i = 1, 2.

Here, theory says that stability happens $\iff \lambda < \mu_1, \mu_2$, and in that case, if $X_i = 1$ (queue *i* is busy at ∞), i = 1, 2, we have, for j, k = 0, 1: Pr(at ∞ , $X_1 = j$, $X_2 = k$) = $[(2\rho_1 - 1)j + 1 - \rho_1][(2\rho_2 - 1)k + 1 - \rho_2]$.

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September 2018 15 / 34

A recurrent G-network



A general recurrent G-network with two nodes. We denote by d_i the probability of leaving the network after a service at queue *i*.

The asymptotic independence of the indicators of busy neurons is valid in general, so also here (and potentials are also asymptotically independent).

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A 3-layer structure



The graph of a 3-layer RNN of the (2,3,1) type (as before, dashed arrows correspond to flows of negative customers/signals).

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September 2018 17 / 34

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On the weights of a RNN

- Think queueing: when a customers leaves queue *i* (necessarily a positive customer), it goes to queue *j* as a positive customer with some fixed probability p⁺_{i,j}, or as a negative customer with some fixed probability p⁻_{i,j}.
- Then, the mean throughput (the frequency) of the flow of positive customers (of spikes) from *i* to *j* is r_ip⁺_{i,j} =: w⁺_{i,j}, and of negative ones is r_ip⁻_{i,j} =: w⁻_{i,j}.
- Since for any neuron *i* in the network, we must have $\sum_{j} (p_{i,j}^+ + p_{i,j}^-) = 1$ (add a queue/neuron 0 representing the network's environment), we have $\sum_{j} (w_{i,j}^+ + w_{i,j}^-) = r_i$.

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The general 3-layer Random Neural Network



Network inputs: those flows arriving at the input neurons; network outputs: the flows leaving the output neurons.

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Random Neural Networks implement rational functions

- Assume the negative ports *of input neurons* aren't used. Assume a single output neuron, so, a scalar network output.
- Call x_i the signal arriving at the positive port of input neuron *i*. Then, we can explicitly write the network output as a function of the inputs.



• The output is thus a rational function of the input. This allows many treatments. Also, for learning, costs (errors) are rational functions of weights, also leading to simple and powerful treatments.

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September 2018 20 / 34

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3 - Extension in the Reservoir Computing class

Outline

- $1 \mathsf{RNNs}$
- 2 Queuing origins

3 — Extension in the Reservoir Computing class

- 4 About deep architectures
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- 6 Some references

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September 2018 21 / 34

Reservoir Computing

- The idea of these models is to develop systems that use the potential for *memorization* of recurrent neural networks without their difficulties in the training process.
- They appeared at the beginning of the 2000s, and are known today under the name of *Reservoir Computing* (RC) paradigm.
- The two most popular RC models are
 - the Echo State Network (ESN)

(H. Jaeger, "The *echo state* approach to analyzing and training recurrent neural networks", German National Research Centre for Information Technology, Tech. Rep. 148, 2001);

 and the Liquid State Machine (LSM) (W. Maass, "Liquid state machines: Motivation, theory, and applications," in Computability in Context: Computation and Logic in the Real World, Imperial College Press, 2010, pp. 275-296).

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3 — Extension in the Reservoir Computing class

Echo State Networks (ESNs)

The main representative of the family. It has

- a first recurrent part called *reservoir*, with fixed weights,
- and a second supervised learning part called *readout*.



The learning process is restricted to the output weights (readout).

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September 2018 23 / 34

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Our Echo State Queueing Networks (ESQNs)

- Echo State Queueing Networks: applying the RC idea to a RNN. Joint work with S. Basterrech (Univ. of Prague).
- Three sets of neurones, a recurrent topology "in the middle".
- Input at time t: $\boldsymbol{a}(t) = (a_1(t), \dots, a_{N_a}(t)).$
- Load of input neuron $u \in 1..N_a$: $\rho_u(t) = a_u(t)/r_u$ (in general, we take $a_u(t) < r_u$).
- For all reservoir units $u = N_a + 1, \dots, N_a + N_x$,

$$\rho_{u}(t) = \frac{\sum_{v=1}^{N_{a}} \frac{a_{v}(t)}{r_{v}} w_{v,u}^{+} + \sum_{v=N_{a}+1}^{N_{a}+N_{x}} \rho_{v}(t-1) w_{v,u}^{+}}{r_{u} + \sum_{v=1}^{N_{a}} \frac{a_{v}(t)}{r_{v}} w_{v,u}^{-} + \sum_{v=N_{a}+1}^{N_{a}+N_{x}} \rho_{v}(t-1) w_{v,u}^{-}}.$$

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September 2018 24 / 34

3 - Extension in the Reservoir Computing class

- The input space in thus "projected" into a new "larger" space.
- The models then computes a linear regression from the projected space into the output space.
- Thus, the network output $\hat{y}(t) = (\hat{y}_1(t), \dots, \hat{y}_{N_b}(t))$ is computed for any $m \in 1..N_b$:

$$y_m(t) = w_{m,0}^{\text{out}} + \sum_{i=1+N_a}^{N_a+N_x} w_{m,i}^{\text{out}} \rho_i(t).$$

- Learning process: the output weights w_*^{out} can be computed using any (fast) procedure, for instance, Least Mean Square algorithms.
- Remark: we can replace this simple structure by, for instance, a classical feedforward 3-level RNN.

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September 2018 25 / 34

4 — About deep architectures

Outline

- $1 \mathsf{RNNs}$
- 2 Queuing origins
- 3 Extension in the Reservoir Computing class
- 4 About deep architectures
- 5 Conclusions and current projects
- 6 Some references

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September 2018 26 / 34

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4 — About deep architectures

Some ongoing work on Deep RNNs

- Imperial College is developing some extensions allowing exploring deep architectures based on RNNs.
- Specific tests have done using well-known databases that show good performances of the model against classic ones.
- The linear side of convolutional structures are obtained by appropriate parameters' choices in the RNN, and then using power expansions related to the denominator of the rational function associated with a Random Neuron.

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RNN & comp. nets.

September 2018 27 / 34

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4 — About deep architectures

Some preliminary experiments at Inria

- In our team at Inria, in collaboration with Technicolor, we can report some preliminary results concerning mixed architectures concerning classic and random neurons.
- The idea is to see the effect of replacing whole layers of neurons in a deep network by RNN-based ones.
- Again, using standard databases, we obtained promising results when RNN-based layers appear at the end rather than in the first layers of the network.

G. Rubino (INRIA Rennes, France)

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5 — Conclusions and current projects

Outline

- $1 \mathsf{RNNs}$
- 2 Queuing origins
- 3 Extension in the Reservoir Computing class
- 4 About deep architectures
- 5 Conclusions and current projects
- 6 Some references

G. Rubino (INRIA Rennes, France)

RNN & comp. nets.

September 2018 29 / 34

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5 — Conclusions and current projects

I refer only to the ML side here

- Random Neural Networks are, at least, interesting competitors in the ML field.
- Several theoretical questions around Reservoir Computing with our ESQN model (mainly around convergence, stability) are open.
- In PSQA, the labels come from subjective tests (that is, from panel of human subjects). We have a project to eliminate the use of those panels. This leads to
 - Big Data problems, coming from the extensive use of automatic but less performant tools to provide quality assessments,
 - then, to the exploration of the use of deep learning architectures.

G. Rubino (INRIA Rennes, France)

RNN & comp. nets.

September 2018 30 / 34

6 — Some references

Outline

- $1 \mathsf{RNNs}$
- 2 Queuing origins
- 3 Extension in the Reservoir Computing class
- 4 About deep architectures
- 5 Conclusions and current projects
- 6 Some references

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RNN & comp. nets.

September 2018 31 / 34

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RNN & comp. nets.

September 2018 33 / 34

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RNN & comp. nets.

September 2018 34 / 34

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