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► **To cite this version:**

Bertha Mayela Toledo Acosta, Xavier Heiligenstein, Grégoire Malandain, Patrick Bouthemey. Intensity-based matching and registration for 3D correlative microscopy with large discrepancies. ISBI 2018 - IEEE 15th International Symposium on Biomedical Imaging, Apr 2018, Washington, United States. pp.493-496, 10.1109/ISBI.2018.8363623 . hal-01930740

**HAL Id: hal-01930740**

**<https://inria.hal.science/hal-01930740>**

Submitted on 22 Nov 2018

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# INTENSITY-BASED MATCHING AND REGISTRATION FOR 3D CORRELATIVE MICROSCOPY WITH LARGE DISCREPANCIES

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## ABSTRACT

Correlative microscopy, especially light and electron microscopy (CLEM), enables the study of cells and subcellular elements in complementary ways, provided a reliable registration between images is efficiently achievable. We propose a general automatic registration method. Due to large discrepancies in appearance, field-of-view, resolution and position, a pre-alignment stage is required before any 3D fine registration stage. We define an intensity-based method for both stages, which leverages a common representation of the two involved image modalities. We report experimental results on different real datasets of 3D correlative microscopy, demonstrating time efficiency and overlay accuracy.

**Index Terms**— 3D microscopy images, 3D CLEM, multimodal patch matching, 3D registration

## 1. INTRODUCTION

In recent years, correlative microscopy has become an important and powerful tool in the bioimaging field. It combines two (or more) microscopy modalities, allowing the study of biological specimens in complementary ways and at different resolutions. Since current tools used by biologists require manual intervention, one key challenge in this area is to make the image overlay between modalities as automatic as possible for an easier and more efficient workflow. It will also favour dissemination of correlative microscopy and enable handling of large amount of images. This is particularly crucial for 3D acquisition. Our goal is precisely to propose an automated registration method for 3D correlative microscopy.

3D multimodal image registration has a long story in medical imaging [1]. Briefly speaking, there are two main approaches for registration [2]. The first one is the geometric approach which first extracts specific points in each image, pairs (or matches) them, and computes the 3D registration transformation from the matched pairs of points. It can handle large transformations. The second approach is the intensity-based one, which iteratively computes the 3D transformation by minimizing a similarity criterion for instance based on mutual information. It implicitly assumes that an initial positioning is given, not too far from the optimal solution. However, 3D correlative microscopy raises specific issues, which makes both approaches not straightforwardly applicable for an automatic workflow as explained just below.

The most frequent combination of correlative microscopy is between light microscopy (LM) and electron microscopy (EM),

referred to as correlative light and electron microscopy (CLEM). Fluorescence LM allows identification and tracking of labeled biomolecules, and provides information on their dynamics and interactions. However, the diffraction limits the resolution, and fluorescence LM cannot visualize unlabeled cellular structures. EM displays much higher resolution, and it can delineate cellular ultrastructure but at the cost of fixing the sample. Since there are several types of LM and EM modalities, any combination results in a specific CLEM method, also dependent on the biological problems under study. Other imaging techniques may accompany CLEM, such as microCT, or X-rays [3, 4, 5].

The technological and technical differences between EM and LM images are in many aspects: field of view, pixel resolution, image size, content, appearance, raising important and specific challenges for automated registration in 3D correlative microscopy. Furthermore, large gaps occur between the initial locations and orientations of the objects of interest in the respective LM and EM stacks in the data acquisition workflow. Then, geometrical and appearance discrepancies between LM and EM stacks hamper a direct computation of the 3D transformation mapping one image stack to the other.

The geometric registration approach is the one usually adopted in the semi-automatic 3D correlative microscopy workflow, but the selection and pairing of corresponding points are typically manually performed. In contrast, existing automatic segmentation methods cannot deliver repeatable point extraction in all LM and EM images. Indeed, these methods may not extract a sufficient amount of reliable point pairs in the two image modalities, in particular due to the lack of structure and texture in fluorescence images. The intensity-based approach for direct 3D registration computation is usually employed in medical imaging, since it can benefit from close initialisation and isotropic volumes. This does not stand for correlative microscopy which then requires a pre-alignment stage [6].

The paper is organized as follows. In Section 2, we briefly survey related work in CLEM. Section 3 introduces the datasets and the corresponding image properties. In Section 4, we present the two stages of our method. Section 5 reports experimental results, and provides a comparison with manual interaction using eC-CLEM[15]. Section 6 contains concluding remarks.

## 2. RELATED WORK IN CLEM

In current CLEM setups, registration is performed by a first global pre-alignment followed by a refined alignment, and usually involved an important user interaction. The manual pre-alignment or matching of the EM and LM stacks is commonly performed by biologists, either during the acquisition step and/or during the post-acquisition registration step. During acquisition, the pre-alignment relies on vi-

This work has been partly supported by the National Council of Science and Technology of Mexico (CONACYT) under the Grant no. 246372/384571.

sually identifying predefined marks on the sample holder, or exploiting fiducial markers introduced in the sample [7, 8]. Likewise, during the registration stage, the biologist has to select pairs of points in the two images, whatever they are (fiducial markers, distinctive features on the sample) [9, 10]. The landmark pairs are then exploited to compute the 3D geometric transformation between EM and LM stacks [11, 12, 13]. The matching step is a demanding and tedious task, especially if a large amount of data must be processed [14]. Such semi-automatic framework is adopted in [4] for registering 3D microCT and LM images, in the recently released eC-CLEM software for 3D correlative microscopy [15], or in [16] to overlay Scanning EM (SEM) and confocal LM volumes.

In above works, the refined registration is addressed by pairing corresponding points, and the user has to iteratively re-apply this procedure (picking points, computing the transformation) until he or she found the computed transformation satisfactory. A few works propose an automated refined registration (the pre-alignment being still manual). In [16], the cell membrane is segmented in the SEM stack and modified to a resolution similar to LM one. Then, EM and LM volumes are registered with an affine transformation and normalized correlation. [17] proposes an automated refined registration based on mutual information and rigid transformation. In [15], an extension to an automatic registration was also proposed, provided spots can be correctly detected in both images, but it was only tested on 2D real CLEM.

Our contribution is to propose automated procedures for both the pre- and the refined alignment for 3D correlative microscopy. Our method is intensity-based for both stages, and leverages a common representation of EM and LM images.

### 3. 3D CLEM FRAMEWORK

To motivate our contribution, we first present the two 3D correlative microscopy sets we will deal with, and we give information on the acquired images. The first set is composed of a serial block face SBFSEM image stack and a confocal image stack. HeLa cells were imaged for LM in a 710 LSM Zeiss inverted confocal microscope; afterwards, they were fixed, stained and embedded for SBF-SEM imaging and acquired using a Sigma VP scanning electron microscope (Carl Zeiss). The LM stacks has two channels: transmitted light and one fluorescent channel, with volume size of  $1024 \times 1024 \times 16$  and pixel size of  $0.22\mu\text{m}$  in  $X$  and  $Y$ , and  $0.6\mu\text{m}$  in  $Z$ , knowing that the  $XY$ -space corresponds to the lateral dimensions of the stack and the  $Z$ -axis to the vertical dimension of the stack. The size of the EM stack is  $666 \times 903 \times 247$  and its pixel size is  $0.14\mu\text{m}$  in  $X$  and  $Y$ , and  $50\text{nm}$  in  $Z$ , which is rather low-magnification EM. A 3D rendering is displayed in Fig.1.

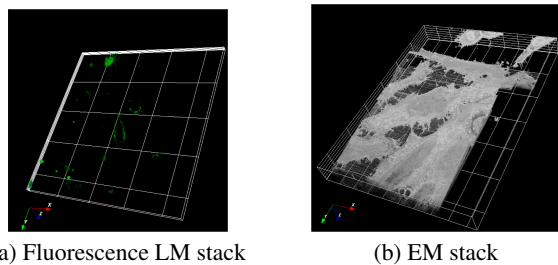


Fig. 1. Exp. 1: 3D CLEM

The second set, shown in Fig.2, includes a stack of microCT and a two-photon fluorescence microscopy stack. The microCT stack of

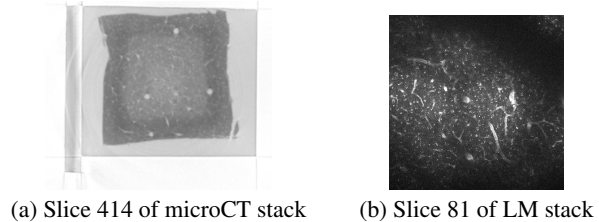


Fig. 2. Exp. 2: 3D microCT and Fluorescence LM

size  $1084 \times 896 \times 1094$  has pixel size of  $1\mu\text{m}$  in  $X$  and  $Y$  and  $1\mu\text{m}$  in  $Z$ , while the FM stack of size  $1024 \times 1024 \times 107$  has pixel size of  $0.59\mu\text{m}$  in  $X$ ,  $0.59\mu\text{m}$  in  $Y$  and  $3.0\mu\text{m}$  in  $Z$ .

In both datasets, the 3D stacks are anisotropic and have significant differences in terms of volume size, pixel resolution, content, appearance, and location of structures of interest between modalities. Nevertheless, in these examples, it turns out that the discrepancy between the two volumes in terms of shift along the  $Z$ -axis and of rotation in the  $XY$  plane are not that significant, but other discrepancies remain.

## 4. OUR AUTOMATED OVERLAY METHOD

### 4.1. Intensity-based XY pre-alignment

To address the large gap between the initial positions of EM and LM stacks, we have defined an intensity-based prealignment method. We restrict to the shift in the  $XY$ -space, since it is the larger component of misalignment (which is often the case by the way). It is tractable for an automatic pre-alignment at that stage. To compute this initial  $XY$  shift, we accordingly reduce the dataset to two dimensions. Projection along the  $Z$ -axis of the LM stack, using the maximum intensity projection (MIP), yields a good distribution of the volume content. If the LM stack is of size  $m \times n \times l$ , LM-MIP is a 2D  $m \times n$  image obtained by scanning LM intensities along the  $Z$ -axis and selecting the highest one for each  $(x, y)$  location of the image grid. The same cannot be applied to the EM stack, since the resulting MIP image will be saturated. Then, we simply select a few slices in the EM stack. CLEM overlay may be performed in both ways, EM to LM, or LM to EM. The overlay is focused on a region of interest (ROI) of the biological sample, which may involve a specific cell or a subcellular structure in a cell, and is specific to each biological project. The ROI is expected to be delineated either by the biologist (which will be in that case the only user interaction), or by an algorithm able to detect the content of interest.

Here we start with the EM stack. Given a 3D ROI delineated in the EM stack, we take the corresponding 2D ROIs in the selected EM slices, and we search for their corresponding ROI in the LM-MPI image. The patch dimensions in the LM-MPI image are inferred from the EM-ROI ones, while taking into account the ratio between pixel resolutions available in the metadata attached to the acquisition. To facilitate the search, we require a comparable appearance for the two images. To do so, we leverage the Laplacian of Gaussian (LoG) transform we introduced in [18] for 2D CLEM registration. The LoG transform maps a 2D EM image and a 2D LM image to closer representation, decreasing the big difference in appearance between the images as illustrated in Fig.4. The LoG transform enhances high spatial frequencies while suppressing local linear intensity variations. The LoG transform of an image  $I$  is expressed as:

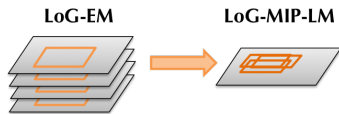
$$\mathcal{L}_\sigma(I) = \Delta(G_\sigma * I), \quad (1)$$

where the Gaussian standard deviation  $\sigma$  acts as an adaptable scale linked to the size of the objects of interest in  $I$ . It is automatically

selected by using the method described in [19] which exploits the Lindeberg’s scale-space approach. We select the scale with the maximum number of blobs, which are local minima in the constructed scale-space domain. By adapting the LoG scale to the EM and LM image content, we lessen the difference in content scale of LM and EM images.

Once a common representation of EM and LM images is created, we have to match the 2D LoG-EM-ROI with its corresponding ROI in the 2D LoG-LM-MIP image. We handle several 2D LoG-EM-ROIs, one by EM slice, to ensure robustness by making the matching not dependent on one particular 2D EM slice. Then, a 2D patch-based exhaustive search is carried out over the LoG-LM-MIP. Due to the differences in orientation between the LM and EM images, it is necessary to adopt a similarity measure that is invariant to rotation and scaling. Therefore, we take histogram-based descriptors for the matching process. We have used two types of histograms: the LoG-values histogram and the Local Directional Pattern (LDP) [20]. We have also implemented two histogram distances as similarity measures: the cosine similarity and the histogram intersection distance to evaluate the similarity of the LoG-EM-ROI with each tested LoG-MIP-LM patch.

If we use  $n$  EM slices taken from the EM stack, we have  $n$  candidate patches for the ROI location in the 2D LM-MIP image as illustrated in Fig.3. The final ROI center location in the LM-MIP image is selected using a robust criterion since outliers may occur, i.e., wrong matching. It is given by the weighted average of the center positions of the inlier patch candidates. The weights are defined as an inverse of the distance between the center of the patch and the median of the centers positions of all candidate patches. Beforehand, outliers are discarded according to the median absolute deviation of their center position to the median of the centers of all selected patches. The difference between the center location of the



**Fig. 3.** ROIs extracted from multiple LoG-EM slices to be located in the LoG-LM-MIP image

selected ROI in the LoG-LM-MIP image and the center of any 2D EM-ROI (since the 2D EM-ROIs are vertically aligned in the 3D EM-ROI stack) yields the 2D shift in the  $XY$ -space. Then, the full LM stack is shifted by applying the estimated 2D translation.

To summarize, our pre-alignment method comprises four main steps: 1) Maximum intensity projection of the LM stack to a 2D image; 2) LoG representation of 2D-LM-MPI image and 2D EM slices; 3) Matching of the ROI of every LoG-EM slice in LoG-LM-MIP image; 4) Pre-alignment of EM and LM stacks by a  $XY$ -shift.

#### 4.2. 3D ROI-based affine registration

Once the pre-alignment is achieved, we can estimate the 3D transformation which will allow to overlay the 3D LM stack onto the 3D EM stack. The 3D transformation is computed between the 3D LoG-EM-ROI and the pre-aligned 3D LoG-LM-ROI. The transformed LoG-LM stack is resampled to fit the same size in the  $Z$ -dimension as the LoG-EM stack using a bilinear interpolator after applying a low-pass filter. The 3D LoG-LM-ROI is recovered using the same coordinates of the 3D LoG-EM-ROI.

The LoG images are still different enough so that an intensity-difference similarity measure cannot provide satisfactory results. We

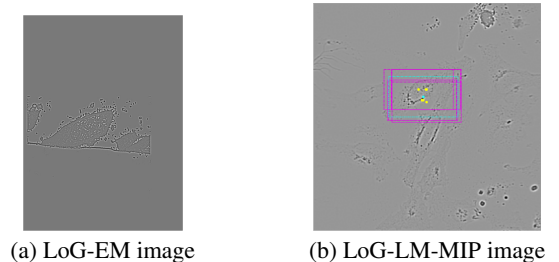
resort to mutual information (MI) as a similarity measure, due to its well-known capability of handling multimodal images. First, a 3D rigid transformation (composed of a rotation and a translation) is estimated. However, given the 3D CLEM workflow, it is not sufficient to account for the geometric relationship between the LM and EM stacks. The EM slices do not lie in the same plane as the LM slices, and distortions between stacks may occur during the acquisition. Consequently, we refine the registration with a 3D affine transform.

Our overall method does not involve any extraction of image features from the EM and LM stacks. It is merely intensity-based, which prevents from any possible segmentation errors and saves computation time. Furthermore, it does not require any parameter setting by the user. We use ITK libraries in C++ for the MI-based registration.

## 5. EXPERIMENTAL RESULTS

*Experiment 1: EM and LM.* To pre-align the EM and LM stacks, we follow the 2D matching process described in Section 4.1. A 2D projection of the LM stack is generated using MIP. EM slices 107-118 were selected to extract a 2D ROI, whose LoG representation (Fig.4a) is matched within the LoG-LM-MIP image. Using [19], we obtain an approximate scale for the LoG transform of EM and LM, respectively estimated as  $\sigma_{EM} = 4.3$  and  $\sigma_{LM} = 2.5$ .

A corresponding patch in the LoG-LM-MIP is found for each

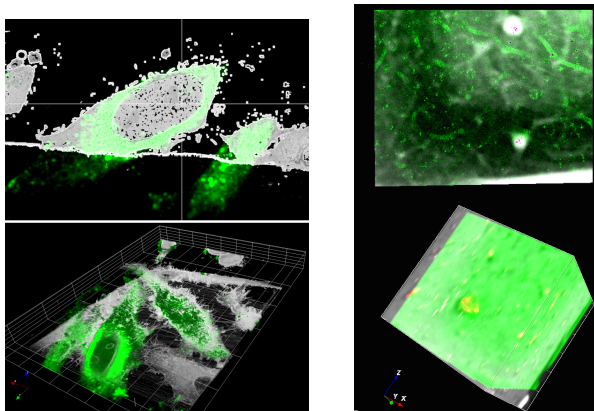


**Fig. 4.** Exp. 1: a) slice 107 of LoG-EM stack, b) LoG-LM-MIP image with patch candidates overprinted in magenta and the selected one in light blue (to be better visualized by zooming in the pdf file)

LoG-EM-ROI by the patch-based search, with a 90% overlap between tested patches, using both cosine and histogram intersection distances. Then, we robustly compute the selected patch from the weighted average of all their centers (Fig.4b). The final overlay of the registered EM and LM ROIs is shown in Figure 5. The accuracy can be appreciated by observing the fluorescence (in green) correctly surrounding the cell nucleus in the EM slice. The computed 3D rigid registration corresponds to a 3D translation of  $(-1.21, -0.5, 7.17)$ , and a rotation of angles  $-7.52^\circ$ ,  $-2.63^\circ$  and  $-1.46^\circ$  around the  $X$ ,  $Y$  and  $Z$  axis respectively. By picking corresponding points in LM and EM stacks, we evaluated an average registration error of 6.5 pixels, moderately less accurate than with manual eC-CLEM.

To compute this registration, it takes 1.54 minutes for the pre-alignment and 13.5 seconds for the 3D registration. Comparatively, manual correlation by a trained biologist on a known dataset using eC-CLEM took 20 minutes, most time being dedicated to primary orientation. Once the initial rotation, translation and scaling achieved (the first four points required in eC-CLEM), the fine correlation can be estimated to 5 minutes per points-pair. On an unknown dataset, initial correlation can take more than one hour.

*Experiment 2: MicroCT and LM.* In this experiment, slices 15-25 are extracted from the microCT stack, and a 2D ROI is extracted from each of their LoG representations. Then, a MIP of the LM stack is computed. The estimated LoG scales are  $\sigma_{\mu CT} = 22.2$  and  $\sigma_{LM} = 2.1$ . The full LM stack is pre-aligned by applying the shift given by the first stage. Then, we compute the 3D affine transformation. Computation time is 3.9 minutes for the pre-alignment stage and 15.4 seconds for the 3D registration. Visual evaluation of the overlay is given in Fig. 5. It is normal that most of the elongated shapes are not overlaid, since they are present in only one of the two modalities.



**Fig. 5.** 3D overlay for experiments 1 (left) and 2 (right). The fluorescence LM is overprinted in green. Top: Overlay visualized for one given slice. Bottom: Overlay visualized on the full 3D stack.

## 6. CONCLUSION

We have defined an original and efficient intensity-based method for automatically overlaying 3D image stacks of different modalities in correlative microscopy (CM). Our method can cope with large appearance, resolution and position discrepancies. It proceeds in two stages: pre-alignment and 3D fine registration. It does not involve any parameter setting, and then, is straightforward to use by biologists. Results on different combinations of 3D correlative microscopy show its genericity. Registration accuracy is satisfying for a fully automatic overlay of the two 3D image stacks. Future work will deal with still more general handling of the pre-alignment (fully 3D shift) and possibly non-rigid 3D registration, while continuing to validate the proposed method on other types of 3D CM datasets.

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