

# Structural Summarization of Semantic Graphs

Ioana Manolescu

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#### Structural Summarization of Semantic Graphs

#### Ioana Manolescu

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ESWC Conference, June 5, 2018

#### Outline

- Motivation: data discovery in semantic-rich RDF graphs
- Pramework: quotient summaries
  - Smaller graph which represents the original one in some sense
- Proposal: use property cliques for summarizing explicit and implicit data
- Summarization algorithms
- Perspectives

Joint work with François Goasdoué (U. Rennes 1 and Inria), Paweł Guzewicz (U. Paris Saclay and Inria), and Šejla Čebirić (U. Paris Saclay and Inria) [ČGM15a, ČGM15b, ČGM17a, GM18, PGA+18]

#### Part I

Motivation: data discovery in RDF graphs

## Big Data needs semantics

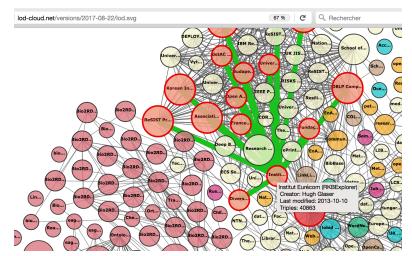
#### Al Magazine, Spring 2015





## RDF graph discovery

An RDF graph can be large and complex, lack a fixed schema, include many heterogeneous values...



#### **RDF** summaries

#### Simplified views of an RDF graph [ČGK+18]

- Most often, a summary is also a graph, and/or: statistics, patterns...
- Summarize: the data, the ontology, both
- Many prior works on graph summarization applied to RDF

#### **RDF** summaries

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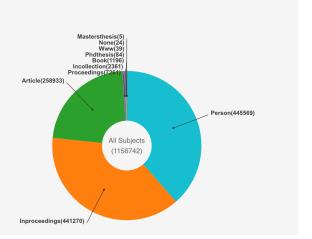
#### Summary uses:

- For **query processing**: give direct access to a group of nodes summarized together, detect empty queries...
- For data discovery: help identify interesting structure or patterns in the data

## RDF graphs are often structurally heterogeneous

#### Subject types in DBLP bibliographic data:

Type distribution (Click All Subjects or a certain type below for further exploration.)



### RDF graphs are often structurally heterogeneous

#### Data properties of DBLP conference articles:



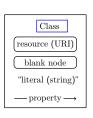
#### Our goal

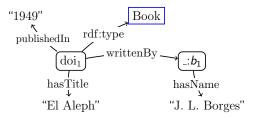
#### Define **structural summaries** which:

- resist to heterogeneity
- flexibly take into account RDF types
- allow summarizing implicit triples
- can be implemented efficiently

## The Resource Description Framework (RDF)

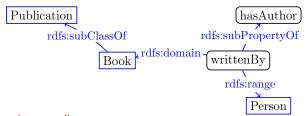
#### RDF graph: set of triples





We consider **RDFS** deductive constraints, stating connections between classes and properties

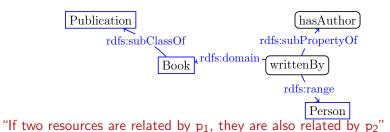
Constraint	Triple	OWA interpretation
Subclass	c <sub>1</sub> rdfs:subClassOf c <sub>2</sub>	$c_1\subseteqc_2$
Subproperty	p <sub>1</sub> rdfs:subPropertyOf p <sub>2</sub>	$\mathtt{p}_1\subseteq\mathtt{p}_2$
Domain typing	p rdfs:domain c	$\Pi_{\mathrm{domain}}(\mathtt{p})\subseteq \mathtt{c}$
Range typing	p rdfs:range c	$\Pi_{\mathrm{range}}(\mathtt{p})\subseteq \mathtt{c}$



"Any c1 is also a c2"

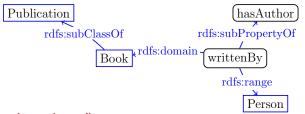
Simple language of <u>deductive constraints</u> between classes and properties

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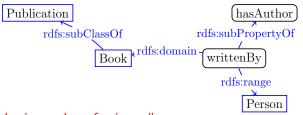
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"Anyone having p is a c"

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"Anyone who is a value of p is a c"

#### Open-world assumption and RDF entailment

RDF data model based on the open-world assumption.

Deductive constraints lead to **implicit triples**: part of the graph even though not explicitly present

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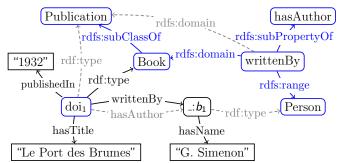
Exhaustive application of entailment leads to saturation (closure)

## The semantics of an RDF graph G is its saturation $G^{\infty}$

#### RDF data graph and RDF schema graph:



#### Saturation of the graph union:



#### Part III

## RDF summarization

#### **RDF** summaries

#### **Problem**

RDF graph G is large, heterogeneous, partially implicit. How to compactly represent  $\underline{\text{all}}$  its structure?

#### **Existing solutions**

Partial representation (frequent patterns, statistics etc.) e.g., [NM11, LYL13]

Potentially not compact e.g., [GW97, CFKP15]

Only for explicit data, e.g., [CDT13, ZDYZ14]

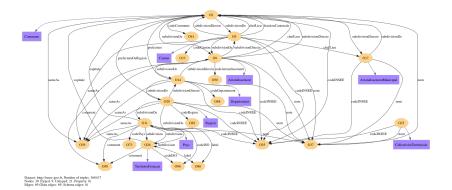
# A summary of DBLP data

#### 150M triples



## A summary of geographic data

French territory division in regions, departments, urban areas, cities, districts etc.
368K triples



### Summarization principle: quotient graphs

Let  $\equiv$  be an equivalence relation on the nodes of G. The **quotient**  $G_{\equiv}$  of a directed graph G by  $\equiv$  is a graph defined as follows:

- $G_{/\equiv}$  nodes: one for  $\equiv$  equivalence class of V
- $G_{/\equiv}$  edges:  $n^1_{\equiv} \xrightarrow{a} n^2_{\equiv}$  iff  $\exists n_1 \xrightarrow{a} n_2 \in G$  such that  $n_1$  represented by  $n^1_{/\equiv}$ ,  $n_2$  represented by  $n^2_{/\equiv}$

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Quotients have interesting summary qualities:

- **1 Property completeness:** All G properties appear in  $G_{\equiv}$
- **Size guarantees:** By definition,  $G_{/\equiv}$  is at most as large as G (usually much smaller)
- **Structure representativeness:** Given a query q, if its structure-only version is empty on  $G_{/\equiv}$ , then q is empty on G

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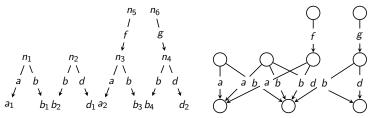
**Problem:** Bisimilarity compresses/summarizes very little!

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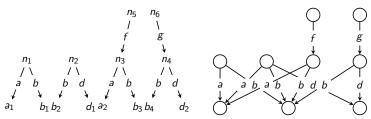
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Still: > 130 property combinations on conf. papers in DBLP **Requirement 1:** We need equivalence relationships robust to structural heterogeneity.

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Can we apply quotientization directly to an RDF graph? Sample graph G and a possible quotient thereof:

A \* type - 
$$u_1$$
  $n_2$  - type  $\Rightarrow$  B  $\nearrow$  type  $\Rightarrow$   $\nearrow$   $p \ p \ p \ r$   $p \ r$   $p \ r$   $p \ r$   $p \ r$ 

Possible loss of implicit triples

#### What about type and schema triples?

Can we apply quotientization directly to an RDF graph? Sample graph G and a possible quotient thereof:

$$A \leftarrow \text{type} - u_1 \qquad n_2 - \text{type} \rightarrow B \qquad \bigcirc - \text{type} \rightarrow \square$$

$$p \quad p \quad p \quad r \qquad p \quad r$$

$$\downarrow \quad \downarrow \quad \downarrow \quad \downarrow \qquad \downarrow \qquad \downarrow$$

$$p_1 \quad p_1 \quad p \quad r \qquad \qquad \bigcirc$$

Possible loss of implicit triples

Requirement 2: Avoid schema loss through quotientization

#### RDF equivalence relation and RDF summaries

To meet Requirement 2, we define:

- Quivalence relation: an equivalence relation on RDF graph nodes such that any class or property node is only equivalent to itself
- Q RDF summary: a quotient of a graph G by an RDF equivalence relation such that any class or property node is represented by itself.

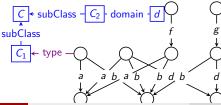
**Consequence:** For any RDF equivalence relation  $\equiv$  and RDF graph G, the schema of  $G_{/\equiv}$  is the schema of G.

⇒ No schema compression! (to be rediscussed briefly)

### Summarization through an RDF equivalence relation

E.g., let  $\equiv_{1 \text{fb}}$  to be the RDF node equivalence obtained from  $\sim_{1 \text{fb}}$ . Sample graph G:

Its quotient through the RDF node equivalence  $\equiv_{1fb}$ :



#### Recap

#### We have seen:

 RDF node equivalence and RDF quotients ⇒ structural representativeness, empty query pruning

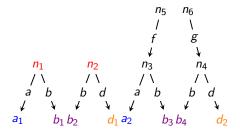
We still need to solve:

- Requirement 1: compact (yet preserve structure) even on heterogeneous graphs
- Requirement 3: can we summarize implicit triples?

We will address them in this order.

### RDF node equivalence based on property cliques

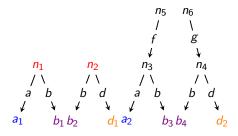
Intuition:  $n_1$ ,  $n_2$  are "of the same kind"; similarly  $b_1$ ,  $b_2$ ,  $b_3$ 



 $n_3$ ,  $n_4$  may or may not be of the same kind as  $n_1$ ,  $n_2$ .

### RDF node equivalence based on property cliques

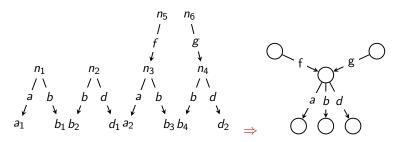
Output property cliques:  $\{a, b, d\}$ ;  $\{f\}$ ;  $\{g\}$ ;  $\emptyset$  Input property cliques:  $\{a\}$ ;  $\{b\}$ ;  $\{d\}$ ;  $\{f\}$ ;  $\{g\}$ ;  $\emptyset$ 



### Weak clique-based summaries

Two nodes are weakly equivalent  $(\equiv_{/W})$  iff they have the same input clique or the same output clique or are weakly equivalent to a third one.

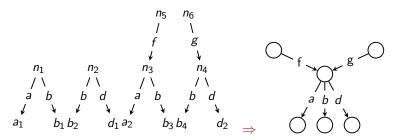
Weak summary  $G_{/W}$  of the sample RDF graph G:



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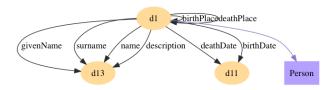


Property: In  $G_{/W}$ , each data property appears exactly once  $\Rightarrow$  its nodes are "source of p, target of p" for each p [ČGM15b].

### Weak clique-based summaries

Property:  $G_{/W}$  nodes are "source of p, target of p" for each p.

**Detecting errors in the data:** why do the birthplace and deathplace loop?



#### Looking in the data, we find:

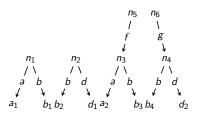
 $\langle \text{http://dbpedia.org/resource/Kunitomo\_lkkansai} \rangle \langle \text{http://www.w3.org/1999/02/22-rdf-syntax-ns\#type} \rangle \langle \text{http://xmlns.com/foaf/0.1/Person} \rangle.$ 

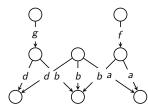
\langle http://dbpedia.org/resource/Kunitomo\_Ikkansai\rangle \langle http://dbpedia.org/ontology/birthPlace\rangle \langle http://dbpedia.org/resource/Kunitomo\_Ikkansai\rangle .

### Strong clique-based summaries

Two nodes are strongly equivalent ( $\equiv_S$ ) iff they have **the same** input clique and the same output clique.

Strong summary  $G_{/\equiv S}$  of the same G:





### Which role should node types play in summarization?

Having the same type(s) is orthogonal w.r.t. having the same structure.

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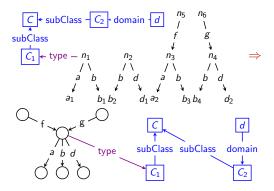
**① Data-then-type:** group nodes first by their data triples, then carry the types from each  $\equiv$  group to its representative.

### Which role should node types play in summarization?

Having the same type(s) is orthogonal w.r.t. having the same structure. Two alternatives:

**Oata-then-type:** group nodes first by their data triples, then carry the types from each  $\equiv$  group to its representative.

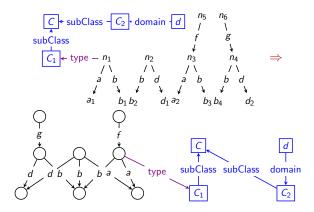
#### Extended Weak summary:



#### Adding types after data summarization

**Oata-then-type:** group nodes first by their data triples, then carry the types from each  $\equiv$  group to its representative.

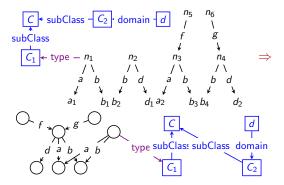
Extended Strong summary:



### Giving proeminence to types

Type-then-data: Group nodes by their type set, and untyped nodes by their data properties.

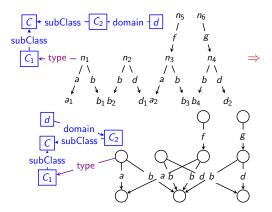
Typed Weak summary  $G_{/\equiv TW}$  of the sample graph:



### Giving proeminence to types

• **Type-then-data:** Group nodes <u>first by their types</u>. Only untyped nodes are grouped by their data properties.

Typed Strong summary  $G_{/\equiv TS}$  of the sample graph:



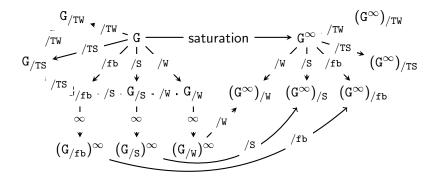
#### RDF summaries outline

Summary	Weak?	Strong?	Types first?
$G_{/\equiv W}$	✓		
G <sub>/≡S</sub>		<b>√</b>	
$G_{/\equiv\mathrm{TW}}$	✓		✓
$G_{/\equiv TS}$		<b>√</b>	<b>√</b>

#### RDF summaries outline

Summary	Weak?	Strong?	FW bisim?	BW bisim?	Types first?
$G_{/\equivW}$	✓				
$G_{/\equiv S}$		<b>√</b>			
${ m G}_{/\equiv{ m TW}}$	<b>√</b>				✓
$G_{/\equiv{ m TS}}$		✓			✓
${\sf G}_{/\equiv{ m fw}}$			✓		
$G_{/\equiv\mathrm{bw}}$				✓	
$G_{/\equiv\mathrm{fb}}$			✓	✓	
${\sf G}_{/\equiv{ m fw,T}}$			✓		✓
$G_{/\equiv\mathrm{bw,T}}$				✓	✓
$G_{/\equiv\mathrm{fb,T}}$			<b>√</b>	<b>√</b>	<b>√</b>

# Relations between RDF summaries [ČGM17b]



# Summary size comparison (more in [ČGM17b])

Graph G	G	Summary ${ t G}_{/\equiv}$	$ \mathtt{G}_{/\equiv} $	cf <sub>≡</sub>
DBLP	150,787,464	${\sf G}_{/{ m W}}$	71	2,123,767
DBLP	150,787,464	${ m G}_{/{ m S}}$	206	731,978
DBLP	150,787,464	${\sf G}_{/{ m fw}}$	262,695	574
LUBM1M	1,227,868	${\sf G}_{/{ m W}}$	161	7,579
LUBM1M	1,227,868	${ t G}_{/{ ext{S}}}$	207	5,903
LUBM1M	1,227,868	${\sf G}_{/{ m fw}}$	1982	617
LUBM10M	11,990,183	${ t G}_{/{ ext{W}}}$	162	74,013
LUBM10M	11,990,183	${ t G}_{/{ m S}}$	206	58,204
LUBM10M	11,990,183	$G_{/\mathrm{fw}}$	24,958	480
LUBM10M	11,990,183	$G_{/\mathrm{bw}}$	6,162	1,944
LUBM10M	11,990,183	${ t G}_{ m /fb}$	11,990,076	1

## Summarizing $G^{\infty}$

Recall: With an RDF Schema, the semantics of G is  $G^{\infty} \Rightarrow$  We really need  $(G^{\infty})_{/\equiv}!$ 

- Saturate G, then summarize
- 2 Can we avoid saturating G?...

## Summarizing $G^{\infty}$

Recall: With an RDF Schema, the semantics of G is  $G^{\infty} \Rightarrow$  We really need  $(G^{\infty})_{/\equiv}!$ 

- Saturate G, then summarize
- 2 Can we avoid saturating G?...

#### **Shortcut theorem** [ČGM17a]

For the summaries  $G_{/\equiv W}$ ,  $G_{/\equiv S}$ ,  $G_{/\equiv fw}$ ,  $G_{/\equiv bw}$ ,  $G_{/\equiv fb}$ :

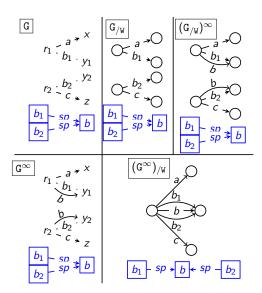
$$(\mathtt{G}^{\infty})_{/\equiv}$$
 is the same as  $((\mathtt{G}_{/\equiv})^{\infty})_{/\equiv}$ 

Also: sufficient condition for any  $\equiv$  to admit the shortcut.

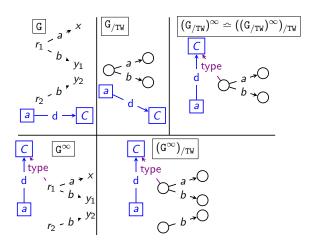
### Shortcut path to $G^{\infty}$

If  $G_{\equiv}$  is much smaller than G, the shortcut may be faster! Up to 20 times in our experiments [ČGM17b]

## Shortcut example: $G_{/\equiv W}$



## Shortcut counter-example: $G_{/\equiv \, { m TW}}$



#### Summarization algorithms

- **① Global algorithms**: visit all G, compute  $\equiv$  relation, then traverse G again and represent each triple in  $G_{/\equiv W}$
- ② Incremental algorithms: visit G, compute ≡ and summary based on knowledge gained so far; adjust summary

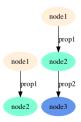
We devised global and incremental summarization algorithms for G/ $\equiv$  W, G/ $\equiv$  S, G/ $\equiv$  TW, G/ $\equiv$  TS.

Difficulty of incremental summarization: adjusting  $\equiv$  and revisiting summarization decisions

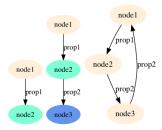
Each color corresponds to a different  $\equiv_{W}$  class



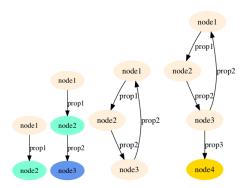
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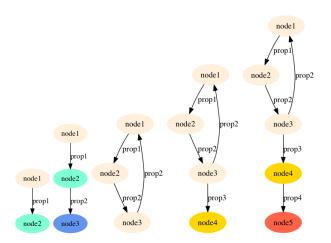
Each color corresponds to a different  $\equiv_{\mathtt{W}} \mathsf{class}$ 

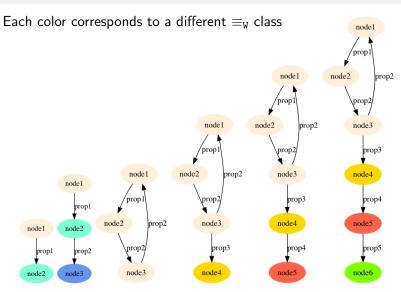


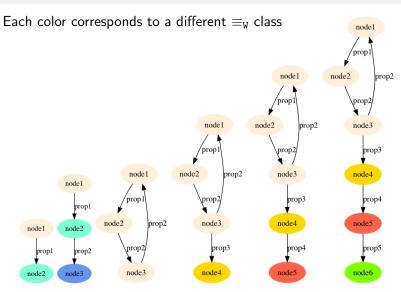
Each color corresponds to a different  $\equiv_{\mathbb{W}}$  class

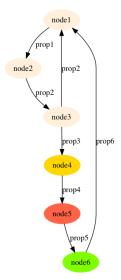


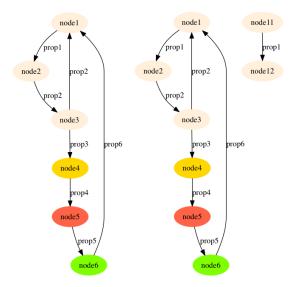
Each color corresponds to a different  $\equiv_{\mathbb{W}}$  class

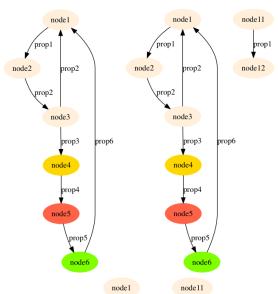


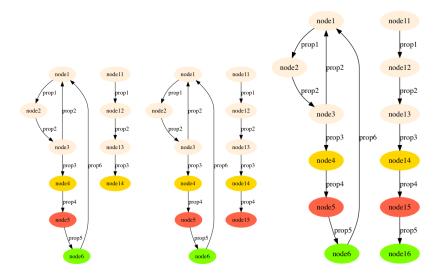




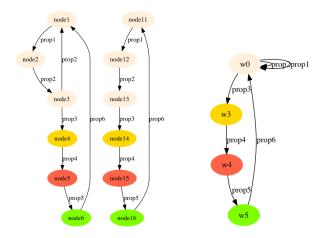






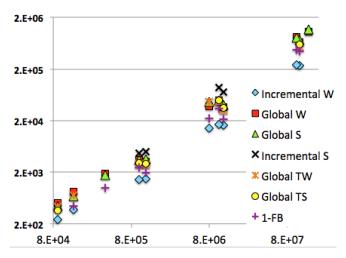


#### Full graph and its summary:



#### Algorithm scale-up

 $10^5$  to  $1.5\times 10^8$  triples



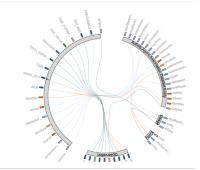
## Summary-enabled LOD cloud exploration [PGA+18]

Collaboration with ILDA Inria data vizualization team on LODAtlas http://lodatlas.lri.fr/

Use summary to derive visualisation instead of the original graph (smaller, faster)

abs-linked-data: Australian Bureau of Statistics (ABS) Linked Data 💆





#### Part IV

### Conclusion

#### The need for RDF graph discovery tools

- RDF graphs can be large and complex, they lack a prescriptive schema
- Semantic rules lead to implicit data
- Structural quotient summaries compactly represent graph structure and semantics.

Available online at: (new version soon)

```
https://team.inria.fr/cedar/projects/rdfsummary/
```

- Type-first summarization variant to cope with large type hierarchies [GM18]
- Integration into LODAtlas platform [PGA+18]

### Part V

## Perspectives

#### Ongoing and future work

#### Ongoing:

- Experiment with new, parallel summarization algorithms based on Spark
- Keyword search in RDF graphs based on quotient summaries

#### Future:

- Controlled inclusion of data value synopsis in the summary
- Extension to more expressive ontology languages
- Integration in a larger platform for <u>summary-based data</u> <u>discovery</u> (with Mirjana Mazuran)
- Exploration of interesting aggregate view of RDF graphs (with Yanlei Diao)

#### References

- [CDT13] Stéphane Campinas, Renaud Delbru, and Giovanni Tummarello. Efficiency and precision trade-offs in graph summary algorithms. In <u>IDEAS</u>, 2013.
- [CFKP15] Mariano P. Consens, Valeria Fionda, Shahan Khatchadourian, and Giuseppe Pirrò. S+EPPs: Construct and explore bisimulation summaries + optimize navigational queries (demo). PVLDB, 8(12), 2015.
- [ČGK+18] Šejla Čebirić, François Goasdoué, Haridimos Kondylakis, Dimitris Kotzinos, Ioana Manolescu, Georgia Troullinou, and Mussab Zneika. Summarizing semantic graphs: A survey. 2018.
- [ČGM15a] Šejla Čebirić, François Goasdoué, and Ioana Manolescu. Query-oriented summarization of RDF graphs. In <u>BICOD</u>, 2015.
- [ČGM15b] Šejla Čebirić, François Goasdoué, and Ioana Manolescu. Query-oriented summarization of RDF graphs (demonstration). <u>PVLDB</u>, 8(12), 2015.
- [ČGM17a] Šejla Čebirić, François Goasdoué, and Ioana Manolescu. A framework for efficient representative summarization of RDF graphs. In <u>International</u> <u>Semantic Web Conference (ISWC)</u>, 2017.
- [ČGM17b] Šejla Čebirić, François Goasdoué, and Ioana Manolescu. Query-Oriented Summarization of RDF Graphs. Research Report RR-8920, INRIA, 2017.

### References (cont.)

- [DMS17] Yanlei Diao, Ioana Manolescu, and Shu Shang. Dagger: Digging for interesting aggregates in RDF graphs. In <u>International Semantic Web</u> Conference (ISWC), 2017.
  - [GM18] Paweł Guzewicz and Ioana Manolescu. Quotient RDF summaries based on type hierarchies. In <u>Data Engineering for the Semantic Web (DESWeb)</u>, 2018.
  - [GW97] Roy Goldman and Jennifer Widom. Dataguides: Enabling query formulation and optimization in semistructured databases. In <u>VLDB</u>, 1997.
- [HHK95] Monika Rauch Henzinger, Thomas A. Henzinger, and Peter W. Kopke. Computing simulations on finite and infinite graphs. In <u>FOCS</u>, 1995.
- [LYL13] Shou-De Lin, Mi-Yen Yeh, and Cheng-Te Li. Sampling and summarization for social networks (tutorial), 2013.
- [NM11] Thomas Neumann and Guido Moerkotte. Characteristic sets: Accurate cardinality estimation for RDF queries with multiple joins. In ICDE, 2011.
- [PGA+18] Emmanuel Pietriga, Hande Gözükan, Caroline Appert, Marie Destandau, Šejla Čebirić, François Goasdoué, and Ioana Manolescu. Browsing linked data catalogs with LODAtlas. In <u>Int'l. Semantic Web Conference (ISWC)</u>, Resources track, 2018.

### References (cont.)

[ZDYZ14] Haiwei Zhang, Yuanyuan Duan, Xiaojie Yuan, and Ying Zhang. ASSG: adaptive structural summary for RDF graph data. In <u>ISWC</u> (Posters and Demonstrations), 2014.