

BLAC-wavelets: a m ultiresolution analysis with non-nested spaces

Georges-Pierre Bonneau, Stefanie Hahmann, Gregory M Nielson

To cite this version:

Georges-Pierre Bonneau, Stefanie Hahmann, Gregory M Nielson. BLAC-wavelets: a m ultiresolution analysis with non-nested spaces. VIS 1996 - 7th Annual IEEE Visualization '96, Oct 1996, San Francisco, United States. pp.1-6, 10.1109/VISUAL.1996.567602. hal-01708581

HAL Id: hal-01708581 <https://inria.hal.science/hal-01708581v1>

Submitted on 13 Feb 2018

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

BLAC-wavelets: a multiresolution analysis with non-nested spaces

Georges-Pierre Bonneau¹ Stefanie Hahmann² Gregory M. Nielson³

Abstract. In the last five years, there has been numerous applications of wavelets and multiresolution analysis in many terration of computer glad particles as dimensional modelling volume and distribution visualization or illumination modelling Classical multiresolution analysis is based on the knowledge of ^a nested set of functional spaces in which the successive approximations of ^a given function converge to that functional where can be existently considered This paper rates from and a theoretical cal framework which which enables multiples multiples multiples in the functional spaces are not nested and ne as they are they still have the property that the successive approximations converged the successive and given function Based on this concept we nally introduce ^a new multiresolution analysis with exact reconstruction for the discussion construction and distribution and allowed the construction of the construction and the construction of the c of multiple of old values which is a blending of the blending of Haar and linear multiple and values of the multiple

With a multiresolution analysis one can represent a given function at multiple levels of detail. The loss of detail into the store is stored into the society wavelet wavelet coefficient coefficiently. Then we can are basis functions encoding the difference between two successive levels of representation. Multiresolution analysis consists in other words in a decomposition of a given function over a coarse subdivision of the domain together with a sequence of wavelet coe-cients and allows an exact reconstruction

Multiresolution analysis based on wavelets is a powerful tool for handling with large data sets It allows an executive representation by means of compression and fast computations One can new compute in numerical analysis and signal decomposition. But in the last five years, they became more and more popular in many fields of computer graphics as different as image processing, geometric modelling, volume visualization or illumination modelling

Compression of large data sets like images can be done by removing small wavelet coe-cients The number cients depends on the error bound the error bound the error bound approximation should be within Within Within a multiresolution analysis it is easy to perform progressive displaying of complex scenes While adding progressively the wavelet coefficients the image is displayed more and more in detail One does not need to to load and display a whole large image all at once. Multiresolution analysis is also suitable for level-ofdetail control in rendering systems. One can go smoothly from a very coarse approximation of an object far away from the viewer to more detailed representations more the viewer approaches the object All these application examples and more can be found in Eck metally a make the property data cut-sectionary sammations converts and this concept we finally introduce a new multiresolution analyon for large data sets defined on uniform grids. We construct a one-payation for large da

Classical multiresolution analysis is based on the knowledge of a nested set of functional spaces in which the successive approximations of a given function converge to that function and can be e-ciently com puted

This paper first proposes a theoretical framework which enables multiresolution analysis even if the functional spaces are not nested, as long as they still have the property that the successive approximations converge to the given function The purpose of this framework is to introduce a new multiresolution analysis of large data sets defined on uniform grids. For these sets two well known wavelet bases, the Haar and the linear basis, can be used. Haar wavelets allow local analysis formulas but they are not continuous Linear wavelets are continuous but their regularity can be a drawback if the analyzed data have many discontinuities. The theoretical framework introduced in this paper enables to find a oneparameter family of wavelet bases which goes smoothly from the Haar to the linear basis The user can choose his own compromise between regularity and locality properties

Laboratoire LHMSI-CNRS, BP 133, F-91403 Orsay, France

⁻ Laboratoire LMC-IMAG, Universite INPG Grenoble, BP 53, F-38041 Grenoble, France

Computer Science Department, Arizona State University, Tempe, AZ 85287-5406, USA

————————————————————

The purpose of this section is to recall briefly the basics of a classical multiresolution analysis, omitting technical details to introduce our new multiresolution framework and to point out links between both theories. Multiresolution analysis based on wavelets, as first introduced by Mallat in [Mall89], leads to a hierarchical scheme for the computation of the wavelet coe-cients The use of fully orthogonal wavelet bases generally implies globally supported wavelets. But the infinite support of such wavelets is usually a disadvantage for practical implementations. This is the reason why we focus on semi-orthogonal wavelet bases

- Classical multiresolution analysis

Let Ω be some domain and $L_2(\Omega)$ the set of all functions with finite energy over Ω . Classical multiresolution analysis is based on the knowledge of a nested set of subspaces V_n of $L_2(\Omega)$.

$$
V_n \subset V_{n+1} \tag{1}
$$

It is also required that

$$
\bigcup_n V_n \text{ is dense in } L_2(\Omega) ,
$$
 (2)

so that for any given function f in $L_2(\Omega)$, the successive approximations f_n of f in V_n will converge. Property (1) ensures that f_{n+1} is always a better approximation of f than f_n . The wavelet spaces W_n are introduced to capture the loss of detail between f_{n+1} and f_n . In other words there must exist some function g_n in W_n so that $f_{n+1} = f_n + g_n$. This is the case if we choose W_n as the orthogonal complement of V_n in V_{n+1} . $V_n \subset V_{n+1}$
 dthat $\bigcup_{n} V_n$ is dense in $L_2(\Omega)$, we function
 f in $L_2(\Omega)$, the successive approximations
 f_n of f in times that
 f_{n+1} is always a better approximation of
 f than f_n . The capture the loss o

$$
V_{n+1} = V_n \oplus W_n \tag{3}
$$

In order to compute the approximations f_n and the details g_n , one has to introduce basis functions for the spaces V_n and W_n . In this section, we won't state more precise any index set. This will be done in section 5. The basis functions (φ_i^*) of v_n are called *scaling functions*. The basis functions (ψ_i^*) of w_n are called wavelet functions

From (1) and (5) follows that there exist some matrices $G^+ = (g_{ik}^+)$ and $H^+ = (h_{ik}^+)$, so that

$$
\varphi_i^n = \sum_k g_{ik}^n \varphi_k^{n+1} \tag{4}
$$

$$
\psi_j^n = \sum_k h_{jk}^n \varphi_k^{n+1} \tag{5}
$$

(4) is known as the remiement equation. Another consequence of (5) is that the functions φ_i^* and ψ_j^* are mutually orthogonal, and therefore we have

$$
\sum_{k} \sum_{l} g_{ik}^{n} h_{jl}^{n} < \varphi_k^{n+1}, \varphi_l^{n+1} > = 0 \tag{6}
$$

The orthogonality equation (b) is used to compute the matrix H^+ and hence the wavelet functions (ψ_i^+) from a given set of scaling functions (φ_i^{\ldots}) and (φ_k^{\ldots}) .

From (3) follows also that the finer scaling functions (φ_k^{n+1}) are linear combinations of the coarser scaling functions (φ_i^+) and the wavelet functions (ψ_i^+) :

$$
\varphi_k^{n+1} = \sum_k \overline{g_{ki}^n} \; \varphi_i^n + \sum_k \overline{h_{kj}^n} \; \psi_k^n
$$

Given an approximation $f_{n+1} = \sum_k x_k^{n+1} \varphi_k^{n+1}$ of f in V_{n+1} , the coarser approximation $f_n = \sum_i x_i^n \varphi_i^n$ and the details $g_n = \sum_i y_i^n \psi_i^n$ are computed by

$$
x_i^n = \sum_k \overline{g_{ki}^n} \ x_k^{n+1} \tag{7}
$$

$$
y_j^n = \sum_k \overline{h_{kj}^n} \ x_k^{n+1} \tag{8}
$$

 (7) and (8) are called analysis formulas.

Computing the finer smoothing coefficients $(x_k^{n+\tau})$ from the coarser one (x_i^n) and the detail coefficients (y_i) is done in the following way:

$$
x_k^{n+1} = \sum_i g_{ik}^n x_i^n + \sum_j h_{jk}^n y_j^n \tag{9}
$$

This equation is known as synthesis formula.

The complete analysis process, called filter bank, is represented by

The complete synthesis process consists of recursively computing the finest smoothing coefficients (x_k^{n+1}) from the coarsest (x_i) and the detail coefficients at each scale, by $n+1$ applications of (9).

2.2 Multiresolution analysis with non-nested spaces

The choice of the scaling functions is the heart of the multiresolution analysis introduced in 2.1. This choice determines the approximation spaces V_j . If the convergence condition (2) is quite intuitive since we want the approximation f_n to converge, it should be possible to define a multiresolution framework even if the condition of nested spaces (1) is not verified. In fact this condition, or equivalently the refinement condition (4) is very restrictive. It forces the scaling functions at all levels to have the same regularity. This is incompatible with the BLAC-scaling functions defined in section 3 of this paper.

The idea applied in section 3 to do multiresolution analysis without the refinement condition, is basically to associate to each scaling function at the level n , a linear combination of scaling functions of the finer level $n + 1$, which is not equal (since it's not possible), but close to it. In other words, we replace the refinement condition by an approximated refinement condition:

$$
\varphi_i^n \simeq \widetilde{\varphi}_i^n = \sum_k g_{ik}^n \varphi_k^{n+1} \tag{10}
$$

The choice of the approximation depends on the application and therefore it will be stated more precisely in the next section. The new approximation space v_n spanned by the functions (φ_i^{\pm}) is close to v_n , and it is also included in V_{n+1} :

$$
V_n \simeq \widetilde{V}_n \subset V_{n+1} \ .
$$

The wavelet space W_n now captures the loss of detail between V_n and V_{n+1} .

$$
V_{n+1} = \widetilde{V}_n \oplus W_n \tag{11}
$$

The orthogonality equation (0) used to compute the wavelets is still the same, but it means now that v . and φ_i (instead of φ_i) are mutually orthogonal.

The analysis and synthesis formulas (7) , (8) and (9) are the same, but it corresponds now to an approximation in two steps

Analysis: f_{n+1} approx \widetilde{f}_n \hat{r}_n = $\sum_i x_i^n \; \widetilde{\varphi}_i^n$ $^{-a_1}$ $\stackrel{\rm{a\,pmatrix}}{\longrightarrow}$ ${\bf f_n} = \sum_i x_i^n \varphi_i^n$ g_n

Figure 1 gives a geometric interpretation of one step of analysis and synthesis in the classical and new multiresolution framework

Figure 1: The classical and new multiresolution framework

This new multiresolution framework is applied in section 3 , where we will need to handle scaling functions with different regularities.

<u>- Black multiples of the solutions of</u>

This section deals with the multiresolution analysis of data defined on uniform grids. Since we want our algorithm tobe applied to very large data sets we keep on low degree scaling and wavelet functions Our starting point while developing BLAC wavelets was to look at the Haar and linear biorthogonal wavelets Sto ab Fin This last kind of wavelets have some regularity they are continuous which is not the case of the piecewise constant Haar wavelets But the regularity of the basis functions is a good point only if the data to be analyzed is also continuous. To illustrate this fact, figure 2 shows the result of one step of analysis on a 16 point data set, all but one equal to zero, by Haar and linear wavelets. We can see that the analysis by Haar wavelets yields only two non zero coe-cients while the analysis by linear wavelets gives more more non alle compression compression in the data follows from omitting all coesses which are near to zero the comparison of this is the linear wavelets yield bad compression to a ratio in the area where the data is discontinuous

The purpose of the BLAC wavelets is to find a compromise between the locality of the analysis (which is perfect for the Haar wavelets) and the regularity of the approximation (which is much better for the linear wavelets). Therefore BLAC stands for Blending of Linear And Constant. The graph on the right of figure 2 shows the result of one analysis step by a family of BLAC wavelets near from the Haar wavelets.

Figure 2: The test data set and comparison of Haar, linear and BLAC analysis

In section 3.1 we describe the BLAC scaling and wavelet functions. Section 3.2 gives some implementation remarks and compare the results of the Haar, BLAC and linear multiresolution analysis on some examples.

$-$ The BLAC scaling and wavelet functions and wavelet functions \mathbf{B}

BLAC scaling functions. The first step in defining a multiresolution analysis as introduced in section 2.2, is the choice of the scaling functions. Since we wanted to find a blending between Haar and linear wavelets, the following fundamental scaling function φ was chosen:

The scaling function φ_i is built from φ by dilation by a factor 2° , and translation of $(i \ 2^{\circ})$:

$$
\varphi_i^n(x) = \varphi\big(2^n(x+i\ 2^{-n})\big) -
$$

The fundamental function φ depends on the blending factor Δ : for $\Delta = 0$, (φ_i) are the usual Haar scaling functions, and for $\Delta = 1$ they are the linear scaling functions. Figure 4 shows the function φ for various values of Δ between 0 and 1.

Figure 4: The BLAC scaling functions

In order to have end-point interpolating scaling functions, we define the first and last scaling functions as follows

Figure 5: The first and last BLAC scaling functions

The approximation space v_n has the dimension $2^n + 1$, and is spanned by the scaling functions $\varphi_0^-, \dots, \varphi_{2^n}^-.$

Approximated refinement equations. The scaling functions of the level of resolution $n+1$ have a slope of $2^{n+1}/\Delta$. They are less regular than the scaling functions at one coarser level of resolution, since they "climb" to 1 more quickly.

The function φ_i is a so-called L-Lipschitz function with regularity $L = 2\gamma/\Delta$. As we pointed out in section 2.2, the fact that the scaling functions at different level of resolution have different regularity implies that no refinement equation can be found. Instead of that, an approximation $\tilde{\varphi}_i^n$ of the coarser i of the coarser i scaling function φ_i as linear combination of the finer scaling functions has to be chosen (see section 2.2, equation (10)). For Haar scaling functions, the exact refinement equation is $\varphi_i^*=\varphi_{2i-1}+\varphi_{2i}$, and in the linear case it is $\varphi_i^* = \frac{1}{2}\varphi_{2i-1}^* + \varphi_{2i}^*$ + $\frac{1}{2}\varphi_{2i+1}^*$. Since we want to blend between Haar and linear, we

choose φ_i^* to be a linear combination of $\varphi_{2i-1}^-, \varphi_{2i}^-,\varphi_{2i+1}^-$. And since we want the analysis scheme to preserve constant functions we search the following approximation of φ_i :

$$
\varphi_i^n \simeq \widetilde{\varphi}_i^n = \alpha \varphi_{2i-1}^{n+1} + \varphi_{2i}^{n+1} + (1-\alpha) \varphi_{2i+1}^{n+1}
$$
\n(12)

in the contract of the contra

included in the approximation space V^+ , as denned in 2.2, and thus that the analysis scheme will preserve them. The constant α is calculated to minimize the L_2 distance between φ_i^+ and φ_i^+ :

$$
\left\|\varphi_i^n - \widetilde{\varphi}_i^n\right\|_{L_2(\mathbf{R})} \longrightarrow \min
$$

The minimum is reached if α is the solution of the following linear equation:

$$
\langle \alpha \varphi_{2i-1}^{n+1} + \varphi_{2i}^{n+1} + (1-\alpha)\varphi_{2i+1}^{n+1} - \varphi_i^n, \varphi_{2i-1}^{n+1} - \varphi_{2i+1}^{n+1} \rangle = 0 \tag{13}
$$

(13) proves that α is independent of the level of resolution n. For $\Delta = 0$, the solution α is equal to 1. and the equation (12) reduces to the Haar refinement equation. For $\Delta = 1$, the solution is $\alpha = 1/2$, and (12) becomes the linear refinement equation. Figure 6 illustrates the approximated refinement equation (12) , and compares it to the refinement equation for the Haar and linear scaling functions.

The approximated refinement equations for the first and last scaling functions involve only two finer scaling functions

$$
\varphi_0^n \simeq \tilde{\varphi}_0^n = \varphi_0^{n+1} + (1 - \alpha)\varphi_1^{n+1}
$$

$$
\varphi_{2^n}^n \simeq \tilde{\varphi}_{2^n}^n = \alpha \varphi_{2^{n+1}-1}^{n+1} + \varphi_{2^{n+1}}^{n+1}
$$

BLAC wavelets. Once the scaling functions and the approximated refinement equation is fixed, the wavelet spaces W_n are also fixed by (11). The wavelet functions must be a base of this space. Obviously there is an infinite number of bases, and as in the Haar and linear case we choose the functions which have a minimal support. This goal is achieved if we impose ψ_i^{\pm} to be a linear combination of five successive scaling functions

$$
\psi_i^n = a \varphi_{2i-1}^{n+1} + b \varphi_{2i}^{n+1} + c \varphi_{2i+1}^{n+1} + d \varphi_{2i+2}^{n+1} + e \varphi_{2i+3}^{n+1}
$$

The coefficients a, b, c, a, e are computed by the fact that ψ_i^+ must be orthogonal to each function of the approximation space v_n . Since there are exactly four basis functions of this space whose support intersects the support of ψ_i^* , the orthogonality condition reduces to:

$$
<\psi_i^n, \tilde{\varphi}_j^n> = 0
$$
 with $j = i - 1, i, i + 1, i + 2$ (14)

(14) is a linear homogeneous system with four equations in the five unknowns a, b, c, d, e . It is uniquely solved if we impose the L_2 -norm of the wavelet to be equal to 1, as usual in multiresolution analysis:

$$
\int |\psi_i^n|^2 = 1
$$

note that the coefficients which who was and have detected of the recordition followed to the resolution one o BLAC wavelet for various values of Δ .

Figure 7: The BLAC wavelets \dagger

The first and last wavelet functions can be defined as the linear combination of only four finer scaling functions

$$
\psi_0^n = b_1 \varphi_0^{n+1} + c_1 \varphi_1^{n+1} + d_1 \varphi_2^{n+1} + e_1 \varphi_3^{n+1}
$$

$$
\psi_{2n-1}^n = a_2 \varphi_{2n+1-3}^{n+1} + b_2 \varphi_{2n+1-2}^{n+1} + c_2 \varphi_{2n+1-1}^{n+1} + d_2 \varphi_{2n+1}^{n+1}
$$

The coefficients $v_1, v_1, u_1, v_1, u_2, v_2, v_2, u_2$ are solution of the following homogeneous systems.

$$
\langle \psi_0^n, \tilde{\varphi}_j^n \rangle = 0, \qquad j = 0, 1, 2
$$

$$
\langle \psi_{2n-1}^n, \tilde{\varphi}_j^n \rangle = 0, \qquad j = 2^n - 2, 2^n - 1, 2^n
$$

These coe-cients are uniquely dened if we choose the rst and last wavelet functions to be normalized

$$
\int |\psi_0^n|^2 = 1
$$

$$
\int |\psi_{2^n}^n|^2 = 1
$$

^y An MPEG movie showing the BLAC wavelet going smoothly from Haar to linear is available via anonymous ftp at ftp.limsi.fr/pub/bonneau/wav.mpg

3.2 Implementation

The analysis and synthesis scheme (7) , (8) and (9) have to be carefully implemented since we want our algorithm to work in large data sets The results of section year to confident for the synthesis formula Normally the coe-cients for the analysis are computed from those of the synthesis by the inverse of a $(2^{n+1}+1) \times (2^{n+1}+1)$ matrix. But we will see that by using orthogonality properties, the computation of one analysis step can be reduced to the inversion of two smaller symmetric positive definite banded matrices.

Given the approximation f_{n+1} of f at the resolution level $n+1$:

$$
f_{n+1} = \sum_{i=0}^{2^{n+1}} x_i^{n+1} \varphi_i^{n+1},
$$

the problem is to find the coarser approximation $f_n = \sum_{i=0}^{2^n} x_i^n \tilde{\varphi}_i^n$ and the detail $g_n = \sum_{i=0}^{2^n-1} y_i^n \psi_i^n$. Since g_n is the error between f_{n+1} and f_n , the following equation needs to be verified

$$
\sum_{i=0}^{2^{n+1}} x_i^{n+1} \varphi_i^{n+1} = \sum_{i=0}^{2^n} x_i^n \tilde{\varphi}_i^n + \sum_{j=0}^{2^n - 1} y_j^n \psi_j^n \tag{15}
$$

To find the smooth coefficients (x_i) , we proceed by taking the scalar product of φ_k^* with both sides of (15). Since the wavelets (ψ_j) are orthogonal to the scaling function φ_k , we get

$$
\langle \sum_{i=0}^{2^{n+1}} x_i^{n+1} \varphi_i^{n+1}, \widetilde{\varphi}_k^n \rangle = \sum_{i=0}^{2^n} x_i^n \langle \widetilde{\varphi}_i^n, \widetilde{\varphi}_k^n \rangle \tag{16}
$$

Thus we see that the smooth coefficients (x_i) are the solution of a linear system whose matrix has the elements $\langle \varphi_i^*, \varphi_k^* \rangle$ and is known as Gram-Schmidt matrix. This matrix has very good properties: it is symmetric positive denite and it is banded We can therefore use the Cholesky algorithm toinverse the system (16). This algorithm is numerically stable for high dimension matrices. This is crucial for the analysis of large data sets. Moreover, the Cholesky algorithm preserves the band structure of the matrix, so that the cost of the inversion of (16) is only of $O(d)$, where d is the size of the data set. b find the coarser approximation $\widetilde{f}_n = \sum_{i=0}^{2^n} x_i^n \widetilde{\varphi}_i^n$ and the detail

Tror between f_{n+1} and \widetilde{f}_n , the following equation needs to be verific
 $\sum_{i=0}^{2^{n+1}} x_i^{n+1} \varphi_i^{n+1} = \sum_{i=0}^{2^n} x_i^n \widetilde{\varphi}_$

Analogously, the detail coefficients (y_j^*) are the solution of the following linear system:

$$
<\sum_{i=0}^{2^n} x_i^{n+1} \varphi_i^{n+1}, \psi_k^n>=\sum_{j=0}^{2^n-1} y_j^n <\psi_j^n, \psi_k^n>.
$$

This system can also be solved by a Cholesky algorithm for band matrices Thus the cost of the compu tation of one analysis step is simply a $O(d)$, where d is the size of the data set.

The scalar products of the scaling functions from which the elements of the matrices can be computed are given in the appendix

Examples

The examples of gure shows at the top the result of the compression of the lena image by a factor of 96% with a BLAC multiresolution analysis for three different values of Δ . On the top left we used \blacksquare was used analysis in the middle \blacksquare was used and to the top right \blacksquare . If υ is the top analysis) was employed. As a consequence of the regularity of the linear wavelets, fuzzy areas appear where the image has sudden discontinuities (see f.ex. along the upper border of the hat). This is what we could expect from the introduction of section 3: too much regularity implies bad compression ratio where the data is discontinuous These fund are to form the form for \blacksquare . And with the form if disappear with $\Delta = 0$. On the other hand, the three images at the bottom, which are the results of an edge detection

algorithm applied to the top images, clearly show that the approximation becomes smoother while Δ increases. For $\Delta = 0$, the contours even follow the support of the wavelet functions with the biggest

Figure 8: Lena^{\ddagger}

To conclude this article we see that BLAC multiresolution analysis enables the user to choose his own compromise between regularity of the basis functions and locality of the analysis or what is equivalent between the smoothness of the approximation, and its sharpness.

References

- 1. G.P. Bonneau; S. Hahmann; G.M. Nielson. BLAC-wavelets: a multiresolution analysis with non-nested spaces, submitted to EUROGRAPHIC'96, january 1996
- 2. A. Cohen; I. Daubechies; J. Feauveau. Bi-orthogonal bases of compactly supported wavelets, Comment Comment Pure Apple Application (Section)
- 3. A. Cohen. Ondelettes et Traitement Numérique du Signal, Eds Masson, Paris (1992).
- 4. M. Eck; T. DeRose, et al. Multiresolution Analysis of Arbitrary Meshes, Proceedings of SIG-GRAPH'95. In Computer Graphics, Annual conference Series, (1995)
- a fine computer and the multiple multiple multiple of the sign of SIGGRAPH α of the Graphics α Annual conference Series
- 6. S. Mallat. A Theory for Multiresolution Signal Decomposition: The Wavelet Representation, IEEE Trans Pattern Anal and Machine Intel
- 7. E. Stollnitz; T. DeRose; D. Salesin. Wavelets for Computer Graphics: A Primer, Part 1, IEEE Computer Graphics Applications
- 8. E. Stollnitz; T. DeRose; D. Salesin. Wavelets for Computer Graphics: A Primer, Part 2, IEEE Computer Graphics Applications

^{*} Available via anonymous ftp at ftp.ilmsi.fr/pub/bonneau/lena fig.rgb in sgi-format.