

Impedance Transmission Conditions for the Electric Potential across a Highly Conductive Casing

Hélène Barucq, Aralar Erdozain, David Pardo, Victor Péron

▶ To cite this version:

Hélène Barucq, Aralar Erdozain, David Pardo, Victor Péron. Impedance Transmission Conditions for the Electric Potential across a Highly Conductive Casing. V-MAD6 - Valparaíso's Mathematics and its Applications Days, Jan 2016, Valparáso, Chile. hal-01692286

HAL Id: hal-01692286 https://inria.hal.science/hal-01692286

Submitted on 24 Jan 2018

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

Perspectives

Impedance Transmission Conditions for the Electric Potential across a Highly Conductive Casing

Aralar Erdozain¹, Victor Péron^{1,2}, Hélène Barucq^{1,2} and David Pardo^{3,4,5}



¹INRIA Bordeaux Sud-Ouest, Team magique 3D

²Université de Pau et des Pays de l'Adour

³University of the Basque Country (UPV/EHU), Leioa, Spain

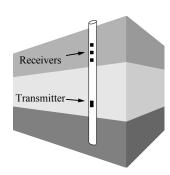
⁴Basque Center for Applied Mathematics (BCAM), Bilbao, Spain

⁵Ikerbasque (Basque Foundation for Sciences), Bilbao, Spain

MOTIVATION

- Main goal: To obtain a better characterization of the Earth's subsurface
- How: Recording borehole resistivity measurements

- Procedure:
 - Well
 - Transmitters
 - Receivers



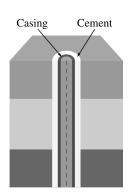
MOTIVATION

Practical Difficulties:

- It is not easy to drill a borehole
- It may collapse

• Practical Solutions:

- Use a metallic casing
- Surround with a cement layer
- Problem solved, but...



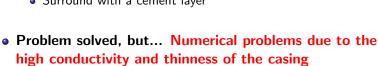
MOTIVATION

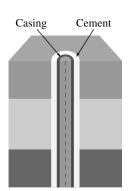
• Practical Difficulties:

- It is not easy to drill a borehole
- It may collapse

• Practical Solutions:

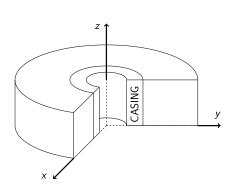
- Use a metallic casing
- Surround with a cement layer



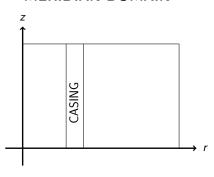


CONFIGURATION OF INTEREST

SECTIONED 3D DOMAIN



MERIDIAN DOMAIN

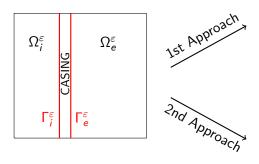


We reduce the 3D problem to a 2D problem due to the axysimmetric configuration.

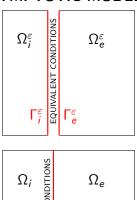
MAIN IDEA

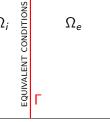
ASYMPTOTIC MODELS

REFERENCE MODEL

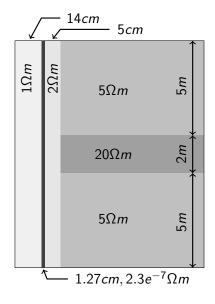


Idea: Replace the casing by equivalent conditions.





REALISTIC SCENARIO



Conductivity and casing width:

$$\begin{cases} \varepsilon = 1.27e - 2m \\ \sigma_c = 4.34e6 \ \Omega^{-1}m^{-1} \end{cases}$$

$$\Rightarrow \sigma_c \approx \varepsilon^{-3}$$

Classical approach:

$$\sigma_{c} = \alpha \qquad \quad \alpha \in \mathbb{R}$$

High conductive case:

$$\sigma_c = \alpha \varepsilon^{-3}$$
 $\alpha \in \mathbb{R}$

Perspectives

REFERENCES

- [1] A.A. Kaufman. The electrical field in a borehole with a casing. *Geophysics*, Vol.55, Issue 1, pp. 29-38, 1990.
- [2] D.Pardo, C.Torres-Verdín and Z.Zhang. Sensitivity study of borehole-to-surface and crosswell electromagnetic measurements acquired with energized steel casing to water displacement in hydrocarbon-bearing layers. *Geophysics*, 73 No.6, F261-F268, 2008.
- [3] M. Duruflé, V. Péron and C. Poignard. Thin Layer Models for Electromagnetism. *Communications in Computational Physics* 16(1):213-238, 2014.
- [4] K. Schmidt, A. Chernov, Robust transmission conditions of high order for thin conducting sheets in two dimensions, *IEEE Trans. Magn.*, 50 (2014), pp. 41–44.

OUTLINE

- Equivalent Conditions
- 2 Numerical Results
- 3 Second Approach
- 4 Application
- 6 Perspectives

OUTLINE

- Equivalent Conditions
- 2 Numerical Results
- Second Approach
- 4 Application
- 6 Perspectives

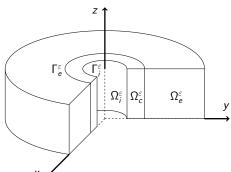
MODEL PROBLEM - 3D

Introduction

STATIC ELECTRIC POTENTIAL

$$\operatorname{div}\left(\left(\sigma-i\epsilon\omega\right)\nabla u\right)=f\ \text{in}\ \Omega$$

$$\Omega = \Omega_i^\varepsilon \cup \Omega_c^\varepsilon \cup \Omega_e^\varepsilon \cup \Gamma_i^\varepsilon \cup \Gamma_e^\varepsilon$$



Where f is a known data, σ is piecewise constant

$$\sigma = \begin{cases} \sigma_i & \text{in } \Omega_i^{\varepsilon} \\ \sigma_c = \alpha \varepsilon^{-3} & \text{in } \Omega_c^{\varepsilon} \\ \sigma_e & \text{in } \Omega_e^{\varepsilon} \end{cases}$$

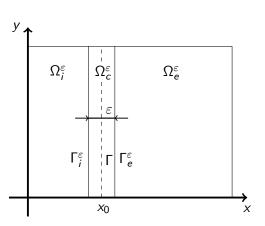
and the solution is expressed as

$$u = \begin{cases} u_i & \text{in } \Omega_i^{\varepsilon} \\ u_c & \text{in } \Omega_c^{\varepsilon} \\ u_e & \text{in } \Omega_e^{\varepsilon} \end{cases}$$

MODEL PROBLEM - 2D

Introduction

Reference problem (P) set in the domain $\Omega = \Omega_i^\varepsilon \cup \Omega_c^\varepsilon \cup \Omega_e^\varepsilon \cup \Gamma_i^\varepsilon \cup \Gamma_e^\varepsilon$. We denote the boundary $\Gamma_0 := (\overline{\partial \Omega_i^\varepsilon - \Gamma_i^\varepsilon}) \cup (\overline{\partial \Omega_e^\varepsilon - \Gamma_e^\varepsilon})$.



$$\begin{cases} \sigma_i \Delta u_i &= f_i & \text{in} \quad \Omega_i^{\varepsilon} \\ \sigma_c \Delta u_c &= 0 & \text{in} \quad \Omega_c^{\varepsilon} \\ \sigma_e \Delta u_e &= f_e & \text{in} \quad \Omega_e^{\varepsilon} \\ u_i &= u_c & \text{on} \quad \Gamma_i^{\varepsilon} \\ u_c &= u_e & \text{on} \quad \Gamma_e^{\varepsilon} \\ \sigma_i \partial_n u_i &= \sigma_c \partial_n u_c & \text{on} \quad \Gamma_e^{\varepsilon} \\ \sigma_c \partial_n u_c &= \sigma_e \partial_n u_e & \text{on} \quad \Gamma_e^{\varepsilon} \\ u &= 0 & \text{on} \quad \partial \Omega \end{cases}$$

Perspectives

EXISTENCE AND UNIQUENESS

Theorem 1

Introduction

There exists $\varepsilon_0 > 0$ s.t. for all $\varepsilon \in (0, \varepsilon_0)$, if $f_i \in L^2(\Omega_i^{\varepsilon})$ and $f_e \in L^2(\Omega_e^{\varepsilon})$, then $\exists ! u \in H_0^1(\Omega)$ solution of (P) and

$$||u||_{1,\Omega} \leq C \left(||f_i||_{0,\Omega_i^{\varepsilon}} + ||f_e||_{0,\Omega_e^{\varepsilon}}\right).$$

Proof:

- Derive variational formulation, for all $v \in H_0^1(\Omega)$, a(u, v) = b(v).
- Prove that a coercive and continuous, b continuous in $H_0^1(\Omega)$.
- Apply the Lax-Milgram Lema.

Definition 1

We define the jump and mean value of the solution u across the casing as

$$[u] = u|_{\mathsf{\Gamma}^{\varepsilon}_{e}} - u|_{\mathsf{\Gamma}^{\varepsilon}_{i}}$$

$$\{u\} = \frac{1}{2} \left(u|_{\Gamma_e^{\varepsilon}} + u|_{\Gamma_i^{\varepsilon}} \right)$$

Definition2

Let u be the reference solution. We say an asymptotic model is of Order k+1, if its solution $u^{[k]}$ satisfies

$$||u-u^{[k]}||_{H^1} < C\varepsilon^{k+1}$$
 when $\varepsilon \to 0$

Perspectives

METHODOLOGY

Introduction

• **Step1:** Derive an Asymptotic Expansion for u when $\varepsilon \longrightarrow 0$

• In the casing:
$$u_c(x,y) = \sum_{n \in \mathbb{N}} \varepsilon^n U^n \left(\frac{x - x_0}{\varepsilon}, y \right)$$

- Outside the casing: $u(x,y) = \sum_{n \in \mathbb{N}} \varepsilon^n u^n(x,y)$
- Step2: Obtain Equivalent Conditions of order k+1 by identifying a simpler problem satisfied by the truncated expansion and neglecting the higher order terms in ε

•
$$u_{k,\varepsilon} := u^0 + \varepsilon u^1 + \varepsilon^2 u^2 + \ldots + \varepsilon^k u^k$$

• Step3: Prove Convergence rates for asymptotic models

MULTISCALE EXPANSION

$$\begin{cases} \partial_X^2 U^k + \partial_y^2 U^{k-2} = 0 & \text{in } \Omega_c^{\varepsilon} \\ \sigma_i \Delta u_i^k = f_i & \text{in } \Omega_i^{\varepsilon} \\ \sigma_e \Delta u_e^k = f_e & \text{in } \Omega_e^{\varepsilon} \\ u_i^k = U^k & \text{on } \Gamma_i^{\varepsilon} \\ U^k = u_e^k & \text{on } \Gamma_i^{\varepsilon} \\ \sigma_i \partial_X u_i^{k-4} = \alpha \partial_X U^k & \text{on } \Gamma_i^{\varepsilon} \\ \alpha \partial_X U^k = \sigma_e \partial_X u_e^{k-4} & \text{on } \Gamma_e^{\varepsilon} \\ U^k = 0 & \text{on } \partial\Omega \end{cases}$$

$$\begin{cases} \partial_X^2 U^k + \partial_y^2 U^{k-2} = 0 & \text{in } \Omega_c^{\varepsilon} \\ \sigma_i \Delta u_i^k = f_i & \text{in } \Omega_i^{\varepsilon} \\ \sigma_e \Delta u_e^k = f_e & \text{in } \Omega_e^{\varepsilon} \\ u_i^k = U^k & \text{on } \Gamma_i^{\varepsilon} \\ u_i^k = u_e^k & \text{on } \Gamma_i^{\varepsilon} \\ \sigma_i \partial_x u_i^{k-4} = \alpha \partial_X U^k & \text{on } \Gamma_i^{\varepsilon} \\ \alpha \partial_X U^k = \sigma_e \partial_x u_e^{k-4} & \text{on } \Gamma_e^{\varepsilon} \\ U^k = 0 & \text{on } \partial\Omega \end{cases}$$

$\partial_X^2 U^k + \partial_y^2 U^{k-2} = 0$ Ω_c^{ε} in **PROCEDURE** $\sigma_i \Delta u_i^k = f_i$ in Ω_i^{ε} $\sigma_e \Delta u_e^k = f_e$ Ω_e^{ε} in $u_i^k = U^k$ on $U^k = u_a^k$ $\Gamma_{\mathbf{c}}^{\varepsilon}$ on $\sigma_i \partial_{\mathsf{x}} u_i^{k-4} = \alpha \partial_{\mathsf{x}} U^k$ on Γ_i^{ε} $\alpha \partial_X U^k = \sigma_e \partial_X u_e^{k-4}$ on $U^k = 0$ $\partial\Omega$ on

MULTISCALE EXPANSION

$$\begin{cases} \partial_X^2 U^k + \partial_y^2 U^{k-2} = 0 & \text{in } \Omega_c^{\varepsilon} \\ \sigma_i \Delta u_i^k = f_i & \text{in } \Omega_i^{\varepsilon} \\ \sigma_e \Delta u_e^k = f_e & \text{in } \Omega_e^{\varepsilon} \\ u_i^k = U^k & \text{on } \Gamma_i^{\varepsilon} \\ U^k = u_e^k & \text{on } \Gamma_e^{\varepsilon} \\ \sigma_i \partial_x u_i^{k-4} = \alpha \partial_X U^k & \text{on } \Gamma_e^{\varepsilon} \\ \alpha \partial_X U^k = \sigma_e \partial_x u_e^{k-4} & \text{on } \Gamma_e^{\varepsilon} \\ U^k = 0 & \text{on } \partial\Omega \end{cases}$$

$$\begin{cases} \partial_X^2 U^k + \partial_y^2 U^{k-2} = 0 & \text{in } \Omega_c^{\varepsilon} \\ \sigma_i \Delta u_i^k = f_i & \text{in } \Omega_i^{\varepsilon} \\ \sigma_e \Delta u_e^k = f_e & \text{in } \Omega_e^{\varepsilon} \\ u_i^k = U^k & \text{on } \Gamma_i^{\varepsilon} \\ U^k = u_e^k & \text{on } \Gamma_i^{\varepsilon} \\ \sigma_i \partial_x u_i^{k-4} = \alpha \partial_X U^k & \text{on } \Gamma_i^{\varepsilon} \\ \partial_x U^k = \sigma_e \partial_x u_e^{k-4} & \text{on } \Gamma_e^{\varepsilon} \\ U^k = 0 & \text{on } \partial\Omega \end{cases}$$

EQUIVALENT MODELS

FIRST APPROACH

(Transmission conditions across the casing)

Order 2:

Introduction

$$\begin{cases} \sigma_i \Delta u_i = f_i & \text{in } \Omega_i^{\varepsilon} \\ u_i = 0 & \text{on } \partial \Omega_i^{\varepsilon} \end{cases}$$

$$\begin{cases} \sigma_e \Delta u_e = f_e & \text{in } \Omega_e^{\varepsilon} \\ u_e = 0 & \text{on } \partial \Omega_e^{\varepsilon} \end{cases}$$

$$(P_2)$$

Order 4:

$$\begin{cases} \sigma_{i}\Delta u_{i} = f_{i} & \text{in } \Omega_{i}^{\varepsilon} \\ \sigma_{e}\Delta u_{e} = f_{e} & \text{in } \Omega_{e}^{\varepsilon} \\ [u] = 0 & \\ [\sigma\partial_{n}u] = -\frac{\alpha}{\varepsilon^{2}}\Delta_{\Gamma^{\varepsilon}}\left\{u\right\} \\ u = 0 & \text{on } \Gamma_{0} \end{cases}$$

$$(P_{4})$$

Theorem 2

Introduction

There exists $\varepsilon_0 > 0$ s.t. for all $\varepsilon \in (0, \varepsilon_0)$, if $f_i \in L^2(\Omega_i^{\varepsilon})$ and $f_e \in L^2(\Omega_e^{\varepsilon})$, then $\exists ! u^{[k]} \in V_{k+1}$ solution of P_{k+1} , k = 1, 3, and

$$\|u^{[k]}\|_{1,\Omega_i^{\varepsilon}\cup\Omega_e^{\varepsilon}}\leq C\left(\|f_i\|_{0,\Omega_i^{\varepsilon}}+\|f_e\|_{0,\Omega_e^{\varepsilon}}\right)$$

$$||u - u^{[k]}||_{1,\Omega^{\varepsilon} \cup \Omega^{\varepsilon}} \le C\varepsilon^{k+1}$$

Where

$$V_2 = \{ v : v_i \in H_0^1(\Omega_i^{\varepsilon}), v_e \in H_0^1(\Omega_e^{\varepsilon}) \}$$

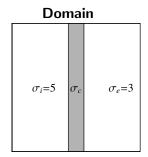
$$V_{4} = \left\{ v : v_{i} \in H^{1}\left(\Omega_{i}^{\varepsilon}\right), v_{e} \in H^{1}\left(\Omega_{e}^{\varepsilon}\right), \nabla_{\Gamma^{\varepsilon}}\left\{v\right\} \in L^{2}\left(\Gamma^{\varepsilon}\right), v|_{\Gamma^{\varepsilon}_{\tau}} = v|_{\Gamma^{\varepsilon}_{\tau}}, v|_{\Gamma_{0}} = 0 \right\}$$

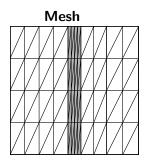
OUTLINE

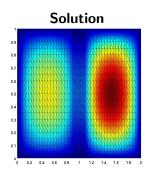
- Equivalent Conditions
- 2 Numerical Results
- Second Approach
- 4 Application
- 6 Perspectives

FEM CODE

- Classic Finite Element Method code
- Straight triangular elements (h refinement)
- Lagrange shape functions of any degree (p refinement)

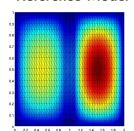


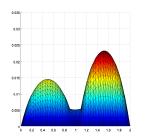




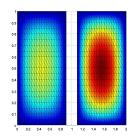
QUALITATIVE COMPARISON

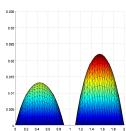
Reference Model



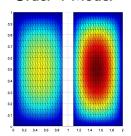


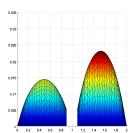
Order 2 Model



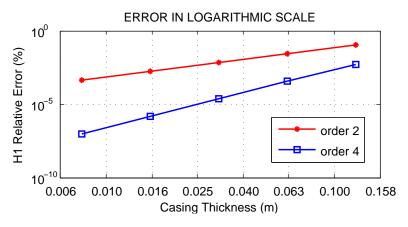


Order 4 Model





CONVERGENCE RATES



| Casing Thickness (ε) | 0.0117 | 0.0234 | 0.0469 | 0.0938 | Expected $(\varepsilon 	o 0)$ |
|----------------------------------|--------|--------|--------|--------|-------------------------------|
| Order 2 Slopes | 1.9969 | 1.9899 | 1.9638 | 1.8624 | 2 |
| Order 4 Slopes | 4.0046 | 4.0039 | 3.9879 | 3.8992 | 4 |

OUTLINE

- Equivalent Conditions
- 2 Numerical Results
- 3 Second Approach
- 4 Application
- Perspectives

SECOND APPROACH

(Transmission conditions across the interface Γ)

Order 1:

Introduction

$$\begin{cases} \sigma_i \Delta u_i = f_i & \text{in } \Omega_i \\ u_i = 0 & \text{on } \partial \Omega_i \end{cases}$$

$$\begin{cases} \sigma_e \Delta u_e = f_e & \text{in } \Omega_e \\ u_e = 0 & \text{on } \partial \Omega_e \end{cases}$$

$$(P_1)$$

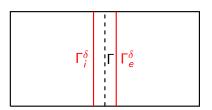
Order 2:

$$\begin{cases} \sigma_i \Delta u_i = f_i & \text{in } \Omega_i \\ \sigma_e \Delta u_e = f_e & \text{in } \Omega_e \\ [u] = -\varepsilon \left\{ \partial_n u \right\} \\ [\partial_n u] = -\frac{4}{\varepsilon} \left\{ u \right\} \\ u = 0 & \text{on } \partial \Omega \end{cases}$$

Stability

Problem

Stability problems for the order 2 model of the second approach due to a non coercive term.



Solution

Use of Artificial Boundaries to move the transmission conditions and recover stability. For $\delta>0.5$

$$\Gamma_i^{\delta} = \{(x, y) : x = x_0 - \delta \varepsilon, y \in (0, y_0)\}$$

$$\Gamma_{\epsilon}^{\delta} = \{(x, y) : x = x_0 + \delta \varepsilon, y \in (0, y_0)\}$$

EQUIVALENT MODELS

SECOND APPROACH

(Transmission conditions across the artificial interfaces)

• Order 2:
$$\begin{cases} \sigma_i \Delta u_i = f_i & \text{in } \Omega_i \\ \sigma_e \Delta u_e = f_e & \text{in } \Omega_e \end{cases}$$
$$[u] = -\varepsilon (1 - 2\delta) \{\partial_n u\} \qquad (P_2)$$
$$[\partial_n u] = -\frac{4(1 - 2\delta)}{\varepsilon} \{u\}$$
$$u = 0 \qquad \text{on } \partial\Omega$$

Stable if $\delta > 0.5$

CONVERGENCE

Theorem 3

Introduction

There exists $\varepsilon_0 > 0$ s.t. for all $\varepsilon \in (0, \varepsilon_0)$, if $f_i \in L^2(\Omega_i^{\varepsilon})$ and $f_e \in L^2(\Omega_e^{\varepsilon})$, then $\exists ! u^{[k]} \in V_{k+1}$ solution of P_{k+1} , k=1,2, and

$$\|u^{[k]}\|_{1,\Omega_i^\varepsilon \cup \Omega_e^\varepsilon} \le C \left(\|f_i\|_{0,\Omega_i^\varepsilon} + \|f_e\|_{0,\Omega_e^\varepsilon}\right)$$

$$||u - u^{[k]}||_{1,\Omega^{\varepsilon} \cup \Omega^{\varepsilon}} \le C\varepsilon^{k+1}$$

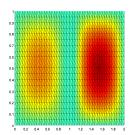
Where

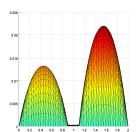
$$V_{1} = \left\{ v : v_{i} \in H_{0}^{1}\left(\Omega_{i}\right), v_{e} \in H_{0}^{1}\left(\Omega_{e}\right) \right\}$$

$$V_{2} = \{ v : v_{i} \in H^{1}(\Omega_{i}), v_{e} \in H^{1}(\Omega_{e}), v_{i}|_{\Gamma} = v_{e}|_{\Gamma}, v|_{\Gamma_{0}} = 0 \}$$

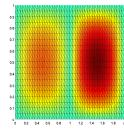
QUALITATIVE COMPARISON

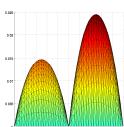
Reference Model



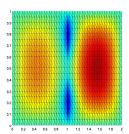


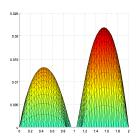
Order 1 Model



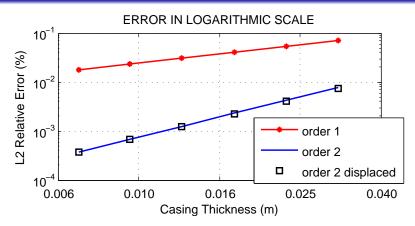


Order 2 Model



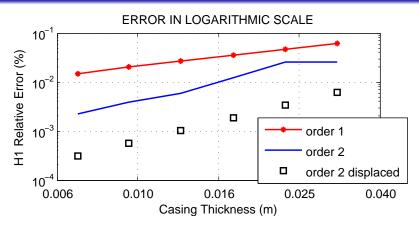


CONVERGENCE RATES L²



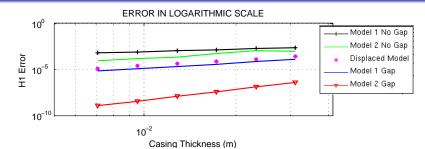
| Casing Thickness (ε) | 0.008 | 0.011 | 0.015 | 0.020 | 0.027 | Expected $(arepsilon 	o 0)$ |
|----------------------------------|-------|-------|-------|-------|--------|-----------------------------|
| Order 1 Slopes | 0.972 | 0.962 | 0.948 | 0.928 | 0.899 | 1 |
| Order 2 Slopes | 2.032 | 2.011 | 2.062 | 2.090 | 1.9636 | 2 |
| Order 2 displaced | 2.005 | 2.006 | 2.007 | 2.008 | 2.007 | 2 |

CONVERGENCE RATES H^1



| Casing Thickness (ε) | 0.008 | 0.011 | 0.015 | 0.020 | 0.027 | Expected $(\varepsilon 	o 0)$ |
|----------------------------------|-------|-------|-------|-------|--------|-------------------------------|
| Order 1 Slopes | 0.982 | 0.975 | 0.966 | 0.953 | 0.935 | 1 |
| Order 2 Slopes | 1.915 | 1.302 | 2.463 | 2.569 | -0.125 | 2 |
| Order 2 displaced | 2.004 | 2.005 | 2.006 | 2.008 | 2.007 | 2 |

COMPARISON



Order Stability ε -independent Domain Model 1 No Gap 1 × 2 Model 2 No Gap X 2 Displaced Model X 2 Model 1 Gap X Model 2 Gap 4

OUTLINE

- Equivalent Conditions
- 2 Numerical Results
- Second Approach
- 4 Application
- 5 Perspectives

Perspectives

APPLICATION

Introduction

$$\sqrt{-1.27}$$
 cm, $2.3e^{-7}\Omega$ m

- $z = z_3$ $z = z_2$ Receivers $z = z_1$ $z = z_0$ Transmitter

- Equation: $\operatorname{div}(\sigma \nabla u) = f$
- Right hand side:

$$f = egin{cases} 1 & ext{In the transmitter} \ 0 & ext{Outside the transmitter} \end{cases}$$

 Objective: Measure the second difference of potential on the Receivers

$$U_2 = u(z_1) - 2u(z_2) + u(z_3)$$

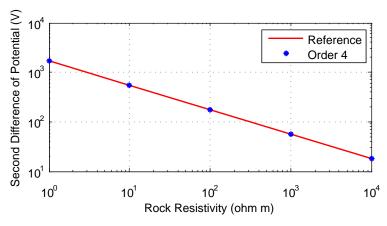
Expected Result: (Model of Kaufman) Relation between second difference of potential and rock resistivity of the form

$$U_2 = k \cdot \rho_{\text{rock}}^{-\frac{1}{2}} \quad k \in \mathbb{R}$$

Equivalent Conditions

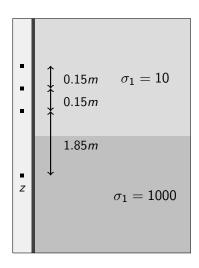
Introduction

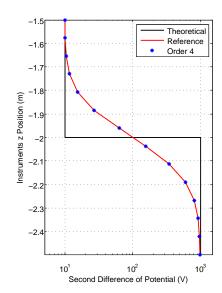
VARYING ROCK CONDUCTIVITY



| Resistivity | [1,10] | $[10,10^2]$ | $[10^2, 10^3]$ | $[10^3, 10^4]$ | Expected |
|------------------------|---------|-------------|----------------|----------------|----------|
| Reference Model Slopes | -0.4914 | -0.4924 | -0.4978 | -0.4991 | -0.5 |
| Order 4 Slopes | -0.4914 | -0.4924 | -0.4977 | -0.4993 | -0.5 |

TWO ROCK LAYERS





OUTLINE

- Equivalent Conditions
- 2 Numerical Results
- Second Approach
- 4 Application
- 6 Perspectives

Perspectives

- Obtain semianalytical solutions to reduce the computational cost.
- Consider physically more realistic scenarios.
- Develop 3D electromagnetic models.
- Study highly deviated boreholes.

Perspectives

- Obtain semianalytical solutions to reduce the computational cost.
- Consider physically more realistic scenarios.
- Develop 3D electromagnetic models.
- Study highly deviated boreholes.

THANK YOU FOR YOUR ATTENTION